click icon to display or hide navigation panel
click on section icon in navigation panel to display section


## Contents Pages

click on chapter number
to display chapter to display chapter
click on section title to display section click on exhibit number to display exhibit

Cover Pages
click on chapter number to return to the table of contents

click on arrow to jump to the next page of text

Chapter 1 summarizes eighth-grade achievement on the
TIMSS 1999 mathematics assessment for each of the
participating countries, and shows trends in student
performance for those countries that also participated in
TIMSS 1995 at the eighth grade. Comparisons of country
performance against international benchmarks, as well as
gender differences in performance, also are provided.
Text Pages
click on section title
to return to table
of contents

## Exhibit Pages

click on exhibit number to jump to text discussion of that exhibit


## TIMSS 1999

## International Mathematics Report

Findings from IEA's Repeat of the Third International Mathematics and Science Study at the Eighth Grade


| The International Study Center <br> Boston College <br> Lynch School of Education | The International Association <br> for the Evaluation of <br> Educational Achievement | December 2000 |
| :--- | :--- | :--- |

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1

## 27 CHAPTER 1

International Student Achievement in Mathematics

29 How Do Countries Differ in Mathematics Achievement?
32 Exhibit 1.1
Distribution of Mathematics Achievement
33 Exhibit 1.2
Multiple Comparisons of Average Mathematics Achievement

34 How Has Mathematics Achievement Changed Since 1995?
36 Exhibit 1.3
Trends in Mathematics Achievement
37 Exhibit 1.4
Mathematics Achievement for TIMSS 1999 Countries That Participated in 1995 at Both the Fourth and Eighth Grades in Relation to the Average Across These Countries

38 How Do Countries Compare with International Benchmarks of Mathematics Achievement?
42 Exhibit 1.5
TIMSS 1999 International Benchmarks of Mathematics Achievement
43 Exhibit 1.6
Percentages of Students Reaching TIMSS 1999 International Benchmarks of Mathematics Achievement
44 Exhibit 1.7
Trends in Percentages of Students Reaching the TIMSS 1999 Top 10\% International Benchmark of Mathematics Achievement
45 Exhibit 1.8
Trends in Percentages of Students Reaching the TIMSS 1999 Upper Quarter International Benchmark of Mathematics Achievement
46 Exhibit 1.9
Trends in Percentages of Students Reaching the TIMSS 1999 Median International Benchmark of Mathematics Achievement
47 Exhibit 1.10
Trends in Percentages of Students Reaching the TIMSS 1999 Lower Quarter International Benchmark of Mathematics Achievement

48 What Are the Gender Differences in Mathematics Achievement?
50 Exhibit 1.11
Average Mathematics Achievement by Gender
51 Exhibit 1.12
Percentages of Girls and Boys Reaching Each Country's Own Upper Quarter and Median Levels of Mathematics Achievement
52 Exhibit 1.13
Trends in Average Mathematics Achievement by Gender
53 Exhibit 1.14
Trends in Gender Differences in Average Mathematics Achievement

## 55 CHAPTER 2

Performance at International Benchmarks

57 How Were the Benchmark Descriptions Developed?

58 How Should the Descriptions be Interpreted

59 Item Examples and Student Performance

60 Achievement at the Top 10\% Benchmark

61 Exhibit 2.1
Description of Top 10\% TIMSS International Benchmark of Mathematics Achievement
64 Exhibit 2.2-2.5
Top 10\% TIMSS International Benchmark Example Items

68 Achievement at the Upper Quarter Benchmark

69 Exhibit 2.6
Description of Upper Quarter TIMSS International Benchmark of Mathematics Achievement
72 Exhibit 2.7-2.11
Upper Quarter TIMSS International Benchmark Example Items

78 Achievement at the Median Benchmark

79 Exhibit 2.12
Description of Median TIMSS International Benchmark of Mathematics Achievement
80 Exhibit 2.13-2.15
Median TIMSS International Benchmark Example Items

84 Achievement at the Lower Quarter Benchmark

85 Exhibit 2.16
Description of Lower Quarter TIMSS International Benchmark of Mathematics Achievement
86 Exhibit 2.17-2.20
Lower Quarter TIMSS International Benchmark Example Items

90 What Issues Emerge from the Benchmark Descriptions?

## 91 CHAPTER 3

Average Achievement in the Mathematics Content Areas

94 How Does Achievement Differ Across Mathematics Content Areas?

96
Average Achievement in Mathematics Content Areas
99 In Which Content Areas Are Countries Relatively Strong or Weak?
102 Exhibit 3.2
Profiles of Relative Performance in Mathematics
Content Areas
104 What Are the Gender Differences in Achievement for the Content Areas? by Gender

108 What Changes Have Occurred in Content Area Achievement?
110 Exhibit 3.4
Trends in Average Percent Correct in Mathematics Content Areas

## 113 CHAPTER 4

Students' Backgrounds and Attitudes Towards Mathematics

115 What Educational Resources Do
Students Have in Their Homes?
118 Exhibit 4.1
Index of Home Educational Resources (HER)
122 Exhibit 4.2
Frequency with Which Students Speak Language of the Test at Home
123 Exhibit 4.3
Trends in Frequency with Which Students Speak Language of the Test at Home
124 Exhibit 4.4
Students' Expectations for Finishing School
125 How Much of Their Out-of-School Time Do Students Spend on Homework During the School Week?
128 Exhibit 4.5
Index of Out-of-School Study Time (OST)
130 Exhibit 4.6
Trends in Index of Out-of-School Study Time (OST)
131 Exhibit 4.7
Total Amount of Out-of-School Time Students Spend Studying Mathematics or Doing Mathematics Homework on a Normal School Day

132 How Do Students Perceive Their Ability in Mathematics?

134 Exhibit 4.8
Index of Students' Self-Concept in Mathematics (SCM)
136 Exhibit 4.9
Index of Students' Self-Concept in Mathematics (SCM)
by Gender
137 What Are Students' Attitudes Towards Mathematics?

140 Exhibit 4.10
Index of Students' Positive Attitudes Towards Mathematics (PATM)
142 Exhibit 4.11
Index of Positive Attitudes Towards Mathematics (PATM) by Gender
143 Exhibit 4.12
Trends in Index of Positive Attitudes Towards Mathematics (PATM)
144 Exhibit 4.13
Trends in Gender Differences in Percentages of Students at High Level of Index of Positive Attitudes Towards Mathematics (PATM)

## 145 CHAPTER 5

The Mathematics Curriculum

148 Does Decision Making About the Intended Curriculum Take Place at the National or Local Level?
149 Exhibit 5.1
Mathematics Curriculum
150 How Do Countries Support and Monitor Curriculum Implementation?

151 Exhibit 5.2
Methods Used to Support or Monitor Curriculum Implementation

152 What Countries Have Public Examinations in Mathematics?

153 Exhibit 5.3
Public Examinations in Mathematics
154 What Countries Have System-Wide Assessment in Mathematics?

155 Exhibit 5.4
System-Wide Assessments in Mathematics
156 How Much Instructional Time Is Recommended for Mathematics?
158 Exhibit 5.5
Instructional Time for Mathematics
160 How Do Countries Deal with Individual Differences?
161 Exhibit 5.6
Differentiation of Instruction for Students with Different Abilities or Interests

162 What Are the Major Characteristics of the Intended Curriculum?

163 Exhibit 5.7
Emphasis on Approaches and Processes
164 What Mathematics Content Do Teachers Emphasize at the Eighth Grade?
165
Subject Matter Emphasized Most in Mathematics Class
166 Are There National or Regional Policies on Using Calculators?
167 Exhibit 5.9
Policy On Calculator Usage
168 What Mathematics Topics Are Included in the Intended Curriculum?
170 Exhibit 5.10
Mathematics Topics Included in the TIMSS Questionnaires
172 Exhibit 5.11
Mathematics Topics in the Intended Curriculum for At
Least $90 \%$ of Students, Up to and Including Eighth Grade

## 183 CHAPTER 6

Teachers and Instruction

173 Have Students Been Taught the Topics Tested by TIMSS?
176 Exhibit 5.12
Percentages of Students Taught Fractions and Number Sense Topics
178 Exhibit 5.13
Percentages of Students Taught Measurement Topics
179 Exhibit 5.14
Percentages of Students Taught Data Representation, Analysis, and Probability Topics
Exhibit 5.15
Percentages of Students Taught Geometry Topics
181
Exhibit 5.16
Percentages of Students Taught Algebra Topics
182 Can Meaningful Comparisons Be Made Between the Intended and Implemented Curriculum?

187 What Preparation Do Teachers Have for Teaching Mathematics?

Age and Gender of Teachers
189 Exhibit 6.2
Preparation to Teach Mathematics
192 Exhibit 6.3
Index of Teachers' Confidence in Preparation to Teach Mathematics (CPTM)

194 How Much School Time Is Devoted to Mathematics Instruction?

196 Exhibit 6.4
Mathematics Instructional Time at Grade 8
197 Exhibit 6.5
Number of Hours Mathematics Is Taught Weekly
198 Exhibit 6.6
Trends in Number of Hours Mathematics Is Taught Weekly
199 Exhibit 6.7
Frequency of Outside Interruption During Mathematics Lessons

200 What Activities Do Students Do in Their Mathematics Lessons?

203 Exhibit 6.8
Mathematics Class Size
204 Exhibit 6.9 Trends in Mathematics Class Size
205 Exhibit 6.10
Time Spent on Various Activities in Mathematics Class
206 Exhibit 6.11
Students Doing Various Activities in Mathematics Class
207 Exhibit 6.12
Presentational Modes Used in Mathematics Class
208 Exhibit 6.13 Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)
210 Exhibit 6.14
Trends in Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)

211 How Are Calculators and Computers Used?
213 Exhibit 6.15 Calculator Use in Mathematics Class

214 Exhibit 6.16 Index of Emphasis on Calculators in Mathematics Class (ECMC)
216 Exhibit 6.17
Trends in Index of Emphasis on Calculators in Mathematics Class (ECMC)
217 Exhibit 6.18
Frequency of Computer Use in Mathematics Class
218 Exhibit 6.19
Trends in Frequency of Computer Use in Mathematics Class
219 Exhibit 6.20
Access to the Internet and Use of the Internet for Mathematics Projects

220 What Are the Roles of Homework and Assessment?

222 Exhibit 6.21
Index of Teachers' Emphasis on Mathematics
Homework (EMH)
224 Exhibit 6.22
Trends in Index of Teachers' Emphasis on Mathematics Homework (EMH)

225 Exhibit 6.23
Types of Assessment Teachers Give Quite A Lot or A Great Deal of Weight

## 7

## 227 CHAPTER 7

School Contexts for Learning and Instruction

229 What School Resources Are Available
to Support Mathematics Learning?
232 Exhibit 7.1
Index of Availability of School Resources for Mathematics Instruction (ASRMI)
234 Exhibit 7.2
Trends in Index of Availability of School Resources for Mathematics Instruction (ASRMI)

235 What Is the Role of the School Principal?

236
Time Principal Spends on Various School-Related
Activities
237 What Are the Schools' Expectations of Parents?

238 Exhibit 7.4
Schools' Expectations for Parental Involvement
239 How Serious Are School Attendance Problems?

240 Exhibit 7.5
Index of Good School and Class Attendance (SCA)
242 Exhibit 7.6
Frequency and Seriousness of Student Attendance Problems

243 How Safe and Orderly Are Schools?
244 Exhibit 7.7
Frequency and Seriousness of Student Behavior Threatening an Orderly School Environment
246 Exhibit 7.8
Frequency and Seriousness of Student Behavior Threatening a Safe School Environment

1

## 249 REFERENCE 1

Students' Backgrounds and Attitudes
Towards Mathematics

250 Exhibit R1.1
Educational Aids in the Home: Dictionary, Study Desk/Table, and Computer
251 Exhibit R1.2
Trends in Educational Aids in the Home
252 Exhibit R1.3
Number of Books in the Home
253 Exhibit R1.4
Trends in Number of Books in the Home
254
Exhibit R1.5
Highest Level of Education of Either Parent
256
Exhibit R1.6
Country Modifications to the Definitions of Educational Levels for Parents' Education or Students' Expectations for Finishing School
258 Exhibit R1.7
Students' Perception of the Importance of Various Activities
Exhibit R1.8
Students' Perception of Their Mothers' View of the Importance of Various Activities

Students' Perception of Their Friends' View of the Importance of Various Activities

## 261 Exhibit R1.10

Why Students Need to Do Well in Mathematics

## 262 Exhibit R1.11

Students' Daily Out-of-School Study Time
263 Exhibit R1.12
Trends in Students' Daily Out-of-School Study Time
264 Exhibit R1.13
Students' Daily Leisure Time
Students' Reports That Mathematics is Not One of Their Strengths
266
Exhibit R1.15
Students' Liking Mathematics
$\mathbf{R}$ R

2
3

## 281 REFERENCE 3

The Mathematics Curriculum

268 Exhibit R2. 1
Achievement Standards in Mathematics
269 Exhibit R2.2
Organization of Mathematics Instruction
270 Exhibit R2.3
Detailed Information About Topics in the Intended Curriculum, Up to and Including Eighth Grade - Fractions and Number Sense

## Exhibit R2.4

Detailed Information About Topics in the Intended
Curriculum, Up to and Including Eighth Grade -
Measurement
273 Exhibit R2.5
Detailed Information About Topics in the Intended Curriculum, Up to and Including Eighth Grade - Data Representation, Analysis, and Probability

## Exhibit R2.6

Detailed Information About Topics in the Intended Curriculum, Up to and Including Eighth Grade - Geometry

Detailed Information About Topics in the Intended Curriculum, Up to and Including Eighth Grade - Algebra
Exhibit R2.8
When Fractions and Number Sense Topics Are Taught
277 Exhibit R2.9
When Measurement Topics Are Taught
278 Exhibit R2.10
When Data Representation, Analysis, and Probability Topics Are Taught
279 Exhibit R2.11
When Geometry Topics Are Taught
280 Exhibit R2.12
When Algebra Topics Are Taught

Teachers and Instruction

282 Exhibit R3.1
Teachers' Major Area of Study in Their BA, MA, or Teacher Training Certification
284 Exhibit R3.2
Teachers' Confidence in Their Preparation to Teach Mathematics Topics
286 Exhibit R3.3
Shortages of Teachers Qualified to Teach Mathematics Affecting Capacity to Provide Instruction
288 Exhibit R3.4
Percentage of Students Whose Mathematics Teachers Agree or Strongly Agree with Statements About the Nature of Mathematics and Mathematics Teaching
290 Exhibit R3.5
Percentage of Students Whose Mathematics Teachers Think Particular Abilities Are Very Important for Students' Success in Mathematics in School

292 Exhibit R3.6
Average Number of Instructional Days in the School Year
293 Exhibit R3.7
Instructional Time in School
294 Exhibit R3.8
How Teachers Spend Their Formally Scheduled School Time
295 Exhibit R3.9
Asking Students to Do Problem-Solving Activities or Computation During Mathematics Lessons
296 Exhibit R3. 10
Trends in Asking Students to Do Problem-Solving Activities During Most or Every Mathematics Lesson
297 Exhibit R3. 11
Students Using Things from Everyday Life in Solving Mathematics Problems
298 Exhibit R3.12
Students' Reports on Frequency of Calculator Use in Mathematics Class

299 Exhibit R3. 13
Trends in Students' Reports on Frequency of Calculator Use in Mathematics Class
300 Exhibit R3. 14
Ways in Which Calculators Are Used
301 Exhibit R3.15
Amount of Mathematics Homework
302 Exhibit R3.16
Assigning Mathematics Homework Based on Projects and Investigations*
303 Exhibit R3.17
Frequency of Having a Quiz or Test in Mathematics Class

## 305 REFERENCE 4

School Contexts for Learning and Instruction

Exhibit R4.1
Shortages or Inadequacies in General Facilities and Materials That Affect Schools' Capacity to Provide Instruction in Mathematics Some or A Lot
307 Exhibit R4.2
Shortages or Inadequacies in Equipment and Materials for Mathematics Instruction That Affect Schools' Capacity to Provide Instruction in Mathematics Some or A Lot

Exhibit R4.3
Availability of Computers for Instructional Purposes
309 Exhibit R4.4
Schools' Access to the Internet

## 311 APPENDIX A

Overview of TIMSS Procedures:
Mathematics Achievement
313 History
313 Participants in TIMSS
315 Exhibit A. 1
Countries Participating in TIMSS 1999 and 1995
316 Developing the TIMSS 1999
Mathematics Test
318 Exhibit A. 2
The Three Aspects and Major Categories of the Mathematics Frameworks
319 Exhibit A. 3
Distribution of Mathematics Items by Content Reporting Category and Performance Category
320 Exhibit A. 4
Distribution of Mathematics Trend and Replacement Items by Content Reporting Category and Performance Category

321 Background Questionnaires
322 Translation and Verification
322 Population Definition and Sampling
325 Exhibit A. 5
Coverage of TIMSS 1999 Target Population
326 Exhibit A. 6
School Sample Sizes
327 Exhibit A. 7
Student Sample Sizes
328 Exhibit A. 8
Overall Participation Rates

330 Scoring the Free-Response Items
331 Exhibit A. 9
TIMSS 1999 Within-Country Free-Response Scoring
Reliability Data for Mathematics Items
332 Test Reliability
332
333
Exhibit A. 10
Cronbach's Alpha Reliability Coefficient - TIMSS 1999 Mathematics Test

335 Estimating Sampling Error
335 Making Multiple Comparisons
336 Setting International Benchmarks of Student Achievement

337 Mathematics Curriculum Questionnaire
338 Exhibit A. 11
Country-Specific Variations in Mathematics Topics in the Curriculum Questionnaire

## 339 APPENDIX B

Multiple Comparisons of Average
Achievement in Mathematics Content Areas
340 Exhibit B. 1
Multiple Comparisons of Average Achievement in
Fractions and Number Sense
341 Exhibit B. 2
Multiple Comparisons of Average Achievement in
Measurement
342 Exhibit B. 3
Multiple Comparisons of Average Achievement in Data
Representation, Analysis, and Probability
343 Exhibit B. 4
Multiple Comparisons of Average Achievement in
Geometry
344 Exhibit B. 5
Multiple Comparisons of Average Achievement in Algebra

## C

## 345 APPENDIX C

The Test-Curriculum Matching Analysis:
Mathematics

350 Exhibit C. 1
Average Percent Correct for Test-Curriculum Matching Analysis - Mathematics
351 Exhibit C. 2
Standard Errors for the Test-Curriculum Matching Analysis Mathematics

## 353 APPENDIX D

Percentiles and Standard Deviations of Mathematics Achievement

354 Exhibit D. 1
Percentiles of Achievement in Mathematics
355 Exhibit D. 2
Standard Deviations of Achievement in Mathematics

## $E$

## 357 APPENDIX E

Acknowledgments

## EXECUTIVE SUMMARY

TIMSS 1999
International
Mathematics
Report


## Executive Summary

In 1999, the Third International Mathematics and Science Study (timss) was replicated at the eighth grade. Involving 41 countries and testing at five grade levels, timss was originally conducted in 1995 to provide a base from which policy makers, curriculum specialists, and researchers could better understand the performance of their educational systems. Conducted under the auspices of the International Association for the Evaluation of Educational Achievement (iea), timss was the first step in a long-term strategy, with further assessments in mathematics and science planned for 1999, 2003, and beyond.
timss 1999, also known as timss-Repeat or timss-R, was designed to provide trends in eighth-grade mathematics and science achievement in an international context. Thirty-eight countries participated in timss 1999. Of these, 26 countries also participated in timss 1995 at the eighth grade and have trend data included in this report. Also, 1999 represents four years since the first timss, and the population of students originally assessed as fourth-graders had advanced to the eighth grade. Thus, for 17 of the 26 countries that participated in timss 1995 at the fourth grade, timss 1999 also provides information about whether the relative performance of these students has changed in the intervening years.

Five content areas were covered in the timss 1999 mathematics test: fractions and number sense; measurement; data representation, analysis, and probability; geometry; and algebra. About one-fourth of the questions were in the free-response format, requiring students to generate and write their answers. (See Chapter 2 for example items illustrating the range of mathematics concepts and processes covered in the timss 1999 tests.) The achievement data are accompanied by extensive questionnaire data about the home, classroom, school, and national contexts within which mathematics learning takes place.

Because a valid and efficient sample in each country is crucial to the quality and integrity of the study, timss developed procedures and standards regarding coverage of the target population, participation, and the age and years of schooling of students. For 1999, all countries met the guidelines, and any variations that occurred are annotated. Indeed, timss 1999 was conducted with rigorous attention to attaining high quality in all aspects of the project.

## Students' Mathematics Achievement

\author{

- Singapore, the Republic of Korea, Chinese Taipei, and Hong Kong
} SAR had the highest average performance, with Singapore and Korea having significantly higher achievement than all other participating countries. Japan also performed very well as did Belgium (Flemish) (see Exhibits 1.1 and 1.2).

Countries that showed an increase in average mathematics achievement between 1995 and 1999 were Latvia (Lss) ${ }^{1}$, Canada, and Cyprus. Only the Czech Republic showed a decrease.

The difference in average achievement for boys and girls was negligible in most countries, except Israel, the Czech Republic, Tunisia, and the Islamic Republic of Iran. The gender differences among highperforming students, although small, were statistically significant, with 27 percent of boys on average across countries in the top achievement quarter, compared with 23 percent of girls. Since boys and girls showed similar increases across countries from 1995 to 1999, the average gender difference remained essentially the same. Korea was the one country that narrowed the gender gap in average mathematics achievement.

[^0]
## Students' Home Environment and Attitudes Towards Mathematics

- On average internationally, students from homes with a high level of educational resources (more than 100 books; all three study aids: computer, study desk, and dictionary; and at least one parent finished university) had higher mathematics achievement than students from homes with fewer resources.

Eighth-grade students internationally had high expectations for further education. On average across countries, more than half the students reported that they expected to finish university. In almost every country there was a positive association between educational expectations and mathematics achievement.

Internationally on average, about 15 percent of the eighth-grade students seem to be convinced that they just cannot do mathematics. In each country, a more positive self-concept in mathematics was associated with higher average achievement. Interestingly, however, several countries with low percentages of students reporting a strong self-concept had high average mathematics achievement, including the five Asian Pacific countries (Singapore, Hong Kong, Chinese Taipei, Korea, and Japan).

Across the participating countries, eighth-grade students generally had positive attitudes towards mathematics. More boys than girls reported high levels of positive attitudes towards mathematics internationally and in a number of countries. There was little change overall in students' attitudes between 1995 and 1999.

## The Mathematics Curriculum

- In 35 of the 38 countries, specifications for students' curricular goals in mathematics were developed as national curricula. The exceptions were Australia, Canada, and the United States.

Testing and assessment were widely used methods to support curriculum implementation. Belgium (Flemish) was the one country that reported having no public examinations in mathematics to certify students or select them for university or academic tracks. Approximately two-thirds of the countries conduct system-wide assessments at two or three grades, primarily to inform policy makers about achievement of the intended curriculum.

On average across countries, the percentage of instructional time designated in official curricula for mathematics instruction remains about the same from grade 4 to grade 6 but then decreases by grade 8 ( 17,16 , and 13 percent, respectively). In contrast, the instructional time specified for science increases from grade 4 to grade 8 (from 11 to 16 percent).
Across countries, the official curricula for eighth grade most commonly placed major emphasis on mastering basic skills and understanding mathematical concepts. Moderate to major emphasis was placed on assessing student learning, "real-life" applications of mathematics, and communicating mathematically. Thirty-three countries reported at least moderate emphasis on solving non-routine problems, but working on mathematics projects was given minor or no emphasis in the intended curriculum of most countries.

According to their teachers, internationally 55 percent of the eighthgrade students were receiving mathematics instruction emphasizing a combination of algebra, geometry, and number sense; about 27 percent instruction emphasizing algebra or algebra combined with geometry; and 14 percent instruction in mainly number. Very few students were given an emphasis in only geometry (three percent).

## Instructional Contexts and Practices

- Internationally, 6o percent of eighth-grade students were taught mathematics by females and 40 percent by males, and similar percentages were found in a number of countries.

Teachers' undergraduate and graduate studies provide some indication of their preparation to teach mathematics. Internationally, 84 percent of students were taught by teachers having mathematics and/or mathematics education as a major area of study.

The timss 1999 results show higher achievement is related to higher levels of teachers' confidence in their preparation to teach mathematics. Internationally, teachers reported relatively high degrees of confidence, with 63 percent of students taught by teachers who believed they were very well prepared.

The percentage of instructional time at the eighth grade that was devoted to mathematics ranged from 9 to 17 percent. For the most part, the percentages reported by teachers corresponded with the percentages targeted in the intended curriculum.

In 1999, teachers reported that approximately half the students were in mathematics classes that met between about two and three and a half hours per week, and another third were in classes meeting about three and a half to five hours. Compared with 1995, this represents a slight increase (five percentage points) for the shorter time period and a commensurate decrease for the longer time period.

Videotapes of mathematics classes in the United States and Japan in TImSS 1995 revealed that outside interruptions can affect the flow of the lesson and detract from instructional time. Internationally in 1999, about one-fifth of the students reported that their mathematics classes were interrupted pretty often or almost always, and 28 percent reported that their classes were never interrupted. In comparison, more than half the students in Japan, Korea, and Tunisia were in classes with no interruptions.

Across the participating countries, teachers reported that the two most predominant activities encountered in mathematics class are teacher lecture and teacher-guided student practice, accounting for nearly half of class time.

- Students in classes emphasizing reasoning and problem-solving had higher achievement than those in classes with a low emphasis on these activities. In Japan, nearly half the students were in classes involving reasoning and problem-solving activities in most lessons. Across countries, however, the majority of students were asked to do such activities in some but not most lessons. There was some evidence of increased emphasis on problem-solving activities between 1995 and 1999. However, the percentage of students asked to practice their computational skills in most or every lesson also increased significantly between 1995 and 1999.
In the Netherlands, Singapore, and Australia, more than four-fifths of the students and their teachers reported at least weekly calculator use. From about two-thirds to four-fifths in England, Canada, New Zealand, Hong Kong, Israel, and the United States reported this level of calculator use. Calculators were used most frequently to check answers, perform routine computations, and solve complex problems. At the other end of the spectrum, a majority of students and their teachers reported using calculators infrequently or never in a number of countries, including Chinese Taipei, Iran, Japan, Korea, Malaysia, the Philippines, Romania, Thailand, and Turkey.

Across countries, the vast majority of students (8o percent) reported never using computers in mathematics class. The trend data from 1995 to 1999, however, show a small but statistically significant shift from the "never" to the "once in while" category. Although there was great variation across countries, about a quarter of the students internationally reported Internet access at school. Despite this access, only 10 percent on average used the Internet to obtain information for mathematics projects on even a monthly basis.

## School Factors

- Students in schools that reported being well resourced generally had higher average mathematics achievement than those in schools where across-the-board shortages affected instructional capacity in mathematics some or a lot. According to their principals, nearly half the students were in schools where instruction was negatively affected by shortages or inadequacies in instructional materials, budget for supplies, school buildings, instructional space, audiovisual resources, and library materials relevant to mathematics instruction. More than half the students were in schools where shortages or inadequacies in computers and computer software affected the capacity to provide mathematics instruction. Countries seemed to have computers either in nearly all of their schools or in only a fraction of them.

Clearly schools around the world expect help from parents. Internationally, $8_{5}$ percent of students attended schools expecting parents to ensure that their children complete their homework, 79 percent attended schools expecting parents to volunteer for school projects or field trips, and about half attended schools expecting parents to help raise funds and to serve on committees.

Internationally, one-fifth of the students attended schools where principals reported that attendance was not a problem. However, 60 percent were in schools where principals reported moderate attendance problems, and 19 percent were in schools with some serious attendance problems.

Generally, the overwhelming majority of eighth-grade students attended schools judged by principals to have few serious problems threatening an orderly or safe school environment.
$\qquad$


## INTRODUCTION

## TIMSS 1999

 International Mathematics ReportIn 1999, the Third International Mathematics and Science Study (Timss) was replicated at the eighth grade.

Thirty-eight countries participated in this mathematics and science assessment, known as timss-R or timss 1999.

The mathematics results are presented in this report for
the 38 countries that participated in timss in 1999.
Trend data also are included for 26 countries that
participated in timss in 1995.

## What is TIMSS?

Originally conducted in 1994-1995, the Third International Mathematics and Science Study (timss) was the largest and most comprehensive comparative international study of education ever undertaken. Designed to provide a base from which policy makers, curriculum specialists, and researchers could better understand the performance of their educational systems, timss compared the mathematics and science achievement of students in $4^{1}$ countries at five grade levels. Using questionnaires, videotapes, and analyses of curriculum materials, timss also investigated the contexts for learning mathematics and science in the participating countries. Information was collected about educational systems, curriculum, teacher and school characteristics, and instructional practices, providing an extremely rich source of valuable insights into mathematics teaching and learning.
timss results, which were first reported in 1996, have stirred debate, spurred reform efforts, and provided important information to academics, researchers, and decision makers around the world. ${ }^{1}$ Since that time most of the participating countries have published one or more national reports, analyzing the findings from their own perspective. In addition, at least 12 book-length international reports have been published, along with hundreds of articles and comments in newsletters, newspapers, and magazines.

## What is TIMSS 1999?

timss was the first step in a long-term strategy, with further assessments in mathematics and science planned for 1999, 2003, and beyond. timss 1999, also known as timss-Repeat or timss-R, is a replication of timss at the lower-secondary or middle-school level - the eighth grade in most countries. As a follow-up to the earlier study, timss 1999 adds to the richness of the timss data and their potential to have an impact on policy and practice.

Administered during the 1998-99 school year, timss 1999 was designed to provide trends in eighth-grade mathematics and science achievement in an international context. Also, 1999 represents four years since the first timss, and the population of students originally assessed as fourth-graders had advanced to the eighth grade. Thus, timss 1999 also provides information about whether the relative performance of

[^1]these students has changed in the intervening years. As in the original 1995 study, timss 1999 included a full range of context questionnaires and the timss-r Videotape Classroom Study examining mathematics and science instructional practices in seven nations. ${ }^{2}$

In countries new to the study as well as those that participated in 1995, the data from timss 1999 can help policy makers and practitioners assess their comparative standing and gauge the rigor and effectiveness of their mathematics and science programs. The aim is to improve the teaching and learning of mathematics and science for students everywhere by providing data about what types of curricula, instructional practices, and school environments result in higher student achievement.

## Who Conducted TIMSS 1999?

The original timss and timss 1999 were conducted by the International Association for the Evaluation of Educational Achievement (iea). With a permanent secretariat based in Amsterdam, the Netherlands, the iea is an independent international cooperative of national research institutions and governmental research agencies. Its primary purpose is to conduct large-scale comparative studies of educational achievement to gain a deeper understanding of the effects of policies and practices within and across systems of education.

Four iea studies in the areas of mathematics and science preceded timss. These were the First International Mathematics Study, 19591967; the First International Science Study, 1966-1973; the Second International Mathematics Study, 1976-1987; and the Second International Science Study, 1980-1989. During the same period, the iea conducted a number of studies that focused on other areas of schooling, including reading literacy, civics, computer applications, and early childhood education.

Funding for timss 1999 was provided by the United States, the World Bank, and the participating countries. Within the United States, funding agencies include the National Center for Education Statistics of the U.S. Department of Education, the National Science Foundation, and the Department of Education's Office of Educational Research and Improvement.

The iea delegated responsibility for the overall direction and management of the project to the International Study Center in the Lynch School of Education at Boston College, headed by Michael O. Martin

[^2]and Ina V.S. Mullis. In carrying out the project, the International Study Center worked closely with the iea Secretariat in Amsterdam, Statistics Canada in Ottawa, the iea Data Processing Center in Hamburg, and Educational Testing Service in Princeton, New Jersey.

## Which Countries Participated?

Exhibit 1 shows the 38 countries that participated in timss 1999. The decision to participate in any IEA study is coordinated through the secretariat in Amsterdam and made solely by each member country according to its own data needs and resources. Exhibit 1 shows that 26 countries also participated in timss $1995 .{ }^{3}$ For these, trend data are included in this report, while for 12 of the participants data are included only for Timss $1999 .{ }^{4}$ Seventeen of the 26 countries that participated in timss 1995 also have data at the fourth grade. ${ }^{5}$ A list of the countries participating in timss 1995 at grades 4 and 8 can be found in Exhibit A. 1 in the appendix.

Each participating country designated a national center to conduct the activities of the study and a National Research Coordinator (NRC) to implement it in accordance with international procedures - a considerable responsibility given the complexity of the data collection and the measurement instruments. The quality of the study depends on the work of the NRCS and their colleagues, and all those involved deserve deep appreciation for their continued commitment to the project. ${ }^{6}$

For the sake of comparability across countries and across assessments, all testing was conducted at the end of the school year, except in Lithuania. As noted in the exhibits in this report, Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year. The six countries on a Southern Hemisphere school schedule (Australia, Chile, Malaysia, New Zealand, Singapore and South Africa) tested in October through December of 1998, which was the end of the school year there. The remaining countries tested at the end of the 1998-1999 school year, most often in May and June of 1999 .

[^3]ountries with Data
from 1995 and 1999

Australia
Belgium (Flemish)
Bulgaria
Canada
Cyprus
Czech Republic
England
Hong Kong, SAR*
Hungary
Iran, Islamic Republic
Israel
Italy
Japan
Korea, Republic of
Latvia (LSS)
Lithuania
Netherlands
New Zealand
Romania
Russian Federation
Singapore
Slovak Republic
Slovenia
South Africa
Thailand
United States


## Countries <br> 



## What is the Comparability Across the Grades and Ages Tested?

Exhibit 2 shows information about the grade tested in each country for TIMSS 1999, including each country's name for the grade and the years of formal schooling students in the grade had completed when they were tested. Based on reassessing the same target population as originally defined for timss in 1995, all countries that participated in timss 1999 were to test students in the upper of the two grades with the largest proportion of 13 -year-olds. Although in 1995 Timss tested students in the two grades with the largest proportion of 13 -year-olds, the 1999 replication was carried out at only the upper of the two middle-school grades tested in 1995.

Exhibit 2 reveals that for most but not all countries, the grade tested represented the eighth year of formal schooling. Thus, solely for convenience, the report usually refers to the grade tested as the eighth grade.

It should be noted that students in Finland, in particular, had one year less of formal schooling and were about half a year younger, on average, than were the students tested internationally. Students in Morocco and the Philippines also had only seven years of formal schooling, as did some students in the Russian Federation. Students in the Czech Republic, England, and Moldova, as well as some in Australia and New Zealand, had nine years of formal schooling, yet the average age of the students was at or below the international average. Two countries, Romania and Slovenia, had students somewhat older than the international average, and a third, South Africa, had students about one year older, though these students had eight years of formal schooling. These countries, however, assessed the same grade as in 1995 in order to measure trends.

Having valid and efficient samples in each country is crucial to the quality and integrity of the study. The accuracy of the survey results depends on the quality of the sampling information available, and particularly on the quality of the samples. TIMSS developed procedures and guidelines to ensure that the national samples were of the highest quality possible. Standards were established and well documented for coverage of the target population, participation rates, and the age of students. For the most part, the national samples were drawn in accordance with the timss standards, and achievement results can be compared with confidence. Countries that deviated from the guidelines are specially annotated in the exhibits in this report. ${ }^{7}$

[^4]|  | Country's Name for Grade Tested | Years of Formal Schooling ${ }^{1}$ | Average Age of Students Tested |
| :---: | :---: | :---: | :---: |
| Australia | 8 or 9 | 8 or 9 | 14.3 |
| Belgium (Flemish) | 2 A \& 2 P | 8 | 14.1 |
| Bulgaria | 8 | 8 | 14.8 |
| Canada | 8 | 8 | 14.0 |
| Chile | 8 | 8 | 14.4 |
| Chinese Taipei | 2nd Grade Junior High School | 8 | 14.2 |
| Cyprus | 8 | 8 | 13.8 |
| Czech Republic | 8 | 8 | 14.4 |
| England | Year 9 | 9 | 14.2 |
| Finland | 7 | 7 | 13.8 |
| Hong Kong, SAR | Secondary 2 | 8 | 14.2 |
| Hungary | 8 | 8 | 14.4 |
| Indonesia | 2nd Grade Junior Secondary | 8 | 14.6 |
| Iran, Islamic Rep. | 8 | 8 | 14.6 |
| Israel | 8 | 8 | 14.1 |
| Italy | 3rd Grade Middle School | 8 | 14.0 |
| Japan | 2nd Grade Lower Secondary | 8 | 14.4 |
| Jordan | 8 | 8 | 14.0 |
| Korea, Rep. of | 2nd Grade Middle School | 8 | 14.4 |
| Latvia (LSS) | 8 | 8 | 14.5 |
| Lithuania ${ }^{\text { }}$ | 9 | 8.5 | 15.2 |
| Macedonia, Rep. of | 8 | 8 | 14.6 |
| Malaysia | Form 2 | 8 | 14.4 |
| Moldova | 8 | 9 | 14.4 |
| Morocco | 7 | 7 | 14.2 |
| Netherlands | Secondary 2 | 8 | 14.2 |
| New Zealand ${ }^{2}$ | Year 9 | 8.5 to 9.5 | 14.0 |
| Philippines | 1st Year High School | 7 | 14.1 |
| Romania | 8 | 8 | 14.8 |
| Russian Federation | 8 | 7 or 8 | 14.1 |
| Singapore | Secondary 2 | 8 | 14.4 |
| Slovak Republic | 8 | 8 | 14.3 |
| Slovenia | 8 | 8 | 14.8 |
| South Africa | 8 | 8 | 15.5 |
| Thailand | Secondary 2 | 8 | 14.5 |
| Tunisia | 8 | 8 | 14.8 |
| Turkey | 8 | 8 | 14.2 |
| United States | 8 | 8 | 14.2 |
|  |  | rnational Avg | 14.4 |

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
1 Years of schooling based on the number of years children in the grade level have been in formal schooling, beginning with primary education (International Standard Classification of Education Level1). Does not include pre-primary education,

2 The official nomenclature used in New Zealand since 1996 refers to students' years of schooling
rather than to a class/grade level. Year 9 students are found in a class level equivalent to grade 8 .

## What Was the Nature of the Mathematics Test?

Together with the quality of the samples, the quality of the test also receives considerable scrutiny in any comparative study. Developing the 1995 TIMss tests was a cooperative venture involving all of the NRCS during the entire process. Through a series of efforts, countries submitted items that were reviewed by mathematics subject-matter specialists, and additional items were written to ensure that the desired mathematics topics were covered adequately. Items were pilot tested, the results were reviewed, and new items were written and piloted. As part of the timss dissemination strategy, approximately two-thirds of the 1995 items were released for public use. For timss 1999, these items were replaced with items similar in content, format, and difficulty level. ${ }^{8}$ All of the potential replacement items were reviewed thoroughly by subject-matter experts and field tested. Nearly all the timss 1999 countries participated in field testing the replacement items with nationally representative samples, and all the nrcs had several opportunities to review the items and scoring criteria. The resulting timss 1999 mathematics test contained 162 items representing a range of mathematics topics and skills.

The timss curriculum frameworks developed for 1995 were also used for 1999. They describe the content dimensions for the timss tests as well as the performance expectations (behaviors that might be expected of students in school mathematics). ${ }^{9}$ Five content areas are covered in the timss 1999 mathematics test. These areas and the percentage of the test items devoted to each are fractions and number sense ( 38 percent), measurement ( $1_{5}$ percent), data representation, analysis, and probability ( 13 percent), geometry ( 13 percent), and algebra ( 22 percent). The performance expectations include knowing ( 19 percent), using routine procedures (23 percent), using complex procedures (24 percent), investigating and solving problems ( 31 percent), and communicating and reasoning (two percent).

About one-fourth of the questions were in the free-response format, requiring students to generate and write their answers. These questions, some of which required extended responses, were allotted about onethird of the testing time. Responses to the free-response questions were evaluated to capture diagnostic information, and some were scored using procedures that permitted partial credit. Chapter 2 of this report contains 16 example items illustrating the range of mathematics concepts and processes covered in the timss 1999 tests.

[^5]The timss 1999 tests were prepared in English and translated into 33 languages. A series of verification checks were conducted to ensure the comparability of the translations. ${ }^{10}$

Testing was designed so that no one student took all the items, which would have required more than three hours. Instead, exactly as in 1995, the test was assembled in eight booklets, each requiring 90 minutes to complete. Each student took only one booklet, and the items were rotated through the booklets so that each item was answered by a representative sample of students.
timss conducted a Test-Curriculum Matching Analysis in which countries examined the timss 1999 test to identify items measuring topics not covered in their curricula. The analysis showed that omitting such items for each country had little effect on the overall pattern of achievement results across all countries. ${ }^{11}$

[^6]
## How Do Country Characteristics Differ?

International studies of student achievement provide valuable comparative information about student performance, instructional practice, and curriculum. Accompanying the benefits of international studies, though, are challenges associated with comparing achievement across countries, cultures, and languages. In both the 1995 and 1999 studies, extensive efforts were made to attend to these issues through careful planning and documentation, cooperation among the participating countries, standardized procedures, and rigorous attention to quality control throughout. ${ }^{12}$

Beyond ensuring the integrity of the study procedures and collecting information about system-wide factors that influence students' opportunity to learn, ${ }^{13}$ the results from comparative studies such as Timss also need to be considered in light of country-wide demographic and economic factors. Some selected demographic characteristics of the timss 1999 countries are presented in Exhibit 3. Countries range widely in population size, from almost 270 million in the United States to less than one million in Cyprus, and in size, from almost 17 million square kilometers in the Russian Federation to less than one thousand in Hong Kong SAR and Singapore. Countries also vary widely on indicators of health, such as life expectancy at birth and infant mortality rate, and of literacy, including adult literacy rate and daily newspaper circulation. Exhibit 4 shows information for selected economic indicators, such as gross national product (GNP) per capita, expenditure on education and research and development as a percentage of GNP, unemployment rate, and amount of development aid. The data reveal that there is great disparity in the economic resources available to countries. Together the indicators in these two exhibits highlight the diversity of the timss 1999 countries, and although the factors they reflect do not necessarily determine high or low performance in mathematics, they do provide a context for considering the challenges involved in the educational task from country to country.

[^7]

Exhibits 3 and 4 Overleaf

|  | Population Size (in millions) ${ }^{1}$ | Area of Country (1000 square kilometers) ${ }^{2}$ | Life Expectancy at Birth ${ }^{3}$ | Infant <br> Mortality Rate (per 1000 live births) ${ }^{4}$ | Adult Literacy Rate (\%) ${ }^{5}$ | Daily Newspaper Circulation (per $1000)^{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Australia | 18.5 | 7682 | 78 | 5 | 99.0 | 296 |
| Belgium (Flemish) ${ }^{7}$ | 10.2 | 33 | 77 | 6 | 99.0 | 161 |
| Bulgaria | 8.3 | 111 | 71 | 18 | 98.2 | 254 |
| Canada | 30.3 | 9221 | 79 | 6 | 99.0 | 158 |
| Chile | 14.6 | 749 | 75 | 11 | 95.2 | 98 |
| Chinese Taipei ${ }^{8}$ | 22.1 | 36 | 75 | 8 | - | - |
| Cyprus ${ }^{9}$ | 0.8 | 9 | - | 6 | 95.9 | 111 |
| Czech Republic | 10.3 | 77 | 74 | 6 | 99.0 | 254 |
| England ${ }^{10}$ | 50.0 | 130 | - | - | 99.0 | - |
| Finland | 5.1 | 305 | 77 | 4 | 99.0 | 455 |
| Hong Kong | 6.5 | 1 | 79 | 5 | 92.4 | 786 |
| Hungary | 10.2 | 92 | 71 | 10 | 99.0 | 186 |
| Indonesia | 200.4 | 1812 | 65 | 47 | 85.0 | 23 |
| Iran, Islamic Rep. | 60.9 | 1622 | 69 | 32 | 73.3 | 26 |
| Israel ${ }^{11}$ | 6.1 | 21 | 78 | 7 | 95.4 | 288 |
| Italy | 57.5 | 294 | 78 | 5 | 98.3 | 104 |
| Japan | 126.1 | 377 | 80 | 4 | 99.0 | 578 |
| Jordan | 4.4 | 89 | 71 | 29 | 87.2 | 42 |
| Korea, Rep. | 46.0 | 99 | 72 | 9 | 97.2 | 394 |
| Latvia | 2.5 | 62 | 69 | 15 | 99.0 | 247 |
| Lithuania | 3.7 | 65 | 71 | 10 | 99.0 | 93 |
| Macedonia | 2.0 | 25 | 72 | 16 | 94.0 | 21 |
| Malaysia | 21.7 | 329 | 72 | 11 | 85.7 | 163 |
| Moldova | 4.3 | 33 | 67 | 20 | 98.3 | 60 |
| Morocco ${ }^{12}$ | 27.3 | 711 | 67 | 51 | 45.9 | 27 |
| Netherlands | 15.6 | 34 | 78 | 5 | 99.0 | 306 |
| New Zealand | 3.8 | 268 | 77 | 7 | 99.0 | 216 |
| Philippines | 73.5 | 298 | 68 | 35 | 94.6 | 82 |
| Romania | 22.6 | 230 | 69 | 22 | 97.8 | 298 |
| Russian Federation | 147.3 | 16889 | 67 | 17 | 99.0 | 105 |
| Singapore | 3.1 | 1 | 76 | 4 | 91.4 | 324 |
| Slovak Republic | 5.4 | 48 | 73 | 9 | 99.0 | 184 |
| Slovenia | 2.0 | 20 | 75 | 5 | 99.0 | 199 |
| South Africa | 40.6 | 1221 | 65 | 48 | 84.0 | 34 |
| Thailand | 60.6 | 511 | 69 | 33 | 94.7 | 64 |
| Tunisia | 9.2 | 155 | 70 | 30 | 67.0 | 31 |
| Turkey ${ }^{13}$ | 62.5 | 815 | 69 | 40 | 83.2 | 110 |
| United States | 267.6 | 9159 | 76 | 7 | 99.0 | 212 |

1 Estimates for 1997 based, in most cases, on a de facto definition. Refugees not permanently settled in the country of asylum are generally considered to be part of their country of origin. World Bank (1999) World Development Indicators, p. 42-44.

2 Area is the total surface area in square kilometers, comprising all land area and inland waters. World Bank (1999) World Development Indicators, p. 120-122.
3 Number of years a newborn infant would live if prevailing patterns of mortality at its birth were to stay the same throughout its life. World Bank (1999) World Development Indicators, p. 110-112.
4 Infant mortality rate is the number of deaths of infants under one year of age during 1997 per 1,000 live births in the same year. World Bank (1999) World Development Indicators, p.16-18.
5 Population aged 15 years and over. UNDP (1999) Human Development Report 1999 (134-137).
6 A newspaper issued at least four times a week is considered to be a daily newspaper. Circulation figures show the average circulation. UNESCO (1999) Statistical Yearbook, IV (106-133).

7 Figures for Belgium (Flemish) are for the whole country of Belgium.
8 Data provided by Department of Statistics, Ministry of Interior, Republic of China.
9 Data for population, area, and infant mortality provided by Cypriot Government Statistics Department.
10 The Statesman's Yearbook, 1998-99. Edited by Barry Turner, p. 1411.
11 Data provided by Israel's Central Bureau of Statistics, publication no. 1133.
12 Data provided by Ministere du plan et de l'initiation economique: Annuaire de Maroc, 1999.
13 Data provided by Turkey's State Institute of Statistics.
A dash $(-)$ indicates data are not available.

|  | Gross National Product per Capita (in US dollars) ${ }^{1}$ | GNP per Capita (Purchasing Power Parity ${ }^{2}$ | Expenditure on Education as \% of Gross National Product ${ }^{3}$ | Expenditure on Research and Development as \% of Gross National Product ${ }^{4}$ | Total Unemployment (\% of total labor force) ${ }^{5}$ | Aid per Capita ${ }^{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Australia | 20650 | 19510 | 5.5 | 1.8 | 8.4 | - |
| Belgium (Flemish) ${ }^{7}$ | 26730 | 23090 | 3.1 | 1.6 | 12.7 | - |
| Bulgaria | 1170 | 3870 | 3.2 | 0.6 | 11.1 | 25 |
| Canada | 19640 | 21750 | 6.9 | 1.7 | 9.4 | 0 |
| Chile | 4820 | 12240 | 3.6 | 0.6 | 5.3 | 9 |
| Chinese Taipei ${ }^{8}$ | 13235 | - | 4.9 | 2.0 | 2.9 | - |
| Cyprus | - | - | 4.5 | 0.2 | - | - |
| Czech Republic | 5240 | 10380 | 5.1 | 1.2 | 3.1 | 10 |
| England | - | - | - | - | - | - |
| Finland | 24790 | 19660 | 7.5 | 2.8 | 14.7 | - |
| Hong Kong | 25200 | 24350 | 2.9 | 0.3 | 2.2 | - |
| Hungary | 4510 | 6970 | 4.6 | 0.7 | 10.5 | 16 |
| Indonesia | 1110 | 3390 | 1.4 | 0.1 | - | 4 |
| Iran, Islamic Rep. | 1780 | 5690 | 4.0 | 0.5 | - | 3 |
| Israel ${ }^{9}$ | 16180 | 17680 | 10.1 | 2.4 | 7.7 | 204 |
| Italy | 20170 | 20100 | 4.9 | 2.2 | 12.1 | - |
| Japan | 38160 | 24400 | 3.6 | 2.8 | 3.2 | - |
| Jordan | 1520 | 3350 | 7.9 | 0.3 | - | 104 |
| Korea, Rep. | 10550 | 13430 | 3.7 | 2.8 | 2.7 | -3 |
| Latvia | 2430 | 3970 | 6.3 | 0.4 | 7.0 | 33 |
| Lithuania | 2260 | 4140 | 5.5 | 0.7 | 7.1 | 27 |
| Macedonia | 1100 | 3180 | 5.1 | - | 38.8 | 75 |
| Malaysia | 4530 | 7730 | 4.9 | 0.2 | 2.5 | -11 |
| Moldova | 460 | 1450 | 10.6 | 0.9 | 1.6 | 15 |
| Morocco | 1260 | 3210 | 5.3 | - | 17.8 | 17 |
| Netherlands | 25830 | 21300 | 5.1 | 2.1 | 6.2 | - |
| New Zealand | 15830 | 15780 | 7.3 | 1.0 | 6.0 | - |
| Philippines | 1200 | 3670 | 3.4 | 0.2 | 7.9 | 9 |
| Romania | 1410 | 4270 | 3.6 | 0.7 | 6.3 | 9 |
| Russian Federation | 2680 | 4280 | 3.5 | 0.9 | 3.4 | 5 |
| Singapore | 32810 | 29230 | 3.0 | 1.1 | 2.4 | 0 |
| Slovak Republic | 3680 | 7860 | 5.0 | 1.1 | 12.6 | 13 |
| Slovenia | 9840 | 11880 | 5.7 | 1.5 | 13.9 | 49 |
| South Africa | 3210 | 7190 | 8.0 | 0.7 | - | 12 |
| Thailand | 2740 | 6490 | 4.8 | 0.1 | 0.9 | 10 |
| Tunisia | 2110 | 5050 | 7.7 | 0.3 | - | 21 |
| Turkey | 3130 | 6470 | 2.2 | 0.5 | 6.6 | 0 |
| United States | 29080 | 29080 | 5.4 | 2.6 | 5.0 | - |

1 World Bank (1999) World Development Indicators, p. 12-14
2 An international dollar has the same purchasing power over GNP as a U.S. dollar in the United States. World Bank (1999) World Development Indicators, p. 12-14.
3 UNESCO (1999) Statistical Yearbook, p.II-(490-513); Belgium figure is for the Flemish community only; Cyprus is for Greek section only.
4 UNESCO (1999) Statistical Yearbook, p.lII-(6-17); Belgium figure is for the Flemish community only; Cyprus is for Greek section only.
5 Unemployment is the share of the labor force that is without work but available for and seeking employment. Definitions of labor force and unemployment differ by country. World Bank (1999) World Development Indicators, p. 58-60.

6 World Bank (1999) World Development Indicators, p. 352-355. Aid per capita includes official development assistance, which consists of disbursement of loans and grants, and official aid, which consists of capital projects, budget and balance of payments support, food and other commodity services, technical co-operation and emergency relief. A negative value indicates repayments exceed aid payments.
7 Figures for Belgium (Flemish) are for the whole country of Belgium
8 Data provided by Department of Statistics, Ministry of Interior, Republic of China.
9 Data Provided by Israel's Central Bureau of Statistics, publication no. 1133.
A dash $(-)$ indicates data are not available or that aggregates cannot be calculated because of missing data in year shown.
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## CHAPTER 1

## International Student

 Achievement in MathematicsChapter 1 summarizes eighth-grade achievement on the Timss 1999 mathematics assessment for each of the participating countries, and shows trends in student performance for those countries that also participated in Timss 1995 at the eighth grade. Comparisons of country performance against international benchmarks, as well as gender differences in performance, also are provided.


## How Do Countries Differ in Mathematics Achievement?

Exhibit 1.1 presents the distribution of student achievement for the 38 countries that participated in timss 1999. ${ }^{1}$ Countries are shown in decreasing order of average (mean) scale score, together with an indication of whether the country average is significantly higher or lower than the international average. The international average of 487 was obtained by averaging across the mean scores for each of the 38 participating countries. The results reveal substantial differences in mathematics achievement between the high- and low-performing countries, from an average of 604 for Singapore to 275 for South Africa. Nineteen countries had average mathematics achievement that was significantly above the international average, including three countries that are participating in timss for the first time - Chinese Taipei, Finland, and Malaysia. ${ }^{2}$ Fourteen countries had average achievement below the international average, including seven countries new to timss - Moldova, Tunisia, the Republic of Macedonia, Turkey, Jordan, Chile, and Morocco.

The broad range of achievement both within and across countries is illustrated in Exhibit 1.1 by a graphical representation of the distribution of student performance within each country. Achievement for each country is shown for the $25^{\text {th }}$ and $75^{\text {th }}$ percentiles as well as for the $5^{\text {th }}$ and $95^{\text {th }}$ percentiles. ${ }^{3}$ Each percentile point indicates the percentages of students performing below and above that point on the scale. For example, 25 percent of the eighth-grade students in each country performed below the 25 th percentile for that country, and 75 percent performed above the 25 th percentile. The range between the $25^{\text {th }}$ and $75^{\text {th }}$ percentiles represents performance by the middle half of the students. In most countries, the range of performance for the middle group was between 100 and 130 scale-score points. In contrast, performance at the $5^{\text {th }}$ and 95 th percentiles represents the extremes in both lower and higher achievement. The range of performance between these two score points, which includes go percent of the population, is approximately 270 points in most countries. The dark boxes at the midpoints of the distributions show the 95 percent confidence intervals around the average achievement in each country. ${ }^{4}$

[^8]As well as showing the wide spread of student achievement within each country, the percentiles also provide a perspective on the size of the differences among countries. Even though performance generally differed very little between one country and the next higher- or lower-performing country, the range in performance across the 38 countries was very large. For example, average performance in Singapore was comparable to or even exceeded performance at the $95^{\text {th }}$ percentile in the lower-performing countries such as Chile, the Philippines, Morocco, and South Africa. This means that only the most proficient students in the lower-performing countries approached the level of achievement of Singaporean students of average proficiency.

To aid in interpretation, Exhibit 1.1 also includes the years of formal schooling and average age of the students in each country. Equivalence of chronological age does not necessarily mean that students have received the same number of years of formal schooling or studied the same curriculum. Most notably, students in Finland, Morocco, the Philippines, and parts of the Russian Federation had fewer years of formal schooling than their counterparts in other countries, while those in the Czech Republic, England, Moldova, and parts of Australia and New Zealand had more years of schooling. The average age of students ranged from 13.8 years in Cyprus and Finland to 15.5 years in South Africa.

Exhibit 1.2 compares overall mean achievement among individual countries. This figure shows whether or not the differences in average achievement between pairs of countries are statistically significant. Selecting a country of interest and reading across the table, a triangle pointing up indicates significantly higher performance than the comparison country listed across the top; a circle indicates no significant difference in performance; and a triangle pointing down indicates significantly lower performance.

The data in Exhibit 1.2 reinforce the point that, when ordered by average achievement, adjacent countries usually did not significantly differ from each other, although the differences in achievement between the highperforming and low-performing countries were very large. Because of this wide range in performance, the pattern for a number of countries was one of having lower mean achievement than some countries, about the same mean achievement as other countries, and higher mean achievement than a third group of countries.


Singapore, the Republic of Korea, Chinese Taipei, and Hong Kong SAR had the highest average performance, with Singapore and Korea having significantly higher mean achievement than the rest of the other participating countries, and Chinese Taipei and Hong Kong significantly better than all the other countries except Japan. Japan also performed very well, with significantly higher achievement than most other participating countries, as did Belgium (Flemish). ${ }^{5}$ Interestingly, the Netherlands, the Slovak Republic, Hungary, Canada, Slovenia, the Russian Federation, Australia, Finland, the Czech Republic, Malaysia, and Bulgaria all performed very similarly. In fact, the difference in performance from one country to the next was often negligible.

5 Average achievement in Belgium (Flemish) was 558 compared to 579 in Japan and 540 in the Netherlands. Even though the differences are comparable, the latter difference was not statistically significant because the Netherlands had a larger than usual standard error.



- Country average significantly higher than international average

No statistically significant difference between country average and international average

- Country average significantly lower than international average

Significance tests adjusted for multiple comparisons
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent
$\square$
$\square$
$\square$

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


- Average achievement significantly higher than comparison country
- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

Significance tests adjusted for multiple comparisons

## How Has Mathematics Achievement Changed Since 1995?

Twenty-six countries took part in the timss eighth-grade assessments in both 1995 and 1999. For these countries, Exhibit 1.3 shows the results and the differences in average achievement between the two years. ${ }^{6}$ Average mathematics achievement across these 26 countries increased slightly, from a scale score of 519 in 1995 to 521 in 1999. However, this increase was not statistically significant.

In some countries, average mathematics achievement increased considerably between 1995 and 1999. The greatest increase was in Latvia (Lss) ${ }^{7}$, with an increase of 17 scale-score points. Canada and Cyprus also had statistically significant gains in average mathematics achievement between 1995 and 1999. Hong Kong, the Netherlands, and Lithuania also had increases of 10 or more scale-score points, although the somewhat larger estimates of measurement error for these countries meant that the differences were not statistically significant. The Lithuanian results should be interpreted with additional caution, since Lithuania conducted the assessment six months later than other participants, when the students were beginning ninth grade rather than finishing eighth grade.

Several countries showed a small decrease in average achievement from 1995 to 1999, but only in the case of the Czech Republic was it statistically significant. Israel, South Africa, and Thailand are shown in a separate panel in Exhibit 1.3 because they used unapproved sampling procedures at the classroom level in 1995. Israel and Thailand showed large decreases since 1995, which could indicate an upward bias in the 1995 results due to their sampling problems in the original timss rather than actual decreases.
timss in 1995 assessed both fourth- and eighth-grade students. This allowed participants to compare their performance relative to each other at the fourth and eighth grades, and gave a cross-sectional perspective on how relative performance changed between grades. ${ }^{8}$ For example, as shown in Exhibit 1.4, Singapore, Korea, Japan, and Hong Kong performed significantly above the international average at the fourth grade in 1995 and again at the eighth grade in 1999. In contrast, the Netherlands and the Czech Republic were significantly above the international average at the fourth grade in 1995, but only similar to it four years later at the eighth grade. Canada had mathematics performance

[^9]
significantly below the international average at the fourth grade in 1995, but similar to it at the eighth grade in 1999. In contrast, the United States and Italy moved from being similar to the international average at the fourth grade in 1995 to significantly below it at the eighth grade in 1999.

It has been argued, at least in the United States, that recent reforms in education had their greatest impact in the earlier grades, and that a second timss assessment could show better results for the eighth grade in 1999 than in 1995. Despite a modest, non-statistically significant gain at the eighth grade (see Exhibit 1.3), however, the data show that the relative position of the U.S. at grade 8 was below the international average in 1999 just as it was in 1995.


Countries with Unapproved Sampling Procedures at the Classroom Level in 1995

| Israel | 513 (6.2) | 482 (4.7) | -32 (7.8) | Difference statistically significant |
| :---: | :---: | :---: | :---: | :---: |
| South Africa | 278 (9.2) | 275 (6.8) | -3 (11.5) |  |
| Thailand | 516 (6.0) | 467 (5.1) | -49 (7.9) | Difference not statistically significant |
|  |  |  |  | Significance tests adjusted for multiple comparisons |

§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below $65 \%$ in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 1.4 Mathematics Achievement for TIMSS 1999 Countries That Participated in 1995 at Both the Fourth and Eighth Grades in Relation to the Average

## 1995



| Eighth Grade |  |
| :---: | ---: |
| Difference From |  |
| Average Across Countries§ |  |
| Singapore | $87(3.8)$ |
| Japan | $59(1.8)$ |
| Korea, Rep. of | $59(2.1)$ |
| Hong Kong, SAR | $47(5.8)$ |
| Czech Republic | $24(4.3)$ |
| Slovenia | $9(2.8)$ |
| Netherlands | $7(5.8)$ |
| Hungary | $5(3.1)$ |
| Canada | $-1(2.2)$ |
| Australia | $-3(3.7)$ |
| New Zealand | $-21(4.5)$ |
| England | $-24(2.9)$ |
| United States | $-29(4.6)$ |
| Italy | $-31(3.3)$ |
| Latvia (LSS) | $-33(3.5)$ |
| Cyprus | $-54(2.3)$ |
| Iran, Islamic Rep. | $-103(3.8)$ |
| Avg. Across Countries ${ }^{\S}$ | $522(0.9)$ |


| Eighth Grade |  |
| :---: | :---: |
| Difference From |  |
| Average Across Countries ${ }^{\S}$ |  |
| Singapore | $80(5.9)$ |
| Korea, Rep. of | $63(2.0)$ |
| Hong Kong, SAR | $58(4.2)$ |
| Japan | $55(1.8)$ |
| Netherlands | $16(6.8)$ |
| Hungary | $8(3.6)$ |
| Canada | $7(2.7)$ |
| Slovenia | $6(2.8)$ |
| Australia | $1(4.7)$ |
| Czech Republic | $-4(4.1)$ |
| Latvia (LSS) | $-19(3.3)$ |
| United States | $-22(3.8)$ |
| England | $-28(4.0)$ |
| New Zealand | $-33(4.9)$ |
| Italy | $-39(4.6)$ |
| Cyprus | $-48(1.9)$ |
| Iran, Islamic Rep. | $-102(3.3)$ |
| Avg. Across Countries ${ }^{\S}$ | $524(1.0)$ |


| Fourth Grade |  |
| ---: | ---: |
| Difference From |  |
| Average Across Countries ${ }^{\S}$ |  |
| Singapore | $73(4.3)$ |
| Korea, Rep. of | $63(1.9)$ |
| Japan | $50(2.0)$ |
| Hong Kong, SAR | $40(3.8)$ |
| Netherlands | $32(2.9)$ |
| Czech Republic | $23(3.0)$ |
| Slovenia | $8(3.1)$ |
| Hungary | $4(3.5)$ |
| United States | $0(2.9)$ |
| Australia | $0(3.0)$ |
| Italy | $-7(4.5)$ |
| Canada | $-12(3.3)$ |
| Latvia (LSS) | $-18(4.4)$ |
| England | $-33(3.2)$ |
| Cyprus | $-42(3.1)$ |
| New Zealand | $-48(4.2)$ |
| Iran, Islamic Rep. | $-130(4.8)$ |
| Avg. Across Countries ${ }^{\S}$ | $517(0.9)$ |


|  |
| :--- |
| Country average significantly higher than average |
| across countries | | Country average not significantly different from |
| :--- |
| average across countries |$\quad$| Country average significantly lower than average |
| :--- |
| across countries |
| Significance tests adjusted for multiple comparisons |

[^10]
## How Do Countries Compare with International Benchmarks of Mathematics Achievement?

The timss mathematics achievement scale summarizes student performance on test items designed to measure a wide range of student knowledge and proficiency. In order to provide meaningful descriptions of what performance on the scale could mean in terms of the mathematics that students know and can do, timss identified four points on the scale for use as international benchmarks, and conducted an ambitious scaleanchoring exercise to describe performance at these benchmarks. Exhibit 1.5 shows the four international benchmarks of mathematics achievement and briefly describes what students scoring at these benchmarks typically know and can do. More detailed descriptions appear in Chapter 2, together with example test items illustrating performance at each benchmark.

The Top 10\% Benchmark is defined at the goth percentile on the timss mathematics scale, taking into account the performance of all students in all countries participating in 1999. This point on the scale, which corresponds to a scale score of 616 , is the point above which the top 10 percent of the students in the timss 1999 assessment scored. Students performing at this level demonstrated that they could organize information, make generalizations, and explain solution strategies in non-routine problem solving situations.

The Upper Quarter Benchmark is the $75^{\text {th }}$ percentile on the mathematics scale. This point, corresponding to a scale score of 555 , is the point above which the top 25 percent of students scored. Students scoring at this benchmark demonstrated that they could apply their mathematical understanding and knowledge in a wide variety of relatively complex situations involving fractions, decimals, geometric properties, and algebraic expressions.

The Median Benchmark, with a score of 479, corresponds to the 5oth percentile, or median. This is the point above which the top half of the students scored on the timss 1999 assessment. Students performing at this level showed they could apply basic mathematical knowledge in straightforward situations, such as one-step word problems involving addition and subtraction or computational problems based on basic properties of geometric figures and simple algebraic relationships.

The Lower Quarter Benchmark is the 25 th percentile and corresponds to a scale score of 396 . This score point was reached by the top 75 percent of students, and may be used as a benchmark of performance for lower-achieving students. Students scoring at this level typically demonstrated computational facility with whole numbers.

Exhibit 1.6 displays the percentage of students in each participating country that reached each international benchmark, in decreasing order by percentage reaching the Top $10 \%$ Benchmark. If student achievement in mathematics were distributed in the same way in every country, then each country would be expected to have approximately 10 percent of its students reaching the Top $10 \%$ Benchmark, 25 percent the Upper Quarter Benchmark, 50 percent the Median Benchmark, and 75 percent the Lower Quarter Benchmark. Although New Zealand came fairly close, no country followed this pattern exactly. Instead, the high-performing countries generally had greater percentages of students reaching each benchmark, and the low-performing countries had lesser percentages. Among the high performers, for example, Singapore, Chinese Taipei, Korea, Hong Kong, and Japan had one-third or more of their students reaching the Top 10\% Benchmark, about two-thirds or more reaching the Upper Quarter Benchmark, around go percent reaching the Median Benchmark, and almost all ( 95 to 99 percent) reaching the Lower Quarter Benchmark. In contrast, low-performing countries such as South Africa, the Philippines, and Morocco had almost no students reaching the Top $10 \%$ Benchmark, no more than one percent reaching the Upper Quarter Benchmark, less than 1 o percent reaching the Median Benchmark, and no more than 31 percent reaching the Lower Quarter Benchmark.

Although Exhibit 1.6 is organized to draw particular attention to the percentage of high-achieving students in each country, it conveys information about the distribution of middle and low performers also. For example, Canada, Australia, and Malaysia had 12 percent of their students reaching the Top $10 \%$ Benchmark, as might be expected, but 94 to 96 percent (rather than 75 percent) reaching the Lower Quarter Benchmark.

Exhibits 1.7 through 1.10 provide more information on the change in student performance from 1995 to 1999 by showing the percentages reaching each international benchmark (Top 10\%, Upper Quarter, Median, and Lower Quarter) in each of the years for the 26 countries that participated in both assessments. ${ }^{9}$ In general, there were very few changes at any of the benchmarks, but these exhibits do provide fur-

9 For Exhibits 1.7 through 1.10 the benchmarks were those computed from the 1999 data.
ther detail about the countries that showed increases or decreases in Exhibit 1.3 in average mathematics achievement from 1995 to 1999. For example, the decrease in performance in the Czech Republic is also apparent at the Upper Quarter, Median, and Lower Quarter benchmarks, implying a decrease at most levels of the proficiency distribution. In contrast, the increase for Latvia (LSs) appears mainly at the Median benchmark, and for Cyprus at the Lower Quarter benchmark.


Exhibits 1.5-1.10 Overleaf

## - Top 10\% Benchmark

Students can organize information, make generalizations, and explain solution strategies in non-routine problem solving situations. They can organize information and make generalizations to solve problems; apply knowledge of numeric, geometric, and algebraic relationships to solve problems (e.g., among fractions, decimals, and percents; geometric properties; and algebraic rules); and find the equivalent forms of algebraic expressions.

## - Upper Quarter Benchmark

Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They can order, relate and compute with fractions and decimals to solve word problems; solve multi-step word problems involving proportions with whole numbers; solve probability problems; use knowledge of geometric properties to solve problems; identify and evaluate algebraic expressions and solve equations with one variable.

## - Median Benchmark

Students can apply basic mathematical knowledge in straightforward situations. They can add or subtract to solve one-step word problems involving whole numbers and decimals; identify representations of common fractions and relative sizes of fractions; solve for missing terms in proportions; recognize basic notions of percents and probability; use basic properties of geometric figures; read and interpret graphs, tables, and scales; and understand simple algebraic relationships.

## - Lower Quarter Benchmark

Students can do basic computations with whole numbers. The few items that anchor at this level provide some evidence that students can add, subtract, and round with whole numbers. When there are the same number of decimal places, they can subtract with multiple regrouping. Students can round whole numbers to the nearest hundred. They recognize some basic notation and terminology.


## Exhibit 1.6 Percentages of Students Reaching TIMSS 1999 International Benchmarks of Mathematics Achievement

TIMSS1999
8
Mathematics


| $\begin{aligned} & \text { Top } \\ & \text { 10\% } \end{aligned}$ | Upper Quarter | Median | Lower Quarter |
| :---: | :---: | :---: | :---: |
| 46 (3.5) | 75 (2.7) | 93 (1.3) | 99 (0.3) |
| 41 (1.7) | 66 (1.5) | 85 (1.0) | 95 (0.6) |
| 37 (1.0) | 68 (0.9) | 91 (0.5) | 99 (0.2) |
| 33 (2.3) | 68 (2.4) | 92 (1.5) | 99 (0.6) |
| 33 (1.1) | 64 (0.9) | 89 (0.5) | 98 (0.3) |
| 23 (1.5) | 54 (1.7) | 85 (1.2) | 98 (0.6) |
| 16 (1.2) | 41 (1.9) | 74 (1.6) | 94 (1.0) |
| 15 (1.2) | 39 (1.4) | 74 (1.4) | 95 (0.7) |
| 15 (1.8) | 37 (2.8) | 72 (2.7) | 94 (1.2) |
| 14 (2.3) | 45 (4.1) | 81 (3.5) | 96 (1.3) |
| 14 (1.4) | 40 (2.3) | 78 (1.8) | 96 (0.6) |
| 12 (1.1) | 38 (1.5) | 77 (1.3) | 96 (0.6) |
| 12 (1.8) | 37 (2.7) | 73 (2.4) | 94 (0.8) |
| 12 (1.4) | 34 (2.4) | 69 (2.2) | 94 (0.8) |
| 11 (1.4) | 33 (2.1) | 69 (2.3) | 94 (1.1) |
| 11 (2.3) | 30 (3.0) | 66 (2.6) | 91 (1.3) |
| 9 (1.0) | 28 (1.6) | 61 (1.9) | 88 (1.0) |
| 8 (1.2) | 25 (2.4) | 56 (2.5) | 85 (1.5) |
| 7 (0.9) | 26 (1.8) | 63 (2.0) | 92 (1.0) |
| 7 (0.9) | 24 (1.9) | 58 (2.1) | 89 (1.3) |
| 6 (0.9) | 31 (1.7) | 75 (1.5) | 96 (0.5) |
| 5 (0.7) | 20 (1.4) | 52 (2.1) | 83 (1.4) |
| 5 (1.1) | 19 (1.9) | 49 (2.6) | 80 (2.1) |
| 5 (0.6) | 18 (1.3) | 47 (1.8) | 77 (1.9) |
| 4 (0.7) | 17 (2.0) | 52 (2.4) | 86 (1.8) |
| 4 (0.7) | 16 (1.5) | 45 (2.2) | 81 (1.7) |
| 4 (0.8) | 16 (1.8) | 44 (2.6) | 81 (1.6) |
| 3 (0.4) | 17 (0.8) | 51 (1.1) | 84 (0.8) |
| 3 (0.4) | 12 (1.0) | 38 (1.9) | 72 (1.8) |
| 3 (0.5) | 11 (0.9) | 32 (1.5) | 62 (1.4) |
| 2 (0.4) | 7 (0.9) | 22 (1.4) | 52 (2.2) |
| 1 (0.3) | 7 (1.0) | 27 (1.9) | 65 (2.0) |
| 1 (0.2) | 5 (0.8) | 25 (1.7) | 63 (1.5) |
| 1 (0.5) | 3 (1.1) | 15 (1.8) | 48 (2.0) |
| 0 (0.1) | 4 (0.5) | 32 (1.6) | 80 (1.3) |
| 0 (0.1) | 1 (0.5) | 8 (1.4) | 31 (2.5) |
| 0 (0.2) | 1 (0.4) | 5 (1.0) | 14 (2.0) |
| 0 (0.0) | 0 (0.2) | 5 (0.4) | 27 (1.1) |



Top 10\% Benchmark (90th Percentile) $=616$ Upper Quarter Benchmark (75th Percentile) $=555$ Median Benchmark (50th Percentile) $=479$

Lower Quarter Benchmark (25th Percentile) =

[^11]$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

## Exhibit 1.7 Trends in Percentages of Students Reaching the TIMSS 1999 Top 10\%

 International Benchmark of Mathematics Achievement

§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 1.8 Trends in Percentages of Students Reaching the TIMSS 1999 Upper Quarter International Benchmark of Mathematics Achievement



§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian-
Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next
school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.



1999 significantly higher than 1995

No significant difference between 1995 and 1999

1999 significantly lower than 1995
V

Significance tests adjusted for multiple comparisons
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 1.10 Trends in Percentages of Students Reaching the TIMSS 1999 Lower Quarter International Benchmark of Mathematics Achievement

| Singapore | Percentage Quarter Inter | $\begin{aligned} & \text { ts } A \\ & \text { ench } \end{aligned}$ | the Lower 95 and 1999 | 1995 <br> Percentage of Students | 1999 <br> Percentage of Students | 1995-1999 <br> Difference |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 100 (0.0) | 99 (0.3) | -1 (0.3) |  |
| Korea, Rep. of |  |  |  | 97 (0.4) | 99 (0.2) | 1 (0.5) | - |
| Hong Kong, SAR |  |  |  | 96 (1.1) | 99 (0.6) | 2 (1.2) | - |
| Japan |  |  |  | 99 (0.2) | 98 (0.3) | 0 (0.3) | ) |
| Belgium (Flemish) |  |  |  | 97 (1.1) | 98 (0.7) | 1 (1.3) | - |
| Netherlands |  |  |  | 95 (1.6) | 96 (1.3) | 1 (2.0) |  |
|  |  |  |  | 96 (0.5) | 96 (0.6) | 0 (0.7) | - |
| Canada |  |  |  | 95 (0.5) | 96 (0.6) | 1 (0.8) | - |
| Slovenia |  |  |  | 97 (0.6) | 95 (0.7) | -3 (0.9) | - |
| Czech Republic |  |  |  | 98 (0.4) | 94 (1.1) | -4 (1.1) | V |
| Australia |  |  |  | 91 (0.9) | 94 (0.8) | 3 (1.2) |  |
| Hungary |  |  |  | 95 (0.8) | 94 (1.0) | -1 (1.2) | - |
| Russian Federation |  |  |  | 94 (1.1) | 94 (1.2) | 0 (1.7) | - |
| Latvia (LSS) |  |  |  | 88 (1.4) | 92 (1.0) | 4 (1.6) | - |
| International Avg. ${ }^{\text {s }}$ |  |  |  | 90 (0.3) | 91 (0.3) | 1 (0.4) | $\bullet$ |
| Bulgaria |  |  |  | 91 (1.0) | 91 (1.3) | 0 (1.6) |  |
| England |  |  |  | 88 (1.1) | 89 (1.3) | 1 (1.6) | - |
| United States |  |  |  | 87 (1.5) | 88 (1.0) | 1 (1.8) | $\bigcirc$ |
| Lithuania |  |  |  | 82 (1.7) | 86 (1.8) | 4 (2.5) | - |
| New Zealand |  |  |  | 90 (1.3) | 85 (1.5) | -4 (2.0) | - |
| Italy |  |  |  | 85 (1.2) | 85 (1.9) | 0 (2.4) | $\bigcirc$ |
| Cyprus |  |  |  | 78 (1.1) | 84 (0.8) | 6 (1.4) | - |
| Romania |  |  |  | 80 (1.6) | 80 (2.1) | 0 (2.7) | - |
| Iran, Islamic Rep. |  |  |  | 61 (2.0) | 63 (1.5) | 1 (2.5) | $\rho$ |
|  | 25 | 50 | 75 |  |  |  |  |
| Countries with Unapproved Sampling Procedures at the Classroom Level in 1995 |  |  |  |  |  |  |  |
| Israel |  |  |  | 92 (1.4) | 82 (2.1) | -10 (2.6) | $\nabla$ |
| South Africa |  |  |  | 15 (3.0) | 14 (2.0) | -1 (3.6) | - |
| Thailand |  |  |  | 93 (0.9) | 81 (1.6) | -13 (1.9) | $\nabla$ |


§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## What Are the Gender Differences in Mathematics Achievement?

Exhibits 1.11 through 1.14 show gender differences in eighth-grade math-

" $\Gamma$ematics achievement in 1999, and also changes since 1995. Exhibit 1.11 presents average achievement separately for girls and boys for each of the timss 1999 countries, as well as the difference between the means. Countries are shown in increasing order of this gender difference. The gender difference for each country is shown by a bar, indicating the amount of the difference, whether the direction of the difference favored girls or boys, and whether the difference is statistically significant (indicated by a darkened bar). On average across all countries there was a modest but significant difference favoring boys, although the situation varied considerably from country to country. In most countries the gender difference was negligible. The only countries with differences large enough to be statistically significant were Israel, the Czech Republic, the Islamic Republic of Iran, and Tunisia. The countries with the greatest differences were Iran and Tunisia, where the mean for boys exceeded the mean for girls by 24 to 25 scale-score points.

Exhibit 1.12 provides information on gender differences in mathematics achievement among students with high performance compared to those in the middle of the achievement distribution. For each country, score levels were computed for the highest-scoring 25 percent of students, called the upper quarter level, and for the top-scoring 50 percent of students, called the median level. The percentages of girls and boys in each country reaching each of the two levels were computed. For equitable performance, 25 percent each of girls and boys should have reached the upper quarter level, and 50 percent each the median level.

On average across countries, 23 percent of girls compared with 27 percent of boys reached the upper quarter level, and 49 percent of girls compared with $5^{1}$ percent of boys reached the median level. These gender differences favoring boys, although small, were statistically significant. Despite this, in nearly all participating countries the percentages of girls and boys reaching the upper quarter and median levels were equivalent. In all but four countries, the percentages reaching the upper quarter and median levels were not significantly different, indicating that gender equity exists in most countries at these levels. However, in Israel, Tunisia, and the United States, the percentages of boys reaching the upper quarter level were significantly greater than the percentages of girls reaching
this level. In Tunisia, the percentage of boys reaching the median level was also significantly greater than the percentage of girls, whereas in the Philippines, the percentage of girls reaching level was greater ( 53 percent for girls vs. 46 percent for boys).

Achievement differences from 1995 to 1999 are presented separately for girls and for boys in Exhibit 1.13. Average mathematics achievement across countries for girls increased significantly in Korea only. Achievement for both girls and boys decreased significantly in the Czech Republic, Israel, and Thailand.

Taking the study of trends in gender differences one step further, Exhibit 1.14 presents the difference in average mathematics achievement between boys and girls in 1995 and in 1999, and shows whether the difference has changed. Korea is the one country showing a significant decrease in the gender difference, from 17 to 5 scale-score points favoring boys. Fortunately, no country showed a significant increase in gender differences in mathematics performance.

† Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
(2) $\square$
$\square$ - 5


## Exhibit 1.12 Percentages of Girls and Boys Reaching Each Country's Own Upper Quarter and Median Levels of Mathematics Achievement

|  | Upper Quarter |  |  | Median |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Girls | Percent of Boys |  | Percent of Girls | Percent of Boys |  |
| Australia Belgium (Flemish) ${ }^{\dagger}$ Bulgaria Canada Chile | $\begin{array}{ll} 24(2.8) \\ 25 & (2.5) \\ 24(3.1) \\ 24(1.2) \\ 23 & (1.9) \end{array}$ | 26 (2.6) <br> 25 (2.5) <br> 26 (3.5) <br> 26 (1.4) <br> 27 (2.6) |  | $\begin{array}{ll} 49 & (3.2) \\ 50 & (3.1) \\ 51 & (3.0) \\ 49 & (1.3) \\ 48 & (2.2) \end{array}$ | 51 (3.0) <br> 50 (3.5) <br> 49 (3.2) <br> 51 (1.9) <br> 52 (2.4) |  |
| Chinese Taipei Cyprus Czech Republic England ${ }^{\dagger}$ Finland | $\begin{array}{ll} 22 & (1.5) \\ 24 & (1.4) \\ 22 & (1.6) \\ 20 & (2.7) \\ 23 & (1.8) \end{array}$ | $\begin{array}{ll} 28 & (1.9) \\ 26 & (1.4) \\ 28 & (2.5) \\ 30 & (2.4) \\ 27 & (2.2) \end{array}$ |  | 49 (1.9) <br> 50 (1.4) <br> 46 (2.4) <br> 46 (3.0) <br> 49 (1.9) | $\begin{array}{ll} 51 & (2.1) \\ 50 & (1.5) \\ 54 & (2.9) \\ 54 & (2.7) \\ 51 & (2.2) \end{array}$ |  |
| Hong Kong, SAR ${ }^{\dagger}$ <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel ${ }^{2}$ | $\begin{array}{ll} 24 & (2.5) \\ 24 & (1.9) \\ 25 & (1.6) \\ 19 & (2.0) \\ 21 & (1.5) \end{array}$ | $\begin{array}{ll} 26 & (2.4) \\ 26 & (1.8) \\ 25 & (1.7) \\ 29 & (2.2) \\ 29 & (1.7) \end{array}$ | $\triangle$ | $\begin{array}{ll} 50 & (2.9) \\ 48 & (2.2) \\ 49 & (2.1) \\ 43 & (2.5) \\ 47 & (2.0) \end{array}$ | $\begin{array}{ll} 50 & (3.1) \\ 52 & (2.1) \\ 52 & (2.1) \\ 55 & (2.5) \\ 53 & (2.2) \end{array}$ |  |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) ${ }^{1}$ | $\begin{array}{ll} 23 & (1.8) \\ 23 & (1.3) \\ 24 & (1.7) \\ 24 & (1.1) \\ 24 & (1.9) \end{array}$ | $\begin{aligned} & 28 \text { (1.7) } \\ & 27(1.1) \\ & 26(2.1) \\ & 26(1.0) \\ & 27(2.1) \end{aligned}$ |  | 47 (2.2) <br> 47 (1.5) <br> 51 (2.0) <br> 48 (1.5) <br> 49 (2.2) | $\begin{array}{ll} 53 & (2.2) \\ 53 & (1.3) \\ 49 & (2.2) \\ 52 & (1.3) \\ 52 & (2.2) \end{array}$ |  |
| Lithuania ${ }^{1 \ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{ll} 24 & (2.5) \\ 26 & (1.8) \\ 26 & (2.3) \\ 24 & (1.6) \\ 21 & (1.7) \end{array}$ | $\begin{array}{ll} 26 & (2.3) \\ 24 & (1.6) \\ 24 & (2.9) \\ 27 & (2.1) \\ 28 & (1.5) \end{array}$ |  | 50 (2.5) <br> 51 (2.4) <br> 52 (2.6) <br> 50 (2.1) <br> 45 (2.2) | $\begin{array}{ll} 50 & (2.5) \\ 49 & (2.0) \\ 48 & (3.4) \\ 51 & (2.2) \\ 54 & (1.7) \end{array}$ |  |
| Netherlands ${ }^{\dagger}$ New Zealand Philippines Romania Russian Federation | $\begin{array}{ll} 24 & (3.6) \\ 26 & (2.6) \\ 27 & (2.7) \\ 25 & (2.3) \\ 24 & (2.4) \end{array}$ | 26 (3.2) <br> 24 (3.5) <br> 23 (2.5) <br> 25 (2.4) <br> 26 (2.5) |  | 48 (4.2) <br> 52 (3.0) <br> 53 (2.7) <br> 51 (2.8) <br> 49 (2.9) | 52 (4.4) <br> 48 (3.5) <br> 46 (2.5) <br> 49 (2.8) <br> 51 (3.2) |  |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{ll} 23 & (3.1) \\ 23 & (2.0) \\ 24 & (1.6) \\ 23 & (2.7) \\ 25 & (2.6) \end{array}$ | $\begin{array}{ll} 26 & (3.4) \\ 27 & (2.2) \\ 26 & (1.5) \\ 27 & (2.3) \\ 24 & (2.4) \end{array}$ |  | 49 (3.6) 48 (2.6) 49 (1.7) 47 (2.5) 50 (2.9) | $\begin{array}{ll} 51 & (4.2) \\ 52 & (2.7) \\ 51 & (2.0) \\ 53 & (2.1) \\ 50 & (2.7) \end{array}$ |  |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 19 \\ & 25 \\ & 25 \\ & 23 \\ & 23 \\ & (1.4) \\ & \hline \end{aligned}$ | $\begin{array}{ll} 31 & (1.6) \\ 25 & (1.9) \\ 27 & (1.9) \end{array}$ | - | $\begin{aligned} & 42(1.7) \\ & 50(2.2) \\ & 49(2.0) \end{aligned}$ | $\begin{aligned} & 59(1.6) \\ & 50(1.8) \\ & 51(2.3) \end{aligned}$ | $\triangle$ |
| International Avg. | 23 (0.4) | 27 (0.4) | $\triangle$ | 49 (0.4) | 51 (0.4) | - |

Significantly greater percentage than other gender
Significance tests adjusted for multiple comparisons
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations. Trends in gender data for Bulgaria are unavailable.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


|  | 1995 |  |  | 1999 |  |  | Change in Gender Difference* |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girls <br> Average Scale Score | Boys Average Scale Score | Difference (Absolute Value) | Girls <br> Average Scale Score | Boys Average Scale Score | Difference (Absolute Value) |  |
| Australia | 520 (4.3) | 517 (5.0) | 3 (5.3) | 524 (5.7) | 526 (5.7) | 2 (6.0) | $\Leftrightarrow$ |
| Belgium (Flemish) | 553 (8.1) | 547 (8.7) | 6 (12.2) | 560 (7.2) | 556 (8.3) | 4 (14.2) | 4 |
| Canada | 522 (2.4) | 520 (3.0) | 2 (3.2) | 529 (2.5) | 533 (3.2) | 3 (2.9) | 4 |
| Cyprus | 471 (2.6) | 465 (3.3) | 7 (3.9) | 479 (2.1) | 474 (2.7) | 4 (3.3) | 4 |
| Czech Republic | 539 (5.4) | 552 (4.6) - | 14 (3.9) | 512 (4.0) | 528 (5.8) - | 17 (5.0) | $\Leftrightarrow$ |
| England | 495 (4.0) | 500 (5.5) | 6 (7.7) | 487 (5.4) | 505 (5.0) | 19 (6.5) | $\square$ |
| Hong Kong, SAR | 559 (7.0) | 577 (7.2) | 17 (7.7) | 583 (4.7) | 581 (5.9) | 2 (6.5) | $\Leftrightarrow$ |
| Hungary | 527 (3.6) | 527 (3.6) | 0 (3.5) | 529 (4.0) | 535 (4.3) | 6 (3.7) | $\Leftrightarrow$ |
| Iran, Islamic Rep. | 405 (6.1) | 429 (4.7) - | 24 (7.8) | 408 (4.2) | 432 (4.8) $\boldsymbol{\wedge}$ | 24 (6.5) | , |
| Italy | 488 (4.5) | 494 (3.7) | 5 (4.8) | 483 (5.5) | 488 (5.4) | 5 (4.8) | $\Leftrightarrow$ |
| Japan | 577 (1.9) | 585 (2.2) ^ | 8 (2.7) | 575 (2.4) | 582 (2.3) | 8 (3.3) | - |
| Korea, Rep. of | 571 (3.0) | 588 (2.7) - | 17 (4.2) | 585 (3.1) | 590 (2.2) | 5 (3.7) | צ1 |
| Latvia (LSS) | 486 (4.0) | 490 (4.2) | 4 (4.0) | 502 (3.8) | 508 (4.4) | 5 (4.5) | $\stackrel{\square}{\square}$ |
| Lithuania | 472 (4.6) | 472 (4.6) | 0 (4.1) | 480 (4.7) | 483 (4.8) | 3 (4.0) | 4 |
| Netherlands | 522 (6.6) | 534 (6.6) ^ | 12 (3.9) | 538 (7.6) | 542 (7.0) | 5 (3.0) | $\Leftrightarrow$ |
| New Zealand | 497 (5.3) | 505 (6.1) | 8 (6.6) | 495 (5.5) | 487 (7.6) | 7 (8.3) | $\beta$ |
| Romania | 473 (4.4) | 475 (5.3) | 2 (3.4) | 475 (6.3) | 470 (6.2) | 5 (4.7) | 4 |
| Russian Federation | 524 (5.0) | 523 (6.2) | 1 (3.5) | 526 (6.0) | 526 (6.4) | 1 (3.3) | $\square$ |
| Singapore | 610 (4.9) | 608 (4.7) | 2 (5.3) | 603 (6.1) | 606 (7.5) | 2 (5.7) | $\cdots$ |
| Slovak Republic | 532 (3.1) | 536 (3.7) | 3 (3.1) | 532 (4.2) | 536 (4.5) | 5 (3.6) | $\Leftrightarrow$ |
| Slovenia | 527 (3.2) | 535 (3.1) | 8 (3.0) | 529 (3.0) | 531 (3.6) | 1 (3.6) | - |
| United States | 490 (4.7) | 495 (5.2) | 5 (3.1) | 498 (3.9) | 505 (4.8) | 7 (3.4) | $\cdots$ |
| International Avg. § | 516 (1.0) | 522 (1.1) $\boldsymbol{\wedge}$ | 6 (1.1) | 520 (1.0) | 524 (1.1) | 5 (1.2) | $\Leftrightarrow$ |
| Countries with Unapproved Sampling Procedures at the Classroom Level in 1995 |  |  |  |  |  |  |  |
| Israel | 500 (7.0) | 530 (6.9) - | 29 (5.8) | 473 (5.1) | 490 (5.3) $\boldsymbol{\wedge}$ | 17 (4.7) | $\Leftrightarrow$ |
| South Africa | 264 (8.4) | 293 (12.7) | 29 (10.9) | 267 (7.5) | 283 (7.3) | 16 (5.9) | - |
| Thailand | 520 (7.4) | 511 (6.1) | 9 (7.0) | 469 (5.7) | 465 (5.5) | 4 (4.9) | - |
|  |  |  |  |  |  | Increased | $\cdots$ |
|  | - Significantly higher than other gender |  |  |  |  | Decreased | $\pm$ |
|  |  |  |  |  |  | No change | $\Leftrightarrow$ |
|  | Significance tests adjusted for multiple comparisons |  |  |  |  |  |  |

* Indicates whether 1999 gender difference is significantly different than 1995 gender difference.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian-Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations. Trends in gender data for Bulgaria are unavailable.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


## CHAPTER 2

## Performance at

 International BenchmarksThe timss 1999 international benchmarks delineate performance of the top 10 percent, top quarter, top half, and lower quarter of students in the countries participating in the study. To help interpret the achievement results, Chapter 2 describes eighth-grade mathematics achievement at each of these benchmarks together with examples of the types of items typically answered correctly by students performing at the benchmark.
$2$


As countries around the world spend their time and energy on improving mathematics education, it is important that educators, curriculum developers, and policy makers understand what students know and can do in mathematics and what areas, concepts, and topics need more focus and effort. To help interpret the overall achievement results presented in Chapter 1, this chapter describes eighth-grade mathematics achievement at each of the timss 1999 international benchmarks together with examples of the types of items typically answered correctly by students performing at the benchmark.

Exhibit 1.6, presented previously in Chapter 1, shows the percentages of students in each country reaching each international benchmark Top 10\%, Upper Quarter, Median, and Lower Quarter. The benchmarks delineate performance of the top 10 percent, top quarter, top half, and lower quarter of students in the countries participating in timss 1999 (goth, $75^{\text {th }}, 5$ oth, and $25^{\text {th }}$ international percentiles, respectively). The analysis of performance at these benchmarks in mathematics suggests that three primary factors appeared to differentiate performance among the four levels:

- The mathematical operation required
- The complexity of the numbers or number system
- The nature of the problem situation.

For example, there is evidence that students performing at the lower end of the scale could add, subtract, and multiply whole numbers. In contrast, students performing at the higher end of the scale solved non-routine problems involving relationships among fractions, decimals, and percents; various geometric properties; and algebraic rules.

## How Were the Benchmark Descriptions Developed?

To develop descriptions of achievement at the timss 1999 international benchmarks, the International Study Center used the scale anchoring method. Scale anchoring is a way of describing students' performance at different points on the TIMSS 1999 achievement scale in terms of the types of items they answer correctly. It involves an empirical component in which items that discriminate between successive points on the scale are identified, and a judgmental component in which subject matter experts examine the content of the items and generalize to students' knowledge and understandings.

For the scale anchoring analysis, the results of students from all the timss 1999 countries were pooled, so that the benchmark descriptions refer to all students achieving at that level. (That is, it does not matter which country the students are from, only how they performed on the test.) Criteria were applied to the timss 1999 achievement scale results to identify the sets of items that students reaching each international benchmark were likely to answer correctly and that those at the next lower benchmark were unlikely to answer correctly. ${ }^{1}$ The sets of items produced by the analysis represented the accomplishments of students reaching each successively higher benchmark, and were used by a panel of subject-matter experts from the timss countries to develop the benchmark descriptions. ${ }^{2}$ The work of the panel involved developing a short description for each item of the mathematical understandings demonstrated by students answering it correctly, summarizing students' knowledge and understanding across the set of items for each benchmark to provide more general statements of achievement, and selecting example items illustrating the descriptions.

## How Should the Descriptions Be Interpreted?

In general, the parts of the descriptions that relate to the mathematical concepts or familiarity with procedures are relatively straightforward. It needs to be acknowledged, however, that the cognitive behavior necessary to answer some items correctly may vary according to students' experience. An item may require only simple recall for a student familiar with the item's content and context, but necessitate problem-solving strategies from a student unfamiliar with the material. Nevertheless, the descriptions are based on what the panel believed to be the way the great majority of eighth-grade students could be expected to perform when responding to the item.

It also needs to be emphasized that the descriptions of achievement characteristic of students at the international benchmarks are based solely on student performance on the timss 1999 items. Since those items were developed in particular to sample the mathematics domains prescribed for this study, neither the set of items nor the descriptions based on them purport to be comprehensive. There are undoubtedly other mathematics curriculum elements on which students at the various benchmarks would have been successful if they had been included in the assessment.

[^12]Please note that students reaching a particular benchmark demonstrated the knowledge and understandings characterizing that benchmark as well as the competencies of students at the lower benchmarks. The description of achievement at each higher benchmark is cumulative, building on the description of achievement demonstrated by students at the next lower benchmark.

Finally, it must be emphasized that the descriptions of the international benchmarks are provided as one possible way of beginning to examine student performance. Some students scoring below a benchmark may indeed know or understand some of the concepts that characterize a higher level. Thus, it is important to consider performance on the individual items and clusters of items in developing a profile of student achievement in each country.

Several example items are included for each benchmark to complement the descriptions by giving a more concrete notion of the abilities students were able to demonstrate. Each example item is accompanied by the percentage of correct responses for each country as well as the international average. In general, the five or six countries scoring highest on the overall test also scored highest on each of the items used to illustrate benchmarks. Likewise, the five or six countries with the lowest mean achievement also tended to have consistently low percentages of correct responses on the illustrative items. Not surprisingly, this was true for items assessing a range of performance expectations - recall, ability to carry out routine procedures, and ability to solve routine and non-routine problems. The timss 1999 results support the premise that successful problem solving is grounded in mastery of more fundamental knowledge and skills.

## Item Examples and Student Performance

The remainder of this chapter describes each benchmark and presents three to five example items illustrating what students know and can do at that level. For each example item, the percent correct for each of the timss 1999 countries is displayed, as well as the international average. The correct answer is circled for multiple-choice items. For open-ended items, the answers shown exemplify the types of student responses that were given full credit. The example items are ones that students reaching each benchmark were likely to answer correctly, and they represent the types of items used to develop the description of achievement at that benchmark. ${ }^{3}$

[^13]
## Achievement at the Top 10\% Benchmark

"
Exhibit 2.1 describes performance at the Top $10 \%$ Benchmark. Students reaching this benchmark demonstrated the ability to organize information in problem-solving situations and to apply their understanding of mathematical relationships. They typically demonstrated success on the knowledge and skills represented by this benchmark, as well as those demonstrated at the Upper Quarter, Median, and Lower Quarter benchmarks.

Example Item 1 in Exhibit 2.2 illustrates the type of measurement item a student performing at the Top $10 \%$ Benchmark generally answered correctly. As can be seen, students had to apply their knowledge of the area of rectangles and inscribed shapes to solve a two-step problem about the area of a garden path. The international average for this item was 42 percent correct. Nevertheless, more than two-thirds of the students answered the item correctly in Hong Kong, Singapore, Japan, Chinese Taipei, and Korea. On average internationally, more than 20 percent of students chose Option A, solving for the area of the larger rectangle rather than that of the path. Option C was an equally popular distracter, with more than 20 percent of students internationally selecting this response.

Unlike students performing at lower benchmarks, students reaching the Top $10 \%$ Benchmark typically could correctly answer multi-step word problems. Example Item 2 in Exhibit 2.3 requires students to select relevant information from two advertisements to solve a complex multi-step word problem involving decimals. Given the price for each issue of a magazine and a certain number of free issues, students were asked to calculate which of the two magazine subscriptions was the less expensive for 24 issues. Students received full credit if they showed correct calculations for at least one of the subscriptions, identified the less expensive magazine, and calculated the difference between the two subscriptions. With an international average of 24 percent correct (for full credit), this item was among the most difficult in timss 1999. Singapore, Korea, and Chinese Taipei were the only countries where the majority of the students answered the item correctly.

Students reaching the Top $10 \%$ Benchmark exhibited an understanding of the properties of similar triangles, as shown by Example Item 3 (see Exhibit 2.4). Given two angle measurements, the length of a side of a triangle, and the dimensions of a second similar triangle, students needed to find the length of an unlabeled side of the first triangle.
Internationally, most eighth-grade students had not mastered the concept of proportionality of corresponding sides, or could not solve the resulting

# Exhibit 2.1 Description of Top 10\% TIMSS International Benchmark of Mathematics Achievement 

Mathematics

## - Top 10\% Benchmark


#### Abstract

Summary Students can organize information, make generalizations, and explain solution strategies in nonroutine problem solving situations. They can organize information and make generalizations to solve problems; apply knowledge of numeric, geometric, and algebraic relationships to solve problems (e.g., among fractions, decimals, and percents; geometric properties; and algebraic rules); and find the equivalent forms of algebraic expressions.


Students can organize information in problem-solving situations. They can select and organize information from two sources to solve a complex word problem involving decimals and organize information to solve a multi-step word problem involving whole numbers.

Students can correctly order the four basic operations in computing with decimals and fractions. Students use their understanding of fractions and decimals in multi-step problem situations. They can solve a problem involving both addition and subtraction of simple common fractions and a problem involving multiplication and subtraction of decimals. They can solve word problems involving fractions and decimals which require analysis of the verbal relations described. They can order a set of decimal fractions of up to three decimal places and can identify the pair of numbers satisfying given conditions involving ordering integers, decimals, and fractions. They can solve a time-distance-rate problem involving decimals and the conversion of minutes to seconds. They can work with part-whole ratios and can solve word problems to find the percent change.

Students can apply their knowledge of measurement in more complex problem situations. They can solve problems involving area and perimeter of rectangles and area of inscribed triangles. They apply knowledge of properties of squares to solve multi-step word problems and draw a new rectangle based on a given rectangle and express the ratio of their areas. They can relate different units of time and apply their knowledge of the number of milliliters in a liter to solve a word problem. They recognize that precision of measurement is related to the size of the unit of measurement.

Students can use their knowledge of angles - overlapping and measures of angles in quadrilaterals - to solve problems. They can use their knowledge of congruent and similar triangles to solve problems concerning corresponding parts. They can identify the coordinates of a point on a line given the coordinates of two other points on the line and locate a point on a number line given its distance from two other points on the line. They can identify the image of a triangle under a rotation in a plane.

Students can use proportion to find missing values in a table. Students can identify an equivalent form of a linear inequality involving a fraction. Students can recognize properties of number operations represented in symbolic form. They can solve a multi-step word problem in which there are two unknowns.

Given the first several terms in pictorial form, that grow in either one or two dimensions, students can make generalizations to find terms in the sequences (e.g. 51st), and they can explain the process used to find those terms.
equation, with only 37 percent, on average, answering the question correctly. In comparison, top-performing Korea had 70 percent correct responses. Only in Korea, Japan, Singapore, Hong Kong, Chinese Taipei, and Belgium (Flemish) did at least half the students provide the correct solution.

The eighth-grade students reaching the Top $10 \%$ Benchmark typically were able to apply a generalization in order to solve a sequence problem like the one shown in Exhibit 2.5. In this algebra problem, given the initial terms in a sequence and the 50th term of that sequence, they generalized to find the $5^{1 \text { st }}$ term. This problem was presented in three parts, A, B, and C. For parts A and B, students were asked to indicate how many circles would be in the 5 th and 7 th figures, respectively, if the pattern were extended. On average internationally, $6_{5}$ percent of the students answered Part A correctly and 54 percent successfully extended the sequence to the 7 th figure in Part B.

To receive full credit for Part C, students had to show or explain how their answer was obtained by providing a general expression or an equation and by calculating the correct number of circles for the 51 st figure. Internationally, on average, 30 percent of the students received full credit for their responses. Most of them added the sequence number to the number of circles in the preceding figure: $1275+5^{1}=1326$. Less than three percent of the students internationally calculated the answer by a general expression: $n(n+1) / 2$ or $5^{1(52) / 2}$. About 13 percent of the students in the Netherlands and Moldova received full credit by calculating their answer using the latter method. In 10 countries, $1_{5}$ percent or less of the students answered Part C of the item correctly. Still, about twothirds of the students in Korea, Chinese Taipei, Japan, and Singapore received full credit for their responses. It seems worthwhile to note that many students internationally ( 33 percent) left the item blank, whereas in the four top-performing countries on this item only six to 12 percent of the students did not attempt the item.


Exhibits 2.2-2.5 Overleaf

## Exhibit 2.2 Top 10\% TIMSS International Benchmark - Example Item 1

An Item That Students Reaching the Top 10\% International Benchmark Are Likely to Answer Correctly*


| Hong Kong, SAR ${ }^{\dagger}$ | Overall <br> Percent <br> Correct |  |
| :---: | :---: | :---: |
|  | 79 (2.0) | - |
| Singapore | 78 (2.6) | $\triangle$ |
| Japan | 74 (1.9) | $\triangle$ |
| Chinese Taipei | 73 (2.1) | - |
| Korea, Rep. of | 67 (1.7) | $\triangle$ |
| Netherlands ${ }^{\text {+ }}$ | 57 (4.4) | - |
| Australia | 52 (2.6) | $\triangle$ |
| Malaysia | 52 (2.1) | - |
| Slovak Republic | 51 (3.3) | - |
| Canada | 51 (3.0) | - |
| Belgium (Flemish) ${ }^{\dagger}$ | 51 (2.2) | - |
| Finland | 46 (3.0) |  |
| Hungary | 46 (2.7) | - |
| Slovenia | 46 (3.2) | - |
| Cyprus | 45 (3.0) | - |
| Italy | 45 (2.7) |  |
| Bulgaria | 42 (3.4) |  |
| International Avg. | 42 (0.4) |  |
| Czech Republic | 40 (3.5) |  |
| England ${ }^{+}$ | 40 (3.3) | - |
| New Zealand | 40 (2.6) | - |
| Tunisia | 38 (2.0) |  |
| Russian Federation | 38 (3.2) | - |
| Thailand | 35 (2.1) |  |
| Moldova | 34 (2.7) | - |
| United States | 33 (1.6) | $\nabla$ |
| Morocco | 31 (2.1) |  |
| Lithuania ${ }^{\text {¹ }}$ | 31 (3.0) |  |
| Macedonia, Rep. of | 30 (2.5) | $\checkmark$ |
| Romania | 29 (2.6) | $\nabla$ |
| Jordan | 29 (2.3) | $\nabla$ |
| - Israel ${ }^{2}$ | 28 (2.1) | $\nabla$ |
| Latvia (LSS) ${ }^{1}$ | 28 (2.5) | $\checkmark$ |
| Iran, Islamic Rep. | 26 (2.1) | $\nabla$ |
| Indonesia | 25 (2.0) | $\nabla$ |
| Turkey | 22 (1.6) | $\nabla$ |
| Chile | 18 (1.6) | V |
| Philippines | 15 (1.2) | $\nabla$ |
| South Africa | 15 (1.2) | $\checkmark$ |

SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1998-1999.

* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent


## Exhibit 2.3 Top 10\% TIMSS International Benchmark - Example Item 2

An Item That Students Reaching the Top 10\% International Benchmark Are Likely to Answer Correctly*


Which magazine is the least expensive for 24 issues? How much less expensive? Show your work.


Teen Life is less expensive by 3 ceds.


* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

## Exhibit 2.4 Top 10\% TIMSS International Benchmark - Example Item 3

An Item That Students Reaching the Top 10\% International Benchmark Are Likely to Answer Correctly*


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\square$
$\square$
$\square$
$\square$
$\square$
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

Internationally comparable data are unavailable for Morocco.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
$\square$
$\square$


## Exhibit 2.5 Top 10\% TIMSS International Benchmark - Example Item 4

An Item That Students Reaching the Top 10\% International Benchmark Are Likely to Answer Correctly*


Figure 1


Figure 2


Figure 3


Figure 4
a) Complete the table below. First, fill in how many circles make up Figure 4.

Then, find the number of circles that would be needed for the 5th figure if the sequence of figures is extended.

| Figure | Number of <br> circles |
| :---: | :---: |
| 1 | 1 |
| 2 | 3 |
| 3 | 6 |
| 4 | 10 |
| 5 | 015 |

b) The sequence of figures is extended to the 7 th figure. How many circles would be needed for Figure 7?

Answer:

c) The 50th figure in the sequence contains 1275 circles. Determine the number of circles in the 51st figure. Without drawing the 51st figure, explain, or show how you arrived at your answer.


1275


The answer shown illustrates the type of student response that was given full credit.

[^14]2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

## Achievement at the Upper Quarter Benchmark

"
Exhibit 2.6 describes performance at the Upper Quarter Benchmark. Eighth-grade students performing at this level applied their mathematical knowledge and understanding in a wide variety of relatively complex problem situations. For example, they demonstrated facility with fractions in a variety of formats, as illustrated by Example Item 5 shown in Exhibit 2.7. This item required students to shade squares in a rectangular grid to represent a given fraction. Since the grid is divided into squares that are a multiple of the fraction's denominator, it requires more than one step to solve the problem. Internationally, about half of the students ( 49 percent on average) were able to shade in nine of the 24 squares to represent $3 / 8$ of the region. Eighty percent or more of the students in Singapore, Hong Kong, Belgium (Flemish), Korea, and Chinese Taipei answered the question correctly.

Example Item 6 is a proportional reasoning word problem that students at the Upper Quarter Benchmark typically answered correctly (see Exhibit 2.8). Given the number of magazines sold by each of two boys and the total amount of money made from the sales, students were to calculate how much money one of the boys made by selling his 8o magazines. On average, 44 percent of students internationally answered this question correctly. In Singapore and Chinese Taipei at least three-quarters of the students answered correctly.

Students reaching the Upper Quarter Benchmark generally were able to apply knowledge of geometric properties. In Example Item 7 in Exhibit 2.9, students needed to use their knowledge of the properties of parallelograms and rectangles to solve for the area of the rectangle (dimensions not labeled) that was part of a different figure with given dimensions. Three-quarters or more of the students in Singapore, Japan, Hong Kong, Korea, and Chinese Taipei answered the item correctly. Internationally, however, less than half the eighth-grade students (43 percent on average) did so.

Exhibit 2.10 presents Example Item 8 asking for the number of triangles of a given dimension needed to cover a rectangle of given dimensions. The international average on this item was 46 percent correct. Many students (approximately 29 percent internationally) incorrectly chose Option A, which is half the number of required triangles needed to fill the rectangle but just enough to cover the perimeter. Japanese students

# Exhibit 2.6 Description of Upper Quarter TIMSS International Benchmark of Mathematics Achievement 

Mathematics

## - Upper Quarter Benchmark


#### Abstract

Summary Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They can order, relate and compute with fractions and decimals to solve word problems; solve multi-step word problems involving proportions with whole numbers; solve probability problems; use knowledge of geometric properties to solve problems; identify and evaluate algebraic expressions and solve equations with one variable.


Students demonstrate some facility with fractions and decimals through computation, ordering, rounding, and use in word problems. They can recognize equivalent fractions, add, subtract, multiply and divide fractions with unlike denominators, and correctly order operations. They can identify the smallest decimal from a set of decimals with differing number of places and provide a fraction that is less than a given fraction. They can solve word problems involving multiplication and division of whole numbers and fractions and use pictorial representations of fractions in solving problems. They can identify the fraction of an hour representing a given time interval and identify fractions representing the comparison of part to whole, given each of two parts in a word problem setting.

Students can select the correct rounding of a number involving four decimal places, identify the decimal that is between two decimals given in hundredths, and solve a word problem that involves multiplying a decimal in thousandths by a multiple of a hundred. They can produce an example of a number that would round to a given value. Given a length rounded to the nearest centimeter, they can identify an example of the actual length expressed to one decimal place. Students can identify the ratio expressing a given whole number comparison in a word problem and recognize the effect of adding the same amount to both terms of a ratio. They can estimate products of whole numbers to solve problems. They can solve multi-step word problems involving proportions with whole numbers.

Students demonstrate their understanding of measurement in several settings. They can compare volumes by visualizing and counting cubes. They can calculate the areas of rectangles contained in diagrams of combined shapes. Given the start time and the duration of an event expressed as a fraction of an hour, they can determine the end time. They can estimate the distance between two points on a map, given the scale, and can read unlabeled tick marks on a scale.

Students can use basic properties of triangles, properties of angles on a straight line, and knowledge of symmetry to find the measures of angles. They can identify the angle in a diagram that represents the best estimate of a given measure and recognize that internal angles on a transversal are supplementary. They can visualize the center of a rotation for a two-dimensional figure, the arrangement of faces of a cube when shown its net, and the number of triangles of given dimensions needed to cover a given rectangle. They can identify false statements about congruent triangles and the properties of rectangles.

Students understand elementary concepts of probability, including independent events. They can solve simple problems involving the relationship between successful and unsuccessful outcomes and probabilities. They also recognize that when outcomes are expressed as fractions of a whole, the least likely outcome corresponds to the smallest fraction. They can extrapolate from a graph and determine the number of values on the horizontal axis of a line graph that correspond to a given value on the vertical axis. On a given graph, students can interpolate to find a value between gradations on one axis matching a given value on the other axis.

Students can recognize that multiplication can represent repeated addition. They can identify the algebraic equation corresponding to a verbal description. They can select a simple, multiplicative expression in one variable that is positive for all negative values of the variable. They can substitute numbers for variables to evaluate an expression, and subtract fractions represented algebraically with the same numeric denominator.

Students can solve a linear equation with or without parentheses. They can identify the linear equation that describes the relationship between two variables given in a table of values and select the formula satisfied by the given values of the variables. They can identify the relationship between the first and second terms in a set of ordered pairs.

Given the first several terms of a sequence in pictorial form, growing in either one or two dimensions, they can find specified terms to extend the sequence.
had the highest performance on this item, with 8o percent answering correctly. About two-thirds or more of the students answered the item correctly in Korea, Hong Kong, Singapore, Belgium (Flemish), and the Netherlands.

Unlike students at lower benchmarks, students reaching the Upper Quarter level typically could solve simple linear equations. As illustrated by Example Item 9 in Exhibit 2.11, for example, students successfully solved for the value of $x$ in a linear equation involving the variable on both sides of the equation. Eighty percent or more of the students in Japan, Hong Kong, and Korea answered this item correctly. On average internationally, 44 percent of students responded correctly.


Exhibits 2.7-2.11 Overleaf


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
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$\square$
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$\square$


## Exhibit 2.8 Upper Quarter TIMSS International Benchmark - Example Item 6

An Item That Students Reaching the Upper Quarter International Benchmark Are Likely to Answer Correctly*
TIMSS1999
$\overbrace{\text { grade }}^{\text {th }}$
Mathematics


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.9 Upper Quarter TIMSS International Benchmark - Example Item 7

An Item That Students Reaching the Upper Quarter International Benchmark Are Likely to Answer Correctly*

## Content Area: Measurement <br> Description: Finds the area of a rectangle contained in a parallelogram of given dimensions.

The figure shows a shaded rectangle inside a parallelogram.


What is the area of the shaded rectangle?

Answer:


* The item was answered correctly by a majority of students reaching this benchmark.
${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
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$\square$

## Exhibit 2.10 Upper Quarter TIMSS International Benchmark - Example Item 8

An Item That Students Reaching the Upper Quarter International Benchmark Are Likely to Answer Correctly*


The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.11 Upper Quarter TIMSS International Benchmark - Example Item 9

An Item That Students Reaching the Upper Quarter International Benchmark Are Likely to Answer Correctly*


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
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$\square$
$\square$
$\square$



## Achievement at the Median Benchmark

### 2.12-2.13 <br> T

Students at the Median Benchmark demonstrated the ability to apply basic mathematical knowledge in straightforward situations (see Exhibit 2.12). For example, as shown by Example Item 10 in Exhibit 2.13 , students showed that they understand rounding and can use it to estimate the results of computations. Given the number of rows of cars in a parking lot and the number of cars in each row, students chose the number sentence that would give the best estimate of the total number of cars. While students at the Lower Quarter Benchmark rounded to the nearest hundred, students at the Median Benchmark successfully rounded numbers to get the best estimate for a product. Moreover, middle-performing students demonstrated greater competence with word problems than did those at the Lower Quarter Benchmark. The international average percent correct for this item was 65 percent. Singapore outperformed other countries with 94 percent correct, followed by $8_{5}$ percent in Hong Kong.

In geometry, students at the Median Benchmark were able to locate a point on a grid with five-unit divisions where the point lies between the grid lines (see Example Item 11 in Exhibit 2.14). Fifty-eight percent of the students on average internationally correctly chose Point $S$ as the point on the grid that could have the coordinates $(7,16)$. In Japan, Korea, Chinese Taipei, Hong Kong and Singapore, 8o percent or more of the students answered correctly. As might be anticipated, students answering incorrectly most commonly chose Point $Q(16,7)$.
$2.15 \square$
Example Item 12 shown in Exhibit 2.15 illustrates students' emerging familiarity with algebraic representation. Internationally on average, nearly two-thirds of the students correctly identified the linear equation corresponding to a given verbal statement involving a variable. In Hong Kong, Singapore, Japan, and Korea, $8_{5}$ percent or more of the students answered correctly.

# Exhibit 2.12 Description of Median TIMSS International Benchmark of Mathematics Achievement 

## Median Benchmark


#### Abstract

Summary Students can apply basic mathematical knowledge in straightforward situations. They can add or subtract to solve one-step word problems involving whole numbers and decimals; identify representations of common fractions and relative sizes of fractions; solve for missing terms in proportions; recognize basic notions of percents and probability; use basic properties of geometric figures; read and interpret graphs, tables, and scales; and understand simple algebraic relationships.


Students can apply basic mathematical knowledge in straightforward situations. They are able to use addition and subtraction to solve one-step word problems involving whole numbers and decimals. They can round whole numbers to the nearest hundred and identify the number sentence that gives the best estimate for the product of two numbers after rounding. Students can arrange four given digits in descending and ascending order to form the largest and smallest possible numbers, and find the difference between those two numbers. Students can approximate the quantity remaining after an amount is reduced by a given percent.

Students demonstrate an understanding of place value in decimal numbers. They can estimate the location of a point representing a decimal number in tenths on a number line marked in whole numbers and identify an unlabeled midway point on a number line marked in tenths. They can set up and solve one-step problems involving addition and subtraction of numbers having up to three decimal places, including situations where the numbers have a different number of decimal places. Given an object of one length, to one decimal place, they can estimate the length of another object.

Students can select the smallest fraction from a list of fractions and can recognize models representing fractions as shaded regions. They can find the missing term in a proportion in word problems and number sentences. Students can solve a simple word problem involving the likelihood of a successful outcome.

Students are able to select the appropriate metric unit to measure the mass of an object. They recognize the inverse relationship between the length of a unit and the number of units required to cover a distance.

Students can locate and interpret data presented in bar graphs, pictographs, pie graphs, and line graphs. Given a table of values for two variables, they can select the graph that represents the given data.

Students can solve problems involving the properties of congruent figures and can select a pair of similar triangles from a set of triangles. They can visualize a rotation of a three-dimensional figure made of cubes. They can locate points in the first quadrant of the Cartesian plane.

Students can select an expression to represent a situation involving multiplication, and identify a linear equation corresponding to a verbal statement. They can find a missing value in a table of values relating $x$ and $y$ values. Using the properties of a balance, they can reason to find an unknown weight. Given diagrams representing the first few terms of a sequence, growing in one dimension, and a partially completed table, they can find the next two terms.

## Exhibit 2.13 Median TIMSS International Benchmark - Example Item 10

An Item That Students Reaching the Median International Benchmark Are Likely to Answer Correctly*
TIMSS 1999

## Content Area: Fractions and Number Sense <br> Description: In a word problem, uses rounding to identify the number sentence that gives the best estimate for the product.

There are 68 rows of cars in a parking lot. Each row has 92 cars. Which of these would give the closest estimate of the total number of cars in the parking lot?
A. $60 \times 90=5400$
B. $60 \times 100=6000$
(C.) $70 \times 90=6300$


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
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$\square$
$\square$
$\square$


## Exhibit 2.14 Median TIMSS International Benchmark - Example Item 11

An Item That Students Reaching the Median International Benchmark Are Likely to Answer Correctly*


* The item was answered correctly by a majority of students reaching this benchmark.

Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.15 Median TIMSS International Benchmark - Example Item 12

An Item That Students Reaching the Median International Benchmark Are Likely to Answer Correctly*



* The item was answered correctly by a majority of students reaching this benchmark.
† Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
$\square$

$\square$
$\square$



## Achievement at the Lower Quarter Benchmark

As shown in Exhibit 2.16, the few items anchoring at the Lower Quarter Benchmark provided evidence that students performing at this level can add, subtract, and round with whole numbers. For example, students answering Example Item 13 correctly rounded 691 and 208 to estimate their sum as close to the sum of 700 and 200 (see Exhibit 2.17). The international average was 8 o percent correct, and 27 countries had threequarters or more of their students choosing the correct answer. In four countries - Singapore, Belgium (Flemish), Japan, and the Netherlands 95 percent or more of the students gave the correct response.

As illustrated by Example Item 14 in Exhibit 2.18, students at the Lower Quarter Benchmark generally could subtract one three-decimal-place number from another with multiple regrouping. Internationally on average, 77 percent of the eighth-grade students selected the correct response to this item. Performance ranged from a high of 92 percent correct in Malaysia to a low of 42 percent correct in South Africa.

Similarly, students at this level could subtract one four-digit integer from another involving multiple regrouping with zeroes (see Example Item 15 in Exhibit 2.19). On this subtraction item also, Malaysia had the highest percentage of students answering this item correctly (94 percent) and South Africa the lowest (37 percent).
2.20

In addition, Example Item 16 in Exhibit 2.20 shows that students at this level could read a thermometer and locate the correct reading in a table. There were thirteen countries where at least 90 percent of the students selected the correct response. In only two countries, Turkey and South Africa, did less than 50 percent of the students answer the item correctly.

# Exhibit 2.16 Description of Lower Quarter TIMSS International Benchmark of Mathematics Achievement 

## - Lower Quarter Benchmark

## Summary

Students can do basic computations with whole numbers.

The few items at this level provide some evidence that students can add, subtract, and round with whole numbers. When there are the same number of decimal places, they can subtract with multiple regrouping. Students can round whole numbers to the nearest hundred. They can read a thermometer and locate the reading in a table. Students recognize some basic notation.

## Exhibit 2.17 Lower Quarter TIMSS International Benchmark - Example Item 13

An Item That Students Reaching the Lower Quarter International Benchmark Are Likely to Answer Correctly*


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
$\square$
$\square$
$\square$
$\square$


## Exhibit 2.18 Lower Quarter TIMSS International Benchmark - Example Item 14



* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only

2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 2.19 Lower Quarter TIMSS International Benchmark - Example Item 15
An Item That Students Reaching the Lower Quarter International Benchmark Are Likely to Answer Correctly*

| Country average significantly higher than |
| ---: |
| international average |


| No statistically significant difference between country |
| ---: |
| average and international average |

Country average significantly lower than
international average

[^15]Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

$\square$

$\square$
$\square$


## Exhibit 2.20 Lower Quarter TIMSS International Benchmark - Example Item 16



* The item was answered correctly by a majority of students reaching this benchmark.
† Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).

[^16]
## What Issues Emerge from the Benchmark Descriptions?

The benchmark descriptions and example items strongly suggest a gradation in achievement, from the top-performing students' ability to generalize and solve non-routine or contextualized problems to the lower-performing students being able primarily to use routine, mainly numeric procedures. The fact that even at the Median Benchmark students demonstrate only limited achievement in problem solving beyond straightforward one-step problems may suggest a need to reconsider the role, or priority, of problem solving in mathematics curricula.

In looking across the item-level results, it also is important to note the variation in performance across the topics covered. For example, on just the few items (16) presented in this chapter, there was a substantial range in performance for many countries. While some countries consistently registered high or low performance, and others had results consistently near the international average, 16 countries performed significantly above the international average on at least one item, and significantly below the international average on at least one item (Australia, Bulgaria, Canada, Cyprus, England, Finland, Latvia (Lss), Lithuania, Malaysia, Moldova, the Netherlands, New Zealand, Romania, Thailand, Tunisia, and the United States). For example, Malaysia had the highest percent correct on a subtraction item (Exhibit 2.19) but performed below the international average on an item requiring selection of information to solve a complex word problem (Exhibit 2.3). In some cases, differences of this sort will result from intended differences in emphasis in national curricula. It is likely, however, that such results may be unintended, and the findings will provide important information about strengths and weaknesses in intended or implemented curricula. At the very least, an indepth examination of the timss 1999 results may reveal aspects of curricula that merit further investigation.


## CHAPTER 3

## Average Achievement

 in the Mathematics Content AreasChapter 3 presents results by the major content areas in mathematics to provide information about the possible effects of curricular variation on average achievement. Average performance and trends are provided for five content areas: fractions and number sense; measurement; data representation, analysis, and probability; geometry; and algebra.


The timss 1999 mathematics assessment was designed to allow as fair comparisons as possible among participating countries. ${ }^{1}$ The test measured achievement on content covered in most systems up to and including the eighth grade. Nevertheless, curriculum data collected as part of timss 1995 and timss 1999 indicate differences among countries in the grade level at which particular topics are introduced and in the teaching emphases given some topics. In addition, within countries there can be variation among teachers in the relative emphasis given particular topics. Chapter 3 presents results by major content areas in mathematics to provide information about the possible effects of this curricular variation on average achievement.

The timss 1999 mathematics test for the eighth grade was designed to enable reporting by five content areas in accordance with the timss mathematics framework. ${ }^{2}$ These areas, with their main topics, are:

- Fractions and number sense

Includes whole numbers, fractions and decimals, integers, exponents, estimation and approximation, proportionality

- Measurement

Includes standard and non-standard units, common measures, perimeter, area, volume, estimation of measures

- Data representation, analysis, and probability

Includes representing and interpreting tables, charts, and graphs; range, mean; informal likelihood, simple numerical probability

## - Geometry

Includes points, lines, planes, angles, visualization, triangles, polygons, circles, transformations, symmetry, congruence, similarity, constructions

## - Algebra

Includes number patterns, representation of numerical situations, solving simple linear equations, operations with expressions, representations of relations and functions.

Chapter 3 presents average achievement for the five major content areas covered by the timss 1999 mathematics test. Gender differences in each content area are shown, and trends in achievement between 1995 and 1999 are presented for those countries that participated in both timss assessments.

[^17]
## How Does Achievement Differ Across Mathematics Content Areas?

$3.1 \square$
Exhibit 3.1 presents average achievement in each of the five mathematics content areas. Countries are displayed in decreasing order of achievement for each content area, and symbols indicate whether a country's performance is statistically significantly above or below the international average. To allow comparison of the relative performance of each country in each content area, the international average for each content area was scaled to be $4^{87}$, the same as the overall international average.

Differences in average achievement between the highest- and lowest-performing countries were greatest for fractions and number sense ( 308 scale-score points) and least for data representation, analysis, and probability (220 scale-score points). The six countries scoring highest in the overall mathematics assessment - Singapore, Korea, Chinese Taipei, Hong Kong, Japan, and Belgium (Flemish) - were also the highest-scoring countries (though not always in the same rank order) in each of the major content areas. Correspondingly, countries scoring lowest on the overall test tended to have low average performance across all five content areas.

In contrast to the consistency in performance across content areas displayed by the higher- and lower-performing countries overall, performance varied substantially for some middle-performing countries. For example, the United States performed significantly above the international average in fractions and number sense; data representation, analysis, and probability; and algebra. In contrast, however, it performed similarly to the international average in measurement and geometry (a shift in ranking from 16th in data representation, analysis, and probability to 27 th in geometry).

Exhibits B. 1 through B. 5 in Appendix B compare average achievement among individual countries for each of the content areas, respectively. The exhibits show whether or not the differences in average achievement between pairs of countries are statistically significant.


Exhibit 3.1 Overleaf

## Exhibit 3.1 Average Achievement in Mathematics Content Areas



[^18]



(3)
 -5


## In Which Content Areas Are Countries Relatively Strong or Weak?

Exhibit 3.2 profiles the relative performance in mathematics content areas within each country, highlighting any variation in performance. For each country, Exhibit 9.2 displays the difference between average performance in each content area and average performance overall. The profiles reveal that many countries performed relatively better or worse in several content areas than they did overall. For example, it can be seen that Australia performed better in measurement than on the test as a whole, but worse in geometry.

Differences in relative performance may be related to one or more of a number of factors, such as emphases in intended curricula or widely used textbooks, strengths or weaknesses in curriculum implementation, and the grade level at which topics are introduced. Differences in the match between the implemented curriculum and content measured by the test may also be a factor. ${ }^{3}$

Looking across countries, algebra was the content area least likely to feature either relatively strong or relatively weak performance. Even where there was variation, countries with disparate cultures and mathematical traditions made up both the group of countries relatively strong in algebra (Chinese Taipei, Hungary, Israel, Macedonia, and the United States) and the group that was relatively weak (Finland, the Philippines, and South Africa).

The profiles of relative performance also reveal more variation across the content areas in some countries than in others. Average achievement across content areas showed considerable variation in several countries. For example, in Morocco, the Philippines, and South Africa, differences of approximately two-thirds of a standard deviation between the highest and lowest content area averages occurred. On the other hand, there were only a small number of scale points of difference between highest and lowest content area means for countries such as Belgium (Flemish), Cyprus, Japan, Jordan, Korea, the Slovak Republic, and Turkey. For the latter countries, the data indicate a greater balance in mathematics content covered by the end of the eighth grade.

For some countries, national patterns of relative strengths and weaknesses profiled in Exhibit 3.2 are reflected in strengths and weaknesses relative to other countries (shown in Exhibit 3.1). For example, the Australian results show lower performance in geometry relative to

[^19]other content areas; geometry is also the only content area in which Australia did not perform significantly above the international average. In general, however, the within-country variations are difficult to discern in the results internationally across countries, particularly for countries with high or low performance.


Exhibit 3.2 Overleaf

## Exhibit 3.2 Profiles of Relative Performance in Mathematics Content Areas


$\square$
$\square$ (3)

$\square$


## What Are the Gender Differences in Achievement for the Content Areas?

Exhibit 3.3 displays average achievement in mathematics content areas by gender. The most striking feature of the exhibit is the very small number of statistically significant differences. In geometry and algebra, there were no significant gender differences in average achievement in any country. Across all content areas, there were only five significant differences three in Tunisia, and one apiece in Israel and the United States. Two of the cases occurred in fractions and number sense (Israel and Tunisia), two in measurement (Tunisia and the United States), and one in data representation, analysis, and probability (Tunisia). Only in fractions and number sense and in measurement were there significant differences in the international averages for girls and boys. It is noted, however, that the few significant differences in content area achievement showed boys having significantly higher achievement than girls.

An important stage of item selection for the Timss 1995 and timss 1999 tests was the examination of item statistics to detect items that differentiated between groups, including girls and boys, at the country level. Such items were scrutinized and retained when there was no apparent source of gender bias. It is therefore likely that the absence of significant gender differences in the averages for girls and boys in a country is due partly to a balance between items on which one or the other gender tends to perform better. It is also reasonable to assume that where significant differences do occur, they result from gender differences in one or more of those factors in student backgrounds and schooling that have consistently been found to affect achievement in mathematics.

In spite of there being very few statistically significant differences between average achievement of girls and boys in the content areas, it is interesting to look at the patterns in differences. As highlighted by the differences in international averages, there is a strong tendency across countries for boys to have higher average achievement than girls in fractions and number sense, measurement, and geometry, and to a lesser extent in data representation, analysis, and probability. In algebra, the pattern shows girls with higher averages than boys (in 24 of the 38 countries).

The patterns in the performance of girls and boys found in TIMss 1999 are consistent with previous ieA mathematics assessments. Girls tended to perform better than boys in algebra in both Timss 1995 and the Second International Mathematics Study (SIMs), ${ }^{4}$ while boys were markedly stronger in measurement in previous studies.

[^20]

Exhibit 3.3 Overleaf

## Exhibit 3.3 Average Achievement in Mathematics Content Areas by Gender

|  | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Fractions | ber Sense |  | Measurement |  |  | Data Representation, Analysis, and Probability |  |  |
|  | Girls | Boys |  | Girls | Boys |  | Girls | Boys |  |
| Australia | 515 (4.7) | 523 (5.7) |  | 525 (6.4) | 534 (6.5) |  | 527 (10.6) | 517 (6.2) |  |
| Belgium (Flemish) ${ }^{\dagger}$ | 555 (6.0) | 558 (7.7) |  | 550 (6.5) | 547 (8.2) |  | 549 (6.7) | 539 (8.8) |  |
| Bulgaria | 502 (7.1) | 505 (7.5) |  | 494 (7.5) | 500 (8.3) |  | 493 (6.4) | 492 (7.1) |  |
| Canada | 530 (2.4) | 536 (3.4) |  | 519 (4.6) | 523 (4.4) |  | 520 (5.2) | 522 (6.6) |  |
| Chile | 400 (6.3) | 406 (6.1) |  | 403 (5.6) | 420 (9.6) |  | 426 (4.5) | 431 (5.3) |  |
| Chinese Taipei | 574 (4.9) | 579 (5.2) |  | 563 (3.3) | 569 (5.2) |  | 557 (5.5) | 561 (7.9) |  |
| Cyprus | 478 (3.8) | 483 (3.9) |  | 470 (3.8) | 471 (5.5) |  | 475 (6.1) | 470 (7.5) |  |
| Czech Republic | 498 (5.7) | 517 (6.1) |  | 525 (6.1) | 545 (6.6) |  | 502 (7.0) | 524 (6.9) |  |
| England ${ }^{\dagger}$ | 487 (6.0) | 507 (5.4) |  | 500 (6.4) | 515 (5.4) |  | 498 (6.8) | 513 (10.9) |  |
| Finland | 527 (4.1) | 535 (4.9) |  | 520 (5.5) | 521 (4.8) |  | 524 (5.5) | 526 (6.4) |  |
| Hong Kong, SAR ${ }^{\dagger}$ | 579 (4.5) | 578 (6.1) |  | 567 (5.7) | 567 (7.3) |  | 546 (5.3) | 548 (7.4) |  |
| Hungary | 520 (4.8) | 531 (4.6) |  | 533 (3.7) | 543 (4.3) |  | 514 (7.5) | 527 (6.2) |  |
| Indonesia | 407 (4.6) | 406 (6.1) |  | 394 (6.8) | 396 (4.7) |  | 419 (4.1) | 428 (6.3) |  |
| Iran, Islamic Rep. | 425 (6.8) | 445 (4.9) |  | 385 (6.9) | 411 (7.9) |  | 421 (6.4) | 435 (8.3) |  |
| \|srael ${ }^{2}$ | 463 (4.9) | 482 (5.2) | $\triangle$ | 449 (6.5) | 465 (4.8) |  | 464 (5.9) | 473 (5.1) |  |
| Italy | 463 (6.7) | 479 (4.8) |  | 494 (5.7) | 508 (5.6) |  | 483 (7.3) | 484 (6.2) |  |
| Japan | 563 (3.4) | 576 (4.0) |  | 556 (3.5) | 559 (3.0) |  | 552 (5.5) | 559 (3.8) |  |
| Jordan | 433 (5.3) | 430 (5.5) |  | 437 (7.9) | 439 (7.1) |  | 438 (9.9) | 434 (7.2) |  |
| Korea, Rep. of | 566 (4.3) | 573 (3.3) |  | 567 (3.8) | 575 (3.2) |  | 574 (6.2) | 579 (5.4) |  |
| Latvia (LSS) ${ }^{1}$ | 490 (4.9) | 503 (5.2) |  | 500 (4.5) | 509 (5.5) |  | 498 (5.0) | 492 (7.4) |  |
| Lithuania ${ }^{\ddagger}$ | 477 (5.1) | 481 (4.9) |  | 463 (4.1) | 472 (5.4) |  | 492 (5.4) | 494 (5.7) |  |
| Macedonia, Rep. of | 436 (6.1) | 437 (5.4) |  | 449 (8.9) | 453 (6.6) |  | 441 (9.7) | 443 (6.3) |  |
| Malaysia | 535 (5.3) | 528 (6.6) |  | 516 (5.6) | 513 (7.4) |  | 493 (6.1) | 488 (10.7) |  |
| Moldova | 461 (4.2) | 470 (6.5) |  | 479 (4.5) | 478 (7.4) |  | 449 (4.6) | 452 (8.1) |  |
| Morocco | 326 (5.7) | 341 (4.5) |  | 341 (6.4) | 353 (4.6) |  | 376 (5.5) | 388 (3.3) |  |
| Netherlands ${ }^{\text {t }}$ | 540 (7.9) | 551 (7.5) |  | 535 (7.5) | 540 (6.2) |  | 534 (10.3) | 541 (8.3) |  |
| New Zealand | 496 (5.6) | 490 (6.9) |  | 494 (5.3) | 498 (7.4) |  | 502 (7.0) | 492 (6.6) |  |
| Philippines | 382 (7.4) | 373 (6.3) |  | 355 (6.4) | 355 (8.6) |  | 410 (5.2) | 403 (4.3) |  |
| Romania | 459 (5.4) | 458 (7.1) |  | 492 (5.9) | 491 (6.8) |  | 453 (6.0) | 452 (5.8) |  |
| Russian Federation | 510 (6.2) | 516 (7.1) |  | 524 (7.0) | 529 (6.1) |  | 502 (7.0) | 501 (9.4) |  |
| Singapore | 607 (6.2) | 609 (6.8) |  | 597 (7.3) | 601 (9.0) |  | 563 (6.8) | 561 (8.8) |  |
| Slovak Republic | 522 (5.4) | 528 (5.3) |  | 531 (3.9) | 543 (4.7) |  | 515 (5.1) | 528 (5.9) |  |
| Slovenia | 523 (4.8) | 531 (4.5) |  | 521 (4.9) | 526 (5.5) |  | 529 (6.6) | 531 (6.9) |  |
| South Africa | 292 (7.7) | 308 (6.7) |  | 322 (5.4) | 336 (5.6) |  | 352 (5.5) | 361 (5.3) |  |
| Thailand | 473 (6.4) | 469 (5.6) |  | 463 (8.9) | 462 (6.4) |  | 480 (6.5) | 471 (5.1) |  |
| Tunisia | 429 (3.1) | 458 (3.4) | $\triangle$ | 429 (3.5) | 455 (3.7) | $\triangle$ | 435 (6.6) | 457 (4.5) | $\triangle$ |
| Turkey | 428 (5.2) | 432 (5.0) |  | 428 (6.7) | 443 (7.7) |  | 446 (5.0) | 445 (4.8) |  |
| United States | 505 (4.5) | 514 (5.0) |  | 475 (4.0) | 489 (4.9) | $\triangle$ | 503 (7.0) | 508 (6.3) |  |
| International Avg. | 484 (0.9) | 491 (0.9) | $\triangle$ | 483 (1.0) | 491 (1.0) | $\triangle$ | 486 (1.1) | 489 (1.1) |  |

- Significantly higher than other gender

Significance tests adjusted for multiple comparisons
† Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.
2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

|  | Average Scale Scores for Mathematics Content Areas |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Geometry |  | Algebra |  |
|  | Girls | Boys | Girls | Boys |
| Australia | 496 (7.5) | 498 (5.4) | 523 (6.6) | 517 (5.4) |
| Belgium (Flemish) ${ }^{\dagger}$ | 538 (6.9) | 531 (9.1) | 545 (6.8) | 535 (8.8) |
| Bulgaria | 523 (5.8) | 525 (7.8) | 516 (5.6) | 509 (5.7) |
| Canada | 511 (6.5) | 503 (4.9) | 526 (3.7) | 524 (5.2) |
| Chile | 408 (6.2) | 415 (6.0) | 399 (4.5) | 398 (6.3) |
| Chinese Taipei | 555 (7.1) | 560 (6.8) | 585 (4.5) | 588 (6.1) |
| Cyprus | 487 (3.9) | 482 (8.2) | 487 (2.2) | 472 (2.4) |
| Czech Republic | 506 (7.6) | 520 (4.9) | 513 (3.9) | 516 (6.7) |
| England ${ }^{\text {+ }}$ | 467 (4.8) | 474 (6.7) | 493 (6.0) | 502 (5.1) |
| Finland | 495 (9.8) | 494 (8.8) | 498 (4.9) | 498 (3.8) |
| Hong Kong, SAR ${ }^{\dagger}$ | 558 (6.1) | 554 (6.4) | 570 (4.8) | 568 (5.6) |
| Hungary | 487 (8.1) | 492 (7.3) | 540 (4.9) | 533 (4.9) |
| Indonesia | 439 (7.3) | 443 (5.8) | 422 (6.8) | 426 (5.9) |
| Iran, Islamic Rep. | 433 (5.4) | 457 (4.1) | 431 (5.8) | 435 (6.9) |
| Israel ${ }^{2}$ | 456 (7.1) | 468 (6.8) | 476 (5.6) | 483 (5.4) |
| Italy | 476 (8.6) | 489 (5.1) | 481 (5.4) | 481 (4.0) |
| Japan | 572 (5.8) | 578 (5.8) | 568 (4.2) | 571 (3.6) |
| Jordan | 451 (8.4) | 447 (7.9) | 446 (5.1) | 433 (8.9) |
| Korea, Rep. of | 569 (7.3) | 578 (4.8) | 585 (3.7) | 585 (3.9) |
| Latvia (LSS) ${ }^{1}$ | 517 (4.2) | 528 (9.0) | 499 (4.5) | 498 (5.0) |
| Lithuania ${ }^{1 \ddagger}$ | 494 (7.0) | 498 (6.1) | 490 (5.1) | 483 (5.8) |
| Macedonia, Rep. of | 459 (6.8) | 460 (8.3) | 469 (4.7) | 461 (4.2) |
| Malaysia | 496 (5.5) | 497 (6.0) | 508 (6.0) | 502 (5.5) |
| Moldova | 480 (7.0) | 481 (7.6) | 480 (4.6) | 475 (5.5) |
| Morocco | 405 (5.3) | 408 (5.4) | 350 (7.4) | 354 (4.2) |
| Netherlands ${ }^{\dagger}$ | 516 (7.0) | 515 (5.2) | 522 (9.3) | 522 (7.4) |
| New Zealand | 481 (8.3) | 474 (6.7) | 506 (5.6) | 487 (6.4) |
| Philippines | 383 (5.5) | 383 (4.2) | 355 (7.6) | 333 (8.8) |
| Romania | 490 (12.2) | 484 (7.3) | 489 (5.5) | 473 (6.0) |
| Russian Federation | 518 (7.2) | 526 (7.4) | 533 (5.7) | 524 (6.3) |
| Singapore | 556 (9.2) | 565 (6.5) | 578 (6.7) | 574 (7.9) |
| Slovak Republic | 524 (8.8) | 529 (6.9) | 530 (5.3) | 521 (4.7) |
| Slovenia | 507 (8.2) | 505 (6.3) | 530 (3.1) | 520 (3.8) |
| South Africa | 333 (8.5) | 338 (6.1) | 290 (8.4) | 296 (9.7) |
| Thailand | 483 (4.7) | 486 (7.9) | 460 (6.0) | 452 (5.4) |
| Tunisia | 476 (7.5) | 492 (5.2) | 450 (3.6) | 460 (2.7) |
| Turkey | 429 (5.5) | 428 (8.1) | 442 (5.1) | 426 (4.7) |
| United States | 469 (5.5) | 477 (5.1) | 507 (4.3) | 504 (4.6) |
| International Avg. | 485 (1.2) | 489 (1.1) | 489 (0.9) | 485 (0.9) |

## What Changes Have Occurred in Content Area Achievement?

To examine changes in achievement in the mathematics content areas, Exhibit $3 \cdot 4$ shows the average percent correct for eighth-grade students in 1995 and 1999 for items given in both the 1995 and 1999 timss assessments, and the difference in performance between assessments. This content area trend analysis uses average percent correct rather than average scale score because there were insufficient items to reliably link the results for both assessments to the timss scale.

Changes in average achievement at a national level are not easy to bring about and inevitably take place over several years. Amending official curricula, producing relevant supporting resources, and changing teacher practice all take time, even under the most favorable conditions. Timss 1999 is only the second in what is expected to become a series of international surveys designed to reveal trends in achievement in mathematics and science. It is not surprising, therefore, that the trend data contained in Exhibit 3.4 reveal only a few significant changes in average achievement in the content areas. It is likely that the next timss administration scheduled for 2003 will show more significant changes in achievement.

Still, even during the four years between 1995 and 1999, statistically significant improvements occurred for Canada and Latvia (LSs) in all content areas except measurement, and for Cyprus in three content areas. Each of these countries also showed slight improvement in the remaining content areas. Average achievement in the Czech Republic showed statistically significant decreases in three content areas, and a slight decline in the remaining two areas. A small but significant increase in the international average for data representation, analysis, and probability, the only content area with a significant change internationally between 1995 and 1999, may be a result of increasing efforts to include elementary statistical concepts at the primary grades.

Although the changes were not statistically significant, Australia, Belgium (Flemish), Hong Kong, the Netherlands, and the United States showed small increases in achievement in all five content area means. Conversely, Bulgaria and Italy had small decreases in average achievement in all content areas (with a significant change in Bulgaria in data representation, analysis, and probability).


Exhibit 3.4 Overleaf

## Exhibit 3.4 Trends in Average Percent Correct in Mathematics Content Areas

|  | Average Percent Correct in Mathematics Content Areas* |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Total Tr | ematics ems |  | Fraction Sense | d Number d Items |  |  | ment tems |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  | 1995 | 1999 |  | 1995 | 1999 |  | 1995 | 1999 |  |  |
| Australia | 68 (0.9) | 69 (1.1) | - | 68 (0.8) | 70 (1.0) | $\bullet$ | 71 (0.9) | 73 (1.1) | - |  |
| Belgium (Flemish) | 73 (1.3) | 76 (0.7) | - | 75 (1.2) | 77 (0.6) | - | 77 (1.5) | 79 (1.1) | $\bullet$ |  |
| Bulgaria | 70 (1.3) | 65 (1.3) | $\bullet$ | 67 (1.6) | 61 (1.4) | - | 69 (1.5) | 63 (1.1) | - |  |
| Canada | 67 (0.5) | 70 (0.4) | - | 69 (0.5) | 72 (0.5) | - | 64 (0.6) | 67 (0.7) | $\bullet$ |  |
| Cyprus | 54 (0.5) | 56 (0.4) | $\triangle$ | 55 (0.5) | 58 (0.5) | - | 45 (0.8) | 46 (0.6) | - |  |
| Czech Republic | 72 (1.0) | 67 (0.9) | $\nabla$ | 67 (1.2) | 61 (1.1) | V | 80 (0.8) | 77 (1.0) | - |  |
| England | 64 (0.6) | 63 (0.9) | - | 65 (0.7) | 65 (0.9) | - | 67 (0.8) | 66 (1.2) | $\bullet$ |  |
| Hong Kong, SAR | 77 (1.3) | 79 (0.9) | $\bullet$ | 78 (1.3) | 81 (0.9) | $\bullet$ | 76 (1.4) | 77 (1.0) | $\bullet$ |  |
| Hungary | 67 (0.8) | 68 (0.8) | $\bullet$ | 63 (0.8) | 65 (0.9) | - | 73 (0.8) | 74 (0.7) | $\bullet$ |  |
| Iran, Islamic Rep. | 44 (0.6) | 44 (0.6) | $\bigcirc$ | 46 (0.7) | 45 (0.7) | - | 31 (1.0) | 34 (0.7) | - |  |
| Italy | 60 (0.9) | 58 (1.1) | $\bullet$ | 57 (1.0) | 55 (1.1) | - | 64 (1.2) | 63 (1.2) | - |  |
| Japan | 78 (0.3) | 78 (0.3) | - | 76 (0.4) | 76 (0.4) | - | 75 (0.4) | 74 (0.5) | - | - |
| Korea, Rep. of | 80 (0.4) | 81 (0.4) | - | 76 (0.5) | 77 (0.4) | - | 81 (0.6) | 83 (0.4) | - |  |
| Latvia (LSS) | 59 (0.8) | 64 (0.8) | - | 54 (0.9) | 59 (0.9) | $\triangle$ | 66 (1.0) | 70 (1.0) | - |  |
| Lithuania | 56 (1.0) | 57 (1.0) | $\bigcirc$ | 52 (1.0) | 54 (1.1) | $\bigcirc$ | 57 (0.9) | 56 (0.9) | - |  |
| Netherlands | 70 (1.6) | 74 (1.6) | $\bullet$ | 70 (1.3) | 75 (1.7) | - | 76 (1.6) | 77 (1.6) | - |  |
| New Zealand | 64 (1.1) | 62 (1.2) | - | 65 (1.0) | 63 (1.2) | - | 66 (1.2) | 65 (1.3) | - |  |
| Romania | 55 (1.0) | 54 (1.1) | - | 51 (0.9) | 50 (1.1) | - | 57 (1.2) | 57 (1.3) | - |  |
| Russian Federation | 68 (1.4) | 68 (1.3) | $\bullet$ | 64 (1.7) | 64 (1.4) | $\bullet$ | 69 (1.1) | 73 (1.3) | - | \% |
| Singapore | 84 (0.7) | 83 (1.1) | - | 87 (0.6) | 85 (1.0) | - | 86 (0.7) | 83 (1.1) | - |  |
| Slovak Republic | 69 (0.7) | 69 (0.9) | - | 66 (0.8) | 67 (1.1) | - | 75 (0.7) | 75 (0.9) | - |  |
| Slovenia | 69 (0.7) | 70 (0.6) | $\bullet$ | 68 (0.8) | 69 (0.7) | - | 72 (0.8) | 72 (0.7) | - | T0 |
| United States | 61 (1.1) | 63 (0.9) | - | 63 (1.1) | 66 (0.9) | - | 53 (1.1) | 55 (1.1) | - |  |
| International Avg. § | 66 (0.2) | 67 (0.2) | - | 65 (0.2) | 66 (0.2) | - | 67 (0.2) | 68 (0.2) | - |  |
| tries with Unapproved S | pling Proc | at the Cl | ssro | Level in |  |  |  |  |  |  |
| Israel | 66 (1.3) | 59 (1.1) | $\nabla$ | 67 (1.2) | 61 (1.0) | V | 63 (1.5) | 55 (1.1) | V |  |
| South Africa | 29 (1.2) | 27 (0.8) | - | 31 (1.2) | 29 (0.8) | - | 30 (1.4) | 28 (0.7) | - |  |
| Thailand | 65 (1.3) | 54 (1.0) | V | 66 (1.3) | 55 (1.1) | $\nabla$ | 63 (1.5) | 51 (1.2) | $\checkmark$ |  |



* Applies only to items that appeared on both the 1995 and 1999 assessments.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.




## CHAPTER 4

## Students' Backgrounds and Attitudes Towards Mathematics

There is abundant evidence that student achievement is related to home background factors, and to students' activities and attitudes. To help interpret the achievement results, Chapter 4 provides detailed information about students' home backgrounds, how they spend their time out of school, their self-concept in mathematics, and their attitudes towards mathematics. Also provided is information on changes in results between 1995 and 1999.


To provide an educational context for interpreting the mathematics achievement results, timss collected detailed information from students about their home backgrounds, how they spend their time out of school, and their attitudes towards mathematics. This chapter presents eighth-grade students' responses to a subset of these questions, together with changes in results between 1995 and 1999. Specifically, one set of questions addresses home resources and support for academic achievement. Another examines how much out-of-school time students spend on their schoolwork. A third set of questions elicits information on students' self-concept in mathematics and their feelings towards mathematics.

In an effort to summarize this information concisely and focus attention on educationally relevant support and practice, timss sometimes has combined information from individual questions to form an index that was more global and reliable than the component questions (e.g., home educational resources). According to their responses, students were placed in a "high," "medium," or "low" category. Cutoff points were established so that the high level of an index corresponds to conditions or activities generally associated with good educational practice and high academic achievement. For each index, the percentages of students in each category are presented in relation to their mathematics achievement. The data for the component questions and more detail about some topic areas are provided in the reference section of this report (see reference section R.1).

## What Educational Resources Do Students Have in Their Homes?

There is no shortage of evidence that students from homes with extensive educational resources have higher achievement in mathematics and other subjects than those from less advantaged backgrounds. This has been documented most recently in a study of the eighth-grade results from timss in $1995 .{ }^{1}$ The international report for these data ${ }^{2}$ showed that students from homes with large numbers of books, with a range of educational study aids, or with parents with university-level education also had higher mathematics achievement. For the 1999 data presented in this report, student responses to these three variables were combined to form an index of home educational resources (HER).

[^21]Exhibit 4.1 summarizes the home educational resources index in a twopage display. The index is described on the first page. Students assigned to the high level of this index reported coming from homes with more than 1 oo books, with all three study aids (a computer, a study desk or table for the student's own use, and a dictionary), and where at least one parent finished university. Students assigned to the low level had 25 or fewer books in the home, not all three study aids, and parents that had not completed secondary education. The remaining students were assigned to the medium level.

The first page of the display also presents the percentage of students at each level of the index for each country, together with the average mathematics achievement for those students. Standard errors are also shown. Countries are ordered by the percentage of students at the high level of the index. The international average across all countries is shown at the bottom of each column. On the second page of the display, the percentage of students at the high level of the index is shown graphically for each country.

There are large differences among countries in the distribution of students across the three categories of the index. Students at the high level of the home educational resources index are relatively rare in most countries, with just nine percent in this category on average internationally. Countries with the greatest percentages included Canada, Australia, Israel, and the United States, each of which had more than one-fifth (22 percent or more) of their students at the high level. At the other extreme, Thailand, Iran, and Morocco had more than half of their students at the low level.

The educational significance of this wide divergence becomes apparent when achievement differences between the levels of the index are considered. There was a substantial difference in the average mathematics achievement of students at the three index levels in every country for which data were available. This is reflected in the international average, where the achievement difference between students at the high level (559) and the low level (431) amounted to 128 score points. This difference is slightly larger than the difference between the highest performing country, Singapore, and the international average.

Since the association between home educational resources and mathematics achievement is well documented in timss and in extensive educational research, low average student achievement in some of the less wealthy countries most likely reflects the low level of educational resources in students' homes. However, since there is far from a one-to-one correspondence
between high performance and home resources, there are clearly other influences at work also. For example, Singapore had about the same percentage of students (five percent) at the high level of the index as Romania and Malaysia, but the average mathematics achievement of its students was considerably higher than that of most participating countries, including Romania and Malaysia.

More detailed information on the student responses that were combined in the home educational resources index is presented in
Exhibits R1.1 through R1.5 in the reference section. Exhibit R1.1 shows the percentage of eighth-grade students in each country that had a dictionary, study desk or table, or computer, and shows that students reporting having all three had higher average mathematics achievement than those without all three. The changes in these percentages presented in Exhibit R1.2 show that between 1995 and 1999 many countries had significant increases in the percentages of students having all three educational aids as well as those with computers in their homes (10 percent increase internationally, on average, for both).

Exhibit R1.3 shows for each country the percentage of students at each of five ranges of numbers of books in the home in relation to average mathematics achievement; changes in these results are shown in Exhibit R1.4. In most countries, the more books students reported in the home, the higher their mathematics achievement. Interestingly, however, the trend appears to be in the direction of having fewer books in the home. Taken together with the increase in home computers, this may reflect the emerging reliance on the Internet as a source of information.

The percentages of students in each of five categories of parents' educational level are shown in Exhibit R1.5, together with their average mathematics achievement. Although participants did their best to use educational categories that were comparable across all countries, the range of educational provision made this difficult. About half of the participating countries had to modify the response options presented to students in the questionnaire in order to conform to their national education system. Exhibit R1. 6 provides details of how these modifications were aligned with the categories of parents' education used in this report. Despite the different educational approaches, structures, and organizations across the timss countries, it is clear that parents' education is positively related to students' mathematics achievement. The pattern across countries was that eighth-grade students whose parents had more education were also those who had higher achievement in mathematics.

| Index of Home Educational Resources |  | High HER |  | Medium HER |  | Low HER |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on students' responses to three questions about home educational resources: number of books in the home; educational aids in the home (computer, study desk/table for own use, dictionary); parents' education (see reference exhibits R1.1, R1.3, R1.5). High level indicates more than 100 books in the home; all three educational aids; and either parent's highest level of education is finished university. Low level indicates 25 or fewer books in the home; not all three educational aids; and both parents' highest level of education is some secondary or less or is not known. Medium level includes all other possible combinations of responses. See reference exhibit R1.6 for national definitions of educational levels; response categories were defined by each country to conform to their own educational system and may not be strictly comparable across countries. | Canada <br> Australia Israel United States Hungary | $\begin{array}{ll} 27 & (1.0) \\ 24 & (1.5) \\ 23 & (1.2) \\ 22 & (1.5) \\ 19 & (1.2) \end{array}$ | $\begin{aligned} & 552(4.1) \\ & 557(5.1) \\ & 514(4.8) \\ & 555(5.1) \\ & 588(5.3) \end{aligned}$ | $\begin{aligned} & 71(1.0) \\ & 72(1.4) \\ & 72(1.1) \\ & 73(1.4) \\ & 75(1.2) \end{aligned}$ | $\begin{aligned} & 525(2.2) \\ & 517(4.9) \\ & 461(3.5) \\ & 492(3.1) \\ & 525(3.1) \end{aligned}$ | $\begin{array}{ll} 2 & \begin{array}{l} (0.2) \\ 3 \\ 3 \\ (0.4) \\ 5 \\ 5 \end{array}(0.6) \\ 4(0.5) \\ 5(0.7) \end{array}$ | 466 (12.5) <br> 387 (10.0) <br> 427 (6.4) <br> 427 (7.9) |
|  | New Zealand Korea, Rep. of Czech Republic Cyprus Bulgaria | $\begin{aligned} & 18(1.2) \\ & 14(0.8) \\ & 13 \\ & (0.8) \\ & 12 \\ & (0.7) \\ & 12 \end{aligned}(1.7)$ | $\begin{aligned} & 546(6.5) \\ & 637(2.8) \\ & 560(6.8) \\ & 526(4.5) \\ & 571(12.9) \end{aligned}$ | 76 (1.1) <br> 80 (0.8) <br> 83 (0.8) <br> 81 (0.8) <br> 82 (1.5) | 484 (4.8) <br> 583 (1.9) <br> 517 (3.9) <br> 476 (1.6) <br> 507 (4.7) | $\begin{aligned} & 6(0.5) \\ & 5(0.3) \\ & 4(0.5) \\ & 8(0.5) \\ & 7(0.8) \end{aligned}$ | $\begin{aligned} & 418 \text { (9.3) } \\ & 513 \text { (5.0) } \\ & 460 \text { (11.3) } \\ & 415(7.1) \\ & 455(9.8) \end{aligned}$ |
|  | Slovenia <br> Slovak Republic Netherlands Russian Federation Latvia (LSS) | $\begin{array}{r} 11(0.8) \\ 10(0.9) \\ 9(1.1) \\ 9(0.8) \\ 8(0.7) \end{array}$ | $\begin{array}{ll} 588 & (5.8) \\ 586 & (6.8) \\ 575 & (10.4) \\ 560 & (8.3) \\ 552 & (7.2) \end{array}$ | 84 (0.8) <br> 86 (0.9) <br> 89 (1.1) <br> 86 (0.7) <br> 88 (0.8) | $\begin{aligned} & 527(2.6) \\ & 531(3.7) \\ & 538(7.1) \\ & 527(5.9) \\ & 504(3.4) \end{aligned}$ | $\begin{aligned} & 5(0.5) \\ & 4(0.5) \\ & 2(0.8) \\ & 6(0.5) \\ & 4(0.5) \end{aligned}$ | $\begin{gathered} 470(8.8) \\ 463(8.0) \\ \sim \sim \\ \sim \sim(12.6) \\ 474(7.9) \end{gathered}$ |
|  | Belgium (Flemish) Chinese Taipei Lithuania ${ }^{\ddagger}$ Chile Italy | $\begin{aligned} & 8(0.7) \\ & 8(0.7) \\ & 7(0.8) \\ & 6(0.9) \\ & 6(0.6) \end{aligned}$ | $\begin{aligned} & 599(6.5) \\ & 666(7.2) \\ & 552(9.2) \\ & 476(13.0) \\ & 528(7.3) \end{aligned}$ | 86 (1.3) <br> 84 (0.7) <br> 83 (1.1) <br> 56 (1.3) <br> 81 (0.8) | 559 (3.9) <br> 586 (3.6) <br> 483 (3.8) <br> 410 (4.3) <br> 484 (3.7) | $\begin{array}{r} 6(1.3) \\ 8(0.6) \\ 10(1.0) \\ 38(1.6) \\ 14(0.8) \end{array}$ | $\begin{aligned} & 490(11.7) \\ & 502(6.6) \\ & 420(8.4) \\ & 355(3.2) \\ & 434(6.4) \end{aligned}$ |
|  | Singapore Romania Malaysia Jordan Macedonia, Rep. of | $\begin{aligned} & 5(0.7) \\ & 5(0.7) \\ & 5(0.6) \\ & 4(0.4) \\ & 4(0.5) \end{aligned}$ | $\begin{aligned} & 663(10.0) \\ & 546(9.7) \\ & 595(5.5) \\ & 502(10.8) \\ & 517(10.8) \end{aligned}$ | $\begin{array}{ll} 87 & (0.6) \\ 73 & (1.6) \\ 71 & (0.9) \\ 71 & (1.0) \\ 73 & (1.4) \end{array}$ | $\begin{aligned} & 605(6.0) \\ & 482(5.2) \\ & 527(4.6) \\ & 440(3.5) \\ & 465(3.8) \end{aligned}$ | $\begin{array}{r} 8(0.7) \\ 22(1.7) \\ 25(1.1) \\ 25(1.1) \\ 23(1.6) \end{array}$ | $\begin{aligned} & 552(7.3) \\ & 435(7.3) \\ & 481(4.3) \\ & 391(4.8) \\ & 389(7.2) \end{aligned}$ |
|  | Tunisia Hong Kong, SAR Philippines South Africa Thailand | $\begin{array}{ll} 3 & (0.5) \\ 3 & (0.3) \\ 3 & (0.5) \\ 2 & (0.4) \\ 2 & (0.3) \end{array}$ | $\begin{gathered} 493(5.6) \\ 612(8.8) \\ 431(28.1) \\ \sim \sim \\ \sim \sim \end{gathered}$ | 59 (1.3) <br> 78 (0.8) <br> 67 (1.1) <br> 54 (1.7) <br> 47 (1.4) | 455 (2.7) <br> 586 (4.2) <br> 353 (6.7) <br> 293 (8.1) <br> 487 (5.9) | 38 (1.5) 19 (0.9) 30 (1.2) 44 (1.8) 51 (1.4) | 434 (2.7) <br> 566 (5.2) <br> 322 (6.6) <br> 246 (6.2) <br> 447 (5.1) |
|  | Moldova Iran, Islamic Rep. <br> Turkey <br> Morocco <br> Indonesia | $\begin{array}{ll} 2 & (0.4) \\ 1 & (0.4) \\ 1 & (0.2) \\ 1 & (0.2) \\ 1 & (0.2) \end{array}$ |  | 80 (1.3) <br> 45 (1.7) <br> 51 (1.5) <br> 36 (1.5) <br> 56 (1.6) | 476 (4.1) <br> 443 (4.2) <br> 445 (5.3) <br> 349 (4.0) <br> 420 (5.1) | 18 (1.3) <br> 54 (1.9) <br> 48 (1.5) <br> 63 (1.6) <br> 44 (1.7) | 443 (6.2) 404 (2.7) 410 (3.9) 333 (3.1) 381 (5.4) |
|  | England Finland Japan | $\begin{aligned} & \text { - - } \\ & \text { - - } \\ & \text { - - } \end{aligned}$ | - - | - - | - - | - - | - - |
|  | International Avg. | $9(0.1)$ | 559 (2.3) | 72 (0.2) | 487 (0.8) | 19 (0.2) | 431 (1.2) |

[^22]|  | Percentage of Students at High Level of Index of Home Educational Resources (HER) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Canada | 0 |  |  |  |  |
| Australia | - - - - - - - - - 0 |  |  |  |  |
| Israel | --.-------........-- 0 |  |  |  |  |
| United States | -..------...........- 0 |  |  |  |  |
| Hungary | 0 |  |  |  |  |
| New Zealand | --->. 0 |  |  |  |  |
| Korea, Rep. of | --..-.-...- 0 |  |  |  |  |
| Czech Republic | -....... 0 |  |  |  |  |
| Cyprus | -- 0 |  |  |  |  |
| Bulgaria | --. 0 |  |  |  |  |
| Slovenia -.........- 0 |  |  |  |  |  |
| Slovak Republic |  |  |  |  |  |
| Netherlands | --- 0 |  |  |  |  |
| Russian Federation | -- 0 |  |  |  |  |
| Latvia (LSS) | --- 0 |  |  |  |  |
| Belgium (Flemish) | - 0 |  |  |  |  |
| Chinese Taipei |  |  |  |  |  |
| Lithuania ......- |  |  |  |  |  |
| Chile -...- 0 |  |  |  |  |  |
| Italy - $\quad 0$ | - 0 |  |  |  |  |
| Singapore | - 0 - - - - |  |  |  |  |
| Romania | $\bigcirc$ |  |  |  |  |
| Malaysia | -.- |  |  |  |  |
| Jordan | -.0 |  |  |  |  |
| Macedonia, Rep. of | - |  |  |  |  |
| Tunisia O |  |  |  |  |  |
| Hong Kong, SAR | $\bigcirc$ |  |  |  |  |
| Philippines | 0 - |  |  |  |  |
| South Africa | - |  |  |  |  |
| Thailand | 0 |  |  |  |  |
| Moldova - |  |  |  |  |  |
| Iran, Islamic Rep. | $\begin{array}{ll}0 & \\ 0 & ¢_{0}^{0} \\ 0 \\ 0\end{array}$ |  |  |  |  |
| Turkey | - |  |  |  |  |
| Morocco | - |  |  |  |  |
| Indonesia | - |  |  |  |  |
| England |  |  |  |  |  |
| Finland |  |  |  |  |  |
| Japan |  |  |  |  |  |
|  |  |  |  |  | نِّ |
| International Avg. |  |  |  |  |  |
|  | $\bigcirc$ |  | 1 |  |  |
|  | 20 | 40 | 60 | 80 | 100 |

Students who speak a language (or languages) in the home that is different from the language spoken in school sometimes benefit from being multilingual. However, sometimes they are still developing proficiency in the language of instruction and can be at a disadvantage in learning situations. Exhibit 4.2 contains students' reports of how frequently they spoke the language of the timss test at home in relation to their average mathematics achievement. Students from homes where the language of the test is always or almost always spoken had higher average achievement than those who spoke it less frequently. On average internationally, however, more than 20 percent of students were from homes where the language of the test was spoken only sometimes ( 17 percent), or never (5 percent). Many countries tested in more than one language in order to cover their whole student population. These included Canada (English and French), Finland (Finnish and Swedish), Hong Kong (Chinese and English), Israel (Hebrew and Arabic), Italy (Italian and German), Macedonia (Macedonian and Albanian), Moldova (Moldavian and Russian), the Philippines (Filipino and English), Romania (Romanian and Hungarian), and South Africa (English and Afrikaans). However, in countries like Indonesia, Morocco, the Philippines, Singapore, and South Africa, where less than one-third of students were from homes where the language of the test is routinely spoken, testing in all possible dialects and languages was prohibitive. Exhibit 4.3 displays, for countries that also took part in timss in 1995, trend data for the language of the test spoken in the home. On average across countries there was very little change.

By the end of the eighth grade, students in most countries can say what their expectations are for further education. Although more than onequarter of the students in some countries did not know, Exhibit $4 \cdot 4$ shows that, on average across countries, more than half of the students reported that they expected to finish university (a four-year degree program or equivalent). The highest percentages were in Canada, Korea, and the United States, where more than three-fourths expected to finish university, but the percentages were substantial in almost every country. In almost every country, also, there was a positive association between educational expectations and mathematics achievement.

Exhibits $\mathrm{R}_{1.7}$ to $\mathrm{R}_{1.9}$ in the reference section present eighth-grade students' reports about how they themselves, their mothers, and their friends feel about the importance of doing well in various academic and non-academic activities. On average, more than go percent of the students reported that they and their mothers agreed that it was important to do well in mathematics, science, and language. Somewhat fewer reported that their
friends agreed it was important to do well in these three subjects ( 77 to 86 percent). As might be anticipated, slightly more students reported that they and their friends felt it was important to have fun ( 92 percent) than reported that their mothers found this important ( 85 percent). More moderate agreement was reported for the importance of doing well in sports (from 81 to 87 percent). Students also were asked why they needed to do well in mathematics (see Exhibit R1.10). Although a motivating factor for 71 percent of the students on average internationally, pleasing their parents was secondary to getting into their desired secondary school or university ( 87 percent) or getting their desired job (81 percent).

|  | Always or Almost Always |  | Sometimes |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia | 89 (1.2) | 529 (4.9) | 10 (1.1) | 516 (10.4) | 1 (0.3) | ~ ~ |
| Belgium (Flemish) | 86 (1.3) | 566 (3.2) | 8 (0.7) | 531 (8.0) | 6 (0.9) | 522 (13.5) |
| Bulgaria | 88 (1.9) | 517 (6.3) | 11 (1.7) | 471 (13.7) | 1 (0.3) | ~ ~ |
| Canada | 91 (0.6) | 532 (2.5) | 8 (0.5) | 523 (6.6) | 2 (0.2) | ~ ~ |
| Chile | 94 (0.5) | 396 (4.9) | 6 (0.5) | 346 (7.7) | 1 (0.1) | ~ ~ |
| Chinese Taipei | 67 (1.4) | 606 (3.9) | 31 (1.3) | 545 (5.3) | 2 (0.2) | ~ ~ |
| Cyprus | 89 (1.1) | 482 (2.2) | 9 (1.0) | 459 (7.4) | 2 (0.3) | ~ ~ |
| Czech Republic | 98 (0.5) | 523 (4.0) | 1 (0.3) | ~ ~ | 1 (0.2) | ~ ~ |
| England | 95 (0.9) | 500 (4.2) | 5 (0.8) | 471 (12.1) | 0 (0.1) | ~ ~ |
| Finland | 97 (0.7) | 524 (2.7) | 3 (0.7) | 495 (15.6) | 1 (0.2) | ~ ~ |
| Hong Kong, SAR | 80 (2.4) | 571 (4.5) | 17 (1.9) | 600 (8.5) | 3 (0.5) | 609 (12.2) |
| Hungary | 99 (0.2) | 538 (4.1) | 0 (0.2) | ~ ~ | 1 (0.1) | ~ ~ |
| Indonesia | 28 (2.5) | 411 (8.0) | 63 (2.3) | 397 (5.0) | 9 (0.8) | 428 (10.6) |
| Iran, Islamic Rep. | 59 (3.4) | 433 (4.3) | 26 (2.1) | 405 (4.2) | 15 (1.6) | 408 (5.0) |
| Israel | 85 (1.2) | 471 (3.6) | 13 (1.1) | 455 (10.0) | 2 (0.3) | ~ ~ |
| Italy | 77 (1.1) | 493 (3.5) | 20 (1.0) | 434 (5.6) | 4 (0.5) | 442 (11.8) |
| Japan | 97 (0.3) | 581 (1.8) | 3 (0.3) | 532 (11.5) | 0 (0.1) | ~ ~ |
| Jordan | 85 (0.9) | 433 (3.9) | 13 (0.8) | 415 (5.5) | 2 (0.3) | ~ ~ |
| Korea, Rep. of | 96 (0.3) | 589 (2.0) | 4 (0.3) | 545 (4.9) | 0 (0.0) | ~ ~ |
| Latvia (LSS) | 92 (1.2) | 506 (3.6) | 6 (0.8) | 493 (10.6) | 2 (0.6) | ~ ~ |
| Lithuania ${ }^{\text { }}$ | 99 (0.3) | 482 (4.5) | 1 (0.3) | ~ ~ | 0 (0.1) | ~ ~ |
| Macedonia, Rep. of | 93 (1.5) | 470 (4.6) | 5 (0.9) | 436 (15.1) | 2 (0.8) | $\sim \sim$ |
| Malaysia | 61 (2.3) | 503 (4.4) | 30 (1.7) | 540 (6.1) | 10 (1.0) | 558 (8.5) |
| Moldova | 89 (1.2) | 473 (4.1) | 10 (1.1) | 445 (7.4) | 1 (0.3) | ~ ~ |
| Morocco | 20 (1.0) | 322 (5.5) | 51 (1.6) | 346 (3.1) | 30 (1.6) | 335 (3.8) |
| Netherlands | 86 (2.4) | 544 (7.8) | 8 (1.2) | 529 (9.0) | 6 (1.8) | 531 (13.7) |
| New Zealand | 90 (0.9) | 495 (5.1) | 9 (0.7) | 470 (9.3) | 1 (0.3) | ~ ~ |
| Philippines | 11 (1.6) | 301 (8.0) | 70 (1.5) | 356 (6.7) | 19 (0.9) | 337 (6.6) |
| Romania | 92 (2.4) | 477 (5.9) | 5 (1.5) | 442 (12.9) | 3 (0.9) | 440 (19.5) |
| Russian Federation | 94 (2.3) | 527 (5.9) | 5 (2.3) | 527 (36.9) | 1 (0.2) | ~ ~ |
| Singapore | 27 (1.8) | 629 (7.1) | 63 (1.6) | 595 (6.4) | 10 (0.5) | 601 (8.2) |
| Slovak Republic | 87 (1.9) | 539 (4.2) | 9 (1.4) | 503 (7.7) | 3 (0.7) | 506 (12.6) |
| Slovenia | 91 (1.0) | 537 (2.8) | 7 (0.7) | 483 (8.3) | 2 (0.4) | ~ ~ |
| South Africa | 23 (2.2) | 370 (11.7) | 53 (1.6) | 259 (4.7) | 24 (1.8) | 224 (9.3) |
| Thailand | 72 (2.4) | 477 (5.6) | 25 (2.1) | 446 (6.6) | 3 (0.4) | 424 (11.7) |
| Tunisia | 88 (1.5) | 449 (2.5) | 8 (1.0) | 443 (6.6) | 4 (0.7) | 453 (13.5) |
| Turkey | 92 (1.4) | 433 (3.9) | 7 (1.3) | 389 (12.2) | 1 (0.2) | ~ ~ |
| United States | 90 (1.0) | 509 (3.8) | 9 (1.0) | 456 (8.2) | 1 (0.1) | ~ ~ |
| International Avg. | 79 (0.3) | 493 (0.8) | 17 (0.2) | 466 (2.3) | 5 (0.1) | 455 (4.1) |

[^23][^24]$\square$


## Exhibit 4.3 Trends in Frequency with Which Students Speak Language of the Test at Home



A 1999 significantly higher than 1995

No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by students.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An "r" indicates a $70-84 \%$ student response rate, based on the lower response rate in either 1995 or 1999.

|  | Finish University ${ }^{1}$ |  | Some Vocational/ Technical Education or University Only ${ }^{2}$ |  | Finish Secondary School Only ${ }^{3}$ |  | Some Secondary School Only |  | Do Not Know |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average <br> Achievement |
| Australia | 55 (1.8) | 554 (5.0) | 14 (0.7) | 524 (5.0) | 17 (1.0) | 479 (7.1) | 5 (0.5) | 460 (7.0) | 9 (0.7) | 501 (7.5) |
| Belgium (Flemish) | 26 (1.1) | 605 (6.4) | 30 (0.9) | 563 (3.8) | 16 (0.9) | 509 (4.5) | 0 (0.0) | ~ ~ | 29 (1.0) | 544 (2.9) |
| Bulgaria | 60 (2.9) | 538 (7.2) | 8 (0.6) | 473 (6.8) | 22 (2.2) | 467 (6.1) | 1 (0.2) | ~ ~ | $9(0.9)$ | 477 (8.9) |
| Canada | 76 (0.9) | 539 (2.6) | 13 (0.6) | 522 (4.7) | 4 (0.3) | 482 (7.7) | 1 (0.1) | ~ ~ | 7 (0.6) | 497 (6.0) |
| Chile | 54 (1.6) | 428 (6.0) | 18 (0.8) | 367 (5.4) | 19 (1.0) | 347 (5.2) | 2 (0.2) | ~ ~ | 7 (0.5) | 359 (6.7) |
| Chinese Taipei | 62 (1.4) | 624 (3.7) | 24 (1.0) | 527 (3.0) | 2 (0.3) | ~ ~ | 0 (0.1) | ~ ~ | 11 (0.6) | 534 (7.2) |
| Cyprus | 51 (1.0) | 515 (2.3) | 14 (0.7) | 455 (3.9) | 13 (0.6) | 431 (4.8) | 6 (0.5) | 372 (8.4) | 16 (0.9) | 460 (5.2) |
| Czech Republic | 38 (1.8) | 564 (4.1) | 5 (0.6) | 542 (7.1) | 39 (1.5) | 496 (3.3) | 8 (1.0) | 452 (7.1) | 10 (0.8) | 493 (7.6) |
| England |  |  |  |  |  |  |  |  |  |  |
| Finland | 10 (0.8) | 564 (5.8) | 22 (1.0) | 541 (3.2) | 41 (1.2) | 503 (3.4) | 3 (0.4) | 481 (7.9) | 24 (0.8) | 519 (4.8) |
| Hong Kong, SAR | 63 (1.7) | 601 (3.8) | 20 (0.9) | 562 (4.9) | 10 (0.8) | 529 (7.7) | 1 (0.2) | ~ ~ | 6 (0.4) | 562 (6.8) |
| Hungary | 56 (1.8) | 575 (3.7) | 0 (0.0) | ~ ~ | 39 (1.7) | 482 (4.0) | 1 (0.2) | ~ ~ | 4 (0.4) | 511 (9.5) |
| Indonesia | 39 (1.8) | 435 (5.7) | 30 (1.1) | 401 (5.3) | 12 (0.9) | 381 (6.1) | 5 (0.5) | 336 (9.2) | 13 (1.0) | 373 (8.4) |
| Iran, Islamic Rep. | 48 (1.7) | 444 (4.6) | 6 (0.4) | 415 (9.6) | 6 (0.5) | 377 (8.8) | 4 (0.5) | 378 (8.7) | 36 (1.2) | 411 (4.0) |
| Israel | 59 (1.0) | 492 (4.2) | 16 (0.6) | 457 (7.0) | 11 (0.7) | 419 (6.2) | 1 (0.2) | ~ ~ | 13 (0.7) | 438 (7.5) |
| Italy | 33 (1.3) | 517 (4.1) | 19 (0.9) | 487 (4.4) | 31 (1.1) | 463 (4.0) | 7 (0.6) | 396 (10.4) | 9 (0.7) | 461 (8.7) |
| Japan | 38 (0.9) | 614 (2.7) | 18 (0.6) | 564 (2.6) | 18 (0.7) | 532 (3.0) | 1 (0.1) | ~ ~ | 25 (0.7) | 572 (3.1) |
| Jordan | 60 (1.1) | 461 (3.9) | 11 (0.6) | 376 (6.1) | 5 (0.5) | 365 (7.8) | 3 (0.3) | 372 (12.6) | 21 (0.8) | 407 (4.8) |
| Korea, Rep. of | 77 (0.7) | 605 (1.9) | 8 (0.4) | 521 (4.2) | 4 (0.3) | 500 (6.3) | 0 (0.1) | ~ ~ | 11 (0.5) | 551 (4.3) |
| Latvia (LSS) | 65 (1.5) | 525 (3.9) | 13 (0.9) | 481 (5.5) | 8 (0.7) | 467 (6.1) | 1 (0.1) | ~ ~ | 13 (1.0) | 466 (6.1) |
| Lithuania ${ }^{\text { }}$ | 45 (2.1) | 523 (4.4) | 25 (1.2) | 455 (4.6) | 6 (0.6) | 439 (8.3) | 2 (0.3) | ~ ~ | 23 (1.2) | 446 (5.4) |
| Macedonia, Rep. of | 53 (1.8) | 491 (3.6) | 11 (0.7) | 444 (5.2) | 17 (1.1) | 413 (6.2) | 8 (0.6) | 375 (9.4) | 11 (0.9) | 395 (10.0) |
| Malaysia | 65 (1.4) | 533 (4.4) | 18 (0.9) | 498 (5.8) | 4 (0.4) | 483 (8.7) | 2 (0.2) | ~ ~ | 11 (0.8) | 501 (6.5) |
| Moldova | 45 (1.7) | 493 (4.2) | 20 (1.1) | 466 (6.5) | 9 (0.8) | 451 (7.7) | 4 (0.6) | 441 (12.5) | 22 (1.2) | 444 (5.5) |
| Morocco | 43 (0.9) | 356 (4.6) | 22 (0.9) | 326 (4.7) | 6 (0.4) | 321 (11.2) | 6 (0.7) | 306 (7.3) | 23 (0.7) | 340 (7.4) |
| Netherlands | 22 (2.8) | 582 (9.6) | 30 (1.8) | 549 (5.7) | 29 (2.6) | 507 (9.0) | 1 (0.2) | ~ ~ | 18 (0.9) | 533 (8.1) |
| New Zealand | 52 (1.5) | 520 (5.8) | 16 (0.7) | 477 (5.2) | 16 (0.8) | 451 (4.9) | 3 (0.3) | 433 (7.7) | 13 (0.7) | 465 (7.0) |
| Philippines | 64 (2.0) | 374 (6.3) | 10 (0.6) | 299 (7.3) | 9 (0.6) | 293 (9.3) | 8 (0.8) | 293 (14.3) | 8 (0.7) | 315 (9.8) |
| Romania | 43 (2.0) | 520 (5.9) | 10 (0.6) | 446 (9.4) | 25 (1.3) | 454 (6.9) | 4 (0.8) | 460 (17.0) | 19 (1.3) | 428 (7.8) |
| Russian Federation | 61 (1.5) | 547 (5.4) | 19 (1.0) | 505 (6.1) | 7 (0.5) | 481 (10.4) | 2 (0.5) | ~ ~ | 11 (0.7) | 496 (7.8) |
| Singapore | 57 (2.1) | 625 (6.1) | 26 (1.6) | 576 (5.5) | 2 (0.3) | ~ ~ | 0 (0.0) | ~ ~ | 15 (0.7) | 587 (8.2) |
| Slovak Republic | 46 (2.3) | 572 (3.8) | 11 (0.8) | 525 (5.5) | 33 (1.6) | 498 (3.6) | 2 (0.3) | ~ ~ | 8 (0.7) | 499 (7.3) |
| Slovenia | 40 (1.0) | 579 (2.8) | 32 (0.9) | 508 (4.0) | 18 (0.7) | 495 (4.2) | 4 (0.4) | 436 (7.7) | 6 (0.5) | 498 (7.5) |
| South Africa | 55 (1.4) | 292 (8.8) | 18 (0.9) | 262 (9.1) | 10 (0.6) | 263 (7.5) | 9 (0.7) | 236 (12.1) | 8 (0.6) | 260 (11.0) |
| Thailand | 55 (1.6) | 493 (5.5) | 4 (0.3) | 458 (10.2) | 23 (1.2) | 439 (5.6) | 5 (0.5) | 415 (10.4) | 13 (0.9) | 437 (6.8) |
| Tunisia | 59 (1.0) | 457 (3.3) | 23 (0.7) | 437 (2.6) | 6 (0.4) | 425 (6.9) | 2 (0.2) | ~ ~ | 10 (0.5) | 442 (6.2) |
| Turkey | 62 (1.3) | 454 (5.0) | 15 (0.8) | 394 (5.0) | 8 (0.5) | 386 (6.9) | 4 (0.4) | 374 (9.1) | 12 (0.5) | 394 (5.9) |
| United States | 78 (1.2) | 516 (3.8) | 9 (0.6) | 466 (5.1) | 5 (0.4) | 426 (6.2) | 1 (0.1) | ~ ~ | 7 (0.5) | 474 (5.9) |
| International Avg. | 52 (0.3) | 517 (0.8) | 17 (0.1) | 469 (1.0) | 15 (0.2) | 442 (1.0) | 3 (0.1) | 390 (3.1) | 14 (0.1) | 462 (1.1) |

Background data provided by students.

* Response categories were defined by each country to conform to their own educational system and may not be strictly comparable across countries. See reference exhibit R1.6 for country modifications to the definitions of educational levels.
1 In most countries, finish university is defined as completion of at least a 4 -year degree program at a university or an equivalent institute of higher education.
2 In some countries, may include higher post-secondary education levels.
3 In most countries, finish secondary school corresponds to completion of an upper-secondary track terminating after 11 to 13 years of schooling (ISCED level 3 vocational, apprenticeship or academic tracks).
$\mp$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash $(-)$ indicates data are not available. A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates a $70-84 \%$ student response rate.


## How Much of Their Out-of-School Time Do Students Spend on Homework During the School Week?

One of the major ways that students can consolidate and extend classroom learning is to spend time out of school studying or doing homework in school subjects. Well-chosen homework assignments can reinforce classroom learning, and by providing a challenge can encourage students to extend their understanding of the subject matter. Homework also allows students who are having trouble keeping up with their classmates to review material taught in class.

To summarize the amount of time typically devoted to homework in each country, timss constructed an index of out-of-school study time (ost) that assigns students to a high, medium, or low level on the basis of the amount of time they reported studying mathematics, science, and other subjects. Students at the high level reported spending more than three hours each day out of school studying all subjects combined. Students at the medium level reported spending more than one hour but not more than three, while those at the low level reported one hour or less per day of out-of-school study.

Exhibit 4.5 presents the percentages of students at the various levels of this index across countries, and their average mathematics achievement. On average across countries, 38 percent of eighth-grade students were at the high level of the out-of-school study time index, and a further $4^{8}$ percent were at the medium level. Only 14 percent, on average, were at the low level, with just one hour of homework or less each day. Countries with a heavy emphasis on homework included Iran, Malaysia, Singapore, Italy, Jordan, Tunisia, Turkey, Macedonia, Romania, Moldova, and Morocco, where more than half of the students were at the high level of the index. In these countries, homework seems to be an important part of teachers' instructional strategy. In contrast, there seems to be relatively little emphasis on homework in Australia, Chile, Chinese Taipei, the Czech Republic, Hong Kong, Japan, Korea, New Zealand, and the United States, where one-fifth or more of students were at the low level of the index.

On average internationally, and in most of the countries, students at the low level of the index also had lower mathematics achievement, on average, than their classmates who reported more out-of-school study time. However, spending a lot of time studying was not usually associated with higher achievement. On average internationally and in many countries, students at the medium level of the study index had average achievement that was as high as or higher than that of students at the
high level. This pattern suggests that, compared with their higher-achieving counterparts, the lower-performing students may do less homework, either because they simply do not do it or because their teachers do not assign it, or more homework, perhaps in an effort to keep up academically.

Exhibit 4.6 presents information on trends in the index of out-of-school study time from 1995 to 1999. Internationally on average there was no change. Among countries with a significant decrease in the percentage at the high level were Cyprus, Hong Kong, Japan, Korea, Singapore, and Thailand. In contrast, Canada, Latvia (Lss), Lithuania, and the Russian Federation had increased percentages at the high level of the index.

More detailed information on the amount of time students reported spending on mathematics homework is presented in Exhibit 4.7. The results reveal that students spend 1.1 hours per day doing mathematics homework, on average internationally. The exhibit also shows the percentages of students that reported spending one hour or more, less than one hour, and no time at all studying mathematics or doing mathematics homework on a normal school day, together with their average mathematics achievement. Half the students, on average internationally, reported spending some time but less than one hour each day, and these students had higher average achievement than those spending one hour or more or those spending no time at all. Another 40 percent reported spending more than one hour per day doing mathematics homework. Countries where more than half of the students reported spending an hour or more included Indonesia, Iran, Italy, Jordan, Malaysia, Morocco, the Philippines, Romania, Singapore, South Africa, Tunisia, and Turkey. The countries where students reported the least mathematics homework included four of the top-performing countries - Chinese Taipei, Hong Kong, Japan, and Korea. In these countries, one-fourth or more of students ( 25 to 34 percent) reported spending no out-of-school time studying mathematics or doing mathematics homework on a normal school day.

Further detail on the student data that underlie the index of out-of-school study time is provided in Exhibit R1.11 in the reference section. On average, in comparison with the 1.1 hours each day students spent on mathematics homework, they reported 2.8 hours of homework in total. Exhibit R1.12 shows essentially no change on average internationally in the amount of homework reported by students from 1995 to 1999. To provide a fuller picture of how students spend their out-of-school time on a school day, Exhibit R1.13, also in the reference section, gives students' reports on how they spend their daily leisure time. The two most popular activities are watching television or videos and playing or talking with friends (each about two hours per day).


Exhibits 4.5-4.7 Overleaf


Index based on students' responses to three questions about out-of-school study time: time spent after school studying mathematics or doing mathematics homework; time spent after school studying science or doing science homework; time spent after school studying or doing homework in school subjects other than mathematics and science (see reference exhibit R1.11). Number of hours based on: no time $=0$, less than 1 hour $=0.5,1-2$ hours $=1.5,3-$ 5 hours $=4$, more than 5 hours $=7$. High level indicates more than three hours studying all subjects combined. Medium level indicates more than one hour to three hours studying all subjects combined. Low level indicates one hour or less studying all subjects combined.

| Iran, Islamic Rep. |  | High OST |  | Medium OST |  | $\begin{aligned} & \text { Low } \\ & \text { OST } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | r | 69 (1.1) | 431 (3.6) | 27 (0.9) | 420 (4.3) | 4 (0.4) | 389 (11.8) |
| Malaysia |  | 65 (1.2) | 522 (4.2) | 31 (1.0) | 524 (6.2) | 3 (0.3) | 494 (11.2) |
| Singapore |  | 59 (1.2) | 608 (5.8) | 35 (0.9) | 609 (7.4) | 7 (0.6) | 559 (10.2) |
| Italy |  | 58 (1.3) | 489 (4.1) | 36 (1.2) | 487 (4.6) | 6 (0.6) | 405 (9.1) |
| Jordan | s | 58 (1.2) | 449 (4.7) | 33 (0.9) | 448 (5.3) | 8 (0.7) | 372 (11.1) |
| Tunisia | r | 58 (0.9) | 450 (3.0) | 34 (0.8) | 457 (3.1) | 8 (0.6) | 454 (7.1) |
| Turkey | $r$ | 56 (1.3) | 442 (4.7) | 39 (1.0) | 429 (5.0) | 6 (0.5) | 404 (9.2) |
| Macedonia, Rep. of | r | 55 (1.3) | 463 (4.0) | 39 (1.1) | 463 (4.6) | 6 (0.5) | 428 (9.4) |
| Romania | $r$ | 55 (1.6) | 491 (6.0) | 33 (1.1) | 468 (5.3) | 12 (1.0) | 430 (7.9) |
| Moldova | r | 52 (1.3) | 478 (4.8) | 38 (1.1) | 476 (4.8) | 10 (0.8) | 455 (7.6) |
| Morocco | s | 51 (1.5) | 349 (3.2) | 34 (1.1) | 349 (6.3) | 15 (0.8) | 339 (6.9) |
| Russian Federation |  | 48 (1.3) | 540 (4.7) | 46 (1.2) | 532 (7.0) | 6 (0.6) | 479 (9.3) |
| Philippines | $s$ | 48 (0.9) | 363 (6.3) | 45 (0.9) | 370 (6.4) | 7 (0.5) | 315 (8.1) |
| Indonesia |  | 47 (1.4) | 413 (5.5) | 43 (1.0) | 408 (5.3) | 11 (0.8) | 392 (8.1) |
| Thailand |  | 45 (1.2) | 482 (5.6) | 47 (1.0) | 463 (5.6) | 8 (0.5) | 428 (6.0) |
| Bulgaria |  | 45 (1.5) | 526 (6.8) | 40 (1.0) | 516 (5.7) | 15 (1.2) | 491 (7.4) |
| South Africa | s | 44 (1.3) | 288 (8.1) | 41 (0.7) | 304 (11.2) | 15 (1.1) | 258 (7.7) |
| Belgium (Flemish) |  | 41 (1.3) | 554 (3.3) | 52 (1.1) | 571 (3.8) | 7 (1.0) | 516 (16.4) |
| Hungary |  | 40 (1.3) | 534 (4.1) | 52 (1.1) | 539 (4.2) | 8 (0.6) | 489 (7.8) |
| Latvia (LSS) |  | 40 (1.2) | 499 (4.2) | 54 (1.2) | 516 (4.0) | 6 (0.5) | 484 (9.3) |
| Cyprus |  | 35 (1.1) | 479 (2.8) | 51 (1.1) | 495 (2.3) | 14 (0.7) | 431 (6.4) |
| Lithuania * |  | 35 (1.2) | 492 (4.8) | 57 (1.2) | 485 (4.4) | 8 (0.8) | 443 (10.1) |
| Israel |  | 35 (1.5) | 456 (5.2) | 53 (1.2) | 488 (3.2) | 12 (0.8) | 471 (7.9) |
| Slovenia |  | 32 (1.0) | 514 (3.8) | 55 (0.9) | 543 (3.1) | 13 (0.8) | 530 (5.7) |
| Chile |  | 29 (0.9) | 397 (6.9) | 51 (0.7) | 403 (5.1) | 20 (0.8) | 389 (5.4) |
| Slovak Republic |  | 24 (0.9) | 522 (4.3) | 65 (1.1) | 541 (4.1) | 10 (0.7) | 536 (7.3) |
| Canada |  | 24 (0.8) | 516 (3.5) | 59 (1.0) | 540 (2.8) | 18 (0.8) | 528 (4.1) |
| Chinese Taipei |  | 23 (1.0) | 625 (4.5) | 42 (0.8) | 602 (3.9) | 35 (1.3) | 542 (4.4) |
| United States |  | 22 (0.8) | 508 (4.8) | 56 (0.9) | 517 (4.1) | 23 (1.3) | 477 (3.9) |
| Netherlands |  | 19 (1.4) | 521 (11.5) | 74 (1.3) | 548 (6.5) | 7 (1.0) | 529 (12.8) |
| Australia |  | 17 (0.9) | 518 (6.0) | 61 (1.4) | 539 (5.0) | 22 (1.4) | 497 (5.6) |
| New Zealand |  | 17 (1.0) | 488 (6.8) | 63 (1.3) | 511 (5.2) | 20 (1.2) | 449 (5.4) |
| Japan |  | 17 (0.9) | 586 (2.9) | 49 (0.9) | 587 (2.1) | 35 (1.3) | 564 (3.1) |
| Hong Kong, SAR |  | 16 (0.8) | 600 (5.3) | 42 (0.9) | 595 (3.9) | 42 (1.4) | 564 (5.0) |
| Czech Republic |  | 16 (1.1) | 500 (5.7) | 62 (1.4) | 527 (4.7) | 22 (1.3) | 519 (6.5) |
| Korea, Rep. of |  | 16 (0.7) | 612 (4.3) | 43 (0.7) | 601 (2.5) | 41 (1.0) | 565 (2.5) |
| Finland |  | 9 (0.7) | 498 (6.6) | 82 (1.0) | 525 (2.6) | $9(0.8)$ | 512 (6.2) |
| England |  | - - | - - | - - | - - | - - | - - |
| International Avg. |  | 38 (0.2) | 492 (0.9) | 48 (0.2) | 497 (0.8) | 14 (0.1) | 463 (1.6) |

[^25]A dash $(-)$ indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate. An " $s$ " indicates a $50-69 \%$ student response rate.


|  | HighOSTPercent of Students |  |  |  | MediumOSTPercent of Students |  |  |  | Low OST Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 <br> Difference |  | 1995 | 1999 | 1995-1999 <br> Differenc |  | 1995 | 1999 | 1995-1999 Differenc |  |
| Australia | 16 (0.7) | 17 (0.9) | 1 (1.1) |  | 58 (1.1) | 61 (1.4) | 2 (1.7) | - | 26 (1.2) | 22 (1.4) | -3 (1.9) | - |
| Belgium (Flemish) | 42 (1.6) | 41 (1.3) | -1 (2.0) | - | 52 (1.3) | 52 (1.1) | -1 (1.7) | - | 6 (0.7) | 7 (1.0) | 1 (1.2) | - |
| Canada | 19 (0.9) | 24 (0.8) | 4 (1.3) | $\triangle$ | 55 (1.2) | 59 (1.0) | 4 (1.6) | - | 26 (1.5) | 18 (0.8) | -8 (1.7) | V |
| Cyprus | 41 (0.9) | 35 (1.1) | -5 (1.4) | $\nabla$ | 44 (0.9) | 51 (1.1) | 7 (1.4) | $\triangle$ | 15 (0.8) | 14 (0.7) | -2 (1.0) | - |
| Czech Republic | 13 (0.7) | 16 (1.1) | 3 (1.3) | - | 60 (1.3) | 62 (1.4) | 2 (1.9) | - | 27 (1.6) | 22 (1.3) | -5 (2.1) | $\bullet$ |
| England | - - | - - | - - |  | - - | - - | - - |  | - - | - - | - - |  |
| Hong Kong, SAR | 28 (1.1) | 16 (0.8) | -12 (1.4) | $\nabla$ | 50 (1.0) | 42 (0.9) | -8 (1.4) | V | 22 (1.4) | 42 (1.4) | 20 (2.0) | $\triangle$ |
| Hungary | 39 (1.4) | 40 (1.3) | 2 (1.9) | - | 53 (1.3) | 52 (1.1) | 0 (1.7) | $\bullet$ | 9 (0.7) | 8 (0.6) | -1 (0.9) | - |
| Iran, Islamic Rep. s | 74 (1.6) | 69 (1.1) | -4 (1.9) | - | 24 (1.4) | 27 (0.9) | 3 (1.7) | - | 3 (0.4) | 4 (0.4) | 2 (0.6) | - |
| Israel ${ }^{\dagger}$ | 31 (1.9) | 33 (1.7) | 2 (2.5) | - | 54 (1.7) | 55 (1.4) | 1 (2.2) | - | 14 (1.3) | 12 (0.9) | -3 (1.6) | - |
| Italy | 60 (1.6) | 60 (1.6) | 0 (2.2) | - | 34 (1.4) | 34 (1.4) | 1 (2.0) | - | 6 (0.7) | 6 (0.7) | -1 (1.0) | - |
| Japan | 27 (1.0) | 17 (0.9) | -10 (1.3) | $\nabla$ | 52 (0.9) | 49 (0.9) | -3 (1.3) | - | 21 (1.1) | 35 (1.3) | 14 (1.7) | - |
| Korea, Rep. of | 27 (1.2) | 16 (0.7) | -11 (1.4) | $\nabla$ | 50 (1.1) | 43 (0.7) | -6 (1.3) | V | 24 (1.0) | 41 (1.0) | 17 (1.4) | - |
| Latvia (LSS) | 26 (1.2) | 40 (1.2) | 13 (1.6) | $\triangle$ | 60 (1.3) | 54 (1.2) | -5 (1.7) | $\nabla$ | 14 (1.0) | 6 (0.5) | -8 (1.2) | V |
| Lithuania | 26 (1.4) | 35 (1.2) | 10 (1.8) | $\triangle$ | 60 (1.3) | 57 (1.2) | -3 (1.8) | - | 15 (1.0) | 8 (0.8) | -7 (1.3) | - |
| Netherlands | 16 (0.8) | 19 (1.4) | 3 (1.6) | $\bullet$ | 76 (1.2) | 74 (1.3) | -2 (1.7) | - | 8 (1.0) | 7 (1.0) | -1 (1.4) | - |
| New Zealand | 16 (0.8) | 17 (1.0) | 1 (1.3) | - | 64 (1.2) | 63 (1.3) | -1 (1.8) | - | 21 (1.2) | 20 (1.2) | -1 (1.7) | - |
| Romania | 51 (1.5) | 55 (1.6) | 4 (2.2) | - | 28 (1.1) | 33 (1.1) | 5 (1.6) | - | 21 (1.3) | 12 (1.0) | -9 (1.7) | V |
| Russian Federation | 36 (1.4) | 48 (1.3) | 13 (1.9) | $\triangle$ | 54 (1.4) | 46 (1.2) | -8 (1.8) | $\nabla$ | 10 (0.7) | 6 (0.6) | -4 (0.9) | $\nabla$ |
| Singapore | 76 (1.0) | 59 (1.2) | -18 (1.5) | $\checkmark$ | 21 (0.8) | 35 (0.9) | 14 (1.3) | - | 3 (0.4) | 7 (0.6) | 4 (0.7) | $\triangle$ |
| Slovak Republic | 22 (0.9) | 24 (0.9) | 2 (1.3) | - | 64 (1.1) | 65 (1.1) | 2 (1.5) | - | 14 (1.0) | 10 (0.7) | -4 (1.2) | V |
| Slovenia | 35 (1.0) | 32 (1.0) | -3 (1.4) | - | 53 (1.0) | 55 (0.9) | 2 (1.4) | - | 12 (0.7) | 13 (0.8) | 1 (1.1) | - |
| Thailand ${ }^{+}$ | 51 (1.6) | 45 (1.2) | -6 (2.0) | $\nabla$ | 43 (1.3) | 47 (1.0) | 4 (1.6) | - | 6 (0.5) | 8 (0.5) | 2 (0.7) | $\triangle$ |
| United States | 22 (0.8) | 22 (0.8) | 0 (1.1) | - | 54 (1.1) | 56 (0.9) | 2 (1.5) | - | 25 (1.3) | 23 (1.3) | -2 (1.8) | - |
| International Avg. ${ }^{\text {§ }}$ | 34 (0.3) | 33 (0.2) | 0 (0.4) | $\bigcirc$ | 51 (0.3) | 51 (0.2) | 0 (0.4) | - | 15 (0.2) | 16 (0.2) | 0 (0.3) | - |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999

V 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by students.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below $65 \%$ in 1995 and 1999, Latvia is annotated LSS for Latvian Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An " r " indicates a 70-84\% student response rate, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates a $50-69 \%$ student response rate, based on the lower response rate in either 1995 or 1999.

|  | One Hour or More |  | Less Than One Hour |  | No Time |  | Average Hours ${ }^{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |  |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{aligned} & 22(1.0) \\ & 47 \\ & 47 \\ & 43 \\ & (1.2) \\ & 28 \\ & 28 \\ & 29 \end{aligned}(1.0)$ | $\begin{aligned} & 515 \text { (6.3) } \\ & 550 \\ & 521 \\ & 521 \\ & \text { (7.1) } \\ & 510 \\ & 394 \\ & 39.3) \\ & (7.1) \end{aligned}$ | $\begin{array}{ll} 63 & (1.1) \\ 50 & (1.0) \\ 45 & (1.3) \\ 61 & (1.0) \\ 54 & (0.7) \end{array}$ | $\begin{aligned} & 537(5.0) \\ & 573(3.7) \\ & 516(5.5) \\ & 542(2.8) \\ & 400(4.7) \end{aligned}$ | $\begin{array}{r} 15(1.0) \\ 3(0.8) \\ 12(1.2) \\ 11(0.8) \\ 17 \end{array}(0.8)$ | $\begin{aligned} & 493 \text { (6.3) } \\ & 476 \text { (21.2) } \\ & 494(9.5) \\ & 527(5.2) \\ & 384(5.9) \end{aligned}$ | $\begin{array}{ll} 0.7 & (0.02) \\ 1.1 & (0.03) \\ 1.1 & (0.04) \\ 0.8 & (0.02) \\ 0.9 & (0.02) \end{array}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{cc} 25 & (1.0) \\ 40 & (1.1) \\ 20(1.1) \\ -- \\ 8(0.7) \end{array}$ | $\begin{gathered} 627(4.7) \\ 469(2.4) \\ 493(5.2) \\ -- \\ 486(6.8) \end{gathered}$ | 44 (0.8) <br> 51 (1.1) <br> 68 (1.3) <br> 85 (0.8) | 604 (3.5) <br> 496 (2.7) <br> 528 (4.6) <br> 525 (2.5) | $\begin{array}{r} 31(1.3) \\ 9(0.6) \\ 12(1.0) \\ -- \\ 7(0.6) \end{array}$ | 529 (4.8) <br> 425 (7.2) <br> 525 (9.2) <br> 506 (8.1) | $\begin{array}{cc} 0.7 & (0.02) \\ 1.1 & (0.03) \\ 0.7 & (0.02) \\ -- \\ 0.6 & (0.01) \end{array}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{ll} 24 & (1.1) \\ 25 & (1.1) \\ 51 & (1.4) \\ 75 & (1.0) \\ 44 & (1.4) \end{array}$ | $\begin{aligned} & 600(4.8) \\ & 514(5.0) \\ & 406(5.4) \\ & 427(3.7) \\ & 454(4.3) \end{aligned}$ | $\begin{array}{ll} 51 & (0.9) \\ 71 & (1.0) \\ 38 & (1.0) \\ 22 & (0.8) \\ 48 & (1.1) \end{array}$ | $\begin{aligned} & 591(3.9) \\ & 540(3.6) \\ & 405(5.6) \\ & 425(3.7) \\ & 491(4.2) \end{aligned}$ | $\begin{array}{r} 25(1.2) \\ 4(0.4) \\ 10(0.8) \\ 3(0.3) \\ 8(0.6) \end{array}$ | $\begin{aligned} & 552 \text { (6.1) } \\ & 497 \text { (9.9) } \\ & 396 \text { (8.4) } \\ & 375 \text { (14.1) } \\ & 436 \text { (11.3) } \end{aligned}$ | $\begin{array}{ll} 0.7 & (0.02) \\ 0.8 & (0.02) \\ 1.2 & (0.03) \\ 1.9 & (0.03) \\ 1.1 & (0.03) \end{array}$ |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 57 & (1.3) \\ 20 & (0.9) \\ 60 & (1.0) \\ 21 & (0.9) \\ 40 & (1.3) \end{array}$ | 482 (4.0) 585 (2.5) 445 (4.3) 610 (4.1) 493 (4.1) | 39 (1.2) <br> 54 (0.9) <br> 33 (0.8) <br> 45 (0.7) <br> 58 (1.3) | 488 (4.5) <br> 586 (2.0) <br> 441 (4.6) <br> 598 (2.0) <br> 516 (4.1) | $\begin{array}{r} 5(0.5) \\ 26(1.2) \\ 8(0.6) \\ 34(1.0) \\ 3(0.4) \end{array}$ | $400(9.5)$ $558(3.8)$ $374(9.8)$ $560(2.6)$ $480(13.8)$ | $\begin{array}{ll} 1.3 & (0.03) \\ 0.6 & (0.01) \\ 1.7 & (0.03) \\ 0.6 & (0.02) \\ 1.0 & (0.02) \end{array}$ |
| Lithuania ${ }^{\text {* }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{ll} 29 & (1.3) \\ 45 & (1.2) \\ 71 & (1.0) \\ 44 & (1.6) \\ 58 & (1.5) \end{array}$ | 483 (5.3) <br> 448 (4.1) <br> 519 (4.2) <br> 473 (5.0) <br> 350 (3.2) | $\begin{array}{ll} 68 & (1.4) \\ 49 & (1.1) \\ 28 & (0.9) \\ 48 & (1.4) \\ 29 & (0.9) \end{array}$ | 486 (4.4) <br> 461 (4.6) <br> 523 (6.5) <br> 476 (4.1) <br> 341 (6.6) | $\begin{array}{r} 3(0.5) \\ 6(0.4) \\ 2(0.2) \\ 8(0.7) \\ 13(0.9) \end{array}$ | $\begin{gathered} 417 \text { (15.8) } \\ 429(9.2) \\ \sim \sim \\ 452(7.6) \\ 324(8.0) \end{gathered}$ | $\begin{array}{ll} 0.9 & (0.03) \\ 1.2 & (0.03) \\ 1.6 & (0.02) \\ 1.1 & (0.03) \\ 1.7 & (0.07) \end{array}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{ll} 14 & (1.5) \\ 20 & (1.2) \\ 53 & (0.8) \\ 66 & (1.8) \\ 45 & (1.5) \end{array}$ | $\begin{array}{ll} 507 & (12.2) \\ 480 & (6.6) \\ 347 & (6.7) \\ 494 & (5.4) \\ 530 & (5.2) \end{array}$ | $\begin{array}{ll} 78 & (1.3) \\ 66 & (1.2) \\ 42 & (0.8) \\ 25 & (1.5) \\ 49 & (1.3) \end{array}$ | $\begin{aligned} & 546(6.7) \\ & 507(5.3) \\ & 363(6.2) \\ & 457(6.2) \\ & 537(6.7) \end{aligned}$ | 8 (1.1) <br> 14 (0.9) <br> 5 (0.4) <br> 9 (0.7) <br> 6 (0.5) | $\begin{aligned} & 559 \text { (14.0) } \\ & 444 \text { (6.7) } \\ & 288 \text { (13.2) } \\ & 417 \text { (7.7) } \\ & 483(10.0) \end{aligned}$ | $\begin{array}{ll} 0.6 & (0.02) \\ 0.7 & (0.02) \\ 1.7 & (0.04) \\ 1.6 & (0.05) \\ 1.1 & (0.03) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | 61 (1.1) <br> 23 (0.9) <br> 29 (1.0) <br> 53 (1.1) <br> 49 (1.2) | $\begin{aligned} & 604(5.7) \\ & 513(4.7) \\ & 511(4.1) \\ & 273(7.9) \\ & 482(5.8) \end{aligned}$ | $\begin{array}{ll} 34 & (1.0) \\ 70 & (0.8) \\ 63 & (1.1) \\ 37 & (0.7) \\ 45 & (1.1) \end{array}$ | $\begin{aligned} & 612(7.6) \\ & 542(3.9) \\ & 541(3.3) \\ & 293(8.6) \\ & 459(5.8) \end{aligned}$ | $\begin{array}{r} 5(0.5) \\ 6(0.6) \\ 8(0.7) \\ 10(0.8) \\ 6(0.4) \end{array}$ | $\begin{aligned} & 562(10.7) \\ & 535 \text { (8.3) } \\ & 530(7.7) \\ & 241 \text { (14.1) } \\ & 424(5.6) \end{aligned}$ | $\begin{array}{ll} 1.3 & (0.02) \\ 0.8 & (0.02) \\ 0.8 & (0.02) \\ 1.8 & (0.04) \\ 1.1 & (0.02) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 66(0.9) \\ & 52(1.4) \\ & 27(1.1) \end{aligned}$ | $\begin{aligned} & 450(2.9) \\ & 448(4.7) \\ & 505 \text { (4.5) } \end{aligned}$ | 27 (0.8) <br> 41 (1.0) <br> 58 (0.7) | $\begin{aligned} & 452(3.4) \\ & 422(4.4) \\ & 514(4.0) \end{aligned}$ | $\begin{array}{r} 7(0.5) \\ 6(0.6) \\ 15(1.1) \end{array}$ | $\begin{aligned} & 439(5.3) \\ & 398(7.1) \\ & 466(4.8) \end{aligned}$ | $\begin{array}{ll} 1.8 & (0.03) \\ 1.2 & (0.02) \\ 0.8 & (0.02) \end{array}$ |
| International Avg. | 40 (0.2) | 486 (0.9) | 50 (0.2) | 495 (0.8) | 10 (0.1) | 455 (1.7) | 1.1 (0.00) |

[^26]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement. An "r" indicates a $70-84 \%$ student response rate.

## How Do Students Perceive Their Ability in Mathematics?

To investigate how students think of their abilities in mathematics, TIMss created an index of students' self-concept in mathematics (SCm). This index is based on student's responses to five statements about their mathematics ability:

- I would like mathematics much more if it were not so difficult
- Although I do my best, mathematics is more difficult for me than for many of my classmates
- Nobody can be good in every subject, and I am just not talented in mathematics
- Sometimes when I do not understand a new topic in mathematics initially, I know that I will never really understand it
- Mathematics is not one of my strengths.

Students who disagreed or strongly disagreed with all five statements were assigned to the high level of the index, while students who agreed or strongly agreed with all five were assigned to the low level. The medium level includes all other possible combinations of responses. (As an example of one of the components of the index, Exhibit R1.14 in the reference section provides the percentages of disagreement and agreement in relation to mathematics achievement for the statement "mathematics is not one of my strengths.")

The percentages of eighth-grade students at each level of this index, and their average mathematics achievement, are presented in Exhibit 4.8. On average internationally, 18 percent of students had a high self-concept in mathematics. The percentages ranged from a high of 45 percent in the Russian Federation to a low of less than five percent in Indonesia, the Philippines, and Thailand. Although there was a clear positive association between self-concept and mathematics achievement internationally and in every country, at the country level the relationship was more complex. Several countries with high average mathematics achievement, including Singapore, Hong Kong, Chinese Taipei, Korea, and Japan, had 15 percent or less of their students in the high self-concept category. Since all of these are Asian Pacific countries, they may share cultural traditions that encourage a modest self-concept. Also, it may be that their rigorous math-
ematics curricula pose a greater challenge to students. Internationally on average, about ${ }_{15}$ percent of the eighth-grade students seem to be convinced that they just cannot do mathematics. They may think they can be good with numbers or with words, but not both. Mathematics to them may seem dry and unimportant to daily life.

Exhibit 4.9 presents the percentages of girls and of boys in each country at the high, medium, and low levels of the mathematics self-concept index. Even though the gender differences in timss mathematics achievement were negligible at the eighth grade in both 1995 and 1999, there was a modest but statistically significant difference favoring boys internationally, especially at the upper quartile within each country (see Exhibit 1.12). Moreover, detailed analyses of the 1995 data showed that gender differences favoring males emerged in several countries during the final year of secondary school. ${ }^{3}$ Therefore, it may not be that surprising to find differences in mathematics self-concept between boys and girls at the eighth grade, internationally and in some countries.

Significantly more boys than girls had a high mathematics self-concept in Canada, Chinese Taipei, the Czech Republic, England, Finland, Hong Kong, Japan, Korea, the Netherlands, and the United States. Conversely, significantly more girls than boys had a low self-concept in Belgium (Flemish), Japan, Morocco, and Tunisia.

3 Mullis, I.V.S., Martin, M.O., Fierros, E.G., Goldberg, A.L., and Stemler, S.E. (2000), Gender Differences in Achievement: IEA's Third International Mathematics and Science Study, Chestnut Hill, MA: Boston College.

Exhibit 4.8 Index of Students' Self-Concept in Mathematics (SCM)


Index based on students' responses to five statements about their mathematics ability: 1) I would like mathematics much more if it were not so difficult; 2) although I do my best, mathematics is more difficult for me than for many of my classmates; 3) nobody can be good in every subject, and I am just not talented in mathematics; 4) sometimes, when I do not understand a new topic in mathematics initially, I know that I will never really understand it; 5) mathematics is not one of my strengths. High level indicates student disagrees or strongly disagrees with all five statements. Low level indicates student agrees or strongly agrees with all five statements. Medium level includes all other possible combinations of responses.

|  | High <br> SCM |  | Medium SCM |  | Low <br> SCM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Russian Federation <br> Canada <br> Finland <br> United States Australia | 45 (1.5) <br> 35 (1.0) <br> 32 (1.2) <br> 31 (1.0) <br> 30 (1.2) | $\begin{aligned} & 568(4.7) \\ & 573(2.9) \\ & 566(3.5) \\ & 551(4.6) \\ & 571(4.7) \end{aligned}$ | $\begin{aligned} & 44(1.1) \\ & 56(1.0) \\ & 55(1.2) \\ & 58(0.8) \\ & 57(1.0) \end{aligned}$ | $\begin{aligned} & 510(6.5) \\ & 517(2.4) \\ & 509(2.7) \\ & 493(3.9) \\ & 517(5.0) \end{aligned}$ | $\begin{array}{r} 11(0.8) \\ 9(0.5) \\ 14(0.8) \\ 11(0.6) \\ 13(0.7) \end{array}$ | $\begin{aligned} & 470(10.9) \\ & 459(6.1) \\ & 465(4.2) \\ & 435(5.6) \\ & 458(5.4) \end{aligned}$ |
| England Hungary New Zealand Israel Netherlands | $\begin{array}{ll} 30 & (1.3) \\ 28 & (1.0) \\ 27 & (1.3) \\ 27 & (1.0) \\ 27 & (2.0) \end{array}$ | 543 (5.0) <br> 589 (4.8) <br> 556 (5.4) <br> 523 (5.2) <br> 578 (7.0) | $\begin{aligned} & 61(1.2) \\ & 60(1.0) \\ & 59(1.1) \\ & 63(0.9) \\ & 65(1.8) \end{aligned}$ | $\begin{aligned} & 487(3.9) \\ & 522(3.6) \\ & 482(4.4) \\ & 460(3.7) \\ & 532(7.7) \end{aligned}$ | $\begin{array}{r} 9(0.6) \\ 13(0.7) \\ 14(0.8) \\ 10(0.6) \\ 8(0.9) \end{array}$ | $\begin{aligned} & 430(6.5) \\ & 459(5.1) \\ & 418(4.8) \\ & 390(7.8) \\ & 490(9.8) \end{aligned}$ |
| Belgium (Flemish) <br> Italy <br> Slovenia <br> Slovak Republic <br> Czech Republic | $\begin{array}{ll} 25 & (0.8) \\ 24 & (0.9) \\ 21 & (0.9) \\ 20 & (1.1) \\ 19 & (1.2) \end{array}$ | $\begin{aligned} & 600(5.4) \\ & 539(3.8) \\ & 593(4.3) \\ & 587(5.2) \\ & 585(5.7) \end{aligned}$ | 62 (0.8) <br> 63 (0.9) <br> 69 (0.9) <br> 62 (0.9) <br> 66 (1.0) | 554 (3.3) 474 (3.8) 523 (2.7) 535 (3.6) 515 (4.0) | 13 (1.1) <br> 13 (0.8) <br> 10 (0.6) <br> 18 (1.0) <br> 15 (1.0) | $\begin{aligned} & 506(7.8) \\ & 412(5.4) \\ & 457(5.5) \\ & 479(3.7) \\ & 461(5.5) \end{aligned}$ |
| Malaysia Lithuania ${ }^{\text { }}$ Turkey Latvia (LSS) Bulgaria | $\begin{aligned} & 19(1.0) \\ & 18(1.3) \\ & 18(0.7) \\ & 18(0.9) \\ & 17(2.4) \end{aligned}$ | $\begin{aligned} & 567(5.5) \\ & 543(6.7) \\ & 488(5.8) \\ & 566(4.9) \\ & 578(9.8) \end{aligned}$ | $\begin{aligned} & 77(0.9) \\ & 69(1.2) \\ & 62(0.7) \\ & 63(1.0) \\ & 61(1.7) \end{aligned}$ | 511 (4.0) 479 (3.8) 430 (4.1) 505 (3.8) 514 (4.7) | $\begin{array}{r} 5(0.4) \\ 13(0.9) \\ 19(0.7) \\ 19(0.8) \\ 22(1.5) \end{array}$ | 466 (5.8) <br> 418 (5.8) <br> 399 (4.6) <br> 453 (4.6) <br> 468 (6.2) |
| Macedonia, Rep. of Cyprus Singapore Hong Kong, SAR Iran, Islamic Rep. | $\begin{aligned} & 16(0.8) \\ & 16(0.8) \\ & 15(1.0) \\ & 14(0.7) \\ & 14(0.7) \end{aligned}$ | $\begin{aligned} & 517(6.5) \\ & 539(3.6) \\ & 656(8.8) \\ & 624(4.6) \\ & 482(5.2) \end{aligned}$ | $\begin{array}{ll} 63 & (0.9) \\ 68 & (0.8) \\ 74 & (0.8) \\ 71 & (0.8) \\ 71 & (0.8) \end{array}$ | $\begin{aligned} & 454(4.1) \\ & 478(2.0) \\ & 603(5.7) \\ & 585(3.8) \\ & 423(3.4) \end{aligned}$ | $\begin{aligned} & 21(0.9) \\ & 16(0.9) \\ & 11(0.7) \\ & 14(0.8) \\ & 15(0.7) \end{aligned}$ | $\begin{aligned} & 406(5.2) \\ & 421(4.4) \\ & 547(7.1) \\ & 531(6.3) \\ & 380(4.2) \end{aligned}$ |
| Tunisia Moldova Jordan Chile Chinese Taipei | $\begin{array}{ll} 14 & (0.6) \\ 13 & (0.9) \\ 12 & (0.6) \\ 11 & (0.7) \\ 11 & (0.5) \end{array}$ | $\begin{aligned} & 488(4.6) \\ & 518(6.3) \\ & 517(6.1) \\ & 466(9.5) \\ & 660(6.0) \end{aligned}$ | 69 (0.7) <br> 67 (1.1) <br> 66 (0.8) <br> 68 (0.8) <br> 75 (0.7) | 447 (2.6) <br> 472 (4.5) <br> 438 (3.9) <br> 398 (3.8) <br> 591 (3.9) | $\begin{array}{ll} 17 & (0.6) \\ 20 & (1.1) \\ 22 & (0.8) \\ 21 & (0.9) \\ 14 & (0.7) \end{array}$ | $\begin{aligned} & 424(3.1) \\ & 446(5.2) \\ & 388(4.4) \\ & 347(5.4) \\ & 506(4.2) \end{aligned}$ |
| Romania Korea, Rep. of South Africa Japan Morocco | $\begin{array}{r} 10(0.7) \\ 10(0.5) \\ 7(0.7) \\ 6(0.4) \\ 5(0.4) \end{array}$ | $\begin{aligned} & 539(7.5) \\ & 646(4.0) \\ & 392(12.7) \\ & 634(6.2) \\ & 405(9.8) \end{aligned}$ | 62 (1.1) 85 (0.5) 67 (0.9) 82 (0.5) 74 (0.8) | $\begin{aligned} & 483(5.2) \\ & 585(1.8) \\ & 279(7.2) \\ & 581(1.8) \\ & 344(3.0) \end{aligned}$ | $\begin{array}{r} 27(1.4) \\ 5(0.3) \\ 26(0.9) \\ 12(0.5) \\ 21(0.7) \end{array}$ | 441 (6.8) <br> 515 (5.7) <br> 239 (5.5) <br> 536 (3.8) <br> 319 (6.9) |
| Indonesia Philippines Thailand | $\begin{aligned} & 4(0.4) \\ & 4(0.5) \\ & 2(0.2) \end{aligned}$ | $\begin{aligned} & 470 \text { (10.1) } \\ & 411 \text { (13.2) } \end{aligned}$ | $\begin{array}{ll} 83 & (0.6) \\ 77 & (0.7) \\ 79 & (0.6) \end{array}$ | $\begin{aligned} & 407(4.8) \\ & 353(6.1) \\ & 474(5.0) \end{aligned}$ | $\begin{aligned} & 13(0.6) \\ & 19(0.7) \\ & 19 \\ & (0.7) \end{aligned}$ | $\begin{aligned} & 366(7.1) \\ & 320(5.3) \\ & 434(6.1) \end{aligned}$ |
| International Avg. | 18 (0.2) | 547 (1.1) | 67 (0.2) | 486 (0.7) | 15 (0.1) | 436 (0.9) |

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates a $70-84 \%$ student response rate.


|  | HighSCMPercent of Students |  |  | Medium SCM Percent of Students |  |  | LowSCMPercent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girls | Boys |  | Girls |  | Boys | Girls |  | Boys |  |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 28 & (1.5) \\ 24 & (1.3) \\ 17 & (2.3) \\ 31 & (1.4) \\ 10 & (0.7) \end{array}$ | $33 \text { (1.5) }$ <br> 26 (1.2) <br> 17 (3.0) <br> 39 (1.1) <br> 13 (1.0) | - | 59 (1.4) <br> 61 (1.5) <br> 62 (2.2) <br> 59 (1.6) <br> 68 (0.9) | ^ | $\begin{aligned} & 55(1.3) \\ & 63(1.2) \\ & 60(1.8) \\ & 52(1.0) \\ & 67(1.0) \end{aligned}$ | $\begin{array}{r} 14(1.0) \\ 16(1.4) \\ 21(1.9) \\ 9(0.7) \\ 22(1.1) \end{array}$ | - | $\begin{array}{r} 12 \\ 11 \\ \hline 10.9) \\ 23 \\ (1.1) \\ 9 \\ (2.2) \\ 20 \end{array}(1.5)$ |  |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{r} 7(0.5) \\ 17(1.1) \\ 16 \text { (1.3) } \\ 24(1.5) \\ 23(1.1) \end{array}$ | $\begin{array}{ll} 14 & (0.8) \\ 15 & (1.0) \\ 22 & (1.5) \\ 36 & (1.8) \\ 40 & (1.7) \end{array}$ |  | 79 (0.8) <br> 68 (1.1) <br> 69 (1.3) <br> 65 (1.5) <br> 62 (1.5) | $\pm$ | $\begin{array}{ll} 72 & (1.0) \\ 68 & (1.0) \\ 63 & (1.3) \\ 57 & (1.7) \\ 48 & (1.5) \end{array}$ | 14 (0.8) <br> 15 (1.3) <br> 15 (1.0) <br> 11 (1.0) <br> 16 (1.3) |  | $\begin{array}{r} 14(0.9) \\ 17(1.0) \\ 15(1.5) \\ 7(0.7) \\ 12(0.9) \end{array}$ |  |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 11(0.9) \\ 27(1.3) \\ 4(0.5) \\ 14(0.7) \\ 26(1.1) \end{array}$ | $\begin{array}{r} 18(0.9) \\ 29(1.5) \\ 5(0.5) \\ 14(1.1) \\ 29(1.4) \end{array}$ | - | $\begin{aligned} & 74(1.2) \\ & 60(1.4) \\ & 83 \\ & \hline 3 \\ & 71 \\ & \hline 1 \end{aligned}(1.8)$ | 4 | $\begin{aligned} & 69(1.0) \\ & 59(1.5) \\ & 83 \\ & \hline 3 \\ & 71 \\ & 71 \\ & 62 \end{aligned}(1.8)$ | 15 (1.1) <br> 13 (1.0) <br> 13 (0.9) <br> 15 (1.1) <br> 10 (1.0) |  | $\begin{array}{r} 14(1.1) \\ 12(1.0) \\ 13(0.7) \\ 15(1.0) \\ 9 \end{array}(0.7)$ |  |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 22(1.1) \\ 3(0.4) \\ 12(0.9) \\ 7(0.6) \\ 17(1.2) \end{array}$ | $\begin{array}{r} 25(1.3) \\ 8(0.7) \\ 12(0.9) \\ 12(0.7) \\ 18 \end{array}(1.2)$ | - | 64 (1.3) <br> 80 (0.9) <br> 65 (1.3) <br> 87 (0.6) <br> 63 (1.5) | ^ | 63 (1.3) <br> 83 (0.9) <br> 67 (1.1) <br> 84 (0.7) <br> 63 (1.1) | $\begin{array}{r} 14(1.0) \\ 17(0.8) \\ 23(1.2) \\ 6(0.4) \\ 20(1.1) \end{array}$ | - | $\begin{array}{r} 13(1.0) \\ 8(0.5) \\ 21(1.2) \\ 4(0.4) \\ 18(1.1) \end{array}$ |  |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 18 \text { (1.6) } \\ 17 \text { (1.1) } \\ 20(1.0) \\ 13 \\ 5(1.1) \\ 5(0.7) \end{array}$ | 18 (1.5) <br> 16 (0.8) <br> 17 (1.2) <br> 13 (1.2) <br> 5 (0.4) |  | 69 (1.7) <br> 64 (1.3) <br> 76 (1.0) <br> 67 (1.3) <br> 71 (1.1) |  | $\begin{aligned} & 69(1.4) \\ & 62(1.3) \\ & 77(1.2) \\ & 68(1.6) \\ & 76(0.9) \end{aligned}$ | $\begin{array}{r} 12(1.2) \\ 19(1.1) \\ 4(0.4) \\ 20(1.3) \\ 24(1.0) \end{array}$ | $\triangle$ | $\begin{array}{r} 13(1.3) \\ 22(1.3) \\ 6(0.6) \\ 19(1.4) \\ 19 \end{array}(0.8)$ |  |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 21(2.1) \\ 27(1.6) \\ 4(0.5) \\ 9(0.8) \\ 48(1.8) \end{array}$ | $\begin{array}{r} 33(2.6) \\ 28(1.6) \\ 5(0.6) \\ 11(0.9) \\ 42 \end{array}(1.8)$ | - | $\begin{aligned} & 69(1.8) \\ & 59(1.4) \\ & 79 \\ & \hline 9 \\ & 64 \\ & \hline 0 \end{aligned}(1.9)$ |  | 61 (2.7) <br> 58 (1.3) <br> 75 (1.0) <br> 60 (1.5) <br> 45 (1.4) | $\begin{array}{ll} 10 & (1.2) \\ 14 & (1.0) \\ 18 & (1.0) \\ 27 & (1.6) \\ 10 & (0.9) \end{array}$ |  | $\begin{array}{rr} 6(1.0) \\ 14 & (1.1) \\ 20 & (0.9) \\ 28 & (1.6) \\ 13 & (1.0) \end{array}$ |  |
| Singapore Slovak Republic Slovenia South Africa Thailand | 13 (0.9) 19 (1.3) 21 (1.1) 6 (0.8) 2 (0.3) | $\begin{array}{r} 17 \\ 21(1.4) \\ 21 \\ 21 \\ (1.4) \\ 7 \\ (0.2) \\ 2 \end{array}(0.3)$ |  | $\begin{array}{ll} 77 & (0.9) \\ 63 & (1.3) \\ 70 & (1.2) \\ 66 & (1.0) \\ 82 & (0.7) \end{array}$ | $\triangle$ <br> 4 | $\begin{aligned} & 72(1.0) \\ & 62(1.4) \\ & 68(1.4) \\ & 68(1.2) \\ & 77(1.0) \end{aligned}$ | $\begin{array}{r} 11(0.8) \\ 18(1.2) \\ 9(0.9) \\ 28(1.2) \\ 16 \end{array}(0.7)$ |  | $\begin{array}{ll} 12 & (0.9) \\ 17 & (1.2) \\ 11 & (0.9) \\ 24 & (1.0) \\ 21 & (1.0) \end{array}$ | $\triangle$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 13(0.8) \\ & 17 \\ & 28 \\ & 28 \end{aligned}(1.8)$ | $\begin{aligned} & 14(0.8) \\ & 19(1.0) \\ & 34(1.2) \end{aligned}$ | - | $\begin{aligned} & 66(1.1) \\ & 63(1.3) \\ & 61(1.2) \end{aligned}$ | - | $\begin{aligned} & 71(0.9) \\ & 62(0.9) \\ & 54(1.0) \end{aligned}$ | $\begin{aligned} & 20(1.0) \\ & 20(1.1) \\ & 11(0.7) \end{aligned}$ | - | $\begin{aligned} & 14(0.8) \\ & 19(0.9) \\ & 11(0.7) \end{aligned}$ |  |
| International Avg. | 17 (0.2) | 20 (0.2) | - | 68 (0.2) | ^ | 66 (0.2) | 16 (0.2) | ^ | 15 (0.2) |  |

Significantly higher than other gender

Significance tests adjusted for multiple comparisons

## Background data provided by students.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

An "r" indicates a $70-84 \%$ student response rate.

## What Are Students' Attitudes Towards Mathematics?

Generating positive attitudes towards mathematics among students is an important goal of mathematics education in many countries. To gain some understanding about eighth-graders' view about the utility of mathematics and their enjoyment of it as a school subject, timss created an index of positive attitudes towards mathematics (patm). Students were asked to state their agreement with the following five statements:

- I like mathematics
- I enjoy learning mathematics
- Mathematics is boring ${ }^{4}$
- Mathematics is important to everyone's life
- I would like a job that involved using mathematics.

For each statement, students responded on a four-point scale indicating whether their feelings about mathematics were strongly positive, positive, negative, or strongly negative. The responses were averaged, with students being placed in the high category if their average indicated a positive or strongly positive attitude on average. Students with a negative or strongly negative attitude on average were placed in the low category. The students between these extremes were placed in the medium category. The results are presented in Exhibit 4.10. ${ }^{5}$

Eighth-grade students generally had positive attitudes towards mathematics, with 37 percent on average across countries in the high category, and a further $5^{2}$ percent in the medium category. Only 11 percent of students were in the low category. Countries with large percentages of students at the high level included Malaysia, Morocco, South Africa, the Philippines, Tunisia, Jordan, Iran, and Indonesia, with more than half the students in this category.

Students' attitudes towards any curriculum area can be related to their achievement in ways that reinforce higher or lower performance. That is, students who do well in mathematics generally have more positive attitudes towards the subject, and those who have more positive attitudes tend to perform better. Within nearly every country there was a clear association between attitudes and mathematics achievement, with students having more positive attitudes also having higher average achievement. As in previous findings, however, the two countries with the least positive attitudes were high-performing Japan and Korea. Again, it may be that the students follow a demanding mathematics cur-

[^27]riculum, one that leads to high achievement but little enthusiasm for mathematics.

Exhibit 4.11 presents the percentages of girls and boys in each country at each level of the positive attitudes towards mathematics index. There were significantly greater percentages of boys than girls with a high level of positive attitudes towards mathematics on average internationally and in a number of countries (i.e., Australia, Bulgaria, Canada, Chile, Chinese Taipei, England, Finland, Hong Kong, Japan, the Netherlands, Singapore, Tunisia, Turkey, and the United States). Only in the Philippines was there a significantly greater percentage of girls at the high level of the index.

Exhibit 4.12 provides information on trends in the index of positive attitudes towards mathematics from 1995 to 1999. There was little change overall or among the countries. Australia and Lithuania had increased percentages of students at the high index level in 1999, and Korea, Slovenia, and Thailand had decreases. At the low level, decreases were found in Hong Kong and Lithuania and increases in Japan and Korea.

Exhibit 4.13 displays trends from 1995 to 1999 in the percentages of girls and boys at the high level of the index. There was very little change over time in the relative attitudes of girls and boys towards mathematics; no country experienced a significant change, positive or negative, in the gender difference in attitudes. For Japan, Australia, the Netherlands, England, and Hong Kong, the gender differences favoring boys at the high level found in 1999 were also present in 1995. Italy and New Zealand had significant differences favoring boys in 1995 that no longer appeared in 1999. Conversely, however, for the United States, Canada, and Singapore, significant differences favoring boys in the high category of positive attitudes appeared in 1999 when none had existed in 1995 .


Exhibits 4.10-4.13 Overleaf

Exhibit 4.10 Index of Students' Positive Attitudes Towards Mathematics (PATM)


[^28]A tilde ( ) indicates insufficient data to report achievement
An " $r$ " indicates a $70-84 \%$ student response rate.


|  | High <br> PATM <br> Percent of Students |  |  | Medium PATM Percent of Students |  |  | Low <br> PATM <br> Percent of Students |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girls | Boys |  | Girls |  | Boys | Girls |  | Boys |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 26 & (1.5) \\ 24 & (1.4) \\ 31 & (2.3) \\ 31 & (1.1) \\ 39 & (1.5) \end{array}$ | $\begin{array}{ll} 34 & (1.5) \\ 26 & (1.7) \\ 42 & (2.9) \\ 38 & (1.2) \\ 51 & (1.6) \end{array}$ | - | $\begin{array}{ll} 57 & (1.4) \\ 53 & (1.8) \\ 54 & (1.7) \\ 53 & (1.4) \\ 51 & (1.3) \end{array}$ | $\pm$ | 53 (1.5) <br> 53 (1.4) <br> 47 (2.3) <br> 48 (1.1) <br> 43 (1.5) | $17 \text { (1.2) }$ <br> 23 (1.6) <br> 15 (1.9) <br> 15 (0.9) <br> 10 (0.6) | - | 13 (1.0) <br> 21 (1.3) <br> 11 (1.3) <br> 13 (0.9) <br> 6 (0.6) |
| Chinese Taipei Cyprus Czech Republic England Finland | 18 (0.9) <br> 51 (1.7) <br> 16 (1.5) <br> 35 (1.7) <br> 15 (1.1) | $\begin{array}{ll} 27 & (1.1) \\ 50 & (1.3) \\ 22 & (1.7) \\ 48 & (1.7) \\ 28 & (1.8) \end{array}$ | - | 61 (1.0) <br> 41 (1.5) <br> 64 (1.7) <br> 55 (1.5) <br> 61 (1.3) | - | 58 (1.0) <br> 41 (1.3) <br> 61 (1.4) <br> 47 (1.5) <br> 58 (1.6) | $\begin{array}{r} 21(0.9) \\ 7(0.8) \\ 20(1.4) \\ 10(0.8) \\ 24(1.6) \end{array}$ | - | $\begin{array}{r} 15(0.8) \\ 10(1.0) \\ 17 \\ (1.3) \\ 6 \end{array}(0.7)$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{ll} 22 & (1.1) \\ 18 & (1.3) \\ 51 & (1.6) \\ 54 & (1.5) \\ 42 & (1.8) \end{array}$ | $\begin{array}{ll} 34 & (1.2) \\ 20 & (1.2) \\ 51 & (1.6) \\ 54 & (1.6) \\ 47 & (1.6) \end{array}$ | $\triangle$ | 65 (1.0) <br> 66 (1.4) <br> 48 (1.6) <br> 40 (1.6) <br> 48 (1.5) | - | 57 (1.1) <br> 64 (1.3) <br> 48 (1.5) <br> 41 (1.4) <br> 43 (1.4) | $\begin{array}{r} 13(0.8) \\ 16(1.2) \\ 1(0.2) \\ 6(0.7) \\ 11(0.8) \end{array}$ | $\triangle$ | $\begin{array}{r} 8(0.6) \\ 16(1.2) \\ 1(0.3) \\ 6(0.6) \\ 10(0.9) \end{array}$ |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 33(1.6) \\ 6(0.5) \\ 50(1.8) \\ 8(0.6) \\ 25(1.4) \end{array}$ | 38 (1.4) <br> 13 (0.7) <br> 58 (1.7) <br> 10 (0.6) <br> 26 (1.6) | - | 52 (1.5) <br> 59 (1.0) <br> 40 (1.6) <br> 64 (1.2) <br> 65 (1.6) |  | 49 (1.4) <br> 64 (1.0) <br> 35 (1.4) <br> 66 (1.0) <br> 66 (1.6) | 15 (1.0) <br> 36 (1.2) <br> 9 (1.0) <br> 28 (1.3) <br> 10 (1.0) | - | $\begin{array}{r} 13(1.0) \\ 23(0.9) \\ 7(0.8) \\ 25(0.9) \\ 8(1.0) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{ll} 32 & (1.8) \\ 46 & (1.3) \\ 75 & (1.2) \\ 28 & (1.4) \\ 72 & (1.6) \end{array}$ | $\begin{array}{ll} 28 & (1.8) \\ 46 & (1.6) \\ 74 & (1.2) \\ 26 & (1.4) \\ 73 & (1.1) \end{array}$ |  | $\begin{array}{ll} 59 & (1.7) \\ 48 & (1.3) \\ 24 & (1.1) \\ 70 & (1.4) \\ 25 & (1.6) \end{array}$ |  | 64 (1.6) <br> 48 (1.4) <br> 26 (1.2) <br> 69 (1.4) <br> 25 (1.1) | $\begin{array}{ll} 8 & (0.9) \\ 7 & (0.6) \\ 1 & (0.2) \\ 2 & (0.4) \\ 2(0.3) \end{array}$ |  | $\begin{array}{ll} 8 & (0.8) \\ 7 & (0.6) \\ 1 & (0.2) \\ 5 & (0.6) \\ 2(0.4) \end{array}$ |
| Netherlands New Zealand Philippines Romania Russian Federation | 12 (1.5) <br> 32 (1.5) <br> 62 (1.4) <br> 35 (1.6) <br> 37 (1.6) | $\begin{array}{ll} 23 & (1.8) \\ 37 & (1.3) \\ 57 & (1.5) \\ 33 & (1.7) \\ 36 & (1.6) \end{array}$ | - | $\begin{array}{ll} 62 & (1.4) \\ 57 & (1.5) \\ 37 & (1.4) \\ 57 & (1.6) \\ 58 & (1.5) \end{array}$ |  | 63 (1.9) <br> 53 (1.4) <br> 40 (1.5) <br> 58 (1.5) <br> 59 (1.4) | $\begin{array}{r} 26(1.9) \\ 11(1.0) \\ 2(0.3) \\ 8(0.9) \\ 5(0.5) \end{array}$ | - | $\begin{array}{r} 14(1.4) \\ 10(1.0) \\ 3(0.3) \\ 9 \\ (1.0) \\ 5(0.6) \end{array}$ |
| Singapore <br> Slovak Republic <br> Slovenia South Africa Thailand | 41 (1.4) <br> 29 (1.6) <br> 18 (1.2) <br> 62 (1.1) <br> 37 (1.5) | 48 (1.4) <br> 32 (1.9) <br> 20 (1.2) <br> 62 (1.2) <br> 36 (1.3) | - | $\begin{array}{ll} 52 & (1.1) \\ 62 & (1.4) \\ 64 & (1.5) \\ 33 & (1.0) \\ 60 & (1.4) \end{array}$ | $\triangle$ | 45 (1.3) <br> 59 (1.8) <br> 62 (1.2) <br> 33 (1.1) <br> 61 (1.2) | $\begin{array}{r} 7(0.7) \\ 10(1.1) \\ 18(1.4) \\ 5(0.5) \\ 3(0.3) \end{array}$ |  | $\begin{array}{r} 7(0.7) \\ 8(1.0) \\ 18(1.2) \\ 4(0.4) \\ 3(0.3) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 51 & (1.3) \\ 38 & (1.3) \\ 32 & (1.3) \end{array}$ | $\begin{aligned} & 62(1.4) \\ & 44(1.2) \\ & 37(1.2) \end{aligned}$ | 4 $\Delta$ | $\begin{array}{ll} 38 & (1.2) \\ 53 & (1.2) \\ 52 & (1.1) \end{array}$ | - | $\begin{array}{ll} 32 & (1.1) \\ 51 & (1.0) \\ 46 & (0.9) \end{array}$ | $\begin{array}{r} 11(0.8) \\ 8(0.7) \\ 16(0.7) \end{array}$ | - | $\begin{array}{r} 5(0.6) \\ 6(0.5) \\ 16(1.1) \end{array}$ |
| International Avg. | 35 (0.2) | 39 (0.2) | - | 53 (0.2) | ^ | 51 (0.2) | 12 (0.2) | ^ | 10 (0.1) |

Significantly higher than other gender

Significance tests adjusted for multiple comparisons

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " r " indicates a 70-84\% student response rate.

|  | High <br> PATM <br> Percent of Students |  |  |  | Medium PATM Percent of Students |  |  |  | Low <br> PATM <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 <br> Differenc |  | 1995 | 1999 | 1995-1999 <br> Differenc |  | 1995 | 1999 | 1995-1999 <br> Differenc |  |
| Australia | 25 (0.9) | 30 (1.2) | 5 (1.5) | $\triangle$ | 57 (0.7) | 55 (1.2) | -2 (1.4) | - | 18 (0.7) | 15 (0.9) | -3 (1.1) | - |
| Belgium (Flemish) | 26 (1.1) | 25 (0.9) | -1 (1.5) | - | 54 (1.1) | 53 (0.9) | -1 (1.4) | - | 20 (0.8) | 22 (1.1) | 2 (1.3) | - |
| Canada | 36 (1.1) | 35 (0.9) | -1 (1.4) | - | 51 (0.9) | 51 (1.0) | 0 (1.3) | - | 13 (0.6) | 14 (0.7) | 1 (1.0) | - |
| Cyprus | 49 (1.4) | 50 (1.2) | 1 (1.8) | - | 42 (1.1) | 41 (1.1) | -1 (1.5) | - | 9 (0.7) | 9 (0.7) | -1 (1.0) | - |
| Czech Republic | 20 (1.1) | 19 (1.2) | -1 (1.6) | - | 63 (1.2) | 63 (1.2) | 0 (1.7) | - | 17 (1.1) | 18 (1.0) | 1 (1.5) | - |
| England | 41 (1.4) | 41 (1.3) | 0 (1.9) | - | 52 (1.3) | 51 (1.2) | -1 (1.7) | - | 7 (0.7) | 8 (0.5) | 1 (0.8) | - |
| Hong Kong, SAR | 24 (1.0) | 28 (0.9) | 4 (1.4) | - | 62 (1.0) | 61 (0.8) | 0 (1.3) | - | 14 (1.0) | 11 (0.6) | -4 (1.1) | $\checkmark$ |
| Hungary | 19 (0.8) | 19 (0.9) | 0 (1.2) | - | 66 (0.9) | 65 (1.0) | -1 (1.3) | - | 16 (0.9) | 16 (1.0) | 0 (1.3) | - |
| Iran, Islamic Rep. | 54 (1.6) | 54 (1.1) | -1 (1.9) | - | 39 (1.2) | 40 (1.0) | 1 (1.6) | $\bullet$ | 7 (0.7) | 6 (0.4) | -1 (0.8) | - |
| Israel ${ }^{\dagger}$ | 37 (2.0) | 43 (1.6) | 5 (2.6) | - | 51 (1.8) | 47 (1.4) | -4 (2.3) | - | 12 (1.5) | 10 (0.7) | -1 (1.6) | - |
| Italy | 40 (1.4) | 35 (1.4) | -5 (2.0) | - | 47 (1.1) | 51 (1.3) | 3 (1.7) | $\bullet$ | 13 (1.0) | 15 (1.1) | 2 (1.5) | - |
| Japan | 10 (0.5) | 9 (0.5) | -1 (0.7) | - | 69 (0.9) | 61 (0.7) | -8 (1.2) | $\nabla$ | 21 (1.0) | 29 (0.9) | 9 (1.3) | $\triangle$ |
| Korea, Rep. of | 12 (0.7) | 9 (0.4) | -3 (0.8) | $\nabla$ | 72 (1.0) | 65 (0.8) | -7 (1.3) | $\nabla$ | 17 (0.7) | 26 (0.8) | 10 (1.1) | $\triangle$ |
| Latvia (LSS) | 26 (1.2) | 26 (1.2) | -1 (1.7) | - | 65 (1.2) | 65 (1.3) | 1 (1.7) | - | 9 (0.8) | $9(0.8)$ | 0 (1.1) | - |
| Lithuania | 19 (1.1) | 30 (1.3) | 12 (1.7) | $\triangle$ | 67 (1.2) | 62 (1.1) | -5 (1.6) | $\nabla$ | 15 (0.9) | 8 (0.7) | -7 (1.1) | $\checkmark$ |
| Netherlands | 15 (1.2) | 17 (1.4) | 2 (1.8) | - | 62 (1.3) | 63 (1.0) | 0 (1.6) | - | 22 (1.7) | 20 (1.4) | -2 (2.2) | - |
| New Zealand | 36 (1.1) | 34 (1.1) | -1 (1.6) | - | 53 (0.9) | 55 (1.1) | 2 (1.4) | - | 11 (0.6) | 10 (0.7) | 0 (1.0) | - |
| Romania | 35 (1.3) | 34 (1.3) | -1 (1.9) | - | 57 (1.2) | 57 (1.1) | 1 (1.6) | - | 8 (0.6) | 9 (0.7) | 0 (0.9) | - |
| Russian Federation | 32 (0.9) | 36 (1.3) | 5 (1.6) | - | 61 (0.9) | 58 (1.2) | -3 (1.5) | $\bullet$ | 7 (0.6) | 5 (0.4) | -2 (0.7) | - |
| Singapore | 45 (1.2) | 45 (1.0) | 0 (1.5) | - | 50 (1.0) | 48 (0.9) | -2 (1.3) | - | 6 (0.5) | 7 (0.5) | 1 (0.7) | - |
| Slovak Republic | 29 (1.0) | 31 (1.5) | 2 (1.8) | - | 61 (0.9) | 60 (1.2) | 0 (1.5) | - | 10 (0.6) | 9 (0.8) | -1 (1.0) | - |
| Slovenia | 24 (1.3) | 19 (0.9) | -5 (1.6) | $\nabla$ | 61 (1.3) | 63 (1.0) | 2 (1.6) | - | 15 (1.2) | 18 (1.0) | 3 (1.6) | - |
| Thailand ${ }^{\text {+ }}$ | 44 (1.9) | 37 (1.1) | -8 (2.2) | $\nabla$ | 54 (1.7) | 61 (1.1) | 7 (2.0) | - | 2 (0.3) | 3 (0.2) | 1 (0.4) | - |
| United States | 35 (1.1) | 35 (1.1) | 0 (1.5) | - | 50 (1.0) | 49 (0.7) | -1 (1.2) | $\bigcirc$ | 15 (0.8) | 16 (0.7) | 1 (1.1) | - |
| International Avg. s | 30 (0.2) | 30 (0.2) | 0 (0.3) | - | 57 (0.2) | 56 (0.2) | -1 (0.3) | - | 13 (0.2) | 14 (0.2) | 1 (0.3) | - |

A 1999 significantly higher than 1995
No significant difference between 1995 and 1999

- 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

## Background data provided by students.

+ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Exhibit 4.13 Trends in Gender Differences in Percentages of Students at High Level of Index of Positive Attitudes Towards Mathematics (PATM)

|  | 1995 |  |  |  | 1999 |  |  |  | Change in Gender Difference* |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girls | Boys |  | Difference (Absolute Value) | Girls | Boys |  | Difference (Absolute Value) |  |
| Latvia (LSS) | 28 (1.7) | 24 (1.7) |  | 5 (2.2) | 25 (1.4) | 26 (1.6) |  | 0 (1.8) | 4 |
| Iran, Islamic Rep. | 54 (2.4) | 55 (2.2) |  | 1 (3.3) | 54 (1.5) | 54 (1.6) |  | 0 (2.4) | $\Leftrightarrow$ |
| Thailand | 44 (2.0) | 45 (2.3) |  | 0 (2.1) | 37 (1.5) | 36 (1.3) |  | 1 (1.6) | 4 |
| Russian Federation | 34 (1.2) | 29 (1.4) |  | 5 (1.8) | 37 (1.6) | 36 (1.6) |  | 1 (1.7) | 4 |
| Slovenia | 24 (1.6) | 24 (1.5) |  | 0 (1.8) | 18 (1.2) | 20 (1.2) |  | 1 (1.4) | $\Leftrightarrow$ |
| Korea, Rep. of | 11 (0.9) | 13 (1.0) |  | 2 (1.4) | 8 (0.6) | 10 (0.6) |  | 2 (0.8) | - |
| Cyprus | 49 (1.6) | 49 (1.8) |  | 0 (2.0) | 51 (1.7) | 50 (1.3) |  | 2 (2.0) | $\Leftrightarrow$ |
| Romania | 34 (1.4) | 35 (1.7) |  | 0 (1.7) | 35 (1.6) | 33 (1.7) |  | 2 (2.0) | 4 |
| Hungary | 21 (1.2) | 17 (1.0) |  | 4 (1.6) | 18 (1.3) | 20 (1.2) |  | 2 (1.7) | - |
| Belgium (Flemish) | 25 (1.7) | 26 (1.4) |  | 1 (2.1) | 24 (1.4) | 26 (1.7) |  | 2 (2.5) | $\rightarrow$ |
| Slovak Republic | 26 (1.4) | 31 (1.5) |  | 5 (2.1) | 29 (1.6) | 32 (1.9) |  | 3 (1.8) | - |
| Italy | 36 (1.9) | 44 (1.7) | - | 8 (2.4) | 33 (2.0) | 37 (1.5) |  | 4 (2.0) | ( |
| Lithuania ${ }^{\text { }}$ | 19 (1.4) | 18 (1.4) |  | 2 (1.8) | 32 (1.8) | 28 (1.8) |  | 4 (2.4) | 4 |
| United States | 34 (1.2) | 36 (1.3) |  | 2 (1.4) | 32 (1.3) | 37 (1.2) | $\triangle$ | 5 (1.3) | 4 |
| New Zealand | 33 (1.5) | 39 (1.3) | - | 6 (1.7) | 32 (1.5) | 37 (1.3) |  | 5 (1.8) | $\Leftrightarrow$ |
| Czech Republic | 19 (1.4) | 20 (1.4) |  | 1 (1.9) | 16 (1.5) | 22 (1.7) |  | 6 (2.1) | $\Leftrightarrow$ |
| Israel | 35 (2.6) | 41 (2.3) |  | 6 (2.7) | 40 (2.0) | 46 (1.7) |  | 6 (2.0) | $\square$ |
| Canada | 34 (1.2) | 39 (1.4) |  | 5 (1.6) | 31 (1.1) | 38 (1.2) | - | 7 (1.5) | - |
| Singapore | 42 (1.5) | 47 (1.5) |  | 5 (1.9) | 41 (1.4) | 48 (1.4) | $\triangle$ | 7 (2.0) | $\Leftrightarrow$ |
| Japan | 8 (0.7) | 13 (0.8) | $\triangle$ | 5 (1.0) | 6 (0.5) | 13 (0.7) | $\triangle$ | 7 (0.8) | $\Leftrightarrow$ |
| Australia | 22 (0.9) | 28 (1.4) | $\triangle$ | 5 (1.5) | 26 (1.5) | 34 (1.5) | $\triangle$ | 8 (1.8) | 4 |
| Netherlands | 10 (1.0) | 21 (1.9) | $\triangle$ | 11 (1.7) | 12 (1.5) | 23 (1.8) | $\triangle$ | 11 (1.6) | $\Leftrightarrow$ |
| England | 36 (1.7) | 46 (2.0) | $\triangle$ | 11 (2.4) | 35 (1.7) | 48 (1.7) | $\triangle$ | 12 (2.3) | - |
| Hong Kong, SAR | 16 (1.2) | 31 (1.4) | $\triangle$ | 15 (1.9) | 22 (1.1) | 34 (1.2) | - | 13 (1.4) | - |
| International Avg. | 29 (0.3) | 32 (0.3) | - | 3 (0.4) | 29 (0.3) | 33 (0.3) | - | 4 (0.4) |  |

Increased

| Increased |
| :---: | :---: |
| Decreased |
| No change |

Background data provided by students.

* Indicates whether 1999 gender difference is significantly different than 1995 gender difference.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

## CHAPTER 5

## The Mathematics Curriculum

The first part of Chapter 5 presents information about the curricular goals in the timss 1999 countries, referred to as the intended curriculum. Data are provided about how the curriculum is supported and monitored within each country and the relationship between national testing and the curriculum. The second part of the chapter contains teachers' reports about the mathematics topics actually studied in their classrooms, also known as the implemented curriculum.


In comparing achievement across countries, it is important to consider differences in students' curricular experiences and how they may affect the mathematics they have studied. At the most fundamental level, students' opportunity to learn the content, skills, and processes tested in the timss 1999 assessment depends to a great extent on the curricular goals and intentions inherent in each country's policies for mathematics education. Just as important as what students are expected to learn, however, is what their teachers choose to teach them. The lessons provided by the teacher ultimately determine what mathematics students are taught.

Chapter 5 presents information about the curricular goals in the timss 1999 countries and teachers' reports about the mathematics content studied. Teacher's instructional programs for their classes are usually guided by an "official curriculum" that describes the mathematics education that should be provided. The official curriculum can be communicated by means of documents or statements of various sorts (often called guides, guidelines, or frameworks) prepared by the education ministry or by national or regional education departments. These documents or statements, together with supporting material such as instructional guides or mandated textbooks, are referred to as the intended curriculum.

To collect information about the intended mathematics curriculum at the eighth grade in each of the timss 1999 countries, the National Research Coordinators responsible for implementing the study completed questionnaires and participated in interviews. As part of the process, information was gathered about factors related to supporting and monitoring the implementation of the official curriculum, including the availability of teacher training, instructional materials, assessments, and audits aligned with the curriculum.

In many cases, teachers need to interpret and modify the intended curriculum according to their perceptions of the needs and abilities of their classes, and this evolves into the implemented curriculum. Research has shown that the implemented curriculum, even in highly regulated educational systems, is not identical to the intended curriculum. To collect data about the implemented curriculum, the mathematics teachers of the students tested in timss 1999 completed questionnaires about whether students had been taught the various mathematics topics covered in the test.

## Does Decision Making About the Intended Curriculum Take Place at the National or Local Level?

Depending on the educational system, students' learning goals are commonly set at three levels: the national or regional level, the school level, and the classroom level. Some countries are highly centralized, with the ministry of education (or highest authority in the system) being exclusively responsible for the major decisions governing the direction of education. In others, such decisions are made regionally or locally. Each approach has its strengths and weaknesses. Centralized decision making can add coherence and uniformity in curriculum coverage, but may constrain a school or teacher's flexibility in tailoring instruction to the needs of students.

Exhibit 5.1 presents information for each timss 1999 country about the highest level of authority responsible for making decisions about the curriculum and gives the curriculum's current status. The data reveal that 35 of the 38 countries reported that the specifications for students' curricular goals were developed as national curricula. Australia determined curricula at the state level, with local input; the United States did so at both the state and local levels, with variability across states; and Canada determined what students are expected to learn at the provincial level.

In recent decades, it has become common for intended curricula to be updated regularly. At the time of the timss 1999 testing, the official mathematics curriculum in 29 countries had been in place for less than a decade, and more than half of them were in revision. Of the eight countries with a mathematics curriculum of more than 10 years' standing, five were being revised. In Australia, Canada, and the United States, curriculum change is made at the state or provincial level, and some mathematics curricula were in revision at the time of testing. The mathematics curricula in these three countries were relatively recent, having been developed within ten years prior to the study.

|  | National or Regional Curriculum | Year Curriculum Introduced | Status of Curriculum |
| :---: | :---: | :---: | :---: |
| Australia | Regional \& Local | 1995-1998 | In revision (2 states); not being revised (3 states); no curriculum statement (3 states) |
| Belgium (Flemish) | National | 1997 | As introduced |
| Bulgaria | National | 1997 | As introduced |
| Canada | Regional | 1997-1998 (most provinces) | As introduced |
| Chile | National | 1980 | In revision |
| Chinese Taipei | National | 1997 | In revision |
| Cyprus | National | 1987 | In revision |
| Czech Republic | National | 1996 | In revision |
| England | National | 1995 | In revision, same structure with minor revisions (to be implemented 2000/01) |
| Finland | National | 1994 | As introduced |
| Hong Kong, SAR | National | 1987 | In revision |
| Hungary | National | 1986 | In revision |
| Indonesia | National | 1994 | In revision |
| Iran, Islamic Rep. | National | 1985 | As introduced |
| Israel | National | 1990 | As introduced |
| Italy | National | 1979 | As introduced |
| Japan | National | 1993 | As introduced |
| Jordan | National | 1993-1994 | In revision |
| Korea, Rep. of | National | 1995 | As introduced |
| Latvia (LSS) | National | 1992 | In revision |
| Lithuania | National | 1997 | In revision |
| Macedonia, Rep. of | National | 1979 (adaptations in 1995) | As introduced |
| Malaysia | National | 1990 | In revision |
| Moldova | National | 1991 | In revision |
| Morocco | National | 1991 | In revision |
| Netherlands | National | 1993 | As introduced |
| New Zealand | National | 1993 | As introduced |
| Philippines | National | 1998 | In revision |
| Romania | National | 1993 | In revision |
| Russian Federation | National | 1997 | In revision |
| Singapore | National | 1993 | In revision |
| Slovak Republic | National | - | - |
| Slovenia | National | 1983 | In revision |
| South Africa | National | 1996 | In revision |
| Thailand | National | 1990 | In revision |
| Tunisia | National | 1997 | As introduced |
| Turkey | National | 1991 | In revision |
| United States ${ }^{1}$ | Regional \& Local | 1994-1999 | As of 1999, 49 of 50 states completed standards |

1 United States: The NCTM standards were developed in 1989 and are in revision. As of 1999, most states had developed content standards. Currently, many states are in the process of updating and revising their standards.

## How Do Countries Support and Monitor Curriculum Implementation?

Education systems use different ways to achieve the best match between the intended and the implemented curriculum. For example, teachers can be trained in the content and pedagogical approaches specified in the curriculum guides. Another way to help ensure alignment is to develop instructional materials, including textbooks, instructional guides, and ministry notes, that are tailored to the curriculum. Systems can also monitor implementation by means of school inspection or audit. The different methods used by the timss 1999 countries are shown in Exhibit 5.2. It is assumed that monitoring implementation encourages teachers to use the official curriculum in planning their teaching programs. Testing and assessment of the intended curriculum are also widely used to support and monitor curriculum implementation; these are addressed in Exhibits $5 \cdot 3$ and $5 \cdot 4$.

Of the methods for supporting and monitoring curriculum implementation shown in Exhibit 5.2, 10 countries reported using all six, and a further 14 countries used five. Nearly all countries (34) used in-service teacher education, and most countries (31) used mandated or recommended textbooks. Ministry notes and directives, or a system of school inspection or audit, were used in 30 countries. Beyond the methods included in the questionnaire, a majority of representatives from the timss national centers reported in interviews that mathematics specialists were employed to advise mathematics teachers.


- Country reported that method is used to support or monitor the implementation of the national/regional curriculum at grade 8
+ Not applicable nationally

Background data provided by National Research Coordinators.

* Other than public examinations and system-wide assessments described in Exhibits 5.3 and 5.4, respectively.
1 Australia: Results shown are for the majority of states/territories.

2 Canada: Results shown are for the majority of provinces.
3 United States: Methods are implemented by individual states and vary from state to state. As of 1998, 13 of 50 have policies on textbook/materials selection; 8 of 50 states have policies recommending textbook/materials.

## What Countries Have Public Examinations in Mathematics?

Using public examinations as a way to select students for university or academic tracks in secondary school can be an important motivating factor for student achievement. Exhibit $5 \cdot 3$ shows information on public examinations and their purpose. Thirty-seven countries reported having public examinations or awards, at one or more grades, that included testing achievement in mathematics. Most countries held their examinations in the final year of schooling for certification and selection to higher education (often, university education). Certification also provides students not going on to full-time post-secondary education with evidence of educational attainment for prospective employers. In about one-third of the countries, public examinations were also reported to be used to select students for entry to different types of secondary school, or to assign them to different tracks or courses within secondary schools. Providing feedback to policy makers in the educational system, schools, or both was also an important use of assessments in some countries.

Belgium (Flemish) was the one country that reported having no public examinations in mathematics. This was the only country where decisions about promotion from one grade to the next, certification, and qualification for entrance to university were made at the school level without reliance on system-wide public examinations.

| Australia <br> Belgium (Flemish) | Public Exams/ Awards | Grade(s) | Purpose/Consequences |
| :---: | :---: | :---: | :---: |
|  | Yes | 12 | Certification and selection for tertiary education |
|  | No |  |  |
| BulgariaCanada | Yes | 7/8, 12 | Candidates for profile schools (grade 7 or 8); certification and entrance to university -- not taken by all students (grade 12) |
|  | Yes | 3,6,8 (1 province); 10, 11 (1 province); 12 (4 provinces) | Feedback to system and schools; certification (grade 12) |
| Chile | Yes | 12 | Entry to university |
| Chinese Taipei | Yes | 9, 12 | Entry to secondary school (grade 9); entry to university (grade 12) |
| Cyprus | Yes | 12 | Certification and entry to university (grade 12); a certification exam occurs on a local level for grade 9 |
|  | Yes | 13 | Certification (mathematics can be chosen as one of four subjects for leaving examination) |
| England | Yes | 10, 12 | Certification (grade 10), certification and entry to university (grade 12); feedback to system and schools |
| Finland | Yes | 12 | Certification and selection for tertiary education |
| Hong Kong, SAR | Yes | 6,11,13 | School placement (grade 6); certification and placement for 12th grade (grade 11); placement in tertiary institutions (grade 13) |
| Hungary <br> Indonesia | Yes | 12 | Certification and entry to university |
|  | Yes | 6, 9, 12 | Leaving exam and selection for junior secondary school (grade 6); selection for senior secondary school (grade 9); leaving exam (grade 12); system-level feedback, in some cases school- and classroom-level feedback |
| Iran, Islamic Rep. | Yes | 11, 12 | Certification (grade 11); entry to tertiary education (grade 12); in addition, provincial exams are administered at grade 8 |
| Israel | Yes | 11 or 12 | Entry to higher education |
| Italy Japan | Yes | 13 | Certification and entry to university |
|  | Yes | 9,12 | Entry to prefectural and municipal upper secondary schools (grade 9); entry to national, prefectural and municipal universities (grade 12) |
| Jordan Korea, Rep. of Latvia (LSS) | Yes | 12 | Certification and entry to tertiary education |
|  | Yes | 12 | College entrance exam for selection of students |
|  | Yes | 9, 12 | Certification |
| Lithuania Macedonia, Rep. Of | Yes | 9,12 | Graduation from Basic and Upper Secondary schools |
|  | Yes | 12 | Certification and entry to university; the exam constitutes $40 \%$ of the required points for entry to university with the remaining points based on university entry exams |
| Malaysia | Yes | $6,9,11,13$ | Feedback to system and schools; achievement test (grade 6); entry to course tracks (grade 9); certification and end of secondary (grade 11); certification and entry to university (grade 13) |
| Moldova | Yes | 9, 11/12 | Certification and selection for high school (grade 9); graduation (grade 11 or 12 depending on school) |
| Morocco | Yes | $6,9,10,11,12$ | Remedial test for retention purposes (grade 6); certification, selection to secondary, and selection to courses (grade 9); certification and entry to tertiary (grade 12); feedback to system and schools |
| Netherlands New Zealand | Yes | 10, 11, 12 | End-of-track examinations; exams recommended at grades 6 and 8 |
|  | Yes | 10, 12 | Certification and course selection (grade 10); entry to tertiary education (grade 12); feedback to system and schools; informal between-school comparisons |
| Philippines | Yes | 6,10 | Feedback to system and schools |
| Romania | Yes | 8,12 | Certification (grade 8); certification (grade 12; mathematics can be chosen as one of 7 subjects) |
| Russian Federation | Yes | 9, 11 | Certification |
| Singapore | Yes | 6,10,12 | Selection into courses; certification and entry to university; feedback to system and schools |
| Slovak Republic | Yes | 12 | Certification (mathematics can be chosen as one of four subjects for leaving exam) |
| Slovenia | Yes | 8,12 | Entry to secondary school (grade 8); certification and entry to tertiary education (grade 12) |
| South Africa | Yes | 12 | Certification and selection for tertiary education |
| Thailand | Yes | 12 | Entry to university |
| Tunisia | Yes | 6, 9, 13 | Regional exam for promotion (grade 6); feedback to system and schools, selection for schools and courses, and promotion (grade 9); certification and entry to university (grade 13) |
| Turkey | Yes | 8,11 | Placement in specialized schools for some students (grade 8); entry to university (grade 11) |
| United States ${ }^{2}$ | Yes | varies | Primarily feedback to system and schools; in 8 states grade promotion is dependent on results; in 18 states graduation is dependent on results of grade 12 exams |

[^29]2 United States: As of 1997-1998, public examinations are administered in 47 of 50 states at grades 7-8 or 9-12.

## What Countries Have System-Wide Assessment in Mathematics?

Although national public examinations can provide information of interest to national and regional policy makers, their main purpose is to make decisions about individual students. In comparison, system-wide assessments are designed primarily to inform policy makers about matters such as national standards of achievement of the intended curriculum objectives, strengths and weaknesses in the curriculum or how it is being implemented, and whether educational achievement is improving or deteriorating.

Exhibit 5.4 summarizes information about national assessments in mathematics. Such assessments were conducted in about two-thirds of the participating countries. Half of these countries assessed all students in the grade, and the other half a sample of students from the grade. Most countries tested two or three grades, with Hong Kong (nine grades) and Korea (seven grades) testing the most grades.

Generally, the purpose of the system-wide assessments was to provide feedback to government policy makers and the public. Feedback to individual schools was a feature reported by some countries whose methodology, namely assessment of the entire grade level, allowed for this type of reporting. In Singapore, the 20 schools found to provide the greatest value-added measures received monetary rewards, as did teachers of the top 25 percent of classes in Chile.

In addition to collecting information about examinations and assessments, questionnaires and interviews were used to determine whether, and to what extent, explicit achievement standards were a feature of intended curricula (see Exhibit R2.1 in the reference section). Twenty-two countries reported that such standards were incorporated in their curricula or related documents. However, the term "achievement standards" means different things in different countries and was unfamiliar to some. Some countries regard them as learning objectives, and others include in this category performance indicators that describe levels of required or desired performance. Exhibit R2.1 includes countries that reported learning objectives or performance objectives as a component of their curriculum documents.

| Australia ${ }^{2}$ | System-Wide Assessments ${ }^{1}$ | Grades |  | Purpose/Consequences |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Entire Grade Level | Sample from Grade Level |  |
|  | Yes | 3, 5 (all states) <br> 7 (four states) |  | System-level, school-level, and individual student-level feedback |
| Belgium (Flemish) <br> Bulgaria <br> Canada ${ }^{3}$ | No |  |  |  |
|  | Yes |  | 4, 8 | System-level feedback, administered only in 1998 |
|  | Yes | 3, 6,9 (5 provinces); 5, 8, 11 (1 province); 4, 7, 10 (1 province); 12 (1 province) | Ages 13 and 16 nationally (most provinces) | System- and school-level feedback |
| Chile | Yes | 4, 8, 10 |  | System-level, school-level, class-level feedback; top 25\% of teachers are given monetary rewards; usually one grade level assessed each year |
| Chinese Taipei <br> Cyprus <br> Czech Republic <br> England <br> Finland | No |  |  |  |
|  | No |  |  |  |
|  | No |  |  |  |
|  | Yes | 1, 5, 8 |  | School-level feedback; course selection and placement for grade 9 |
|  | Yes |  | 4, 6, 9 | System-level feedback |
| Hong Kong, SAR <br> Hungary <br> Indonesia | Yes |  | 1-9 | System-level feedback |
|  | Yes |  | $4,6,8,10,12$ | System-level, school-level, and individual-level feedback |
|  | Yes |  | various grades | System-level feedback, assessments given irregularly at different primary grades |
| Iran, Islamic Rep. Israel | No |  |  |  |
|  | Yes |  | 4,8 | System-level feedback |
| Italy <br> Japan <br> Jordan | Yes |  | $6,8,10,13$ | System-level feedback; first administered in 1999 with a grade 4 assessment instituted in 2000 |
|  | Yes |  | $5,6,7,8,9$ | System-level feedback |
|  | Yes |  | 4, 5, 8, 10 | System-level feedback; monitoring reform impact; curricular revisions |
| Korea, Rep. of Latvia (LSS) | Yes | $4,5,6,7,8,10,11$ |  | System-level feedback |
|  | No |  |  |  |
| Lithuania <br> Macedonia, Rep. Of <br> Malaysia <br> Moldova <br> Morocco | No |  |  |  |
|  | Yes |  | $4,5,6,7,8$ | System-level feedback and research purposes (projects and curriculum development) |
|  | Yes | 6, 9, 11, 13 |  | System- and school-level feedback; "good schools" publicized |
|  | No |  |  |  |
|  | Yes | 6, 9, 10, 11, 12 |  | System- and school-level feedback |
| Netherlands <br> New Zealand Philippines Romania <br> Russian Federation | Yes | 10, 11, 12 | 6 | System-level feedback |
|  | Yes |  | 3,7 | System-level feedback |
|  | Yes | 6,10 |  | System- and school-level feedback (the assessment was sample-based up until 1999) |
|  | No |  |  |  |
|  | Yes |  | various grades | Irregularly for research purposes |
| Singapore | Yes | 6,10,12 |  | System- and school-level feedback; selection into courses, certification and entry to university |
| Slovak Republic <br> Slovenia South Africa Thailand | No |  |  |  |
|  | No |  |  | Assessments administered in grades 1-8 from 1991-1996 |
|  | No |  |  |  |
|  | Yes | 6, 9, 12 |  | System-level feedback |
| Tunisia | Yes | 4, 6, 9, 13 |  | System- and school-level feedback; may lead to redistribution of teachers in the regions; assessments at grades 4 and 6 developed regionally |
| Turkey <br> United States | Yes |  | 5, 8, 11 | System- and school-level feedback |
|  | Yes |  | 4, 8, 12 | National and state-level feedback |

[^30]
## How Much Instructional Time Is Recommended for Mathematics?

The different percentages of time devoted to mathematics instruction at different grades highlight one of the difficulties in investigating the relationship between achievement and instructional time across countries. If instructional time is measured only for the eighth grade, the total time for which students in a country have been exposed to instruction in mathematics during their schooling may be under- or over-estimated. These data for grades 4,6 , and 8 provide a better estimate of students' intended instructional time for mathematics across the school years.

Percentages of instructional time designated for mathematics specified in the intended curricula for grades 4,6 , and 8 are shown in Exhibit 5.5. The pattern across countries shows that the percentage of time remains the same or decreases from grade 4 to grade 6 and again from grade 6 to grade 8 , with 18 countries reporting a decrease in instructional time in mathematics from grade 6 to grade 8 . Interestingly, the reverse pattern holds for science. ${ }^{1}$ Average percentages of time for mathematics instruction across all countries were 17 percent, 16 percent, and 13 percent for grades 4,6 , and 8 , respectively. An opposite trend was found for Morocco and Tunisia, where instructional time for mathematics increased in the eighth grade. Cyprus data show a sharp drop from 17 percent in each of grades 4 and 6 to nine percent in grade 8 . Percentages of total instructional time specified for mathematics ranged from eight percent at each of grades 4,6 , and 8 for Thailand to 20 percent or more for six countries at grade 4 , two at grade 6, and one (Morocco) at grade 8. Schools' and teachers' reports of the percentage of instructional time actually devoted to the sciences at grade 8, shown in Exhibit 6.4 in the next chapter, generally correspond with the intended percentages reported in Exhibit 5.5.

[^31]

Exhibit 5.5 Overleaf

| Australia | Instructional Time Specified for Mathematics |  |  | Comments |
| :---: | :---: | :---: | :---: | :---: |
|  | Grade 4 | Grade 6 | Grade 8 |  |
|  | N/S | N/S | N/S | At primary level, English and mathematics are given about the same amount of instructional time. The proportion of time decreases in secondary school. Some students do not study mathematics in their final year of secondary school. |
| Belgium (Flemish) | 18\% | 18\% | 15\% | Instructional time varies from 10\% to 16\% in grades 9-10, and from 6\% to 25\% in grades 11-12. |
| Bulgaria | 16\% | 13\% | 13\% | At grade $1,18 \%$ of instructional time is devoted to mathematics. This decreases slightly to $15 \%$ at 5 th grade and is $13 \%$ from grades $6-9$. Instructional time ranges from $11-14 \%$ in grades 10-12. |
| Canada | 15\% | 15\% | 15\% | For three provinces, there is no change in emphasis as students progress through school. For two provinces, the proportion of time dedicated to mathematics decreases and in one province it increases after grade 6 . |
| Chile | 17\% | 17\% | 17\% | The primary school curriculum states that 5 of 30 classes per week must be devoted to mathematics. |
| Chinese Taipei <br> Cyprus <br> Czech Republic <br> England | 12\% | 18\% | 11\% |  |
|  | 17\% | 17\% | 9\% |  |
|  | 20\% | 15\% | 13\% |  |
|  | N/S | N/S | N/S | The national curriculum does not specify instructional time fo mathematics. The proposed curriculum assumes 126 hours per year for grade 4 (year 5 ), and 90 hours per year for grades 6 and 8 (years 7 and 9 ). |
| Finland | 16\% | 16\% | 10\% | The curriculum framework indicates the minimum amount of instructional time on average for grade spans 1-6 and 7-9. Schools decide on instructional time for specific grades. |
| Hong Kong, SAR | 15\% | 15\% | 15\% | Total instructional time on mathematics increases to $17.5 \%$ at grade 9 and 11-20\% at grades 12 and 13. |
| Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | - | - | - |  |
|  | 14\% | 14\% | 14\% |  |
|  | 14\% | 14\% | 11\% |  |
|  | 15\% | 14\% | 13\% |  |
| Italy <br> Japan | N/S | 10-15\% | 10-15\% | The curriculum indicates 20\% instructional time be devoted to mathematics and science as one subject. The exact distribution of time for each of these subjects is decided by the teacher. |
|  | 17\% | 17\% | 13\% | Time devoted to mathematics is less in lower secondary school, especially at grade 7 where it is only $10 \%$. However, mathematics instructional time at grade 8 is the same as Japanese language and social sciences. |
| Jordan | 18\% | 15\% | 13\% | At grade 1 about $20 \%$ of instructional time is devoted to mathematics. This decreases slightly in other grades and is about $13 \%$ from grades $8-10$. |
| Korea, Rep. of Latvia (LSS) | 14\% | 13\% | 12\% |  |
|  | 20\% | 16\% | 16\% |  |
| Lithuania <br> Macedonia, Rep. of Malaysia | 17-22\% | 14-17\% | 13\% | Mathematics is usually treated as an important subject since it is one of the two basic school exit exams at grade 10. |
|  | 20\% | 17\% | 13\% |  |
|  | 20\% | 20\% | 13\% | From grade 8 through secondary school, the instructional time specified for mathematics remains about the same. The mathematics curriculum emphasizes understanding concepts and mastering processes (calculating, measuring, computing, communicating mathematically, and problem solving). Emphasis for the higher-level processes increases as students progress through school. |
| Moldova <br> Morocco | 17\% | 17\% | 16\% |  |
|  | 15\% | 15\% | 20\% |  |
| Netherlands <br> New Zealand | N/S | N/S | 10\% | Students can choose to stop taking mathematics after grade 9, depending on their course of study. |
|  | N/S | N/S | N/S | All schools are required to teach mathematics as part of a "balanced curriculum." Schools decide on instructional time. In general, in primary school, mathematics is allocated the second highest proportion of instructional time, after language (which includes reading). Time for mathematics, science, and English are about the same in secondary school. |
| Philippines | 12\% | 11\% | 10\% | To supplement the regular mathematics program, enrichment topics and activities are included in mathematics for grade 7, especially in the special science classes/schools. |
| Romania | 17\% | 17\% | 15\% |  |
| Russian Federation | 18\% | 17\% | 15\% | Mathematics is given less emphasis than philology in grades 1-7. Emphasis on mathematics in grades $8-9$ is still less than philology and is equal or slightly less than science and social science. |

Background data provided by National Research Coordinators.
All data rounded to the nearest whole number.
$\mathrm{N} / \mathrm{S}$ indicates instructional time not specified in the national/regional curriculum.
A dash ( - ) indicates data not available
$\square$ 1) $\square$


5

| Singapore | Instructional Time Specified for Mathematics |  |  | Comments |
| :---: | :---: | :---: | :---: | :---: |
|  | Grade 4 | Grade 6 | Grade 8 |  |
|  | 22\% | 20\% | 15\% | Students are required to study mathematics, English and the mother-tongue language throughout primary and secondary school. Pupils who are planning to pursue further study in mathematics or a related discipline are offered an additional mathematics subject in grade 9 . |
| Slovak Republic | - | - | - |  |
| Slovenia | 23\% | 16\% | 16\% | Instructional time for mathematics is relatively equal to instructional time for other subjects. |
| South Africa | N/S | N/S | N/S |  |
| Thailand | 8\% | 8\% | 8\% | There is no change in content, but there is change in depth. |
| Tunisia | 15\% | 15\% | 16\% | Mathematics is given the most instructional time after the mother tongue, Arabic. Time devoted to mathematics remains constant, but the amount of instructional time for mathematics compared to other subjects increases in grades 4 and up. |
| Turkey | 13\% | 13\% | 13\% | There is a tendency to enhance student-centered teaching and learning activities. |
| United States | N/S | N/S | N/S | States do not generally specify; it is largely a local decision. |

## How Do Countries Deal with Individual Differences?

The challenge of maximizing opportunity to learn for students with widely differing abilities and interests is met differently in different countries. Exhibit 5.6 summarizes questionnaire and interview data on how countries dealt with this issue in organizing the intended curricula.

Some countries indicated using more than one method of dealing with individual differences among students, and in these cases the category describing the main method was reported. The most common approach, found in 24 countries, was to have the same intended curriculum for all students, but to recommend that teachers adapt the level and scope of their teaching to the abilities and needs of their students. Adaptations for individuals and classes were also recommended in the intended curricula of some countries with different levels of curricula or different curricula for different groups.

In the Czech Republic, England, and Israel, mathematics topics were taught at different levels with different groups. The Czech Republic had four levels, Israel three, and England nine. In England's curriculum, the levels were defined in terms of progressively more complex performance to be demonstrated. Among the countries with different curricula for different groups of students, Belgium (Flemish) and the Russian Federation each provided two different levels, Singapore three, and the Netherlands four.

National Research Coordinators from seven countries reported that their official mathematics curricula did not address the issue of differentiating instruction for grade 8 students with different abilities or interests, but this does not necessarily mean that schools and teachers in those countries did not make allowance for individual differences. Schools' reports on how they organize to accommodate students with different abilities or interests are shown in Exhibit R2.2 in the reference section. Substantial percentages of students in many countries were in schools that offered remedial mathematics, including several of the countries without specific curricular statements about differentiation.

| Australia <br> Belgium (Flemish) | CurriculumAddressesDifferentiation | Approaches to Addressing Students with Different Abilities or Interests at Grade 8 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Same Curriculum for All Students, and Teachers Adapt to Students' Needs | Same Curriculum with Different Levels for Different Groups | Different Curricula for Different Groups | Number of Curriculum Levels |
|  | Yes | Yes | No | No | 1 |
|  | Yes | No | No | Yes | 2 |
| Bulgaria | Yes | Yes | No | No | 1 |
| Canada | Yes | Yes | No | No | 1 |
| Chile | No |  |  |  |  |
| Chinese Taipei | Yes | Yes | No | No | 1 |
| Cyprus | Yes | Yes | No | No | 1 |
| Czech Republic | Yes | No | Yes | No | 4 |
| England ${ }^{1}$ | Yes | No | Yes | No | 9 |
| Finland | Yes | Yes | No | No | 1 |
| Hong Kong, SAR | Yes | Yes | No | No | 1 |
| Hungary | Yes | Yes | No | No | 1 |
| Indonesia | No |  |  |  |  |
| Iran, Islamic Rep. | Yes | Yes | No | No | 1 |
| Israel | Yes | No | Yes | No | 3 |
| Italy | No |  |  |  |  |
| Japan | No |  |  |  |  |
| Jordan | Yes | Yes | No | No | 1 |
| Korea, Rep. of | Yes | Yes | No | No | 1 |
| Latvia (LSS) | No |  |  |  |  |
| Lithuania | No |  |  |  |  |
| Macedonia, Rep. Of | Yes | Yes | No | No | 1 |
| Malaysia | Yes | Yes | No | No | 1 |
| Moldova | No |  |  |  |  |
| Morocco | Yes | Yes | No | No | 1 |
| Netherlands | Yes | No | No | Yes | 4 |
| New Zealand | Yes | Yes | No | No | 1 |
| Philippines | Yes | Yes | No | No | 1 |
| Romania | Yes | Yes | No | No | 1 |
| Russian Federation | Yes | No | No | Yes | 2 |
| Singapore | Yes | No | No | Yes | 3 |
| Slovak Republic | Yes | Yes | No | No | 1 |
| Slovenia | Yes | Yes | No | No | 1 |
| South Africa | Yes | Yes | No | No | 1 |
| Thailand | Yes | Yes | No | No | 1 |
| Tunisia | Yes | Yes | No | No | 1 |
| Turkey | Yes | Yes | No | No | 1 |
| United States ${ }^{2}$ | Yes | Yes | No | No | 1 |

[^32]2 United States: Most state standards are designed for all students.

## What Are the Major Characteristics of the Intended Curriculum?

"
Exhibit $5 \cdot 7$ indicates the relative emphasis given to various aspects of mathematics instruction in the intended curriculum. As might be anticipated for students at this point in their schooling, major emphasis was most commonly placed on mastering basic skills and understanding mathematical concepts. Most countries moderately or strongly emphasized assessing student learning. Similarly, "real-life" applications of mathematics were encouraged in the curriculum of most countries, with $1_{5}$ countries giving this approach major emphasis and 16 moderate emphasis. The Netherlands' intended curriculum was reported to emphasize this approach more than either mastering basic skills or understanding mathematics concepts. Communicating mathematically, an aspect of teaching and learning that has received increasing attention in recent years, was included in the curriculum of most countries and was accorded major emphasis in 13 countries. Similarly, recent efforts to improve students' abilities to apply their mathematical understandings have led to recommendations for more experience with novel problem-solving situations. Thirty-three countries reported at least moderate emphasis on solving non-routine problems.

The mathematical area with the greatest variation across countries' intended curricula was deriving formal proofs. It was given major emphasis in eight countries, moderate emphasis in 13, and minor or no emphasis in 16 . Integration of mathematics with other subjects to some degree was a common aim across countries, and about half the countries placed some emphasis on a thematic approach. Working on mathematics projects was given minor or no emphasis in the intended curriculum of most countries, as was a multicultural approach.


## What Mathematics Content Do Teachers Emphasize at the Eighth Grade?

Teachers of the mathematics classes tested were asked what subject matter they emphasized most in their classes (e.g., geometry, algebra, various combinations of content, etc.). Their responses are presented in Exhibit 5.8.

More than a quarter of the students received instruction emphasizing mainly number in eight countries: Canada, Chile, Finland, Lithuania, Malaysia, the Philippines, Thailand, and the United States. Internationally on average, more than half the students were taught a combination of mathematics topics (i.e., combined algebra, geometry, number, etc.). However, there was considerable variation among countries, ranging from all students in England being given the combined emphasis to none in the Russian Federation. In the latter, 100 percent of the students were taught combined algebra and geometry. Internationally on average, about one-fifth of the students received the combined algebra and geometry emphasis.

Twenty percent or more of students were in mathematics classes that emphasized algebra in Korea, Morocco, Singapore, and the United States. Very few students were given an emphasis in geometry (three percent on average internationally), with Tunisia the only country where 20 percent or more of the students were in classes that emphasized geometry.

|  | Percentage of Students Whose Teachers Report the Subject Matter Emphasized Most in Their Grade 8 Mathematics Class |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mainly Number | Combined Algebra, Geometry, Number, etc. | Combined Algebra and Geometry | Algebra | Geometry | Other |
| Australia Belgium (Flemish) Bulgaria Canada Chile | 10 (3.3) <br> 0 (0.0) <br> 26 (3.0) <br> 72 (3.6) | 65 (3.6) <br> 27 (4.2) <br> 53 (2.8) <br> 15 (2.8) | 17 (2.3) <br> 64 (4.7) <br> 6 (1.6) <br> 4 (1.7) | $\begin{aligned} & -- \\ & 3(1.2) \\ & 8(3.2) \\ & 6(1.4) \\ & 0(0.0) \end{aligned}$ | $\begin{aligned} & -- \\ & 2(1.3) \\ & 1(0.8) \\ & 1(0.0) \\ & 3(1.3) \end{aligned}$ | $\begin{aligned} & -- \\ & 3(2.3) \\ & 0(0.0) \\ & 9(1.9) \\ & 6(1.9) \end{aligned}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{r} 2(1.1) \\ 1(0.0) \\ 0(0.2) \\ 0(0.0) \\ 32(4.3) \end{array}$ | $\begin{array}{r} 57(4.2) \\ 71(4.4) \\ 76(3.9) \\ 100(0.0) \\ 46(4.6) \end{array}$ | $\begin{array}{r} 24(3.6) \\ 21(3.7) \\ 19(3.9) \\ 0(0.0) \\ 12(3.2) \end{array}$ | $\begin{aligned} & 4(1.7) \\ & 7(2.3) \\ & 4(1.2) \\ & 0(0.0) \\ & 3(1.3) \end{aligned}$ | $\begin{array}{ll} 9 & (2.6) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 4(1.4) \end{array}$ | $\begin{array}{ll} 4 & (1.6) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 3 & (1.5) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 7(2.4) \\ 11(2.6) \\ 10(3.0) \\ 17(4.1) \\ 1(0.4) \end{array}$ | 60 (4.8) <br> 75 (3.1) <br> 71 (4.9) <br> 57 (4.3) <br> 35 (4.0) | $\begin{array}{r} 11(2.8) \\ 8(1.9) \\ 10(2.5) \\ 14(3.1) \\ 42(4.1) \end{array}$ | $\begin{array}{r} 13(3.3) \\ 5(1.6) \\ 5(2.2) \\ 6(2.1) \\ 19(3.4) \end{array}$ | $\begin{aligned} & 4(1.8) \\ & 0(0.0) \\ & 4(2.7) \\ & 6(2.1) \\ & 1(0.6) \end{aligned}$ | $\begin{array}{ll} 5 & (2.1) \\ 0 & (0.0) \\ 0 & (0.4) \\ 0 & (0.0) \\ 2 & (1.3) \end{array}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 2(1.0) \\ 7(2.0) \\ 20(3.6) \\ 6(1.9) \\ 1(0.6) \end{array}$ | $\begin{array}{ll} 67 & (3.8) \\ 30 & (4.1) \\ 71 & (3.9) \\ 51 & (4.0) \\ 71 & (3.7) \end{array}$ | $\begin{array}{r} 22(3.3) \\ 35(4.0) \\ 3(1.5) \\ 20(3.1) \\ 20(3.1) \end{array}$ | $\begin{array}{r} 5(1.8) \\ 16(3.1) \\ 3(1.4) \\ 20(3.4) \\ 7(2.5) \end{array}$ | $\begin{aligned} & 4(1.4) \\ & 9(2.5) \\ & 2(1.2) \\ & 2(1.1) \\ & 0(0.0) \end{aligned}$ | $\begin{array}{ll} 1 & (0.0) \\ 4 & (1.6) \\ 1 & (1.0) \\ 2 & (0.9) \\ 0 & (0.0) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 42(3.9) \\ 8(2.5) \\ 34(4.3) \\ x \times \\ 10(2.1) \end{array}$ | $\begin{gathered} 0(0.0) \\ 51(4.5) \\ 61(4.4) \\ \times x \\ 34(2.7) \end{gathered}$ | $\begin{gathered} 28(3.7) \\ 37(4.1) \\ 1(0.0) \\ x \quad x \\ 20(2.9) \end{gathered}$ | $\begin{gathered} 17(3.2) \\ 4(2.4) \\ 3(1.4) \\ x \quad x \\ 20(2.4) \end{gathered}$ | $\begin{aligned} & 1(1.0) \\ & 1(0.5) \\ & 1(0.0) \\ & \text { x x } \\ & 13(1.9) \end{aligned}$ | $\begin{aligned} & 11(2.6) \\ & 0(0.0) \\ & 1(0.6) \\ & \text { x x } \\ & 3(1.0) \end{aligned}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{r} 4(3.2) \\ 1(0.0) \\ 42(4.4) \\ 4(1.9) \\ 0(0.0) \end{array}$ | $\begin{array}{rr} 77 & (4.6) \\ 98 & (1.3) \\ 47 & (4.6) \\ 72 & (4.1) \\ 0 & (0.0) \end{array}$ | $\begin{array}{r} 13(2.9) \\ 0(0.0) \\ 2(1.3) \\ 21(3.3) \\ 100(0.0) \end{array}$ | $\begin{array}{ll} 2 & (1.1) \\ 0 & (0.0) \\ 3 & (1.7) \\ 2 & (1.4) \\ 0 & (0.0) \end{array}$ | $\begin{array}{ll} 1 & (0.8) \\ 1 & (0.9) \\ 1 & (0.9) \\ 1 & (0.0) \\ 0 & (0.0) \end{array}$ | $\begin{array}{ll} 3 & (1.6) \\ 1 & (0.0) \\ 4 & (1.9) \\ 0 & (0.0) \\ 0 & (0.0) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 8(2.3) \\ 12(3.0) \\ 5(1.9) \\ 3(1.2) \\ 44(3.5) \end{array}$ | 46 (4.5) <br> 74 (4.0) <br> 77 (3.8) <br> 59 (4.4) <br> 47 (3.7) | $\begin{array}{r} 12(2.9) \\ 7(2.0) \\ 14(3.0) \\ 25(3.8) \\ 4(1.6) \end{array}$ | $\begin{array}{r} 29(3.7) \\ 4(1.9) \\ 2(1.1) \\ 10(2.6) \\ 2(1.0) \end{array}$ | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 3 & (1.4) \\ 0 & (0.0) \end{array}$ | $\begin{aligned} & 5(1.7) \\ & 4(1.8) \\ & 4(1.1) \\ & 1(0.8) \\ & 2(1.4) \end{aligned}$ |
| Tunisia <br> Turkey <br> United States | $\begin{gathered} 8(2.5) \\ -- \\ 28(3.0) \end{gathered}$ | $\begin{gathered} 41(4.4) \\ -- \\ 32(3.4) \end{gathered}$ | $\begin{gathered} 21(3.3) \\ -- \\ 6(1.6) \end{gathered}$ | $\begin{gathered} 8(2.4) \\ -- \\ 27(2.7) \end{gathered}$ | $\begin{gathered} 22(3.4) \\ -- \\ 1(0.8) \end{gathered}$ | $\begin{aligned} & 1(0.7) \\ & -- \\ & 6(1.4) \end{aligned}$ |
| International Avg. | 14 (0.4) | 55 (0.6) | 19 (0.5) | 8 (0.4) | 3 (0.2) | 2 (0.2) |

## Background data provided by teachers.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students. An "x" indicates teacher response data available for $<50 \%$ of students.

## Are There National or Regional Policies on Using Calculators?

"「
For the timss 1999 countries, official policies on calculator use are summarized in Exhibit 5.9. The data indicate wide variation across countries, ranging from encouraging unrestricted use, through use with restrictions, to banning calculator use entirely. Official documents of 23 countries included an explicit policy on the use of calculators. Seven of these reported that their curriculum policy allowed unrestricted use of calculators, and 14 restricted use. In Canada and the United States, policy varied across provinces and states, respectively.

Several countries commented that calculators were not permitted in lower grades of their primary school systems, and others that the use of calculators in these grades was limited so that students could master basic computational skills, both mentally and using pencil and paper. During preparation of the original timss tests, the question whether students should be permitted to use calculators in the test was considered, but for equity reasons timss decided not to permit the use of calculators at the middle school grades.

| AustraliaBelgium (Flemish) | Curriculum Contains Recommendations About Use of Calculators | Type of Policy | Comments |
| :---: | :---: | :---: | :---: |
|  | Yes | Unrestricted Use | Calculators are unrestricted as a teaching/learning tool. Computational skills like mental arithmetic are also promoted. |
|  | Yes | Restricted Use | Calculators are permitted on a limited basis so that students can master the basic skills of computation and mental calculation. Calculator usage increases and is compulsory after grade 9. |
| Bulgaria Canada | No |  |  |
|  | Yes | Unrestricted, 2 provinces, Restricted, 8 provinces | In general, calculator use is encouraged, except in lower grades in some provinces. |
| Chile | No |  |  |
| Chinese Taipei | Yes | Restricted Use | Calculators are not allowed on entrance exams so teachers limit their use in the classroom. |
| Cyprus <br> Czech Republic | Yes | Restricted Use | Calculators are not permitted in final exams until grade 10. |
|  | Yes | Restricted Use | Computational skills are practiced without calculators. |
| England | Yes | Restricted Use | Calculator use increases as students progress through school. The emphasis is on pupils having a range of skills: calculator, pencil and paper, and mental computation. Graphic calculators are required at higher levels. |
| Finland | Yes | Unrestricted Use | Although permitted at the lower levels, policy indicates that the use of calculators is more appropriate at the upper levels (grades 7-9). |
| Hong Kong, SAR | Yes | Unrestricted Use | Calculators may be used for exploration only from grades 1 to 6 . No restrictions are set on the use of calculators for students from grade 7 onwards. |
| Hungary | Yes | Restricted Use | Calculator use considered appropriate in higher grades. |
| Indonesia | Yes | Restricted Use | Calculators are not permitted in lower grades. |
|  | No |  |  |
| Israel | Yes | Unrestricted Use | Calculators are permitted through all school levels (grades 1-12). |
| Italy <br> Japan Jordan <br> Rep. of <br> ia (LSS) | No |  |  |
|  | Yes | Unrestricted Use | Calculators are not permitted until grade 5. |
|  | Yes | Restricted Use | The curriculum does not contain an explicit policy on classroom use of calculators, but policy does indicate that calculator usage is prohibited during tests. |
|  | Yes | Restricted Use | Currently, calculators are not used in class. However, the new curriculum, to be implemented in 2000/1, recommends the wide use of calculators. |
|  | No |  |  |
| Lithuania <br> Macedonia, Rep. Of <br> Malaysia <br> Moldova <br> Morocco | No |  |  |
|  | No |  |  |
|  | No |  | Calculators are used as learning aids. At the secondary level, calculators may be used in public exams when calculation and computational skills are not being assessed. |
|  | Yes | Restricted Use | For specific problems, a calculator is acceptable. |
|  | No |  |  |
| Netherlands | Yes | Unrestricted Use | Calculators are compulsory at national exam level. In grades 11-12 the graphic calculator is compulsory for mathematics students. |
| New Zealand | Yes | Unrestricted Use | The policy assumes that calculators will be available and used "appropriately" at all levels. |
| Philippines | No |  | In the high school, calculators are used mainly for statistics and trigonometry. |
| Romania <br> Russian Federation | No |  |  |
|  | Yes | Restricted Use | There is some use of calculators in elementary school. Recommended use of calculators on a level with oral and written calculations in secondary school. Students are not allowed to use calculators on public exams in grades 9 and 11. |
| Slovak Republic <br> Slovenia <br> South Africa | Yes | Restricted Use | In primary school, students are not allowed to use calculators in mathematics. In secondary school, the use of calculators is allowed from grade 7, though the use is restricted. |
|  | - | - |  |
|  | No |  |  |
|  | Yes | Restricted Use | As students progress through school, the policy becomes less restricted. For grades 8-12, the policy restriction indicates that students may not use a programmable calculator. |
| Thailand | No |  |  |
| Tunisia | Yes | Restricted Use | Calculators are not permitted until grade 8. |
| Turkey | No |  |  |
| United States | Yes | Varies from state to state |  |

[^33]
## What Mathematics Topics Are Included in the Intended Curriculum?

In the course of their meetings on planning and implementation of timss 1999, the National Research Coordinators developed a list of mathematics topics that they agreed covered most of the content in the intended mathematics curriculum in their respective countries. This list of topics, presented in Exhibit 5.10, built on the topics covered in the timss 1995 mathematics test and included in the teacher questionnaire. It represents a comprehensive list of the topics likely to have been included in the curricula of the participating countries up to and including eighth grade. From the following choices, the National Research Coordinators indicated the percentage of students in their own countries expected to have been taught each topic:

- All or almost all students (at least go percent)
- About half of the students
- Only the more able students (top track - about 25 percent)
- Only the most advanced students (1o percent or less).

Exhibit 5.11 summarizes the data according to the percentage of topics intended to be taught to all or almost all students (at least go percent) in each country, across the entire list of topics and for each content area. On average across countries, curricular guidelines called for nearly all students to have been taught three-fourths of the topics overall. Internationally on average, the greatest percentage of topics intended to be taught to 90 percent or more of the students was in fractions and number sense ( 86 percent) and in measurement ( 83 percent).

About two-thirds of the topics in geometry ( 67 percent) and algebra (68 percent), internationally on average, were expected to have been taught to nearly all students. In eight countries, including high-performing Japan, Korea, and Singapore, countries reported that 10 or more of the 11 algebra topics were intended to be taught to at least go percent of the students. Information on specific topics in the intended curricula for each content area is presented in Exhibits R2.3 through R2.7 in the reference section of this report.

The least agreement between the intended curricula and the topic areas was in data representation, analysis, and probability, with an international average of 60 percent of the topics intended to be taught. Only seven countries intended for all five topics listed for this content area to be taught to nearly all students: Australia, Canada, Moldova, New Zealand, the Russian Federation, Turkey, and the United States.

It should be noted that some countries reported having different curricula or different levels of curriculum for different groups of students, as detailed in Exhibit 5.6. Not surprisingly, then, these countries often reported that about half, only the more able ( 25 percent), or the top io percent of students were expected to have been taught substantial percentages of the topics, in particular those in geometry and algebra. The three countries with the lowest percentages of topics overall intended to be taught to nearly all students have differentiated curricula - England, Israel, and the Netherlands.

In addition, if content within a topic area required different responses, National Research Coordinators chose the response that best represented the entire topic area and noted the discrepancy (see Exhibit A. 11 in the appendix for details).

## Exhibit 5.10 Mathematics Topics Included in the TIMSS Questionnaires

## Fractions and Number Sense

- Whole numbers - including place values, factorization and operations (+, -, x, $\div$ )
- Understanding and representing common fractions
- Computations with common fractions
- Understanding and representing decimal fractions
- Computations with decimal fractions
- Relationships between common and decimal fractions, ordering of fractions
- Rounding whole numbers and decimal fractions
- Estimating the results of computations
- Number lines

Whole number powers of integers

- Computations with percentages and problems involving percentages
- Simple computations with negative numbers
- Square roots (of perfect squares less than 144), small integer exponents

Prime factors, highest common factor, lowest common multiple, rules for divisibility

- Sets, subsets, union, intersection, Venn diagrams

Rate problems

- Concepts of ratio and proportion; ratio and proportion problems


## Measurement

- Units of measurement; standard metric units
- Reading measurement instruments
- Estimates of measurement; accuracy of measurement

Conversions of units between measurement systems

- Perimeter and area of simple shapes - triangles, rectangles and circles
- Perimeter and area of combined shapes
- Volume of rectangular solids - i.e., Volume $=$ length x width x height

Volume of other solids (e.g., pyramids, cylinders, cones, spheres)
Computing with measurements ( $+,-, x, \div)$

- Scales applied to maps and models


## Data Representation, Analysis, and Probability

Collecting and graphing data from a survey

- Representation and interpretation of data in graphs, charts, and tables
- Arithmetic mean

Median and mode

- Simple probabilities - understanding and calculations

Topics included in the curriculum and teacher questionnaires (intended and implemented curriculum)
Topics also included in the curriculum questionnaire (intended curriculum).


## Geometry

- Cartesian coordinates of points in a plane
- Coordinates of points on a given straight line
- Simple two dimensional geometry - angles on a straight line, parallel lines, triangles and quadrilaterals
- Congruence and similarity
- Angles - (acute, right, supplementary, etc.)
- Pythagorean theorem (without proof)
- Symmetry and transformations (reflection and rotation)
- Visualization of three-dimensional shapes
- Geometric constructions with straight-edge and compass
- Regular polygons and their properties - names (e.g., hexagon and octagon), sum of angles, etc.
- Proofs (formal deductive demonstrations of geometric relationships)

Sine, cosine, and tangent in right-angle triangles
Nets of solids

## Algebra

- Number patterns and simple relations
- Writing expressions for general terms in number pattern sequence
- Translating from verbal descriptions to symbolic expressions
- Simple algebraic expressions
- Evaluating simple algebraic expressions by substitution of given value of variables
- Representing situations algebraically; formulas
- Solving simple equations
- Solving simple inequalities
- Solving simultaneous equations in two variables
* Interpreting linear relations
- Using the graph of a relationship to interpolate/extrapolate

Topics included in the curriculum and teacher questionnaires (intended and implemented curriculum).
Topics also included in the curriculum questionnaire (intended curriculum).

Exhibit 5.11 Mathematics Topics in the Intended Curriculum for At Least 90\% of Students, Up to and Including Eighth Grade

TIMSS 1999
8
Mathematics

|  | Percentage of Topics Intended to Be Taught to All or Almost All (at least 90\%) Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Overall | Fractions and Number Sense | Measurement | Data <br> Representation, Analysis, and Probability | Geometry | Algebra |
| Australia | 89 | 94 | 100 | 100 | 85 | 73 |
| Belgium (Flemish) | 80 | 100 | 90 | 80 | 62 | 64 |
| Bulgaria | 82 | 88 | 100 | 40 | 77 | 82 |
| Canada | 82 | 94 | 90 | 100 | 77 | 55 |
| Chile | 61 | 76 | 80 | 80 | 54 | 18 |
| Chinese Taipei | 59 | 82 | 50 | 40 | 46 | 55 |
| Cyprus | 63 | 82 | 70 | 0 | 54 | 64 |
| Czech Republic | 77 | 94 | 90 | 80 | 69 | 45 |
| England | 25 | 29 | 30 | 40 | 23 | 9 |
| Finland | 57 | 65 | 80 | 60 | 31 | 55 |
| Hong Kong, SAR | 79 | 94 | 80 | 40 | 77 | 73 |
| Hungary | 77 | 94 | 60 | 60 | 69 | 82 |
| Indonesia | 86 | 94 | 100 | 60 | 85 | 73 |
| Iran, Islamic Rep. | 80 | 88 | 100 | 40 | 77 | 73 |
| Israel | 41 | 47 | 40 | 60 | 23 | 45 |
| Italy | 91 | 100 | 80 | 80 | 92 | 91 |
| Japan | 89 | 82 | 100 | 80 | 85 | 100 |
| Jordan | 89 | 100 | 100 | 80 | 85 | 73 |
| Korea, Rep. of | 80 | 82 | 100 | 80 | 54 | 91 |
| Latvia (LSS) | 70 | 82 | 80 | 20 | 54 | 82 |
| Lithuania | 80 | 94 | 100 | 40 | 69 | 73 |
| Macedonia, Rep. of | 59 | 59 | 60 | 0 | 69 | 73 |
| Malaysia | 80 | 94 | 90 | 40 | 85 | 64 |
| Moldova | 95 | 94 | 90 | 100 | 92 | 100 |
| Morocco | 59 | 82 | 90 | 40 | 54 | 9 |
| Netherlands | 46 | 53 | 40 | 60 | 54 | 27 |
| New Zealand | 80 | 100 | 70 | 100 | 69 | 64 |
| Philippines | 71 | 94 | 90 | 80 | 23 | 73 |
| Romania | 93 | 100 | 100 | 20 | 100 | 100 |
| Russian Federation | 75 | 88 | 60 | 100 | 62 | 73 |
| Singapore | 89 | 94 | 100 | 80 | 77 | 91 |
| Slovak Republic | - | - | - | - | - | - |
| Slovenia | 91 | 100 | 100 | 40 | 92 | 91 |
| South Africa | 73 | 88 | 100 | 0 | 69 | 64 |
| Thailand | 73 | 88 | 90 | 40 | 54 | 73 |
| Tunisia | 79 | 100 | 90 | 60 | 62 | 64 |
| Turkey | 91 | 88 | 90 | 100 | 85 | 100 |
| United States | 93 | 100 | 100 | 100 | 85 | 82 |
| International Avg. | 75 | 86 | 83 | 60 | 67 | 68 |

$\square$

$\square$


## Have Students Been Taught the Topics Tested by TIMSS?

In interpreting the achievement results, it is important to consider how extensively the topics tested are taught in the participating countries. As shown in Exhibits 5.12 through 5.16 , the five major mathematics content areas assessed in timss 1999 were represented by 34 topic areas. For each area, teachers indicated whether their students had been taught the topics before this year, one to five periods this year, more than five periods this year; whether the topics had not yet been taught; or whether the teacher did not know. Exhibits 5.12 through $5 \cdot 16$ show the percentages of students in each country reported to have been taught each topic before or during the year of the testing.

According to their teachers, nearly all of the students in all of the countries had been taught the topics in fractions and number sense, as
shown in Exhibit 5.12. The international average for each topic exceeded go percent of students, with the exception of "square roots (of perfect squares less than 144), small integer exponents" and "concepts of ratio and proportions; ratio and proportion problems," with averages of 83 and 87 percent, respectively. Exhibit R2.8 in the reference section indicates that many students had instruction in these topics before the eighth grade.

Similarly, instructional coverage was high for the measurement topics presented in Exhibit $5 \cdot 13$. At least 87 percent of students, on average internationally, were taught five of the six topics. The topic with the lowest international average was "scales applied to maps and models." Two topics, "units of measurement; standards metric units" and "perimeter and area of simple shapes - triangles, rectangles, and circles," were taught to 96 percent of the students on average, internationally. As indicated by Exhibit R2.9 in the reference section, measurement topics received less emphasis in the eighth grade than
 fractions and number sense topics (see Exhibit R2.8). As with fractions and number sense, substantial percentages of students had studied the measurement topics before the eighth grade.

Corresponding to the reports for the intended curricula, teachers reported lower average percentages internationally across the data representation, analysis, and probability topic areas, shown in Exhibit 5.14. Teachers were asked about three topics in this content area, including "representation and interpretation of data in graphs, charts, and tables." Most of the test items in this content area dealt with interpretation of graphs and tables, and the international average for students who were taught this topic was 75 percent. The average percentages of
students taught the other two topics in this content area were 70 percent for "arithmetic mean" and 43 percent for "simple probabilities." In 22 countries, teachers indicated that less than half the students were taught the latter topic. For most students, the topics in this content area were receiving moderate attention at the eighth grade, and few students had been taught them at earlier grades (see Exhibit R2.10).

Teachers reported a range of instructional coverage across topics in geometry, presented in Exhibit 5.15. "Simple two dimensional geometry angles on a straight line, parallel lines, triangles and quadrilaterals" was reported to have been taught internationally on average to 95 percent of the students, and "visualization of three-dimensional shapes" was taught to only 57 percent. The two topics showing the greatest variation across countries were "symmetry and transformations" and "visualization of three-dimensional shapes." In more than nine countries, these topics were reported to be taught to less than 50 percent of the students, and in at least 15 countries to 70 percent or more of the students. As shown in Exhibit R2.11 in the reference section, only small percentages of students had completed instruction in the geometry topics before the eighth grade. According to their teachers, most were receiving moderate emphasis on the geometry topics in the eighth grade. On average internationally, 22 percent of students had not yet been taught $5^{\circ}$ percent or more of the geometry topics.

Teachers across countries reported that most students had studied the algebra topics. The international average percentage of students taught each of these topics exceeded 85 percent, with the exception of "solving simple inequalities," with an average of 66 percent. Four of the five topics were taught to 70 percent or fewer of the students in three countries, Chile, Finland, and the Philippines. In contrast, substantial percentages of students ( 90 percent or more) had been introduced to all algebra topics before or during the eighth grade in ten countries, including high-performing Japan, Korea, and Singapore. For many countries, however, teachers reported presenting algebra topics during the eighth grade for substantial percentages of students (see Exhibit R2.12).


Exhibits 5.12-5.16 Overleaf

Exhibit 5.12 Percentages of Students Taught Fractions and Number Sense Topics*


[^34]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. $A n$ " $s$ " indicates teacher response data available for $50-69 \%$ of students. An "x" indicates teacher response data available for $<50 \%$ of students.

|  | Estimating the results of computations | Number lines | Computations with percentages and problems involving percentages | Simple computations with negative numbers | Square roots (of perfect squares less than 144), small integer exponents | Concepts of ratio and proportions; ratio and proportion problems |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Australia Belgium (Flemish) Bulgaria Canada Chile |  $96(1.4)$ <br> $r$ $94(2.0)$ <br> $s$ $98(1.2)$ <br> $r$ $100(0.3)$ <br>  $88(2.7)$ |  $99(0.9)$ <br>  $96(2.5)$ <br> $r$ $47(5.3)$ <br> $r$ $100(0.1)$ <br>  $99(0.9)$ |  $97(1.5)$ <br>  $93(2.1)$ <br> s $97(1.7)$ <br> $r$ $98(0.8)$ <br>  $80(3.1)$ |  $99(1.0)$ <br>  $89(2.6)$ <br> s $99(1.3)$ <br> $r$ $97(1.6)$ <br>  $77(3.2)$ |  $94(2.2)$ <br>  $80(2.2)$ <br> $r$ $38(4.3)$ <br> $r$ $96(1.2)$ <br>  $57(3.7)$ |  $86(3.6)$  <br>  70 $(2.8)$ <br> $r$ $98(1.0)$  <br> $r$ $95(1.3)$  <br>  88 $(2.3)$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{rr}  & 95(2.0) \\ r & 96(2.1) \\ & 100(0.0) \\ s & 96(1.7) \\ & 86(3.6) \end{array}$ | $\begin{array}{lr}  & 99(0.8) \\ \text { s } & 100(0.0) \\ & 100(0.0) \\ s & 97(1.3) \\ & 96(1.9) \end{array}$ | $\begin{array}{rr}  & 94(1.9) \\ r & 100(0.0) \\ & 100(0.0) \\ \text { s } & 96(1.3) \\ & 48(4.3) \end{array}$ | $\begin{array}{rr}  & 100(0.3) \\ r & 100(0.0) \\ & 100(0.0) \\ \text { s } & 96(1.3) \\ & 98(1.6) \end{array}$ | $\begin{array}{lr}  & 96(1.6) \\ \text { s } & 100(0.0) \\ & 100(0.0) \\ \text { s } & 87(2.0) \\ & 20(3.1) \end{array}$ | $\begin{array}{rr}  & 90(2.6) \\ \text { r } & 100(0.0) \\ & 100(0.2) \\ \mathrm{s} & 79(2.7) \\ & 14(3.1) \end{array}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | $\begin{array}{rr} r & 94(2.2) \\ & 100(0.0) \\ & 97(2.0) \\ r & 86(3.2) \\ r & 94(1.5) \end{array}$ | 92 (2.6) <br> 95 (1.6) <br> 100 (0.0) <br> 100 (0.0) <br> 99 (0.5) | $\begin{array}{r} 95(1.9) \\ 100(0.0) \\ 100(0.0) \\ 99(1.1) \\ 92(2.1) \end{array}$ | $\begin{array}{r} 99(0.8) \\ 100 \\ \hline 0.0 \\ 99 \\ \hline \end{array}(0.4)$ | $98(1.2)$ $99(0.8)$ $98(1.3)$ $100(0.0)$ $r \quad 83(2.9)$ | $91(2.5)$ $98(1.0)$ $92(2.9)$ $r \quad 100(0.0)$ $r$ $35(4.5)$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) |  | $\begin{array}{rr} 99 & (0.8) \\ 100 & (0.0) \\ 100 & (0.0) \\ 98 & (1.2) \\ 30 & (4.3) \end{array}$ | $\begin{array}{r} 96(1.6) \\ 100(0.0) \\ 100(0.0) \\ 92(2.0) \\ 100(0.0) \end{array}$ | $\begin{array}{r} 98(1.1) \\ 100(0.0) \\ 100(0.0) \\ 95(1.8) \\ 100(0.0) \end{array}$ | $\begin{array}{r} 100(0.0) \\ 14(3.0) \\ 100(0.0) \\ 64(4.1) \\ 98(0.7) \end{array}$ | $\begin{array}{ll} 99 & (0.8) \\ 97 & (1.6) \\ 99 & (0.5) \\ 90 & (2.3) \\ 98 & (1.1) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{gathered} -- \\ 82(3.2) \\ 98 \text { (1.1) } \\ -- \\ -- \end{gathered}$ | $\begin{array}{cc}  & -- \\ r & 83(3.1) \\ & 100(0.0) \\ & -- \\ & -- \end{array}$ | $\begin{gathered} 92(2.3) \\ 96(1.5) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 88(2.7) \\ 99(0.6) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 91(2.5) \\ 98(1.0) \\ -- \\ -- \end{gathered}$ | $\begin{array}{cc}  & -- \\ & \\ 97(1.9) \\ 97(1.3) \\ & -- \\ & -- \end{array}$ |
|  | $\begin{array}{cc} r & 99(1.0) \\ & 97(0.9) \\ 91(2.3) \\ & 99(0.9) \\ & -- \end{array}$ | $\begin{array}{r} 99(0.9) \\ 97 \\ 94(1.5) \\ 94 \\ 100(0.1) \\ -- \end{array}$ | $\begin{gathered} 98 \\ 93 \\ 93 \\ (1.2) \\ 97 \\ (1.5) \\ 100(0.0) \\ - \end{gathered}$ | $\begin{gathered} 98(1.4) \\ 96 \\ 97 \\ 87 \\ (3.2) \\ 100(0.0) \\ - \end{gathered}$ | $\begin{array}{r} 92(3.1) \\ 86 \\ 65 \\ 65 \\ (4.8) \\ 100 \\ (0.0) \\ - \end{array}$ | $\begin{gathered} \text { r } \quad 80(5.8) \\ 67(3.8) \\ 92(2.4) \\ 100(0.0) \\ \\ \\ \\ \end{gathered}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | 100 (0.4) <br> 99 (0.6) <br> 98 (1.3) <br> 94 (2.1) | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 98(1.0) \end{gathered}$ | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 100(0.0) \end{gathered}$ | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 98(1.1) \end{gathered}$ | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 94(2.3) \end{gathered}$ | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 99(0.8) \end{gathered}$ |
| Tunisia <br> Turkey United States | $\begin{array}{cc} \text { s } & 35(4.5) \\ & \text { x } \\ & 100 \\ & (0.2) \end{array}$ | $54(4.4)$ <br>  <br> $80(2.8)$ <br>  <br>  <br>  <br>  <br> $9(0.5)$ | 81 (3.6) 97 (1.6) 96 (1.4) | $\begin{array}{ll} 92 & (2.5) \\ 99 & (0.7) \\ 97 & (1.1) \end{array}$ | $\begin{array}{ll} 20 & (3.7) \\ 96 & (1.2) \\ 82 & (3.7) \end{array}$ | $\begin{array}{ll} \text { r } & 35(4.3) \\ & 99(0.4) \\ & 93(1.8) \end{array}$ |
| International Avg. | 93 (0.4) | 92 (0.3) | 95 (0.3) | 97 (0.2) | 83 (0.4) | 87 (0.4) |

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \& Units of measurement, standard metric units \& Reading measurement instuments \& Estimates of measurement, accuracy of measurement \& Perimeter and area of simple shapes triangles, rectangles, and circles \& Perimeter and area of combined shapes \& Volume of rectangular solids i.e., volume \(=\) length \(\times\) width \(\times\) height \& Scales applied to maps and models \\
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& \begin{tabular}{r} 
\\
\\
\\
\\
\(99(1.0)\) \\
5 \\
\hline \\
\hline
\end{tabular}\(\quad 98(1.8)\) \& \[
\begin{array}{ll}
\mathrm{r} \& 96(2.0) \\
\mathrm{r} \& 83(3.8) \\
\mathrm{s} \& 87(3.1) \\
\mathrm{r} \& 97(1.2) \\
\& 74(3.6)
\end{array}
\] \& \begin{tabular}{rr} 
\& \(94(2.2)\) \\
\(r\) \& \(85(4.1)\) \\
s \& \(92(2.7)\) \\
\(r\) \& \(97(1.0)\) \\
\& \(67(3.9)\)
\end{tabular} \&  \& \[
\begin{array}{ll} 
\& 97(1.4) \\
r \& 85(3.9) \\
\mathrm{s} \& 84(4.2) \\
\mathrm{r} \& 96(1.3) \\
\& 74(3.8)
\end{array}
\] \& \[
\begin{array}{ll} 
\& 85(3.2) \\
\& 89(3.5) \\
\mathrm{s} \& 94(2.6) \\
\mathrm{r} \& 68(2.7) \\
\& 45(4.4)
\end{array}
\] \& \begin{tabular}{rr} 
\& \(73(4.4)\) \\
\& \(88(2.2)\) \\
5 \& \(87(3.0)\) \\
\(r\) \& \(92(2.1)\) \\
\& \(49(4.0)\)
\end{tabular} \\
\hline Chinese Taipei Cyprus Czech Republic England Finland \& \[
\begin{array}{rr} 
\& 96(1.7) \\
\text { s } \& 100(0.0) \\
\& 100(0.2) \\
\text { s } \& 98(0.9) \\
\& 98(0.9)
\end{array}
\] \& \begin{tabular}{cc} 
\& \(95(2.0)\) \\
\& x \\
\& \\
r \& \(99(0.6)\) \\
s \& \(96(1.3)\) \\
r \& \(88(3.0)\)
\end{tabular} \& \begin{tabular}{cc} 
\& \(90(2.7)\) \\
\& x x \\
\& \(97(1.2)\) \\
S \& \(86(2.8)\) \\
r \& \(77(4.0)\)
\end{tabular} \& \[
\begin{array}{rr} 
\& 100(0.3) \\
\text { s } \& 100(0.0) \\
\& 100(0.0) \\
\text { s } \& 98(1.0) \\
\& 65(4.2)
\end{array}
\] \& \[
\begin{array}{rr} 
\& 92(2.3) \\
\text { s } \& 100(0.0) \\
\& 90(3.2) \\
\text { s } \& 96(1.1) \\
\& 51(4.5)
\end{array}
\] \& \[
\begin{array}{rr} 
\& 99(0.7) \\
\mathrm{r} \& 67(3.7) \\
\& 100(0.0) \\
\mathrm{s} \& 93(1.4) \\
\& 58(4.3)
\end{array}
\] \& \(r\)
\(74(3.8)\)
\(43(5.0)\)

$98(1.2)$
5
$76(2.6)$

$20(3.7)$ <br>

\hline | Hong Kong, SAR |
| :--- |
| Hungary |
| Indonesia |
| Iran, Islamic Rep. |
| Israel | \& \[

$$
\begin{array}{r}
98(1.2) \\
100(0.0) \\
96(1.6) \\
\\
91(2.7) \\
r \quad 90(2.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
96(1.9) \\
\\
\\
\\
\\
\\
\\
\\
94(00(0.2) \\
\mathrm{s} \\
\mathrm{~s} \\
\hline 86(2.6) \\
\hline
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
92(2.5) \\
100(0.2) \\
\\
87(3.5) \\
\\
86(3.0) \\
\mathrm{s} \quad 81(3.9)
\end{array}
$$
\] \& $100(0.0)$

$99(0.6)$
$100(0.0)$
$100(0.0)$
$r \quad 84(3.1)$ \& $99(0.8)$
$97(1.2)$
$98(1.1)$
$97(1.6)$
$r \quad 62(4.0)$ \& $98(1.5)$
$98(1.1)$
$87(3.6)$
$97(1.7)$

$r \quad 47(4.7)$ \& |  | $91(2.7)$ |
| ---: | ---: | ---: |
|  | $90(2.5)$ |
|  | $94(2.1)$ |
|  | $81(4.1)$ |
| 5 | $43(5.0)$ | <br>


\hline | Italy |
| :--- |
| Japan |
| Jordan |
| Korea, Rep. of Latvia (LSS) | \& \[

$$
\begin{array}{r}
100(0.0) \\
90(2.5) \\
100(0.0) \\
85(2.7) \\
99(0.7)
\end{array}
$$
\] \& $96(1.6)$

$r \quad 84(3.3)$
$100(0.0)$
$84(2.7)$
$92(2.7)$ \& $90(2.3)$
$r \quad 66(4.2)$
$97(1.6)$
$93(2.1)$

$71(4.5)$ \& | 99 (0.8) |
| :--- |
| 99 (0.7) |
| 100 (0.0) |
| 98 (1.2) |
| 96 (1.8) | \& \[

$$
\begin{array}{ll}
96 & (1.3) \\
78 & (3.3) \\
99 & (0.9) \\
95 & (1.8) \\
72 & (4.6)
\end{array}
$$

\] \& | 95 (1.4) |
| :--- |
| 98 (1.4) |
| 99 (0.5) |
| 98 (1.0) |
| 81 (3.9) | \& | 91 (2.2) |
| :--- |
| 84 (3.1) |
| 88 (3.1) |
| 73 (3.4) |
| 94 (2.4) | <br>


\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{gathered}
-- \\
88(2.7) \\
96 \text { (1.7) } \\
-- \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{array}{cc} 
& -- \\
r & 81(3.7) \\
& 93(2.0) \\
& -- \\
& --
\end{array}
$$

\] \& |  |
| :---: |
|  |
|  |
|  |
| $82(3.4)$ |
|  |
|  |
|  |
|  |
|  |
|  |
|  |
|  |
|  |
|  |
| - | \& \[

$$
\begin{gathered}
-- \\
92(2.8) \\
97(2.0) \\
-- \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{array}{cc} 
& -- \\
r & 91(3.0) \\
& 95(2.3) \\
& -- \\
& --
\end{array}
$$

\] \& \[

$$
\begin{array}{cc} 
& -- \\
r & 95(1.5) \\
& 91(2.4) \\
& -- \\
& --
\end{array}
$$

\] \& \[

$$
\begin{array}{cc} 
& -- \\
\text { s } & 70(4.4) \\
& 86(3.0) \\
& -- \\
& --
\end{array}
$$
\] <br>

\hline  \& $$
\begin{array}{cc}
r \quad 93(4.7) \\
& 99(0.8) \\
88(2.8) \\
100(0.0) \\
& --
\end{array}
$$ \& \[

$$
\begin{array}{cc}
s & 54(8.4) \\
& 95(1.6) \\
83(3.4) \\
& 100(0.0) \\
& --
\end{array}
$$

\] \& \[

$$
\begin{array}{cc}
r \quad 78(6.3) \\
85(2.9) \\
82(3.3) \\
& 96(1.7) \\
& --
\end{array}
$$

\] \& | 98 (1.2) |
| :--- |
| 95 (1.8) |
| 92 (2.3) |
| 100 (0.0) | \& | 84 (4.9) |
| :--- |
| 92 (2.1) |
| 83 (3.1) |
| 99 (0.9) |
| - - | \& | 89 (4.9) |
| :--- |
| 92 (1.8) |
| 76 (3.7) |
| 99 (0.9) |
| -- | \& | 88 (5.3) |
| :--- |
| 66 (4.1) |
| 40 (4.4) |
| 98 (1.3) |
| $--$ | <br>


\hline Singapore Slovak Republic Slovenia South Africa Thailand \& | 100 (0.0) |
| :--- |
| 99 (1.2) |
| 100 (0.0) |
| 91 (2.5) | \& \[

$$
\begin{array}{cc}
r & 98(1.2) \\
r & 77(4.2) \\
& 91(2.7) \\
& -- \\
& 86(3.0)
\end{array}
$$

\] \& \[

$$
\begin{gathered}
98(1.3) \\
r \quad 93(2.7) \\
93(2.2) \\
-- \\
88(2.7)
\end{gathered}
$$

\] \& \[

$$
\begin{gathered}
100(0.0) \\
100(0.0) \\
100(0.0) \\
-- \\
95(1.8)
\end{gathered}
$$

\] \& \[

$$
\begin{array}{r}
100(0.0) \\
99(0.8) \\
100(0.0) \\
-- \\
78(3.7)
\end{array}
$$

\] \& | 100 (0.0) |
| :--- |
| 97 (1.5) |
| 97 (1.3) |
| 99 (0.7) | \& | 96 (1.6) |
| :--- |
| 99 (1.2) |
| 97 (1.7) |
| 85 (3.0) | <br>


\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& \[

$$
\begin{array}{ll}
94 & (2.2) \\
89 & (2.6) \\
96 & (1.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
r & 74(3.9) \\
& 88(2.4) \\
r & 92(1.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
r & 53(4.6) \\
& 90(2.2) \\
r & 91(1.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
98 & (1.3) \\
92 & (2.2) \\
95 & (1.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
89 & (2.6) \\
79 & (3.1) \\
90 & (1.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
89 & (2.5) \\
56 & (3.8) \\
83 & (2.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
r & 47(5.2) \\
r & 60(3.6) \\
r & 84(2.5)
\end{array}
$$
\] <br>

\hline International Avg. \& 96 (0.3) \& 89 (0.5) \& 87 (0.5) \& 96 (0.3) \& 89 (0.5) \& 87 (0.5) \& 77 (0.6) <br>
\hline
\end{tabular}

Background data provided by teachers.

* Taught before or during this school year.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

A dash (-) indicates data are not available.
An "r" indicates teacher response data available for $70-84 \%$ of students. An "s" indicates teacher response data available for $50-69 \%$ of students. An " $x$ " indicates teacher response data available for $<50 \%$ of students.

## Exhibit 5.14 Percentages of Students Taught Data Representation, Analysis, and Probability Topics*

|  | Representation and interpretation of data in graphs, charts, and tables | Arithmetic mean | Simple probabilities understanding and calculations |
| :---: | :---: | :---: | :---: |
| Australia Belgium (Flemish) Bulgaria Canada Chile | 92 $(2.4)$ <br> 86 $(4.1)$ <br> 71 $(6.6)$ <br> 91 $(2.4)$ <br> 49 $(3.8)$ | $\begin{array}{ll} 74 & (3.5) \\ 93 & (2.1) \\ 39 & (5.5) \\ 81 & (2.7) \\ 49 & (3.5) \end{array}$ |  $52(4.3)$ <br> $r$ $24(3.0)$ <br> $r$ $10(2.6)$ <br> $r$ $72(3.3)$ <br>  $35(3.6)$ |
| Chinese Taipei Cyprus Czech Republic England Finland |  $11(2.3)$ <br> $r$ $1(0.1)$ <br>  $49(5.6)$ <br>  $99(0.4)$ <br>  $65(3.5)$ |  $12(2.7)$ <br> $r$ $6(2.2)$ <br>  $88(3.4)$ <br>  $93(2.3)$ <br>  $62(4.3)$ |  $4(1.6)$ <br> $r$ $0(0.0)$ <br>  $7(2.8)$ <br>  $90(2.4)$ <br>  $14(3.3)$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | 65 (4.5) <br> 99 (0.8) <br> 93 (2.1) <br> 94 (3.8) <br> 62 (4.4) | $\begin{array}{ll} 30 & (4.1) \\ 92 & (2.4) \\ 93 & (2.4) \\ 92 & (3.8) \\ 71 & (3.8) \end{array}$ | 10 (2.8) <br> 56 (3.5) <br> 95 (1.9) <br> 45 (5.0) <br> 28 (3.8) |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) | 84 (3.0) <br> 43 (4.7) <br> 93 (2.6) <br> 95 (1.7) <br> 98 (1.3) | 62 (3.6) <br> 38 (4.5) <br> 93 (2.6) <br> 78 (3.2) <br> 99 (0.6) | $\begin{array}{r} 49(3.8) \\ 3(1.4) \\ 95(1.8) \\ 99(0.6) \\ 40(4.3) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{gathered} 76(4.5) \\ 56(3.8) \\ -- \\ -- \end{gathered}$ | 82 (3.4) <br> 38 (3.5) <br> - - <br> - - | 45 (5.0) <br> 33 (3.7) <br> - - |
| > Netherlands New Zealand Philippines Romania Russian Federation | 87 (4.7) <br> 87 (3.0) <br> 60 (4.2) <br> 95 (2.2) | $\begin{gathered} 77(5.7) \\ 77(3.4) \\ 34(4.3) \\ 100(0.0) \\ -- \end{gathered}$ | 46 (6.5) <br> 61 (3.9) <br> 29 (4.2) <br> 95 (1.7) <br> -- |
| Singapore Slovak Republic Slovenia South Africa Thailand | 97 (1.7) <br> 72 (4.7) <br> 97 (1.4) <br> 90 (2.9) | $\begin{gathered} 88(3.2) \\ 98(1.2) \\ 94(2.2) \\ -- \\ 57(4.3) \end{gathered}$ | s $17(4.2)$ <br>  $30(4.7)$ <br> $r$ $40(4.4)$ <br>  -- <br>  $44(4.2)$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 38 & (4.4) \\ 79 & (2.6) \\ 96 & (1.2) \end{array}$ | $\begin{array}{ll} 28 & (4.0) \\ 93 & (2.2) \\ 93 & (1.6) \end{array}$ | $\begin{array}{r} 6(2.3) \\ 78(4.0) \\ 79(2.3) \end{array}$ |
| International Avg. | 75 (0.6) | 70 (0.6) | 43 (0.6) |

Background data provided by teachers.

* Taught before or during this school year
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash (-) indicates data are not available.
An "r" indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for $50-69 \%$ of students.

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \& Cartesian coordinates of points in a plane \& Coordinates of points on a given straight line \& Simple two dimensional geometry - angles on a straight line, parallel lines, triangles and quadrilaterals \& Congruence and similarity \& Symmetry and transformations (reflection and rotation) \& \& ualization of -dimensional shapes <br>
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& $92(2.4)$
$78(3.0)$
$92(2.5)$
$r \quad 81(2.5)$

$59(3.7)$ \& |  | $80(3.7)$ |
| :--- | :--- |
|  | $54(3.9)$ |
| $r$ | $91(3.9)$ |
| $r$ | $84(2.6)$ |
|  | $65(3.9)$ | \& $96(1.7)$

$91(4.1)$
$r \quad 100(0.5)$
$r$
$94(1.8)$

$96(1.5)$ \& $61(4.2)$
$79(2.5)$

$81(3.6)$
$84(2.7)$

$69(3.8)$ \& |  | $64(3.8)$ |
| ---: | :--- |
|  | $87(2.9)$ |
|  | $82(3.4)$ |
| $r \quad 78(2.4)$ |  |
|  | $26(3.0)$ | \& $r$

$r$

$r$ \& $$
\begin{array}{ll}
75 & (4.2) \\
57 & (4.0) \\
24 & (4.7) \\
63 & (3.2) \\
47 & (4.3)
\end{array}
$$ <br>

\hline Chinese Taipei Cyprus Czech Republic England Finland \& |  | $100(0.0)$ |
| ---: | ---: |
| $r$ | $6(2.5)$ |
|  | $94(2.6)$ |
| $s$ | $94(1.3)$ |
|  | $93(1.9)$ | \& \[

$$
\begin{array}{ll} 
& 99(0.9) \\
& 90(4.3) \\
& 20 \\
& 88(4.9) \\
\mathrm{s} & 79(3.1) \\
& 64(4.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{rr} 
& 78(3.5) \\
\mathrm{r} & 100(0.0) \\
& 100(0.0) \\
\mathrm{s} & 95(1.6) \\
& 88(2.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll} 
& 60(4.3) \\
& 6 \\
& 16(4.0) \\
& 86(3.7) \\
\mathrm{s} & 54(4.1) \\
& 36(3.8)
\end{array}
$$

\] \& |  | $26(3.7)$ |
| :--- | :--- |
|  | $29(4.7)$ |
| r | $23(1.1)$ |
|  | $98(1.6)$ |
| s | $88\left(\begin{array}{l}1 \\ \hline\end{array}\right.$ |
|  | $37(4.0)$ | \& s \& \[

$$
\begin{array}{ll}
42 & (4.1) \\
40 & (5.1) \\
73 & (5.2) \\
75 & (3.0) \\
30 & (4.0)
\end{array}
$$
\] <br>

\hline Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel \& $$
\begin{array}{r}
98(1.3) \\
100(0.3) \\
100(0.0) \\
97(1.4) \\
87(3.1)
\end{array}
$$ \& \[

$$
\begin{array}{r}
95(1.9) \\
92(2.3) \\
\\
\\
\\
\\
\\
r \\
100(0.0) \\
r
\end{array}
$$ \quad 83(3.0)

\] \& 97 (1.6) 99 (0.7) 94 (2.5) 98 (1.0) 91 (2.5) \& | 89 (2.8) |
| :--- |
| 82 (3.1) |
| 66 (3.9) |
| 97 (1.5) |
| 53 (4.0) | \& | r | $31(4.6)$ |
| ---: | :--- |
|  | $97(1.2)$ |
|  | $56(4.2)$ |
|  | $95(1.7)$ |
| $r \quad 21(3.3)$ |  | \& r

r \& $$
\begin{array}{ll}
29 & (4.7) \\
70 & (3.6) \\
28 & (4.1) \\
77 & (4.0) \\
11 & (2.6)
\end{array}
$$ <br>

\hline | Italy |
| :--- |
| Japan |
| Jordan |
| Korea, Rep. of Latvia (LSS) | \& \[

$$
\begin{array}{r}
93(1.9) \\
100(0.0) \\
95(1.9) \\
98(1.1) \\
99(1.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
79 & (3.0) \\
99 & (1.0) \\
93 & (2.5) \\
99 & (0.7) \\
99 & (0.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
98 & (1.2) \\
97 & (1.4) \\
98 & (1.1) \\
99 & (0.7) \\
99 & (0.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
91 & (2.0) \\
98 & (1.2) \\
99 & (0.5) \\
99 & (0.7) \\
72 & (4.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
65 & (3.8) \\
98 & (1.3) \\
27 & (4.0) \\
71 & (3.7) \\
11 & (2.4)
\end{array}
$$

\] \& \& \[

$$
\begin{array}{rr}
89 & (2.4) \\
82 & (2.9) \\
99 & (1.1) \\
52 & (4.2) \\
7 & (1.9)
\end{array}
$$
\] <br>

\hline | Lithuania |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{gathered}
-- \\
95(1.5) \\
\text { x x } \\
-- \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{gathered}
91(2.7) \\
\mathrm{x} \mathrm{x} \\
-- \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{gathered}
90(2.6) \\
96(1.4) \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{array}{cc} 
& -- \\
r & 95(1.5) \\
71(3.1) \\
& -- \\
& --
\end{array}
$$

\] \& \[

$$
\begin{gathered}
-- \\
90(2.6) \\
68(3.7) \\
-- \\
--
\end{gathered}
$$

\] \& r \& \[

$$
\begin{array}{ll}
74 \\
70 & (4.3)
\end{array}
$$
\] <br>

\hline Netherlands
New Zealand
Philippines
Romania

Russian Federation \& \begin{tabular}{rr}
\& $97(1.5)$ <br>
\& $83(2.9)$ <br>
\& $49(4.4)$ <br>
\& $99(0.6)$ <br>
\& --

 \& 

<br>
$r$ \& $97(1.5)$ <br>
$69(3.6)$ <br>
$57(4.3)$ <br>
\& $99(0.6)$ <br>
\& --

\end{tabular} \& \[

$$
\begin{array}{r}
98 \\
97 \\
97 \\
77 \\
77 \\
(1.6) \\
100
\end{array}
$$(0.0)

\] \& \[

$$
\begin{array}{r}
49(5.8) \\
49(4.2) \\
50(4.1) \\
100(0.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
78 & (5.3) \\
76 & (3.1) \\
26 & (3.8) \\
86 & (2.7)
\end{array}
$$

\] \& $r$ \& \[

$$
\begin{array}{cc}
60 & (6.2) \\
70 & (3.7) \\
31 & (3.7) \\
97 & (1.7) \\
--
\end{array}
$$
\] <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& | 91 (2.6) |
| :--- |
| 74 (4.1) |
| 99 (0.9) |
| 91 (2.7) | \& | 93 (2.4) |
| :--- |
| 73 (4.4) |
| 100 (0.0) |
| 88 (3.1) | \& | 96 (1.8) |
| :--- |
| 95 (2.3) |
| 100 (0.0) |
| 90 (2.9) | \& \[

$$
\begin{array}{r}
96(1.9) \\
28(3.7) \\
100(0.0) \\
-- \\
92(2.6)
\end{array}
$$

\] \& | 84 (3.4) |
| :--- |
| 41 (5.0) |
| 100 (0.0) |
| 53 (4.5) | \& r

$r$ \& $$
\begin{gathered}
72(4.4) \\
43(5.0) \\
86(2.9) \\
-- \\
74(4.1)
\end{gathered}
$$ <br>

\hline | Tunisia |
| :--- |
| Turkey United States | \& \[

$$
\begin{array}{r}
14(3.2) \\
90(2.6) \\
r \quad 83(2.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
78 & (3.3) \\
99 & (0.6) \\
82 & (2.5)
\end{array}
$$

\] \& | 86 (2.9) |
| :--- |
| 97 (1.3) |
| 89 (2.0) | \& \[

$$
\begin{array}{rr}
r & 8(2.6) \\
& 97(1.3) \\
r & 80(2.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
30(4.0) \\
86(3.0) \\
r \quad 62(2.9)
\end{array}
$$

\] \& \& | 50 (4.4) |
| :--- |
| 37 (3.5) |
| 61 (2.7) | <br>

\hline International Avg. \& 85 (0.4) \& 84 (0.5) \& 95 (0.3) \& 72 (0.6) \& 63 (0.6) \& \& 57 (0.7) <br>
\hline
\end{tabular}

Background data provided by teachers.

* Taught before or during this school year.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

A dash ( - ) indicates data are not available.
An " r " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students. An " "x" indicates teacher response data available for $<50 \%$ of students.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

|  | Number patterns and simple relations | Simple algebraic expressions | Representing situations algebraically; formulas | Solving simple equations | Solving simple inequalities |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Australia Belgium (Flemish) Bulgaria Canada Chile |  $100(0.0)$ <br> $r$ $86(2.9)$ <br> $r$ $98(1.1)$ <br> $r$ $98(1.0)$ <br>  $66(3.7)$ |  | $96(1.6)$ $84(3.1)$ $98(1.3)$ $r \quad 92(2.1)$ $56(3.9)$ | $\begin{array}{r} 94(1.8) \\ \\ \\ 85(2.8) \\ \\ r \quad 100(0.5) \\ r \\ \\ 94(2.3) \\ 84(2.6) \end{array}$ |  |
| Chinese Taipei Cyprus Czech Republic England Finland |  $92(2.5)$ <br>  $92(3.3)$ <br> $r$ $84(1.2)$ <br> $r$ $99(0.6)$ <br> $s$ $98(0.6)$ <br>  $49(4.8)$ | $\begin{array}{rr}  & 99(0.8) \\ r & 89(3.9) \\ & 100(0.0) \\ \text { s } & 96(1.1) \\ & 73(3.9) \end{array}$ | $\begin{array}{rr}  & 99(0.8) \\ r & 100(0.0) \\ & 97(1.9) \\ \text { s } & 89(1.8) \\ & 47(4.3) \end{array}$ | $\begin{array}{lr}  & 98(1.2) \\ \text { s } & 100(0.0) \\ & 96(2.0) \\ \text { s } & 93(1.5) \\ & 52(4.3) \end{array}$ | $\begin{array}{rr}  & 43(4.2) \\ r & 100(0.0) \\ & 32(5.2) \\ \text { s } & 39(3.7) \\ & 4(1.6) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $87(3.0)$ <br> $94(2.1)$ <br> $61(4.2)$ <br> $99(0.7)$ <br>  <br>  <br>  <br>  | $\begin{array}{r} 100(0.0) \\ 100(0.3) \\ 92(2.6) \\ 100(0.0) \\ 97(1.2) \end{array}$ | $\begin{array}{r} 100(0.0) \\ 98(1.3) \\ 91(2.5) \\ 96(1.7) \\ 88(3.0) \end{array}$ | $\begin{array}{r} 100(0.0) \\ 100(0.0) \\ 97(1.8) \\ 100(0.0) \\ 99(0.9) \end{array}$ | $\begin{array}{ll} 27 & (4.0) \\ 99 & (0.8) \\ 96 & (2.0) \\ 24 & (3.8) \\ 92 & (1.8) \end{array}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 98 & (1.2) \\ 94 & (2.4) \\ 35 & (4.1) \\ 95 & (1.3) \\ 92 & (2.6) \end{array}$ | $\begin{array}{r} 100(0.4) \\ 100(0.0) \\ 99(0.9) \\ 99(0.7) \\ 100(0.0) \end{array}$ | $\begin{array}{r} 95(1.7) \\ 98(1.2) \\ 96(1.7) \\ 96(1.6) \\ 100(0.0) \end{array}$ | $\begin{array}{r} 95(1.7) \\ 100(0.0) \\ 100(0.0) \\ 99(0.7) \\ 100(0.0) \end{array}$ | $\begin{array}{ll} 27 & (2.9) \\ 99 & (0.7) \\ 60 & (4.2) \\ 99 & (1.0) \\ 96 & (1.8) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of Malaysia <br> Moldova <br> Morocco | 81 (3.7) <br> 98 (1.2) <br> - - <br> - - | $\begin{gathered} -- \\ 94(2.5) \\ 99(0.9) \\ -- \\ -- \end{gathered}$ | 97 (1.5) <br> 98 (1.1) <br> $--$ <br> - - | $\begin{array}{cc}  & -- \\ & \\ & 99(0.7) \\ 99(1.0) \\ & -- \\ & -- \end{array}$ | 97 (1.5) <br> 72 (3.4) <br> - - |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{r} 87(4.9) \\ 99(0.8) \\ 70(3.6) \\ 100(0.0) \end{array}$ | $\begin{array}{rr}  & 86(4.9) \\ 97(1.2) \\ 78(3.3) \\ 100(0.0) \\ & -- \end{array}$ | 81 (6.0) <br> 91 (2.5) <br> 66 (4.0) <br> 99 (1.0) <br> $--$ | $\begin{gathered} 76(5.3) \\ 90(2.5) \\ 69(4.2) \\ 100(0.0) \\ -- \end{gathered}$ | $\begin{gathered} 39(6.4) \\ 38(4.3) \\ 45(4.3) \\ 99(0.9) \\ -- \end{gathered}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{gathered} 98(1.4) \\ 99(0.9) \\ 98(1.1) \\ -- \\ 75(4.1) \end{gathered}$ | $\begin{gathered} 100(0.0) \\ 100(0.1) \\ 100(0.0) \\ -- \\ 75(4.3) \end{gathered}$ | 100 (0.0) <br> 97 (1.5) <br> 99 (0.6) <br> 74 (4.2) | $\begin{gathered} 100(0.0) \\ 100(0.0) \\ 100(0.0) \\ -- \\ 99(0.5) \end{gathered}$ | $\begin{gathered} 93(2.3) \\ 93(2.5) \\ 92(2.5) \\ -- \\ 97(1.3) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 71 & (4.0) \\ 91 & (2.0) \\ 97 & (1.1) \end{array}$ | $\begin{array}{ll} 85 & (3.3) \\ 93 & (2.2) \\ 98 & (0.9) \end{array}$ | $61(4.7)$ $94(2.0)$ $96(1.1)$ | $\begin{aligned} & 72(4.0) \\ & 99(1.0) \\ & 98(0.6) \end{aligned}$ | $\begin{array}{ll} 21 & (3.7) \\ 99 & (0.7) \\ 83 & (2.3) \end{array}$ |
| International Avg. | 88 (0.5) | 94 (0.4) | 90 (0.4) | 94 (0.3) | 66 (0.5) |

Background data provided by teachers.

* Taught before or during this school year.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^35]
## Can Meaningful Comparisons Be Made Between the Intended and Implemented Curriculum?

The timss 1999 results indicate some discrepancies in a number of countries between the intended curriculum in mathematics and the implemented curriculum as reported by teachers. There are many cases of topics intended to be taught to all, or almost all, students in a country for which teachers reported lower coverage. For example, curricular goals and aims in 25 countries included "visualization of three-dimensional shapes" for all or almost all students, but teachers in only eight countries reported that at least 75 percent of the students had been taught this topic. Interestingly, there are also cases for which teachers reported greater topic coverage than would be expected from the intended curriculum. Substantial percentages of students in several countries had been taught "simple probabilities" even when this topic was not included in the official curriculum. Such discrepancies are consistent with previous IEA studies. ${ }^{2}$ However, considering the broad nature of the topics, care should be taken in interpreting the results. Further analysis will need to be done within each country to strengthen the match between the intended and implemented curricula.

[^36]
## CHAPTER 6

## Teachers and Instruction

To provide information about mathematics teachers and instruction, Chapter 6 presents teachers' reports on their background and training and their instructional practices. Information also is presented about the materials used in instruction, the activities students do in class, the use of calculators and computers in mathematics lessons, the role of homework, and the reliance on different types of assessment approaches.


Teachers and the instructional approaches they use ultimately determine the mathematics students learn. Teachers structure the content and pace of lessons, introducing new material, selecting various instructional activities, and monitoring students' developing understanding of the mathematics concepts being studied. Teachers may help students use technology and tools to investigate mathematical ideas, analyze students' work for misconceptions, and promote positive attitudes toward mathematics. They may also assign homework and conduct informal as well as formal assessments to evaluate achievement outcomes.

To collect information about mathematics instruction, tIMss administered a two-part questionnaire in which teachers were asked to provide information about their background and training and their instructional practices. Information was also collected about the materials used in instruction, the activities students do in class, the use of calculators and computers in mathematics lessons, the role of homework, and the reliance on different types of assessment approaches. Chapter 6 presents teachers' responses to some of these questions.

Because the sampling for the teacher questionnaires was based on participating students, teachers' responses do not necessarily represent all eighth-grade mathematics teachers in each country. Rather, they represent teachers of the representative samples of students assessed. It is important to note that when information from the teacher questionnaire is being reported, the student is always the unit of analysis. That is, the data shown are the percentages of students whose teachers reported on various characteristics or instructional strategies. Using the student as the unit of analysis makes it possible to describe the instruction received by representative samples of students. Although this perspective may differ from that obtained by simply collecting information from teachers, it is consistent with the timss goals of providing information about the educational contexts and performance of students.

The teachers who completed the questionnaires were the mathematics teachers of the students who took the timss 1999 test. The general sampling procedure was to sample a mathematics class from each participating school, administer the test to those students, and ask their teacher to complete the questionnaire. Thus, the information about instruction is tied directly to the students tested. Sometimes, however, teachers did not complete the questionnaire assigned to them, so most
countries had some percentage of students for whom no teacher questionnaire information is available. The exhibits in this chapter have special notations on this point. For a country where teacher responses are available for 70 to 84 percent of the students, an " $r$ " is included next to its data. Where teacher responses are available for 50 to 69 percent of students, an "s" is included. Where teacher responses are available for less than $5^{\circ}$ percent, an "x" replaces the data.

## What Preparation Do Teachers Have for Teaching Mathematics?

This section presents information about background characteristics of mathematics teachers, including age and gender, major area of study, and certification. Teachers' confidence in teaching various mathematics topics is also discussed.

As shown in Exhibit 6.1, the majority of the eighth-grade students were taught mathematics by teachers in their $30 s$ and 40 . If there was a steady replenishing of the teaching force, one might expect approximately equivalent percentages of students taught by teachers in their 20s, 3os, 4 os, and 5 os. Very few countries, however, had a comparatively younger teaching force. Internationally on average, only 16 percent of students were taught by teachers younger than age 30 . The three countries with the most students (about one-third) taught by younger teachers were Hong Kong, Iran, and Singapore. Although 21 percent of the students internationally were taught by teachers age $5^{\circ}$ or older, the teaching force was relatively older in a number of countries. About one-third or more of the students (from 32 to 47 percent) in Chile, the Czech Republic, Finland, Italy, Macedonia, Moldova, Romania, and the Slovak Republic had teachers at least 50 years of age.

Internationally on average, 6o percent of eighth-grade students were taught mathematics by females and 40 percent by males, and similar percentages were found in a number of countries. However, at least 75 percent of students had female teachers in Bulgaria, Hungary, Israel, Italy, Latvia (Lss), Lithuania, Moldova, the Philippines, the Russian Federation, Singapore, the Slovak Republic, and Slovenia. By contrast, in no country were as many as three-fourths of the students taught mathematics by male teachers. The three countries with the most students taught by male teachers were Iran (7o percent), Japan (73 percent), and the Netherlands ( 72 percent).

Exhibit 6.2 presents teachers' reports about their major areas of study and certification. Teachers' undergraduate and graduate studies provide some indication of their preparation to teach mathematics. On average internationally, 84 percent of students were taught by teachers having mathematics and/or mathematics education as a major area of study. Teachers can have dual majors, or different majors at the undergraduate and graduate level. Exhibit R3. 1 in the reference section provides detail for each of the following major areas of study: mathematics,
 mathematics education, science or science education, education (other than mathematics or science education), and other, which includes majors in any other areas.

|  | Percentage of Students by Age of Teachers |  |  |  | Percentage of Students by Gender of Teachers |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 29 Years or Under | 30-39 Years | 40-49 Years | 50 Years or Older | Female | Male |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 23(4.0) \\ 20(2.7) \\ 8(2.4) \\ 17(2.4) \\ 3(1.1) \end{array}$ | $\begin{array}{ll} 25 & (3.3) \\ 15 & (2.4) \\ 33 & (5.7) \\ 33 & (2.7) \\ 17 & (2.7) \end{array}$ | 36 (4.1) <br> 38 (3.0) <br> 38 (4.8) <br> 25 (3.1) <br> 47 (3.6) | $\begin{array}{ll} 16 & (3.0) \\ 27 & (3.1) \\ 21 & (4.1) \\ 26 & (3.0) \\ 33 & (3.5) \end{array}$ | 42 (4.3) <br> 66 (4.8) <br> 87 (2.8) <br> 53 (3.0) <br> 45 (3.9) | 58 (4.3) <br> 34 (4.8) <br> 13 (2.8) <br> 47 (3.0) <br> 55 (3.9) |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{rr}  & 10(2.6) \\ & 3(1.0) \\ & 7(2.5) \\ 5 & 20(2.9) \\ & 10(2.8) \end{array}$ | 34 (4.0) <br> 42 (4.1) <br> 29 (4.8) <br> 23 (3.5) <br> 15 (2.8) | 30 (4.0) <br> 33 (3.5) <br> 22 (5.0) <br> 35 (3.6) <br> 30 (3.6) | $\begin{aligned} & 26(3.4) \\ & 23(3.4) \\ & 43(5.6) \\ & 22(2.7) \\ & 45(4.4) \end{aligned}$ | $51(4.1)$ $67(4.4)$ $73(4.0)$ $48(3.8)$ $59(4.4)$ | 49 (4.1) <br> 33 (4.4) <br> 27 (4.0) <br> 52 (3.8) <br> 41 (4.4) |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | $\begin{array}{r} 32(4.2) \\ 8(2.3) \\ 23(3.8) \\ 36(4.8) \\ 21(3.0) \end{array}$ | $\begin{array}{ll} 38 & (4.5) \\ 20 & (3.2) \\ 50 & (3.9) \\ 23 & (3.1) \\ 26 & (3.2) \end{array}$ | $\begin{array}{ll} 19 & (3.3) \\ 46 & (4.1) \\ 20 & (3.3) \\ 39 & (4.8) \\ 36 & (3.4) \end{array}$ | $\begin{array}{r} 11(2.6) \\ 26(3.2) \\ 8(2.6) \\ 2(1.2) \\ 17(2.5) \end{array}$ | $\begin{array}{ll} 44 & (4.1) \\ 80 & (3.2) \\ 44 & (4.7) \\ 30 & (3.8) \\ 78 & (3.1) \end{array}$ | $\begin{array}{ll} 56 & (4.1) \\ 20 & (3.2) \\ 56 & (4.7) \\ 70 & (3.8) \\ 22 & (3.1) \end{array}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 0(0.0) \\ 21(3.3) \\ 27(3.7) \\ 19(3.0) \\ 14(3.2) \end{array}$ | $\begin{array}{r} 8(2.0) \\ 39(4.3) \\ 45(4.6) \\ 53(3.7) \\ 33 \end{array}$ | 58 (4.1) <br> 33 (3.7) <br> 24 (3.2) <br> 15 (2.5) <br> 28 (4.4) | $\begin{array}{r} 34(3.8) \\ 7(2.1) \\ 4(1.5) \\ 13(2.8) \\ 25(4.2) \end{array}$ | 76 (3.1) <br> 27 (3.6) <br> 48 (4.5) <br> 59 (3.4) <br> 91 (2.6) | $\begin{array}{r} 24(3.1) \\ 73(3.6) \\ 52(4.5) \\ 41(3.4) \\ 9(2.6) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ Macedonia, Rep. of Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 5(1.7) \\ 1(0.9) \\ 28(3.6) \\ 4(1.7) \\ 4(1.3) \end{array}$ | $\begin{aligned} & 34(4.1) \\ & 29(3.6) \\ & 39(4.4) \\ & 24(4.0) \\ & 34(3.2) \end{aligned}$ | $\begin{aligned} & 32(3.9) \\ & 23(3.6) \\ & 27(3.6) \\ & 39(4.0) \\ & 58(3.2) \end{aligned}$ | $\begin{array}{r} 29(4.0) \\ 47(3.5) \\ 6(1.8) \\ 33(4.3) \\ 4(1.0) \end{array}$ | $\begin{array}{ll} 90 & (2.5) \\ 50 & (4.6) \\ 68 & (3.6) \\ 76 & (3.6) \\ 39 & (3.1) \end{array}$ | $\begin{array}{ll} 10 & (2.5) \\ 50 & (4.6) \\ 32 & (3.6) \\ 24 & (3.6) \\ 61 & (3.1) \end{array}$ |
| Netherlands <br> New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 15(4.3) \\ 16(3.3) \\ 25(3.6) \\ 8(2.1) \\ 8(2.0) \end{array}$ | $\begin{aligned} & 17(3.9) \\ & 19(3.4) \\ & 37(4.1) \\ & 19(3.6) \\ & 32(3.7) \end{aligned}$ | 41 (5.4) <br> 35 (4.2) <br> 23 (3.2) <br> 30 (4.2) <br> 29 (2.9) | $\begin{aligned} & 26(5.3) \\ & 30(4.2) \\ & 15(2.7) \\ & 42(4.2) \\ & 31 \end{aligned}(4.0)$ | $\begin{array}{ll} 28 & (5.0) \\ 44 & (4.0) \\ 75 & (3.9) \\ 63 & (4.1) \\ 93 & (2.6) \end{array}$ | $\begin{array}{r} 72(5.0) \\ 56(4.0) \\ 25(3.9) \\ 37(4.1) \\ 7(2.6) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 37(4.4) \\ 9(2.4) \\ 6(1.6) \\ 29(3.4) \\ 23(3.2) \end{array}$ | $\begin{array}{ll} 25 & (4.0) \\ 21 & (3.9) \\ 43 & (4.3) \\ 55 & (4.1) \\ 28 & (3.6) \end{array}$ | 15 (3.2) <br> 38 (4.8) <br> 39 (4.2) <br> 13 (3.2) <br> 43 (3.7) | $\begin{array}{r} 23(3.6) \\ 32(4.3) \\ 12(2.7) \\ 3(1.3) \\ 6(2.1) \end{array}$ | $\begin{array}{ll} 75 & (4.1) \\ 86 & (3.3) \\ 89 & (2.8) \\ 39 & (4.9) \\ 69 & (3.7) \end{array}$ | $\begin{array}{ll} 25 & (4.1) \\ 14 & (3.3) \\ 11 & (2.8) \\ 61 & (4.9) \\ 31 & (3.7) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 21 & (3.0) \\ 23 & (3.4) \\ 11 & (2.0) \end{array}$ | $\begin{aligned} & 35(3.9) \\ & 15 \\ & 25 \\ & 25 \end{aligned}$ | $\begin{array}{ll} 40 & (4.2) \\ 56 & (3.9) \\ 37 & (3.9) \end{array}$ | $\begin{array}{r} 4(1.7) \\ 5(2.3) \\ 27(2.9) \end{array}$ | $\begin{array}{ll} 39 & (4.3) \\ 41 & (3.9) \\ 60 & (3.0) \end{array}$ | $\begin{array}{ll} 61 & (4.3) \\ 59 & (3.9) \\ 40 & (3.0) \end{array}$ |
| International Avg. | 16 (0.5) | 30 (0.6) | 33 (0.6) | 21 (0.5) | 60 (0.6) | 40 (0.6) |

[^37][^38]

[^39]$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

Eighty-five percent of students, on average internationally, were taught mathematics by teachers having a teaching certificate in any subject. In TIMSS 1995, detailed information collected about certification indicated a wide range of criteria across countries. ${ }^{1}$ For example, the number of years of post-secondary education required for a teaching qualification ranged from two years in Iran to as many as six years in Canada; many countries reported four years. Almost all countries reported that teaching practice was required, and a large number reported that an evaluation or examination was required for certification. In some countries, such as the United States, the types of certification varied according to the policies of different states. Despite difficulties in interpretation illustrated by the 1995 data, however, it is interesting to note that in timss 1999 the percentages of students taught by teachers reporting that they had a certificate ranged from 32 percent in Cyprus to 100 percent in Australia, Hungary, Japan, and Singapore. There was even more variation among countries when both certification and having had mathematics as a major were considered. The percentage of students taught by teachers both certified and having had mathematics or mathematics education as a major ranged from 25 percent in Canada to 99 percent in Hungary and Macedonia, with an international average of 73 percent.

To gauge teachers' confidence to teach mathematics topics, timss constructed an index of teachers' confidence in their preparation to teach mathematics (CPTM), presented in Exhibit 6.3. Teachers were asked how well prepared they felt to teach each of 12 mathematics topics (e.g., properties of geometric figures, solving linear equations and inequalities). Responses were given on a three-point scale; very well prepared was assigned a value of three, somewhat prepared two, and not well prepared one. Students were assigned to the high level of the index if their teachers reported that they felt very well prepared, on average across the 12 topics ( 2.75 or higher). The medium level indicates that teachers reported being somewhat to well prepared (averages from 2.25 to 2.75 ), and the low level that they reported being only somewhat prepared or less (averages less than 2.25).

The results show that average mathematics achievement is related to how well teachers felt they were prepared to teach mathematics, with higher achievement related to higher levels of teachers' confidence in their preparation. On average internationally, teachers reported relatively high degrees of confidence, with 63 percent of students taught by teachers who believed they were very well prepared. Countries where 85 percent or more of the students were taught by teachers who believed they were very well prepared were Macedonia, the United States, the Slovak Republic,

[^40]Cyprus, Jordan, New Zealand, and the Czech Republic. Interestingly, countries with substantial percentages of students whose teachers reported a low level of confidence included both high- and low-performing countries. One-third or more of the students in Chile, Hungary, Japan, Slovenia, Thailand, and Tunisia were taught by teachers feeling only somewhat prepared or less.

The detail for the 12 topics included in the index is provided in Exhibit R3.2 in the reference section. On average across countries, the topics having the most students (from 79 to 82 percent) taught by teachers who felt very well prepared were fractions, decimals, and percentages; ratios and proportions; perimeter, area, and volume; evaluate and perform operations on algebraic expressions; and solving linear equations and inequalities. Teachers reported being least well prepared to teach understanding and calculations related to simple probabilities; just more than half the students internationally ( 55 percent on average) were taught by teachers who felt very well prepared to teach this topic. Exhibit R3.3 shows principals' opinions about the degree to which shortages of qualified mathematics teachers affect the capacity to provide instruction. On average internationally, principals reported that such shortages affect the quality of instruction some or a lot for one-third of the students. Bulgaria, Jordan, Moldova, Tunisia, and Turkey reported shortages affecting capacity to provide instruction a lot for more than half their students.

Teachers' beliefs about mathematics learning and instruction are to some degree related to their preparation. Exhibits R3.4 and R3.5 in the reference section show the percentages of eighth-grade students whose mathematics teachers reported certain beliefs about mathematics, the way mathematics should be taught, and the importance of various cognitive skills in achieving success in the discipline. In general, there was substantial agreement about the inherent nature of mathematical abilities. For example, in most countries 8o percent or more of students had teachers who agreed that some students have a natural talent for mathematics. There was also nearly complete agreement that more than one representation should be used in teaching a mathematics topic. The greatest variation in views pertained to the importance of being able to remember formulas and procedures; only about 10 percent of students in Slovenia were taught by teachers who believed this ability was very important for students' success in mathematics, while about 90 percent of students in the Philippines had teachers who believed that to be the case.

## Index of Teachers' Confidence in Preparation to Teach Mathematics

Index based on teachers' responses to 12 questions about how prepared they feel to teach different mathematics topics (see reference exhibit R3.2) based on a 3-point scale: $1=$ not well prepared; 2 = somewhat prepared; 3 = very well prepared. Average is computed across the 12 items for items for which the teacher did not respond do not teach. High level indicates average is greater than or equal to 2.75. Medium level indicates average is greater than or equal to 2.25 and less than 2.75. Low level indicates average is less than 2.25.

| Macedonia, Rep. of United States | High CPTM |  | Medium CPTM |  | Low <br> CPTM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | 92 (2.2) | 447 (4.7) | 8 (2.1) | 435 (16.2) | 1 (0.6) | ~ ~ |
|  | 87 (2.4) | 505 (4.2) | 11 (2.3) | 489 (7.0) | 2 (1.0) | ~ ~ |
| Slovak Republic | 87 (3.2) | 532 (3.8) | 11 (3.1) | 531 (14.1) | 2 (1.3) | ~ |
| Cyprus | 87 (2.7) | 478 (1.8) | 13 (2.7) | 468 (6.6) | 0 (0.0) | ~ |
| Jordan | 86 (3.0) | 429 (3.8) | 11 (2.7) | 418 (11.0) | 3 (1.3) | 400 (15.9) |
| New Zealand | 85 (3.0) | 496 (5.4) | 10 (2.5) | 460 (15.7) | 5 (1.7) | 459 (19.2) |
| Czech Republic | 85 (3.6) | 521 (5.1) | 14 (3.8) | 519 (9.5) | 1 (1.3) | ~ ~ |
| Netherlands | 81 (6.2) | 542 (7.1) | 10 (3.0) | 514 (22.4) | $9(5.8)$ | 514 (58.7) |
| Romania | 79 (3.5) | 478 (6.6) | 20 (3.5) | 453 (8.8) | 1 (0.0) | ~ |
| Australia | 77 (4.1) | 529 (5.7) | 16 (3.4) | 521 (9.8) | 6 (2.3) | 502 (23.9) |
| Finland | 76 (3.0) | 522 (3.2) | 15 (3.0) | 523 (7.0) | 10 (1.9) | 507 (7.8) |
| Malaysia | 75 (3.9) | 525 (5.1) | 20 (3.3) | 511 (10.3) | 5 (2.3) | 462 (28.2) |
| Israel | 75 (2.8) | 472 (5.5) | 21 (2.4) | 464 (7.7) | 5 (1.8) | 448 (15.0) |
| Turkey | 75 (3.1) | 434 (5.5) | 21 (2.9) | 412 (7.6) | 4 (1.4) | 406 (9.1) |
| Iran, Islamic Rep. | 72 (3.6) | 425 (4.2) | 25 (3.5) | 420 (6.8) | 3 (1.4) | 388 (8.8) |
| Chinese Taipei | 71 (3.6) | 586 (4.5) | 15 (3.1) | 587 (10.9) | 14 (2.7) | 572 (6.8) |
| Canada | 71 (2.7) | 537 (3.3) | 21 (3.0) | 530 (6.6) | 8 (1.8) | 515 (14.6) |
| Indonesia | 69 (4.7) | 411 (5.9) | 27 (4.5) | 377 (8.8) | 4 (1.7) | 447 (21.5) |
| Singapore | 66 (4.2) | 603 (7.1) | 24 (3.7) | 619 (12.0) | 10 (2.8) | 578 (20.8) |
| Belgium (Flemish) | 65 (3.2) | 559 (5.8) | 32 (3.1) | 561 (5.6) | 3 (1.4) | 558 (27.1) |
| Latvia (LSS) | 64 (4.3) | 508 (4.8) | 28 (4.4) | 504 (6.8) | 8 (2.3) | 489 (11.1) |
| Hong Kong, SAR | 61 (4.3) | 579 (5.5) | 28 (3.9) | 591 (8.2) | 11 (2.7) | 571 (12.0) |
| Italy | 60 (3.9) | 479 (5.5) | 27 (3.5) | 481 (7.2) | 13 (2.3) | 479 (12.4) |
| Morocco | 57 (2.9) | 336 (3.7) | 37 (2.8) | 338 (4.4) | 7 (1.3) | 340 (8.7) |
| Bulgaria | 54 (5.4) | 517 (9.7) | 29 (4.6) | 515 (9.4) | 17 (5.8) | 488 (10.0) |
| Hungary | 54 (4.1) | 531 (5.2) | 12 (2.8) | 526 (12.1) | 34 (3.7) | 533 (6.6) |
| South Africa | 54 (4.0) | 290 (10.5) | 33 (3.6) | 256 (9.2) | 14 (2.7) | 266 (14.2) |
| Moldova | 52 (4.5) | 465 (5.1) | 27 (3.8) | 473 (8.1) | 21 (3.6) | 471 (11.4) |
| Korea, Rep. of | 48 (3.9) | 585 (3.2) | 31 (3.8) | 590 (4.1) | 21 (3.0) | 588 (3.5) |
| Philippines | 41 (3.8) | 355 (8.8) | 44 (3.9) | 341 (8.7) | 14 (2.9) | 326 (13.1) |
| Slovenia | 34 (3.5) | 530 (4.3) | 32 (3.7) | 530 (4.9) | 34 (4.0) | 530 (5.0) |
| Tunisia | 25 (3.7) | 447 (4.7) | 42 (4.1) | 447 (3.5) | 34 (3.7) | 449 (4.8) |
| Chile | 24 (3.2) | 405 (9.1) | 31 (3.2) | 385 (5.5) | 45 (3.7) | 391 (7.5) |
| Thailand | 18 (3.5) | 487 (15.6) | 26 (3.8) | 468 (10.6) | 55 (4.4) | 461 (6.1) |
| Japan | 8 (2.1) | 584 (6.1) | 24 (3.6) | 589 (4.2) | 68 (4.0) | 573 (2.6) |
| England | -- | -- | -- | -- | -- | -- |
| Lithuania * | -- | -- | -- | -- | -- | -- |
| Russian Federation | -- | -- | -- | -- | -- | -- |
| International Avg. | 63 (0.6) | 489 (1.1) | 23 (0.6) | 481 (1.7) | 14 (0.5) | 473 (2.9) |

[^41]

## How Much School Time Is Devoted to Mathematics Instruction?

Exhibit 6.4 presents information about the amount of mathematics instruction given to eighth-grade students in the timss 1999 countries. Since different systems have school years of different lengths (see reference Exhibit R3.6) and different arrangements of weekly and daily instruction, the comparisons are given in terms of the average number of hours of mathematics instruction over the school year as reported by mathematics teachers. Countries providing 150 or more hours per year were Indonesia, Morocco, Thailand, Chile, and Canada. Countries providing fewer than 100 hours were Bulgaria, Turkey, the Netherlands, Finland, Macedonia, and Cyprus. The percentage of instructional time at the eighth grade that was devoted to mathematics ranged from 17 percent in Indonesia and the Russian Federation to nine percent in Chinese Taipei, Cyprus, and the Netherlands (see Exhibit R3.7 for details on the total instructional time in each country). For most countries, the percentages of time devoted to mathematics reported by teachers correspond with the percentages targeted in the intended curriculum (see Exhibit $5 \cdot 5$ ).

As shown in Exhibit 6.5, teachers of about half the students, on average internationally, reported that mathematics classes meet for at least two hours per week but fewer than three and a half. For another one-third of students, classes meet for at least three and a half hours but fewer than five. At least three and a half hours per week of mathematics instruction was reported for more than 50 percent of the students in Canada, Chile, the Czech Republic, Hong Kong, Indonesia, Israel, Italy, Latvia (Lss), Moldova, Morocco, New Zealand, the Russian Federation, the Slovak Republic, South Africa, Tunisia, and the United States. The data reveal no clear pattern between the number of in-class instructional hours and mathematics achievement either across or within countries. Common sense and research both support the idea that time on task is an important contributor to achievement, yet this time can be spent more or less efficiently. Time alone is not enough; it needs to be spent on high-quality mathematics instruction. Devoting extensive class time to remedial activities can deprive students of this. Also, instructional time can be spent out of school in various tutoring programs; low-performing students may be receiving additional instruction.

Exhibit 6.6 shows trends between 1995 and 1999 in the number of hours mathematics is taught weekly. On average internationally, the students receiving at least two hours of mathematics instruction per week but fewer than three and a half increased significantly by five percentage points, and those receiving three and a half to fewer than five hours decreased by seven percentage points. There was little change internationally in the percentage of students receiving five hours or more. The Czech Republic and the Slovak Republic showed a decrease in the weekly hours of mathematics instruction. Belgium (Flemish) and Singapore showed a significant increase in the percentage of students receiving five hours or more of instruction per week.

Videotapes of mathematics classes in the United States and Japan in TImSS 1995 revealed that outside interruptions can affect the flow of the lesson and detract from instructional time. ${ }^{2}$ As shown in Exhibit 6.7, on average internationally about one-fifth of the students ( 21 percent) tested in timss 1999 were in mathematics classes that were interrupted pretty often or almost always. In comparison, 28 percent were in classes that were never interrupted; in Japan, Korea, and Tunisia, more than half the students were in such classes.

Across countries, students' mathematics teachers spent only about 60 percent of their formally scheduled school time teaching mathematics (see Exhibit R3. 8 in the reference section). Of the remaining time, about 10 percent was spent teaching subjects other than mathematics,
$\Gamma^{6}$
 about 10 percent on curriculum planning, and about 20 percent on a various administrative and other duties.

[^42]

[^43][^44]
$\square$


|  | 5 Hours or More |  | 3.5 Hours to < 5 |  | 2 Hours to < 3.5 |  | Less Than 2 Hours |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 3(1.7) \\ 4(1.0) \\ 4(3.0) \\ 17(2.2) \\ 13(2.4) \end{array}$ | $\begin{aligned} & 530(46.0) \\ & 590 \text { (11.7) } \\ & 606 \text { (29.5) } \\ & 520 \text { (6.4) } \\ & 394 \text { (13.7) } \end{aligned}$ | $\begin{array}{r} 44(4.4) \\ 40(2.8) \\ 8(2.3) \\ 55(3.2) \\ 83 \end{array}$ | $\begin{aligned} & 534(7.7) \\ & 595(4.1) \\ & 525(27.0) \\ & 544(3.9) \\ & 391(5.0) \end{aligned}$ | $\begin{array}{r} 50(4.6) \\ 43(3.8) \\ 73(4.6) \\ 26(2.7) \\ 3(1.3) \end{array}$ | $\begin{aligned} & 517(6.7) \\ & 544(7.7) \\ & 498(5.0) \\ & 523(6.1) \\ & 414(12.7) \end{aligned}$ | $\begin{array}{r} 3(1.4) \\ 13(3.4) \\ 14(3.3) \\ 3(0.9) \\ 1(0.7) \end{array}$ | $\begin{gathered} 565(30.5) \\ 502(18.9) \\ 543(9.0) \\ 503(6.3) \\ \sim \sim \end{gathered}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 1 & (1.1) \\ 0 & (0.0) \\ 4 & (2.1) \\ 2 & (1.2) \\ 1 & (0.9) \end{array}$ | $600 \text { (28.1) }$ | $\begin{array}{r} 48(4.4) \\ 0(0.0) \\ 52(4.4) \\ 3(1.4) \\ 7(2.4) \end{array}$ | $\begin{gathered} 592(5.8) \\ \sim \sim \\ \sim 17(5.3) \\ 481(10.2) \\ 535(14.0) \end{gathered}$ | $\begin{array}{r} 51(4.5) \\ 100(0.0) \\ 44(4.4) \\ 95(2.0) \\ 87(2.9) \end{array}$ | 577 (5.5) 476 (1.8) 517 (6.4) 512 (5.3) 520 (2.9) | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.2) \\ 4 & (1.5) \end{array}$ | $518 \text { (12.2) }$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 9(2.3) \\ 3(1.1) \\ 21(3.7) \\ 12(2.6) \\ 4(1.5) \end{array}$ | $\begin{array}{ll} 579 & (15.2) \\ 583 & \text { (34.4) } \\ 384 \text { (9.4) } \\ 419 & (11.4) \\ 470 & (28.7) \end{array}$ | $\begin{array}{ll} 71(4.0) \\ 15 & (2.7) \\ 76 & (3.8) \\ 14(2.9) \\ 65 & (4.1) \end{array}$ | $\begin{aligned} & 583 \text { (5.6) } \\ & 522 \text { (12.6) } \\ & 408 \text { (6.1) } \\ & 413(8.9) \\ & 464(5.8) \end{aligned}$ | $\begin{array}{r} 17(3.1) \\ 80(2.9) \\ 1(0.2) \\ 50(4.8) \\ 29(3.9) \end{array}$ | $\begin{gathered} 587(11.1) \\ 531(3.9) \\ \sim \sim \\ 423(4.9) \\ 481(8.5) \end{gathered}$ | $\begin{array}{r} 3(1.5) \\ 1(0.8) \\ 3(1.2) \\ 24(4.0) \\ 2(1.2) \end{array}$ | $\begin{gathered} 553(16.7) \\ \sim \sim \\ 409(27.4) \\ 429(5.7) \\ \sim \sim \end{gathered}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 9 & (2.1) \\ 1 & (1.3) \\ 5 & (1.9) \\ 2(0.9) \\ 7 & (2.5) \end{array}$ | $\begin{gathered} 469(11.5) \\ \sim \sim \\ 463(21.0) \\ \sim \sim \\ \sim 87 \\ \sim \end{gathered}$ | $\begin{array}{r} 55(3.8) \\ 2(1.3) \\ 7(2.2) \\ 3(1.1) \\ 62(3.9) \end{array}$ | $\begin{gathered} 483(5.3) \\ \sim \\ \sim \\ 439(20.1) \\ 602(9.6) \\ 516(4.6) \end{gathered}$ | 29 (4.0) <br> 95 (2.0) <br> 88 (2.8) <br> 93 (1.8) <br> 31 (4.2) | $\begin{aligned} & 475(7.4) \\ & 577(2.1) \\ & 424(3.7) \\ & 587(2.1) \\ & 491(5.6) \end{aligned}$ | $\begin{aligned} & 6(1.8) \\ & 2(0.9) \\ & 0(0.0) \\ & 3(1.1) \\ & 0(0.0) \end{aligned}$ | $\begin{aligned} & 484(10.3) \\ & \sim \sim \\ & \sim \sim \\ & 587(11.7) \\ & \sim \sim \end{aligned}$ |
| Lithuania $\ddagger$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{aligned} & -- \\ & 0(0.0) \\ & 0(0.0) \\ & 8(2.4) \\ & 96(1.1) \end{aligned}$ | $\begin{aligned} & 481 \text { (17.9) } \\ & 337(2.9) \end{aligned}$ | $\begin{array}{r} -- \\ 2(1.0) \\ 2(1.2) \\ 80(3.3) \\ 0(0.0) \end{array}$ | $466 \text { (4.5) }$ | $\begin{array}{r} 97(1.2) \\ 93(2.1) \\ 5(1.5) \\ 3(1.0) \end{array}$ | $\quad--$ $447(4.4)$ $520(4.6)$ $485(18.0)$ $338(10.5)$ | $\begin{array}{ll} 1 & (0.6) \\ 5 & (1.8) \\ 7 & (1.9) \\ 1 & (0.6) \end{array}$ | $\begin{gathered} 533 \text { (24.0) } \\ 467 \text { (19.7) } \\ \sim \sim \end{gathered}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{r} 0(0.0) \\ 1(0.0) \\ 11(2.5) \\ 9(2.5) \\ 11(2.5) \end{array}$ | $326 \text { (15.0) }$ <br> 477 (21.8) <br> 553 (13.4) | $\begin{array}{r} 0(0.0) \\ 56(3.9) \\ 8(2.5) \\ 12(2.3) \\ 57(4.1) \end{array}$ | 494 (7.0) <br> 384 (33.0) <br> 483 (12.0) <br> 528 (7.7) | $\begin{array}{rr} 100 & (0.5) \\ 41 & (3.8) \\ 78 & (3.4) \\ 70 & (3.9) \\ 32 & (3.8) \end{array}$ | $\begin{aligned} & 537(7.2) \\ & 488(8.3) \\ & 343(7.1) \\ & 471(6.8) \\ & 513(8.5) \end{aligned}$ | $\begin{array}{r} 0(0.0) \\ 2(1.1) \\ 3(0.9) \\ 10(2.4) \\ 0(0.0) \end{array}$ | 361 (22.5) <br> 481 (15.3) |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 9(2.3) \\ 5(2.1) \\ 0(0.0) \\ 9(2.6) \\ 30(4.9) \end{array}$ | $\begin{gathered} 592(24.7) \\ 503(15.2) \\ \sim \\ \sim \\ 275(24.4) \\ 483(11.4) \end{gathered}$ | 37 (3.8) <br> 50 (4.8) <br> 26 (4.1) <br> 58 (4.2) <br> 9 (3.3) | $\begin{aligned} & 586 \text { (11.2) } \\ & 534 \text { (5.3) } \\ & 537(4.5) \\ & 277(8.8) \\ & 448(18.5) \end{aligned}$ | $\begin{array}{ll} 48 & (4.0) \\ 44 & (4.7) \\ 74 & (4.1) \\ 23 & (3.5) \\ 58 & (5.1) \end{array}$ | 623 (7.5) <br> 534 (6.1) <br> 528 (3.3) <br> 269 (13.3) <br> 461 (7.3) | $\begin{array}{r} 5(2.0) \\ 0(0.0) \\ 0(0.0) \\ 10(2.4) \\ 2(1.4) \end{array}$ | $\begin{aligned} 608 & (20.0) \\ \sim & \sim \\ \sim & \sim \\ 273 & (17.2) \\ \sim & \sim \end{aligned}$ |
| Tunisia <br> Turkey r <br> United States | $\begin{array}{r} 1(1.0) \\ 5(1.6) \\ 16(2.2) \end{array}$ | $\begin{aligned} & 418 \text { (16.3) } \\ & 490(9.2) \end{aligned}$ | $\begin{array}{r} 86(2.8) \\ 5(1.6) \\ 56(3.4) \end{array}$ | $\begin{aligned} & 448 \text { (2.8) } \\ & 415(10.5) \\ & 501(4.9) \end{aligned}$ | $\begin{aligned} & 12(2.6) \\ & 77(3.4) \\ & 17(2.6) \end{aligned}$ | $\begin{aligned} & 441(6.7) \\ & 429(5.0) \\ & 528(11.6) \end{aligned}$ | $\begin{array}{r} 1(1.0) \\ 13(2.7) \\ 11(2.3) \end{array}$ | $\begin{aligned} & 427 \text { (11.0) } \\ & 491 \text { (14.5) } \end{aligned}$ |
| International Avg. | 9 (0.3) | 481 (3.5) | 34 (0.5) | 492 (2.3) | 53 (0.5) | 490 (1.9) | 4 (0.3) | 485 (4.7) |

## Background data provided by teachers.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^45]|  | 5 Hours or More |  |  | 3.5 Hours to < 5 |  |  | 2 Hours to < 3.5 |  |  | Less Than 2 Hours |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  |
| Australia | 3 (1.7) | 2 (1.8) | $\bullet$ | 44 (4.4) | -1 (6.4) | - | 50 (4.6) | -3 (6.7) | - | 3 (1.4) | 1 (1.7) | - |
| Belgium (Flemish) | 4 (1.0) | 4 (1.0) | - | 40 (2.8) | -10 (5.3) | - | 43 (3.8) | -7 (5.8) | - | 13 (3.4) | 13 (3.4) | $\triangle$ |
| Canada | 17 (2.2) | -1 (4.2) | $\bigcirc$ | 55 (3.2) | 6 (6.1) | - | 26 (2.7) | -5 (5.2) | - | 3 (0.9) | 0 (1.5) | - |
| Cyprus | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $x \times$ | $x \times$ |  | x X | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  |
| Czech Republic | 4 (2.1) | 1 (2.6) | - | 52 (4.4) | -38 (5.2) | $\nabla$ | 44 (4.4) | 38 (4.8) | - | 0 (0.0) | -1 (0.9) | - |
| England | 2 (1.2) | 2 (1.2) | - | 3 (1.4) | -7 (3.1) | - | 95 (2.0) | 6 (3.4) | - | 0 (0.2) | -1 (0.9) |  |
| Hong Kong, SAR | 9 (2.3) | 2 (3.6) | - | 71 (4.0) | 9 (6.8) | - | 17 (3.1) | -9 (6.0) | - | 3 (1.5) | -2 (2.8) |  |
| Hungary | 3 (1.1) | 2 (1.5) | - | 15 (2.7) | -8 (4.6) | - | 80 (2.9) | 5 (4.8) | - | 1 (0.8) | 1 (0.8) |  |
| Iran, Islamic Rep. | -- | -- |  | - - | -- |  |  | -- |  |  | -- |  |
| Israel ${ }^{\dagger}$ | 4 (1.7) | -2 (4.0) | - | 63 (4.5) | 16 (9.4) | - | 30 (4.3) | -11 (9.7) | - | 3 (1.5) | -4 (4.2) |  |
| Italy | 9 (2.4) | -4 (4.5) | - | 56 (4.9) | 2 (7.1) | - | 30 (4.9) | 1 (6.6) | - | 5 (2.0) | 1 (2.7) |  |
| Japan | 1 (1.3) | 1 (1.3) | - | 2 (1.3) | -2 (2.1) | - | 95 (2.0) | 4 (3.1) | - | 2 (0.9) | -2 (2.0) |  |
| Korea, Rep. of | 2 (0.9) | -3 (2.5) | - | 3 (1.1) | -2 (2.0) | - | 93 (1.8) | 3 (3.3) | - | 3 (1.1) | 2 (1.2) | - |
| Latvia (LSS) | 7 (2.5) | -1 (3.5) | - | 62 (3.9) | 0 (5.6) | - | 31 (4.2) | 2 (5.8) | - | 0 (0.0) | -1 (0.1) | V |
| Lithuania | - - | -- |  | - - | -- |  | - - | - - |  | - - | - - |  |
| Netherlands | 0 (0.0) | - - | - | 0 (0.0) | -- | $\bullet$ | 100 (0.5) | 3 (2.0) | - | 0 (0.0) | -3 (1.9) | - |
| New Zealand | 1 (0.0) | -3 (1.5) | - | 56 (3.9) | 6 (5.7) | - | 41 (3.8) | -1 (5.6) | - | 2 (1.1) | -3 (2.1) | - |
| Romania | 9 (2.5) | 6 (3.1) | - | 12 (2.3) | 3 (3.3) | - | 70 (3.9) | -10 (5.2) | - | 10 (2.4) | 1 (3.5) | - |
| Russian Federation | 11 (2.5) | -2 (4.8) | - | 57 (4.1) | -12 (6.0) | - | 32 (3.8) | 15 (4.7) | $\triangle$ | 0 (0.0) | - - | - |
| Singapore | 9 (2.3) | 9 (2.3) | - | 37 (3.8) | -10 (6.0) | - | 48 (4.0) | -4 (6.1) | - | 5 (2.0) | 5 (2.0) | - |
| Slovak Republic | 5 (2.1) | -6 (3.6) | - | 50 (4.8) | -36 (5.7) | V | 44 (4.7) | 42 (4.9) | $\triangle$ | 0 (0.0) | -- | - |
| Slovenia | 0 (0.0) | -1 (0.8) | - | 26 (4.1) | 13 (5.3) | - | 74 (4.1) | -12 (5.3) | - | 0 (0.0) | -- | - |
| Thailand ${ }^{\dagger}$ | $\times \mathrm{x}$ | $\mathrm{x} \times$ |  | x x | x x |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  |
| United States | 16 (2.2) | 6 (3.3) | $\bullet$ | 56 (3.4) | -2 (5.8) | - | 17 (2.6) | -6 (4.6) | - | 11 (2.3) | 3 (3.2) | $\bullet$ |
| International Avg. ${ }^{\text {§ }}$ | 6 (0.4) | 1 (0.6) | - | 34 (0.7) | -7 (1.1) | V | 56 (0.8) | 5 (1.1) | $\triangle$ | 4 (0.4) | 2 (0.5) | $\triangle$ |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
- 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by teachers.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " " " indicates teacher response data available for $<50 \%$ of students, based on the lower response rate in either 1995 or 1999.

|  | Never |  | Once in a While |  | Pretty Often |  | Almost Always |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 11(0.7) \\ 24(1.1) \\ 19(0.9) \\ 9(0.4) \\ 18(0.7) \end{array}$ | $\begin{aligned} & 523(8.2) \\ & 557(5.9) \\ & 511(7.5) \\ & 528(4.2) \\ & 395(8.5) \end{aligned}$ | 66 (1.1) <br> 62 (1.1) <br> 64 (1.2) <br> 64 (1.0) <br> 49 (0.8) | 534 (5.0) 566 (2.9) 522 (5.1) 540 (2.4) 407 (4.8) | 16 (0.8) <br> 9 (0.7) <br> 10 (0.9) <br> 18 (0.7) <br> 17 (0.6) | $\begin{aligned} & 510(7.9) \\ & 562 \text { (6.8) } \\ & 506 \text { (13.9) } \\ & 517 \text { (3.9) } \\ & 384(5.5) \end{aligned}$ | $\begin{array}{r} 7(0.7) \\ 5(0.8) \\ 7(0.6) \\ 9(0.7) \\ 16(0.7) \end{array}$ | $\begin{aligned} & 485(8.3) \\ & 505(20.3) \\ & 456(10.7) \\ & 502(7.8) \\ & 362(6.6) \end{aligned}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 22 & (1.1) \\ 26 & (1.0) \\ 33 & (1.7) \\ 10 & (0.8) \\ 34 & (1.3) \end{array}$ | 580 (6.1) <br> 479 (3.9) <br> 520 (4.0) <br> 508 (9.5) <br> 526 (3.6) | 56 (1.0) 49 (1.0) 59 (1.3) 66 (1.2) 57 (1.3) | $\begin{aligned} & 594(4.4) \\ & 485(2.2) \\ & 524(4.7) \\ & 509(4.2) \\ & 523(3.2) \end{aligned}$ | $\begin{array}{r} 17(0.9) \\ 19(0.9) \\ 4(0.5) \\ 19(1.1) \\ 6(0.6) \end{array}$ | $\begin{aligned} & 580(5.4) \\ & 470(4.9) \\ & 517(11.4) \\ & 474(6.0) \\ & 502(7.1) \end{aligned}$ | $\begin{aligned} & 6(0.6) \\ & 5(0.5) \\ & 4(0.8) \\ & 6(0.6) \\ & 3(0.3) \end{aligned}$ | $\begin{aligned} & 563 \text { (9.0) } \\ & 434 \text { (8.6) } \\ & 472 \text { (13.7) } \\ & 437 \text { (8.9) } \\ & 473 \text { (10.4) } \end{aligned}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | 36 (1.0) <br> 46 (1.5) <br> 15 (1.0) <br> 33 (1.2) <br> 20 (1.0) | $\begin{aligned} & 585(4.4) \\ & 541(4.3) \\ & 386(8.2) \\ & 425(4.2) \\ & 457(7.7) \end{aligned}$ | 54 (0.8) 45 (1.3) 75 (1.1) 39 (1.0) 47 (1.3) | $\begin{aligned} & 588(4.0) \\ & 528(4.3) \\ & 413(4.6) \\ & 435(4.2) \\ & 485(3.7) \end{aligned}$ | $\begin{array}{r} 8(0.6) \\ 5(0.4) \\ 8(0.6) \\ 15(0.8) \\ 20(0.8) \end{array}$ | $\begin{aligned} & 552(8.9) \\ & 497(7.8) \\ & 378(9.6) \\ & 404(6.4) \\ & 469(5.2) \end{aligned}$ | $\begin{array}{r} 2(0.2) \\ 4(0.4) \\ 2(0.2) \\ 14(0.6) \\ 13(0.7) \end{array}$ | 515 (13.5) <br> 414 (6.2) <br> 446 (7.3) |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | 16 (1.0) <br> 53 (1.4) <br> 29 (1.0) <br> 57 (0.9) <br> 39 (1.3) | 480 (5.5) 580 (2.7) 440 (5.2) 581 (2.0) 501 (4.6) | 54 (1.2) <br> 42 (1.3) <br> 39 (0.9) <br> 38 (0.8) <br> 52 (1.3) | 488 (4.0) <br> 581 (2.5) <br> 455 (4.3) <br> 598 (3.0) <br> 513 (3.9) | $\begin{array}{r} 18(1.0) \\ 4(0.3) \\ 19(0.7) \\ 4(0.2) \\ 5(0.5) \end{array}$ | 477 (5.3) <br> 559 (5.9) <br> 414 (4.8) <br> 579 (7.5) <br> 491 (8.6) | $\begin{array}{r} 11(0.8) \\ 1(0.2) \\ 14(0.8) \\ 1(0.1) \\ 3(0.4) \end{array}$ | $\begin{gathered} 450(7.6) \\ \sim \sim \\ 403(6.8) \\ \sim \sim \\ \sim \\ \sim 1 \\ \sim \end{gathered}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | 33 (1.3) <br> 32 (1.1) <br> 32 (1.5) <br> 34 (1.3) | $\begin{gathered} -- \\ 464(4.5) \\ 509(5.2) \\ 478(5.9) \\ 350(4.7) \end{gathered}$ | 48 (1.1) <br> 60 (1.0) <br> 50 (1.5) <br> 26 (1.1) | $\begin{gathered} -- \\ 464(5.2) \\ 525(4.4) \\ 477(4.3) \\ 355(4.2) \end{gathered}$ | 10 (0.6) <br> 7 (0.5) <br> 10 (0.6) <br> 23 (0.8) | $\begin{gathered} -- \\ 416(7.0) \\ 526(7.8) \\ 450(6.2) \\ 331(5.9) \end{gathered}$ | $\begin{aligned} & -- \\ & 9(0.6) \\ & 2(0.2) \\ & 8(0.6) \\ & 16(0.8) \end{aligned}$ | 404 (9.2) <br> 434 (7.4) <br> 322 (8.7) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 39(1.3) \\ 7(0.5) \\ 14(0.6) \\ 38(1.7) \\ 17(1.5) \end{array}$ | $\begin{array}{ll} 539 & (7.7) \\ 474 & (10.9) \\ 351 & (8.3) \\ 481 & (5.7) \\ 538 & (11.1) \end{array}$ | $\begin{array}{ll} 55 & (1.3) \\ 53 & (1.3) \\ 36 & (1.1) \\ 50 & (1.6) \\ 64 & (1.5) \end{array}$ | 544 (8.3) <br> 515 (4.9) <br> 368 (7.2) <br> 481 (5.8) <br> 533 (5.2) | $\begin{array}{r} 4(0.5) \\ 27(1.0) \\ 25(0.7) \\ 7(0.6) \\ 10(0.9) \end{array}$ | $\begin{aligned} & 524(14.0) \\ & 481(6.1) \\ & 344 \text { (7.7) } \\ & 450(11.0) \\ & 506(7.5) \end{aligned}$ | $\begin{array}{r} 2(0.4) \\ 13(0.8) \\ 25(1.1) \\ 5(0.5) \\ 9(0.7) \end{array}$ | 440 (8.3) <br> 320 (7.2) <br> 417 (13.0) <br> 497 (6.9) |
| Singapore <br> Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 16(0.8) \\ 37(1.3) \\ 9(0.9) \\ 24(1.2) \\ 23(0.8) \end{array}$ | $\begin{aligned} & 592(8.9) \\ & 534(4.7) \\ & 504(6.6) \\ & 261(6.2) \\ & 453(5.7) \end{aligned}$ | 64 (1.0) <br> 55 (1.1) <br> 58 (1.2) <br> 27 (1.2) <br> 65 (1.0) | $\begin{array}{ll} 614(5.9) \\ 537 & (4.3) \\ 541 & (2.8) \\ 323 & (10.4) \\ 478 & (5.3) \end{array}$ | $\begin{array}{r} 14(0.6) \\ 6(0.7) \\ 20(0.9) \\ 23(0.6) \\ 9(0.6) \end{array}$ | $\begin{aligned} & 585 \text { (7.4) } \\ & 515 \text { (13.0) } \\ & 530(4.7) \\ & 269 \text { (10.0) } \\ & 447(8.4) \end{aligned}$ | $\begin{array}{r} 6(0.4) \\ 2(0.3) \\ 12(0.7) \\ 26(0.9) \\ 3(0.3) \end{array}$ | $579(9.5)$ $\sim \sim$ $\sim 06(6.8)$ $251(6.3)$ $427(12.3)$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 63(0.9) \\ & 49 \\ & 10 \\ & 10 \end{aligned}(0.4)$ | $\begin{aligned} & 451(2.5) \\ & 445(4.1) \\ & 494(8.2) \end{aligned}$ | $\begin{array}{ll} 23 & (0.7) \\ 40 & (1.0) \\ 59 & (0.9) \end{array}$ | $\begin{aligned} & 451(3.3) \\ & 430(5.0) \\ & 522(3.9) \end{aligned}$ | $\begin{array}{r} 7(0.4) \\ 6(0.4) \\ 20(0.5) \end{array}$ | $\begin{aligned} & 433(6.5) \\ & 396(7.7) \\ & 488(3.9) \end{aligned}$ | $\begin{array}{r} 7(0.4) \\ 5(0.5) \\ 11(0.6) \end{array}$ | $\begin{aligned} & 432 \text { (7.6) } \\ & 374 \text { (11.1) } \\ & 455 \text { (5.1) } \end{aligned}$ |
| International Avg. | 28 (0.2) | 487 (1.2) | 52 (0.2) | 499 (0.8) | 13 (0.1) | 474 (1.4) | 8 (0.1) | 442 (1.8) |

[^46][^47]
## What Activities Do Students Do in Their Mathematics Lessons?

Because it can affect pedagogical strategies, class size data are shown in

"Exhibit 6.8. Teachers' reports about the size of their eighth-grade mathematics class reveal that across countries the average class size was 31 students, but there was considerable variation - from more than 50 students in the Philippines and South Africa to fewer than 20 students in Belgium (Flemish) and Finland. The relationship between class size and achievement is difficult to disentangle, given the variety of policies and practices and the fact that smaller classes can be used for both advanced and remedial learning. As shown in Exhibit 6.9, Cyprus, Korea, and Slovenia significantly reduced the average size of their mathematics classes between 1995 and 1999, and no countries showed increases.

Exhibit 6.1o presents a profile of the activities most commonly encountered in mathematics classes around the world, as reported by mathematics teachers. The two predominant activities, accounting for nearly half of class time on average, were teacher lecture ( 23 percent of class time) and teacher-guided student practice ( 22 percent). As shown in Exhibit 6.11, most students ( 86 percent on average internationally) agreed with teachers' reports, saying that their teachers frequently showed them how to do mathematics problems. According to 55 to 59 percent of the students, discussing homework and working independently on worksheets or textbooks were also frequent activities in class. Students also reported that use of the board was an extremely common presentational mode (see Exhibit 6.12). On average internationally, 92 percent of students reported that teachers used the board at least pretty often, and 60 percent reported that students used it at least pretty often. The use of an overhead projector was a popular presentational mode for teachers in some countries, with more than $4^{\circ}$ percent of the students in Canada, Finland, Singapore, South Africa, and the United States reporting that their teachers use it at least pretty often.

Educators, parents, employers, and most of the public support the goal of improving students' capacity for mathematics problem-solving. To examine the emphasis placed on that goal, timss created an index of teachers' emphasis on mathematics reasoning and problem-solving (EMRPS). As shown in Exhibit 6.13, the index is based on teachers' responses about how often they asked students to explain the reasoning behind an idea, represent and analyze relationships using tables, charts, or graphs, work on problems for which there was no immediate solution, and write equations to represent relationships. Students were placed in the high category if, on
average, they were asked to do these activities in most of their lessons. The medium level represents students asked to do these activities in some to most lessons, and students in the low category did the activities only in some lessons or rarely.

Nearly half the Japanese students were at the high level, compared with the international average of 15 percent. Across countries, most students ( 61 percent on average) were in the medium category. Countries with more than 70 percent of their students in the medium category were Romania, Slovenia, Bulgaria, the Czech Republic, the Slovak Republic, Hungary, Moldova, and the Russian Federation. Emphasizing reasoning and problem-solving was related to performance, with students at the high and medium levels having higher average achievement than those at the low level, both internationally and for most countries.

Exhibit R3.9 in the reference section shows the percentages of students asked in most or every lesson to engage in each of the activities included in the problem-solving index. For comparison purposes the percentages of students asked to practice computational skills in most or every lesson are also shown. According to their teachers, internationally on average, nearly three-fourths of the students (73 percent) were asked to practice their computational skills in most or every mathematics lesson. Nearly as many ( 7 o percent) were asked to explain the reasoning behind an idea this frequently. The other three problem-solving activities occurred much less often. Forty-three percent of students, on average across countries, wrote equations representing relationships in most or every lesson, but only about one-fourth ( 26 percent) represented and analyzed relationships using tables or graphs, and about one-fifth ( 21 percent) worked on problems for which there was no immediately obvious method of solution.

Exhibit 6.14 shows trend data for the index of teachers' emphasis on mathematics reasoning and problem-solving. These data suggest
 increased emphasis on problem-solving activities since the first timss assessment. Between 1995 and 1999, there was a small but significant increase (four percent) in the percentage of students at the high index level. Among countries, only Canada showed a significant increase, as the percentage of Canadian students in the high category rose from 4 to 13 percent. As shown in Exhibit R3.10 in the reference section, the international averages for the percentages of students asked to do the activities in most or every mathematics lesson increased for three of the activities (all except explain the rea-
soning behind an idea, which already was very frequent). Interestingly, however, the percentage of students asked to practice their computational skills in most or every lesson also increased significantly between 1995 and 1999.

Teachers were not asked about the emphasis placed on using things from everyday life in solving mathematics problems, but students were (see Exhibit R3.11). In most of the countries, students reported a moderate emphasis on doing these types of problems in mathematics class. Nearly two-thirds ( 65 percent), on average internationally, said these activities occurred once in a while or pretty often, and an additional 15 percent said they occurred almost always.


[^48]An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students. An "x" indicates teacher response data available for $<50 \%$ of students.

|  | Overall Average Class Size |  |  | 1-20 Students |  |  | 21-35 Students |  |  | 36 or More Students |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average | 1995-1999 Differenc |  | Percent of Students 1999 | 1995-199 <br> Differenc |  | Percent of Students 1999 | 1995-199: Differenc |  | Percent of Students 1999 | 1995-199 <br> Differenc |  |
| Australia | 27 (0.3) | 1 (0.5) | - | 9 (2.4) | -4 (3.3) | - | 91 (2.4) | 5 (3.4) | - | 0 (0.0) | -1 (0.8) | - |
| Belgium (Flemish) | 19 (0.4) | -1 (0.5) | - | 58 (3.5) | 9 (5.0) | $\bullet$ | 42 (3.5) | -9 (5.0) | - | 0 (0.0) | - - | - |
| Canada | 27 (0.3) | 0 (0.5) | - | 11 (2.1) | 0 (3.0) | $\bullet$ | 87 (2.3) | 0 (3.3) | - | 2 (1.0) | 0 (1.4) | - |
| Cyprus | 29 (0.2) | -2 (0.5) | $\checkmark$ | 0 (0.2) | -1 (0.7) | $\bullet$ | 100 (0.2) | 1 (0.7) | $\bullet$ | 0 (0.0) | - - | $\bullet$ |
| Czech Republic | 24 (0.4) | -1 (0.6) | - | 18 (4.2) | 5 (5.3) | - | 82 (4.2) | -5 (5.3) | - | 0 (0.0) | -- | - |
| England | $x$ x | $x \mathrm{x}$ |  | x x | $x$ x |  | x x | x x |  | x x | x x |  |
| Hong Kong, SAR | 37 (0.5) | -1 (0.8) | $\bullet$ | 7 (1.8) | 3 (2.6) | $\bullet$ | 15 (3.0) | 7 (4.3) | $\bullet$ | 78 (3.4) | -10 (4.9) | - |
| Hungary | 21 (0.5) | -1 (0.7) | - | 48 (4.2) | 11 (6.1) | - | 51 (4.1) | -10 (6.2) | - | 1 (0.0) | -1 (1.1) | - |
| Iran, Islamic Rep. | 33 (0.5) | -3 (1.3) | - | 5 (1.6) | 4 (1.8) | - | 57 (4.2) | 5 (7.2) | $\bullet$ | 38 (4.2) | -9 (7.2) | - |
| Israel ${ }^{\dagger}$ | 25 (0.8) | -4 (1.5) | - | 34 (3.7) | 21 (5.6) | $\triangle$ | 48 (4.4) | -13 (8.8) | - | 18 (3.5) | -8 (7.9) | - |
| Italy | 20 (0.4) | 1 (0.6) | - | 53 (4.8) | -11 (6.9) | - | 47 (4.7) | 10 (6.8) | - | 1 (0.0) | 1 (0.0) | $\triangle$ |
| Japan | 36 (0.2) | -1 (0.4) | - | 1 (0.0) | 0 (0.0) | $\triangle$ | 41 (3.4) | 8 (5.3) | $\bullet$ | 58 (3.3) | -9 (5.3) | - |
| Korea, Rep. of | 42 (0.5) | -8 (0.9) | V | 0 (0.0) | -2 (1.4) | $\bullet$ | 12 (2.2) | 10 (2.6) | - | 88 (2.2) | -7 (2.9) | - |
| Latvia (LSS) | 22 (0.5) | 0 (1.0) | - | 45 (4.2) | 4 (7.1) | $\bullet$ | 55 (4.2) | 1 (7.3) | - | 0 (0.0) | -5 (2.1) | - |
| Lithuania | 23 (0.3) | 2 (0.6) | - | 32 (2.8) | -11 (5.8) | - | 68 (2.8) | 11 (5.8) | - | 0 (0.0) | - - | - |
| Netherlands | 25 (0.5) | 0 (0.8) | - | 13 (4.1) | -3 (6.4) | - | 87 (4.1) | 3 (6.4) | - | 0 (0.0) | - - | - |
| New Zealand | 25 (0.4) | -1 (0.6) | - | 17 (2.9) | 6 (4.0) | $\bullet$ | 82 (2.8) | -7 (4.0) | - | 1 (0.0) | 1 (0.0) | $\triangle$ |
| Romania | 24 (0.4) | -2 (0.9) | - | 30 (2.9) | 7 (5.2) | - | 65 (3.2) | -1 (5.4) | $\bullet$ | 5 (1.9) | -5 (3.6) | - |
| Russian Federation | 24 (0.5) | -1 (0.6) | - | 19 (3.2) | 4 (4.2) | - | 81 (3.2) | -3 (4.3) | - | 0 (0.0) | -1 (0.2) | V |
| Singapore | 37 (0.3) | 0 (0.5) | - | 1 (0.4) | 0 (0.8) | - | 32 (3.8) | -1 (5.8) | $\bullet$ | 68 (3.8) | 1 (5.8) | - |
| Slovak Republic | 25 (0.4) | -1 (0.5) | $\bigcirc$ | 15 (2.6) | 0 (3.8) | - | 85 (2.6) | 0 (3.9) | - | 0 (0.2) | 0 (0.8) | - |
| Slovenia | 22 (0.3) | -2 (0.4) | $\checkmark$ | 29 (3.2) | 13 (4.4) | - | 71 (3.2) | -13 (4.4) | $\bullet$ | 0 (0.0) | - - | - |
| Thailand ${ }^{\dagger}$ | x x | x x |  | $x \mathrm{x}$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | x x |  |
| United States | 26 (0.7) | 1 (1.0) | - | 21 (2.6) | -4 (4.3) | $\bullet$ | 73 (3.0) | 3 (4.7) | $\bullet$ | 6 (1.4) | 1 (2.3) | - |
| International Avg. § | 27 (0.1) | -1 (0.2) | v | 21 (0.6) | 2 (0.9) | - | 63 (0.7) | 0 (1.1) | $\bullet$ | 16 (0.4) | -1 (0.6) | - |



## Background data provided by teachers.

$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995
§ International average is for countries that participted and met sampling guidelines in both 1995 and 1999
Trend notes: Because coverage fell below $65 \%$ in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates teacher response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999. An "x" indicates teacher response data available for $<50 \%$ of students, based on the lower response rate in either 1995 or 1999.

\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \& \multicolumn{8}{|c|}{Average Percentage of Class Time Spent in a Typical Month of Lessons} \\
\hline \& Administrative Tasks \& Homework Review \& Lecture-Style Presentation by Teacher \& TeacherGuided Student Practice \& Re-teaching and Clarification of Content/ Procedures \& Student Independent Practice \& Tests and Quizzes \& Other \\
\hline \begin{tabular}{l}
Australia Belgium (Flemish) \\
Bulgaria \\
Canada Chile
\end{tabular} \& \[
\begin{array}{r} 
\\
4(0.4) \\
\\
\\
\\
\\
r \\
2(0.3) \\
\\
\\
\\
5(0.4) \\
6(0.2)
\end{array}
\] \& \(9(0.5)\)
\(7(0.4)\)
\(7(0.4)\)
\(r \quad 14(0.4)\)

$14(0.6)$ \& $19(1.3)$
$24(1.1)$
$37(1.7)$
$r \quad 20(0.9)$
$24(1.2)$ \& $22(0.9)$
$29(1.0)$
$18(1.1)$
$r \quad 18(0.8)$

$18(0.9)$ \& $$
\begin{array}{r}
12(0.6) \\
10(0.4) \\
\\
r \\
10(0.5) \\
r \\
\\
10(0.3) \\
19(0.8)
\end{array}
$$ \& $22(1.3)$

$14(0.9)$
$14(1.3)$
$r \quad 20(0.7)$
$8(0.5)$ \& $8(0.3)$

$r$
$10(0.3)$
$10(0.6)$

$12(0.3)$
$(0.6)$ \& $3(0.4)$

$1(0.4)$

$3(0.3)$

$3(0.6)$ <br>

\hline | Chinese Taipei |
| :--- |
| Cyprus |
| Czech Republic |
| England Finland | \& \[

$$
\begin{array}{ll} 
& 3(0.6) \\
& 3(0.4) \\
& 3(0.3) \\
& 3(0.2) \\
& 2(0.3)
\end{array}
$$

\] \& |  | $12(0.5)$ |
| ---: | ---: |
| $r$ | $21(0.8)$ |
|  | $5(0.4)$ |
| s | $6(0.5)$ |
|  | $16(0.6)$ | \& |  | $39(1.3)$ |
| ---: | ---: |
| $r$ | $17(1.0)$ |
|  | $23(0.7)$ |
| s | $18(0.9)$ |
|  | $15(0.7)$ | \& \[

$$
\begin{array}{rl} 
& 15(0.5) \\
\mathrm{r} & 25(1.0) \\
& 29(1.2) \\
\mathrm{s} & 27(1.2) \\
& 25(1.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{rl} 
& 11(0.6) \\
r & 12(0.5) \\
& 10(0.5) \\
& 11(0.4) \\
& 10(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{rr} 
& 9(0.5) \\
r & 10(1.0) \\
& 19(1.0) \\
\text { s } & 24(1.5) \\
& 24(1.4)
\end{array}
$$

\] \&  \& \[

$$
\begin{array}{ll} 
& 2(0.4) \\
& \begin{array}{l}
2(0.3) \\
\\
\\
\\
\\
\\
3(0.4) \\
\\
3(0.7) \\
2(0.3)
\end{array}
\end{array}
$$
\] <br>

\hline | Hong Kong, SAR |
| :--- |
| Hungary |
| Indonesia |
| Iran, Islamic Rep. |
| Israel | \& \[

$$
\begin{aligned}
& 5(0.7) \\
& 2(0.2) \\
& 7(0.5) \\
& 6(0.9) \\
& 4(0.6)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
12(0.7) \\
\\
\\
\\
\\
\\
\\
\\
\\
\\
r \\
r
\end{array}
$$ 15(0.5)
\] \& $32(1.6)$

$14(0.7)$
$11(1.0)$
$25(2.4)$

$r \quad 19(0.8)$ \& \[
$$
\begin{array}{r} 
\\
\\
\\
\\
29(0.8) \\
\\
\\
29(1.0) \\
\\
\\
r
\end{array}
$$ 21(2.6)

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
\\
\\
\\
13(0.5) \\
\\
13(0.6) \\
\\
r \quad 22(2.6) \\
r
\end{array}
$$ 14(0.8)

\] \&  \& \[

$$
\begin{array}{r}
8(0.4) \\
\\
\\
\\
\\
\\
16(0.4) \\
\\
r \quad 22(0.9) \\
r \quad 10(0.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r} 
\\
3(0.4) \\
\\
3(0.4) \\
\\
4(0.4) \\
\\
\\
\hline
\end{array}
$$
\] <br>

\hline | Italy |
| :--- |
| Japan Jordan |
| Korea, Rep. of Latvia (LSS) | \& \[

$$
\begin{array}{ll}
2(0.2) \\
2(0.5) \\
8(1.0) \\
3(0.6) \\
3(0.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.5) \\
5(0.4) \\
18(1.2) \\
6(0.3) \\
11(0.7)
\end{array}
$$

\] \& | 25 (0.7) |
| :--- |
| 34 (1.6) |
| 18 (1.4) |
| 33 (1.4) |
| 16 (0.9) | \& \[

$$
\begin{aligned}
& 22(0.7) \\
& 26(1.3) \\
& 22(1.5) \\
& 22(0.8) \\
& 33(1.6)
\end{aligned}
$$

\] \& \[

$$
\begin{aligned}
& 13(0.4) \\
& 16 \\
& (0.9) \\
& 14 \\
& (1.1) \\
& 14 \\
& (0.8) \\
& 13
\end{aligned}
$$(0.8)

\] \& | 12 (0.5) |
| :--- |
| 9 (0.7) |
| 16 (1.3) |
| 14 (0.8) |
| 10 (0.9) | \& \[

$$
\begin{array}{r}
12(0.5) \\
7(0.5) \\
15(1.2) \\
7(0.3) \\
7(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
1 & (0.2) \\
2 & (0.3) \\
6 & (0.9) \\
3 & (0.4) \\
7 & (0.8)
\end{array}
$$
\] <br>

\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{ll}
2 & (0.2) \\
5 & (0.3) \\
7 & (0.7) \\
5 & (1.1) \\
3 & (0.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
8(0.4) \\
17(1.0) \\
15(1.0) \\
14(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
22 & (0.7) \\
41 & (1.2) \\
19 & (1.1) \\
21 & (1.1) \\
28 & (1.1)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 26(1.0) \\
& 18(0.8) \\
& 27(1.3) \\
& 20(0.9) \\
& 19(1.0)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
10(0.3) \\
7(0.4) \\
13(0.8) \\
11(0.5) \\
12(0.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.6) \\
11(0.5) \\
11(0.9) \\
18(0.9) \\
5(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
13(0.5) \\
7(0.4) \\
10(0.5) \\
9(0.5) \\
12(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
2 & (0.3) \\
3 & (0.3) \\
4 & (0.5) \\
5 & (0.5) \\
5 & (0.7)
\end{array}
$$
\] <br>

\hline Netherlands
New Zealand
Philippines
Romania

Russian Federation \& $$
\begin{aligned}
& 5(0.4) \\
& 5(0.3) \\
& 8(1.1) \\
& 4(0.5) \\
& 2(0.1)
\end{aligned}
$$ \& \[

$$
\begin{array}{r}
15(1.5) \\
9(0.4) \\
12(1.0) \\
12(0.4) \\
10(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
9(1.2) \\
17(0.9) \\
24(1.4) \\
26(1.2) \\
25(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
5(1.0) \\
22(1.1) \\
19(1.2) \\
16(0.8) \\
17(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
18 & (1.1) \\
11 & (0.6) \\
13 & (1.0) \\
12 & (0.6) \\
11 & (0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
32 & (2.0) \\
24 & (1.2) \\
18 & (1.2) \\
12 & (0.5) \\
17 & (0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
11(0.6) \\
8(0.3) \\
18(1.1) \\
14(0.7) \\
12(0.6)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 5(1.0) \\
& 3(0.5) \\
& 4(0.5) \\
& 4(0.4) \\
& 5(0.4)
\end{aligned}
$$
\] <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& $$
\begin{array}{r}
6(0.6) \\
3(0.3) \\
4(0.3) \\
13(1.4) \\
10
\end{array}
$$ \& \[

$$
\begin{array}{r}
13(0.7) \\
8(0.3) \\
11(0.5) \\
26(1.6) \\
16
\end{array}
$$(1.2)

\] \& \[

$$
\begin{array}{r}
28(1.5) \\
9(0.8) \\
24(1.0) \\
23(1.8) \\
22(1.5)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 20(1.2) \\
& 30(1.1) \\
& 24(0.8) \\
& 26(1.7) \\
& 19(1.1)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
9(0.3) \\
13(0.5) \\
16(0.7) \\
21(1.6) \\
15(1.0)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 12(0.8) \\
& 23(1.1) \\
& 10(0.7) \\
& 21(1.8) \\
& 16 \\
& 16
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
11(0.5) \\
8(0.3) \\
22(1.3) \\
14(1.1)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 3(0.3) \\
& 4(0.5) \\
& 3(0.4) \\
& 7(1.1) \\
& 3(0.5)
\end{aligned}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& \[

$$
\begin{array}{r}
3(0.3) \\
\\
\\
\mathrm{r}(0.6) \\
6(0.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.8) \\
9(0.7) \\
r \quad 15(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
20(1.7) \\
\\
49(1.2) \\
r \quad 20(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
27(1.4) \\
14(0.8) \\
r \quad 18(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
11(0.7) \\
13(0.8) \\
r \quad 12(0.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
8(0.7) \\
\\
r \quad 17(0.7) \\
r(0.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
12(0.7) \\
\\
\\
r \quad 11(0.6) \\
\hline
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
4(0.4) \\
\\
4(0.6) \\
r \quad 4(0.5)
\end{array}
$$
\] <br>

\hline International Avg. \& 5 (0.1) \& 12 (0.1) \& 23 (0.2) \& 22 (0.2) \& 13 (0.1) \& 15 (0.2) \& 11 (0.1) \& 4 (0.1) <br>
\hline
\end{tabular}

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " r " indicates teacher response data available for $70-84 \%$ of students. An " s " indicates teacher response data available for $50-69 \%$ of students.

|  | Percentage of Students Reporting Almost Always or Pretty Often |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | We Discuss Our Completed Homework | Teacher Shows Us How to Do Mathematics | We Work on Worksheets or Textbooks on Our | We Work on Mathematics Projects | We Begin Our Homework |
| Australia | 44 (1.8) | 93 (0.7) | 91 (1.2) | 25 (1.7) | 56 (1.6) |
| Belgium (Flemish) | 43 (1.4) | 69 (0.9) | 64 (1.0) | 16 (1.1) | 20 (1.4) |
| Bulgaria | 48 (1.9) | 89 (1.0) | 32 (1.2) | 15 (1.0) | 21 (1.4) |
| Canada | 62 (1.4) | 92 (0.5) | 92 (0.5) | 28 (1.1) | 82 (1.2) |
| Chile | 47 (1.3) | 89 (0.9) | 40 (1.1) | 46 (1.6) | 55 (1.2) |
| Chinese Taipei | 55 (1.0) | 91 (0.5) | 59 (1.2) | 55 (1.2) | 34 (1.0) |
| Cyprus | 72 (1.1) | 92 (0.7) | 67 (1.0) | 29 (1.0) | 52 (2.3) |
| Czech Republic | 42 (1.8) | 86 (1.1) | 51 (2.4) | 8 (0.6) | 16 (1.6) |
| England | 62 (1.5) | 93 (0.7) | 88 (1.5) | 35 (1.4) | 27 (1.6) |
| Finland | 37 (1.3) | 67 (1.3) | 90 (1.0) | 7 (0.8) | 47 (2.0) |
| Hong Kong, SAR | 35 (1.1) | 91 (0.6) | 69 (1.2) | 67 (1.4) | 40 (1.1) |
| Hungary | 71 (1.5) | 87 (1.0) | 63 (1.7) | 96 (0.4) | 18 (1.2) |
| Indonesia | 48 (1.0) | 88 (0.6) | 36 (1.5) | 86 (0.9) | 13 (0.7) |
| Iran, Islamic Rep. | 56 (1.0) | 82 (0.7) | 45 (0.9) | 30 (1.1) | 34 (1.3) |
| Israel | 64 (1.3) | 90 (0.6) | 72 (1.2) | 20 (1.0) | 65 (1.5) |
| Italy | 64 (1.4) | 80 (1.2) | 34 (1.2) | 22 (1.3) | 39 (2.3) |
| Japan | 19 (1.2) | 88 (0.7) | 38 (1.5) | 6 (0.7) | 20 (1.3) |
| Jordan | 76 (0.9) | 92 (0.6) | 45 (1.1) | 40 (1.4) | 59 (1.1) |
| Korea, Rep. of | 10 (0.5) | 85 (0.8) | 29 (0.7) | 46 (1.2) | 17 (0.7) |
| Latvia (LSS) | 48 (1.8) | 86 (1.0) | 54 (1.2) | - - | 28 (1.6) |
| Lithuania ${ }^{\text {\# }}$ | - - | - - | -- | - - | - - |
| Macedonia, Rep. of | 72 (1.3) | 86 (0.8) | 66 (1.6) | 37 (1.1) | 30 (1.4) |
| Malaysia | 61 (1.0) | 92 (0.5) | 13 (0.7) | 68 (1.1) | 67 (1.3) |
| Moldova | 61 (1.3) | 91 (0.8) | 66 (1.7) | 52 (1.6) | 32 (1.6) |
| Morocco | 69 (0.8) | 86 (0.6) | 53 (1.0) | 49 (1.1) | 53 (1.2) |
| Netherlands | 68 (3.7) | 70 (2.7) | 92 (1.1) | 3 (0.7) | 89 (1.5) |
| New Zealand | 55 (1.8) | 92 (0.6) | 89 (1.0) | 33 (1.5) | 43 (1.7) |
| Philippines | 78 (0.8) | 87 (0.8) | 64 (1.0) | 56 (1.2) | 49 (1.1) |
| Romania | 62 (1.4) | 83 (0.9) | 49 (1.1) | 38 (2.0) | 27 (1.6) |
| Russian Federation | 53 (1.4) | 78 (1.2) | 62 (1.3) | 19 (0.9) | 10 (0.8) |
| Singapore | 61 (1.0) | 97 (0.4) | 75 (0.9) | 15 (1.1) | 60 (1.9) |
| Slovak Republic | 59 (1.9) | 81 (1.0) | 53 (1.6) | 11 (0.8) | 39 (1.9) |
| Slovenia | 60 (1.7) | 76 (1.5) | 57 (1.8) | 19 (0.9) | 28 (1.9) |
| South Africa | 72 (0.8) | 83 (0.7) | 67 (1.2) | 59 (1.4) | 69 (1.1) |
| Thailand | 29 (1.2) | 91 (0.7) | 52 (1.1) | 19 (1.0) | 80 (0.9) |
| Tunisia | 63 (1.2) | 85 (0.9) | 57 (1.0) | 77 (0.7) | 32 (1.1) |
| Turkey | 35 (1.1) | 84 (0.7) | 38 (0.9) | 22 (0.8) | 21 (1.2) |
| United States | 79 (1.2) | 94 (0.6) | 86 (0.7) | 29 (1.3) | 74 (1.6) |
| International Avg. | 55 (0.2) | 86 (0.2) | 59 (0.2) | 36 (0.2) | 42 (0.2) |

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate

|  | Percentage of Students Reporting Almost Always or Pretty Often |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Teacher <br> Uses the Board | Teacher Uses an Overhead Projector | Teacher Uses a Computer to Demonstrate Ideas in Mathematics | Students Use the Board | Students Use an Overhead Projector |
| Australia | 96 (0.8) | 10 (1.5) | 4 (0.4) | 15 (1.4) | 3 (0.4) |
| Belgium (Flemish) | 96 (0.7) | 11 (1.7) | 2 (0.5) | 42 (1.8) | 2 (0.8) |
| Bulgaria | 93 (0.6) | 10 (1.1) | 4 (0.6) | 79 (2.1) | 7 (0.7) |
| Canada | 91 (0.9) | 42 (2.7) | 5 (0.5) | 25 (1.2) | 7 (0.8) |
| Chile | 96 (0.6) | 10 (0.8) | 10 (0.9) | 79 (1.5) | 6 (0.6) |
| Chinese Taipei | 96 (0.4) | 4 (0.4) | 2 (0.2) | 48 (1.6) | 2 (0.3) |
| Cyprus | 97 (0.3) | 12 (0.7) | 7 (0.6) | 92 (0.6) | 8 (0.5) |
| Czech Republic | 97 (0.4) | 9 (1.6) | 2 (0.4) | 91 (1.7) | 4 (0.5) |
| England | 94 (1.5) | 19 (2.6) | 6 (0.8) | 13 (1.0) | 3 (0.6) |
| Finland | 94 (1.4) | 42 (2.9) | 2 (0.4) | 52 (2.6) | 5 (0.7) |
| Hong Kong, SAR | 96 (0.4) | 9 (0.8) | 3 (0.4) | 46 (1.7) | 3 (0.4) |
| Hungary | 96 (0.6) | 6 (0.7) | 3 (0.4) | 62 (1.7) | 3 (0.4) |
| Indonesia | 93 (0.5) | 6 (0.5) | 2 (0.5) | 45 (1.4) | 4 (0.4) |
| Iran, Islamic Rep. | 94 (0.5) | 8 (0.6) | 0 (0.1) | 89 (0.7) | 5 (0.4) |
| Israel | 90 (0.6) | 19 (1.1) | 11 (0.9) | 40 (1.6) | 13 (0.9) |
| Italy | 94 (0.5) | 8 (0.9) | 5 (0.6) | 84 (1.1) | 7 (0.6) |
| Japan | 99 (0.2) | 4 (0.8) | 1 (0.4) | 50 (2.5) | 1 (0.3) |
| Jordan | 91 (0.6) | 23 (1.0) | 12 (1.2) | 80 (0.9) | 19 (1.0) |
| Korea, Rep. of | 93 (0.5) | 10 (0.8) | 7 (0.9) | 38 (1.7) | 3 (0.3) |
| Latvia (LSS) | 83 (1.3) | 7 (1.1) | 5 (0.7) | 83 (1.7) | 4 (0.5) |
| Lithuania ${ }^{\ddagger}$ | - - | - - | - - | - - | - - |
| Macedonia, Rep. of | 95 (0.7) | 22 (1.5) | 6 (0.8) | 89 (1.1) | 14 (0.9) |
| Malaysia | 96 (0.5) | 6 (1.0) | 1 (0.2) | 52 (1.4) | 3 (0.3) |
| Moldova | 83 (0.9) | 37 (1.8) | 13 (1.1) | 85 (0.8) | 31 (1.6) |
| Morocco | $r \quad 87$ (0.7) | $5 \quad 32$ (1.1) | s $\quad 9(1.0)$ | 71 (1.2) | s 24 (1.0) |
| Netherlands | 90 (1.6) | 7 (1.4) | 2 (0.3) | 9 (1.2) | 2 (0.3) |
| New Zealand | 95 (0.8) | 32 (2.7) | 7 (0.7) | 24 (1.5) | 7 (0.7) |
| Philippines | 89 (0.7) | 35 (1.4) | 19 (1.5) | 63 (1.1) | 30 (1.4) |
| Romania | 94 (0.4) | 12 (0.9) | 2 (0.3) | 92 (0.7) | 9 (0.8) |
| Russian Federation | 96 (0.4) | 7 (1.0) | 1 (0.2) | 92 (0.6) | 4 (0.5) |
| Singapore | 96 (1.3) | 75 (2.1) | 11 (1.2) | 52 (2.0) | 21 (1.1) |
| Slovak Republic | 89 (1.2) | 10 (1.4) | 2 (0.3) | 95 (0.6) | 3 (0.4) |
| Slovenia | 95 (0.5) | 29 (2.2) | 5 (0.6) | 72 (2.1) | 7 (0.7) |
| South Africa | 86 (0.8) | 45 (1.6) | - - | 56 (1.7) | 36 (1.5) |
| Thailand | 93 (0.8) | 7 (0.8) | 6 (0.6) | 33 (1.5) | 4 (0.5) |
| Tunisia | 84 (0.8) | 13 (0.8) | 1 (0.3) | 71 (0.9) | 8 (0.6) |
| Turkey | 93 (0.4) | 13 (0.8) | 2 (0.3) | 80 (0.9) | 8 (0.6) |
| United States | 80 (1.9) | 59 (3.3) | 9 (0.7) | 37 (1.9) | 16 (1.0) |
| International Avg. | 92 (0.1) | 19 (0.3) | 5 (0.1) | 60 (0.2) | 9 (0.1) |

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An "r" indicates a $70-84 \%$ student response rate. An " $s$ " indicates a 50-69\% student response rate.

Exhibit 6.13 Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)


Index based on teachers' responses to four questions about how often they ask students to: 1) explain the reasoning behind an idea; 2) represent and analyze relationships using tables, charts, or graphs; 3) work on problems for which there is no immediately obvious method of solution; 4) write equations to represent relationships (see reference exhibit R3.9).
Average is computed across the four items based on a 4point scale: $1=$ never or almost never; 2 = some lessons; 3 = most lessons; 4 = every lesson. High level indicates average is greater than or equal to 3 . Medium level indicates average is greater than or equal to 2.25 and less than 3. Low level indicates average is less than 2.25.


[^49][^50]

Exhibit 6.14 Trends in Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)

TIMSS 1999
8
Mathematics

|  | High <br> EMRPS <br> Percent of Students |  |  |  | Medium EMRPS <br> Percent of Students |  |  |  | Low <br> EMRPS <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 Difference |  | 1995 | 1999 | 1995-1999 Difference |  | 1995 | 1999 | 1995-1999 <br> Difference |  |
| Australia | 2 (1.1) | 7 (2.1) | 5 (2.4) | - | 43 (3.8) | 54 (4.5) | 11 (5.9) | - | 55 (3.9) | 39 (4.3) | -16 (5.8) | - |
| Belgium (Flemish) | 0 (0.0) | 1 (0.4) | 1 (0.4) | $\bullet$ | 29 (3.3) | 39 (3.1) | 10 (4.5) | - | 71 (3.3) | 61 (3.1) | -11 (4.5) | - |
| Canada | 4 (1.7) | 13 (2.0) | 9 (2.6) | $\triangle$ | 54 (5.0) | 62 (3.4) | 8 (6.0) | - | 42 (5.1) | 26 (3.0) | -16 (6.0) | - |
| Cyprus | 20 (4.4) | 13 (3.5) | -7 (5.6) | $\bullet$ | 51 (6.0) | 68 (4.9) | 16 (7.7) | - | 29 (5.6) | 19 (3.8) | -9 (6.8) | - |
| Czech Republic | 18 (4.1) | 21 (4.2) | 3 (5.8) | - | 65 (5.9) | 73 (4.6) | 8 (7.5) | - | 17 (5.0) | 6 (2.6) | -11 (5.7) | - |
| England | 4 (1.4) | 3 (1.4) | -1 (2.0) | - | 62 (3.2) | 66 (3.5) | 4 (4.7) | - | 34 (3.1) | 31 (3.4) | -4 (4.6) | - |
| Hong Kong, SAR | 5 (2.4) | 6 (2.2) | 1 (3.2) | - | 41 (5.5) | 56 (3.6) | 15 (6.6) | $\bigcirc$ | 54 (5.4) | 38 (3.7) | -16 (6.5) | - |
| Hungary | 20 (3.1) | 16 (3.0) | -4 (4.3) | $\bigcirc$ | 71 (4.0) | 74 (3.3) | 3 (5.2) | - | 10 (2.4) | 10 (2.3) | 1 (3.4) | - |
| Iran, Islamic Rep. | 6 (2.1) | 16 (3.5) | 10 (4.0) | - | 52 (5.3) | 45 (4.2) | -7 (6.7) | - | 42 (5.4) | 39 (4.1) | -3 (6.8) | - |
| Israel ${ }^{\dagger}$ | 13 (4.5) | 17 (2.8) | 4 (5.3) | - | 58 (7.5) | 62 (3.6) | 4 (8.3) | - | 29 (7.6) | 21 (3.1) | -8 (8.2) | - |
| Italy | 15 (3.4) | 28 (3.8) | 14 (5.1) | - | 66 (4.7) | 58 (4.5) | -8 (6.5) | - | 19 (3.5) | 14 (3.3) | -6 (4.8) | - |
| Japan | 37 (4.1) | 49 (4.1) | 12 (5.9) | - | 54 (4.1) | 45 (4.1) | -9 (5.8) | - | 10 (2.3) | 7 (2.1) | -3 (3.1) | - |
| Korea, Rep. of | 15 (3.2) | 21 (3.0) | 6 (4.4) | $\bullet$ | 70 (4.2) | 66 (3.3) | -4 (5.3) | $\bigcirc$ | 15 (3.5) | 13 (2.4) | -2 (4.3) | - |
| Latvia (LSS) | 14 (3.8) | 6 (2.0) | -8 (4.2) | - | 60 (4.9) | 64 (4.4) | 4 (6.6) | $\bigcirc$ | 26 (4.2) | 30 (4.1) | 4 (5.9) | - |
| Lithuania | 6 (2.1) | 9 (2.4) | 4 (3.2) | - | 66 (3.9) | 67 (3.7) | 1 (5.4) | - | 28 (3.9) | 23 (3.7) | -5 (5.4) | - |
| Netherlands | -- | -- | -- |  |  |  | -- |  | -- | - - | - - |  |
| New Zealand s | 2 (1.2) | 5 (2.2) | 3 (2.5) | $\bullet$ | 50 (4.1) | 48 (4.3) | -2 (6.0) | - | 49 (4.3) | 47 (4.0) | -2 (5.9) | - |
| Romania | 26 (3.6) | 22 (4.5) | -3 (5.8) | - | 69 (4.0) | 73 (4.4) | 5 (5.9) | $\bigcirc$ | 6 (1.9) | 4 (1.7) | -1 (2.5) | - |
| Russian Federation | 5 (1.6) | 11 (2.5) | 6 (3.0) | - | 78 (4.0) | 74 (3.9) | -4 (5.6) | - | 17 (3.6) | 15 (3.6) | -2 (5.0) | - |
| Singapore s | 2 (1.4) | 7 (2.1) | 5 (2.5) | - | 48 (4.9) | 47 (4.0) | -1 (6.3) | - | 50 (4.8) | 47 (4.4) | -3 (6.5) | - |
| Slovak Republic | 12 (2.7) | 18 (3.9) | 6 (4.7) | - | 80 (3.1) | 71 (4.2) | -8 (5.3) | - | 8 (2.2) | 10 (2.8) | 2 (3.6) | - |
| Slovenia | 11 (2.9) | 21 (3.6) | 10 (4.6) | $\bullet$ | 74 (4.3) | 72 (3.9) | -3 (5.9) | - | 14 (3.6) | 7 (2.0) | -8 (4.1) | - |
| Thailand ${ }^{\dagger}$ | 2 (0.3) | 6 (1.6) | 4 (1.6) | $\bullet$ | 36 (5.4) | 58 (4.7) | 21 (7.1) | - | 62 (5.5) | 36 (4.5) | -25 (7.1) | $\nabla$ |
| United States | 10 (2.7) | 18 (2.5) | 8 (3.7) | $\bullet$ | 52 (3.7) | 57 (2.9) | 5 (4.7) | - | 38 (3.6) | 24 (2.7) | -13 (4.5) | - |
| International Avg. § | 11 (0.6) | 15 (0.6) | 4 (0.9) | $\Delta$ | 59 (1.0) | 61 (0.9) | 2 (1.3) | - | 30 (0.9) | 24 (0.7) | -6 (1.1) | $\nabla$ |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by teachers.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $s$ " indicates teacher response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999.

## How Are Calculators and Computers Used?

Exhibit 6.15 shows data on students' access to calculators for use in mathematics class and policies on their use for those with access. In 14 countries, teachers reported that nearly all students (more than go percent) had access to calculators in class. The countries with this high degree of access were Australia, Belgium (Flemish), Canada, the Czech Republic, England, Finland, Hong Kong, Israel, Lithuania, the Netherlands, New Zealand, Singapore, the Slovak Republic, and the United States. For students in classes with access to calculators, most teachers reported some type of restricted use (for about two-thirds of the students on average internationally).

TIMss combined students' and teachers' reports on the frequency of calculator use to create an index of emphasis on calculators in mathematics class (ECMC), presented in Exhibit 6.16. Students were placed in the high category if they reported using calculators in class almost always or pretty often and their teachers reported calculator use of at least once or twice a week. At the other end of the spectrum, students were placed at the low level if they reported using calculators only once in a while or never and their teachers reported asking students to use calculators never or hardly ever. There was enormous variation in the results across countries. The Netherlands, Singapore, and Australia had more than four-fifths of their students (from 84 percent to 95 percent) in the high category. In contrast, a number of countries had half or more of their students in the low category, including Chinese Taipei, Iran, Korea, Japan, Malaysia, Romania, Thailand, and Turkey. Since several high-performing countries have restricted calculator use and large percentages of students are in the low-use category, the relationship between calculator use and performance is difficult to interpret. Although on average internationally the relationship is unclear, in most of the countries where emphasis on calculator use was high, there was a positive association between calculator use and mathematics achievement.

Exhibit R9. 12 in the reference section shows the detailed results for students' reports on frequency of calculator use. In the Netherlands, 67 percent of the students reported almost always using calculators in their mathematics lessons. Countries with the next highest level of use included Canada, Israel, New Zealand, South Africa, and the United States (from 42 to 45 percent). Exhibit R3. 13 shows the trends between 1995 and 1999. Internationally on average, there was a small but significant decrease in the percentage of students who reported that they almost always used calculators. Teachers were asked how often they asked stu-

dents to use calculators for a variety of activities. The percentages of students asked to use calculators for each activity at least once or twice a week are shown in Exhibit R3.14. According to teachers, they asked the most students to use calculators at least weekly for checking answers, performing routine computations, and solving complex problems (43 to 44 percent internationally each). About one-fourth of the students across countries were asked to explore number concepts and one-fifth to use calculators on their tests.

Exhibit 6.17 shows trend data for the index of emphasis on calculators in mathematics class. There was a shift toward less frequent use of calculators between 1995 and 1999. Significantly fewer students were at the high level of the emphasis on calculators index in 1999 than in 1995 in five countries: the Czech Republic, England, Latvia (Lss), the Russian Federation, and the Slovak Republic. Two countries, Belgium (Flemish) and Thailand, had increased percentages of students in the high category. As shown in Exhibit R3.13, changes in students' reports on the frequency of calculator use from 1995 to 1999 show a significant decrease in the percentage of students in the almost always category in eight countries: Cyprus, the Czech Republic, England, Hong Kong, Latvia, Romania, the Russian Federation, and the Slovak Republic. The Netherlands and Singapore, however, showed increases in that category.

Students' reports on their frequency of computer use in mathematics class are presented in Exhibit 6.18. Across countries, the vast majority of students ( 80 percent on average internationally) reported never using computers in mathematics class. The trend data, however, show a small but statistically significant shift from the never to the once in a while category (see Exhibit 6.19). Significantly more students reported using computers in mathematics class once in a while in 1999 than in 1995 in six countries: Canada, Hong Kong, Korea, Singapore, Slovenia, and Thailand.

Because the Internet provides a wealth of opportunities for students to collect and analyze data, timss began asking about students' access to the Internet and whether they used the World Wide Web to access information for mathematics projects. The data in Exhibit 6.20 indicate great variation across countries in Internet access. Still, the international averages show about one-quarter of the students with access to the Internet at school. The international average for using the Internet to access information for mathematics class on even a monthly basis was 10 percent (less than half those reporting access).


[^51]Exhibit 6.16 Index of Emphasis on Calculators in Mathematics Class (ECMC)*

| Index of Emphasis on Calculators in Mathematics Class |  | High ECMC |  | Medium ECMC |  | Low ECMC |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on students' reports of the frequency of using calculators in mathematics lessons and teachers' reports of students' | Netherlands Singapore Australia England Canada | 95 (1.1) <br> 85 (1.6) <br> 84 (2.4) <br> 80 (2.3) <br> 79 (1.9) | $\begin{aligned} & 538(7.2) \\ & 611(6.3) \\ & 531(5.5) \\ & 524(5.7) \\ & 537(3.0) \end{aligned}$ | $\begin{array}{r} 5(1.1) \\ 15(1.6) \\ 12(1.8) \\ 19(2.2) \\ 18(1.7) \end{array}$ | $\begin{aligned} & 512 \text { (23.5) } \\ & 567 \text { (7.1) } \\ & 515 \text { (12.9) } \\ & 462 \text { (6.5) } \\ & 523 \text { (4.7) } \end{aligned}$ | $\begin{aligned} & 0(0.0) \\ & 0(0.0) \\ & 4(1.6) \\ & 1(0.7) \\ & 3(0.9) \end{aligned}$ | $484 \text { (24.7) }$ $548 \text { (6.8) }$ |
| use of calculators in mathematics class for five activities: checking answers; tests and exams; routine computation; solving complex problems; and exploring | New Zealand Hong Kong, SAR <br> Israel <br> United States <br> Italy | $\begin{array}{ll} 77 & (2.8) \\ 75 & (1.9) \\ 67 & (2.4) \\ 65 & (3.2) \\ 52 & (2.4) \end{array}$ | 494 (5.5) <br> 586 (4.4) <br> 472 (4.3) <br> 515 (4.5) <br> 486 (4.6) | $\begin{array}{ll} 19 & (2.2) \\ 25 & (1.8) \\ 31 & (2.3) \\ 31 & (2.9) \\ 37 & (2.3) \end{array}$ | 482 (9.9) <br> 577 (6.3) <br> 468 (8.4) <br> 489 (6.4) <br> 474 (5.7) | $\begin{array}{r} 4(1.7) \\ 0(0.2) \\ 2(0.7) \\ 5(1.2) \\ 11(1.8) \end{array}$ | $\begin{gathered} 537(28.2) \\ \sim \sim \\ \sim \sim \\ 476(10.8) \\ 483(12.0) \end{gathered}$ |
| number concepts (see reference exhibits R3.12R3.14). High level indicates the student reported using calculators in mathematics lessons almost always or pretty | South Africa Finland Slovak Republic Belgium (Flemish) Czech Republic | 51 (2.8) <br> 46 (3.0) <br> 41 (3.1) <br> 39 (2.7) <br> 35 (3.2) | 280 (9.9) <br> 520 (3.5) <br> 541 (5.8) <br> 571 (6.3) <br> 528 (7.1) | 40 (1.9) <br> 47 (2.9) <br> 55 (3.3) <br> 54 (2.7) <br> 60 (3.5) | $\begin{aligned} & 266(7.3) \\ & 523(3.4) \\ & 527(4.4) \\ & 562 \text { (6.9) } \\ & 517 \text { (4.7) } \end{aligned}$ | $\begin{array}{r} 10(2.0) \\ 6(1.9) \\ 3(1.7) \\ 7(2.6) \\ 5(2.0) \end{array}$ | $\begin{aligned} & 314 \text { (24.3) } \\ & 517 \text { (8.6) } \\ & 521 \text { (18.3) } \\ & 532 \text { (27.9) } \\ & 507 \text { (26.2) } \end{aligned}$ |
| often, and the teacher reported students use calculators at least once or twice a week for any of the tasks. Low level indicates the student reported using | Russian Federation <br> Hungary <br> Moldova <br> Morocco s <br> Chile | $\begin{array}{ll} 29 & (2.3) \\ 28 & (2.4) \\ 24 & (1.6) \\ 18 & (1.3) \\ 18 & (1.9) \end{array}$ | $\begin{aligned} & 522(9.3) \\ & 535(6.3) \\ & 476(5.4) \\ & 321(4.6) \\ & 404(8.9) \end{aligned}$ | $\begin{aligned} & 60(2.1) \\ & 53(3.1) \\ & 59(2.1) \\ & 59(1.7) \\ & 55(2.8) \end{aligned}$ | $\begin{aligned} & 528(6.3) \\ & 530(5.1) \\ & 468(5.0) \\ & 343(3.6) \\ & 395(5.2) \end{aligned}$ | $\begin{aligned} & 12(2.4) \\ & 19(2.8) \\ & 17(2.6) \\ & 22(1.9) \\ & 27(2.9) \end{aligned}$ | $\begin{aligned} & 539 \text { (13.3) } \\ & 527 \text { (8.6) } \\ & 467 \text { (10.2) } \\ & 350 \text { (6.8) } \\ & 389(7.3) \end{aligned}$ |
| calculators once in a while or never, and the teacher reported students use calculators never or hardly ever for all of the tasks. Medium level includes all other possible | Latvia (LSS) Cyprus <br> Macedonia, Rep. of Jordan Slovenia | 16 (2.2) <br> 14 (1.8) <br> 14 (1.8) <br> 10 (1.4) <br> 10 (1.6) | $\begin{aligned} & 514(8.6) \\ & 468(5.6) \\ & 465(8.6) \\ & 416(10.8) \\ & 518(8.6) \end{aligned}$ | 53 (3.6) <br> 56 (3.3) <br> 47 (2.6) <br> 62 (3.1) <br> 62 (3.4) | $\begin{aligned} & 502(4.8) \\ & 477(3.2) \\ & 455(5.2) \\ & 431(5.0) \\ & 530(3.8) \end{aligned}$ | 31 (3.4) <br> 30 (3.9) <br> 39 (3.5) <br> 28 (3.5) <br> 29 (3.9) | 505 (4.4) <br> 483 (4.3) <br> 448 (6.7) <br> 446 (6.7) <br> 538 (4.3) |
| combinations of responses. | Bulgaria Philippines Indonesia Tunisia Romania | $\begin{aligned} & 8(1.2) \\ & 6(1.1) \\ & 6(1.0) \\ & 4(0.7) \\ & 3(0.7) \end{aligned}$ | $\begin{aligned} & 501 \text { (14.0) } \\ & 321 \text { (16.1) } \\ & 415 \text { (13.7) } \\ & 424 \text { (8.2) } \\ & 477 \text { (17.5) } \end{aligned}$ | 68 (3.5) <br> 48 (2.9) <br> 60 (4.1) <br> 60 (3.5) <br> 39 (3.8) | 518 (4.9) <br> 342 (7.2) <br> 411 (7.0) <br> 444 (2.7) <br> 487 (9.3) | 24 (3.9) <br> 46 (3.4) <br> 34 (4.3) <br> 35 (3.6) <br> 58 (4.1) | $\begin{array}{ll} 503(19.4) \\ 352(8.1) \\ 391 & (9.2) \\ 456(4.4) \\ 470 & (5.6) \end{array}$ |
|  | Turkey | 3 (0.4) | 411 (11.5) | 42 (4.0) | 428 (4.9) | 55 (4.2) | 433 (5.6) |
|  | Iran, Islamic Rep. | 2 (0.5) | ~ ~ | 42 (3.9) | 425 (5.5) | 56 (4.2) | 422 (4.0) |
|  | Thailand | 2 (0.3) | ~ ~ | 39 (3.4) | 478 (7.8) | 59 (3.6) | 459 (6.2) |
|  | Chinese Taipei | 2 (0.4) | ~ ~ | 48 (4.0) | 576 (4.8) | 50 (4.2) | 598 (5.4) |
|  |  | 1 (0.3) | ~ ~ | 35 (4.1) | 522 (8.8) | 64 (4.2) | 518 (6.1) |
|  | Korea, Rep. of | 0 (0.3) | $\sim$ | 29 (3.3) | 587 (4.0) | 71 (3.3) | 587 (2.4) |
|  | Japan | 0 (0.1) | ~ ~ | 21 (3.2) | 573 (6.4) | 79 (3.2) | 579 (2.2) |
|  | Lithuania ${ }^{\text { }}$ | -- | - | -- | - - | -- | -- |
|  | International Avg. | 32 (0.3) | 481 (1.8) | 42 (0.5) | 484 (1.2) | 26 (0.5) | 481 (3.3) |

* The use of calculators on TIMSS was not allowed in 1995 or in 1999.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^52]

Exhibit 6.17 Trends in Index of Emphasis on Calculators in Mathematics Class (ECMC)*
TIMSS 1999
8
Mathematics

|  | HighECMCPercent of Students |  |  |  | Medium <br> ECMC <br> Percent of Students |  |  |  | Low <br> ECMC <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 <br> Differenc |  | 1995 | 1999 | 1995-1999 <br> Difference |  | 1995 | 1999 | 1995-1999 <br> Difference |  |
| Australia | 85 (2.5) | 84 (2.4) | -1 (3.5) | - | 11 (1.6) | 12 (1.8) | 1 (2.4) | - | 4 (1.5) | 4 (1.6) | 0 (2.2) | - |
| Belgium (Flemish) | 20 (3.2) | 39 (2.7) | 19 (4.2) | $\triangle$ | 43 (3.9) | 54 (2.7) | 11 (4.8) | - | 37 (4.7) | 7 (2.6) | -30 (5.4) | $\checkmark$ |
| Canada | 70 (2.6) | 79 (1.9) | 9 (3.3) | - | 26 (2.1) | 18 (1.7) | -7 (2.6) | - | 5 (2.6) | 3 (0.9) | -2 (2.7) | - |
| Cyprus | 23 (3.7) | 14 (1.8) | -9 (4.1) | - | 56 (3.9) | 56 (3.3) | -1 (5.1) | - | 21 (4.8) | 30 (3.9) | 9 (6.2) | - |
| Czech Republic | 59 (3.8) | 35 (3.2) | -24 (5.0) | $\nabla$ | 38 (3.7) | 60 (3.5) | 23 (5.1) | $\triangle$ | 3 (1.8) | 5 (2.0) | 1 (2.7) | - |
| England | 90 (1.3) | 80 (2.3) | -10 (2.7) | $\nabla$ | 10 (1.3) | 19 (2.2) | 9 (2.6) | $\triangle$ | 0 (0.0) | 1 (0.7) | 1 (0.7) | - |
| Hong Kong, SAR | 76 (4.2) | 75 (1.9) | -1 (4.6) | - | 18 (3.5) | 25 (1.8) | 7 (3.9) | $\bullet$ | 6 (2.4) | 0 (0.2) | -5 (2.4) | - |
| Hungary | 37 (3.2) | 28 (2.4) | -8 (4.0) | - | 44 (2.8) | 53 (3.1) | 9 (4.2) | - | 20 (3.5) | 19 (2.8) | -1 (4.5) | - |
| Iran, Islamic Rep. r | 1 (0.4) | 2 (0.5) | 1 (0.6) | - | 49 (4.7) | 42 (3.9) | -7 (6.1) | $\bullet$ | 50 (4.7) | 56 (4.2) | 6 (6.4) | - |
| Israel ${ }^{\dagger}$ | 63 (5.7) | 69 (2.8) | 6 (6.3) | - | 32 (5.1) | 30 (2.7) | -3 (5.8) | $\bullet$ | 5 (2.8) | 1 (0.8) | -4 (2.9) | - |
| Italy | 48 (3.9) | 53 (3.1) | 5 (5.0) | - | 42 (3.6) | 38 (2.8) | -5 (4.6) | $\bullet$ | 10 (2.4) | 10 (2.1) | 0 (3.2) | - |
| Japan | 0 (0.2) | 0 (0.1) | 0 (0.2) | - | 23 (3.2) | 21 (3.2) | -3 (4.5) | $\bullet$ | 76 (3.3) | 79 (3.2) | 3 (4.6) | - |
| Korea, Rep. of | 0 (0.1) | 0 (0.3) | 0 (0.3) | - | 25 (3.7) | 29 (3.3) | 3 (4.9) | - | 74 (3.7) | 71 (3.3) | -3 (5.0) | - |
| Latvia (LSS) | 49 (3.7) | 16 (2.2) | -33 (4.4) | $\checkmark$ | 42 (3.0) | 53 (3.6) | 11 (4.7) | $\bullet$ | 9 (2.5) | 31 (3.4) | 22 (4.2) | $\Delta$ |
| Lithuania | - - | - - |  |  |  |  | - - |  | - - | - - | - - |  |
| Netherlands | 89 (2.2) | 95 (1.1) | 6 (2.4) | $\bullet$ | 11 (2.2) | 5 (1.1) | -6 (2.4) | - | 0 (0.0) | 0 (0.0) | - - | - |
| New Zealand | 70 (2.8) | 77 (2.8) | 7 (3.9) | - | 23 (2.5) | 19 (2.2) | -4 (3.3) | - | 6 (1.9) | 4 (1.7) | -2 (2.6) | - |
| Romania | 5 (1.1) | 3 (0.7) | -2 (1.3) | - | 42 (3.3) | 39 (3.8) | -3 (5.0) | - | 54 (3.7) | 58 (4.1) | 5 (5.5) | - |
| Russian Federation | 50 (3.0) | 29 (2.3) | -21 (3.8) | $\nabla$ | 44 (2.8) | 60 (2.1) | 16 (3.5) | $\triangle$ | 7 (1.8) | 12 (2.4) | 5 (3.0) | - |
| Singapore | 79 (2.2) | 85 (1.6) | 6 (2.7) | - | 20 (2.1) | 15 (1.6) | -5 (2.6) | - | 1 (0.1) | 0 (0.0) | -1 (0.1) | $\checkmark$ |
| Slovak Republic | 68 (2.8) | 41 (3.1) | -26 (4.2) | $\nabla$ | 32 (2.8) | 55 (3.3) | 24 (4.3) | $\triangle$ | 1 (0.6) | 3 (1.7) | 3 (1.8) | - |
| Slovenia | 13 (2.1) | 10 (1.6) | -3 (2.6) | - | 55 (3.8) | 62 (3.4) | 7 (5.1) | $\bigcirc$ | 32 (4.4) | 29 (3.9) | -4 (5.8) | - |
| Thailand ${ }^{+}$r | 1 (0.2) | 2 (0.3) | 1 (0.4) | $\triangle$ | 33 (5.2) | 39 (3.4) | 6 (6.2) | - | 66 (5.2) | 59 (3.6) | -7 (6.3) | - |
| United States | 67 (3.4) | 65 (3.2) | -2 (4.7) | - | 27 (2.5) | 31 (2.9) | 4 (3.8) | $\bullet$ | 7 (1.9) | 5 (1.2) | -2 (2.2) | - |
| International Avg. § | 47 (0.6) | 43 (0.5) | -4 (0.8) | $\nabla$ | 33 (0.7) | 36 (0.6) | 3 (0.9) | $\triangle$ | 20 (0.6) | 20 (0.6) | 1 (0.8) | - |



Background data provided by students and teachers.

* The use of calculators on TIMSS was not allowed in 1995 or in 1999
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
An " $r$ " indicates teacher and/or student response data available for $70-84 \%$ of students.

|  | Almost Always or Pretty Often |  | Once in a While |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia | 6 (1.1) | 502 (15.1) | 23 (2.3) | 535 (6.0) | 71 (3.0) | 524 (5.7) |
| Belgium (Flemish) | 1 (0.4) | ~ ~ | 5 (1.2) | 536 (17.4) | 93 (1.3) | 562 (3.1) |
| Bulgaria | 3 (0.5) | 473 (15.4) | 4 (0.5) | 486 (12.3) | 93 (0.8) | 517 (5.9) |
| Canada | 8 (0.7) | 507 (7.1) | 25 (1.5) | 534 (3.8) | 67 (1.6) | 534 (2.5) |
| Chile | 8 (0.9) | 362 (12.1) | 11 (0.9) | 388 (7.7) | 81 (1.6) | 399 (4.5) |
| Chinese Taipei | 13 (0.6) | 548 (7.5) | 21 (0.6) | 564 (5.2) | 66 (0.9) | 601 (3.8) |
| Cyprus | 6 (0.4) | 422 (6.0) | 13 (0.7) | 459 (5.3) | 81 (0.8) | 485 (2.2) |
| Czech Republic | 2 (0.7) | ~ | 14 (2.4) | 526 (8.4) | 84 (2.6) | 520 (3.8) |
| England | 11 (1.7) | 466 (10.4) | 43 (2.2) | 512 (5.1) | 46 (2.7) | 492 (5.2) |
| Finland | 3 (0.9) | 487 (10.8) | 21 (2.2) | 524 (4.4) | 76 (2.7) | 521 (3.1) |
| Hong Kong, SAR | 8 (0.5) | 561 (9.5) | 18 (0.8) | 577 (6.2) | 75 (1.1) | 587 (4.1) |
| Hungary | 3 (0.5) | 481 (18.9) | 6 (1.0) | 501 (11.3) | 92 (1.2) | 536 (3.6) |
| Indonesia | 1 (0.3) | ~ ~ | 4 (0.4) | 389 (16.2) | 95 (0.5) | 407 (4.6) |
| Iran, Islamic Rep. | 0 (0.2) | ~ ~ | 4 (0.4) | 413 (10.7) | 96 (0.4) | 426 (3.3) |
| Israel | 14 (1.0) | 429 (9.3) | 19 (1.5) | 470 (8.2) | 67 (2.2) | 479 (4.2) |
| Italy | 11 (1.3) | 464 (7.4) | 17 (1.6) | 489 (5.5) | 72 (2.3) | 482 (4.0) |
| Japan | 2 (0.5) | $\sim \sim$ | 21 (2.3) | 576 (3.7) | 76 (2.7) | 581 (2.0) |
| Jordan r | 13 (1.2) | 377 (5.9) | 12 (0.8) | 406 (7.3) | 75 (1.6) | 454 (4.2) |
| Korea, Rep. of | 3 (0.3) | 567 (7.9) | 13 (0.7) | 596 (3.9) | 83 (0.8) | 587 (2.2) |
| Latvia (LSS) | 2 (0.3) | ~ ~ | 3 (0.6) | 475 (15.3) | 95 (0.6) | 507 (3.4) |
| Lithuania ${ }^{\ddagger}$ |  |  |  |  |  | -- |
| Macedonia, Rep. of | 4 (0.6) | 395 (12.8) | 8 (0.5) | 420 (8.8) | 88 (0.8) | 462 (3.7) |
| Malaysia | 1 (0.2) | ~ ~ | 6 (0.4) | 524 (8.2) | 93 (0.4) | 520 (4.3) |
| Moldova | 11 (0.9) | 434 (7.3) | 16 (1.2) | 461 (5.9) | 73 (1.7) | 480 (4.4) |
| Morocco s | 6 (0.8) | 313 (15.8) | 10 (0.8) | 336 (11.9) | 84 (1.2) | 350 (4.0) |
| Netherlands | 1 (0.2) | ~ ~ | 19 (3.2) | 543 (9.6) | 80 (3.2) | 541 (8.2) |
| New Zealand | 6 (0.7) | 426 (9.4) | 21 (2.2) | 517 (8.8) | 73 (2.4) | 491 (5.5) |
| Philippines | 8 (1.0) | 294 (9.5) | 12 (0.7) | 319 (11.3) | 80 (1.3) | 362 (5.8) |
| Romania | 1 (0.3) | ~ ~ | 5 (0.4) | 447 (13.0) | 93 (0.5) | 481 (5.4) |
| Russian Federation | 1 (0.2) | ~ | 3 (0.4) | 513 (11.1) | 97 (0.4) | 530 (5.7) |
| Singapore | 11 (0.8) | 590 (11.0) | 43 (2.5) | 625 (6.8) | 46 (2.7) | 589 (6.1) |
| Slovak Republic | 1 (0.2) | ~ ~ | 4 (0.9) | 536 (10.2) | 95 (1.0) | 535 (3.9) |
| Slovenia | 5 (0.6) | 473 (9.9) | 15 (1.2) | 516 (6.5) | 81 (1.4) | 537 (2.5) |
| South Africa | -- | -- | -- | -- | -- | -- |
| Thailand | 5 (0.6) | 431 (12.8) | 10 (0.6) | 471 (7.4) | 85 (1.0) | 470 (5.0) |
| Tunisia | 1 (0.2) | ~ ~ | 9 (0.5) | 440 (5.3) | 90 (0.6) | 451 (2.4) |
| Turkey | 2 (0.2) | ~ ~ | 5 (0.5) | 415 (11.2) | 93 (0.6) | 436 (4.3) |
| United States | 12 (1.1) | 463 (7.3) | 27 (2.0) | 520 (5.2) | 61 (2.7) | 506 (4.0) |
| International Avg. | 5 (0.1) | 455 (2.8) | 14 (0.2) | 488 (1.5) | 80 (0.3) | 498 (0.7) |

[^53]A dash (-) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement.
An " $r$ " indicates a $70-84 \%$ student response rate. An "s" indicates a $50-69 \%$ student response rate.

|  | Almost Always or Pretty Often |  |  | Once in a While |  |  | Never |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 | 1995-1999 <br> Difference |  | Percent of Students 1999 | 1995-1999 <br> Difference |  | Percent of Students 1999 | 1995-1999 <br> Difference |  |
| Australia | 6 (1.1) | 1 (1.4) | - | 23 (2.3) | 5 (2.9) | - | 71 (3.0) | -6 (3.6) | 。 |
| Belgium (Flemish) r | 1 (0.4) | 0 (0.8) | - | 5 (1.2) | 1 (1.5) | - | 93 (1.3) | -1 (1.7) | - |
| Canada | 8 (0.7) | 4 (0.8) | - | 25 (1.5) | 12 (1.9) | $\triangle$ | 67 (1.6) | -15 (2.2) | $\nabla$ |
| Cyprus | 6 (0.4) | -5 (0.9) | $\checkmark$ | 13 (0.7) | -3 (1.1) | $\bigcirc$ | 81 (0.8) | 8 (1.2) | $\triangle$ |
| Czech Republic s | 2 (0.7) | -2 (1.9) | - | 14 (2.4) | 6 (3.1) | $\bullet$ | 84 (2.6) | -5 (3.9) | - |
| England | 11 (1.7) | 2 (2.0) | - | 43 (2.2) | -3 (3.2) | - | 46 (2.7) | 2 (3.8) | - - |
| Hong Kong, SAR | 8 (0.5) | 4 (0.7) | - | 18 (0.8) | 11 (0.9) | - | 75 (1.1) | -16 (1.3) | - ${ }^{\circ}$ |
| Hungary | 3 (0.5) | 0 (0.6) | - | 6 (1.0) | 0 (1.3) | $\bullet$ | 92 (1.2) | -1 (1.4) | - ${ }_{\circ}^{\circ}$ |
| Iran, Islamic Rep. r | 1 (0.3) | -4 (0.6) | V | 4 (0.3) | 0 (0.5) | - | 96 (0.5) | 3 (1.0) | - |
| Israel ${ }^{\dagger}$ | 11 (1.0) | 0 (3.1) | - | 19 (1.7) | 6 (3.1) | - | 70 (2.4) | -6 (5.1) | $\sum$ |
| Italy | 11 (1.6) | 1 (1.9) | - | 15 (1.6) | 1 (2.2) | - | 74 (2.2) | -2 (3.1) | > |
| Japan s | 2 (0.5) | -2 (1.3) | - | 21 (2.3) | 2 (3.5) | - | 76 (2.7) | 0 (4.2) | - 出 |
| Korea, Rep. of | 3 (0.3) | 2 (0.4) | - | 13 (0.7) | 8 (0.8) | - | 83 (0.8) | -10 (1.0) | - |
| Latvia (LSS) s | 2 (0.3) | -2 (0.5) | $\checkmark$ | 3 (0.6) | -2 (1.1) | $\bullet$ | 95 (0.6) | 4 (1.3) | $\sim$ |
| Lithuania | - - | - - |  | - - | - - |  | - - | - - | $\stackrel{C}{0}$ |
| Netherlands | 1 (0.2) | -1 (0.4) | $\bullet$ | 19 (3.2) | 1 (4.6) | - | 80 (3.2) | -1 (4.7) | - |
| New Zealand | 6 (0.7) | 2 (0.9) | - | 21 (2.2) | 4 (3.1) | - | 73 (2.4) | -5 (3.5) | - |
| Romania | 1 (0.3) | -12 (0.9) | $\nabla$ | 5 (0.4) | -3 (0.8) | $\nabla$ | 93 (0.5) | 15 (1.3) | - $\sum^{\text {N }}$ |
| Russian Federation r | 1 (0.2) | -1 (0.4) | $\nabla$ | 3 (0.4) | -2 (0.7) | $\bullet$ | 97 (0.4) | 3 (0.9) | $\triangle$ |
| Singapore | 11 (0.8) | 9 (1.0) | - | 43 (2.5) | 35 (2.8) | $\triangle$ | 46 (2.7) | -44 (3.1) | , |
| Slovak Republic r | 1 (0.2) | 0 (0.3) | - | 4 (0.9) | -1 (1.3) | $\bullet$ | 95 (1.0) | 1 (1.4) | $\stackrel{\text { E }}{ }$ |
| Slovenia | 5 (0.6) | 1 (0.7) | - | 15 (1.2) | 7 (1.3) | - | 81 (1.4) | -9 (1.6) | - 믈 |
| Thailand ${ }^{\dagger}$ | 5 (0.6) | 2 (0.8) | - | 10 (0.6) | 5 (0.9) | $\triangle$ | 85 (1.0) | -6 (1.4) | - |
| United States | 12 (1.1) | 1 (1.8) | - | 27 (2.0) | 6 (2.7) | - | 61 (2.7) | -8 (3.7) | - |
| International Avg. § | 5 (0.2) | 0 (0.2) | - | 16 (0.4) | 4 (0.5) | $\triangle$ | 79 (0.4) | -4 (0.6) | - |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by students.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates a $50-69 \%$ student response rate, based on the lower response rate in either 1995 or 1999.
$\square$
$\square$


[^54]
## What Are the Roles of Homework and Assessment?

The amount of time students spend on homework assignments is an important consideration in examining their opportunity to learn mathe-


R3. 15
. matics. Exhibit 6.21 presents the index of teachers' emphasis on mathematics homework (емн). Students in the high category had teachers who reported giving relatively long homework assignments (more than 30 minutes) on a relatively frequent basis (at least once or twice a week). Those in the low category had teachers who gave short assignments (less than 30 minutes) relatively infrequently (less than once a week or never). The medium level includes all other possible combinations of responses. The detailed results from teachers' reports about the length and frequency of their homework assignments are found in the reference section in Exhibit R9. 15 .

The results show substantial variation across countries in the emphasis placed on homework. More than 70 percent of the students in Iran, Italy, Romania, Thailand, and Malaysia were in the high category. For the majority of countries, most students were in the medium category. Very few students were in the low category. One notable exception is Japan (34 percent in the low category), where students were more likely to spend extra time in tutoring and special schools than doing homework. ${ }^{3}$ There was little relationship between amount of homework assigned and students' performance. Again, lower-performing students may need more homework assignments for remedial reasons. The comparison between 1995 and 1999 data in Exhibit 6.22 shows little change in teachers' reports on the emphasis given to mathematics homework.

Since problem-solving activities will potentially be more beneficial if they can be extended to out-of-class-situations and stretched over a longer time, timss asked teachers how often they assigned homework based on projects and investigations. The data in Exhibit R3. 16 in the reference section show that most students ( 82 percent on average internationally) had teachers that never or rarely give such homework.

One theme in recommendations for educational reform is to make assessment a continuous process that relies on a variety of sources of data and methods, rather than a few high-stakes tests. Exhibit 6.23 shows teachers' reports about the weight given to various types of assessment, which varied greatly from country to country. Internationally, the least weight reportedly was given to external standardized tests, teacher-made objective tests, and projects or practical exercises. On average across countries, about two-fifths of the students (from 37 to 42 percent) had mathematics teachers who reported giving quite a lot or a great deal of weight to such

[^55]assessments. The most heavily weighted assessment was students' responses in class. On average internationally, this was given quite a lot or a great deal of weight for 77 percent of the students. Teachers reported that the next heaviest weight was given to teacher-made tests requiring explanations ( 67 percent of students on average internationally) and to observations of students ( 64 percent).

As shown in Exhibit R3. 17 in the reference section, eighth-grade students reported substantial variation in the frequency of testing in mathematics class. On average internationally, students were split about in half, with 57 percent reporting having a quiz or test in class almost always or pretty often and 43 percent reporting such testing only once in a while or never. At least three-fourths of the students reported frequent testing in Belgium (Flemish), Canada, Chile, Cyprus, the Russian Federation, Tunisia, and the United States. In contrast, at least threefourths of the students reported infrequent testing in Hungary, Korea, Latvia (LSs), and Turkey. There was a tendency for the most frequent testing to be associated with lower-achieving students. One could argue that these students can least afford time diverted from their instructional program. However, teachers may provide shorter lessons and followup quizzes for lower-achieving students to monitor their grasp of the subject matter more closely.

Exhibit 6.21 Index of Teachers' Emphasis on Mathematics Homework (EMH)

| Index of Teachers' <br> Emphasis on <br> Mathematics <br> Homework |  | High <br> EMH |  | Medium EMH |  | Low <br> EMH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on teachers' responses to two questions about how often they usually assign mathematics homework and how many minutes of mathematics homework they usually assign students (see reference exhibit R3.15). High level indicates the assignment of more than 30 minutes of homework at least once or twice a week. Low level indicates the assignment of less than 30 minutes of homework less than once a week or never assigning homework. Medium level includes all other possible combinations of responses. | Iran, Islamic Rep. <br> Italy <br> Romania <br> Thailand <br> Malaysia | $\begin{array}{ll} 90 & (2.7) \\ 80 & (3.0) \\ 76 & (3.9) \\ 73 & (3.7) \\ 72 & (3.8) \end{array}$ | 421 (3.5) 479 (4.9) 471 (6.7) 473 (6.8) 518 (6.0) | 10 (2.6) <br> 20 (2.9) <br> 24 (3.9) <br> 27 (3.7) <br> 27 (3.8) | $\begin{aligned} & 435(14.9) \\ & 479(7.9) \\ & 477(9.9) \\ & 451(6.9) \\ & 518(9.6) \end{aligned}$ | $\begin{array}{ll} 1 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.0) \end{array}$ |  |
|  | Singapore Indonesia <br> Russian Federation <br> Moldova Israel | 66 (4.6) <br> 61 (4.6) <br> 57 (4.6) <br> 57 (4.4) <br> 51 (3.4) | 613 (6.9) <br> 413 (7.3) <br> 527 (6.7) <br> 469 (6.1) <br> 474 (5.4) | 34 (4.6) <br> 39 (4.6) <br> 43 (4.6) <br> 43 (4.4) <br> 49 (3.3) | $\begin{aligned} & 587(10.6) \\ & 394(9.6) \\ & 525(7.8) \\ & 469(6.8) \\ & 459(5.7) \end{aligned}$ | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.4) \end{array}$ | ~~ |
|  | Turkey <br> Bulgaria <br> Chinese Taipei <br> Hong Kong, SAR <br> Macedonia, Rep. of | 50 (4.0) <br> 49 (5.4) <br> 48 (3.6) <br> 41 (4.3) <br> 39 (4.3) | 437 (5.5) <br> 524 (9.9) <br> 593 (6.4) <br> 580 (5.9) <br> 430 (6.8) | 46 (3.8) <br> 51 (5.4) <br> 50 (3.7) <br> 57 (4.4) <br> 60 (4.3) | $\begin{aligned} & 421(5.4) \\ & 496(7.4) \\ & 580(5.5) \\ & 585(5.8) \\ & 456(5.9) \end{aligned}$ | $\begin{array}{ll} 4 & (1.4) \\ 1 & (0.5) \\ 2 & (1.1) \\ 2 & (1.2) \\ 1 & (0.6) \end{array}$ | $401 \text { (10.2) }$ |
|  | Cyprus Jordan Tunisia England South Africa | 36 (4.4) <br> 32 (3.8) <br> 31 (3.9) <br> 28 (2.9) <br> 25 (3.1) | $\begin{aligned} & 477(3.3) \\ & 423(7.1) \\ & 458(4.6) \\ & 529(8.2) \\ & 261(9.9) \end{aligned}$ | $\begin{array}{ll} 64(4.4) \\ 68 & (3.8) \\ 66 & (4.0) \\ 71 & (3.0) \\ 75 & (3.1) \end{array}$ | 476 (2.6) 428 (5.2) 445 (2.9) 485 (4.7) 281 (7.8) | $\begin{aligned} & 0(0.0) \\ & 0(0.0) \\ & 3(1.5) \\ & 1(0.5) \\ & 0(0.0) \end{aligned}$ | $428 \text { (14.5) }$ |
|  | Lithuania ${ }^{\ddagger}$ <br> United States Korea, Rep. of Latvia (LSS) Chile | $\begin{aligned} & 25(3.7) \\ & 25(2.1) \\ & 25(3.4) \\ & 21(3.5) \\ & 20(3.4) \end{aligned}$ | 504 (9.4) <br> 528 (9.6) <br> 587 (4.2) <br> 514 (8.0) <br> 391 (9.4) | $\begin{array}{ll} 75 & (3.7) \\ 75 & (2.0) \\ 62 & (3.6) \\ 78 & (3.7) \\ 61 & (3.8) \end{array}$ | $\begin{aligned} & 474(4.9) \\ & 495(3.8) \\ & 586(2.9) \\ & 504(4.1) \\ & 390(5.1) \end{aligned}$ | $\begin{array}{r} 0(0.0) \\ 1(0.6) \\ 14(2.6) \\ 2(1.3) \\ 19(2.9) \end{array}$ | $\begin{gathered} 593(4.4) \\ \sim \sim \\ 402(10.8) \end{gathered}$ |
|  | Morocco <br> Hungary <br> Slovenia <br> Canada <br> Philippines | 19 (2.7) <br> 17 (3.1) <br> 17 (2.8) <br> 16 (2.3) <br> 14 (3.0) | $\begin{aligned} & 339(6.1) \\ & 535(9.5) \\ & 529(6.4) \\ & 527(6.2) \\ & 358(15.6) \end{aligned}$ | $\begin{array}{ll} 72 & (3.4) \\ 83 & (3.1) \\ 83 & (2.8) \\ 83 & (2.4) \\ 84 & (3.0) \end{array}$ | $\begin{aligned} & 337(2.8) \\ & 531(4.1) \\ & 530(3.1) \\ & 532(2.8) \\ & 340(6.8) \end{aligned}$ | $\begin{array}{r} 10(1.7) \\ 0(0.0) \\ 0(0.0) \\ 1(0.6) \\ 2(1.1) \end{array}$ | $335 \text { (7.6) }$ |
|  | Japan Netherlands Australia Belgium (Flemish) Finland | $\begin{array}{ll} 11 & (2.5) \\ 11 & (2.6) \\ 11 & (2.7) \\ 10 & (2.0) \\ 10 & (2.3) \end{array}$ | $\begin{aligned} & 578 \text { (3.9) } \\ & 555 \text { (14.6) } \\ & 531 \text { (13.5) } \\ & 582 \text { (8.6) } \\ & 521 \text { (10.8) } \end{aligned}$ | $\begin{array}{ll} 55 & (4.3) \\ 88 & (2.6) \\ 87 & (2.8) \\ 73 & (3.6) \\ 90 & (2.3) \end{array}$ | $\begin{aligned} & 580(2.8) \\ & 538(8.0) \\ & 526(5.4) \\ & 557(5.5) \\ & 521(2.8) \end{aligned}$ | $\begin{array}{r} 34(4.3) \\ 1(0.5) \\ 2(1.0) \\ 17(3.2) \\ 0(0.0) \end{array}$ | $\begin{aligned} 574 & (5.3) \\ \sim & \sim \\ \sim & \sim \\ 548 & \sim(15.0) \\ & \sim \end{aligned}$ |
|  | New Zealand Slovak Republic Czech Republic | $\begin{aligned} & 5(1.8) \\ & 3(1.7) \\ & 2(1.2) \end{aligned}$ | $\begin{gathered} 475(13.1) \\ 554 \text { (28.7) } \\ \sim \sim \end{gathered}$ | 92 (2.1) <br> 94 (2.5) <br> 85 (3.8) | $\begin{aligned} & 495(5.4) \\ & 532(3.9) \\ & 520(4.8) \end{aligned}$ | $\begin{array}{r} 2(1.1) \\ 3(1.8) \\ 13(3.6) \end{array}$ | $\begin{aligned} & 566 \text { (14.6) } \\ & 513 \text { (9.9) } \end{aligned}$ |
|  | International Avg. | 35 (0.6) | 491 (1.8) | 62 (0.6) | 485 (1.0) | 4 (0.2) | 484 (4.0) |

[^56]

Exhibit 6.22 Trends in Index of Teachers' Emphasis on Mathematics Homework (EMH)
TIMSS1999
8
Mathematics

|  | High <br> EMH <br> Percent of Students |  |  |  | Medium <br> EMH <br> Percent of Students |  |  |  | Low <br> EMH <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | 1995 | 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | 1995 | 1999 | 1995-1999 Difference |  |
| Australia | 8 (1.9) | 11 (2.7) | 3 (3.3) | - | 88 (2.5) | 87 (2.8) | -1 (3.8) | - | 5 (1.6) | 2 (1.0) | -2 (1.9) | 。 |
| Belgium (Flemish) | 14 (2.8) | 10 (2.0) | -3 (3.4) | $\bigcirc$ | 72 (4.1) | 73 (3.6) | 1 (5.4) | - | 15 (3.4) | 17 (3.2) | 2 (4.6) | - |
| Canada | 14 (3.2) | 16 (2.3) | 3 (4.0) | - | 84 (3.3) | 83 (2.4) | -1 (4.1) | $\bullet$ | 3 (1.2) | 1 (0.6) | -2 (1.4) | - |
| Cyprus | 41 (5.8) | 36 (4.4) | -5 (7.3) | $\bigcirc$ | 59 (5.8) | 64 (4.4) | 5 (7.3) | $\bigcirc$ | 0 (0.0) | 0 (0.0) | -- |  |
| Czech Republic | 1 (0.6) | 2 (1.2) | 1 (1.4) | - | 86 (4.1) | 85 (3.8) | -1 (5.6) | - | 13 (4.1) | 13 (3.6) | 0 (5.4) | - |
| England | 47 (3.5) | 28 (2.9) | -20 (4.5) | $\nabla$ | 50 (3.4) | 71 (3.0) | 21 (4.5) | $\triangle$ | 3 (1.0) | 1 (0.5) | -2 (1.1) | - |
| Hong Kong, SAR | 28 (4.8) | 41 (4.3) | 14 (6.5) | - | 68 (5.3) | 57 (4.4) | -10 (7.0) | - | 5 (3.0) | 2 (1.2) | -3 (3.2) | - |
| Hungary | 13 (2.8) | 17 (3.1) | 4 (4.1) | - | 86 (2.8) | 83 (3.1) | -3 (4.2) | - | 1 (0.1) | 0 (0.0) | -1 (0.1) | $\nabla$ |
| Iran, Islamic Rep. | 81 (3.5) | 90 (2.7) | 8 (4.4) | - | 18 (3.4) | 10 (2.6) | -8 (4.3) | - | 1 (0.6) | 1 (0.0) | 0 (0.6) | - |
| Israel ${ }^{\dagger}$ | 45 (8.3) | 52 (3.8) | 6 (9.1) | - | 53 (8.4) | 47 (3.8) | -6 (9.2) | $\bigcirc$ | 1 (0.3) | 1 (0.5) | 0 (0.6) | - |
| Italy | 76 (3.6) | 81 (3.5) | 6 (5.0) | - | 23 (3.6) | 18 (3.4) | -5 (5.0) | - | 1 (0.1) | 0 (0.0) | 0 (0.1) | V |
| Japan | 16 (3.4) | 11 (2.5) | -5 (4.2) | - | 57 (4.3) | 55 (4.3) | -2 (6.1) | $\bullet$ | 27 (3.7) | 34 (4.3) | 7 (5.7) | - |
| Korea, Rep. of | 38 (4.7) | 25 (3.4) | -14 (5.8) | $\bigcirc$ | 57 (4.8) | 62 (3.6) | 5 (6.0) | $\bullet$ | 5 (2.0) | 14 (2.6) | 9 (3.3) | - |
| Latvia (LSS) | 8 (2.6) | 21 (3.5) | 12 (4.4) | $\bigcirc$ | 92 (2.6) | 78 (3.7) | -14 (4.5) | $\nabla$ | 0 (0.0) | 2 (1.3) | 2 (1.3) | - |
| Lithuania | 19 (3.1) | 25 (3.7) | 6 (4.8) | - | 81 (3.1) | 75 (3.7) | -6 (4.8) | - | 0 (0.0) | 0 (0.0) | -- |  |
| Netherlands | 5 (2.4) | 11 (2.6) | 6 (3.5) | $\bigcirc$ | 93 (2.7) | 88 (2.6) | -4 (3.8) | - | 2 (1.4) | 1 (0.5) | -1 (1.5) | - |
| New Zealand | 6 (1.9) | 5 (1.8) | 0 (2.6) | $\bigcirc$ | 89 (2.4) | 92 (2.1) | 3 (3.3) | - | 5 (1.8) | 2 (1.1) | -3 (2.1) | - |
| Romania | 85 (2.9) | 76 (3.9) | -9 (4.9) | $\bigcirc$ | 15 (2.9) | 24 (3.9) | 9 (4.9) | - | 0 (0.0) | 0 (0.0) | -- |  |
| Russian Federation | 54 (4.1) | 57 (4.6) | 3 (6.1) | - | 46 (4.1) | 43 (4.6) | -3 (6.1) | - | 0 (0.0) | 0 (0.0) | - - |  |
| Singapore | 69 (4.6) | 66 (4.6) | -3 (6.4) | - | 30 (4.4) | 34 (4.6) | 4 (6.3) | $\bigcirc$ | 1 (0.9) | 0 (0.0) | -1 (0.9) | - |
| Slovak Republic | 4 (1.7) | 3 (1.7) | -1 (2.4) | - | 95 (1.9) | 94 (2.5) | -1 (3.1) | - | 1 (0.0) | 3 (1.8) | 2 (1.8) | - |
| Slovenia | 22 (3.9) | 17 (2.8) | -5 (4.8) | $\bigcirc$ | 78 (3.9) | 83 (2.8) | 5 (4.8) | $\bullet$ | 0 (0.0) | 0 (0.0) | - - | - |
| Thailand ${ }^{\dagger}$ | 55 (4.9) | 73 (3.7) | 18 (6.1) | $\bigcirc$ | 45 (4.9) | 27 (3.7) | -18 (6.1) | - | 0 (0.0) | 0 (0.0) | -- | - |
| United States | 18 (2.4) | 25 (2.1) | 6 (3.1) | - | 79 (2.4) | 75 (2.0) | -5 (3.2) | - | 3 (0.9) | 1 (0.6) | -2 (1.1) | - |
| International Avg. § | 30 (0.7) | 31 (0.7) | 0 (1.0) | - | 66 (0.8) | 65 (0.7) | -1 (1.1) | - | 4 (0.4) | 4 (0.3) | 0 (0.5) | - |



Background data provided by teachers.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999.
$\square$


|  | Percentage of Students by Type of Assessment |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | External Standardized Tests | Teacher-Made Tests Requiring Explanations | Teacher-Made Objective Tests | Homework Assignments | Projects or Practical Exercises | Observations of Students | Students' <br> Responses in Class |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 14(3.0) \\ 12 & (3.0) \\ 34 & (4.7) \\ 21 & (3.1) \\ 29 & (3.5) \end{array}$ | 37 (4.5) <br> 94 (1.4) <br> 83 (2.8) <br> 61 (3.0) <br> 79 (3.3) |  $32(4.0)$ <br>  $11(2.4)$ <br>  $31(5.6)$ <br> r $26(2.8)$ <br>  $62(3.6)$ |  $38(3.7)$ <br>  $23(3.0)$ <br>  $81(3.3)$ <br> $r$ $51(3.8)$ <br>  $55(4.0)$ |  $32(3.3)$ <br>  $12(2.1)$ <br>  $30(4.0)$ <br> $r$ $38(2.7)$ <br>  $45(3.9)$ |  | 40 (3.5) <br> 52 (4.4) <br> 99 (0.8) <br> 42 (3.4) <br> 87 (2.2) |
| Chinese Taipei Cyprus Czech Republic England Finland |  $36(4.0)$ <br>  $39(4.7)$ <br>  <br>  <br>  <br>  <br> 5$\quad 53(5.4)$ <br> $51(4.1)$  <br>  $21(3.8)$ | $r$$43(4.0)$ <br> $59(4.8)$ <br>  <br>  <br> 5 <br> $97(1.8)$ <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> $18(3.6)$ | $\begin{array}{rr}  & 76(3.4) \\ \text { r } & 37(4.7) \\ & 9(2.6) \\ \text { s } & 7(1.4) \\ & 20(3.3) \end{array}$ |  | $r$$17(3.4)$ <br> $66(4.0)$ <br>  <br>  <br> 5$23(5.2)$ <br>  <br> $41(3.4)$ <br>  <br>  <br>  <br> $52(4.1)$ | $\begin{array}{ll}  & 68(3.1) \\ \mathrm{r} & 99(0.9) \\ & 80(4.2) \\ \mathrm{s} & 78(2.9) \\ & 83(3.6) \end{array}$ | $\begin{array}{ll}  & 72(3.6) \\ \mathrm{r} & 99(1.0) \\ & 98(1.5) \\ \mathrm{s} & 78(2.7) \\ & 90(2.9) \end{array}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{ll} 17 & (3.2) \\ 44 & (4.1) \\ 50 & (4.8) \\ 76 & (3.8) \\ 10 & (2.0) \end{array}$ | $\begin{array}{ll} 52(4.2) \\ 66 & (4.1) \\ 81 & (3.2) \\ 79 & (3.4) \\ 78 & (3.3) \end{array}$ | $\begin{aligned} & 47(3.6) \\ & 17(3.1) \\ & 44(4.8) \\ & 46(4.3) \\ & 28(3.5) \end{aligned}$ | 44 (4.0) <br> 36 (3.9) <br> 65 (4.3) <br> 78 (3.2) <br> 53 (3.5) | $\begin{aligned} & 10(2.6) \\ & 62(3.8) \\ & 72(4.3) \\ & 20(2.8) \\ & 40(3.9) \end{aligned}$ | $\begin{array}{ll} 38 & (4.3) \\ 71 & (3.7) \\ 76 & (4.1) \\ 38 & (4.0) \\ 44 & (3.2) \end{array}$ | 44 (4.3) <br> 88 (2.9) <br> 81 (3.7) <br> 86 (3.1) <br> 59 (3.3) |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 22 & (3.2) \\ 15 & (2.9) \\ 30 & (4.0) \\ 37 & (3.8) \\ 80 & (3.8) \end{array}$ | $\begin{array}{ll} 92 & (2.2) \\ 55 & (4.4) \\ 78 & (3.8) \\ 48 & (3.7) \\ 81 & (4.1) \end{array}$ | $\begin{array}{ll} 63 & (3.8) \\ 25 & (3.9) \\ 32 & (4.2) \\ 45 & (3.7) \\ 50 & (4.6) \end{array}$ | 67 (3.6) <br> 47 (4.0) <br> 70 (3.7) <br> 32 (3.6) <br> 63 (4.6) | $\begin{array}{ll} 75 & (3.1) \\ 41 & (4.0) \\ 41 & (4.3) \\ 43 & (3.3) \\ 69 & (4.3) \end{array}$ | 96 (1.4) <br> 67 (4.1) <br> 82 (3.1) <br> 50 (4.1) <br> 79 (3.7) | 99 (0.6) <br> 65 (4.3) <br> 88 (2.6) <br> 61 (4.1) <br> 98 (1.2) |
| Lithuania ${ }^{\ddagger}$ Macedonia, Rep. of Malaysia Moldova Morocco | 35 (3.9) <br> 69 (4.3) <br> 18 (3.2) <br> 60 (4.6) <br> 30 (2.9) | 57 (4.3) <br> 63 (4.1) <br> 38 (4.1) <br> 95 (2.0) <br> 74 (3.1) | 14 (2.7) <br> 65 (4.2) <br> 66 (4.2) <br> 55 (4.3) <br> 42 (3.0) | 25 (3.4) <br> 85 (3.1) <br> 84 (3.2) <br> 84 (3.5) <br> 80 (2.7) | 18 (3.5) <br> 47 (4.2) <br> 32 (4.2) <br> 48 (4.5) <br> 78 (2.2) | $\begin{array}{ll} 27 & (3.7) \\ 98 & (1.5) \\ 76 & (3.7) \\ 85 & (3.0) \\ 78 & (2.5) \end{array}$ | $\begin{array}{r} 75(3.7) \\ 100(0.0) \\ 86(2.8) \\ 88(2.6) \\ 87(1.8) \end{array}$ |
| > Netherlands > New Zealand Philippines Romania Russian Federation | $\begin{gathered} 29(5.5) \\ 16(3.0) \\ 38(4.1) \\ 66(4.0) \\ -- \end{gathered}$ | $\begin{aligned} & 96(1.8) \\ & 59(4.2) \\ & 74(4.0) \\ & 80(3.4) \\ & 98(1.0) \end{aligned}$ | $\begin{array}{ll} 20 & (5.8) \\ 23 & (3.5) \\ 73 & (4.0) \\ 55 & (4.2) \\ 54 & (4.4) \end{array}$ | $\begin{array}{ll} 18(4.7) \\ 39 & (4.0) \\ 79 & (3.4) \\ 79 & (3.2) \\ 68 & (3.7) \end{array}$ | $\begin{array}{r} 8(2.6) \\ 29(3.6) \\ 72(4.4) \\ 35(4.3) \\ 59(3.8) \end{array}$ | $\begin{array}{ll} 28 & (4.7) \\ 55 & (4.5) \\ 77 & (3.4) \\ 86 & (2.6) \\ 91 & (2.2) \end{array}$ | $\begin{array}{ll} 27 & (5.4) \\ 55 & (4.6) \\ 95 & (1.9) \\ 98 & (1.2) \\ 86 & (2.5) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{ll} 36 & (4.2) \\ 79 & (4.2) \\ 41 & (4.8) \\ 39 & (4.3) \\ 28 & (4.0) \end{array}$ | $\begin{aligned} & 22(3.9) \\ & 89(3.1) \\ & 61(3.9) \\ & 55(4.1) \\ & 70(3.6) \end{aligned}$ | $\begin{array}{r} 5(2.0) \\ 56(5.5) \\ 14(2.7) \\ 49(4.7) \\ 72(3.7) \end{array}$ | 61 (4.5) <br> 29 (4.3) <br> 51 (4.3) <br> 74 (4.4) <br> 80 (3.5) | 37 (4.2) <br> 69 (4.9) <br> 32 (3.8) <br> 35 (4.1) <br> 43 (4.0) | 46 (4.6) <br> 83 (3.1) <br> 46 (4.2) <br> 58 (3.4) <br> 60 (3.9) | $\begin{array}{ll} 52 & (4.2) \\ 98 & (1.1) \\ 82 & (3.4) \\ 76 & (3.4) \\ 71 & (3.7) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 24 & (3.7) \\ 24 & (3.1) \\ 28 & (3.0) \end{array}$ | $\begin{aligned} & 78 \\ & 78 \\ & 50 \\ & 50 \end{aligned}(4.3)$ | $\begin{array}{ll} 64 & (4.1) \\ 35 & (4.4) \\ 28 & (3.5) \end{array}$ | $\begin{array}{ll} 76 & (3.8) \\ 58 & (3.4) \\ 56 & (4.3) \end{array}$ | $\begin{array}{ll} 62 & (4.1) \\ 31 & (3.7) \\ 33 & (3.5) \end{array}$ | $\begin{array}{ll} 74 & (4.0) \\ 51 & (4.3) \\ 40 & (3.2) \end{array}$ | $\begin{array}{ll} 89 & (2.8) \\ 96 & (1.5) \\ 41 & (3.6) \end{array}$ |
| International Avg. | 37 (0.6) | 67 (0.6) | 39 (0.6) | 60 (0.6) | 42 (0.6) | 64 (0.6) | 77 (0.5) |

[^57][^58]

## CHAPTER 7

## School Contexts for

 Learning and InstructionChapter 7 presents findings about the school contexts for learning and instruction in mathematics, including school characteristics, policies, and practices.

Information is presented about the extent of school resources in each country, including computers and Internet access. Data also are provided about the role of the school principal and issues related to school climate and environment, including attendance problems and school safety.


## What School Resources Are Available to Support Mathematics Learning?

Some school resources are specific to mathematics, but many are general resources that improve learning opportunities across the curriculum. All the available resources, however, can work together to support mathematics learning and instruction.

To measure the extent of school resources in each of the participating countries, timss created an index of availability of school resources for mathematics instruction (ASRMI). As described in Exhibit 7.1, the index is based on schools' average response to five questions about shortages that affect general capacity to provide instruction and five questions about shortages that affect mathematics instruction in particular. Students were placed in the high category if principals reported that shortages, both general and for mathematics in particular, had no or little effect on instructional capacity. The medium level indicates that one type of shortage affects instruction some or a lot, and the low level that both shortages affect it some or a lot.

Students in schools that reported being well resourced generally had higher average mathematics achievement than those in schools where across-the-board shortages affect instructional capacity some or a lot. For example, in Australia, 33 percent of the students were in the high category with average mathematics achievement of 538 , compared with eight percent in the low category with an average of 509 . In very few countries Belgium (Flemish), Singapore, and the Czech Republic -were the majority of students in the high category. On average internationally, only 19 percent of the students were at the high level, and 63 percent at the medium level. It is interesting to note that in high-performing Hong Kong, Chinese Taipei, and Korea, fewer than one-fourth of the students were in schools with a high level of resources.

Exhibit R4. 1 in the reference section shows the results for each of the types of facilities and materials summarized in the general capacity part of the index. There was substantial variation across countries, but internationally on average, nearly half the students were in schools where instruction was negatively affected by shortages or inadequacies in instructional materials, budget for supplies, school buildings, and instructional space.

Exhibit R4.2, also in the reference section, shows the results for each of the types of equipment and materials summarized in the mathematics instructional capacity part of the index. More than half of the students, on average internationally, were in schools where shortages or inadequa-
cies in computers and computer software affected the capacity to provide mathematics instruction. Half the students were in schools where the lack of audio-visual resources affected instruction, and 46 percent were in schools needing more library materials relevant to mathematics instruction. Only about one-third of the students, however, were in schools needing more calculators.

R4.3-R4.4
Exhibits $\mathrm{R}_{4} \cdot 3$ and $\mathrm{R}_{4} \cdot 4$ in the reference section present more data on access to computers and the Internet for instructional purposes. Countries seem to have computers either in nearly all of their schools or in only a fraction of them. Internationally on average, 6o percent of the students were in schools with a student to computer ratio of less than 15 to one, and 25 percent were in schools having no computers. Forty-one percent of the students, on average across countries, attended schools with access to the World Wide Web, and another 29 percent were in schools planning to have access to the Internet by 2001.
$7.2 \square$
Exhibit 7.2 presents trends in the index of availability of school resources for mathematics instruction. There was little or no change between 1995 and 1999 in the percentages of students in schools with low and medium levels of resources. There was a small but significant increase, internationally on average, in the percentage of students in the high category. The Czech Republic, Hungary, Italy, New Zealand, and the United States had increased percentages of students at the high level of the index.


Exhibits 7.1 and 7.2 Overleaf


[^59] some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An "r" indicates school response data available for $70-84 \%$ of students.


## Exhibit 7.2 Trends in Index of Availability of School Resources for Mathematics Instruction (ASRMI)

|  | High <br> ASRMI <br> Percent of Students |  |  |  | Medium <br> ASRMI <br> Percent of Students |  |  |  | Low <br> ASRMI <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 <br> Difference |  | 1995 | 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | 1995 | 1999 | 1995-1999 <br> Difference |  |
| Australia r | 42 (5.0) | 33 (4.1) | -9 (6.5) | - | 52 (5.2) | 60 (4.1) | 8 (6.6) | - | 6 (2.4) | 8 (1.9) | 1 (3.1) | - |
| Belgium (Flemish) | 48 (5.3) | 54 (4.6) | 6 (7.1) | - | 52 (5.3) | 46 (4.6) | -6 (7.1) | - | 0 (0.0) | 0 (0.0) | - - |  |
| Canada | 25 (3.2) | 31 (2.5) | 6 (4.0) | - | 73 (3.1) | 64 (2.7) | -9 (4.1) | $\bullet$ | 2 (0.8) | 5 (1.1) | 3 (1.4) | - |
| Cyprus r | 31 (0.5) | 15 (0.2) | -16 (0.5) | $\nabla$ | 63 (0.5) | 85 (0.2) | 22 (0.6) | $\triangle$ | 6 (0.4) | 0 (0.0) | -6 (0.4) | V |
| Czech Republic | 30 (5.0) | 50 (3.6) | 20 (6.2) | $\triangle$ | 70 (4.9) | 49 (3.9) | -21 (6.2) | $\checkmark$ | 0 (0.4) | 2 (1.5) | 1 (1.5) | - |
| England | 25 (4.7) | 26 (4.2) | 1 (6.3) | - | 73 (4.9) | 72 (4.4) | -2 (6.6) | - | 2 (1.5) | 2 (1.5) | 0 (2.1) | - |
| Hong Kong, SAR | 23 (5.4) | 22 (4.1) | 0 (6.8) | - | 72 (5.6) | 67 (4.4) | -5 (7.1) | - | 5 (2.6) | 10 (2.7) | 5 (3.7) | - |
| Hungary | 19 (3.2) | 35 (4.0) | 16 (5.1) | $\triangle$ | 79 (3.3) | 59 (4.1) | -20 (5.2) | $\nabla$ | 2 (1.2) | 6 (2.2) | 4 (2.5) | - |
| Iran, Islamic Rep. | 1 (0.9) | 6 (1.8) | 5 (2.0) | - | 67 (4.7) | 71 (4.1) | 4 (6.2) | - | 32 (4.7) | 23 (3.7) | -9 (5.9) | - |
| Israel ${ }^{+}$s | 17 (6.1) | 38 (5.0) | 21 (7.9) | - | 76 (7.2) | 60 (5.0) | -17 (8.8) | - | 7 (4.4) | 2 (1.6) | -4 (4.7) | - |
| Italy | 9 (2.4) | 27 (4.0) | 18 (4.7) | $\triangle$ | 73 (4.0) | 67 (4.6) | -6 (6.1) | - | 18 (3.3) | 6 (2.3) | -12 (4.0) | - |
| Japan | 28 (3.5) | 36 (4.3) | 9 (5.6) | $\bullet$ | 68 (3.9) | 61 (4.2) | -7 (5.7) | - | 4 (1.9) | 3 (1.5) | -2 (2.4) | - |
| Korea, Rep. of | 4 (1.6) | 4 (1.6) | 0 (2.3) | - | 82 (3.2) | 81 (3.5) | -2 (4.7) | - | 14 (2.9) | 16 (3.1) | 2 (4.2) | - |
| Latvia (LSS) r | 2 (0.9) | 2 (1.4) | 1 (1.6) | - | 51 (4.3) | 58 (4.2) | 7 (6.0) | - | 47 (4.4) | 40 (4.0) | -7 (5.9) | - |
| Lithuania | 2 (1.1) | 8 (2.2) | 6 (2.5) | - | 79 (3.5) | 67 (3.6) | -12 (5.0) | $\bullet$ | 19 (3.3) | 25 (3.5) | 6 (4.8) | - |
| Netherlands | 46 (7.1) | 40 (6.2) | -6 (9.4) | - | 53 (7.0) | 60 (6.2) | 7 (9.3) | - | 1 (0.1) | 0 (0.0) | -1 (0.1) | V |
| New Zealand | 15 (2.9) | 34 (4.3) | 19 (5.2) | $\triangle$ | 79 (3.6) | 62 (4.3) | -17 (5.6) | $\nabla$ | 6 (2.1) | 4 (1.7) | -2 (2.7) | - |
| Romania | 4 (1.4) | 6 (2.4) | 2 (2.8) | - | 73 (3.8) | 67 (3.7) | -5 (5.3) | - | 23 (3.7) | 26 (3.5) | 3 (5.1) | - |
| Russian Federation | 1 (0.0) | 1 (0.9) | 1 (0.9) | - | 46 (4.5) | 47 (4.0) | 0 (6.1) | - | 53 (4.6) | 52 (3.9) | -1 (6.0) | - |
| Singapore | 55 (4.6) | 50 (4.0) | -5 (6.1) | - | 43 (4.4) | 46 (4.1) | 4 (6.0) | - | 2 (1.2) | 4 (1.4) | 2 (1.8) | - |
| Slovak Republic | 13 (2.7) | 8 (2.4) | -5 (3.7) | - | 84 (2.7) | 85 (2.9) | 1 (4.0) | $\bullet$ | 3 (1.4) | 7 (2.4) | 4 (2.8) | - |
| Slovenia $r$ | 12 (3.3) | 15 (2.8) | 4 (4.3) | - | 80 (4.1) | 72 (3.7) | -9 (5.5) | - | 8 (2.9) | 13 (2.4) | 5 (3.7) | - |
| Thailand ${ }^{\dagger}$ | 0 (0.0) | 1 (0.8) | 1 (0.8) | - | 58 (5.2) | 49 (4.0) | -9 (6.6) | $\bullet$ | 41 (5.2) | 50 (4.0) | 8 (6.6) | - |
| United States r | 18 (3.2) | 37 (3.8) | 19 (5.0) | $\triangle$ | 75 (3.6) | 59 (3.6) | -16 (5.1) | $\nabla$ | 6 (1.4) | 4 (1.5) | -3 (2.1) | - |
| International Avg. ${ }^{\text {s }}$ | 21 (0.8) | 25 (0.7) | 4 (1.1) | $\triangle$ | 68 (0.9) | 64 (0.9) | -4 (1.2) | - | 12 (0.5) | 12 (0.5) | 0 (0.7) | - |



Background data provided by schools.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An "r" indicates school response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " " " indicates school response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999.


## What Is the Role of the School Principal?

To better understand the roles and responsibilities of schools across countries, TIMss asked school principals how much time per month they spend on various school-related activities. More specifically, they were asked how much time they spend on instructional leadership activities, including discussing educational objectives with teachers, initiating curriculum revisions and planning, training teachers, and engaging in professional development activities. They were asked how much time they spend per month talking with parents, counseling and disciplining students, and responding to requests from local, regional, or national education officials. They also responded to questions about how much time they spend carrying out administrative duties, including hiring teachers, representing the school in the community and at official meetings, and doing internal tasks (e.g., regulations, school budget, and timetable). Finally, they were asked how much time they spend teaching. The results presented in Exhibit 7.3 show that principals reported spending, internationally on average, $5^{1}$ hours per month on administrative duties, 35 hours per month communicating with various constituents, 33 hours per month on instructional leadership activities, and 16 hours per month teaching. ${ }^{1}$

Countries where principals reported spending an average of at least 75 hours per month on administrative duties included Australia, Chinese Taipei, Hong Kong, and New Zealand. Principals reported spending at least 50 hours per month communicating with various groups in Australia, Canada, and the United States. Principals in 10 countries reported spending at least 40 hours per month on instructional leadership activities, and in eight countries they reported that teaching duties (including preparation) occupied at least 30 hours per month.

It is noteworthy that a number of countries, such as Australia, Canada, Chinese Taipei, Hong Kong, New Zealand, Singapore, Thailand, and the United States, have similar patterns in principals' use of time. For example, unlike in most European countries, principals in these countries spend relatively little time teaching, and most of it on administrative duties, communicating with constituents, and engaging in instructional leadership activities.

[^60]| AustraliaBelgium (Flemish)BulgariaCanadaChile | Average Total Hours Per Month Spent on Activities ${ }^{1}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Instructional Leadership Activities ${ }^{2}$ |  | Communicating with Students, Parents, and Education Officials ${ }^{3}$ |  | ministrative Duties ${ }^{4}$ |  | Teaching (including preparation) |
|  | $r$ | $\begin{array}{ll} 33 & (1.9) \\ 29 & (2.3) \\ 38 & (2.5) \\ 25 & (1.1) \\ 31 & (1.4) \end{array}$ |  | 50 (2.7) <br> 27 (2.1) <br> 39 (1.9) <br> 54 (1.4) <br> 36 (1.5) |  | $\begin{aligned} & 75(3.2) \\ & 56(2.5) \\ & 47(2.3) \\ & 54(2.1) \\ & 53(3.0) \end{aligned}$ |  | $\begin{array}{r} 3(0.7) \\ 0(0.1) \\ 21(1.0) \\ 5(0.9) \\ 5(0.6) \end{array}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $r$ | $\begin{gathered} 24(1.4) \\ 18(0.1) \\ 32(1.9) \\ -- \\ 27(1.5) \end{gathered}$ |  | $\begin{array}{cc} 34 & (1.7) \\ 46 & (0.1) \\ 33 & (1.8) \\ -- \\ 29 & (1.2) \end{array}$ |  | $\begin{array}{cc} 86 & (4.1) \\ 33 & (0.1) \\ 44(2.4) \\ -- \\ 66(2.7) \end{array}$ |  | $\begin{gathered} 4(0.6) \\ 18(0.0) \\ 36(1.8) \\ -- \\ 24(1.6) \end{gathered}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | r | 43 (3.2) <br> 47 (2.1) <br> 15 (1.8) <br> 28 (1.6) <br> 43 (2.4) |  | $\begin{array}{ll} 29 & (1.8) \\ 28 & (1.2) \\ 20 & (1.6) \\ 42 & (2.4) \\ 38 & (2.1) \end{array}$ |  | $\begin{array}{ll} 75 & (4.2) \\ 46 & (2.1) \\ 40 & (2.9) \\ 35 & (3.0) \\ 43 & (2.5) \end{array}$ |  | $\begin{array}{r} 3(0.6) \\ 35(1.6) \\ 16(1.8) \\ 4(0.6) \\ 24(1.8) \end{array}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | r | 36 (1.4) <br> 33 (2.0) <br> 31 (1.8) <br> 30 (2.1) <br> 33 (1.9) | r | $\begin{array}{ll} 44 & (2.1) \\ 19 & (1.3) \\ 43 & (2.1) \\ 22 & (1.6) \\ 26 & (1.9) \end{array}$ | r | 45 (1.7) <br> 69 (3.6) <br> 27 (1.8) <br> 46 (3.6) <br> 58 (3.8) | $r$ | $\begin{aligned} & -- \\ & 1(0.8) \\ & 9(0.9) \\ & 3(0.5) \\ & 41(2.7) \end{aligned}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of Malaysia <br> Moldova <br> Morocco | $r$ | $\begin{array}{r} 40(1.7) \\ 40(2.2) \\ 24(1.5) \\ 45(1.9) \\ 9(0.8) \end{array}$ | r | $\begin{array}{ll} 34 & (1.4) \\ 34 & (1.7) \\ 31 & (1.7) \\ 32 & (1.5) \\ 24 & (1.7) \end{array}$ | r | $\begin{array}{ll} 50 & (2.4) \\ 32 & (1.9) \\ 61 & (3.1) \\ 55 & (2.7) \\ 29 & (4.9) \end{array}$ | $r$ | $\begin{array}{rr} 33 & (1.4) \\ 16 & (1.9) \\ 22 & (2.1) \\ 41 & (1.7) \\ 0 & (0.0) \end{array}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $r$ $r$ | $\begin{array}{ll} 42 & (4.0) \\ 39 & (2.0) \\ 30 & (2.0) \\ 31 & (1.6) \\ 44 & (1.9) \end{array}$ | r | $\begin{array}{ll} 20 & (2.0) \\ 45 & (1.9) \\ 31 & (1.8) \\ 32 & (1.5) \\ 33 & (1.7) \end{array}$ | r | 49 (5.6) <br> 83 (3.6) <br> 42 (3.4) <br> 40 (2.3) <br> 65 (3.1) | $r$ | $\begin{array}{r} 7(1.7) \\ 5(0.8) \\ 10(1.8) \\ 45(2.3) \\ 46(2.1) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand |  | $\begin{array}{ll} 45 & (2.2) \\ 36 & (1.8) \\ 43 & (2.2) \\ 19 & (1.2) \\ 37 & (2.2) \end{array}$ |  | $\begin{array}{ll} 46 & (1.9) \\ 31 & (1.5) \\ 29 & (1.2) \\ 34 & (2.3) \\ 32 & (1.7) \end{array}$ |  | 56 (3.1) <br> 34 (2.0) <br> 41 (2.2) <br> 43 (3.4) <br> 68 (3.8) | $r$ | $\begin{array}{r} 3(0.6) \\ 32(1.2) \\ 11(1.0) \\ 22(2.6) \\ 6(1.0) \end{array}$ |
| Tunisia <br> Turkey <br> United States |  | $\begin{aligned} & 28(2.0) \\ & 25(1.7) \\ & 34(1.9) \end{aligned}$ |  | $\begin{array}{ll} 47 & (2.6) \\ 43 & (2.0) \\ 52 & (2.4) \end{array}$ |  | $\begin{array}{ll} 55 & (2.6) \\ 46 & (2.9) \\ 56 & (3.2) \end{array}$ | $r$ | $\begin{array}{r} 17(1.9) \\ 3(0.6) \end{array}$ |
| International Avg. |  | 33 (0.3) |  | 35 (0.3) |  | 51 (0.5) |  | 16 (0.2) |

## Background data provided by schools.

1 Total hours reported for activities in each category averaged across students. Activites are not necessarily exclusive; principals may have reported engaging in more than one activity at the same time.
2 Includes discussing educational objectives with teachers; initiating curriculum revision and/or planning; training teachers; and professional development activities.
3 Includes talking with parents, counseling and disciplining of students and responding to requests from local, regional, or national education officials.

4 Includes hiring teachers; representing the school in the community; representing the school at official meetings; internal administrative tasks (e.g., regulations, school budget, timetable).
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates data are not available.
An " $r$ " indicates school response data available for $70-84 \%$ of students.

## What Are the Schools' Expectations of Parents?

The schools' expectations for parental involvement are shown in Exhibit $7 \cdot 4$. Clearly schools expect help from parents. On average across countries, 85 percent of the students attended schools expecting parents to ensure that their children complete their homework, and 79 percent attended schools expecting parents to volunteer for school projects or field trips. About half the students were in schools expecting parents to help raise funds and to serve on committees. Only 28 percent were in schools expecting parents to help as aides in the classroom.

At the country level, in all countries with the exception of Japan, at least 60 percent of students were in schools where parents were expected to ensure that their children complete their homework. Twenty countries had at least go percent of their students in such schools, and in Canada and the United States almost all students ( 99 percent) were in such schools. The expectation that parents would serve as classroom aides was especially high in Iran, and low in Finland, Indonesia, Japan, and New Zealand. All Malaysian and Lithuanian students were in schools where parents were expected to volunteer for school projects or field trips. Raising funds was an expectation of parents for at least 75 percent of the students in Cyprus, Morocco, the Slovak Republic, South Africa, and Turkey. At least three-quarters of students were in schools where parents were expected to serve on committees in Australia, Iran, Latvia (Lss), Macedonia, Romania, South Africa, and Turkey.

|  | Percentage of Students Whose Schools Reported That They Expect Parents to Be Involved in the School-Related Activity |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Be Sure Child Completes Homework | Serve as Teacher Aides in Classroom | Volunteer for School Projects, Programs, or Field Trips | Raise Funds for the School | Serve on Committees ${ }^{1}$ |
| Australia | 96 (1.7) | 6 (1.9) | 66 (4.5) | 61 (5.4) | 78 (3.9) |
| Belgium (Flemish) | 94 (2.1) | 19 (3.7) | 39 (4.3) | 9 (2.7) | 10 (2.7) |
| Bulgaria | 73 (5.6) | 64 (5.1) | 63 (5.5) | 55 (5.2) | 22 (3.5) |
| Canada | 99 (0.6) | 15 (1.7) | 82 (2.2) | 52 (3.4) | 55 (2.7) |
| Chile | 92 (2.1) | 73 (3.3) | 94 (1.9) | 57 (3.6) | 33 (3.1) |
| Chinese Taipei | 97 (1.3) | 58 (4.2) | 90 (2.5) | 41 (4.2) | 56 (4.4) |
| Cyprus | 78 (0.2) | 15 (0.1) | 44 (0.2) | 87 (0.1) | 18 (0.2) |
| Czech Republic | 91 (3.1) | 7 (2.7) | 80 (3.8) | 32 (4.7) | 35 (4.9) |
| England | - - |  |  |  |  |
| Finland | 94 (2.0) | 4 (1.5) | 72 (4.3) | 23 (4.2) | 57 (4.8) |
| Hong Kong, SAR | 96 (1.8) | 30 (4.2) | 77 (3.8) | 60 (4.6) | 21 (3.7) |
| Hungary | 96 (1.6) | 35 (3.8) | 95 (1.9) | 12 (2.5) | 35 (3.9) |
| Indonesia | 97 (1.5) | 4 (1.8) | 70 (4.5) | 59 (4.2) | 28 (4.4) |
| Iran, Islamic Rep. | 95 (2.1) | 82 (3.7) | 96 (2.0) | 74 (3.7) | 85 (2.7) |
| Israel | 77 (4.0) | 16 (3.0) | 90 (2.4) | 42 (4.6) | 48 (4.8) |
| Italy | 91 (2.3) | 9 (2.2) | 70 (3.4) | 25 (3.1) | 42 (3.7) |
| Japan | 43 (4.4) | 5 (2.0) | 81 (2.8) | 6 (2.0) | 8 (2.2) |
| Jordan | 78 (3.7) | 23 (3.5) | 77 (3.9) | 29 (4.1) | 17 (3.3) |
| Korea, Rep. of | 64 (3.9) | 33 (4.1) | 71 (3.8) | 31 (3.8) | 44 (4.2) |
| Latvia (LSS) | 69 (4.1) | 65 (4.4) | 95 (2.1) | 45 (4.7) | 75 (4.0) |
| Lithuania ${ }^{\text { }}$ | 88 (2.6) | 11 (2.6) | 100 (0.0) | 62 (3.9) | 73 (3.8) |
| Macedonia, Rep. of | 72 (3.6) | 27 (4.1) | 48 (4.1) | 53 (3.9) | 95 (2.0) |
| Malaysia | 97 (1.4) | 29 (4.0) | 100 (0.0) | 64 (4.3) | 21 (3.2) |
| Moldova | 66 (4.5) | 46 (4.4) | 66 (3.4) | 55 (4.5) | 62 (4.3) |
| Morocco | 62 (3.2) | 37 (3.9) | 90 (2.2) | 80 (2.9) | 14 (2.6) |
| Netherlands | 81 (5.6) | 46 (6.2) | 61 (6.2) | 16 (5.2) | 46 (6.5) |
| New Zealand | 97 (1.6) | 4 (1.6) | 74 (3.7) | 62 (4.2) | 21 (3.5) |
| Philippines | 86 (2.9) | 30 (4.1) | 89 (2.8) | 65 (4.1) | 37 (4.0) |
| Romania | 90 (2.6) | 8 (2.4) | 86 (3.2) | 73 (4.1) | 79 (4.3) |
| Russian Federation | 78 (3.1) | 36 (3.3) | 91 (1.7) | 59 (2.8) | 59 (4.1) |
| Singapore | 95 (1.8) | 6 (2.2) | 44 (4.5) | 51 (4.3) | 41 (4.3) |
| Slovak Republic | 84 (2.8) | 42 (5.0) | 90 (2.9) | 81 (3.3) | 65 (4.1) |
| Slovenia | 98 (1.3) | 16 (2.8) | 94 (2.1) | 35 (3.8) | 42 (4.0) |
| South Africa | 93 (1.8) | 39 (4.4) | 97 (1.2) | 87 (2.4) | 99 (0.8) |
| Thailand | 92 (2.2) | 40 (3.6) | 76 (3.5) | 69 (3.6) | 48 (3.8) |
| Tunisia | 73 (4.0) | 15 (3.2) | 71 (3.6) | 55 (3.7) | 21 (3.3) |
| Turkey | 85 (2.8) | 33 (3.9) | 94 (2.3) | 78 (3.2) | 89 (2.4) |
| United States | r 99 (0.7) | r 15 (3.0) | 94 (1.7) | r 55 (4.7) | r 68 (4.1) |
| International Avg. | 85 (0.5) | 28 (0.6) | 79 (0.5) | 51 (0.6) | 47 (0.6) |

[^61]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates school response data available for $70-84 \%$ of students.


## How Serious Are School Attendance Problems?

In some countries, schools are confronted with high rates of absenteeism, which can influence instructional continuity and reduce the time for learning. In general, research has shown that greater truancy is related to less serious attitudes towards school and lower academic achievement. To examine this issue, timss developed an index of good school and class attendance (SCA) based on schools' responses to three questions about the seriousness of students' absenteeism, arriving late at school, and skipping class. The high index level indicates schools reported that all three behaviors are not a problem. The low level indicates that two or more are a serious problem, or two are minor problems and the third a serious problem. The medium category includes all other possible combinations of responses.

The results of the index are presented in Exhibit 7.5. Sixty percent of students on average internationally were in the medium category, where principals had judged their schools to have a moderate attendance problem. Exactly one-fifth of the students were in schools at the high level of the index, and another 19 percent were in schools at the low index level.

The information used to compute this index appears in Exhibit 7.6, together with data showing the percentages of students in schools where the behaviors occur at least weekly. Student attendance problems were common and considered to be a serious problem in many countries, and were most acute in South Africa. For most countries, however, schools reported the frequency of the attendance problems to be greater than their seriousness.

| Index of Good School and Class Attendance |  | High SCA |  | Medium SCA |  | $\begin{aligned} & \text { Low } \\ & \text { SCA } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on schools' responses to three questions about the seriousness of attendance problems in school: arriving late at school; absenteeism; skipping class (see exhibit 7.6). High level indicates that all three behaviors are reported to be not a problem. Low level indicates that two or more behaviors are reported to be a serious problem, or two behaviors are reported to be minor problems and the third a serious problem. Medium level includes all other possible combinations of responses. | Belgium (Flemish) <br> Slovenia <br> Jordan <br> Iran, Islamic Rep. <br> Czech Republic | 52 (4.4) <br> 39 (4.0) <br> 39 (4.2) <br> 37 (4.9) <br> 36 (5.8) | $\begin{aligned} & 579(7.1) \\ & 531(4.3) \\ & 430(6.2) \\ & 422(5.8) \\ & 526(9.9) \end{aligned}$ | $\begin{array}{ll} 45 & (4.5) \\ 58 & (4.0) \\ 56 & (4.5) \\ 61 & (4.9) \\ 56 & (6.0) \end{array}$ | $\begin{aligned} & 536(7.4) \\ & 533(3.2) \\ & 426(5.9) \\ & 423(4.4) \\ & 516(4.4) \end{aligned}$ | $\begin{aligned} & 3(1.0) \\ & 4(1.7) \\ & 5(1.9) \\ & 2(1.3) \\ & 8(2.3) \end{aligned}$ | $\begin{gathered} 535 \text { (9.3) } \\ 474 \text { (15.5) } \\ 404 \text { (8.0) } \\ \sim \sim \\ \sim 39(20.2) \end{gathered}$ |
|  | Italy <br> Singapore <br> Korea, Rep. of <br> Macedonia, Rep. of Slovak Republic | $\begin{array}{ll} 33 & (3.3) \\ 32 & (4.1) \\ 31 & (3.7) \\ 31 & (4.2) \\ 31 & (4.3) \end{array}$ | $\begin{aligned} & 497 \text { (5.8) } \\ & 630 \text { (11.9) } \\ & 585(3.7) \\ & 448(9.3) \\ & 534(6.8) \end{aligned}$ | 58 (3.6) <br> 64 (4.0) <br> 61 (4.0) <br> 51 (4.5) <br> 57 (4.5) | 481 (5.1) <br> 592 (7.0) <br> 588 (2.4) <br> 448 (7.7) <br> 535 (4.7) | $\begin{array}{r} 9(2.4) \\ 3(1.6) \\ 9(2.4) \\ 19(3.2) \\ 12(3.3) \end{array}$ | $\begin{aligned} & 424(12.4) \\ & 597(19.3) \\ & 595(5.4) \\ & 433(14.2) \\ & 513(11.4) \end{aligned}$ |
|  | Netherlands Chinese Taipei Turkey Hong Kong, SAR Bulgaria | $\begin{array}{ll} 30 & (7.3) \\ 28 & (3.7) \\ 26 & (3.1) \\ 25 & (3.9) \\ 23 & (5.7) \end{array}$ | $\begin{aligned} & 524(14.5) \\ & 616(7.6) \\ & 450(9.5) \\ & 603(7.4) \\ & 510(9.3) \end{aligned}$ | 46 (7.3) <br> 61 (3.6) <br> 62 (3.9) <br> 68 (4.3) <br> 61 (5.4) | 555 (6.6) <br> 570 (4.0) <br> 422 (4.6) <br> 582 (6.8) <br> 516 (9.0) | $\begin{array}{r} 24(7.5) \\ 11(2.7) \\ 12(2.8) \\ 7(2.5) \\ 17(3.1) \end{array}$ | $\begin{aligned} & 519 \text { (27.9) } \\ & 591 \text { (10.1) } \\ & 418 \text { (11.6) } \\ & 540(13.3) \\ & 495 \text { (12.8) } \end{aligned}$ |
|  | Hungary United States Cyprus Canada Thailand | $\begin{aligned} & 23(3.6) \\ & 19(3.0) \\ & 19(0.1) \\ & 18(2.2) \\ & 17(3.3) \end{aligned}$ | 546 (9.7) 534 (11.5) 482 (3.8) 530 (7.1) 461 (10.9) | $\begin{array}{ll} 60 & (4.2) \\ 68 & (3.4) \\ 54 & (0.2) \\ 73 & (3.0) \\ 68 & (4.3) \end{array}$ | $\begin{aligned} & 529(5.0) \\ & 498(5.2) \\ & 476(2.2) \\ & 530(3.0) \\ & 472(6.6) \end{aligned}$ | $\begin{array}{r} 17(3.1) \\ 13(2.5) \\ 27(0.2) \\ 9(2.0) \\ 14(3.3) \end{array}$ | $\begin{array}{ll} 521(10.8) \\ 470(9.3) \\ 476 & (5.2) \\ 535 & (7.9) \\ 473 & (19.9) \end{array}$ |
|  | Australia Chile Finland Tunisia New Zealand | $\begin{array}{ll} 17 & (3.5) \\ 16 & (3.1) \\ 15 & (2.9) \\ 15 & (3.1) \\ 15 & (2.9) \end{array}$ | 543 (8.2) 414 (11.9) 520 (7.8) 461 (5.7) 511 (14.9) | $\begin{array}{ll} 70 & (4.0) \\ 70 & (3.8) \\ 67 & (4.4) \\ 60 & (3.8) \\ 69 & (3.7) \end{array}$ | $\begin{aligned} & 528(6.0) \\ & 391(5.4) \\ & 520(3.6) \\ & 448(3.4) \\ & 495(6.0) \end{aligned}$ | $\begin{array}{ll} 13 & (3.3) \\ 13 & (2.7) \\ 18 & (3.8) \\ 26 & (3.6) \\ 16 & (2.5) \end{array}$ | $\begin{array}{ll} 489 & (14.8) \\ 380 & (6.9) \\ 522 & (5.0) \\ 440 & (3.5) \\ 443 & (10.8) \end{array}$ |
|  | Romania Lithuania ${ }^{\text { }}$ Latvia (LSS) Russian Federation Indonesia | $\begin{array}{ll} 15 & (3.2) \\ 12 & (2.6) \\ 11 & (2.6) \\ 10 & (1.7) \\ 10 & (2.6) \end{array}$ | $\begin{array}{ll} 476 & (13.2) \\ 481 & (13.4) \\ 503 & (11.6) \\ 535 & (12.0) \\ 396 & (17.0) \end{array}$ | $\begin{array}{ll} 55 & (4.2) \\ 56 & (4.2) \\ 63 & (4.6) \\ 70 & (3.8) \\ 57 & (4.5) \end{array}$ | 466 (7.7) <br> 491 (5.8) <br> 506 (5.1) <br> 532 (6.4) <br> 408 (7.9) | $\begin{array}{ll} 31 & (4.1) \\ 32 & (3.7) \\ 26 & (4.3) \\ 20 & (3.4) \\ 33 & (4.1) \end{array}$ | $\begin{aligned} & 478 \text { (10.5) } \\ & 468 \text { (6.9) } \\ & 497(6.5) \\ & 500(8.2) \\ & 389(8.6) \end{aligned}$ |
|  | Philippines <br> Japan <br> Israel <br> Malaysia <br> Morocco | $\begin{aligned} & 8(2.4) \\ & 7(2.4) \\ & 7(2.3) \\ & 6(2.4) \\ & 4(1.4) \end{aligned}$ | $\begin{array}{ll} 345 & (16.6) \\ 590 & (12.2) \\ 458 & (17.7) \\ 503 & (21.2) \\ 337 & (11.4) \end{array}$ | 72 (3.9) <br> 47 (4.1) <br> 57 (4.8) <br> 69 (4.1) <br> 56 (4.3) | $\begin{aligned} & 351(8.2) \\ & 579(2.6) \\ & 478(5.6) \\ & 527(5.4) \\ & 336(3.7) \end{aligned}$ | $\begin{array}{ll} 20 & (3.4) \\ 46 & (3.9) \\ 36 & (4.6) \\ 25 & (3.8) \\ 40 & (4.4) \end{array}$ | $\begin{aligned} & 323(9.6) \\ & 576(2.4) \\ & 449(10.4) \\ & 500(9.2) \\ & 339(4.0) \end{aligned}$ |
|  | South Africa Moldova England | $\begin{aligned} & 3(1.2) \\ & 1(1.0) \\ & -- \end{aligned}$ | $386 \text { (34.0) }$ | 44 (3.9) <br> 63 (3.8) | $\begin{gathered} 295(12.4) \\ 469(4.8) \\ -- \end{gathered}$ | 53 (4.0) <br> 35 (3.8) | $\begin{gathered} 251(8.0) \\ 463(7.7) \\ -- \end{gathered}$ |
|  | International Avg. | 20 (0.6) | 497 (2.8) | 60 (0.7) | 488 (1.0) | 19 (0.5) | 474 (2.0) |

[^62]$\square$




[^63]A dash (-) indicates data are not available.
An " $r$ " indicates school response data available for 70-84\% of students.

## How Safe and Orderly Are Schools?

The frequency and seriousness of student behavior threatening an orderly school environment are presented in Exhibit 7.7. The three behaviors are violating the dress code, creating a classroom disturbance, and cheating. Violation of dress code is likely to reflect, at least partially, whether there is a uniform requirement. For many countries, violating the dress code was not reported to be a serious problem, and on average internationally only six percent of the students were in schools where it was a serious problem.

In contrast, 13 percent of the students, on average internationally, were in schools that reported classroom disturbances to be a serious problem. Most countries showed a pattern in which a larger percentage of students were in schools where classroom disturbances occurred at least weekly compared with the percentage of students in schools where it was considered a serious problem. The single exception was Japan, where just five percent of the students were in schools in which classroom disturbances occurred weekly, and yet 29 percent were in schools that considered classroom disturbances to be a serious problem.

The frequency and seriousness of student behavior threatening a safe school environment are shown in Exhibit 7.8. The five behaviors are vandalism, theft, physical injury to other students, intimidation or ver-
 bal abuse of other students, and intimidation or verbal abuse of teachers or staff. As in other reports of student behavior, cross-national comparisons are difficult because of differing perceptions of what constitutes a serious problem. However, with only a few exceptions, the overwhelming majority of students attend schools judged to have few serious problems. The incidence of these student behaviors was generally low in most countries. The exception was intimidation or verbal abuse of other students, for which several countries had relatively high percentages of students in schools where the behavior occurs at least weekly; in Australia, Israel, the Netherlands, and the United States, close to half of the students were in such schools.


## Background data provided by schools.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^64]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.



Exhibit 7.8 Overleaf

## Exhibit 7.8 Frequency and Seriousness of Student Behavior Threatening a Safe School Environment

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{3}{*}{} \& \multicolumn{6}{|c|}{Percentage of Students Whose Schools Reported the Behavior} <br>
\hline \& \multicolumn{2}{|c|}{Vandalism} \& \multicolumn{2}{|r|}{Theft} \& \multicolumn{2}{|l|}{Physical Injury to Other Students} <br>
\hline \& Occurs at Least Weekly \& Is a Serious Problem \& Occurs at Least Weekly \& Is a Serious Problem \& Occurs at Least Weekly \& Is a Serious Problem <br>
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& $$
\begin{array}{r}
27(4.2) \\
8(2.4) \\
5(1.8) \\
15(1.5) \\
9(2.3)
\end{array}
$$ \& $$
\begin{aligned}
& 2(1.2) \\
& 9(2.6) \\
& 4(1.6) \\
& 6(2.0) \\
& 7(2.0)
\end{aligned}
$$ \& $$
\begin{array}{r}
23(3.7) \\
7(2.2) \\
1(0.6) \\
7(1.4) \\
10(2.3)
\end{array}
$$ \& $$
\begin{aligned}
& 1(0.7) \\
& 9(2.5) \\
& 1(1.0) \\
& 6(1.9) \\
& 7(1.9)
\end{aligned}
$$ \& $$
\begin{array}{r}
14(3.1) \\
8(1.9) \\
4(1.4) \\
6(1.8) \\
12(2.5)
\end{array}
$$ \& $$
\begin{array}{ll}
3 & (1.4) \\
6 & (2.1) \\
1 & (0.0) \\
4(1.5) \\
9 & (1.8)
\end{array}
$$ <br>
\hline Chinese Taipei Cyprus Czech Republic England Finland \& $14(3.1)$
$r \quad 18(0.1)$
$13(2.7)$

$6(2.2)$ \& $11(2.5)$
$r \quad 22(0.2)$
$21(3.6)$
--

$3(1.6)$ \& |  | $7(2.2)$ |
| :--- | :--- |
| $r$ | $8(0.1)$ |
|  | $3(1.9)$ |
|  | -- |
|  | $3(1.8)$ | \& $16(2.9)$

$r \quad 23(0.2)$
$17(3.8)$
--

$1(0.8)$ \& $$
\begin{aligned}
& 8(2.3) \\
& 2(0.0) \\
& 2(1.7) \\
& -- \\
& 7(2.5)
\end{aligned}
$$ \& $21(3.2)$

$r \quad 20(0.2)$
$17(3.7)$

$2(1.4)$ <br>

\hline Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel \& \[
$$
\begin{array}{r}
18(3.7) \\
10(2.6) \\
4(1.8) \\
3(1.4) \\
30(4.2)
\end{array}
$$

\] \& | $r$ | $6(2.3)$ |
| ---: | ---: |
|  | $30(3.5)$ |
|  | $29(4.0)$ |
| $r$ | $4(1.6)$ |
| $r$ | $28(4.1)$ | \& \[

$$
\begin{array}{r}
8(2.6) \\
2(1.1) \\
1(0.9) \\
1(0.6) \\
10(2.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{lr}
r & 5(2.2) \\
& 25(3.4) \\
& 30(4.1) \\
& 4(1.6) \\
r & 15(3.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
5(2.1) \\
8(2.0) \\
0(0.0) \\
3(1.4) \\
24(4.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{lr}
r & 3(1.6) \\
& 23(3.1) \\
& 26(3.9) \\
r & 2(1.4) \\
r & 18(3.7)
\end{array}
$$
\] <br>

\hline Italy Japan Jordan Korea, Rep. of Latvia (LSS) \& \[
$$
\begin{array}{r}
7(1.9) \\
3(1.3) \\
5(1.8) \\
12(2.8) \\
2(1.3)
\end{array}
$$

\] \& | $18(2.8)$ |  |
| ---: | ---: |
| $23(3.5)$ |  |
| $r$ | $16(3.6)$ |
|  | $10(2.5)$ |
| $r$ | $4(2.0)$ | \& \[

$$
\begin{array}{ll}
4 & (1.4) \\
1 & (0.9) \\
2 & (1.1) \\
9 & (2.5) \\
0(0.0)
\end{array}
$$

\] \& | $16(2.8)$ |
| ---: |
| $25(3.7)$ |
| $r \quad 12(3.1)$ |
|  |
| $13(3.0)$ |
|  |
|  |
|  |
|  | \& \[

$$
\begin{array}{r}
9(2.1) \\
1(0.9) \\
9(2.5) \\
10(2.6) \\
5(2.3)
\end{array}
$$
\] \& $19(3.0)$

$22(3.6)$
$r \quad 10(2.7)$
$r \quad 9(2.6)$
$r$$\quad 8(2.6)$ <br>

\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{r}
0(0.0) \\
3(1.4) \\
12(3.0) \\
1(1.0) \\
17(2.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
6(1.7) \\
8(2.6) \\
17(3.4) \\
3(1.3) \\
34(4.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
0 & (0.0) \\
1 & (0.9) \\
7 & (2.0) \\
0(0.0) \\
8 & (1.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
9(2.0) \\
6(2.2) \\
12(2.8) \\
8(2.3) \\
26(3.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
1 & (0.0) \\
3 & (1.6) \\
2 & (1.1) \\
0 & (0.0) \\
9 & (2.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
7(1.3) \\
9(2.4) \\
11(2.2) \\
2(1.2) \\
25(3.6)
\end{array}
$$
\] <br>

\hline | Netherlands |
| :--- |
| New Zealand Philippines Romania Russian Federation | \& \[

$$
\begin{array}{rr}
r & 45(7.6) \\
21(3.5) \\
& 16(3.2) \\
& 0(0.0) \\
& 0(0.4)
\end{array}
$$

\] \& | $r \quad 28(7.4)$ |
| ---: |
| $4(1.8)$ |
| $11(2.4)$ |
| $11(2.9)$ |
|  |
|  |
|  |
|  |
|  |
| $(1.5)$ | \& \[

$$
\begin{array}{rr}
r \quad 22(5.9) \\
& 15(3.0) \\
& 6(2.2) \\
& 2(1.3) \\
& 1(0.5)
\end{array}
$$
\] \& $r \quad 19(6.4)$

$4(1.5)$
$2(1.1)$
$19(3.5)$

$6(2.0)$ \& \[
$$
\begin{array}{ll}
r \quad 2(1.3) \\
& 8(2.0) \\
& 6(2.0) \\
& 9(2.6) \\
& 2(1.1)
\end{array}
$$

\] \& | $r \quad 4(2.0)$ |
| ---: |
|  |
| $1(0.9)$ |
| $1(0.7)$ |
| $22(3.5)$ |
|  |
|  |
|  |
|  |
| $(1.3)$ | <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& $$
\begin{array}{r}
5(1.8) \\
15(3.4) \\
8(2.0) \\
18(3.3) \\
9(2.3)
\end{array}
$$ \& \[

$$
\begin{array}{r}
2(1.3) \\
24(4.1) \\
2(1.5) \\
32(4.2) \\
3(1.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
5(2.0) \\
2(1.4) \\
3(1.3) \\
16(2.7) \\
4(1.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
2(1.4) \\
17(3.4) \\
1(0.8) \\
29(4.2) \\
4(1.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
1 & (0.7) \\
3 & (1.7) \\
4 & (1.9) \\
7 & (2.0) \\
3 & (1.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
0(0.0) \\
15(3.8) \\
1(0.8) \\
14(3.3) \\
3(1.5)
\end{array}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& \[

$$
\begin{array}{r}
9(2.5) \\
10(2.0) \\
r \quad 11(2.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
35(4.4) \\
11(2.9) \\
r \quad 1(0.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
2(1.2) \\
6(1.9) \\
r \quad 10(2.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
29(4.0) \\
10(3.1) \\
r \quad 2(1.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
5(1.9) \\
7(1.4) \\
r \quad 10(2.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
28(3.8) \\
10(2.8) \\
r \quad 3(1.8)
\end{array}
$$
\] <br>

\hline International Avg. \& 11 (0.4) \& 13 (0.5) \& 6 (0.3) \& 12 (0.5) \& 6 (0.3) \& 10 (0.4) <br>
\hline
\end{tabular}

[^65]A dash (-) indicates data are not available.
An " $r$ " indicates school response data available for 70-84\% of students.



## REFERENCE 1

Students' Backgrounds and Attitudes Towards Mathematics

|  | Have All Three Educational Aids |  | Do Not Have All Three Educational Aids |  | Percentage of Students |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Have Dictionary | Have Study Desk/Table for Own Use | Have Computer |
|  | Percent of Students | Average Achievement |  |  |  | Percent of Students | Average Achievement |
| Australia | 82 (1.1) | 533 (4.8) | 18 (1.1) | 492 (6.3) | 99 (0.2) | 95 (0.4) | 86 (1.0) |
| Belgium (Flemish) | 82 (1.2) | 567 (3.3) | 18 (1.2) | 520 (8.6) | 98 (0.7) | 96 (0.6) | 86 (1.0) |
| Bulgaria | 21 (2.4) | 546 (13.1) | 79 (2.4) | 502 (4.8) | 89 (0.9) | 87 (1.2) | 23 (2.3) |
| Canada | 78 (0.8) | 537 (2.6) | 22 (0.8) | 510 (3.1) | 98 (0.2) | 91 (0.6) | 85 (0.8) |
| Chile | 21 (1.7) | 442 (9.8) | 79 (1.7) | 381 (3.2) | 97 (0.4) | 78 (0.9) | 23 (1.7) |
| Chinese Taipei | 61 (1.1) | 608 (3.8) | 39 (1.1) | 551 (4.4) | 98 (0.2) | 94 (0.4) | 63 (1.0) |
| Cyprus | 56 (0.8) | 493 (2.6) | 44 (0.8) | 459 (2.6) | 97 (0.3) | 97 (0.3) | 58 (0.9) |
| Czech Republic | 43 (1.2) | 541 (4.5) | 57 (1.2) | 504 (4.6) | 94 (0.8) | 91 (0.7) | 47 (1.2) |
| England | 79 (0.9) | 507 (4.0) | 21 (0.9) | 461 (6.0) | 98 (0.3) | 92 (0.6) | 85 (0.8) |
| Finland | 71 (1.2) | 528 (3.0) | 29 (1.2) | 501 (3.5) | 89 (0.7) | 97 (0.4) | 79 (0.9) |
| Hong Kong, SAR | 57 (1.3) | 592 (4.1) | 43 (1.3) | 571 (4.9) | 99 (0.1) | 75 (0.9) | 72 (1.3) |
| Hungary | 48 (1.4) | 562 (4.0) | 52 (1.4) | 504 (3.9) | 95 (0.8) | 95 (0.5) | 50 (1.4) |
| Indonesia | 6 (0.8) | 468 (15.0) | 94 (0.8) | 400 (4.8) | 86 (0.9) | 84 (1.1) | 7 (0.8) |
| Iran, Islamic Rep. | 5 (0.7) | 457 (9.5) | 95 (0.7) | 422 (3.1) | 51 (1.5) | 47 (2.2) | 7 (0.8) |
| Israel | 78 (1.5) | 486 (3.2) | 22 (1.5) | 409 (6.2) | 98 (0.3) | 97 (0.3) | 80 (1.5) |
| Italy | 59 (1.1) | 492 (4.0) | 41 (1.1) | 461 (4.2) | 98 (0.3) | 93 (0.6) | 63 (1.0) |
| Japan | 52 (1.0) | 592 (2.3) | 48 (1.0) | 566 (2.3) | 99 (0.1) | 97 (0.2) | 52 (0.9) |
| Jordan | 16 (0.9) | 469 (6.9) | 84 (0.9) | 425 (3.7) | 80 (0.9) | 73 (1.1) | 23 (1.1) |
| Korea, Rep. of | 65 (0.9) | 602 (1.7) | 35 (0.9) | 561 (3.0) | 99 (0.2) | 96 (0.2) | 67 (0.9) |
| Latvia (LSS) | 14 (1.0) | 537 (6.0) | 86 (1.0) | 500 (3.5) | 94 (0.7) | 98 (0.3) | 15 (1.0) |
| Lithuania ${ }^{\text { }}$ | 15 (1.1) | 529 (8.1) | 85 (1.1) | 474 (4.1) | 86 (0.9) | 95 (0.5) | 16 (1.1) |
| Macedonia, Rep. of | 18 (1.2) | 484 (5.6) | 82 (1.2) | 442 (4.3) | 83 (1.2) | 87 (0.8) | 21 (1.3) |
| Malaysia | 28 (1.2) | 563 (5.5) | 72 (1.2) | 503 (4.1) | 99 (0.2) | 87 (0.6) | 31 (1.3) |
| Moldova | 5 (0.6) | 489 (11.8) | 95 (0.6) | 469 (3.8) | 72 (1.3) | 79 (0.9) | 7 (0.7) |
| Morocco | 6 (0.7) | 357 (11.5) | 94 (0.7) | 339 (2.3) | 71 (1.2) | 52 (1.1) | 9 (0.9) |
| Netherlands | 94 (1.0) | 543 (7.2) | 6 (1.0) | 509 (8.7) | 100 (0.2) | 99 (0.2) | 96 (1.0) |
| New Zealand | 67 (1.3) | 512 (5.6) | 33 (1.3) | 453 (4.5) | 97 (0.4) | 90 (0.6) | 72 (1.2) |
| Philippines | 11 (0.9) | 392 (14.9) | 89 (0.9) | 342 (5.9) | 89 (0.7) | 74 (1.0) | 15 (0.9) |
| Romania | 11 (0.8) | 509 (10.2) | 89 (0.8) | 471 (5.1) | 69 (1.6) | 76 (1.4) | 14 (1.0) |
| Russian Federation | 19 (1.2) | 537 (6.6) | 81 (1.2) | 524 (6.3) | 88 (1.3) | 92 (0.8) | 22 (1.2) |
| Singapore | 75 (1.4) | 615 (6.1) | 25 (1.4) | 573 (7.1) | 99 (0.2) | 92 (0.5) | 80 (1.3) |
| Slovak Republic | 36 (1.3) | 556 (5.2) | 64 (1.3) | 522 (3.7) | 96 (0.5) | 88 (0.8) | 41 (1.3) |
| Slovenia | 61 (1.2) | 547 (2.8) | 39 (1.2) | 506 (3.6) | 92 (0.6) | 96 (0.3) | 66 (1.2) |
| South Africa | 8 (1.0) | 415 (15.1) | 92 (1.0) | 265 (6.6) | 75 (1.1) | 56 (1.1) | 11 (1.1) |
| Thailand | 8 (0.6) | 538 (9.2) | 92 (0.6) | 462 (5.1) | 75 (1.2) | 63 (1.5) | 8 (0.7) |
| Tunisia | 23 (1.3) | 462 (3.5) | 77 (1.3) | 444 (2.6) | 87 (1.0) | 92 (0.6) | 24 (1.3) |
| Turkey | 8 (0.6) | 471 (7.1) | 92 (0.6) | 426 (4.4) | 89 (0.7) | 69 (1.3) | 10 (0.7) |
| United States | 74 (1.3) | 518 (3.7) | 26 (1.3) | 463 (4.3) | 97 (0.3) | 90 (0.5) | 80 (1.2) |
| International Avg. | 41 (0.2) | 516 (1.2) | 59 (0.2) | 471 (0.8) | 90 (0.1) | 86 (0.1) | 45 (0.2) |

[^66][^67]|  | Have All Three Educational Aids |  |  | Have Dictionary |  |  | Have Study Desk/ Table for Own Use |  |  | Have Computer |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | 1995-1999 <br> Difference |  | Percent of Students | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students | 1995-199 <br> Difference |  |
| Australia | 82 (1.1) | 16 (1.6) | $\triangle$ | 99 (0.2) | 11 (0.8) | $\triangle$ | 95 (0.4) | -2 (0.5) | $\checkmark$ | 86 (1.0) | 13 (1.5) | $\triangle$ |
| Belgium (Flemish) | 82 (1.2) | 19 (1.8) | $\triangle$ | 98 (0.7) | 0 (0.8) | - | 96 (0.6) | -1 (0.8) | - | 86 (1.0) | 19 (1.6) | $\triangle$ |
| Canada | 78 (0.8) | 21 (1.6) | - | 98 (0.2) | 2 (0.4) | $\triangle$ | 91 (0.6) | $2(0.8)$ | - | 85 (0.8) | 24 (1.6) | $\triangle$ |
| Cyprus | 56 (0.8) | 18 (1.2) | $\triangle$ | 97 (0.3) | 0 (0.5) | - | 97 (0.3) | 1 (0.6) | - | 58 (0.9) | 19 (1.3) | $\triangle$ |
| Czech Republic | 43 (1.2) | 11 (1.8) | $\triangle$ | 94 (0.8) | -1 (0.9) | - | 91 (0.7) | 2 (0.9) | - | 47 (1.2) | 11 (1.7) | $\triangle$ |
| England | 79 (0.9) | -1 (1.4) | - | 98 (0.3) | 0 (0.5) | - | 92 (0.6) | 2 (1.0) | - | 85 (0.8) | -4 (1.2) | $\checkmark$ |
| Hong Kong, SAR | 57 (1.3) | 24 (2.2) | $\triangle$ | 99 (0.1) | 0 (0.2) | $\bullet$ | 75 (0.9) | -5 (1.4) | $\nabla$ | 72 (1.3) | 33 (2.3) | $\triangle$ |
| Hungary | - - | - - |  | - - | - - |  | 95 (0.5) | 3 (0.9) | $\triangle$ | 50 (1.4) | 13 (1.8) | - |
| Iran, Islamic Rep. | 5 (0.7) | 4 (0.8) | $\triangle$ | 51 (1.5) | -2 (2.1) | - | 47 (2.2) | 8 (3.0) | - | 7 (0.8) | 3 (1.0) | $\triangle$ |
| Israel ${ }^{+}$ | 83 (1.7) | 9 (2.7) | $\triangle$ | 99 (0.2) | -1 (0.3) | - | 98 (0.2) | 0 (0.5) | - | 85 (1.8) | 9 (2.7) | $\triangle$ |
| Italy | 58 (1.4) | -1 (2.1) | - | 98 (0.4) | -1 (0.4) | - | 93 (0.6) | -1 (1.0) | - | 62 (1.3) | 0 (2.0) | - |
| Japan | -- | -- |  |  | - - |  |  | - - |  |  | -- |  |
| Korea, Rep. of | 65 (0.9) | 27 (1.5) | $\triangle$ | 99 (0.2) | 0 (0.3) | - | 96 (0.2) | 1 (0.5) | - | 67 (0.9) | 27 (1.5) | $\triangle$ |
| Latvia (LSS) | 14 (1.0) | 2 (1.3) | $\bullet$ | 94 (0.7) | 1 (0.9) | - | 98 (0.3) | 0 (0.5) | - | 15 (1.0) | 2 (1.3) | - |
| Lithuania | - - | - - |  | 86 (0.9) | -2 (1.4) | - | 95 (0.5) | 1 (0.8) | - | - - | - - |  |
| Netherlands | 94 (1.0) | 11 (1.6) | $\triangle$ | 100 (0.2) | 0 (0.2) | - | 99 (0.2) | 0 (0.3) | - | 96 (1.0) | 11 (1.6) | $\triangle$ |
| New Zealand | 67 (1.3) | 11 (1.9) | $\triangle$ | 97 (0.4) | -2 (0.4) | $\nabla$ | 90 (0.6) | 0 (0.8) | - | 72 (1.2) | 12 (1.8) | $\triangle$ |
| Romania | 11 (0.8) | 3 (1.3) | - | 69 (1.6) | 9 (2.2) | $\triangle$ | 76 (1.4) | 7 (1.9) | 4 | 14 (1.0) | -5 (1.5) | $\checkmark$ |
| Russian Federation | 19 (1.2) | -11 (1.9) | $\nabla$ | 88 (1.3) | -1 (1.7) | - | 92 (0.8) | -3 (1.1) | - | 22 (1.2) | -13 (2.0) | $\nabla$ |
| Singapore | 75 (1.4) | 28 (2.0) | $\triangle$ | 99 (0.2) | 0 (0.2) | - | 92 (0.5) | 0 (0.7) | - | 80 (1.3) | 31 (2.0) | $\triangle$ |
| Slovak Republic | 36 (1.3) | 9 (1.8) | $\triangle$ | 96 (0.5) | 0 (0.7) | - | 88 (0.8) | 1 (1.1) | - | 41 (1.3) | 10 (1.8) | $\triangle$ |
| Slovenia | 61 (1.2) | 18 (1.8) | $\triangle$ | 92 (0.6) | -2 (0.8) | - | 96 (0.3) | 3 (0.7) | $\triangle$ | 66 (1.2) | 19 (1.8) | $\triangle$ |
| Thailand ${ }^{\dagger}$ | 8 (0.6) | 4 (1.0) | - | 75 (1.2) | 8 (2.4) | $\triangle$ | 63 (1.5) | -2 (2.6) | - | 8 (0.7) | 4 (1.1) | $\triangle$ |
| United States | 74 (1.3) | 18 (2.1) | - | 97 (0.3) | 0 (0.5) | - | 90 (0.5) | 0 (0.9) | - | 80 (1.2) | 21 (2.1) | $\triangle$ |
| International Avg. ${ }^{\text {s }}$ | 53 (0.2) | 10 (0.4) | $\triangle$ | 93 (0.1) | 1 (0.2) | $\triangle$ | 90 (0.2) | 1 (0.2) | $\triangle$ | 57 (0.2) | 10 (0.4) | $\triangle$ |



Background data provided by students.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below $65 \%$ in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.

|  | Three or More Bookcases (More Than 200 Books) |  | $\begin{gathered} \text { About Two } \\ \text { Bookcases } \\ \text { (101-200 Books) } \end{gathered}$ |  | $\begin{gathered} \text { About One } \\ \text { Bookcase } \\ \text { (26-100 Books) } \end{gathered}$ |  | About One Shelf (11-25 Books) |  | None or Very Few (0-10 Books) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 38 \\ 34 \\ 14 \\ (1.2) \\ 37 \\ 31 \\ 31 \\ (0.2) \\ 9 \end{array}(0.9)$ | $\begin{aligned} & 544(5.0) \\ & 580(5.1) \\ & 544(8.2) \\ & 543(3.5) \\ & 442(13.1) \end{aligned}$ | $\begin{aligned} & 27(0.9) \\ & 14(0.6) \\ & 19(0.9) \\ & 24(0.8) \\ & 11(0.6) \end{aligned}$ | $\begin{aligned} & 526(5.9) \\ & 578(7.3) \\ & 513(6.3) \\ & 536(3.5) \\ & 424(8.3) \end{aligned}$ | $\begin{array}{ll} 24 & (0.9) \\ 31 & (1.3) \\ 24 & (1.1) \\ 28 & (0.7) \\ 28 & (0.9) \end{array}$ | $\begin{aligned} & 511(5.0) \\ & 569(6.1) \\ & 499(5.6) \\ & 527(3.3) \\ & 414(4.9) \end{aligned}$ | $\begin{array}{r} 7(0.6) \\ 21(0.7) \\ 12(1.0) \\ 11(0.5) \\ 32 \end{array}$ | 498 (8.6) <br> 549 (5.1) <br> 466 (6.7) <br> 507 (5.1) <br> 374 (4.0) | $\begin{array}{r} 3(0.4) \\ 19(1.3) \\ 9(1.3) \\ 5(0.3) \\ 20(1.1) \end{array}$ | $\begin{aligned} & 479(13.3) \\ & 523(4.9) \\ & 457(9.6) \\ & 510(5.9) \\ & 355(3.0) \end{aligned}$ |
| Chinese Taipei <br> Cyprus <br> Czech Republic <br> England <br> Finland | $\begin{array}{ll} 16 & (0.8) \\ 17 & (0.8) \\ 28 & (1.4) \\ 26 & (1.2) \\ 22 & (1.1) \end{array}$ | $\begin{aligned} & 637(5.8) \\ & 497(4.3) \\ & 539(5.0) \\ & 537(6.1) \\ & 538(5.0) \end{aligned}$ | $\begin{aligned} & 12(0.5) \\ & 23 \\ & 23 \\ & (0.9) \\ & 30 \\ & (1.4) \\ & 23 \\ & (0.8) \\ & 22 \end{aligned}(0.9)$ | $\begin{aligned} & 629(5.7) \\ & 494(3.9) \\ & 532(5.6) \\ & 505(4.9) \\ & 527(4.3) \end{aligned}$ | $\begin{array}{ll} 31 & (0.7) \\ 36 & (1.0) \\ 34 & (1.1) \\ 32 & (1.1) \\ 39 & (1.1) \end{array}$ | $\begin{aligned} & 599(4.4) \\ & 479(2.6) \\ & 506(5.1) \\ & 488(3.8) \\ & 521(3.3) \end{aligned}$ | $\begin{array}{r} 23(0.7) \\ 19(0.9) \\ 7(0.8) \\ 13(0.8) \\ 14(0.8) \end{array}$ | $\begin{aligned} & 563(4.0) \\ & 450(4.0) \\ & 472(7.2) \\ & 456(5.8) \\ & 492(3.7) \end{aligned}$ | $\begin{array}{r} 17(0.9) \\ 5(0.5) \\ 1(0.2) \\ 7(0.7) \\ 4(0.4) \end{array}$ | $\begin{gathered} 513(4.4) \\ 428(9.2) \\ \sim \sim \\ 438(9.7) \\ 483(8.3) \end{gathered}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{r} 8(0.5) \\ 38(1.4) \\ 5(0.5) \\ 9(0.7) \\ 22(1.3) \end{array}$ | $\begin{aligned} & 588 \text { (8.8) } \\ & 564 \text { (4.0) } \\ & 406 \text { (12.1) } \\ & 461 \text { (7.2) } \\ & 495(4.9) \end{aligned}$ | $\begin{array}{r} 10(0.5) \\ 21(0.8) \\ 5(0.4) \\ 8(0.7) \\ 21(0.8) \end{array}$ | $\begin{aligned} & 590(7.4) \\ & 548 \text { (4.3) } \\ & 430 \text { (11.8) } \\ & 452 \text { (6.8) } \\ & 497(5.2) \end{aligned}$ | $\begin{array}{ll} 27 & (0.7) \\ 25 & (1.0) \\ 26 & (0.9) \\ 22 & (0.6) \\ 33 & (1.0) \end{array}$ | $\begin{aligned} & 592(4.3) \\ & 513(3.5) \\ & 421(5.1) \\ & 441(4.5) \\ & 469(4.7) \end{aligned}$ | $\begin{array}{ll} 27 & (0.7) \\ 12 & (0.8) \\ 39 & (1.0) \\ 32 & (0.8) \\ 18 & (0.9) \end{array}$ | $\begin{aligned} & 584(5.0) \\ & 467(6.6) \\ & 395(5.1) \\ & 417(3.1) \\ & 431(5.2) \end{aligned}$ | $\begin{array}{r} 28(0.9) \\ 3(0.5) \\ 26(1.3) \\ 29(1.4) \\ 6(0.5) \end{array}$ | $\begin{aligned} & 568 \text { (4.3) } \\ & 429 \text { (10.2) } \\ & 399(7.0) \\ & 397(3.2) \\ & 412(9.8) \end{aligned}$ |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) | 20 (0.9) <br> 18 (0.7) <br> 10 (0.6) <br> 20 (0.8) <br> 47 (1.4) | $\begin{aligned} & 505(5.6) \\ & 605(4.6) \\ & 462(6.1) \\ & 625(2.9) \\ & 525(4.2) \end{aligned}$ | 15 (0.7) <br> 18 (0.6) <br> 10 (0.6) <br> 23 (0.6) <br> 25 (0.9) | $\begin{aligned} & 495(4.9) \\ & 598(4.0) \\ & 467(8.8) \\ & 605(3.1) \\ & 501(4.5) \end{aligned}$ | $\begin{array}{ll} 28 & (0.9) \\ 31 & (0.7) \\ 28 & (0.8) \\ 36 & (0.7) \\ 21 & (0.9) \end{array}$ | $\begin{aligned} & 487(4.5) \\ & 577(2.7) \\ & 448(4.4) \\ & 581(2.2) \\ & 483(4.4) \end{aligned}$ | $\begin{array}{r} 25 \\ 25 \\ 19 \\ (0.9) \\ 31 \\ (0.6) \\ 10 \\ (0.1) \\ 6 \\ (0.5) \end{array}$ | 460 (5.4) 565 (4.3) 423 (3.9) 550 (3.8) 455 (9.4) | $\begin{array}{r} 12(0.8) \\ 14(0.6) \\ 21(1.2) \\ 10(0.4) \\ 1(0.2) \end{array}$ | 444 (7.0) <br> 549 (4.8) <br> 395 (4.7) <br> 527 (5.1) |
| Lithuania ${ }^{*}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 17(1.0) \\ 7(0.7) \\ 9(0.7) \\ 9(0.7) \\ 3(0.3) \end{array}$ | $\begin{aligned} & 524(5.8) \\ & 475(8.7) \\ & 566(6.8) \\ & 497(7.0) \\ & 352(18.8) \end{aligned}$ | $\begin{array}{r} 21(1.0) \\ 9(0.6) \\ 12(0.6) \\ 11(0.8) \\ 5(0.4) \end{array}$ | $\begin{aligned} & 513(4.8) \\ & 483 \\ & 546 \\ & 54.2) \\ & 498 \\ & 4.8 \\ & 352 \\ & 35 \end{aligned}(8.6)$ | $\begin{array}{ll} 36 & (1.2) \\ 30 & (1.2) \\ 32 & (0.9) \\ 28 & (1.0) \\ 20 & (1.0) \end{array}$ | $\begin{aligned} & 478 \text { (4.3) } \\ & 475(5.0) \\ & 536(5.0) \\ & 482(4.6) \\ & 347 \end{aligned}(6.3)$ | $\begin{array}{ll} 20 & (1.1) \\ 38 & (1.3) \\ 34 & (0.9) \\ 33 & (1.2) \\ 35 & (0.9) \end{array}$ | $\begin{aligned} & 440(5.9) \\ & 438(4.5) \\ & 499(3.9) \\ & 462(5.3) \\ & 344(6.1) \end{aligned}$ | $\begin{array}{r} 7(0.8) \\ 15(1.3) \\ 13 \end{array} \begin{array}{r} (0.8) \\ 20 \\ \hline \end{array}(1.1)$ | 417 (7.4) <br> 401 (8.4) <br> 477 (4.8) <br> 445 (6.0) <br> 330 (6.9) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 24(1.8) \\ 33(1.1) \\ 5(0.4) \\ 15(1.3) \\ 23(1.5) \end{array}$ | $\begin{aligned} & 564 \text { (8.5) } \\ & 518 \text { (6.3) } \\ & 358 \text { (16.9) } \\ & 517 \text { (8.5) } \\ & 556 \text { (6.3) } \end{aligned}$ | $\begin{array}{r} 23(1.2) \\ 24(0.8) \\ 5(0.4) \\ 15(0.9) \\ 29(1.1) \end{array}$ | $\begin{aligned} & 551 \text { (8.1) } \\ & 507 \text { (5.7) } \\ & 376 \text { (15.9) } \\ & 509 \text { (8.3) } \\ & 539 \text { (5.5) } \end{aligned}$ | $\begin{array}{ll} 31 & (1.1) \\ 27 & (0.8) \\ 15 & (0.8) \\ 32 & (1.1) \\ 31 & (1.3) \end{array}$ | $\begin{array}{ll} 540 & (8.2) \\ 480 & (5.6) \\ 378 & (10.4) \\ 476 & (5.1) \\ 517 & (5.3) \end{array}$ | 15 (1.4) <br> 10 (0.7) <br> 33 (0.9) <br> 24 (1.6) <br> 13 (1.0) | $\begin{aligned} & 512(9.6) \\ & 450(6.6) \\ & 353(7.2) \\ & 450(8.4) \\ & 485(9.0) \end{aligned}$ | $\begin{array}{r} 8(1.4) \\ 6(0.5) \\ 41(1.4) \\ 14(1.1) \\ 4(0.5) \end{array}$ | $\begin{aligned} & 499 \text { (11.1) } \\ & 408 \text { (9.1) } \\ & 325(4.8) \\ & 431 \text { (7.6) } \\ & 460(16.2) \end{aligned}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | 12 (0.6) <br> 17 (0.9) <br> 14 (0.9) <br> 7 (0.5) <br> 6 (0.5) | $\begin{aligned} & 618 \text { (8.3) } \\ & 565 \text { (5.3) } \\ & 561 \text { (5.4) } \\ & 320 \text { (16.8) } \\ & 504 \text { (9.1) } \end{aligned}$ | $\begin{array}{r} 14(0.7) \\ 24(1.0) \\ 20(0.8) \\ 6(0.5) \\ 8(0.5) \end{array}$ | $\begin{aligned} & 627(9.0) \\ & 554(4.4) \\ & 555(4.2) \\ & 343 \text { (17.8) } \\ & 488(7.9) \end{aligned}$ | 40 (1.1) <br> 43 (1.1) <br> 46 (1.0) <br> 14 (0.8) <br> 27 (0.9) | $\begin{aligned} & 613 \text { (6.1) } \\ & 528(3.8) \\ & 530(2.8) \\ & 317(10.4) \\ & 486(5.9) \end{aligned}$ | 22 (1.0) <br> 14 (1.0) <br> 16 (0.8) <br> 31 (0.8) <br> 37 (1.1) | 586 (6.8) 490 (4.9) 488 (6.2) 281 (6.6) 459 (4.8) | $12(0.8)$ <br> 2 (0.4) <br> 4 (0.4) <br> 43 (1.6) <br> 22 (1.0) | $\begin{gathered} 572(7.2) \\ \sim \\ \sim \\ 479(11.4) \\ 248(9.6) \\ 443(6.5) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{r} 9(0.6) \\ 6(0.4) \\ 28(1.2) \end{array}$ | $\begin{aligned} & 462(5.8) \\ & 444(8.6) \\ & 537 \text { (5.5) } \end{aligned}$ | $\begin{array}{r} 9(0.6) \\ 8(0.5) \\ 22(0.6) \end{array}$ | $\begin{aligned} & 468(5.5) \\ & 457 \text { (6.5) } \\ & 523 \text { (3.5) } \end{aligned}$ | $\begin{array}{ll} 25 & (0.7) \\ 28 & (0.8) \\ 29 & (0.8) \end{array}$ | $\begin{aligned} & 459(3.3) \\ & 448(6.0) \\ & 495(3.1) \end{aligned}$ | $\begin{aligned} & 36(0.9) \\ & 37(0.8) \\ & 14(0.7) \end{aligned}$ | $\begin{aligned} & 438(2.7) \\ & 421(4.7) \\ & 461(5.0) \end{aligned}$ | $\begin{array}{r} 21(1.1) \\ 22(1.1) \\ 8(0.6) \end{array}$ | $\begin{aligned} & 438(3.3) \\ & 405(5.2) \\ & 439(5.2) \end{aligned}$ |
| International Avg. | 18 (0.2) | 515 (1.3) | 16 (0.1) | 509 (1.1) | 29 (0.2) | 492 (0.8) | 22 (0.1) | 464 (0.9) | 14 (0.2) | 443 (1.6) |

[^68][^69]

[^70]Background data provided by students.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.


Background data provided by students

* Response categories were defined by each country to conform to their own educational system and may not be strictly comparable across countries. See reference exhibit R1.6 for country modifications to the definitions of educational levels.
1 In most countries, defined as completion of at least a 4 -year degree program at a university or an equivalent institute of higher education.
2 Finished upper secondary school with or without some tertiary education not equivalent to a university degree. In most countries, finished secondary corresponds to completion of an upper-secondary track terminating after 11 to 13 years of schooling (ISCED level 3 vocational, apprenticeship or academic tracks).

3 Finished primary school or attended some secondary school not equivalent to completion of upper secondary.
4 Some primary school or did not go to school.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates data are not available. A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates a $70-84 \%$ student response rate.


Exhibit R1.6 Overleaf

## Exhibit R1.6 Country Modifications to the Definitions of Educational Levels for Parents' Education or Students' Expectations for Finishing School*

|  | Finished University | Finished Upper Secondary School But Not University |  |
| :---: | :---: | :---: | :---: |
|  |  | Post-Secondary Level | Upper-Secondary Level ${ }^{1}$ |
| Internationally Defined Level | Finished University | Some Vocational-Technical Education After Secondary School or Some University | Finished Secondary School |
| Australia § |  |  |  |
| Belgium (Flemish) § |  | Post-Secondary Tertiary Higher Education Outside University or Some Years of University | Finish Higher Secondary School |
| Canada | Finish University or College | Some Vocational-Technical Education After Secondary School or Some University or College |  |
| Chile |  |  |  |
| Cyprus s | University Degree |  | Finish Upper Secondary |
| Czech Republic (P) ${ }^{\text {¢ } \ddagger}$ | Finish University (4-5 years university study) | Some Vocational-Technical Education After Secondary School or Some University | Vocational Training or Secondary With Maturita |
| Czech Republic (S) | Finish University (4-5 years university study) | Medium-cycle higher education or bachelor studies (3 years university study or special higher education) | Vocational Training or Secondary With Maturita |
| Finland |  |  | Finish secondary school (about 12 years) |
| Hungary § | University or College Degree | Not Included | Apprenticeship (3-year trade school) or Final Exam in Secondary School (4-year academic/vocational) |
| Indonesia | Completed University Degree (Sarjana $1 / 2 / 3)$ | Academy ( 3 years or less of higher education outside university - Diploma D1/D2/D3) or Some University (Did Not Complete Degree) | Finish Secondary (SMP, SMA, SMEA, STM, etc.) |
| Italy s | Finish University (Laurea or Dottorato di Ricerca; 4-6 Year Diploma) | Vocational/Professional Course After Secondary Diploma or Some University (2-3 Year Short-Course Diploma) | Finish Secondary School With Maturita (Classical/Technical) or Vocational Training Diploma |
| Japan (S) ${ }^{3}$ | University or Graduate School | Vocational/Technical Education After Secondary or 2-year college | Upper secondary |
| Korea, Rep. of \$ |  |  |  |
| Latvia (LSS) § | Higher Education (5 years) | Vocational School (Post-Secondary) or Technikum (3 years) or Some Higher Education | Finish Secondary or Vocational School (11 years) |
| Lithuania § | University or Other Higher Education | Vocational or Agricultural School or College (Technical, Art, Music) |  |
| Netherlands | University With Diploma | Vocational/Technical Education After Secondary (bv.heao, hts, pedagogical academy) or Some Years At University (Without Diploma) | Finish Secondary School With Diploma |
| New Zealand (P) $\ddagger$ | University or Teachers' College (College of Education) | Vocational/Polytechnic Education After Secondary School or Some University | Complete Form 6 or Form 7 |
| New Zealand (S) § | University, College of Education (teacher training) or degree or national diploma course at polytech | Certificate course at polytech (e.g, trade certificate) or some university | Finish secondary school (complete Form 6 or Form 7) |
| Philippines § | Finish College/University | Some Vocational/Technical Education After High School or Some College/University | Finish High School |
| Romania § | Finish University (facultate) | Post-Secondary Technical School or Did Not Complete University | Finish Senior Secondary (liceu) |
| Singapore s |  | Finish JC/Pre-U or Polytechnic or Some Other Vocational/Technical Education After Secondary (e.g., ITE, VITB)' [includes GCE 'A' level, which is 2 years additional schooling beyond completion of secondary.] | Finish Secondary School |
| Slovenia (S) ${ }^{\text {5 }}$ |  |  | Finish gymnasium or secondary school |
| South Africa § |  | Finish Technikon or Some University | Finish Secondary |
| Thailand § | Graduate level (Finish Tertiary Education, 4 years) | Diploma/Undergraduate Level (higher certificate, 2 years) | Finish Academic or Vocational/Technical Upper-Secondary Track |
| Tunisia | Bachelor's Degree (BA) |  |  |
| United States (P) $\ddagger$ | Completed Bachelor's Degree at College or University | Some Vocational-Technical Education After Secondary School or Some Community College, College or University Courses | Finish High School |
| United States (S) s | Finish community college, college or university | Some Vocational-Technical Education After Secondary School or Some Community College, College or University Courses | Finish High School |

National educational level is the same as the internationally-defined level

* Educational levels were translated and defined in most countries to be comparable to the interna-tionally-defined levels. Countries that used modified response options to conform to their national education systems are indicated to aid in the interpretation of the reporting categories in exhibits 4.4 and R1.5. National modifications pertain to both the parents' education and students' expectations questions unless otherwise indicated.
1 Upper-secondary corresponds to ISCED level 3 tracks terminating after 11 to 13 years in most countries. (Education at a Glance, OECD, 1995.)

2 Primary school or lower educational levels were included only in the parents' education question.
3 Japan administered the question pertaining to students' expectations but not the question pertaining to parents education.
§ Some educational levels modified from 1995.
$\ddagger$ Educational levels differ for the parents' education (P) question and the students' expectations (S) question

Exhibit R1.6: Country Modifications to the Definitions of Educational Levels for Parents' Education or Students'
TIMSS 1999 Expectations for Finishing School* (Continued)

| Finished Primary School But Not Upper Secondary School |  | Did Not Finish Primary School ${ }^{2}$ |  |
| :---: | :---: | :---: | :---: |
| Lower-Secondary Level | Primary Level ${ }^{2}$ |  |  |
| Finished Some Secondary School | Finished Primary School | Some Primary School or Did Not Go to School | Internationally Defined Level |
|  |  | Less Than Year 6 in Primary School | Australia |
| Finish Lower Secondary School | Finish Basic School | Some Years of Basic School or Did Not Go to School | Belgium (Flemish) |
|  |  |  | Canada |
|  | Finish Primary School (grade 8) |  | Chile |
| Finish Lower Secondary (Gymnasium - grade 9) |  |  | Cyprus |
| Vocational Training or Secondary School Without Maturita |  | Not Included | Czech Republic (P) |
| Vocational Training or Secondary School Without Maturita |  |  | Czech Republic (S) |
| Some Secondary School (10-11 years) | Finish Primary School (about 9 years) | Did Not Go to School, Primary School or Part of Lower Secondary (< 9 years) | Finland |
| Finish General School (grade 8) | Some General School | Not Included | Hungary |
|  | Finish Primary School (SD) |  | Indonesia |
| Finish Middle School |  |  | Italy |
| Lower Secondary |  |  | Japan (S) |
| Some High School | Finish Middle School | Some middle school or did not go to school | Korea, Rep. of |
|  |  |  | Latvia (LSS) |
|  | Finish Basic School (grade 10) | Some Basic School or Did Not Go to School | Lithuania |
| Some Years of Secondary School (mavo, havo, vwo) without Diploma | Finish Primary School (grade 8) |  | Netherlands |
|  |  |  | New Zealand (P) |
|  |  |  | New Zealand (S) |
| Some High School | Finish Elementary School | Some Elementary School or Did Not Go to School | Philippines |
| Did Not Complete Senior Secondary | Finish Junior Secondary (Gymnasium - grade 8) | Did Not Finish Grade 8 or Did Not Go to School | Romania |
|  |  |  | Singapore |
|  |  |  | Slovenia (S) |
|  |  |  | South Africa |
| Finish Lower Secondary School | Finish Upper Primary School | Finish Lower Primary School or Did Not Go to School | Thailand |
|  |  |  | Tunisia |
| Some High School | Finish Elementary School | Finish elementary school or did not go to school | United States (P) |
| Some High School |  |  | United States (S) |


|  | Percentage of Students Agreeing That It Is Important to Do Each Activity |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Do Well in Mathematics | Do Well in Science | Do Well in Language | Have Time to Have Fun | Be Good at Sports |
| Australia | 97 (0.3) | 92 (0.6) | 97 (0.4) | 99 (0.2) | 83 (0.8) |
| Belgium (Flemish) | 98 (0.3) | 91 (0.8) | 96 (0.4) | 98 (0.4) | 77 (0.9) |
| Bulgaria | 96 (0.6) | 91 (0.8) | 96 (0.5) | 96 (0.5) | 83 (1.0) |
| Canada | 98 (0.2) | 95 (0.4) | 97 (0.5) | 99 (0.2) | 82 (0.6) |
| Chile | 99 (0.2) | 98 (0.2) | 98 (0.2) | 98 (0.3) | 95 (0.4) |
| Chinese Taipei | 89 (0.5) | 89 (0.5) | 89 (0.5) | 99 (0.1) | 94 (0.3) |
| Cyprus | 96 (0.3) | 91 (0.5) | 96 (0.3) | 97 (0.3) | 90 (0.5) |
| Czech Republic | 98 (0.3) | 93 (0.6) | 97 (0.4) | 97 (0.4) | 82 (1.0) |
| England | 99 (0.2) | 97 (0.3) | 99 (0.2) | 98 (0.3) | 79 (0.9) |
| Finland | 93 (0.6) | 84 (0.9) | 91 (0.6) | 96 (0.4) | 82 (1.0) |
| Hong Kong, SAR | 95 (0.4) | 86 (0.7) | 96 (0.4) | 97 (0.3) | 84 (0.6) |
| Hungary | 97 (0.3) | 87 (0.6) | 97 (0.4) | 96 (0.4) | 68 (0.9) |
| Indonesia | 97 (0.3) | 98 (0.2) | 98 (0.2) | 71 (1.0) | 96 (0.3) |
| Iran, Islamic Rep. | 96 (0.4) | 96 (0.3) | 94 (0.5) | 89 (0.6) | 93 (0.5) |
| Israel | 98 (0.3) | 90 (0.7) | 92 (0.6) | 96 (0.4) | 86 (0.7) |
| Italy | 97 (0.4) | 94 (0.5) | 97 (0.3) | 98 (0.3) | 89 (0.6) |
| Japan | 88 (0.5) | 83 (0.7) | 89 (0.6) | 99 (0.2) | 82 (0.6) |
| Jordan | 96 (0.4) | 97 (0.3) | 95 (0.4) | 87 (0.7) | 89 (0.5) |
| Korea, Rep. of | 90 (0.4) | 87 (0.5) | 89 (0.4) | 92 (0.3) | 88 (0.5) |
| Latvia (LSS) | 98 (0.3) | 86 (0.9) | 98 (0.3) | 97 (0.3) | 88 (0.7) |
| Lithuania ${ }^{\text { }}$ | 97 (0.4) | 84 (1.0) | 98 (0.3) | 96 (0.4) | 92 (0.6) |
| Macedonia, Rep. of | 95 (0.4) | 96 (0.4) | 97 (0.3) | 94 (0.5) | 95 (0.4) |
| Malaysia | 99 (0.1) | 99 (0.1) | 99 (0.2) | 78 (1.0) | 93 (0.5) |
| Moldova | 93 (0.7) | 95 (0.6) | 95 (0.4) | 92 (0.7) | 91 (0.5) |
| Morocco | $r \quad 91$ (0.5) | 92 (0.6) | 90 (0.5) | 65 (1.1) | 91 (0.5) |
| Netherlands | 98 (0.3) | 94 (0.9) | 99 (0.3) | 98 (0.3) | 76 (1.5) |
| New Zealand | 97 (0.3) | 93 (0.5) | 97 (0.3) | 98 (0.2) | 86 (0.8) |
| Philippines | 91 (0.6) | 93 (0.5) | 90 (0.8) | 78 (1.0) | 87 (0.7) |
| Romania | 97 (0.4) | 94 (0.6) | 98 (0.3) | 91 (0.8) | 83 (1.0) |
| Russian Federation | 97 (0.4) | 96 (0.3) | 97 (0.4) | 98 (0.3) | 90 (0.6) |
| Singapore | 99 (0.2) | 98 (0.2) | 100 (0.1) | 93 (0.6) | 90 (0.5) |
| Slovak Republic | 99 (0.2) | 96 (0.5) | 99 (0.2) | 99 (0.2) | 91 (0.7) |
| Slovenia | 91 (0.6) | 80 (0.9) | 92 (0.5) | 97 (0.3) | 87 (0.7) |
| South Africa | 90 (0.5) | 89 (1.3) | 91 (0.6) | 72 (1.1) | 83 (0.7) |
| Thailand | 95 (0.3) | 96 (0.3) | 97 (0.3) | 92 (0.5) | 95 (0.3) |
| Tunisia | 96 (0.5) | 97 (0.3) | 96 (0.3) | 83 (0.7) | 91 (0.5) |
| Turkey | 96 (0.3) | 97 (0.3) | 97 (0.2) | 75 (1.0) | 86 (0.6) |
| United States | 97 (0.3) | 96 (0.3) | 96 (0.3) | 99 (0.2) | 84 (0.6) |
| International Avg. | 96 (0.1) | 92 (0.1) | 96 (0.1) | 92 (0.1) | 87 (0.1) |

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An "r" indicates a $70-84 \%$ student response rate.

## Exhibit R1.8 $\quad$ Students' Perception of Their Mothers' View of the Importance of Various Activities

TIMSS1999
$\overbrace{}^{\text {th }}$
Mathematics

|  | Percentage of Students Agreeing That Their Mothers Think It Is Important to Do Each Activity |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Do Well in Mathematics | Do Well in Science | Do Well in Language | Have Time to Have Fun | Be Good at Sports |
| Australia | 98 (0.2) | 96 (0.4) | 98 (0.3) | 95 (0.5) | 78 (0.7) |
| Belgium (Flemish) | 97 (0.4) | 92 (0.6) | 97 (0.5) | 96 (0.5) | 66 (1.6) |
| Bulgaria | 97 (0.3) | 92 (0.6) | 96 (0.6) | 90 (0.7) | 79 (1.3) |
| Canada | 99 (0.1) | 98 (0.3) | 99 (0.2) | 96 (0.4) | 76 (0.8) |
| Chile | 99 (0.2) | 98 (0.2) | 99 (0.2) | 93 (0.5) | 95 (0.4) |
| Chinese Taipei | 95 (0.5) | 95 (0.4) | 93 (0.4) | 95 (0.3) | 91 (0.4) |
| Cyprus | 96 (0.4) | 92 (0.5) | 97 (0.3) | 95 (0.4) | 85 (0.8) |
| Czech Republic | 99 (0.2) | 96 (0.5) | 99 (0.3) | 90 (0.7) | 72 (1.1) |
| England | 99 (0.2) | 98 (0.3) | 99 (0.2) | 94 (0.5) | 74 (1.0) |
| Finland | 96 (0.4) | 90 (0.7) | 95 (0.4) | 88 (0.7) | 74 (1.1) |
| Hong Kong, SAR | 96 (0.3) | 87 (0.7) | 97 (0.3) | 82 (0.7) | 73 (0.9) |
| Hungary | 97 (0.4) | 86 (0.7) | 97 (0.3) | 83 (0.8) | 46 (1.1) |
| Indonesia | 97 (0.3) | 98 (0.3) | 98 (0.2) | 65 (1.0) | 95 (0.4) |
| Iran, Islamic Rep. | 94 (0.4) | 94 (0.5) | 93 (0.5) | 82 (0.8) | 89 (0.6) |
| Israel | 98 (0.2) | 94 (0.5) | 96 (0.3) | 94 (0.4) | 83 (0.8) |
| Italy | 99 (0.3) | 97 (0.3) | 99 (0.2) | 95 (0.4) | 84 (0.8) |
| Japan | 92 (0.5) | 87 (0.6) | 92 (0.5) | 94 (0.4) | 82 (0.6) |
| Jordan | 95 (0.4) | 96 (0.3) | 95 (0.5) | 82 (0.8) | 86 (0.7) |
| Korea, Rep. of | 95 (0.3) | 90 (0.4) | 92 (0.4) | 66 (0.7) | 78 (0.6) |
| Latvia (LSS) | 98 (0.4) | 90 (0.7) | 98 (0.3) | 90 (0.7) | 82 (0.7) |
| Lithuania ${ }^{\text { }}$ | 95 (0.5) | 80 (1.0) | 97 (0.4) | 85 (0.8) | 86 (0.8) |
| Macedonia, Rep. of | 96 (0.3) | 97 (0.3) | 97 (0.3) | 91 (0.7) | 91 (0.6) |
| Malaysia | 99 (0.1) | 98 (0.2) | 98 (0.2) | 66 (1.2) | 90 (0.5) |
| Moldova | 91 (0.6) | 91 (0.6) | 93 (0.6) | 85 (0.9) | 86 (0.7) |
| Morocco | 88 (0.7) | 86 (0.7) | 88 (0.6) | 53 (1.2) | 86 (0.7) |
| Netherlands | 98 (0.3) | 94 (0.8) | 98 (0.3) | 97 (0.5) | 59 (1.9) |
| New Zealand | 98 (0.2) | 96 (0.3) | 98 (0.2) | 95 (0.4) | 84 (0.9) |
| Philippines | 90 (0.7) | 93 (0.5) | 89 (0.8) | 75 (0.8) | 85 (0.6) |
| Romania | 97 (0.5) | 96 (0.7) | 98 (0.4) | 79 (1.0) | 75 (1.5) |
| Russian Federation | 96 (0.4) | 96 (0.4) | 97 (0.4) | 92 (0.4) | 86 (0.7) |
| Singapore | 99 (0.2) | 98 (0.2) | $98(0.2)$ | 76 (0.9) | 80 (0.7) |
| Slovak Republic | 99 (0.2) | 98 (0.3) | 99 (0.2) | 96 (0.4) | 89 (0.8) |
| Slovenia | 91 (0.5) | 83 (0.8) | 94 (0.5) | 89 (0.6) | 82 (0.9) |
| South Africa | 89 (0.6) | 89 (1.2) | 91 (0.6) | 70 (1.0) | 81 (0.8) |
| Thailand | 94 (0.4) | 96 (0.3) | 97 (0.3) | 80 (0.7) | 93 (0.4) |
| Tunisia | 92 (0.7) | 96 (0.3) | 94 (0.4) | 72 (0.7) | 87 (0.5) |
| Turkey | 94 (0.5) | 95 (0.4) | 95 (0.4) | 67 (1.0) | 79 (0.9) |
| United States | 98 (0.2) | 98 (0.2) | 98 (0.2) | 93 (0.4) | 76 (0.6) |
| International Avg. | 96 (0.1) | 93 (0.1) | 96 (0.1) | 85 (0.1) | 81 (0.1) |

[^71]Exhibit R1.9 Students' Perception of Their Friends' View of the Importance of Various Activities

TIMSS 1999
$\overbrace{-}^{\text {th }}$
Mathematics


Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

An "r" indicates a 70-84\% student response rate.

|  | Percentage of Students Reporting |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | To Get Desired Job |  |  | To Please Parents |  |  | To Get Into Desired Secondary School or University |  |  |
|  | Strongly Agree | Agree | Disagree/ Strongly Disagree | Strongly Agree | Agree | Disagree/ Strongly Disagree | Strongly Agree | Agree | Disagree/ Strongly Disagree |
| Australia | 37 (1.2) | 42 (1.0) | 21 (1.0) | 24 (1.0) | 48 (1.0) | 29 (1.0) | 36 (1.2) | 44 (1.0) | 20 (1.0) |
| Belgium (Flemish) | 18 (1.2) | 40 (1.4) | 42 (1.1) | 15 (0.6) | 52 (1.2) | 33 (1.1) | 24 (0.8) | 46 (1.3) | 30 (1.2) |
| Bulgaria | 45 (1.2) | 39 (1.1) | 16 (1.0) | 25 (1.1) | 36 (1.3) | 40 (1.3) | 50 (1.4) | 36 (1.3) | 14 (0.9) |
| Canada | 43 (1.1) | 40 (0.9) | 17 (0.6) | 25 (0.5) | 46 (0.6) | 30 (0.6) | 57 (0.8) | 36 (0.6) | 7 (0.5) |
| Chile | 52 (1.0) | 33 (0.8) | 15 (0.6) | 38 (0.9) | 35 (0.7) | 27 (1.0) | 66 (0.9) | 26 (0.8) | 7 (0.5) |
| Chinese Taipei | 27 (0.7) | 50 (0.8) | 23 (0.9) | 29 (0.8) | 50 (0.6) | 20 (0.7) | 42 (0.9) | 46 (0.7) | 11 (0.5) |
| Cyprus | 55 (1.2) | 33 (1.1) | 12 (0.6) | 29 (0.9) | 37 (0.8) | 35 (0.9) | 53 (1.1) | 32 (1.0) | 16 (0.7) |
| Czech Republic | 32 (1.2) | 48 (1.2) | 20 (1.0) | 22 (1.1) | 56 (1.0) | 22 (1.0) | 46 (1.3) | 39 (1.0) | 15 (0.9) |
| England | 36 (1.2) | 41 (1.0) | 23 (1.0) | 21 (1.0) | 41 (0.9) | 38 (1.0) | 43 (1.3) | 42 (1.1) | 15 (0.9) |
| Finland | 22 (1.1) | 46 (1.0) | 32 (1.3) | 8 (0.6) | 35 (1.1) | 57 (1.1) | 25 (1.0) | 56 (1.0) | 19 (0.9) |
| Hong Kong, SAR | 28 (0.8) | 53 (0.8) | 19 (0.6) | 26 (0.7) | 55 (0.7) | 19 (0.7) | 29 (0.8) | 49 (0.8) | 22 (0.8) |
| Hungary | 25 (0.9) | 58 (1.0) | 16 (0.8) | 8 (0.5) | 45 (1.0) | 47 (1.1) | 33 (1.0) | 49 (1.0) | 18 (1.0) |
| Indonesia | 46 (0.9) | 50 (0.8) | 4 (0.3) | 45 (0.9) | 50 (0.8) | 5 (0.4) | 46 (0.9) | 49 (0.7) | 5 (0.3) |
| Iran, Islamic Rep. | 50 (1.3) | 35 (0.8) | 15 (0.8) | 60 (1.1) | 34 (1.0) | 6 (0.4) | 59 (1.3) | 32 (1.1) | 9 (0.7) |
| Israel | 51 (1.3) | 31 (0.9) | 18 (0.8) | 37 (1.0) | 35 (1.0) | 29 (0.8) | 66 (1.2) | 27 (1.0) | 7 (0.5) |
| Italy | 30 (0.7) | 45 (1.0) | 24 (0.8) | 27 (1.0) | 51 (1.0) | 22 (0.9) | 33 (0.7) | 46 (1.0) | 20 (0.9) |
| Japan | 12 (0.5) | 39 (0.7) | 49 (1.0) | 6 (0.4) | 25 (0.7) | 69 (0.8) | 34 (0.8) | 54 (0.7) | 11 (0.7) |
| Jordan | 60 (0.8) | 30 (0.8) | 10 (0.5) | 59 (1.0) | 30 (0.9) | 11 (0.7) | 69 (0.9) | 23 (0.7) | 7 (0.6) |
| Korea, Rep. of | 10 (0.5) | 34 (0.6) | 56 (0.7) | 12 (0.5) | 50 (0.7) | 38 (0.7) | 31 (0.7) | 54 (0.7) | 15 (0.5) |
| Latvia (LSS) | 36 (1.2) | 50 (1.3) | 14 (0.8) | 21 (0.9) | 52 (1.1) | 27 (1.2) | 47 (1.2) | 46 (1.1) | 7 (0.5) |
| Lithuania ${ }^{\text { }}$ | 43 (1.3) | 46 (1.3) | 11 (0.9) | 10 (0.7) | 28 (1.2) | 62 (1.2) | 44 (1.3) | 44 (1.3) | 12 (0.9) |
| Macedonia, Rep. of | 41 (1.1) | 40 (1.0) | 19 (0.8) | 35 (1.1) | 34 (0.9) | 31 (1.2) | 53 (1.0) | 37 (0.9) | 9 (0.5) |
| Malaysia | 61 (1.0) | 34 (0.9) | 5 (0.3) | 59 (1.2) | 35 (0.9) | 7 (0.6) | 64 (1.1) | 32 (1.0) | 4 (0.4) |
| Moldova | 40 (1.1) | 46 (1.1) | 14 (0.8) | 31 (1.2) | 47 (1.0) | 23 (1.2) | 39 (1.1) | 47 (0.9) | 15 (0.8) |
| Morocco | r 59 (0.9) | 32 (0.9) | 10 (0.6) | r 61 (0.8) | 31 (0.7) | 8 (0.6) | r 58 (0.9) | 33 (0.8) | 9 (0.7) |
| Netherlands | 18 (1.2) | 37 (0.9) | 45 (1.3) | 7 (0.8) | 36 (1.2) | 57 (1.3) | 20 (1.2) | 45 (1.1) | 35 (1.6) |
| New Zealand | 41 (1.1) | 43 (0.9) | 17 (0.8) | 24 (1.0) | 46 (0.9) | 31 (0.9) | 39 (1.0) | 45 (1.0) | 16 (0.9) |
| Philippines | 44 (1.1) | 44 (0.8) | 11 (0.7) | 34 (0.8) | 48 (0.7) | 19 (0.7) | 47 (1.0) | 41 (0.8) | 12 (0.7) |
| Romania | 40 (1.3) | 48 (1.2) | 12 (0.8) | 34 (1.3) | 49 (1.1) | 17 (1.4) | 45 (1.3) | 43 (1.1) | 12 (0.8) |
| Russian Federation | 42 (1.1) | 42 (1.0) | 16 (0.8) | 20 (0.7) | 40 (1.0) | 39 (1.3) | 40 (1.0) | 48 (1.0) | 12 (0.6) |
| Singapore | 40 (1.0) | 46 (0.8) | 13 (0.6) | 26 (0.8) | 46 (0.6) | 28 (0.8) | 54 (1.1) | 41 (1.0) | 5 (0.4) |
| Slovak Republic | 31 (1.1) | 53 (1.1) | 17 (1.0) | 13 (0.8) | 47 (1.3) | 40 (1.6) | 49 (1.1) | 45 (0.9) | 6 (0.5) |
| Slovenia | 25 (1.0) | 52 (1.0) | 24 (1.0) | 6 (0.6) | 26 (0.9) | 67 (1.1) | 35 (1.0) | 54 (1.0) | 11 (0.6) |
| South Africa | 58 (0.9) | 29 (0.6) | 13 (0.7) | 43 (1.0) | 35 (1.0) | 22 (0.8) | 57 (1.0) | 28 (0.7) | 15 (0.6) |
| Thailand | 43 (0.9) | 52 (0.9) | 5 (0.4) | 50 (0.9) | 47 (0.9) | 3 (0.3) | 54 (1.0) | 42 (0.9) | 4 (0.3) |
| Tunisia | 51 (1.0) | 33 (0.9) | 16 (0.6) | 36 (0.9) | 42 (0.7) | 22 (0.8) | 51 (0.9) | 34 (0.7) | 15 (0.6) |
| Turkey | 43 (0.8) | 44 (0.7) | 13 (0.6) | 36 (0.9) | 42 (0.8) | 22 (0.8) | 55 (0.8) | 38 (0.7) | 8 (0.3) |
| United States | 41 (0.8) | 40 (0.7) | 18 (0.6) | 34 (0.8) | 47 (0.7) | 19 (0.6) | 58 (1.2) | 36 (1.0) | 6 (0.3) |
| International Avg. | 39 (0.2) | 42 (0.2) | 19 (0.1) | 29 (0.1) | 42 (0.1) | 30 (0.2) | 46 (0.2) | 41 (0.2) | 13 (0.1) |

## Background data provided by students.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An "r" indicates a $70-84 \%$ student response rate.


Background data provided by students.
1 Average hours based on: No time $=0$; less than 1 hour $=5 ; 1-2$ hours $=1.5 ; 3-5$ hours $=4$; more than 5 hours=7.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent

A dash (-) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate. An "s" indicates a $50-69 \%$ student response rate.

|  | Spend Any Time Studying All Three Mathematics, Science, and Other Subjects |  |  | Spend At Least 3 Hours Studying Across Subjects |  |  | Spend 1 Hour or More Studying Mathematics |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 | 1995-1999 Difference |  | Percent of Students 1999 | 1995-1999 Difference |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  |
| Australia | 74 (1.6) | 4 (2.1) |  | 17 (0.9) | 1 (1.1) | - | 22 (1.0) | 1 (1.4) | - |
| Belgium (Flemish) | 85 (1.2) | -3 (1.5) |  | 41 (1.3) | -1 (2.0) | - | 47 (1.2) | 1 (2.0) | - |
| Canada | 78 (1.0) | 7 (2.0) | - | 24 (0.8) | 4 (1.3) | $\triangle$ | 28 (1.0) | 4 (1.5) | - |
| Cyprus | 79 (0.8) | 4 (1.2) | - | 35 (1.1) | -5 (1.4) | V | 40 (1.1) | -7 (1.4) | V |
| Czech Republic | 74 (1.4) | 5 (2.2) | $\bullet$ | 16 (1.1) | 3 (1.3) | - | 20 (1.1) | 4 (1.5) | - |
| England | - - | -- |  | -- | -- |  | -- | -- |  |
| Hong Kong, SAR | 53 (1.3) | -17 (2.1) | $\nabla$ | 16 (0.8) | -12 (1.4) | V | 24 (1.1) | -10 (1.6) | V |
| Hungary | 90 (0.8) | 2 (1.1) | - | 40 (1.3) | 2 (1.9) | - | 25 (1.1) | -3 (1.6) | - |
| Iran, Islamic Rep. | 92 (0.5) | -3 (0.7) | V | 69 (1.1) | S $\quad-4$ (1.9) | $\bullet$ | 75 (1.0) | -3 (1.5) | - |
| Israel ${ }^{\dagger}$ | 80 (0.9) | 4 (1.7) | - | 33 (1.7) | 2 (2.5) | - | 44 (1.5) | 3 (2.9) | - |
| Italy | 92 (0.8) | 0 (1.2) | - | 60 (1.6) | 0 (2.2) | - | 57 (1.6) | -1 (2.4) | - |
| Japan | 59 (1.4) | -13 (1.9) | $\nabla$ | 17 (0.9) | -10 (1.3) | $\nabla$ | 20 (0.9) | -10 (1.3) | V |
| Korea, Rep. of | 50 (0.9) | -15 (1.6) | $\nabla$ | 16 (0.7) | -11 (1.4) | $\nabla$ | 21 (0.9) | -12 (1.5) | V |
| Latvia (LSS) | 89 (0.7) | 9 (1.6) | $\triangle$ | 40 (1.2) | 13 (1.6) | $\triangle$ | 40 (1.3) | 8 (1.8) | $\triangle$ |
| Lithuania | 89 (1.0) | 7 (1.5) | $\triangle$ | 35 (1.2) | 10 (1.8) | $\triangle$ | 29 (1.3) | 5 (1.7) | - |
| Netherlands | 89 (1.1) | -1 (1.6) | - | 19 (1.4) | 3 (1.6) | - | 14 (1.5) | 3 (1.8) | - |
| New Zealand | 76 (1.3) | 0 (1.8) | $\bullet$ | 17 (1.0) | 1 (1.3) | - | 20 (1.2) | 2 (1.5) | - |
| Romania | 76 (1.2) | 1 (1.8) | - | 55 (1.6) | r 4 (2.2) | - | 66 (1.8) | 3 (2.6) | - |
| Russian Federation | 89 (0.7) | 4 (1.1) | - | 48 (1.3) | 13 (1.9) | $\triangle$ | 45 (1.5) | 10 (1.9) | - |
| Singapore | 90 (0.8) | -2 (1.0) | - | 59 (1.2) | -18 (1.5) | $\nabla$ | 61 (1.1) | -16 (1.5) | V |
| Slovak Republic | 88 (0.8) | 4 (1.3) | $\triangle$ | 24 (0.9) | 2 (1.3) | - | 23 (0.9) | 4 (1.4) | - |
| Slovenia | 85 (1.0) | -1 (1.3) | - | 32 (1.0) | -3 (1.4) | - | 29 (1.0) | -6 (1.5) | V |
| Thailand ${ }^{\text {+ }}$ | 88 (0.6) | -3 (1.0) | $\bullet$ | 45 (1.2) | -6 (2.0) | V | 49 (1.2) | -6 (2.2) | - |
| United States | 72 (1.6) | 1 (2.1) | - | 22 (0.8) | 0 (1.1) | - | 27 (1.1) | 0 (1.5) | - |
| International Avg. s | 79 (0.2) | 0 (0.4) | - | 33 (0.2) | 0 (0.4) | - | 35 (0.3) | -1 (0.4) | - |



[^72]Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates a $50-69 \%$ student response rate, based on the lower response rate in either 1995 or 1999.

| Australia <br> Belgium (Flemish) | Average Hours Spent Each Day ${ }^{1}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Watching Television or Videos | Playing Computer Games | Playing or Talking With Friends | Doing Jobs at Home | Playing Sports | Reading a Book for Enjoyment |
|  | 2.3 (0.05) | 0.8 (0.03) | 1.5 (0.03) | 0.9 (0.03) | 1.6 (0.03) | 0.6 (0.02) |
|  | 2.1 (0.04) | 0.9 (0.04) | 1.8 (0.05) | 1.0 (0.04) | 1.8 (0.07) | 0.6 (0.02) |
| Bulgaria | 2.8 (0.05) | 0.8 (0.04) | 2.6 (0.06) | 1.9 (0.04) | 1.5 (0.05) | 1.0 (0.03) |
| Canada | 2.2 (0.03) | 0.8 (0.02) | 2.1 (0.04) | 1.1 (0.03) | 1.9 (0.03) | 0.7 (0.04) |
| Chile | 2.7 (0.05) | 0.6 (0.02) | 1.9 (0.04) | 1.5 (0.03) | 2.0 (0.03) | 0.7 (0.02) |
| Chinese Taipei | 2.0 (0.04) | 0.9 (0.03) | 1.3 (0.03) | 1.0 (0.02) | 1.2 (0.02) | 0.9 (0.02) |
| Cyprus | 2.2 (0.04) | 1.0 (0.03) | 1.8 (0.04) | 0.9 (0.03) | 1.4 (0.04) | 0.7 (0.02) |
| Czech Republic | 2.3 (0.05) | 0.9 (0.06) | 3.0 (0.07) | 1.2 (0.03) | 2.0 (0.05) | 1.0 (0.04) |
| England | 2.6 (0.05) | 1.2 (0.04) | 2.5 (0.08) | 0.8 (0.02) | 1.6 (0.04) | 0.6 (0.02) |
| Finland | 2.5 (0.04) | 1.1 (0.03) | 3.2 (0.07) | 0.9 (0.02) | 1.6 (0.04) | 0.8 (0.02) |
| Hong Kong, SAR | 2.4 (0.04) | 1.0 (0.03) | 1.3 (0.04) | 0.6 (0.01) | 1.0 (0.03) | 0.8 (0.02) |
| Hungary | 2.7 (0.05) | 1.0 (0.03) | 2.0 (0.05) | 1.6 (0.04) | 1.5 (0.04) | 0.8 (0.02) |
| Indonesia | 1.7 (0.05) | 0.2 (0.02) | 1.1 (0.02) | 1.9 (0.03) | 1.0 (0.02) | 0.9 (0.02) |
| Iran, Islamic Rep. | 1.8 (0.04) | 0.3 (0.03) | 1.3 (0.04) | 1.7 (0.04) | 1.3 (0.06) | 0.9 (0.02) |
| Israel | 3.1 (0.05) | 1.5 (0.04) | 2.4 (0.04) | 1.3 (0.05) | 1.8 (0.05) | 1.0 (0.03) |
| Italy | 1.8 (0.03) | 1.0 (0.03) | 2.7 (0.05) | 1.1 (0.03) | 1.7 (0.03) | 0.7 (0.02) |
| Japan | 3.1 (0.05) | 0.9 (0.03) | 1.8 (0.04) | 0.5 (0.02) | 1.1 (0.03) | 0.8 (0.02) |
| Jordan | 1.7 (0.04) | 0.8 (0.04) | 1.1 (0.04) | 1.3 (0.05) | 1.4 (0.05) | 1.4 (0.04) |
| Korea, Rep. of | 2.9 (0.04) | 0.8 (0.03) | 1.3 (0.03) | 0.6 (0.01) | 0.6 (0.02) | 0.6 (0.01) |
| Latvia (LSS) | 2.8 (0.05) | 0.7 (0.03) | 2.6 (0.06) | 1.7 (0.03) | 1.3 (0.03) | 0.9 (0.03) |
| Lithuania ${ }^{\text {* }}$ | 2.4 (0.05) | 0.6 (0.03) | 2.4 (0.06) | 1.6 (0.05) | 1.0 (0.03) | 0.7 (0.02) |
| Macedonia, Rep. of | 2.2 (0.05) | 0.7 (0.04) | 1.8 (0.05) | 1.9 (0.04) | 1.8 (0.05) | 1.2 (0.04) |
| Malaysia | 1.9 (0.05) | 0.5 (0.02) | 1.2 (0.03) | 1.8 (0.03) | 1.1 (0.02) | 1.1 (0.02) |
| Moldova | 2.6 (0.07) | 1.0 (0.05) | 1.9 (0.06) | 3.2 (0.09) | 1.4 (0.04) | 1.5 (0.04) |
| Morocco | 1.1 (0.03) | $r \quad 0.7$ (0.02) | 0.9 (0.03) | 1.5 (0.03) | 1.5 (0.04) | 1.4 (0.05) |
| Netherlands | 2.4 (0.10) | 0.9 (0.04) | 2.6 (0.09) | 0.8 (0.04) | 1.8 (0.06) | 0.7 (0.04) |
| New Zealand | 2.5 (0.05) | 0.9 (0.04) | 1.6 (0.04) | 1.0 (0.03) | 1.5 (0.04) | 0.7 (0.02) |
| Philippines | 1.7 (0.04) | 0.7 (0.03) | 1.2 (0.03) | 2.4 (0.05) | 1.6 (0.04) | 1.6 (0.04) |
| Romania | 2.2 (0.06) | 0.6 (0.04) | 1.6 (0.05) | 2.0 (0.06) | 1.2 (0.04) | 1.0 (0.03) |
| Russian Federation | 2.6 (0.05) | 0.7 (0.03) | 3.0 (0.05) | 1.5 (0.03) | 1.3 (0.03) | 1.2 (0.03) |
| Singapore | 2.4 (0.04) | 1.1 (0.03) | 1.5 (0.04) | 0.9 (0.02) | 1.5 (0.04) | 1.0 (0.02) |
| Slovak Republic | 2.5 (0.06) | 0.6 (0.03) | 2.7 (0.06) | 1.6 (0.05) | 1.9 (0.04) | 0.7 (0.02) |
| Slovenia | 2.3 (0.05) | 0.9 (0.03) | 1.8 (0.04) | 1.2 (0.03) | 1.6 (0.04) | 0.7 (0.02) |
| South Africa | 2.0 (0.07) | 0.8 (0.04) | 1.5 (0.04) | 2.0 (0.04) | 2.0 (0.05) | 1.8 (0.05) |
| Thailand | 2.1 (0.05) | 0.4 (0.02) | 1.6 (0.04) | 1.6 (0.02) | 1.5 (0.03) | 1.0 (0.02) |
| Tunisia | 2.0 (0.04) | 0.9 (0.03) | 1.3 (0.03) | 1.7 (0.04) | 1.9 (0.04) | 1.4 (0.03) |
| Turkey | 1.6 (0.04) | r 0.4 (0.02) | 1.5 (0.03) | 1.1 (0.04) | 1.4 (0.03) | 1.2 (0.03) |
| United States | 2.5 (0.06) | 0.9 (0.02) | 2.4 (0.05) | 1.1 (0.03) | 1.9 (0.03) | 0.6 (0.02) |
| International Avg. | 2.3 (0.01) | 0.8 (0.01) | 1.9 (0.01) | 1.4 (0.01) | 1.5 (0.01) | 1.0 (0.00) |

Background data provided by students.

* Activities are not necessarily exclusive; students may have reported engaging in more than one activity at the same time.
1 Average hours based on: No time $=0$; less than 1 hour $=5 ; 1-2$ hours $=1.5 ; 3-5$ hours $=4$; more than 5 hours $=7$.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An "r" indicates a $70-84 \%$ student response rate.


## Background data provided by students.

[^73]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An "r" indicates a $70-84 \%$ student response rate.

|  | Like a Lot |  | Like |  | Dislike |  | Dislike a Lot |  | Average ${ }^{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |  |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 17 & (0.9) \\ 20 & (0.9) \\ 22 & (1.9) \\ 24 & (1.0) \\ 26 & (1.0) \end{array}$ | $\begin{aligned} & 552 \text { (6.6) } \\ & 598 \text { (5.1) } \\ & 540 \text { (12.0) } \\ & 561 \text { (3.8) } \\ & 416 \text { (6.6) } \end{aligned}$ | 51 (1.0) 46 (1.3) 46 (1.3) 49 (1.6) 47 (0.7) | $\begin{aligned} & 528(5.4) \\ & 562(4.2) \\ & 520(5.3) \\ & 531(2.6) \\ & 392 \text { (4.5) } \end{aligned}$ | $\begin{array}{ll} 23 & (1.0) \\ 24 & (1.3) \\ 23 & (1.3) \\ 18 & (0.8) \\ 20 & (0.8) \end{array}$ | $\begin{aligned} & 512(6.7) \\ & 537(6.8) \\ & 491(5.3) \\ & 513(4.8) \\ & 378(4.5) \end{aligned}$ | 10 (0.7) 10 (0.7) <br> 9 (1.1) <br> 9 (0.5) <br> 6 (0.4) | $\begin{aligned} & 496(6.5) \\ & 518(5.1) \\ & 475(7.7) \\ & 486(4.6) \\ & 364(9.2) \end{aligned}$ | 2.7 $(0.03)$ <br> 2.8 $(0.02)$ <br> 2.8 $(0.04)$ <br> 2.9 $(0.02)$ <br> 2.9 $(0.02)$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 15 & (0.7) \\ 30 & (1.0) \\ 11 & (0.9) \\ 23 & (1.1) \\ 17 & (1.1) \end{array}$ | $\begin{aligned} & 654(5.3) \\ & 513(3.3) \\ & 580(7.9) \\ & 514(6.8) \\ & 558(4.1) \end{aligned}$ | 41 (0.8) <br> 47 (1.1) <br> 44 (1.5) <br> 54 (1.1) <br> 47 (1.4) | $\begin{aligned} & 617 \text { (3.5) } \\ & 472 \text { (2.8) } \\ & 530(4.5) \\ & 497(4.3) \\ & 522(3.6) \end{aligned}$ | $\begin{aligned} & 33(0.8) \\ & 15(0.8) \\ & 34(1.7) \\ & 16(0.9) \\ & 27(1.2) \end{aligned}$ | $\begin{aligned} & 546(5.2) \\ & 452(4.9) \\ & 498(5.6) \\ & 487(5.5) \\ & 508(3.5) \end{aligned}$ | $\begin{array}{r} 12(0.6) \\ 8(0.6) \\ 11(0.8) \\ 6(0.5) \\ 9(1.0) \end{array}$ | $\begin{aligned} & 502(5.3) \\ & 426(5.4) \\ & 489(7.6) \\ & 470(8.7) \\ & 480(6.8) \end{aligned}$ | 2.6 $(0.02)$ <br> 3.0 $(0.02)$ <br> 2.5 $(0.03)$ <br> 3.0 $(0.02)$ <br> 2.7 $(0.03)$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | $\begin{aligned} & 22(0.7) \\ & 14(0.7) \\ & 22(1.2) \\ & 35(1.1) \\ & 29 \end{aligned}(1.2)$ | 610 (4.7) <br> 592 (7.6) <br> 418 (6.9) <br> 447 (5.4) <br> 469 (7.7) | 53 (0.7) <br> 48 (1.3) <br> 70 (1.0) <br> 49 (0.9) <br> 45 (0.9) | 587 (4.0) <br> 537 (4.1) <br> 403 (4.9) <br> 416 (3.1) <br> 476 (4.3) | $\begin{array}{r} 20(0.8) \\ 30(1.2) \\ 8(0.7) \\ 10(0.5) \\ 17(0.9) \end{array}$ | $\begin{aligned} & 558(4.7) \\ & 506(4.1) \\ & 377(8.0) \\ & 394(7.5) \\ & 472(5.7) \end{aligned}$ | $\begin{aligned} & 5(0.4) \\ & 8(0.7) \\ & 1(0.1) \\ & 6(0.5) \\ & 8(0.5) \end{aligned}$ | $\begin{gathered} 521(7.3) \\ 501(7.2) \\ \sim \sim \\ 389 \\ (7.1) \\ 429(6.3) \end{gathered}$ | 2.9 $(0.02)$ <br> 2.7 $(0.02)$ <br> 3.1 $(0.02)$ <br> 3.1 $(0.02)$ <br> 3.0 $(0.03)$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 30(1.0) \\ 9(0.5) \\ 41(1.4) \\ 12(0.5) \\ 11(0.7) \end{array}$ | $\begin{aligned} & 517(4.6) \\ & 631(5.7) \\ & 451(5.8) \\ & 647(4.2) \\ & 549(6.7) \end{aligned}$ | $\begin{array}{ll} 38 & (1.1) \\ 39 & (0.9) \\ 41 & (0.9) \\ 42 & (0.8) \\ 50 & (1.3) \end{array}$ | 482 (4.3) <br> 600 (2.2) <br> 425 (3.4) <br> 608 (2.4) <br> 513 (4.1) | $\begin{aligned} & 22(0.8) \\ & 38(1.0) \\ & 11(0.7) \\ & 38(0.7) \\ & 32(1.3) \end{aligned}$ | $\begin{aligned} & 446(5.1) \\ & 563(2.5) \\ & 403(5.6) \\ & 557(2.7) \\ & 486(4.5) \end{aligned}$ | 10 (0.7) <br> 14 (0.6) <br> 7 (0.6) <br> 8 (0.4) <br> 7 (0.6) | $\begin{aligned} & 433(5.8) \\ & 530(4.1) \\ & 411(6.7) \\ & 536(3.8) \\ & 472(7.5) \end{aligned}$ | 2.9 $(0.02)$ <br> 2.4 $(0.02)$ <br> 3.2 $(0.03)$ <br> 2.6 $(0.02)$ <br> 2.6 $(0.02)$ |
| Lithuania Macedonia, Rep. of Malaysia <br> Moldova Morocco | $\begin{aligned} & 16(1.1) \\ & 30 \\ & \hline 0 \\ & 42 \\ & (1.0) \\ & 26 \\ & \hline \end{aligned}(1.0)$ | $\begin{aligned} & 527(7.6) \\ & 460(6.3) \\ & 540(4.7) \\ & 455(5.1) \\ & 352(3.9) \end{aligned}$ | $\begin{aligned} & 55(1.3) \\ & 51(1.0) \\ & 53(1.0) \\ & 17(0.8) \\ & 33 \end{aligned}(0.7)$ | 483 (4.5) <br> 451 (4.2) <br> 505 (4.5) <br> 453 (5.7) <br> 335 (6.6) | $\begin{array}{r} 24(1.2) \\ 14(0.8) \\ 4(0.2) \\ 53(1.4) \\ 9(0.6) \end{array}$ | $\begin{aligned} & 458(5.2) \\ & 440(6.2) \\ & 486(6.1) \\ & 486(4.4) \\ & 307(8.2) \end{aligned}$ | $\begin{aligned} & 4(0.5) \\ & 5(0.4) \\ & 1(0.1) \\ & 4(0.6) \\ & 3(0.3) \end{aligned}$ | $\begin{gathered} 446(12.1) \\ 446 \text { (10.8) } \\ \sim \sim \\ 485(13.1) \\ 308(17.7) \end{gathered}$ | $\begin{array}{ll} 2.8 & (0.02) \\ 3.1 & (0.02) \\ 3.4 & (0.01) \\ 2.6 & (0.02) \\ 3.4 & (0.01) \end{array}$ |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{gathered} -- \\ 20(1.0) \\ 32(1.0) \\ 19(0.8) \\ 22(1.0) \end{gathered}$ | $\begin{gathered} -- \\ 516(7.5) \\ 358(8.0) \\ 513(7.4) \\ 562(5.5) \end{gathered}$ | 53 (0.9) <br> 59 (1.0) <br> 50 (0.9) <br> 56 (0.8) | $\begin{gathered} -- \\ 496(5.0) \\ 348(5.9) \\ 483(6.1) \\ 529(5.8) \end{gathered}$ | $\begin{aligned} & \text { - - } \\ & 20(0.8) \\ & 7(0.5) \\ & 25(1.0) \\ & 19(0.9) \end{aligned}$ | $\begin{aligned} & 478 \text { (6.6) } \\ & 313 \text { (10.7) } \\ & 445 \text { (6.7) } \\ & 498 \text { (8.1) } \end{aligned}$ | $\begin{aligned} & -- \\ & 8(0.6) \\ & 2(0.2) \\ & 6(0.7) \\ & 3(0.3) \end{aligned}$ | $\begin{gathered} 441(7.8) \\ \sim \\ \sim \\ 435(10.9) \\ 460(13.3) \end{gathered}$ | $\begin{gathered} -- \\ 2.8(0.02) \\ 3.2(0.01) \\ 2.8(0.02) \\ 3.0(0.02) \end{gathered}$ |
| Singapore <br> Slovak Republic <br> Slovenia <br> South Africa Thailand | $\begin{aligned} & 30(1.0) \\ & 16(1.0) \\ & 12(0.7) \\ & 53(1.0) \\ & 13 \end{aligned}(0.7)$ | 626 (6.6) <br> 584 (5.7) <br> 585 (6.4) <br> 275 (6.5) <br> 518 (6.2) | 49 (0.8) <br> 54 (1.2) <br> 48 (1.6) <br> 35 (0.9) <br> 66 (0.8) | $\begin{aligned} & 602(6.4) \\ & 536(4.0) \\ & 536(3.2) \\ & 276(9.2) \\ & 467(5.1) \end{aligned}$ | $\begin{array}{r} 14(0.6) \\ 24(1.2) \\ 29(1.1) \\ 8(0.4) \\ 18(0.9) \end{array}$ | $\begin{aligned} & 583(7.3) \\ & 507 \text { (5.2) } \\ & 513 \text { (3.7) } \\ & 288 \text { (11.3) } \\ & 441 \text { (6.0) } \end{aligned}$ | $\begin{array}{r} 6(0.4) \\ 6(0.6) \\ 11(0.8) \\ 5(0.3) \\ 2(0.2) \end{array}$ | $\begin{gathered} 564(7.5) \\ 492(8.3) \\ 496(6.7) \\ 268(16.6) \\ \sim \sim \end{gathered}$ | $\begin{array}{ll} 3.0 & (0.02) \\ 2.8 & (0.03) \\ 2.6 & (0.02) \\ 3.4 & (0.02) \\ 2.9 & (0.02) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 31 & (0.9) \\ 27 & (1.0) \\ 23 & (0.9) \end{array}$ | $\begin{aligned} & 472 \text { (3.5) } \\ & 460 \text { (6.1) } \\ & 527 \text { (4.5) } \end{aligned}$ | $\begin{aligned} & 46(0.8) \\ & 50(0.8) \\ & 46 \\ & \hline 6 \end{aligned}$ | $\begin{aligned} & 448(3.1) \\ & 428(4.1) \\ & 505(4.0) \end{aligned}$ | $\begin{aligned} & 15(0.6) \\ & 17(0.8) \\ & 19(0.7) \end{aligned}$ | $\begin{aligned} & 423(4.0) \\ & 409(5.4) \\ & 496(4.5) \end{aligned}$ | $\begin{array}{r} 9(0.5) \\ 7(0.4) \\ 12(0.7) \end{array}$ | $\begin{aligned} & 412(3.1) \\ & 393(8.0) \\ & 465(5.6) \end{aligned}$ | $\begin{array}{ll} 3.0 & (0.02) \\ 3.0 & (0.02) \\ 2.8 & (0.02) \end{array}$ |
| International Avg. | 24 (0.2) | 518 (0.9) | 48 (0.2) | 489 (0.8) | 21 (0.2) | 466 (1.0) | 7 (0.1) | 456 (1.4) | 2.9 (0.00) |

Background date provided by students.
1 Average scale value based on: Like a lot=4; like=3; dislike=2; dislike a lot=1.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^74]
## REFERENCE 2

The Mathematics
Curriculum

|  | Achievement Standards |
| :---: | :---: |
| Australia | Achievement standards are stated as learning outcomes. |
| Belgium (Flemish) | Achievement standards are stated in terms of final learning objectives for A Stream and developmental objectives for B Stream. Students not meeting the standards may need to repeat the grade, receive reduced hours of instruction, or be moved to an easier class. |
| Bulgaria | Achievement standards are stated as broad descriptions of what students should know. Students not meeting the standards take an extra exam to be promoted; some students may need to repeat the grade. |
| Canada | Achievement standards are stated as specific learning outcomes. Students are expected to learn each concept, topic, or application. |
| Chile | There are no performance standards but there are objectives describing what students should learn. The revised curriculum will include performance standards stated as expected learning outcomes. |
| Chinese Taipei | The curriculum does not incorporate achievement standards. |
| Cyprus | The curriculum does not incorporate achievement standards. |
| Czech Republic | The curriculum provides a description of the skills and knowledge students must have. Teachers decide if the student has met the curriculum standards and considers this in promotion. If a student fails a single subject, the student must repeat the grade. |
| England | Achievement standards are established as a system of levels, each level with its own description of performance. On average, at age 7 students are expected to be at level 2 ; at age 11 level 4 ; and at age 13 level $5 / 6$. One level is regarded as two years progress. The government has set a target of $75 \%$ of 11 year olds reaching level 4 (or above) in mathematics by the year 2002. |
| Finland | The curriculum does not incorporate achievement standards. |
| Hong Kong, SAR | The achievement standards are stated as learner-centered objectives. A core of content is identified in the mathematics curriculum; exams and assessments have a portion of items from this core. |
| Hungary | Standards are stated as learning objectives. |
| Indonesia | There are instructional objectives in the curriculum but no performance standards. |
| Iran, Islamic Rep. | The curriculum does not incorporate achievement standards. |
| Israel | The curriculum does not incorporate achievement standards. |
| Italy | The curriculum does not incorporate achievement standards. |
| Japan | Achievement standards are stated in the national curriculum as learning objectives, such as "To help students..." or "To enable students to...". |
| Jordan | Objectives are defined in the curriculum and the minimum percent of attainment for each objective is specified (e.g., performs operations on real numbers - 80\%). |
| Korea, Rep. of | Achievement standards will be included in the revised curriculum (to be implemented at the 8th grade in 2001). |
| Latvia (LSS) | The curriculum incorporates achievement standards. |
| Lithuania | Achievement standards are not a part of curricula, but are prepared as a separate document. The draft of the National Educational Standards was released in 1997. As of 1999, the document had not been officially approved. |
| Macedonia, Rep. Of | Achievement standards are stated as learning objectives. |
| Malaysia | Achievement standards are stated as mathematic skills in the curriculum content specifications document. |
| Moldova | The curriculum incorporates achievement standards. |
| Morocco | The curriculum does not incorporate achievement standards. |
| Netherlands | Achievement standards are stated as learning objectives, such as "Students develop a competence..." or "Students learn to research...". |
| New Zealand | Achievement standards are stated as learning outcomes expressed at eight levels of learning independent of age and grade. |
| Philippines | Achievement standards are stated as learning competencies. |
| Romania | The achievement standards are stated as learning objectives, such as "The student should be able to arrive at a conclusion based on experimental work". |
| Russian Federation | The requirements for content of instruction and for students' knowledge and performance (learning outcomes: "student should...") are included in the curriculum. They are recommended for schools by the Ministry of Education. |
| Singapore | Achievement standards are stated in terms of learning objectives and assessment guidelines (i.e. table of specifications). |
| Slovak Republic | Learning objectives are included in the curriculum. Performance standards are in development. |
| Slovenia | The curriculum states standards for student performance by grade level and subject area. If a student's achievement in a subject is under minimal standard, the student receives an unsatisfactory mark and must take a correcting exam in that subject. Students receiving three or more unsatisfactory marks must repeat the grade. |
| South Africa | The standards are not specific. A list of content to be covered is provided. |
| Thailand | The achievement standards describe what students should learn including performance levels and explicit criteria. Students must pass 50\% of the standards. (The standards are set by the department that conducts the assessments and are NOT prescribed in the national curriculum.) Passing or failing the standards has no consequences for students. |
| Tunisia | Achievement standards are stated as learning objectives. |
| Turkey | Achievement standards are stated as objectives, such as "Ability to understand/know...". |
| United States | By 1999, all states were required to have performance standards. |


|  | Percentage of Students Whose Schools Reported Various Organizational Approaches in Mathematics Instruction to Accommodate Students with Different Abilities or Interests in Mathematics |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | All Classes Study Similar Content but at Different Levels of Difficulty |  | Students Are Grouped by Ability within Classes |  | Enrichment Mathematics Is Offered |  | Remedial Mathematics Is Offered |  | Different Classes Study Different Content |
| Australia Belgium (Flemish) Bulgaria Canada Chile |  $57(4.0)$ <br>  $66(5.1)$ <br>  $64(5.1)$ <br> s $77(3.4)$ <br>  $70(3.4)$ | s | $\begin{array}{ll} 57 & (4.3) \\ 11 & (3.2) \\ 62 & (5.1) \\ 43 & (4.3) \\ 25 & (2.9) \end{array}$ | s | 76 (3.6) <br> 36 (5.0) <br> 42 (5.1) <br> 66 (3.8) <br> 29 (2.8) | s | $\begin{array}{ll} 76 & (4.0) \\ 81 & (4.7) \\ 28 & (4.4) \\ 87 & (2.5) \\ 83 & (3.0) \end{array}$ | S | $\begin{array}{r} 33(3.9) \\ 100(0.0) \\ 10(2.5) \\ 17(3.0) \\ 15(3.0) \end{array}$ |
| Chinese Taipei <br> Cyprus <br> Czech Republic <br> England <br> Finland |  <br>  <br>  <br>  <br>  <br>  <br>  <br> $50(4.2)$ <br>  <br> $68(4.3)$ <br>  <br>  <br>  | r | $\begin{array}{rr} 25 & (3.7) \\ 35 & (0.2) \\ 44 & (5.0) \\ 57 & (4.7) \\ 5 & (1.3) \end{array}$ | r | $\begin{array}{ll} 88 & (2.7) \\ 12 & (0.1) \\ 29 & (3.9) \\ 48 & (5.0) \\ 43 & (3.9) \end{array}$ | r | $\begin{array}{ll} 81 & (3.5) \\ 52 & (0.2) \\ 62 & (4.3) \\ 61 & (4.8) \\ 95 & (1.8) \end{array}$ | $r$ | 18 (3.1) <br> 5 (0.1) <br> 7 (3.0) <br> 0 (0.0) <br> 7 (2.5) |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $62(4.9)$  <br> $r$ $85(3.0)$ <br>  $46(4.8)$ <br>  $0(0.0)$ <br> $r$ $71(4.7)$ | s | 17 (3.5) <br> 52 (4.3) <br> 20 (3.4) <br> 39 (4.7) <br> 51 (5.2) | s | 63 (4.4) <br> 60 (4.5) <br> 97 (1.1) <br> 27 (4.5) <br> 69 (4.3) | 5 | $\begin{array}{ll} 59 & (4.8) \\ 73 & (3.7) \\ 95 & (1.7) \\ 80 & (4.2) \\ 66 & (4.0) \end{array}$ | $r$ | $\begin{array}{r} 3(1.7) \\ 10(2.7) \\ 12(2.8) \\ 0(0.0) \\ 16(4.0) \end{array}$ |
| Italy <br> Japan Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 0(0.0) \\ 31(3.9) \\ 69(4.3) \\ 66(3.9) \\ 69(4.6) \end{array}$ |  | $\begin{array}{r} 0(0.0) \\ 13(3.1) \\ 42(4.6) \\ 41(4.3) \\ 40(4.7) \end{array}$ |  | $\begin{aligned} & 51(3.8) \\ & 32(3.5) \\ & 75(3.8) \\ & 27(3.5) \\ & 24(4.1) \end{aligned}$ |  | 81 (3.0) <br> 67 (4.3) <br> 91 (2.5) <br> 26 (3.5) <br> 94 (2.0) |  | $\begin{array}{r} 0(0.0) \\ 13(2.9) \\ 1(0.0) \\ 38(4.5) \\ 2(1.2) \end{array}$ |
| Lithuania ${ }^{\text { }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 0(0.0) \\ 56(4.2) \\ 56(4.5) \\ 81(3.5) \\ 67(4.0) \end{array}$ |  | $\begin{array}{r} 36(3.4) \\ 25(3.5) \\ 57(3.9) \\ 71(3.5) \\ 5(1.7) \end{array}$ |  | $\begin{array}{r} 72(3.6) \\ 92(2.3) \\ 95(1.8) \\ 74(3.7) \\ 6(1.8) \end{array}$ |  | $\begin{array}{ll} 67 & (4.0) \\ 96 & (1.7) \\ 87 & (2.8) \\ 61 & (4.5) \\ 47 & (4.7) \end{array}$ |  | $\begin{array}{r} 0(0.0) \\ 3(1.5) \\ 39(4.4) \\ 20(3.5) \\ 5(1.7) \end{array}$ |
| Netherlands New Zealand Philippines Romania Russian Federation | 55 (6.8) <br> 81 (3.2) <br> 86 (3.3) <br> 85 (3.2) <br> 32 (3.8) | $r$ | 39 (6.9) <br> 41 (4.6) <br> 42 (4.6) <br> 51 (4.9) <br> 47 (4.0) | $r$ | 90 (3.8) <br> 84 (2.8) <br> 76 (3.9) <br> 85 (3.1) <br> 90 (3.0) | $r$ | 64 (7.5) <br> 91 (2.7) <br> 75 (3.8) <br> 90 (2.2) <br> 53 (3.8) | $r$ | $\begin{array}{r} 60(6.8) \\ 5(2.1) \\ 18(3.3) \\ 5(1.7) \\ 25(3.5) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand |  $0(0.0)$ <br>  $71(3.7)$ <br>  $0(0.0)$ <br> s $63(4.6)$ <br>  $93(2.4)$ | s | $\begin{array}{r} 0(0.0) \\ 41(4.2) \\ 36 \\ 36 \\ 33 \\ (4.0) \\ 42 \end{array}(4.2)$ | s | 80 (3.5) <br> 38 (4.9) <br> 99 (0.5) <br> 45 (6.1) <br> 40 (3.7) | s | $\begin{array}{ll} 99 & (0.8) \\ 83 & (3.8) \\ 98 & (1.1) \\ 57 & (4.6) \\ 40 & (3.9) \end{array}$ | s | $\begin{array}{r} 82(3.6) \\ 7(2.4) \\ 0(0.0) \\ 13(3.5) \\ 3(1.2) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $91(2.3)$ $70(3.7)$ $r \quad 49(4.7)$ |  | $\begin{array}{r} 8(2.6) \\ 18(2.8) \\ 49(4.2) \end{array}$ | $r$ | $\begin{array}{ll} 50 & (4.1) \\ 23 & (3.8) \\ 79 & (2.8) \end{array}$ |  | 85 (3.2) <br> 47 (4.8) <br> 64 (3.9) | $r$ | $\begin{array}{r} 7(1.8) \\ 14(2.9) \\ 37(4.2) \end{array}$ |
| International Avg. | 58 (0.6) |  | 35 (0.6) |  | 58 (0.6) |  | 72 (0.6) |  | 17 (0.5) |

[^75]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates school response data available for 70-84\% of students. An "s" indicates school response data available for 50-69\% of students.





## Exhibit R2.4 Detailed Information About Topics in the Intended Curriculum, Up to and Including Eighth Grade - Measurement



[^76]


Background data provided by National Research Coordinators.


Background data provided by National Research Coordinators.

|  | Percentage of Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Taught Topics Before This Year Only |  | Taught Topics During This Year ${ }^{1}$ |  |  | Not Yet |
|  | More Than 80\% of Topics | More Than 50\% Up to and Including $80 \%$ of Topics | More Than 50\% of Topics Each Taught More Than 5 Periods | More Than 50\% of Topics Each Taught at Least 1-5 Periods | $50 \%$ or Less of Topics Taught | Taught 50\% or More of Topics |
| Australia Belgium (Flemish) Bulgaria s Canada Chile | $\begin{array}{r} 7(2.3) \\ 21(3.0) \\ 60(4.8) \\ 1(0.6) \\ 0(0.0) \end{array}$ | 18 (3.6) <br> 19 (2.3) <br> 29 (4.3) <br> 9 (2.0) <br> 3 (1.3) | $\begin{array}{r} 19(3.5) \\ 2(1.0) \\ 1(0.9) \\ 27(2.7) \\ 57(3.9) \end{array}$ |  | $\begin{array}{r} 3(1.3) \\ 10(3.6) \\ 2(1.5) \\ 1(0.4) \\ 5(1.6) \end{array}$ | $\begin{array}{ll} 0 & (0.0) \\ 6 & (2.9) \\ 1 & (0.9) \\ 0 & (0.3) \\ 0 & (0.0) \end{array}$ |
| Chinese Taipei Cyprus Czech Republic England s Finland | $\begin{array}{r} 90(2.4) \\ 1(1.1) \\ 53(5.7) \\ 8(2.4) \\ 0(0.3) \end{array}$ | $\begin{array}{r} 8(2.1) \\ 72(4.2) \\ 25(4.3) \\ 19(3.3) \\ 5(1.3) \end{array}$ | $\begin{array}{r} 0(0.0) \\ 1(0.0) \\ 5(2.2) \\ 3(0.9) \\ 13(3.3) \end{array}$ | $\begin{array}{r} 2(1.1) \\ 17(2.9) \\ 16(3.3) \\ 63(4.8) \\ 63 \end{array}$ | $\begin{array}{r} 0(0.0) \\ 10(3.3) \\ 1(0.8) \\ 6(2.1) \\ 16(3.3) \end{array}$ | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.6) \\ 3 & (1.6) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | 18 (3.0) <br> 38 (4.0) <br> 26 (4.1) <br> 3 (1.3) <br> 38 (3.7) | $\begin{array}{ll} 56 & (4.5) \\ 29 & (3.6) \\ 25 & (4.2) \\ 27 & (4.7) \\ 37 & (3.7) \end{array}$ | $\begin{array}{r} 2(1.2) \\ 8(2.3) \\ 12(2.8) \\ 1(0.8) \\ 3(1.3) \end{array}$ | 18 (3.6) <br> 24 (3.6) <br> 37 (4.6) <br> 63 (5.0) <br> 18 (3.1) | $\begin{aligned} & 5(2.0) \\ & 1(0.0) \\ & 0(0.5) \\ & 5(1.7) \\ & 4(1.4) \end{aligned}$ | $\begin{array}{ll} 1 & (0.8) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.7) \end{array}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 39 & (3.9) \\ 51 & (4.9) \\ 18 & (3.3) \\ 10 & (2.4) \\ 22 & (3.7) \end{array}$ | 42 (4.1) <br> 30 (4.3) <br> 31 (3.9) <br> 14 (2.8) <br> 42 (4.3) | $\begin{array}{r} 4(1.3) \\ 1(0.0) \\ 13(2.9) \\ 11(2.5) \\ 5(2.0) \end{array}$ | $\begin{array}{ll} 14 & (2.9) \\ 16 & (3.3) \\ 38 & (4.2) \\ 57 & (4.0) \\ 26 & (4.0) \end{array}$ | $\begin{array}{ll} 1 & (0.5) \\ 2 & (1.2) \\ 1 & (0.0) \\ 6 & (2.0) \\ 5 & (1.9) \end{array}$ | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 2 & (1.3) \\ 0 & (0.0) \end{array}$ |
| Lithuania ${ }^{\text {* }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{gathered} -- \\ 81(3.3) \\ 8(2.0) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 5(2.0) \\ 29(3.8) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 1(0.0) \\ 13(2.7) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 1(0.0) \\ 48(4.1) \\ -- \\ -- \end{gathered}$ | $\begin{aligned} & -- \\ & 1(0.0) \\ & 1(0.8) \\ & -- \\ & -- \end{aligned}$ | 12 (2.7) <br> 1 (0.9) <br> - - <br> - - |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{gathered} 8(2.3) \\ 0(0.0) \\ 7(2.1) \\ 75(3.9) \\ -- \end{gathered}$ | $\begin{array}{r} 28(5.8) \\ 1(0.9) \\ 15(3.2) \\ 11(2.8) \\ -- \end{array}$ | $\begin{gathered} 17(6.3) \\ 14(2.9) \\ 22(3.7) \\ 1(0.7) \\ -- \end{gathered}$ | 41 (5.8) <br> 83 (3.1) <br> 52 (4.2) <br> 13 (2.9) <br> - - | $\begin{aligned} & 5(2.7) \\ & 1(0.0) \\ & 3(1.3) \\ & 0(0.0) \\ & -- \end{aligned}$ | $\begin{aligned} & 0(0.0) \\ & 2(0.8) \\ & 0(0.0) \\ & 0(0.0) \\ & -- \end{aligned}$ |
| Singapore Slovak Republic Slovenia South Africa Finland s | $\begin{array}{cc} 37 & (4.2) \\ 55 & (4.5) \\ 44(4.1) \\ -- \\ 0(0.0) \end{array}$ | 35 (4.3) <br> 22 (4.2) <br> 27 (4.2) <br> 6 (2.0) | $\begin{gathered} 6(2.0) \\ 7(2.7) \\ 11(2.4) \\ -- \\ 15(4.1) \end{gathered}$ | $\begin{gathered} 22(3.7) \\ 16(2.6) \\ 17(3.1) \\ -- \\ 63(4.5) \end{gathered}$ | $\begin{gathered} 0(0.0) \\ 0(0.0) \\ 0(0.0) \\ -- \\ 15(4.0) \end{gathered}$ | $\begin{aligned} & 0(0.0) \\ & 0(0.0) \\ & 0(0.0) \\ & -- \\ & 2(1.9) \end{aligned}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{r} 7(2.3) \\ 16(3.0) \\ 8(1.4) \end{array}$ | $\begin{array}{r} 29(4.0) \\ 28(3.6) \\ 9(1.4) \end{array}$ | $\begin{array}{r} 32(4.6) \\ 8(1.7) \\ 34(2.8) \end{array}$ | $\begin{array}{r} 3(1.5) \\ 35(3.5) \\ 48 \end{array}$ | $\begin{array}{r} 23(3.7) \\ 13(2.6) \\ 1(0.7) \end{array}$ | $\begin{aligned} & 6(2.2) \\ & 0(0.2) \\ & 0(0.1) \end{aligned}$ |
| International Avg. | 26 (0.5) | 24 (0.6) | 11 (0.5) | 34 (0.6) | 4 (0.3) | 1 (0.2) |

Background data provided by teachers.

* Categories of topic coverage for fractions and number sense are based on combined responses to questions about the individual mathematics subtopics in the content area described in exhibit 5.12.
1 For each topic in 5.12 , teachers were asked if the topic was taught before this year, taught $1-5$ periods this year, taught more than 5 periods this year, or not yet taught. Topics taught during this year, regardless if taught before this year, are included in this category.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash $(-)$ indicates data are not available.
An "r" indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

|  | Percentage of Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Taught Topics Before This Year Only |  | Taught Topics During This Year ${ }^{1}$ |  |  | Not Yet |
|  | More Than 80\% of Topics | More Than 50\% Up to and Including $80 \%$ of Topics | More Than 50\% of Topics Each Taught More Than 5 Periods | More Than 50\% of Topics Each Taught at Least 1-5 Periods | $50 \%$ or Less of Topics Taught | or More of Topics |
| Australia Belgium (Flemish) <br> Bulgaria <br> Canada <br> Chile | $\begin{array}{r} 3(1.5) \\ 33(3.5) \\ 67(4.9) \\ 1(0.5) \\ 1(0.9) \end{array}$ | $\begin{array}{r} 6(2.3) \\ 27(3.8) \\ 19(3.8) \\ 8(1.6) \\ 7(2.0) \end{array}$ | $\begin{array}{r} 20(3.7) \\ 4(3.4) \\ 1(0.1) \\ 21 \\ 20 \\ 20 \end{array}(3.9)$ | $\begin{array}{r} 64(4.6) \\ 19(3.0) \\ 8(2.3) \\ 56(3.4) \\ 35 \end{array}$ | $\begin{array}{r} 6(1.6) \\ 13(3.7) \\ 5(1.9) \\ 11(1.4) \\ 12(2.4) \end{array}$ | $\begin{array}{r} 2(1.3) \\ 3(1.4) \\ 1(0.7) \\ 2(0.8) \\ 24(3.5) \end{array}$ |
| Chinese Taipei Cyprus s Czech Republic England S Finland | $\begin{array}{r} 20(3.6) \\ 0(0.0) \\ 50(5.9) \\ 8(2.4) \\ 2(1.1) \end{array}$ | $\begin{array}{rr} 53 & (4.4) \\ 16 & (5.4) \\ 29 & (5.0) \\ 18 & (2.7) \\ 6 & (1.7) \end{array}$ | $\begin{array}{r} 3(1.4) \\ 10(4.6) \\ 4(2.0) \\ 5(1.3) \\ 3(1.3) \end{array}$ | $\begin{array}{r} 5(1.8) \\ 51(7.0) \\ 14(3.4) \\ 58(3.8) \\ 41 \end{array}$ | $\begin{array}{r} 17(3.3) \\ 23(5.4) \\ 4(1.7) \\ 8(1.5) \\ 21 \end{array}(3.4)$ | $\begin{array}{r} 2(1.4) \\ 0(0.0) \\ 0(0.0) \\ 3(0.9) \\ 28 \end{array}(4.1)$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 15(3.1) \\ 31(3.5) \\ 9(2.2) \\ 18(2.7) \\ 37 \end{array}$ | $\begin{array}{ll} 28 & (4.2) \\ 33 & (3.7) \\ 18 & (4.0) \\ 30 & (4.5) \\ 14 & (3.4) \end{array}$ | $\begin{array}{r} 5(1.8) \\ 7(2.1) \\ 13(3.3) \\ 2(0.8) \\ 3(1.8) \end{array}$ | $\begin{array}{ll} 41 & (4.4) \\ 28 & (3.7) \\ 51 & (4.7) \\ 35 & (4.1) \\ 10 & (3.0) \end{array}$ | $\begin{array}{r} 10(2.8) \\ 2(1.0) \\ 8(2.5) \\ 10(2.6) \\ 7(2.4) \end{array}$ | 1 (1.1) <br> 0 (0.0) <br> 0 (0.0) <br> 4 (1.7) <br> 29 (5.0) |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 29(3.8) \\ 49 & (4.6) \\ 39 & (4.4) \\ 11 & (2.5) \\ 26 & (4.0) \end{array}$ | $\begin{array}{ll} 42 & (4.0) \\ 26 & (4.3) \\ 33 & (4.3) \\ 19 & (3.3) \\ 41 & (4.4) \end{array}$ | $\begin{array}{ll} 7 & (2.3) \\ 1 & (0.8) \\ 3 & (1.5) \\ 8 & (2.4) \\ 2 & (1.0) \end{array}$ | $\begin{array}{r} 15(2.9) \\ 8(2.1) \\ 20(3.3) \\ 49(4.1) \\ 11 \end{array}$ | $\begin{array}{r} 7(1.8) \\ 5(2.0) \\ 4(1.7) \\ 7(2.0) \\ 15(2.9) \end{array}$ | $\begin{array}{r} 1(0.6) \\ 12(2.9) \\ 0(0.0) \\ 6(1.7) \\ 5(2.1) \end{array}$ |
| Lithuania ${ }^{\text { }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{gathered} -- \\ 31(4.3) \\ 18(2.9) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 44(4.4) \\ 18(3.4) \\ -- \end{gathered}$ | $\begin{aligned} & -- \\ & 2(1.2) \\ & 7(1.6) \\ & -- \end{aligned}$ | $\begin{gathered} -- \\ 7(2.1) \\ 46(4.7) \\ -- \\ -- \end{gathered}$ | $\begin{aligned} & 4 \text { (1.8) } \\ & 9(2.6) \end{aligned}$ | $\begin{array}{r} 13(3.0) \\ 2(1.0) \\ -- \end{array}$ |
| Netherlands $r$ <br> New Zealand  <br> Philippines  <br> Romania  <br> Russian Federation  | $\begin{gathered} 6(3.3) \\ 0(0.0) \\ 5(1.5) \\ 69(4.4) \\ -- \end{gathered}$ | $\begin{gathered} 8(2.7) \\ 1(0.8) \\ 1(1.0) \\ 20(3.9) \\ -- \end{gathered}$ | 15 (6.2) <br> 12 (2.6) <br> 20 (3.4) <br> 1 (0.0) <br> - - | $\begin{array}{ll} 51 & (6.8) \\ 80 & (3.3) \\ 53 & (4.0) \\ 10 & (2.5) \end{array}$ | $\begin{array}{r} 15(3.6) \\ 1(0.9) \\ 6(2.2) \\ 1(0.0) \\ -- \end{array}$ | $\begin{array}{r} 7(4.7) \\ 5(1.8) \\ 15(3.2) \\ 0(0.0) \\ -- \end{array}$ |
| Singapore <br> Slovak Republic <br> Slovenia <br> South Africa <br> Thailand | $\begin{array}{cc} 39 & (4.8) \\ 23 & (4.2) \\ 29 & (3.9) \\ -- \\ 4(1.5) \end{array}$ | $\begin{array}{cc} 32 & (4.6) \\ 40 & (5.0) \\ 34 & (3.7) \\ -- \\ 11 & (2.7) \end{array}$ | $\begin{gathered} 8(2.5) \\ 6(2.3) \\ 8(2.1) \\ -- \\ 13(2.9) \end{gathered}$ | 19 (3.7) <br> 23 (4.3) <br> 26 (3.8) <br> 55 (4.5) | $\begin{aligned} & 2(1.1) \\ & 8(2.4) \\ & 3(1.6) \\ & -- \\ & 6(2.2) \end{aligned}$ | $\begin{gathered} 0(0.0) \\ 0(0.0) \\ 0(0.0) \\ -- \\ 10(2.4) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 33 & (4.3) \\ 18 & (3.3) \\ 10 & (2.2) \end{array}$ | $\begin{array}{ll} 40 & (4.5) \\ 34 & (3.8) \\ 11 & (1.9) \end{array}$ | $\begin{array}{r} 8(2.5) \\ 5(1.5) \\ 16(2.9) \end{array}$ | $\begin{array}{r} 2(1.4) \\ 16(2.3) \\ 54(3.6) \end{array}$ | $\begin{array}{r} 10(2.5) \\ 16(2.9) \\ 3(0.9) \end{array}$ | $\begin{array}{r} 8(2.2) \\ 13(2.8) \\ 6(1.4) \end{array}$ |
| International Avg. | 22 (0.6) | 23 (0.6) | 8 (0.4) | 32 (0.7) | 8 (0.4) | 6 (0.4) |

Background data provided by teachers.

* Categories of topic coverage for measurement are based on combined responses to questions about the individual mathematics subtopics in the content area described in exhibit 5.13.
1 For each topic in 5.13 , teachers were asked if the topic was taught before this year, taught $1-5$ periods this year, taught more than 5 periods this year, or not yet taught. Topics taught during this year, regardless if taught before this year, are included in this category.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^77]|  | Percentage of Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Taught Topics Before This Year Only |  | Taught Topics During This Year ${ }^{1}$ |  |  | No |
|  | More Than 80\% of Topics | More Than 50\% Up to and Including $80 \%$ of Topics | More Than 50\% of Topics Each Taught More Than5 Periods | More Than $50 \%$ of Topics Each Taught at Least 1-5 Periods | $50 \%$ or Less of Topics Taught | or More of Topics |
| Australia Belgium (Flemish) <br> Bulgaria <br> Canada <br> Chile | $\begin{array}{ll} 2 & (1.2) \\ 8 & (1.6) \\ 2 & (1.1) \\ 2 & (0.8) \\ 3 & (1.4) \end{array}$ | $\begin{array}{r} 3(1.8) \\ 23(3.0) \\ 8(2.5) \\ 5(1.6) \\ 8(2.3) \end{array}$ | $\begin{array}{r} 19(2.8) \\ 0(0.0) \\ 4(1.6) \\ 27(3.2) \\ 14(2.5) \end{array}$ | $\begin{array}{ll} 46 & (4.2) \\ 27 & (4.2) \\ 10 & (2.7) \\ 45 & (3.4) \\ 20 & (3.3) \end{array}$ | $\begin{array}{r} 5(1.9) \\ 24(3.0) \\ 12(2.9) \\ 8(0.8) \\ 2(1.1) \end{array}$ | 25 (3.5) <br> 18 (4.2) <br> 64 (5.2) <br> 13 (3.0) <br> 53 (3.5) |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 2 & (1.2) \\ 0 & (0.0) \\ 2 & (1.7) \\ 7 & (1.7) \\ 0 & (0.0) \end{array}$ | $\begin{array}{r} 3(1.4) \\ 0(0.0) \\ 24(5.1) \\ 15(3.2) \\ 1(0.9) \end{array}$ | $\begin{array}{r} 1(0.8) \\ 0(0.0) \\ 1(1.0) \\ 11(2.2) \\ 2(1.3) \end{array}$ | $\begin{array}{r} 1(0.7) \\ 0(0.0) \\ 7(2.1) \\ 62(3.9) \\ 35(4.5) \end{array}$ | $\begin{array}{r} 1(0.0) \\ 0(0.0) \\ 13(3.8) \\ 3(1.3) \\ 10(2.3) \end{array}$ | $\begin{array}{r} 92(2.1) \\ 100(0.0) \\ 52(5.3) \\ 3(0.7) \\ 52(4.1) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 3(1.6) \\ 6(1.9) \\ 2(1.0) \\ 2(1.1) \\ 13(2.9) \end{array}$ | $\begin{array}{r} 13(3.1) \\ 20(3.4) \\ 0(0.0) \\ 6(1.9) \\ 12 \end{array}(2.9)$ | $\begin{array}{r} 1(0.9) \\ 7(1.9) \\ 21(3.2) \\ 1(0.8) \\ 6(2.2) \end{array}$ | $\begin{array}{r} 7(2.3) \\ 45(4.0) \\ 70 \\ 70 \\ 78 \\ 78 \\ \hline \end{array}(4.4)$ | $\begin{array}{r} 6(2.2) \\ 15(2.7) \\ 1(0.8) \\ 4(1.5) \\ 13(2.8) \end{array}$ | $\begin{array}{r} 70(4.2) \\ 8(2.3) \\ 6(2.1) \\ 9(3.9) \\ 44(4.2) \end{array}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 2 & (1.1) \\ 2 & (1.2) \\ 6 & (2.1) \\ 3 & (1.3) \\ 4(1.8) \end{array}$ | $\begin{array}{r} 17(2.8) \\ 8(2.7) \\ 53(4.3) \\ 23(3.4) \\ 40 \end{array}(4.3)$ | $\begin{array}{r} 10(2.2) \\ 1(0.7) \\ 4(1.8) \\ 21(3.2) \\ 3(1.3) \end{array}$ | 33 (3.9) <br> 12 (2.9) <br> 25 (3.9) <br> 38 (4.0) <br> 28 (3.9) | $\begin{array}{r} 4(1.5) \\ 10(2.6) \\ 4(1.7) \\ 10(2.5) \\ 22(3.8) \end{array}$ | 34 (3.4) <br> 68 (4.2) <br> 7 (2.6) <br> 4 (1.6) <br> 3 (1.7) |
| Lithuania ${ }^{\text { }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{aligned} & 16(3.5) \\ & 3(1.4) \\ & -- \end{aligned}$ | $\begin{gathered} 16(3.4) \\ 6(2.0) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 2(1.3) \\ 12(2.5) \\ -- \\ -- \end{gathered}$ | $\begin{aligned} & 16(3.5) \\ & 13 \end{aligned}$ | $\begin{gathered} 18(3.4) \\ 0(0.0) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} 31(4.1) \\ 66(3.7) \\ -- \end{gathered}$ |
| Netherlands <br> New Zealand Philippines Romania Russian Federation | $\begin{gathered} 0(0.0) \\ 1(0.8) \\ 1(0.0) \\ 28(4.1) \\ -- \end{gathered}$ | $\begin{array}{r} 7(2.6) \\ 1(0.9) \\ 1(0.9) \\ 46(4.9) \end{array}$ | $\begin{array}{r} 17(5.8) \\ 12(3.0) \\ 9(2.3) \\ 1(0.7) \end{array}$ | 48 (6.6) <br> 65 (4.1) <br> 28 (4.1) <br> 19 (3.5) $\qquad$ | $\begin{aligned} & 6(2.3) \\ & 1(0.8) \\ & 0(0.0) \\ & 4(1.6) \\ & -- \end{aligned}$ | $\begin{gathered} 22(5.7) \\ 19(3.1) \\ 61(4.5) \\ 2(1.3) \\ -- \end{gathered}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 2(1.4) \\ 12(3.2) \\ 21(3.2) \\ -- \\ 6(2.1) \end{array}$ | $\begin{aligned} & 2(1.3) \\ & 38(5.0) \\ & 27(4.2) \\ &-- \\ & 3(1.5) \end{aligned}$ | $\begin{array}{r} 28(3.7) \\ 2(1.7) \\ 4(1.9) \\ -- \\ 18(3.3) \end{array}$ | $\begin{array}{r} 54(3.2) \\ 6(2.4) \\ 17(3.4) \\ -- \\ 30(4.2) \end{array}$ | $\begin{array}{r} 1(0.0) \\ 13(3.1) \\ 22(3.3) \\ -- \\ 1(1.0) \end{array}$ | $\begin{gathered} 13(3.3) \\ 29(4.3) \\ 9(2.5) \\ -- \\ 42(4.4) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 5(2.0) \\ & 1(0.9) \\ & 6(1.5) \end{aligned}$ | $\begin{array}{r} 7(2.3) \\ 21(3.5) \\ 7(2.5) \end{array}$ | $\begin{array}{r} 4(1.8) \\ 14(2.5) \\ 26(2.4) \end{array}$ | $\begin{array}{r} 1(0.0) \\ 43 \\ \hline \end{array}$ | $\begin{aligned} & 2(1.1) \\ & 8(2.2) \\ & 2(1.1) \end{aligned}$ | $\begin{array}{r} 82(3.7) \\ 14(3.5) \\ 6(1.3) \end{array}$ |
| International Avg. | 5 (0.3) | 14 (0.5) | 9 (0.4) | 30 (0.6) | 7 (0.4) | 34 (0.6) |

Background data provided by teachers.

* Categories of topic coverage for data representation, analysis, and probability are based on combined responses to questions about the individual mathematics subtopics in the content area described in exhibit 5.14.
1 For each topic in 5.14 , teachers were asked if the topic was taught before this year, taught $1-5$ peri ods this year, taught more than 5 periods this year, or not yet taught. Topics taught during this year, regardless if taught before this year, are included in this category.
$\pm$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
$A n$ " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

|  | Percentage of Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Taught Topics Before This Year Only |  | Taught Topics During This Year ${ }^{1}$ |  |  | Not Yet |
|  | More Than 80\% of Topics | More Than 50\% Up to and Including $80 \%$ of Topics | More Than 50\% of Topics Each Taught More Than 5 Periods | More Than $50 \%$ of Topics Each Taught at Least 1-5 Periods | $50 \%$ or Less of Topics Taught | or More of Topics |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 2 & (0.9) \\ 0 & (0.0) \\ 1 & (0.7) \\ 2 & (0.5) \\ 3 & (1.3) \end{array}$ | $\begin{array}{r} 3(1.4) \\ 5(1.4) \\ 19(3.8) \\ 3(1.0) \\ 4(1.4) \end{array}$ | $\begin{array}{r} 14(3.4) \\ 10(1.9) \\ 7(2.3) \\ 14(2.9) \\ 12(2.5) \end{array}$ | 47 (4.6) <br> 47 (3.5) <br> 24 (4.2) <br> 52 (3.2) <br> 20 (3.0) | 14 (3.1) <br> 15 (2.1) <br> 38 (6.2) <br> 12 (2.2) <br> 19 (2.8) | 19 (3.9) <br> 22 (2.4) <br> 11 (3.0) <br> 18 (2.6) <br> 42 (3.7) |
| Chinese Taipei Cyprus Czech Republic England $s$ Finland | $\begin{array}{r} 1(0.0) \\ 0(0.0) \\ 35(4.6) \\ 13(2.4) \\ 0(0.0) \end{array}$ | $\begin{array}{r} 1(0.5) \\ 0(0.0) \\ 23(4.8) \\ 18(3.1) \\ 0(0.0) \end{array}$ | $\begin{array}{ll} 6 & (2.1) \\ 0 & (0.0) \\ 4 & (2.3) \\ 2(0.8) \\ 1 & (0.8) \end{array}$ | $\begin{array}{r} 18(3.3) \\ 0(0.0) \\ 17(3.1) \\ 29(2.5) \\ 39(4.3) \end{array}$ | 42 (4.1) <br> 14 (3.7) <br> 17 (3.8) <br> 23 (3.4) <br> 4 (1.7) | $\begin{array}{r} 33(4.1) \\ 86(3.7) \\ 4(1.9) \\ 15(2.7) \\ 56(4.3) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 13(2.7) \\ 9(2.4) \\ 6(2.1) \\ 0(0.0) \\ 0(0.5) \end{array}$ | $\begin{array}{r} 21(3.5) \\ 21(3.0) \\ 2(1.3) \\ 5(3.7) \\ 2(1.0) \end{array}$ | $\begin{array}{r} 5(2.0) \\ 14(3.0) \\ 9(2.7) \\ 5(1.6) \\ 11(2.7) \end{array}$ | 16 (2.7) <br> 25 (3.4) <br> 42 (4.7) <br> 81 (4.0) <br> 20 (3.3) | $\begin{array}{r} 30(4.0) \\ 28(3.5) \\ 18(3.2) \\ 5(1.8) \\ 20 \end{array}(3.4)$ | $\begin{array}{r} 14(3.2) \\ 3(1.3) \\ 22(3.5) \\ 4(1.6) \\ 47(4.0) \end{array}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 2 & (1.0) \\ 2 & (1.5) \\ 1 & (0.0) \\ 5 & (1.8) \\ 1 & (0.8) \end{array}$ | $\begin{array}{r} 10(2.8) \\ 21(3.2) \\ 3(1.4) \\ 6(1.8) \\ 6(2.1) \end{array}$ | $\begin{array}{r} 9(2.2) \\ 8(2.4) \\ 18(3.6) \\ 12(2.4) \\ 1(0.9) \end{array}$ | 29 (3.6) <br> 35 (4.1) <br> 53 (4.1) <br> 57 (4.4) <br> 8 (2.3) | 41 (3.9) <br> 32 (4.4) <br> 22 (3.5) <br> 19 (3.4) <br> 58 (4.7) | $\begin{array}{r} 9(2.3) \\ 1(1.0) \\ 3(1.6) \\ 1(0.0) \\ 26(3.9) \end{array}$ |
| Lithuania ${ }^{\text {* }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{gathered} 20(3.3) \\ 2(1.0) \\ -- \\ -- \end{gathered}$ | 37 (4.1) <br> 1 (0.7) | $\begin{gathered} -- \\ 3(1.3) \\ 17(3.1) \\ -- \\ -- \end{gathered}$ | $\begin{aligned} & 12(2.9) \\ & 45 \end{aligned}$ | $\begin{aligned} & 18(3.5) \\ & 8(2.5) \\ & -- \\ & -- \end{aligned}$ | 10 (2.7) <br> 28 (3.3) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{gathered} 3(1.3) \\ 0(0.0) \\ 2(1.2) \\ 30(4.6) \\ -- \end{gathered}$ | $\begin{array}{r} 17(4.5) \\ 0(0.0) \\ 2(1.1) \\ 30(4.4) \\ -- \end{array}$ | $\begin{array}{r} 15(5.1) \\ 7(2.1) \\ 8(2.3) \\ 0(0.0) \\ -- \end{array}$ | $\begin{aligned} & 24(5.1) \\ & 67(3.5) \\ & 30(3.7) \\ & 19(3.2) \end{aligned}$ | $\begin{array}{r} 25(4.8) \\ 3(1.6) \\ 1(0.8) \\ 21(3.2) \\ -- \end{array}$ | 17 (4.9) <br> 22 (3.3) <br> 57 (4.3) <br> 0 (0.0) <br> - - |
| Singapore <br> Slovak Republic <br> Slovenia South Africa Thailand | $\begin{gathered} 1(0.0) \\ 6(2.3) \\ 11(2.7) \\ -- \\ 4(1.8) \end{gathered}$ | $\begin{gathered} 1(0.0) \\ 21(3.8) \\ 23(3.6) \\ -- \\ 5(1.7) \end{gathered}$ | $\begin{array}{r} 24(4.1) \\ 1(0.8) \\ 13(2.8) \\ -- \\ 12(2.9) \end{array}$ | $\begin{array}{r} 62(4.4) \\ 6(2.4) \\ 30(3.9) \\ -- \\ 53(4.5) \end{array}$ | $\begin{array}{r} 5(2.0) \\ 19(4.0) \\ 24(3.2) \\ -- \\ 13(2.4) \end{array}$ | $\begin{gathered} 7(2.4) \\ 47(4.4) \\ 0(0.0) \\ -- \\ 14(3.3) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 1(1.0) \\ & 4(1.3) \\ & 3(1.0) \end{aligned}$ | $\begin{array}{r} 9(2.6) \\ 11(2.5) \\ 7(1.4) \end{array}$ | $\begin{array}{r} 4(1.7) \\ 7(2.2) \\ 14(2.2) \end{array}$ | $\begin{array}{r} 2(1.1) \\ 45(4.0) \\ 42 \end{array}$ | $\begin{aligned} & 12(2.7) \\ & 27(3.3) \\ & 10(2.0) \end{aligned}$ | $\begin{array}{r} 72(4.0) \\ 5(1.7) \\ 25(2.9) \end{array}$ |
| International Avg. | 6 (0.3) | 10 (0.5) | 9 (0.4) | 33 (0.6) | 20 (0.6) | 22 (0.5) |

Background data provided by teachers.

* Categories of topic coverage for geometry are based on combined responses to questions about the individual mathematics subtopics in the content area described in exhibit 5.15.
1 For each topic in 5.15 , teachers were asked if the topic was taught before this year, taught $1-5$ periods this year, taught more than 5 periods this year, or not yet taught. Topics taught during this year, regardless if taught before this year, are included in this category.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash $(-)$ indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

|  | Percentage of Students |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Taught Topics Before This Year Only |  | Taught Topics During This Year ${ }^{1}$ |  |  | Not |
|  | More Than 80\% of Topics | More Than 50\% Up to and Including $80 \%$ of Topics | More Than $50 \%$ of Topics Each Taught More Than5 Periods | More Than $50 \%$ of Topics Each Taught at Least 1-5 Periods | $50 \%$ or Less of Topics Taught | or More of Topics |
| Australia <br> Belgium (Flemish) <br> Bulgaria <br> Canada <br> Chile | $\begin{array}{r} 1(0.9) \\ 1(0.7) \\ 22(3.6) \\ 1(0.5) \\ 0(0.0) \end{array}$ | $\begin{array}{r} 2(1.2) \\ 9(1.9) \\ 18(4.1) \\ 1(0.4) \\ 1(0.5) \end{array}$ | 46 (4.9) <br> 20 (2.9) <br> 24 (4.6) <br> 54 (3.0) <br> 31 (3.5) | 45 (4.9) <br> 43 (3.6) <br> 32 (6.3) <br> 38 (2.6) <br> 35 (3.8) | $\begin{array}{r} 3(1.5) \\ 11(2.1) \\ 3(1.5) \\ 0(0.0) \\ 2(0.9) \end{array}$ | $\begin{array}{r} 3(1.6) \\ 16(3.2) \\ 1(0.5) \\ 6(2.3) \\ 32(3.9) \end{array}$ |
| $\begin{array}{rr} \text { Chinese Taipei } \\ \text { Cyprus } & r \\ \text { Czech Republic } & \\ \text { England } & s \\ \text { Finland } \end{array}$ | $\begin{array}{r} 28(3.6) \\ 0(0.0) \\ 2(1.2) \\ 0(0.0) \\ 0(0.0) \end{array}$ | $\begin{array}{r} 57(4.0) \\ 3(1.9) \\ 3(1.5) \\ 8(2.4) \\ 1(1.3) \end{array}$ | $\begin{array}{r} 4(1.7) \\ 29(4.9) \\ 69(5.0) \\ 21(2.9) \\ 10(2.3) \end{array}$ | $\begin{array}{r} 8(2.1) \\ 65(5.1) \\ 20 \\ \hline 0 \\ 60 \\ \hline \end{array}(3.4)$ | $\begin{aligned} & 2(1.1) \\ & 3(0.2) \\ & 5(2.4) \\ & 4(1.3) \\ & 4(2.0) \end{aligned}$ | $\begin{array}{r} 1(0.0) \\ 0(0.0) \\ 2(1.7) \\ 7(1.4) \\ 52(4.5) \end{array}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 4(1.6) \\ 11(2.4) \\ 3(1.3) \\ 0(0.0) \\ 2(0.8) \end{array}$ | $\begin{array}{r} 19(3.3) \\ 18(3.3) \\ 8(2.3) \\ 4(1.5) \\ 10 \end{array}(2.2)$ | $\begin{array}{ll} 25 & (4.0) \\ 40 & (4.6) \\ 21 & (3.4) \\ 11 & (2.8) \\ 49 & (3.5) \end{array}$ | 43 (3.9) <br> 29 (3.8) <br> 58 (4.6) <br> 76 (4.1) <br> 28 (3.5) | $\begin{array}{r} 10(2.7) \\ 2(1.2) \\ 7(2.2) \\ 9(3.9) \\ 9(2.2) \end{array}$ | $\begin{array}{ll} 1 & (0.0) \\ 0 & (0.0) \\ 3 & (1.8) \\ 0 & (0.0) \\ 1 & (0.9) \end{array}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 0 & (0.0) \\ 5 & (2.3) \\ 1 & (0.8) \\ 5 & (1.7) \\ 6 & (1.9) \end{array}$ | $\begin{array}{r} 1(0.0) \\ 30(4.2) \\ 14(2.9) \\ 9(2.5) \\ 8(2.6) \end{array}$ | 67 (3.7) <br> 38 (3.9) <br> 15 (3.2) <br> 36 (4.0) <br> 58 (4.5) | $\begin{array}{ll} 28 & (3.3) \\ 25 & (4.0) \\ 43 & (4.3) \\ 48 & (4.0) \\ 28 & (3.8) \end{array}$ | $\begin{array}{r} 0(0.0) \\ 2(1.1) \\ 21(4.1) \\ 1(0.0) \\ 0(0.5) \end{array}$ | $\begin{array}{ll} 4 & (1.5) \\ 0 & (0.0) \\ 6 & (2.1) \\ 1 & (0.7) \\ 0 & (0.0) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{aligned} & -- \\ & 2(1.2) \\ & 1(0.9) \\ & -- \\ & -- \end{aligned}$ | $\begin{gathered} -- \\ 46(4.3) \\ 0(0.0) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 14(2.5) \\ 29(3.6) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 23(3.9) \\ 68(3.8) \\ -- \\ -- \end{gathered}$ | $\begin{gathered} -- \\ 11(3.1) \\ 0(0.0) \\ -- \\ -- \end{gathered}$ | $\begin{aligned} & -- \\ & 4(1.8) \\ & 1(1.0) \\ & -- \\ & -- \end{aligned}$ |
|  | $\begin{array}{r} 1(0.1) \\ 0(0.0) \\ 1(0.6) \\ 10(2.7) \\ \\ \hline \end{array}$ | $\begin{array}{r} 2(1.1) \\ 0(0.0) \\ 2(1.2) \\ 16(3.5) \end{array}$ | $\begin{array}{cc} 32 & (6.4) \\ 35 & (4.0) \\ 20 & (3.6) \\ 23 & (3.6) \\ -- \end{array}$ | 34 (6.2) <br> 56 (4.3) <br> 45 (4.3) <br> 51 (4.2) | $\begin{array}{r} 12(3.9) \\ 0(0.0) \\ 1(0.6) \\ 0(0.0) \\ -- \end{array}$ | $\begin{array}{r} 19(6.0) \\ 8(2.4) \\ 32(3.8) \\ 0(0.0) \\ -- \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{aligned} & 2(1.1) \\ & 1(1.0) \\ & 4(1.6) \\ & -- \\ & 5(1.7) \end{aligned}$ | $\begin{gathered} 18(3.4) \\ 10(3.2) \\ 14(3.1) \\ -- \\ 4(1.2) \end{gathered}$ | $\begin{array}{cc} 32(3.9) \\ 63 & (4.8) \\ 39 & (4.1) \\ -- \\ 14 & (3.0) \end{array}$ | 48 (4.8) <br> 23 (3.6) <br> 42 (4.6) <br> 58 (4.2) | $\begin{aligned} & 1(1.0) \\ & 3(1.5) \\ & 1(1.0) \\ & -- \\ & 1(1.0) \end{aligned}$ | $\begin{gathered} 0(0.0) \\ 0(0.0) \\ 0(0.0) \\ -- \\ 18(3.6) \end{gathered}$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 8 \text { (2.7) } \\ & 4(1.4) \\ & 3(1.2) \end{aligned}$ | $\begin{array}{r} 21(4.1) \\ 10(2.6) \\ 0(0.3) \end{array}$ | $\begin{array}{ll} 20 & (3.5) \\ 31 & (3.7) \\ 62 & (2.7) \end{array}$ | $\begin{array}{r} 4(1.9) \\ 49(3.5) \\ 32 \end{array}$ | $\begin{array}{r} 13 \\ 0(3.1) \\ 0(0.0) \\ 0(0.2) \end{array}$ | $\begin{array}{r} 33(4.4) \\ 5(1.7) \\ 2(0.9) \end{array}$ |
| International Avg. | 4 (0.3) | 11 (0.4) | 33 (0.7) | 40 (0.7) | 4 (0.3) | 8 (0.4) |

Background data provided by teachers.

* Categories of topic coverage for algebra are based on combined responses to questions about the individual mathematics subtopics in the content area described in exhibit 5.16.
1 For each topic in 5.16 , teachers were asked if the topic was taught before this year, taught $1-5$ periods this year, taught more than 5 periods this year, or not yet taught. Topics taught during this year, regardless if taught before this year, are included in this category.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An "r" indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.


## REFERENCE 3

Teachers and Instruction


Background data provided by teachers.
1 Teachers who responded that they majored in more than one area are reflected in all categories that apply.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent

A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students. An "x" indicates teacher response data available for $<50 \%$ of students.


Exhibit R3.2 Overleaf

## Exhibit R3.2 Teachers' Confidence in Their Preparation to Teach Mathematics Topics



[^78][^79]|  | Percentage of Students Whose Teachers Report Feeling Very Well Prepared to Teach Topic¹ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coordinate geometry | Algebraic representation | Evaluate and perform operations on algebraic expressions | Solving linear equations and inequalities | Representation and interpretation of data in graphs, charts, and tables | Simple probabilities understanding and calculations | Average ${ }^{2}$ |
|  | $\begin{array}{ll} 87 & (3.2) \\ 71 & (3.9) \\ 29 & (4.7) \\ 64 & (3.6) \\ 31 & (3.6) \end{array}$ |  $83(3.7)$ <br>  $85(3.1)$ <br>  $62(6.0)$ <br> $r$ $83(2.5)$ <br>  $38(3.8)$ | 85 (3.5) <br> 86 (2.6) <br> 80 (5.8) <br> 82 (2.5) <br> 39 (4.1) | $84(3.4)$ $83(3.3)$ $81(5.7)$ $r \quad 74(2.8)$ $46(3.8)$ | 86 (3.4) <br> 64 (2.9) <br> 49 (5.6) <br> 79 (2.9) <br> 41 (4.0) | $84(3.3)$ $30(4.6)$ $36(5.4)$ $r \quad 70(3.3)$ $39(3.4)$ | 84 (2.7) <br> 80 (1.4) <br> 66 (4.8) <br> 79 (1.7) <br> 44 (2.8) |
| Chinese Taipei | 81 (3.2) | 82 (2.9) | 85 (2.9) | 84 (3.0) | 74 (3.7) | 73 (3.7) | 78 (2.6) |
| Cyprus | 64 (4.4) | 95 (1.7) | 99 (0.9) | 100 (0.0) | 78 (3.7) | 57 (4.6) | 89 (0.9) |
| Czech Republic | 84 (4.2) | 88 (3.6) | 95 (2.4) | 97 (1.9) | 75 (5.1) | 52 (5.6) | 88 (1.8) |
| England Finland | $80 \text { (3.0) }$ | $86 \text { (2.6) }$ | $89 \text { (2.0) }$ | $88 \text { (1.7) }$ | $73 \text { (3.4) }$ | $63 \text { (4.0) }$ | $81 \text { (1.9) }$ |
| Hong Kong, SAR | 82 (3.4) | 85 (3.2) | 87 (3.0) | 74 (3.9) | 58 (4.4) | 58 (3.9) | 72 (2.6) |
| Hungary | 50 (4.3) | 53 (4.0) | 65 (3.8) | 67 (3.7) | - - | - - | 59 (3.3) |
| Indonesia | 86 (3.6) | 90 (2.6) | 81 (3.5) | 90 (2.6) | 69 (3.9) | 80 (3.1) | 81 (2.1) |
| Iran, Islamic Rep. | 78 (3.2) | 87 (2.3) | 89 (2.5) | 81 (3.1) | 77 (3.7) | 47 (4.1) | 81 (1.8) |
| Israel | 84 (2.7) | 84 (2.9) | 94 (2.2) | 96 (1.7) | 86 (2.8) | 74 (3.5) | 84 (1.6) |
| Italy | 64 (4.0) | 62 (3.8) | 79 (2.9) | 71 (3.2) | 70 (3.1) | 53 (4.2) | 69 (2.3) |
| Japan | 25 (3.9) | 28 (4.4) | 33 (4.3) | 37 (4.4) | 19 (3.3) | 19 (3.7) | 23 (2.6) |
| Jordan | 77 (3.7) | 84 (3.1) | 93 (2.1) | 94 (2.0) | 91 (2.4) | 93 (2.2) | 88 (1.7) |
| Korea, Rep. of | 49 (3.4) | 56 (3.9) | 74 (3.3) | 83 (2.9) | 55 (3.8) | 67 (3.9) | 61 (2.5) |
| Latvia (LSS) | 81 (3.7) | 93 (2.1) | 90 (2.7) | 90 (2.7) | 70 (3.9) | 22 (3.7) | 73 (2.1) |
| Lithuania ${ }^{\text {* }}$ | - - | - - | - - | - - | -- | -- | - - |
| Macedonia, Rep. of | 82 (3.4) | 99 (1.0) | 100 (0.0) | 99 (0.7) | 81 (3.3) | 65 (4.2) | 92 (1.0) |
| Malaysia | 82 (3.6) | 89 (3.1) | 88 (3.2) | 89 (2.9) | 79 (3.7) | 46 (4.6) | 81 (2.5) |
| Moldova | 66 (4.3) | 71 (4.2) | 78 (3.8) | 76 (3.8) | 54 (4.6) | 32 (4.8) | 64 (3.2) |
| Morocco | 72 (2.6) | 72 (2.8) | 74 (3.5) | 91 (1.8) | 59 (3.2) | 59 (3.5) | 75 (1.3) |
| Netherlands | 88 (5.9) | 87 (6.0) | 77 (6.4) | 87 (5.9) | 85 (5.8) | 77 (6.3) | 84 (5.3) |
| New Zealand | 87 (2.9) | 91 (2.4) | 87 (2.8) | 87 (3.0) | 87 (2.6) | 86 (2.5) | 88 (1.9) |
| Philippines | 35 (4.5) | 73 (3.5) | 82 (3.0) | 62 (3.8) | 62 (3.9) | 28 (4.0) | 64 (2.3) |
| Romania | 32 (5.2) | 68 (4.7) | 98 (1.0) | 96 (1.6) | 82 (3.7) | 54 (4.7) | 85 (1.3) |
| Russian Federation | - |  |  | - - | - - |  | - - |
| Singapore | 79 (3.6) | 85 (3.3) | 86 (3.1) | 89 (2.9) | 80 (3.6) | 46 (5.2) | 78 (2.7) |
| Slovak Republic | 90 (3.1) | 95 (1.8) | 99 (1.0) | 99 (1.0) | 75 (3.7) | 45 (5.2) | 89 (1.5) |
| Slovenia | 50 (4.3) | 47 (4.1) | 64 (4.0) | 71 (3.7) | 38 (3.8) | 22 (4.0) | 50 (2.9) |
| South Africa | 53 (4.6) | 85 (2.3) | 81 (3.0) | 81 (3.1) | 67 (4.5) | 62 (4.4) | 71 (1.9) |
| Thailand | 30 (5.4) | 31 (5.0) | 33 (5.0) | 39 (4.5) | 34 (4.2) | 32 (5.1) | 32 (3.0) |
| Tunisia | 42 (4.8) | 52 (5.0) | 58 (3.9) | 71 (3.8) | 47 (4.5) | 38 (4.6) | 51 (2.6) |
| Turkey | 87 (2.3) | 83 (3.0) | 83 (2.7) | 90 (2.5) | 74 (3.8) | 85 (2.9) | 83 (1.6) |
| United States | 82 (2.6) | 94 (1.6) | 95 (1.3) | 93 (1.5) | 94 (1.5) | 90 (2.1) | 90 (1.2) |
| International Avg. | 66 (0.7) | 76 (0.6) | 80 (0.6) | 81 (0.5) | 68 (0.7) | 55 (0.7) | 73 (0.4) |

Exhibit R3.3 Shortages of Teachers Qualified to Teach Mathematics Affecting Capacity to Provide Instruction

TIMSS1999
$\overbrace{0}^{\text {th }}$
Mathematics

|  | None |  | A Little |  | Some |  | A Lot |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | 60 (4.2) <br> 84 (3.6) <br> 25 (4.1) <br> 54 (3.1) <br> 34 (3.5) | 533 (6.7) <br> 557 (4.5) <br> 497 (9.6) <br> 536 (3.1) <br> 418 (9.6) | $\begin{array}{r} 32(3.9) \\ 12(3.3) \\ 4(1.1) \\ 27(3.2) \\ 39(3.7) \end{array}$ | $\begin{aligned} & 513(9.3) \\ & 554(22.4) \\ & 491(20.6) \\ & 531(4.3) \\ & 383(6.0) \end{aligned}$ | $\begin{array}{r} 5(1.5) \\ 2(1.2) \\ 6(1.9) \\ 16(2.4) \\ 20(3.3) \end{array}$ | $\begin{gathered} 520(17.4) \\ \sim \sim \\ 495(14.7) \\ 514(7.7) \\ 378(6.3) \end{gathered}$ | $\begin{array}{r} 3(1.6) \\ 1(0.9) \\ 65(4.6) \\ 3(0.8) \\ 7(1.9) \end{array}$ | $\begin{gathered} 484(29.4) \\ \sim \\ \sim \\ 519 \\ 525(8.4) \\ 365(5.2) \end{gathered}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 43 & (4.3) \\ 63 & (0.2) \\ 90 & (2.9) \\ 71 & (4.1) \\ 82 & (3.3) \end{array}$ | $\begin{aligned} & 591(5.1) \\ & 473(2.4) \\ & 521(4.7) \\ & 508(5.8) \\ & 519 \end{aligned}(3.1)$ | $\begin{array}{r} 36(4.4) \\ 28(0.2) \\ 6(2.6) \\ 19(3.6) \\ 12(3.0) \end{array}$ | $\begin{aligned} & 584(7.3) \\ & 483(2.9) \\ & 506 \text { (15.6) } \\ & 482(7.3) \\ & 527(6.0) \end{aligned}$ | $\begin{array}{r} 12(3.0) \\ 4(0.0) \\ 3(1.8) \\ 8(2.8) \\ 3(1.3) \end{array}$ | $\begin{aligned} & 590 \text { (11.4) } \\ & 490 \text { (3.7) } \\ & 527 \text { (26.2) } \\ & 485 \text { (17.1) } \\ & 524 \text { (8.2) } \end{aligned}$ | $\begin{array}{ll} 9 & (2.2) \\ 6 & (0.1) \\ 1 & (0.9) \\ 2(1.2) \\ 2(1.1) \end{array}$ | $\begin{gathered} 551(13.3) \\ 486(11.6) \\ \sim \sim \\ \sim \sim \\ \sim \sim \end{gathered}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | 55 (4.5) <br> 84 (2.7) <br> 16 (3.2) <br> 27 (3.5) <br> 56 (4.4) | $596(6.0)$ $531(4.0)$ $425(16.5)$ $429(5.5)$ $464(6.9)$ | $\begin{array}{r} 28(4.2) \\ 5(1.8) \\ 33(4.2) \\ 23(3.4) \\ 35(4.3) \end{array}$ | $\begin{aligned} & 555(9.6) \\ & 552(22.2) \\ & 402(8.6) \\ & 416(8.1) \\ & 466(7.7) \end{aligned}$ | $\begin{array}{r} 10(2.6) \\ 4(1.4) \\ 35(4.6) \\ 29(4.2) \\ 7(2.1) \end{array}$ | 583 (15.9) 558 (18.1) 398 (9.7) 425 (6.3) $470(31.8)$ | $\begin{array}{r} 7(2.1) \\ 8(2.0) \\ 16(3.1) \\ 21(3.3) \\ 3(1.2) \end{array}$ | $\begin{aligned} & 602(15.1) \\ & 504(17.3) \\ & 395(20.3) \\ & 416(7.7) \\ & 437(57.3) \end{aligned}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 38(4.1) \\ 65(3.9) \\ 9(2.5) \\ 19(3.2) \\ 39(4.7) \end{array}$ | $\begin{aligned} & 478(5.5) \\ & 579(2.1) \\ & 426(11.2) \\ & 589(5.4) \\ & 499(6.7) \end{aligned}$ | $\begin{array}{r} 36(3.6) \\ 17(2.8) \\ 5(2.1) \\ 48(3.9) \\ 21(3.8) \end{array}$ | $\begin{aligned} & 483(7.6) \\ & 583(4.2) \\ & 444 \text { (31.8) } \\ & 587(2.5) \\ & 515(5.5) \end{aligned}$ | $\begin{array}{r} 20(3.3) \\ 8(2.4) \\ 4(1.7) \\ 22(3.8) \\ 16(3.9) \end{array}$ | $\begin{aligned} & 473 \text { (9.0) } \\ & 577 \text { (6.0) } \\ & 407 \text { (13.2) } \\ & 586 \text { (4.4) } \\ & 508 \text { (11.7) } \end{aligned}$ | $\begin{array}{r} 6(1.7) \\ 10(2.5) \\ 82(3.4) \\ 11(2.7) \\ 23(4.2) \end{array}$ | $\begin{aligned} & 487(13.3) \\ & 572(5.5) \\ & 428(4.0) \\ & 591(4.9) \\ & 499(7.8) \end{aligned}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{ll} 91 & (2.5) \\ 78 & (3.4) \\ 27 & (3.5) \\ 16 & (2.7) \\ 23 & (3.2) \end{array}$ | 483 (4.6) <br> 452 (4.9) <br> 536 (9.5) <br> 470 (8.4) <br> 339 (5.3) | $\begin{array}{r} 3(1.4) \\ 5(2.0) \\ 23(3.7) \\ 10(2.6) \\ 29(3.2) \end{array}$ | $\begin{aligned} & 467 \text { (10.1) } \\ & 433 \text { (24.5) } \\ & 525(11.3) \\ & 473 \text { (18.6) } \\ & 334(4.5) \end{aligned}$ | $\begin{array}{r} 3(1.6) \\ 10(2.3) \\ 16(3.3) \\ 16(3.1) \\ 27(3.7) \end{array}$ | 453 (21.3) <br> 413 (18.2) <br> 517 (14.6) <br> 473 (11.7) <br> 334 (4.1) | $\begin{array}{r} 3(1.4) \\ 7(2.2) \\ 34(4.2) \\ 58(4.0) \\ 21(3.9) \end{array}$ | 495 (18.9) 431 (20.9) 504 (7.7) 468 (5.1) 343 (5.3) |
| Netherlands $r$ New Zealand Philippines Romania Russian Federation | 52 (6.5) <br> 58 (3.5) <br> 27 (3.9) <br> 86 (2.5) <br> 51 (3.9) | $\begin{array}{ll} 546 & (11.8) \\ 497 & (6.9) \\ 369 & (14.5) \\ 475 & (6.9) \\ 526(7.2) \end{array}$ | $\begin{array}{r} 23(5.3) \\ 26(3.9) \\ 30(3.9) \\ 2(1.1) \\ 9(2.3) \end{array}$ | $\begin{array}{cl} 541 & (15.4) \\ 476 & (10.7) \\ 327 & (9.7) \\ \sim & \sim \\ 523 & (24.4) \end{array}$ | $\begin{array}{r} 19(6.8) \\ 12(2.6) \\ 25(3.6) \\ 4(1.7) \\ 10(2.0) \end{array}$ | $\begin{aligned} & 518 \text { (22.8) } \\ & 465 \text { (13.8) } \\ & 338 \text { (12.8) } \\ & 421 \text { (17.7) } \\ & 526 \text { (15.2) } \end{aligned}$ | $\begin{array}{r} 5(2.0) \\ 4(1.9) \\ 19(3.4) \\ 8(2.0) \\ 30(3.8) \end{array}$ | $\begin{array}{ll} 560 & (22.0) \\ 530 & (27.1) \\ 340 & (9.4) \\ 467 & (21.7) \\ 526 & (10.6) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | 58 (4.1) <br> 79 (4.0) <br> 36 (3.9) <br> 23 (3.2) <br> 13 (2.9) | $608(9.0)$ $538(4.0)$ $526(4.8)$ $295(15.6)$ $470(18.5)$ | $\begin{array}{r} 26(4.1) \\ 6(2.3) \\ 7(2.0) \\ 25(3.7) \\ 15(3.3) \end{array}$ | $\begin{aligned} & 599(10.9) \\ & 502(11.6) \\ & 525 \text { (8.5) } \\ & 275(12.5) \\ & 474(9.6) \end{aligned}$ | $\begin{array}{r} 12(2.8) \\ 8(2.3) \\ 15(2.6) \\ 26(3.8) \\ 35(4.4) \end{array}$ | $\begin{aligned} & 607 \text { (13.9) } \\ & 522 \text { (15.4) } \\ & 534 \text { (4.5) } \\ & 273 \text { (10.4) } \\ & 465 \text { (8.2) } \end{aligned}$ | $\begin{array}{r} 4(1.6) \\ 8(2.8) \\ 42(3.9) \\ 27(3.7) \\ 37(4.3) \end{array}$ | $\begin{aligned} & 592(17.5) \\ & 511(6.2) \\ & 533(5.0) \\ & 260(14.4) \\ & 467(8.7) \end{aligned}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{r} 7(2.4) \\ 6(1.9) \\ 62(4.2) \end{array}$ | $\begin{aligned} & 467 \text { (8.6) } \\ & 450(21.7) \\ & 514(5.3) \end{aligned}$ | $\begin{array}{r} 7(2.2) \\ 12(2.5) \\ 23(3.5) \end{array}$ | $\begin{aligned} & 457 \text { (11.9) } \\ & 437(16.7) \\ & 497(6.2) \end{aligned}$ | $\begin{array}{r} 9(2.5) \\ 20(3.7) \\ 13 \end{array}$ | $\begin{aligned} & 448(7.6) \\ & 425(6.6) \\ & 461(9.3) \end{aligned}$ | $\begin{array}{r} 76 \\ 62(3.8) \\ 6 \\ 3(1.0) \end{array}$ | $\begin{aligned} & 446(2.8) \\ & 427(5.1) \\ & 446(15.1) \end{aligned}$ |
| International Avg. | 47 (0.6) | 493 (1.4) | 20 (0.5) | 484 (2.6) | 14 (0.5) | 478 (2.4) | 19 (0.5) | 477 (3.0) |

Background data provided by schools.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year

[^80]

Exhibit R3.4 Overleaf

## Exhibit R3.4 Percentage of Students Whose Mathematics Teachers Agree or Strongly

Agree with Statements About the Nature of Mathematics and Mathematics Teaching



Background data provided by teachers.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^81]

## Exhibit R3.5 Percentage of Students Whose Mathematics Teachers Think Particular

 Abilities Are Very Important for Students' Success in Mathematics in School

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.




[^82]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
An "r" indicates school response data available for 70-84\% of students. An "s" indicates school response data available for $50-69 \%$ of students. An "x" indicates school response data available for < $50 \%$ of students.


## Background data provided by schools.

1 Computed as the ratio of instructional hours to total hours averaged across students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An " $r$ " indicates school response data available for $70-84 \%$ of students. An " $s$ " indicates school response data available for $50-69 \%$ of students. An "x" indicates school response data available for $<50 \%$ of students.

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[b]{3}{*}{Australia Belgium (Flemish) Bulgaria Canada Chile} \& \multicolumn{5}{|l|}{Percentage of Formally Scheduled School Time Averaged Across Students} \\
\hline \& Teaching Mathematics, Science, and Other Subjects \& Teaching Mathematics \& Curriculum Planning \({ }^{1}\) \& Administrative Duties \& Other Activities \({ }^{2}\) \\
\hline \& \[
\begin{array}{ll} 
\& 80(1.2) \\
r \& 85(1.1) \\
71 \& (3.6) \\
78 \& (1.0) \\
75 \& (1.3)
\end{array}
\] \& \begin{tabular}{rrr} 
\& \(61(2.3)\) \\
\(r\) \& \(70(1.7)\) \\
\(63(3.2)\) \\
\(43(1.3)\) \\
\(59(1.6)\)
\end{tabular} \& \(r \quad 3(0.6)\)
\(3(0.5)\)

$7(2.1)$

$8(0.4)$ \& \[
$$
\begin{array}{ll}
5 & (1.0) \\
1 & (0.3) \\
5 & (1.0) \\
2 & (0.5) \\
4 & (0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{rl} 
& 12(1.0) \\
r & 10(0.8) \\
& 15(1.2) \\
& 14(1.0) \\
& 13(0.7)
\end{array}
$$
\] <br>

\hline | Chinese Taipei |
| :--- |
| Cyprus |
| Czech Republic |
| England Finland | \& |  | $55(2.0)$ |
| :--- | :--- |
| $r$ | $92(1.3)$ |
|  | $70(2.1)$ |
| 5 | $87(0.9)$ |
|  | $85(0.6)$ | \& |  | $55(2.0)$ |
| :--- | :--- |
| $r$ | $92(1.3)$ |
|  | $46(2.1)$ |
|  | $80(1.3)$ |
|  | $47(1.4)$ | \& |  | $9(0.9)$ |
| ---: | ---: |
| $r$ | $2(0.4)$ |
|  | $12(1.6)$ |
| 5 | $1(0.3)$ |
|  | $2(0.3)$ | \& |  | $4(0.9)$ |
| :--- | :--- |
|  |  |
|  | $1(0.4)$ |
|  | $3(0.5)$ |
| $s$ | $2(0.3)$ |
|  | $1(0.4)$ | \& |  | $32(1.6)$ |
| ---: | ---: |
| $r$ | $6(0.8)$ |
|  | $15(1.0)$ |
| $s$ | $10(0.8)$ |
|  | $12(0.4)$ | <br>


\hline Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel \& |  | $\mathrm{x} x$ |
| :---: | :---: |
| $68(1.3)$ |  |
| 65 | $(2.0)$ |
|  | $67(2.0)$ |
| $r \quad 80(1.5)$ |  | \& |  | x x |
| :---: | :---: |
|  | $46(1.5)$ |
| $63(2.1)$ |  |
|  | $64(2.0)$ |
| $\mathrm{r} \quad 72(1.7)$ |  | \&  \& \[

$$
\begin{aligned}
& \text { x x } \\
& 5(0.4) \\
& 8(0.9) \\
& 1(0.2) \\
& 3(0.8)
\end{aligned}
$$

\] \& \[

$$
\begin{aligned}
& \text { x x } \\
& 17(0.9) \\
& 16(1.2) \\
& 22(1.7) \\
& 9(0.7)
\end{aligned}
$$
\] <br>

\hline | Italy |
| :--- |
| Japan Jordan |
| Korea, Rep. of Latvia (LSS) | \& \[

$$
\begin{array}{ll}
87 & (1.1) \\
68 & (1.8) \\
67 & (1.4) \\
54 & (1.3) \\
72 & (2.1)
\end{array}
$$

\] \& | 52 (0.8) |
| :--- |
| 63 (1.9) |
| 65 (1.5) |
| 54 (1.3) |
| 64 (2.4) | \& \[

$$
\begin{array}{r}
7(0.8) \\
7(0.8) \\
11(0.6) \\
11(0.6) \\
4(0.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
0(0.1) \\
4(0.4) \\
4(0.3) \\
14(0.8) \\
3(0.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
6(0.6) \\
21 \\
21 \\
\hline 17
\end{array}
$$ $$
\begin{array}{r}
(0.9) \\
21
\end{array}
$$(0.9)
\] <br>

\hline | Lithuania ${ }^{\text {* }}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& | 65 (1.5) |
| :--- |
| 52 (1.2) |
| 65 (1.0) |
| 56 (1.8) |
| 88 (1.3) | \& |  | $61(1.6)$ |
| ---: | ---: | ---: |
|  | $48(1.5)$ |
|  | $52(1.5)$ |
| $r$ | $50(2.0)$ |
|  | $88(1.3)$ | \& \[

$$
\begin{array}{rr}
10 & (0.8) \\
21 & (1.0) \\
11 & (0.4) \\
15 & (1.2) \\
2 & (0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
5 & (1.2) \\
5 & (0.2) \\
6 & (0.3) \\
6 & (1.0) \\
1 & (0.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{rr}
20 & (0.9) \\
22 & (0.9) \\
19 & (0.8) \\
24 & (1.2) \\
9 & (1.2)
\end{array}
$$
\] <br>

\hline Netherlands ${ }^{3}$
New Zealand
Philippines
Romania

Russian Federation ${ }^{4}$ \& $5 \quad$\begin{tabular}{cc}
88 \& $(0.9)$ <br>
83 \& $(1.2)$ <br>
70 \& $(1.9)$ <br>
\& $60(2.0)$ <br>
\& --

\end{tabular} \& \[

$$
\begin{array}{ll}
\text { s } & 75(2.6) \\
& 68(2.1) \\
& 57(2.2) \\
& 54(1.8) \\
& --
\end{array}
$$

\] \& \[

$$
\begin{gathered}
-- \\
3(0.6) \\
8(0.9) \\
10(0.8) \\
--
\end{gathered}
$$

\] \& \[

$$
\begin{aligned}
& -- \\
& 4(0.7) \\
& 3(0.6) \\
& 5(0.9) \\
& --
\end{aligned}
$$

\] \& \[

$$
\begin{array}{ll}
12 & (0.9) \\
10 & (0.8) \\
20 & (1.4) \\
25 & (1.5)
\end{array}
$$
\] <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& |  | 73 | $(0.8)$ |
| ---: | ---: | ---: |
| 69 | $(1.9)$ |  |
|  | $65(1.1)$ |  |
| $r$ | $71(1.9)$ |  |
| 60 | $(1.3)$ |  | \& |  | 55 | $(1.8)$ |
| :---: | :---: | :---: |
|  | 51 | $(2.2)$ |
|  | 58 | $(1.5)$ |
| $r$ | $52(2.2)$ |  |
|  | 51 | $(1.4)$ | \& |  | -- |
| ---: | ---: |
|  | $12(1.1)$ |
|  | $16(0.9)$ |
| $r$ | $6(0.7)$ |
|  | 16 |$(0.8)$ \& \[

$$
\begin{aligned}
& 3(0.3) \\
& 6(0.8) \\
& 5(0.4) \\
& 7(0.7) \\
& 4(0.6)
\end{aligned}
$$

\] \& |  | $24(0.7)$ |  |
| ---: | ---: | ---: |
|  | 12 | $(0.7)$ |
|  | 13 | $(0.6)$ |
| $r$ | $16(1.3)$ |  |
|  | $21(1.0)$ |  | <br>


\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& | 57 (1.4) |
| :--- |
| 67 (1.6) |
| 75 (1.3) | \& | 56 (1.4) |
| :--- |
| 61 (1.7) |
| 65 (1.7) | \& \[

$$
\begin{array}{ll}
22 & (1.1) \\
12 & (0.8) \\
13 & (0.8)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 2(0.6) \\
& 3(0.8) \\
& 2(0.4)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{ll}
19 & (1.1) \\
18 & (0.9) \\
11 & (0.8)
\end{array}
$$
\] <br>

\hline International Avg. \& 71 (0.3) \& 60 (0.3) \& 9 (0.2) \& 4 (0.1) \& 16 (0.2) <br>
\hline
\end{tabular}

Background data provided by teachers.
1 Includes individual curriculum planning and cooperative curriculum planning.
2 Includes student supervision (other than teaching), student counseling/appraisal, other non-student contact time, and other activities.
3 Netherlands: Data in other activities category reflects the total reported for curriculum planning, administrative duties and other activities.
4 Russian Federation: Formally scheduled school time is for instruction only; teachers are not formally scheduled for other activities.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash $(-)$ indicates data are not available.
An "r" indicates teacher response data available for $70-84 \%$ of students. An "s" indicates teacher response data available for $50-69 \%$ of students. An " $x$ " indicates teacher response data available for $<50 \%$ of students.

## Exhibit R3.9 Asking Students to Do Problem-Solving Activities or Computation During Mathematics Lessons

TIMSS1999
$\overbrace{\text { grade }}^{\text {th }}$
Mathematics

|  | Percentage of Students Whose Teachers Report Most or Every Lesson |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Explain Reasoning Behind an Idea | Represent and Analyze Relationships Using Tables, Charts, or Graphs | Work on Problems for Which There Is No Immediately Obvious Method of Solution | Write Equations to Represent Relationships | Practice Computational Skills |
| Australia | 62 (4.2) | 15 (2.9) | 10 (2.4) | 32 (4.1) | 55 (4.4) |
| Belgium (Flemish) | 67 (3.5) | 2 (0.8) | 5 (3.1) | 12 (2.0) | 76 (2.7) |
| Bulgaria | 93 (2.1) | 23 (3.7) | 25 (4.3) | 40 (5.3) | 69 (4.9) |
| Canada | 76 (2.7) | 20 (2.6) | 18 (2.8) | 44 (2.8) | 64 (3.3) |
| Chile | 69 (3.5) | 23 (3.2) | 27 (3.1) | 20 (3.2) | 81 (2.8) |
| Chinese Taipei | 54 (4.1) | 39 (4.4) | 11 (2.1) | 57 (4.2) | 54 (4.5) |
| Cyprus | 91 (2.7) | 13 (3.6) | 8 (2.6) | r 64 (5.1) | 57 (5.1) |
| Czech Republic | 94 (2.6) | 21 (4.0) | 22 (4.2) | 69 (5.4) | 81 (4.4) |
| England | s 70 (3.0) | 13 (2.7) | 6 (2.1) | $5 \quad 22$ (3.4) | 52 (3.6) |
| Finland | 75 (3.6) | 19 (3.6) | 16 (3.0) | 15 (3.0) | 84 (3.2) |
| Hong Kong, SAR | 33 (4.1) | 17 (3.5) | 18 (3.5) | 60 (3.5) | 78 (3.1) |
| Hungary | 79 (3.4) | 31 (3.6) | 22 (3.5) | 69 (3.8) | 90 (2.4) |
| Indonesia | 45 (4.4) | 45 (4.1) | 14 (3.2) | 67 (4.5) | 93 (2.4) |
| Iran, Islamic Rep. | 55 (4.5) | 26 (3.7) | 31 (4.0) | 23 (3.7) | 71 (3.5) |
| Israel | 75 (3.3) | 35 (3.7) | 17 (3.3) | 59 (3.5) | 56 (3.6) |
| Italy | 84 (3.0) | 44 (3.8) | 45 (3.6) | 30 (3.4) | 65 (3.4) |
| Japan | 82 (3.2) | 62 (4.1) | 41 (4.4) | 80 (3.0) | 62 (4.5) |
| Jordan | 73 (3.8) | 36 (4.5) | 16 (3.2) | 35 (3.9) | 91 (2.6) |
| Korea, Rep. of | 65 (3.2) | 38 (4.0) | 28 (3.5) | 65 (3.9) | 55 (4.3) |
| Latvia (LSS) | 61 (4.6) | 17 (3.7) | 12 (2.9) | 40 (4.3) | 91 (2.5) |
| Lithuania ${ }^{\text { }}$ | 73 (4.2) | 23 (3.5) | 17 (3.4) | 41 (4.3) | 92 (2.3) |
| Macedonia, Rep. of | 79 (3.4) | 32 (3.8) | 26 (3.2) | 49 (4.2) | 80 (3.6) |
| Malaysia | 49 (4.0) | 32 (3.8) | 41 (3.6) | 45 (3.9) | 88 (2.8) |
| Moldova | 93 (2.2) | 13 (3.1) | 20 (3.4) | 27 (3.4) | 82 (3.4) |
| Morocco | 57 (2.9) | 5 (1.4) | 11 (1.7) | 53 (3.0) | 74 (2.6) |
| Netherlands | 65 (5.6) | 28 (5.6) | 33 (6.4) | 23 (5.4) | 40 (4.8) |
| New Zealand | 56 (4.0) | 10 (2.6) | 10 (2.8) | 17 (3.0) | 67 (3.9) |
| Philippines | 70 (3.9) | 33 (3.8) | 25 (3.7) | 40 (4.2) | 95 (1.8) |
| Romania | 93 (2.2) | 30 (4.5) | 27 (4.2) | 33 (4.2) | 91 (2.4) |
| Russian Federation | 84 (3.3) | 11 (2.5) | 13 (2.9) | 40 (3.7) | 88 (2.3) |
| Singapore | 44 (4.9) | 14 (3.2) | 15 (3.4) | 29 (3.8) | 51 (4.4) |
| Slovak Republic | 89 (3.2) | 11 (2.9) | 25 (4.3) | 52 (4.9) | 87 (3.4) |
| Slovenia | 77 (3.3) | 41 (3.6) | 43 (4.0) | 82 (3.0) | 84 (2.8) |
| South Africa | 63 (3.5) | 27 (3.4) | 28 (4.0) | 44 (4.1) | 30 (3.8) |
| Thailand | 54 (3.9) | 12 (2.5) | 21 (3.4) | 25 (3.7) | 92 (2.1) |
| Tunisia | 81 (3.4) | 35 (3.8) | 10 (2.5) | 20 (3.7) | 56 (4.2) |
| Turkey | 69 (4.0) | 55 (3.5) | 24 (3.3) | 63 (2.9) | 79 (3.3) |
| United States | 72 (3.1) | 24 (2.6) | 19 (2.6) | 54 (2.8) | 66 (3.7) |
| International Avg. | 70 (0.6) | 26 (0.6) | 21 (0.6) | 43 (0.6) | 73 (0.6) |

[^83]
# Exhibit R3.10 Trends in Asking Students to Do Problem-Solving Activities During Most or Every Mathematics Lesson 

TIMSS1999
© ${ }_{\text {grade }}^{\text {th }}$

|  | Explain Reasoning Behind an Idea |  |  |  | Represent and Analyze Relationships Using Tables, Charts, or Graphs |  |  |  | Work on Problems for Which There Is No Immediately Obvious Method of Solution |  |  |  | Write Equations to Represent Relationships |  |  |  | Practice Computational Skills |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 |  | 1995-1999 Difference |  | $\begin{aligned} & \text { Percent of } \\ & \text { Students } \\ & 1999 \end{aligned}$ |  | 1995-1999 Difference |  | Percent of Students 1999 |  | 1995-1999 Difference |  | Percent of Students 1999 |  | 1995-1999 Difference |  | Percent of Students 1999 |  | 1995-1999 Difference |  |
| Australia | 62 (4.2) | $r$ | 7 (5.9) | - | 15 (2.9) |  | 7 (3.4) | - | 10 (2.4) |  | 5 (2.9) | - | 32 (4.1) | $r$ | 17 (4.8) | $\triangle$ | 55 (4.4) | $r$ | 4 (5.5) | - |
| Belgium (Flemish) | 67 (3.5) |  | -5 (5.8) | - | 2 (0.8) |  | 2 (0.8) | - | 5 (3.1) |  | 2 (3.5) | - | 12 (2.0) |  | 6 (2.8) | - | 76 (2.7) |  | 9 (4.7) | - |
| Canada | 76 (2.7) | $r$ | 5 (5.3) | - | 20 (2.6) |  | 14 (3.3) | $\triangle$ | 18 (2.8) |  | 6 (4.4) | $\bigcirc$ | 44 (2.8) |  | 16 (4.5) | $\pm$ | 64 (3.3) |  | 4 (5.7) | - |
| Cyprus | 91 (2.7) | $r$ | 2 (4.7) | $\bigcirc$ | 13 (3.6) | + | -12 (5.9) | - | 8 (2.6) | $r$ | -11 (5.3) | - | 64 (5.1) | $r$ | 15 (8.1) | - | 57 (5.1) | $r$ | 0 (8.1) | - |
| Czech Republic | 94 (2.6) |  | 12 (5.2) | - | 21 (4.0) |  | 0 (6.3) | - | 22 (4.2) |  | 3 (5.0) | - | 69 (5.4) |  | 7 (8.0) | - | 81 (4.4) |  | 4 (6.5) | - |
| England | 70 (3.0) | 5 | 5 (4.4) | - | 13 (2.7) | 5 | -4 (3.8) | 。 | 6 (2.1) | 5 | 1 (2.5) | - | 22 (3.4) | 5 | 1 (4.4) | - | 52 (3.6) | $s$ | 10 (4.5) | $\bigcirc$ |
| Hong Kong, SAR | 33 (4.1) |  | 0 (6.9) | - | 17 (3.5) |  | 1 (5.1) | - | 18 (3.5) |  | 8 (5.0) | - | 60 (3.5) |  | 20 (6.2) | $\triangle$ | 78 (3.1) |  | 23 (6.7) | $\triangle$ |
| Hungary | 79 (3.4) |  | -7 (4.7) | - | 31 (3.6) |  | 8 (5.0) |  | 22 (3.5) |  | 7 (4.7) | - | 69 (3.8) |  | 1 (5.5) | - | 90 (2.4) |  | 4 (3.6) | - |
| Iran, Islamic Rep. | 55 (4.5) |  | -4 (7.2) | - | 26 (3.7) | $r$ | 7 (5.8) | - | 31 (4.0) |  | 15 (5.4) | - | 23 (3.7) |  | 2 (5.7) | - | 71 (3.5) |  | 28 (6.4) | $\triangle$ |
| Israel ${ }^{\dagger}$ | 74 (3.6) | $r$ | 49 (7.7) | - | 34 (4.1) |  | -24 (9.6) | - | 15 (3.5) | $r$ | -59 (7.2) | $\nabla$ | 58 (3.8) | $r$ | 14 (9.7) | - | 53 (4.0) | $r$ | 8 (10.7) |  |
| Italy | 84 (3.5) |  | 3 (4.9) | - | 42 (4.5) |  | 3 (6.5) | - | 45 (4.1) |  | 19 (5.9) | $\triangle$ | 27 (4.0) |  | 9 (5.2) | - | 62 (4.4) |  | 7 (6.4) | - |
| Japan | 82 (3.2) |  | 5 (4.7) | - | 62 (4.1) |  | 6 (5.9) | - | 41 (4.4) |  | 18 (5.7) | $\triangle$ | 80 (3.0) |  | 9 (5.2) | - | - - |  | - - |  |
| Korea, Rep. of | 65 (3.2) |  | -11 (4.9) | - | 38 (4.0) |  | -2 (6.2) | - | 28 (3.5) |  | 3 (5.2) | - | 65 (3.9) |  | 10 (6.0) | - | 55 (4.3) |  | 27 (5.6) | $\triangle$ |
| Latvia (LSS) | 61 (4.6) | $r$ | -15 (5.9) | - | 17 (3.7) | $r$ | -9 (5.9) | - | 12 (2.9) | $r$ | -14 (5.2) | - | 40 (4.3) |  | -1 (6.4) | - | - - |  | -- |  |
| Lithuania | 73 (4.2) |  | 0 (5.6) | - | 23 (3.5) |  | 15 (4.2) | $\triangle$ | 17 (3.4) |  | 5 (4.5) | - | 41 (4.3) |  | -2 (6.2) | - | 92 (2.3) |  | -6 (2.5) | - |
| Netherlands |  |  |  |  |  |  | - - |  |  |  |  |  |  |  | -- |  | - - |  | -- |  |
| New Zealand | 56 (4.0) |  | -7 (6.1) | - | 10 (2.6) |  | 3 (3.6) | - | 10 (2.8) |  | 5 (3.3) | - | 17 (3.0) |  | 7 (3.9) | $\bullet$ | 67 (3.9) |  | 20 (6.2) | $\triangle$ |
| Romania | 93 (2.2) |  | -1 (2.8) | - | 30 (4.5) |  | 6 (5.8) | , | 27 (4.2) |  | -13 (6.0) | - | 33 (4.2) |  | 11 (5.6) | - | 91 (2.4) |  | 3 (3.6) | - |
| Russian Federation | 84 (3.3) |  | -7 (4.1) | - | 11 (2.5) |  | 6 (3.1) | - | 13 (2.9) |  | 2 (3.7) | - | 40 (3.7) |  | 9 (5.9) | - | 88 (2.3) |  | 1 (3.7) | - |
| Singapore | 44 (4.9) |  | 2 (7.0) | - | 14 (3.2) |  | -1 (4.5) | - | 15 (3.4) |  | 8 (4.1) | - | 29 (3.8) |  | 4 (5.4) | - | 51 (4.4) |  | 1 (6.3) |  |
| Slovak Republic | 89 (3.2) |  | 4 (4.6) | - | 11 (2.9) |  | 1 (3.9) | - | 25 (4.3) |  | 4 (5.5) | - | 52 (4.9) |  | -10 (6.5) | - | 87 (3.4) |  | 24 (5.7) | $\triangle$ |
| Slovenia | 77 (3.3) | $r$ | 31 (5.9) | $\triangle$ | 41 (3.6) | $r$ | 19 (5.3) | $\triangle$ | 43 (4.0) | $r$ | -1 (6.6) | - | 82 (3.0) | $r$ | 16 (5.4) | $\triangle$ | 84 (2.8) | $r$ | 5 (5.2) | - |
| Thailand ${ }^{\text {+ }}$ | 54 (3.9) | $r$ | 23 (6.6) | - | 12 (2.5) | 5 | 8 (3.2) | - | 21 (3.4) | $s$ | 2 (6.2) | - | 25 (3.7) | $r$ | 8 (5.9) | - | 92 (2.1) | $r$ | 5 (4.9) | - |
| United States | 72 (3.1) | $r$ | 5 (4.8) | - | 24 (2.6) |  | 12 (3.8) | $\triangle$ | 19 (2.6) | r | 7 (3.7) | - | 54 (2.8) | $r$ | 17 (5.0) | $\triangle$ | 66 (3.7) | $r$ | 8 (5.8) | - |
| International Avg. ${ }^{\text {s }}$ | 72 (0.8) |  | 1 (1.2) | - | 23 (0.8) |  | 4 (1.1) | $\triangle$ | 21 (0.8) |  | 4 (1.1) | $\triangle$ | 45 (0.8) |  | 7 (1.2) | $\triangle$ | 71 (0.8) |  | 8 (1.2) | $\triangle$ |



Background data provided by teachers.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " r " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates teacher response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999.

|  | Almost Always |  | Pretty Often |  | Once in a While |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 16(0.7) \\ 7(0.7) \\ 11(0.8) \\ 19(0.7) \\ 26 \end{array}(0.7)$ | $\begin{array}{ll} 512 & (5.9) \\ 531 & (13.8) \\ 476 & (6.5) \\ 518 & (3.6) \\ 400 & (4.6) \end{array}$ | $\begin{array}{ll} 37 & (1.2) \\ 20 & (0.8) \\ 19 & (1.6) \\ 33 & (0.8) \\ 24 & (0.6) \end{array}$ | $\begin{aligned} & 525(5.3) \\ & 560(4.4) \\ & 516 \\ & 53.6) \\ & 534 \\ & 398 \end{aligned}(4.3)$ | 38 (1.0) <br> 47 (1.1) <br> 46 (1.3) <br> 36 (0.9) <br> 29 (0.7) | $\begin{array}{ll} 535 & (5.6) \\ 567 & (4.0) \\ 523 & (6.6) \\ 536 & (2.7) \\ 400 & (6.8) \end{array}$ | $\begin{array}{ll} 10 & (0.7) \\ 27 & (1.1) \\ 24 & (1.3) \\ 11 & (0.7) \\ 22 & (0.8) \end{array}$ | $\begin{array}{ll} 515 & (9.4) \\ 552 & (4.8) \\ 511 & (7.7) \\ 531 & (4.6) \\ 374 & (5.5) \end{array}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | 11 (0.5) <br> 16 (1.1) <br> 11 (0.9) <br> 14 (0.8) <br> 6 (0.7) | $\begin{aligned} & 596 \\ & 576 \\ & 476 \\ & (6.2) \\ & 522 \\ & (8.1) \\ & 486 \\ & 510 \\ & 510 \end{aligned}(8.2)$ | 31 (0.8) <br> 37 (1.0) <br> 36 (1.4) <br> 41 (1.3) <br> 21 (1.1) | $\begin{array}{ll} 600 & (4.0) \\ 491 & (2.8) \\ 530 & (4.2) \\ 499 & (5.2) \\ 526 & (4.2) \end{array}$ | 43 (0.8) <br> 32 (1.0) <br> 37 (1.5) <br> 34 (1.0) <br> 57 (1.2) | $\begin{array}{ll} 590 & (4.4) \\ 474 & (2.9) \\ 519 & (5.0) \\ 505 & (4.9) \\ 524 & (2.8) \end{array}$ | 15 (0.7) <br> 15 (0.8) <br> 16 (1.2) <br> 11 (0.8) <br> 16 (0.9) | 540 (6.5) 455 (5.1) 499 (8.3) 489 (8.2) $507 \text { (5.7) }$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{r} 6(0.3) \\ 6(0.5) \\ 4(0.3) \\ 13(0.5) \\ 22(1.0) \end{array}$ | $573(8.0)$ $495(8.2)$ $380(12.6)$ $406(8.3)$ $449(7.3)$ | $\begin{array}{ll} 24 & (0.8) \\ 18 & (0.8) \\ 15 & (0.8) \\ 18 & (0.6) \\ 26 & (1.0) \end{array}$ | $\begin{array}{ll} 583 & (6.5) \\ 525 & (6.3) \\ 385 & (8.1) \\ 420 & (4.9) \\ 466 & (5.2) \end{array}$ | 56 (0.9) <br> 49 (1.0) <br> 46 (1.2) <br> 38 (0.9) <br> 34 (0.9) | $\begin{array}{ll} 587 \\ 540 & (4.0) \\ 424 & (5.4) \\ 433 & (4.3) \\ 489 & (4.9) \end{array}$ | $\begin{array}{ll} 15 & (0.7) \\ 27 & (1.2) \\ 35 & (1.2) \\ 32 & (1.0) \\ 18 & (0.9) \end{array}$ | $\begin{array}{ll} 570 & (6.1) \\ 531 & (5.5) \\ 388 & (6.1) \\ 422 & (4.2) \\ 468 & (5.6) \end{array}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 10(0.6) \\ 2(0.2) \\ 31(1.1) \\ 3(0.3) \\ 36 \end{array}(1.1)$ | 456 (7.7) <br> 419 (5.8) <br> 580 (7.5) <br> 510 (4.2) | $\begin{array}{ll} 19 & (0.8) \\ 17 & (0.7) \\ 30 & (0.9) \\ 12 & (0.6) \\ 34 & (0.9) \end{array}$ | 494 (6.2) <br> 590 (3.5) <br> 438 (4.6) <br> 602 (3.2) <br> 503 (4.9) | 38 (1.0) 55 (0.8) 28 (0.9) 47 (0.8) 26 (0.8) | $\begin{array}{ll} 489 & (4.0) \\ 583 & (2.1) \\ 450 & (5.7) \\ 595 & (2.3) \\ 505 & (5.1) \end{array}$ | $\begin{array}{rr} 33 & (1.2) \\ 27 & (1.0) \\ 12 & (0.6) \\ 37 & (0.8) \\ 4 & (0.4) \end{array}$ | 471 (4.5) <br> 564 (3.3) <br> 426 (6.9) <br> 573 (2.7) <br> 490 (6.9) |
| Lithuania Macedonia, Rep. of Malaysia <br> Moldova <br> Morocco | 26 (0.9) <br> 6 (0.4) <br> 14 (1.0) <br> 25 (0.9) | $\begin{gathered} -- \\ 445(5.9) \\ 522(8.9) \\ 456(7.4) \\ 325(5.0) \end{gathered}$ | 31 (1.0) <br> 17 (0.7) <br> 26 (1.3) <br> 30 (0.7) | $\begin{gathered} -- \\ 461(4.9) \\ 522(5.4) \\ 468(5.2) \\ 340(8.8) \end{gathered}$ | 31 (1.1) <br> 40 (1.1) <br> 43 (1.5) <br> 23 (0.9) | $\begin{gathered} -- \\ 451(4.3) \\ 526(4.9) \\ 479(4.7) \\ 362(5.3) \end{gathered}$ | 12 (0.7) <br> 37 (1.2) <br> 17 (0.9) <br> 22 (1.0) | 445 (6.6) <br> 511 (4.8) <br> 470 (6.6) <br> 341 (6.9) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 7(0.6) \\ 20(0.9) \\ 40 \\ \hline 1.1 .1) \\ 13 \\ \hline \end{array}(0.8)$ | $\begin{array}{ll} 544 & (10.2) \\ 462 & (6.8) \\ 346 & (6.3) \\ 451 & (7.7) \\ 506 & (6.7) \end{array}$ | $\begin{array}{ll} 20 & (0.9) \\ 39 & (1.0) \\ 25 & (0.8) \\ 18 & (0.9) \\ 23 & (1.2) \end{array}$ | $\begin{array}{ll} 549 & (8.5) \\ 501 & (5.2) \\ 351 & (8.2) \\ 473 & (6.1) \\ 538 & (8.3) \end{array}$ | 49 (1.6) <br> 35 (0.9) <br> 25 (0.7) <br> 46 (1.3) <br> 46 (1.4) | 542 (8.1) <br> 504 (5.6) <br> 350 (7.1) <br> 487 (5.8) <br> 533 (6.0) | $\begin{array}{r} 23(1.5) \\ 7(0.5) \\ 10(0.5) \\ 23(1.0) \\ 17 \end{array}$ | $\begin{array}{ll} 530 & (8.4) \\ 473 & (10.0) \\ 335 & (8.9) \\ 470 & (7.7) \\ 521 & (6.3) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | 16 (0.8) <br> 13 (0.7) <br> 11 (0.8) <br> 36 (1.0) <br> 8 (0.4) | $\begin{array}{ll} 578 & (7.8) \\ 528 & (5.5) \\ 514 & (6.7) \\ 261 & (5.6) \\ 463 & (8.7) \end{array}$ | 34 (0.9) <br> 35 (1.3) <br> 24 (1.1) <br> 24 (0.9) <br> 24 (0.9) | $\begin{array}{ll} 606 & (6.9) \\ 542 & (4.4) \\ 537 & (4.3) \\ 281 & (10.3) \\ 476 & (6.5) \end{array}$ | 36 (1.1) 41 (1.1) 52 (1.2) 18 (0.7) 45 (0.9) | $\begin{array}{ll} 617 & (6.3) \\ 535 & (4.4) \\ 535 & (3.2) \\ 307 & (11.0) \\ 474 & (5.0) \end{array}$ | $\begin{array}{ll} 14 & (0.8) \\ 11 & (0.8) \\ 13 & (0.8) \\ 21 & (1.3) \\ 24 & (1.0) \end{array}$ | $\begin{array}{ll} 599 & (6.1) \\ 514 & (6.2) \\ 518 & (5.8) \\ 270 & (9.6) \\ 450 & (5.5) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 17 & (0.7) \\ 11 & (0.6) \\ 23 & (0.9) \end{array}$ | $\begin{aligned} & 444(3.2) \\ & 419(5.7) \\ & 489(5.1) \end{aligned}$ | $\begin{array}{ll} 22 & (0.7) \\ 15 & (0.6) \\ 31 & (0.8) \end{array}$ | $\begin{aligned} & 452(4.6) \\ & 442(5.2) \\ & 509(3.8) \end{aligned}$ | $\begin{array}{ll} 37 & (0.9) \\ 45 & (0.9) \\ 34 & (0.7) \end{array}$ | $\begin{aligned} & 451(3.5) \\ & 437(5.2) \\ & 515 \end{aligned}(4.1)$ | $\begin{aligned} & 24(0.8) \\ & 29(1.1) \\ & 12(0.7) \end{aligned}$ | $\begin{aligned} & 443(2.5) \\ & 425(4.9) \\ & 493 \\ & \hline \end{aligned}(6.8)$ |
| International Avg. | 15 (0.1) | 474 (1.4) | 26 (0.2) | 493 (0.9) | 39 (0.2) | 497 (0.9) | 19 (0.2) | 478 (1.0) |

[^84][^85]|  | Almost Always |  | Pretty Often |  | Once in a While |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 51(2.0) \\ 16(1.3) \\ 5(0.6) \\ 44(1.9) \\ 14(1.3) \end{array}$ | $\begin{aligned} & 531 \text { (5.7) } \\ & 553 \text { (6.4) } \\ & 486 \text { (14.2) } \\ & 532 \text { (3.2) } \\ & 387 \text { (8.1) } \end{aligned}$ | $\begin{array}{r} 36(1.4) \\ 30(1.6) \\ 7(0.8) \\ 35(1.2) \\ 12(0.8) \end{array}$ | $\begin{aligned} & 525(5.5) \\ & 567 \text { (6.0) } \\ & 505 \text { (10.4) } \\ & 535 \text { (3.0) } \\ & 395(7.8) \end{aligned}$ | $\begin{array}{r} 9(1.0) \\ 49(2.1) \\ 35(2.0) \\ 17(1.5) \\ 30(1.3) \end{array}$ | $508(10.4)$ $560(4.5)$ $520(6.2)$ $523(4.1)$ $401(5.8)$ | $\begin{array}{r} 3(1.2) \\ 5(1.2) \\ 52(2.3) \\ 3(0.9) \\ 43(2.2) \end{array}$ | $\begin{array}{ll} 488 & (25.9) \\ 528 & (11.4) \\ 512 & (7.3) \\ 523 & (14.8) \\ 390 & (5.2) \end{array}$ |
| Chinese Taipei <br> Cyprus <br> Czech Republic <br> England <br> Finland | $\begin{array}{r} 2(0.2) \\ 6(0.6) \\ 14(2.1) \\ 30(1.6) \\ 19 \end{array}$ | 453 (8.2) <br> 520 (7.5) <br> 518 (6.5) <br> 520 (6.0) | $\begin{array}{r} 7(0.4) \\ 18(1.0) \\ 27(1.7) \\ 53(1.4) \\ 32(1.6) \end{array}$ | $\begin{aligned} & 543 \text { (7.9) } \\ & 472 \text { (4.8) } \\ & 530 \\ & 500 \\ & 500 \\ & 519 \end{aligned}(3.3)$ | 45 (1.0) <br> 41 (1.1) <br> 48 (2.5) <br> 16 (1.1) <br> 46 (2.5) | $\begin{aligned} & 591(4.0) \\ & 484(3.1) \\ & 518(4.6) \\ & 460(5.9) \\ & 523(3.2) \end{aligned}$ | $\begin{array}{r} 46(1.1) \\ 35(1.8) \\ 12(2.0) \\ 1(0.3) \\ 2(0.6) \end{array}$ | $\begin{gathered} 591(5.0) \\ 478(3.0) \\ 507(8.0) \\ \sim \sim \\ \sim \sim \end{gathered}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{r} 26(1.4) \\ 13(1.2) \\ 2(0.3) \\ 5(0.3) \\ 45(1.8) \end{array}$ | $\begin{gathered} 591(5.0) \\ 538(7.5) \\ \sim \\ \sim \\ 385(11.0) \\ 463(4.9) \end{gathered}$ | $\begin{array}{r} 51(1.0) \\ 22(1.4) \\ 11(1.0) \\ 6(0.4) \\ 25(0.9) \end{array}$ | $\begin{aligned} & 582(4.5) \\ & 536 \\ & 3 \\ & 395 \\ & \hline \end{aligned}(7.9)$ | $\begin{array}{ll} 21 & (1.4) \\ 39 & (2.0) \\ 46 & (1.8) \\ 21 & (1.0) \\ 22 & (1.2) \end{array}$ | $\begin{aligned} & 575(5.2) \\ & 535(4.5) \\ & 423(5.8) \\ & 432(4.5) \\ & 480(6.6) \end{aligned}$ | $\begin{array}{r} 2(0.5) \\ 27(2.5) \\ 41(2.4) \\ 68(1.3) \\ 8(1.0) \end{array}$ | $\sim \sim$ $522(6.3)$ $385(6.3)$ $424(3.8)$ $453(14.8)$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 35(1.9) \\ 0(0.1) \\ 12(0.8) \\ 0(0.1) \\ 9(1.2) \end{array}$ | $\begin{gathered} 485(4.4) \\ \sim \sim \\ 380(5.9) \\ \sim \sim \\ \sim \\ \sim 01 \end{gathered}$ | $\begin{array}{r} 22(0.9) \\ 3(0.4) \\ 16(0.8) \\ 1(0.2) \\ 14(1.2) \end{array}$ | $\begin{gathered} 483(5.3) \\ 545(8.2) \\ 410(6.5) \\ \sim \sim \\ 515(7.8) \end{gathered}$ | $\begin{array}{ll} 26 & (1.5) \\ 28 & (2.1) \\ 29 & (1.1) \\ 13 & (0.5) \\ 39 & (1.8) \end{array}$ | $\begin{aligned} & 477(5.6) \\ & 580(3.7) \\ & 445(4.5) \\ & 574(5.1) \\ & 502(4.8) \end{aligned}$ | 16 (1.7) <br> 68 (2.3) <br> 43 (1.8) <br> 86 (0.7) <br> 38 (2.5) | $\begin{aligned} & 473(7.6) \\ & 580(2.4) \\ & 450(4.5) \\ & 590(2.3) \\ & 506(3.8) \end{aligned}$ |
| Lithuania ${ }^{\text { }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} \text { - - } \\ 13(1.0) \\ 1(0.2) \\ 13(0.8) \\ 14(0.9) \end{array}$ | $\begin{gathered} 436(7.1) \\ \sim \\ 469(7.3) \\ 312(9.7) \end{gathered}$ | 15 (1.1) <br> 4 (0.5) <br> 19 (1.0) <br> 23 (1.0) | $\begin{aligned} & -- \\ & 461(6.4) \\ & 515(14.6) \\ & 470(5.4) \\ & 328(6.3) \end{aligned}$ | $\begin{array}{ll} 33 & (1.5) \\ 23 & (1.2) \\ 38 & (1.3) \\ 21 & (0.8) \end{array}$ | 457 (5.2) <br> 522 (5.6) <br> 475 (4.7) <br> 345 (8.2) | $\begin{aligned} & -- \\ & 40(2.2) \\ & 72(1.6) \\ & 29(1.8) \\ & 42(1.2) \end{aligned}$ | 454 (4.3) <br> 520 (4.6) <br> 468 (6.4) <br> 355 (3.8) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 67(2.0) \\ 43(1.8) \\ 9(0.6) \\ 4(0.5) \\ 16(1.2) \end{array}$ | $\begin{aligned} & 547(6.5) \\ & 492(6.6) \\ & 297(7.4) \\ & 422(12.4) \\ & 508(8.7) \end{aligned}$ | $\begin{array}{r} 29(1.6) \\ 38(1.5) \\ 14(0.7) \\ 6(0.6) \\ 19(1.0) \end{array}$ | $\begin{aligned} & 533(9.5) \\ & 493(4.8) \\ & 324(8.4) \\ & 456(11.8) \\ & 528(8.4) \end{aligned}$ | $\begin{array}{r} 4(0.6) \\ 16(1.6) \\ 28(1.1) \\ 23(1.5) \\ 47(1.3) \end{array}$ | $\begin{aligned} & 494(16.4) \\ & 494(9.4) \\ & 354(7.6) \\ & 483(7.6) \\ & 533(6.3) \end{aligned}$ | $\begin{array}{r} 0(0.1) \\ 3(0.9) \\ 49(1.6) \\ 67(2.0) \\ 18(1.7) \end{array}$ | 499 (27.5) <br> 359 (6.1) <br> 479 (5.5) <br> 532 (7.6) |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 36(1.5) \\ 21(1.7) \\ 6(0.8) \\ 45(1.8) \\ 3(0.4) \end{array}$ | 610 (7.4) 540 (6.7) 506 (11.1) 261 (7.9) 451 (16.0) | $\begin{array}{r} 50(1.0) \\ 26(1.4) \\ 11(1.0) \\ 21(0.9) \\ 7(0.5) \end{array}$ | $\begin{aligned} & 610(6.1) \\ & 544(6.0) \\ & 520(6.4) \\ & 296(10.6) \\ & 467(9.6) \end{aligned}$ | $\begin{array}{ll} 14 & (1.2) \\ 40 & (2.2) \\ 42 & (1.9) \\ 15 & (1.0) \\ 35 & (1.1) \end{array}$ | $\begin{aligned} & 572(6.5) \\ & 526(4.3) \\ & 532(4.1) \\ & 306(15.5) \\ & 482(6.1) \end{aligned}$ | $\begin{array}{r} 1(0.2) \\ 14(1.8) \\ 41(2.6) \\ 19(1.4) \\ 55(1.6) \end{array}$ | $\quad \sim \sim$ $531(7.8)$ 536 (3.3) 268 (13.4) 460 (5.2) |
| Tunisia <br> Turkey <br> United States | $\begin{array}{r} 5(0.4) \\ 5(0.3) \\ 42(2.3) \end{array}$ | $\begin{aligned} & 425(6.0) \\ & 385(9.2) \\ & 516(5.1) \end{aligned}$ | $\begin{array}{r} 7(0.4) \\ 5(0.4) \\ 28(1.1) \end{array}$ | $\begin{aligned} & 433(6.3) \\ & 404(7.6) \\ & 506(4.6) \end{aligned}$ | $\begin{array}{ll} 28 & (1.2) \\ 27 & (1.1) \\ 22 & (1.5) \end{array}$ | $\begin{aligned} & 447(3.1) \\ & 432(5.9) \\ & 493(4.8) \end{aligned}$ | $\begin{array}{r} 60(1.5) \\ 63(1.4) \\ 8(1.2) \end{array}$ | $\begin{aligned} & 453(2.9) \\ & 439(4.3) \\ & 471 \text { (7.4) } \end{aligned}$ |
| International Avg. | 19 (0.2) | 469 (2.0) | 20 (0.2) | 482 (1.1) | 29 (0.2) | 488 (1.2) | 32 (0.3) | 476 (2.2) |

Background data provided by students.

* The use of calculators on TIMSS was not allowed in 1995 or in 1999.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year:

[^86]Exhibit R3.13 Trends in Students' Reports on Frequency of Calculator Use in Mathematics Class*

TIMSS1999
8 .
Mathematics



Background data provided by students.

* The use of calculators on TIMSS was not allowed in 1995 or in 1999.
${ }^{\dagger}$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{3}{*}{} \& \multicolumn{6}{|c|}{Percentage of Students} <br>
\hline \& \& \multicolumn{5}{|r|}{Ways in Which Students Use Calculators At Least Once or Twice a Week} <br>
\hline \& Ever Use Calculators \& Checking Answers \& Tests and Exams \& Routine Computations \& Solving Complex Problems \& Exploring Number Concepts <br>
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& $$
\begin{array}{r}
6(2.1) \\
7(2.5) \\
25(3.9) \\
3(1.0) \\
32(3.2)
\end{array}
$$ \& $$
\begin{array}{ll}
81 & (4.0) \\
55 & (4.6) \\
30 & (4.3) \\
82 & (2.3) \\
35 & (3.0)
\end{array}
$$ \& $$
\begin{array}{r}
61(4.0) \\
34(3.5) \\
10(2.9) \\
58(2.9) \\
9(2.1)
\end{array}
$$ \& $88(3.0)$

45

$r$ $43(5.7)$ \& \[
$$
\begin{array}{ll}
81 & (3.3) \\
53 & (4.5) \\
33 & (5.2) \\
91 & (1.8) \\
33 & (3.4)
\end{array}
$$

\] \& | $57(4.7)$ |
| ---: |
|  |
|  |
|  |
|  |
|  |
| $r \quad 27(4.0)$ |
|  |
|  |
| $69(3.5)$ |
|  |
|  | <br>


\hline | Chinese Taipei |
| :--- |
| Cyprus |
| Czech Republic |
| England Finland | \& \[

$$
\begin{array}{r}
55(4.6) \\
30(4.1) \\
5(2.3) \\
0(0.4) \\
8(2.3)
\end{array}
$$

\] \& |  | $5(1.7)$ |
| ---: | ---: |
|  | $44(4.8)$ |
|  | $60(4.9)$ |
|  | $74(3.6)$ |
|  | $56(4.3)$ | \& |  | $2(1.0)$ |
| ---: | ---: |
|  | $1(0.1)$ |
| $r$ | $18(3.6)$ |
|  | $32(3.4)$ |
|  | $23(3.8)$ | \&  \& \[

$$
\begin{array}{lr} 
& 9(2.5) \\
r & 28(4.9) \\
& 60(5.0) \\
s & 72(3.8) \\
& 68(4.1)
\end{array}
$$

\] \& |  | $8(2.3)$ |
| ---: | ---: |
|  | $14(3.3)$ |
|  | $22(4.6)$ |
|  | $41(4.1)$ |
|  | $32(4.1)$ | <br>

\hline Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel \& $$
\begin{array}{r}
1(0.9) \\
20(3.1) \\
37(4.8) \\
59(4.5) \\
3(0.7)
\end{array}
$$ \& \[

$$
\begin{array}{r}
85(2.8) \\
53(3.5) \\
11(2.7) \\
9(2.5) \\
78(3.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
58(4.2) \\
13(2.8) \\
6(2.2) \\
2(1.1) \\
69(3.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
88 & (2.8) \\
34 & (3.7) \\
12 & (3.1) \\
13 & (4.1) \\
80 & (2.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{rr} 
& 74(3.6) \\
& 49(3.9) \\
& 27(4.3) \\
& 5(2.1) \\
r & 66(3.6)
\end{array}
$$
\] \& $39(3.9)$

$15(2.9)$

$17(2.9)$
$r$$\quad 8(2.2)$ <br>

\hline | Italy |
| :--- |
| Japan |
| Jordan |
| Korea, Rep. of Latvia (LSS) | \& | 13 (2.1) |
| :--- |
| 81 (3.3) |
| 38 (4.4) |
| 72 (3.4) |
| 33 (3.5) | \& \[

$$
\begin{array}{r}
66(2.8) \\
0(0.0) \\
20(3.9) \\
1(0.9) \\
23(3.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(2.8) \\
1(0.7) \\
2(1.1) \\
1(0.9) \\
2(1.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
58(3.2) \\
5(2.0) \\
21(3.7) \\
2(1.2) \\
26(3.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
68(3.4) \\
4(1.7) \\
23(3.8) \\
5(1.7) \\
32(3.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
21(3.3) \\
1(1.0) \\
13(2.8) \\
2(1.2) \\
12(2.8)
\end{array}
$$
\] <br>

\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{r}
8(2.3) \\
49(4.0) \\
67(4.4) \\
21(3.3) \\
30(2.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
69(4.1) \\
32(4.0) \\
9(2.4) \\
59(4.1) \\
29(2.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
15(3.2) \\
1(0.8) \\
0(0.0) \\
11(3.0) \\
8(1.5)
\end{array}
$$

\] \& | 56 (4.2) |
| :--- |
| 31 (4.2) |
| 7 (2.0) |
| 48 (4.0) |
| 40 (2.7) | \& \[

$$
\begin{array}{ll}
70 & (3.9) \\
24 & (3.2) \\
11 & (2.4) \\
45 & (3.9) \\
18 & (2.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
32(4.0) \\
15(2.6) \\
4(1.5) \\
21(3.4) \\
20(2.9)
\end{array}
$$
\] <br>

\hline | Netherlands |
| :--- |
| New Zealand |
| Philippines |
| Romania |
| Russian Federation | \& \[

$$
\begin{array}{r}
1(0.1) \\
5(2.1) \\
56(4.1) \\
64(4.4) \\
14(2.7)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 91(2.9) \\
& 76(3.7) \\
& 17(2.7) \\
& 16(3.1) \\
& 58(3.9)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
68(5.4) \\
46(4.2) \\
7(2.2) \\
1(0.0) \\
3(1.3)
\end{array}
$$

\] \& | 97 (1.8) |
| :--- |
| 85 (3.2) |
| 10 (2.8) |
| 17 (3.5) |
| 47 (4.4) | \& \[

$$
\begin{array}{r}
90(3.0) \\
73 \\
73 \\
15 \\
(3.6) \\
6 \\
\hline
\end{array}
$$(1.9)

\] \& \[

$$
\begin{array}{r}
65(6.3) \\
59(4.1) \\
10(2.2) \\
5(2.1) \\
15(3.0)
\end{array}
$$
\] <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& \[
$$
\begin{array}{r}
0(0.0) \\
3(1.7) \\
31(4.2) \\
18(2.9) \\
62(4.1)
\end{array}
$$

\] \& | 88 (3.0) |
| :--- |
| 61 (4.3) |
| 26 (4.0) |
| 53 (3.9) |
| 11 (2.0) | \& | 61 (4.5) |
| :--- |
| 15 (3.5) |
| 4 (1.8) |
| 41 (4.5) |
| 1 (0.9) | \& | 85 (3.5) |
| :--- |
| 57 (4.5) |
| 23 (3.7) |
| 46 (4.2) |
| 13 (2.9) | \& | 93 (2.5) |
| :--- |
| 72 (4.6) |
| 23 (3.6) |
| 53 (4.0) |
| 13 (2.6) | \& \[

$$
\begin{array}{r}
67(3.9) \\
55(4.7) \\
7(2.0) \\
52(3.3) \\
9(2.4)
\end{array}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& \[

$$
\begin{array}{r}
36(3.9) \\
59(4.8) \\
5(1.2)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 20(3.3) \\
& 15(2.8) \\
& 69(3.5)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
3(1.6) \\
3(1.1) \\
45(3.2)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 15(3.0) \\
& 12(2.6) \\
& 62(3.9)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
5(1.7) \\
17(2.9) \\
75(3.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
7(1.9) \\
10(2.4) \\
59(3.2)
\end{array}
$$
\] <br>

\hline International Avg. \& 28 (0.5) \& 44 (0.6) \& 20 (0.4) \& 43 (0.6) \& 43 (0.6) \& 26 (0.5) <br>
\hline
\end{tabular}

Background data provided by teachers.

* The use of calculators on TIMSS was not allowed in 1995 or in 1999.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^87]

Background data provided by teachers.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An "s" indicates teacher response data available for $50-69 \%$ of students.

|  | Sometimes or Always |  | Never or Rarely |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) <br> Bulgaria Canada Chile | $\begin{array}{r} 27(4.1) \\ 3(1.1) \\ 7(2.1) \\ 24(2.9) \\ 28(3.6) \end{array}$ | $\begin{aligned} & 526 \text { (7.2) } \\ & 567 \text { (19.0) } \\ & 544 \text { (28.1) } \\ & 531 \text { (4.9) } \\ & 397 \text { (8.0) } \end{aligned}$ | $\begin{array}{ll} 73 & (4.1) \\ 97 & (1.1) \\ 93 & (2.1) \\ 76 & (2.9) \\ 72 & (3.6) \end{array}$ | 527 (6.1) <br> 567 (3.9) <br> 510 (6.4) <br> 535 (3.4) <br> 390 (5.5) |
| Chinese Taipei Cyprus Czech Republic England $s$ Finland | $\begin{array}{r} 4(1.6) \\ 16(3.7) \\ 3(1.7) \\ 14(2.5) \\ 10(2.6) \end{array}$ | $\begin{aligned} & 577 \text { (22.9) } \\ & 488 \text { (5.6) } \\ & 537 \text { (9.7) } \\ & 518 \text { (9.1) } \\ & 542 \text { (10.7) } \end{aligned}$ | 96 (1.6) <br> 84 (3.7) <br> 97 (1.7) <br> 86 (2.5) <br> 90 (2.6) | 585 (4.1) <br> 475 (2.3) <br> 520 (4.6) <br> 509 (5.6) <br> 518 (2.6) |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 3(1.4) \\ 5(1.8) \\ 23(3.5) \\ 10(2.2) \\ 18(3.0) \end{array}$ | $\begin{aligned} & 636 \text { (14.9) } \\ & 509 \text { (8.4) } \\ & 418 \text { (12.0) } \\ & 422 \text { (12.5) } \\ & 469(9.9) \end{aligned}$ | $\begin{aligned} & 97(1.4) \\ & 95(1.8) \\ & 77(3.5) \\ & 90(2.2) \\ & 82(3.0) \end{aligned}$ | $\begin{aligned} & 581(4.4) \\ & 532(3.9) \\ & 399(6.7) \\ & 422(3.5) \\ & 469(5.1) \end{aligned}$ |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of <br> Latvia (LSS) | $\begin{array}{r} 30(3.5) \\ 1(0.7) \\ 28(3.9) \\ 16(2.9) \\ 6(2.0) \end{array}$ | $\begin{gathered} 468(6.9) \\ \sim \sim \\ 423(7.7) \\ 586(5.6) \\ 525(20.7) \end{gathered}$ | 70 (3.5) <br> 99 (0.7) <br> 72 (3.9) <br> 84 (2.9) <br> 94 (2.0) | $\begin{aligned} & 484(4.7) \\ & 579(1.8) \\ & 428(4.6) \\ & 588(2.3) \\ & 504(3.6) \end{aligned}$ |
| Lithuania ${ }^{\text { }}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{array}{ll} 12 & (2.8) \\ 13 & (3.0) \\ 18 & (3.3) \\ 29 & (4.3) \\ 24 & (3.0) \end{array}$ | $\begin{aligned} & 503 \text { (11.8) } \\ & 422(15.2) \\ & 514 \text { (11.1) } \\ & 483 \text { (9.1) } \\ & 344(7.1) \end{aligned}$ | 88 (2.8) <br> 87 (3.0) <br> 82 (3.3) <br> 71 (4.3) <br> 76 (3.0) | $\begin{aligned} & 479(4.9) \\ & 450(4.8) \\ & 520(5.0) \\ & 462(4.9) \\ & 335(2.7) \end{aligned}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{ll} 10 & (5.3) \\ 27 & (3.5) \\ 46 & (4.5) \\ 24 & (4.3) \\ 34 & (3.7) \end{array}$ | $\begin{aligned} & 510(44.2) \\ & 529 \text { (10.0) } \\ & 345 \text { (9.0) } \\ & 474 \text { (13.7) } \\ & 539(8.4) \end{aligned}$ | $\begin{aligned} & 90(5.3) \\ & 73(3.5) \\ & 54(4.5) \\ & 76(4.3) \\ & 66(3.7) \end{aligned}$ | $\begin{aligned} & 540(6.9) \\ & 481(5.9) \\ & 343(8.4) \\ & 473(7.0) \\ & 520(6.9) \end{aligned}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 20(3.6) \\ 6(2.2) \\ 11(2.8) \\ 40(3.7) \\ 43(3.8) \end{array}$ | $\begin{aligned} & 616(14.5) \\ & 562(16.5) \\ & 526(10.4) \\ & 252(6.6) \\ & 476(9.2) \end{aligned}$ | $\begin{array}{ll} 80 & (3.6) \\ 94 & (2.2) \\ 89 & (2.8) \\ 60 & (3.7) \\ 57 & (3.8) \end{array}$ | $\begin{aligned} & 602(6.8) \\ & 530(3.9) \\ & 531(2.7) \\ & 291(9.2) \\ & 461(6.5) \end{aligned}$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 15(3.1) \\ & 27(3.3) \\ & 24(2.8) \end{aligned}$ | $\begin{aligned} & 445(6.3) \\ & 434(9.1) \\ & 499(8.3) \end{aligned}$ | $\begin{array}{ll} 85 & (3.1) \\ 73 & (3.3) \\ 76 & (2.8) \end{array}$ | $\begin{aligned} & 446(2.7) \\ & 426(4.9) \\ & 504(4.9) \end{aligned}$ |
| International Avg. | 18 (0.5) | 491 (2.2) | 82 (0.5) | 487 (0.8) |

Background data provided by teachers.

* Based on average response to questions about assigning homework based on small investigation(s) or gathering data, working individually on long term projects or experiments, and working as a small group on long term projects or experiments.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An "r" indicates teacher response data available for $70-84 \%$ of students. An "s" indicates teacher response data available for $50-69 \%$ of students.

|  | Almost Always |  | Pretty Often |  | Once in a While or Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia | 18 (1.1) | 506 (7.2) | 40 (1.1) | 531 (5.4) | 42 (1.6) | 529 (5.8) |
| Belgium (Flemish) | 19 (0.9) | 534 (4.1) | 56 (1.7) | 568 (4.1) | 25 (1.6) | 558 (8.8) |
| Bulgaria | 10 (0.7) | 484 (8.5) | 20 (1.5) | 532 (10.4) | 70 (1.6) | 512 (5.0) |
| Canada | 25 (1.6) | 516 (3.9) | 50 (1.4) | 534 (2.9) | 25 (1.1) | 541 (4.1) |
| Chile | 47 (1.1) | 392 (4.2) | 32 (0.8) | 399 (5.6) | 21 (0.9) | 389 (6.0) |
| Chinese Taipei | 27 (1.2) | 589 (5.1) | 46 (1.0) | 590 (4.2) | 27 (1.5) | 576 (6.5) |
| Cyprus | 16 (0.8) | 459 (4.9) | 65 (1.0) | 487 (1.9) | 19 (1.0) | 461 (4.1) |
| Czech Republic | 7 (1.2) | 494 (10.9) | 33 (1.7) | 522 (4.9) | 60 (2.3) | 522 (4.5) |
| England | 14 (0.9) | 463 (5.6) | 46 (1.6) | 500 (4.8) | 40 (1.9) | 507 (5.4) |
| Finland | 9 (0.8) | 494 (6.0) | 30 (1.2) | 515 (3.7) | 61 (1.4) | 527 (2.8) |
| Hong Kong, SAR | 9 (0.7) | 569 (7.3) | 37 (1.6) | 579 (4.9) | 54 (2.2) | 587 (5.2) |
| Hungary | 7 (0.5) | 508 (8.3) | 18 (0.9) | 533 (4.6) | 75 (1.1) | 534 (4.0) |
| Indonesia | 13 (0.7) | 415 (6.6) | 42 (1.3) | 408 (5.6) | 45 (1.5) | 396 (5.5) |
| Iran, Islamic Rep. | 23 (0.9) | 411 (5.1) | 27 (0.9) | 421 (5.1) | 49 (1.3) | 430 (3.5) |
| Israel | 23 (0.9) | 439 (5.3) | 39 (1.0) | 473 (4.3) | 39 (1.3) | 486 (5.5) |
| Italy | 9 (0.8) | 452 (8.7) | 19 (0.9) | 476 (6.3) | 72 (1.3) | 485 (3.7) |
| Japan | 12 (1.4) | 571 (6.1) | 30 (1.5) | 582 (3.2) | 58 (2.1) | 579 (2.6) |
| Jordan | 30 (1.1) | 427 (5.3) | 35 (1.0) | 432 (5.6) | 35 (1.1) | 441 (4.5) |
| Korea, Rep. of | 7 (0.5) | 587 (6.9) | 18 (0.8) | 601 (4.5) | 75 (1.2) | 584 (1.9) |
| Latvia (LSS) | 3 (0.4) | 476 (13.2) | 11 (0.8) | 502 (7.5) | 86 (0.9) | 507 (3.6) |
| Lithuania ${ }^{ \pm}$ |  | - | - - | - - | -- | -- |
| Macedonia, Rep. of | 17 (0.7) | 417 (6.4) | 34 (1.1) | 463 (4.8) | 49 (1.2) | 457 (4.8) |
| Malaysia | 12 (0.5) | 522 (6.1) | 31 (1.0) | 527 (5.9) | 56 (1.3) | 515 (4.5) |
| Moldova | 30 (1.5) | 471 (5.4) | 40 (1.3) | 475 (5.2) | 30 (1.2) | 464 (4.1) |
| Morocco r | 33 (1.5) | 333 (4.2) | 32 (1.1) | 335 (4.6) | 35 (1.3) | 353 (4.4) |
| Netherlands | 14 (1.5) | 510 (10.5) | 47 (1.9) | 538 (6.7) | 39 (1.7) | 555 (8.2) |
| New Zealand | 24 (1.6) | 466 (7.8) | 35 (1.2) | 503 (6.1) | 41 (1.7) | 499 (5.6) |
| Philippines | 44 (1.3) | 350 (7.2) | 30 (1.0) | 360 (6.9) | 27 (1.1) | 329 (6.4) |
| Romania | 30 (1.3) | 467 (6.6) | 39 (1.3) | 486 (6.4) | 30 (1.5) | 474 (7.5) |
| Russian Federation | 26 (1.1) | 517 (6.6) | 50 (1.3) | 541 (6.5) | 24 (1.3) | 510 (6.5) |
| Singapore | 19 (0.9) | 597 (8.3) | 45 (1.0) | 609 (6.5) | 36 (1.4) | 602 (6.4) |
| Slovak Republic | 8 (0.7) | 496 (7.2) | 49 (1.6) | 540 (4.3) | 43 (1.7) | 535 (4.3) |
| Slovenia | 26 (1.1) | 508 (4.0) | 47 (1.1) | 536 (3.3) | 27 (1.3) | 544 (4.6) |
| South Africa | 42 (1.6) | 261 (6.6) | 31 (1.0) | 287 (11.0) | 27 (1.1) | 287 (10.0) |
| Thailand | 32 (1.2) | 464 (5.8) | 33 (0.7) | 467 (5.1) | 36 (1.1) | 472 (6.5) |
| Tunisia | 55 (1.1) | 449 (2.9) | 36 (0.9) | 449 (3.1) | 9 (0.6) | 441 (5.0) |
| Turkey | 13 (0.7) | 411 (7.2) | 11 (0.6) | 423 (7.2) | 76 (1.0) | 437 (4.2) |
| United States | 40 (1.6) | 491 (3.7) | 46 (1.3) | 520 (4.3) | 14 (0.9) | 493 (6.1) |
| International Avg. | 21 (0.2) | 473 (1.2) | 36 (0.2) | 493 (0.9) | 43 (0.2) | 490 (0.9) |

[^88]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " r " indicates a $70-84 \%$ student response rate.


## REFERENCE 4

School Contexts for
Learning and Instruction

\begin{tabular}{|c|c|c|c|c|c|}
\hline \& \multicolumn{5}{|c|}{Percentage of Students Affected by Shortage or Inadequacy} \\
\hline \& Instructional Materials \& Budget for Supplies \& School Buildings/ Grounds \& Heating/Cooling and Lighting \& Instructional Space \\
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& \[
\begin{array}{r}
26(3.7) \\
6(2.2) \\
92(2.2) \\
45(2.8) \\
23(3.1)
\end{array}
\] \& \[
\begin{array}{r}
22(4.1) \\
5(2.1) \\
80(5.8) \\
43(2.8) \\
34(3.0)
\end{array}
\] \& \[
\begin{array}{ll}
32(4.1) \\
20 \& (3.3) \\
71 \& (4.3) \\
29 \& (2.8) \\
38 \& (3.6)
\end{array}
\] \& \[
\begin{array}{r}
21(3.5) \\
4(1.8) \\
72(4.1) \\
11(1.9) \\
22(2.9)
\end{array}
\] \& \[
\begin{array}{ll}
27 \& (4.0) \\
20 \& (4.2) \\
63 \& (5.0) \\
25 \& (2.4) \\
31 \& (3.8)
\end{array}
\] \\
\hline \begin{tabular}{l}
Chinese Taipei \\
Cyprus \\
Czech Republic \\
England \\
Finland
\end{tabular} \& \begin{tabular}{r} 
\\
\\
\\
\\
\\
\\
\(r \quad 7(4.4)\) \\
\\
\hline \(22(5.0)\) \\
\(37(4.9)\) \\
\\
\\
\end{tabular} \(31(4.0)\) \& \(45(4.0)\)

$r \quad 52(0.1)$

$31(4.5)$

$10(2.8)$ \& | $59(4.1)$ |
| ---: |
|  |
|  |
| $61(0.2)$ |
|  |
|  |
| $15(3.3)$ |
| $42(5.3)$ |
|  |
|  |
|  | \& $41(3.9)$

$r \quad 5(0.3)$

$17(3.4)$
$16(3.6)$ \&  <br>

\hline Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel \& $$
\begin{array}{ll}
35 & (3.9) \\
27 & (3.9) \\
45 & (4.4) \\
26 & (4.0) \\
15 & (3.1)
\end{array}
$$ \& \[

$$
\begin{array}{ll}
21 & (3.9) \\
25 & (3.7) \\
36 & (4.3) \\
61 & (3.7) \\
18 & (3.3)
\end{array}
$$

\] \& | 57 (4.8) |
| :--- |
| 32 (3.8) |
| 39 (4.1) |
| 68 (4.0) |
| 42 (4.5) | \& \[

$$
\begin{array}{ll}
24(3.4) \\
17 & (3.4) \\
36 & (4.6) \\
50 & (4.7) \\
28 & (3.8)
\end{array}
$$

\] \& | 57 (4.6) |
| :--- |
| 39 (4.2) |
| 44 (3.9) |
| 54 (3.9) |
| 33 (4.4) | <br>


\hline | Italy Japan Jordan |
| :--- |
| Korea, Rep. of Latvia (LSS) | \& | 28 (3.5) |
| :--- |
| 17 (2.9) |
| 74 (4.1) |
| 37 (3.9) |
| 80 (3.8) | \& | 28 (3.6) |
| :--- |
| 14 (3.0) |
| 64 (4.3) |
| 29 (4.0) |
| 87 (3.3) | \& \[

$$
\begin{array}{ll}
31 & (3.7) \\
29 & (3.8) \\
75 & (3.9) \\
51 & (4.5) \\
72 & (4.0)
\end{array}
$$

\] \& | 15 (2.7) |
| :--- |
| 31 (3.5) |
| 74 (3.7) |
| 52 (4.2) |
| 65 (4.9) | \& | 35 (3.4) |
| :--- |
| 34 (3.5) |
| 69 (3.7) |
| 55 (4.2) |
| 65 (4.2) | <br>


\hline | Lithuania ${ }^{\text { }}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{ll}
82 & (3.3) \\
38 & (4.3) \\
38 & (4.3) \\
97 & (0.9) \\
59 & (4.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
65 & (3.9) \\
75 & (3.8) \\
44 & (4.2) \\
95 & (1.8) \\
77 & (3.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
31 & (4.0) \\
74 & (3.7) \\
40 & (4.6) \\
77 & (3.9) \\
58 & (4.3)
\end{array}
$$

\] \& | 45 (4.1) |
| :--- |
| 52 (4.2) |
| 26 (3.4) |
| 91 (2.4) |
| 45 (4.1) | \& | 56 (3.8) |
| :--- |
| 63 (4.4) |
| 40 (4.2) |
| 69 (4.0) |
| 45 (4.0) | <br>


\hline | Netherlands |
| :--- |
| New Zealand Philippines Romania Russian Federation | \& \[

$$
\begin{array}{ll}
\text { r } & 10(4.0) \\
& 24(3.6) \\
67(4.0) \\
& 54(4.6) \\
92(2.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
\text { r } & 19(6.4) \\
& 27(3.5) \\
& 52(4.4) \\
& 74(3.8) \\
& 81(3.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
45 & (7.0) \\
37 & (4.2) \\
56 & (3.9) \\
50 & (4.8) \\
73 & (3.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
9(2.8) \\
6(2.1) \\
49 \\
\hline 96 \\
36 \\
63
\end{array}
$$(4.9)
\] \& $26(5.3)$

$29(3.9)$
$52(4.3)$
$46(4.3)$
$69(3.2)$ <br>

\hline | Singapore |
| :--- |
| Slovak Republic Slovenia South Africa Thailand | \& | 10 (2.2) |
| :--- |
| 44 (4.4) |
| 55 (4.2) |
| 67 (4.1) |
| 86 (3.0) | \& \[

$$
\begin{array}{r}
7(2.0) \\
67(4.0) \\
68(4.0) \\
66(4.1) \\
84(2.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
23 & (2.6) \\
31 & (4.6) \\
60 & (4.5) \\
61 & (4.3) \\
81 & (3.2)
\end{array}
$$

\] \& | 11 (2.4) |
| :--- |
| 12 (2.9) |
| 49 (4.3) |
| 59 (4.1) |
| 63 (4.1) | \& \[

$$
\begin{array}{ll}
26 & (3.3) \\
42 & (5.0) \\
62 & (4.2) \\
57 & (3.7) \\
78 & (3.1)
\end{array}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& $83(3.2)$

$80(3.6)$

$r \quad 22(2.9)$ \& $$
\begin{array}{r}
77(3.5) \\
\\
60(4.0) \\
\mathrm{r} \quad 27(4.1)
\end{array}
$$ \& $87(2.8)$

$78(3.6)$
$r \quad 33(3.4)$ \& $48(4.5)$
$74(3.5)$

$r \quad 17(3.5)$ \& $$
\begin{array}{r}
76(3.7) \\
75(4.0) \\
r \quad 33(3.4)
\end{array}
$$ <br>

\hline International Avg. \& 45 (0.6) \& 47 (0.6) \& 50 (0.7) \& 36 (0.6) \& 47 (0.6) <br>
\hline
\end{tabular}

[^89][^90]
## Exhibit R4.2 Shortages or Inadequacies in Equipment and Materials for Mathematics Instruction That Affect Schools' Capacity to Provide Instruction in Mathematics Some or A Lot

\begin{tabular}{|c|c|c|c|c|c|}
\hline \& \multicolumn{5}{|c|}{Percentage of Students Affected by Shortage or Inadequacy} <br>
\hline \& Computers for Mathematics Instruction \& Computer Software for Mathematics Instruction \& Calculators for Mathematics Instruction \& Library Materials Relevant to Mathematics Instruction \& Audio-Visual Resources for Mathematics Instruction <br>
\hline Australia Belgium (Flemish) Bulgaria Canada Chile \& $$
\begin{aligned}
& 49(4.7) \\
& 30(3.3) \\
& 86(3.0) \\
& 47(2.9) \\
& 46
\end{aligned}
$$ \& $$
\begin{aligned}
& 50(4.7) \\
& 25(3.4) \\
& 80(3.5) \\
& 59(2.7) \\
& 50(3.7)
\end{aligned}
$$ \& $$
\begin{array}{r}
11(2.7) \\
2(1.1) \\
53(5.0) \\
26(3.0) \\
35(3.5)
\end{array}
$$ \& $$
\begin{array}{ll}
20 & (3.4) \\
15 & (3.0) \\
78 & (3.6) \\
34 & (3.7) \\
47 & (3.4)
\end{array}
$$ \& $$
\begin{array}{ll}
22 & (3.9) \\
19 & (3.0) \\
72 & (4.2) \\
34 & (3.4) \\
49 & (3.9)
\end{array}
$$ <br>
\hline Chinese Taipei Cyprus Czech Republic England Finland \& $57(4.3)$

$54(0.2)$
$37(4.0)$
$r$
$51(5.2)$

$49(4.1)$ \& |  |
| ---: |
| $66(4.2)$ |
| $r \quad 45(0.3)$ |
|  |
|  |
| $33(4.0)$ |
| $53(5.0)$ |
|  |
|  |
| $54(3.9)$ | \& |  | $47(4.7)$ |
| ---: | ---: |
|  | $12(0.2)$ |
|  | $8(3.0)$ |
| $r$ | $23(3.8)$ |
|  | $13(3.2)$ | \& \[

$$
\begin{array}{rl} 
& 56(4.4) \\
& 21(0.2) \\
& 16(3.8) \\
r & 29(4.5) \\
& 14(3.2)
\end{array}
$$

\] \& | $63(4.2)$ |
| ---: |
|  |
| $30(0.2)$ |
|  |
| $14(3.5)$ |
| $r$ |
| $30(4.5)$ |
|  |
|  |
|  | <br>


\hline | Hong Kong, SAR |
| :--- |
| Hungary |
| Indonesia |
| Iran, Islamic Rep. Israel | \& | 61 (4.8) |
| :--- |
| 49 (4.5) |
| 37 (4.8) |
| 71 (4.4) |
| 45 (5.0) | \& \[

$$
\begin{array}{ll}
70(4.2) \\
54 & (4.7) \\
37 & (4.7) \\
73 & (4.2) \\
47 & (4.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
16 & (3.1) \\
22 & (3.4) \\
38 & (4.6) \\
63 & (4.2) \\
25 & (4.1)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 32(3.4) \\
& 18(3.4) \\
& 52(4.8) \\
& 75(3.6) \\
& 41
\end{aligned}
$$

\] \& | 45 (4.5) |
| :--- |
| 31 (4.0) |
| 43 (4.8) |
| 69 (4.7) |
| 45 (4.3) | <br>


\hline | Italy |
| :--- |
| Japan |
| Jordan |
| Korea, Rep. of Latvia (LSS) | \& | 38 (3.8) |
| :--- |
| 33 (4.2) |
| 63 (4.3) |
| 64 (4.0) |
| 73 (4.3) | \& | 50 (3.7) |
| :--- |
| 42 (4.2) |
| 61 (4.3) |
| 71 (3.8) |
| 73 (4.4) | \& \[

$$
\begin{array}{r}
18(3.3) \\
7(2.2) \\
42(4.5) \\
42(3.9) \\
37(4.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
32 & (3.8) \\
12 & (2.8) \\
59 & (4.6) \\
58 & (4.5) \\
67 & (3.9)
\end{array}
$$

\] \& | 42 (3.6) |
| :--- |
| 25 (3.9) |
| 67 (4.5) |
| 70 (4.0) |
| 69 (4.7) | <br>


\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{ll}
76 & (3.7) \\
88 & (2.9) \\
40 & (4.4) \\
81 & (3.2) \\
54 & (4.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
79 & (3.6) \\
90 & (2.5) \\
42 & (4.6) \\
79 & (3.6) \\
54 & (4.8)
\end{array}
$$

\] \& | 45 (4.2) |
| :--- |
| 84 (3.1) |
| 29 (3.6) |
| 78 (3.5) |
| 55 (4.8) | \& \[

$$
\begin{array}{ll}
56 & (4.0) \\
88 & (2.7) \\
47 & (4.0) \\
90 & (1.9) \\
62 & (4.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
72 & (3.9) \\
90 & (2.5) \\
48 & (4.2) \\
90 & (2.4) \\
67 & (4.8)
\end{array}
$$
\] <br>

\hline  \& |  |
| ---: | | $(6.8)$ |
| ---: |
| $47(4.2)$ |
|  |
| $57(3.8)$ |
|  |
| $85(3.3)$ |
| $89(2.2)$ | \& $r$

$47(60.6)$

$88(3.3)$
$83(2.5)$

$87(2.9)$ \& |  |  |
| ---: | ---: |
|  | $2(1.2)$ |
| $21(3.4)$ |  |
|  | $54(3.8)$ |
| $69(4.1)$ |  |
|  | $69(4.3)$ | \& \[

$$
\begin{array}{ll}
\text { r } & 18(5.0) \\
& 20(3.6) \\
& 66(3.8) \\
68(4.3) \\
& 71(3.8)
\end{array}
$$
\] \& $18(4.3)$

$65(3.6)$

$69(3.9)$
$82(3.5)$ <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& \[
$$
\begin{array}{ll}
30 & (4.2) \\
85 & (3.3) \\
51 & (4.2) \\
76 & (3.2) \\
74 & (3.8)
\end{array}
$$

\] \& | 44 (4.8) |
| :--- |
| 87 (2.9) |
| 50 (4.3) |
| 74 (3.6) |
| 75 (3.7) | \& \[

$$
\begin{array}{r}
5(1.8) \\
35(4.8) \\
18 \\
67 \\
67 \\
\text { (3.4) } \\
54
\end{array}
$$(3.8)

\] \& \[

$$
\begin{array}{ll}
13 & (2.8) \\
41 & (5.0) \\
39 & (3.6) \\
74 & (3.5) \\
88 & (3.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
17 & (3.4) \\
60 & (3.8) \\
42 & (4.0) \\
75 & (3.9) \\
88 & (3.0)
\end{array}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& $38(4.0)$

$67(4.1)$

$r \quad 47(4.2)$ \& \[
$$
\begin{array}{r}
39(4.1) \\
\\
68(4.0) \\
r \quad 48(4.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
34(4.1) \\
37(3.7) \\
\text { r } \quad 16(3.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
40(4.2) \\
78(3.3) \\
r \quad 29(4.0)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
42(4.2) \\
79(3.9) \\
r \quad 25(3.2)
\end{array}
$$
\] <br>

\hline International Avg. \& 57 (0.7) \& 59 (0.7) \& 35 (0.6) \& 46 (0.6) \& 50 (0.6) <br>
\hline
\end{tabular}

[^91]( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
An " $r$ " indicates school response data available for $70-84 \%$ of students.

| Percentage |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |

Background data provided by schools.
1 Ratio of grade 8 enrollment to total computers for instructional use by grade 8 teachers and students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^92]

[^93] some totals may appear inconsistent.

An "r" indicates school response data available for 70-84\% of students.
$\qquad$


## APPENDIX A

Overview of TIMSS Procedures:
Mathematics Achievement


## History

TIMSS 1999 represents the continuation of a long series of studies conducted by the International Association for the Evaluation of Educational Achievement (iea). Since its inception in 1959, the iea has conducted more than 15 studies of cross-national achievement in the curricular areas of mathematics, science, language, civics, and reading. IEA conducted its First International Science Study (fiss) in 197071 and the Second International Science Study (siss) in 1983-84. The First and Second International Mathematics Studies (fims and sims) were conducted in 1964 and 198o-82, respectively. The Third International Mathematics and Science Study (timss), conducted in 1994-1995, was the largest and most complex iea study to date, and included both mathematics and science at third and fourth grades, seventh and eighth grades, and the final year of secondary school.

In 1999, timss again assessed eighth-grade students in both mathematics and science to measure trends in student achievement since 1995. timss 1999 was also known as timss-Repeat, or timss-r.

## Participants in TIMSS

Of the 42 countries that participated in TIMSs ${ }^{1}$ at the eighth grade in 1995, 26 availed themselves of the opportunity to measure changes in the achievement of their students by also taking part in 1999 (see Exhibit A.1). Twelve additional countries participated in 1999, for a total of 38 countries. Of those taking part in 1999, 19 had also participated in 1995 at the fourth grade. ${ }^{2}$ Since fourth-grade students in 1995 were in eighth grade in 1999, these countries can compare the eighthgrade performance of this cohort of students with their performance at the fourth grade, as well as with the eighth-grade performance of students in other countries.

[^94]$\qquad$
$\qquad$ C. (D) (E)


## Developing the TIMSS 1999 Mathematics Test

The timss curriculum framework underlying the mathematics tests was developed for timss in 1995 by groups of mathematics educators with input from the timss National Research Coordinators (NRCs). As shown in Exhibit A.2, the mathematics curriculum framework contains three dimensions or aspects. The content aspect represents the subject matter content of school mathematics. The performance expectations aspect describes, in a non-hierarchical way, the many kinds of performances or behaviors that might be expected of students in school mathematics. The perspectives aspect focuses on the development of students' attitudes, interest, and motivation in mathematics. Because the frameworks were developed to include content, performance expectations, and perspectives for the entire span of curricula from the beginning of schooling through the completion of secondary school, some aspects may not be reflected in the eighth-grade timss assessment. ${ }^{3}$ Working within the framework, mathematics test specifications for timss in 1995 were developed that included items representing a wide range of mathematics topics and eliciting a range of skills from the students. The 1995 tests were developed through an international consensus involving input from experts in mathematics and measurement specialists, ensuring they reflected current thinking and priorities in the mathematics.

About one-third of the items in the 1995 assessment were kept secure to measure trends over time; the remaining items were released for public use. An essential part of the development of the 1999 assessment, therefore, was to replace the released items with items of similar content, format, and difficulty. With the assistance of the Science and Mathematics Item Replacement Committee, a group of internationally prominent mathematics and science educators nominated by participating countries to advise on subject-matter issues in the assessment, over 300 mathematics and science items were developed as potential replacements. After an extensive process of review and field testing, 114 items were selected for use as replacements in the 1999 mathematics assessment.

Exhibit A. 3 presents the five content areas included in the 1999 mathematics test and the numbers of items and score points in each area. Distributions are also included for the five performance categories derived from the performance expectations aspect of the curriculum framework. Exhibit A. 4 shows how the trend and replacement items were distributed across these content areas and performance categories. About one-fourth of the items were in the free-response format, requiring students to generate and write their own answers. Designed to take about

[^95]one-third of students' test time, some free-response questions asked for short answers while others required extended responses with students showing their work or providing explanations for their answers. The remaining questions used a multiple-choice format. In scoring the tests, correct answers to most questions were worth one point. Consistent with the approach of allotting students longer response time for the constructed-response questions than for multiple-choice questions, however, responses to some of these questions (particularly those requiring extended responses) were evaluated for partial credit, with a fully correct answer being awarded two points (see later section on scoring). The total number of score points available for analysis thus somewhat exceeds the number of items.

Every effort was made to help ensure that the tests represented the curricula of the participating countries and that the items exhibited no bias towards or against particular countries. The final forms of the test were endorsed by the nRCS of the participating countries. ${ }^{4}$ In addition, countries had an opportunity to match the content of the test to their curriculum. They identified items measuring topics not covered in their intended curriculum. The information from this Test-Curriculum Matching Analysis, provided in Appendix C, indicates that omitting such items has little effect on the overall pattern of results.

[^96]| Content | Performance <br> Expectations |
| :---: | :---: |
| Numbers | Knowing |
| Measurement | Using Routine Procedures |
| Geometry | Investigating and Problem <br> Solving |
| Proportionality |  |
| Functions, Relations, and | Mathematical Reasoning |
| Equations |  |
| Probability and Statistics |  |
| Elementanicating |  |
| Validation, and Structure |  |


| Perspectives |
| :---: |
| Attitudes |
| Careers |
| Participation |
| Increasing Interest |
| Habits of Mind |


| Content Category | Percentage of Items | Total Number of Items | Number of MultipleChoice Items | Number of FreeResponse Items ${ }^{1}$ | Number of Score Points ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fractions and Number Sense | 38 | 61 | 47 | 14 | 62 |
| Measurement | 15 | 24 | 15 | 9 | 26 |
| Data Representation, Analysis and Probability | 13 | 21 | 19 | 2 | 22 |
| Geometry | 13 | 21 | 20 | 1 | 21 |
| Algebra | 22 | 35 | 24 | 11 | 38 |
| Total | 100 | 162 | 125 | 37 | 169 |
| Performance Category | Percentage of Items | Total Number of Items | Number of MultipleChoice Items | Number of FreeResponse Items ${ }^{1}$ | Number of Score Points ${ }^{2}$ |
| Knowing | 19 | 30 | 28 | 2 | 30 |
| Using Routine Procedures | 23 | 38 | 28 | 10 | 39 |
| Using Complex Procedures | 24 | 39 | 34 | 5 | 40 |
| Investigating and Solving Problems | 31 | 51 | 34 | 17 | 53 |
| Communicating and Reasoning | 2 | 4 | 1 | 3 | 7 |
| Total | 100 | 162 | 125 | 37 | 169 |


| Content Category |  |  | Repl | ment is |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of Items | Number of Points | Number of Items | Number of Points | Number of Items | Number of Points |
| Fractions and Number Sense | 17 | 17 | 44 | 45 | 61 | 62 |
| Measurement | 6 | 6 | 18 | 20 | 24 | 26 |
| Data Representation, Analysis and Probability | 8 | 8 | 13 | 14 | 21 | 22 |
| Geometry | 6 | 6 | 15 | 15 | 21 | 21 |
| Algebra | 11 | 11 | 24 | 27 | 35 | 38 |
| Total | 48 | 48 | 114 | 121 | 162 | 169 |
| Performance Category |  |  | Repl | ment s |  |  |
|  | Number of Items | Number of Points | Number of Items | Number of Points | Number of Items | Number of Points |
| Knowing | 16 | 16 | 14 | 14 | 30 | 30 |
| Using Routine Procedures | 8 | 8 | 30 | 31 | 38 | 39 |
| Using Complex Procedures | 13 | 13 | 26 | 27 | 39 | 40 |
| Investigating and Solving Problems | 11 | 11 | 40 | 42 | 51 | 53 |
| Communicating and Reasoning | - | - | 4 | 7 | 4 | 7 |
| Total | 48 | 48 | 114 | 121 | 162 | 169 |

## TIMSS Test Design

Not all of the students in the timss assessment responded to all of the mathematics items. To ensure broad subject-matter coverage without overburdening individual students, timss used a rotated design that included both the mathematics and science items. Thus, the same students participated in both the mathematics and science testing. As in 1995, the 1999 assessment consisted of eight booklets, each requiring go minutes of response time. Each participating student was assigned one booklet only. In accordance with the design, the mathematics and science items were assembled into 26 clusters (labeled A through Z). The secure trend items were in clusters A through H , and items replacing the released 1995 items in clusters I through Z. Eight of the clusters were designed to take 12 minutes to complete; 10 of the clusters, 22 minutes; and 8 clusters, 10 minutes. In all, the design provided 396 testing minutes, 198 for mathematics and 198 for science. Cluster A was a core cluster assigned to all booklets. The remaining clusters were assigned to the booklets in accordance with the rotated design so that representative samples of students responded to each cluster. ${ }^{5}$

## Background Questionnaires

timss in 1999 administered a broad array of questionnaires to collect data on the educational context for student achievement and to measure trends since 1995. National Research Coordinators, with the assistance of their curriculum experts, provided detailed information on the organization, emphases, and content coverage of the mathematics and science curriculum. The students who were tested answered questions pertaining to their attitudes towards mathematics and science, their academic self-concept, classroom activities, home background, and out-of-school activities. The mathematics and science teachers of sampled students responded to questions about teaching emphasis on the topics in the curriculum frameworks, instructional practices, professional training and education, and their views on mathematics and science. The heads of schools responded to questions about school staffing and resources, mathematics and science course offerings, and teacher support.

[^97]
## Translation and Verification

The timss instruments were prepared in English and translated into 33 languages, with 10 of the 38 countries collecting data in two languages. In addition, it sometimes was necessary to modify the international versions for cultural reasons, even in the nine countries that tested in English. This process represented an enormous effort for the national centers, with many checks along the way. The translation effort included (1) developing explicit guidelines for translation and cultural adaptation; (2) translation of the instruments by the national centers in accordance with the guidelines, using two or more independent translations; (3) consultation with subject-matter experts on cultural adaptations to ensure that the meaning and difficulty of items did not change; (4) verification of translation quality by professional translators from an independent translation company; (5) corrections by the national centers in accordance with the suggestions made; (6) verification by the International Study Center that corrections were made; and (7) a series of statistical checks after the testing to detect items that did not perform comparably across countries. ${ }^{6}$

## Population Definition and Sampling

timss in 1995 had as its target population students enrolled in the two adjacent grades that contained the largest proportion of 13 -year-old students at the time of testing, which were seventh- and eighth-grade students in most countries. timss in 1999 used the same definition to identify the target grades, but assessed students in the upper of the two grades only, which was the eighth grade in most countries. ${ }^{7}$

The selection of valid and efficient samples is crucial to the quality and success of an international comparative study such as timss. The accuracy of the survey results depends on the quality of sampling information and that of the sampling activities themselves. For timss, nRCS worked on all phases of sampling with staff from Statistics Canada. nrcs received training in how to select the school and student samples and in the use of the sampling software. In consultation with the timss sampling referee (Keith Rust, Westat, Inc.), staff from Statistics Canada reviewed the national sampling plans, sampling data, sampling frames, and sample execution. The sampling documentation was used by the International Study Center, in consultation with Statistics Canada and the sampling referee, to evaluate the quality of the samples.

[^98]In a few situations where it was not possible to test the entire internationally desired population (all students in the upper of the two adjacent grades with the greatest proportion of 13 -year-olds), countries were permitted to define a national desired population that excluded part of the internationally desired population. Exhibit A. 5 shows any differences in coverage between the international and national desired populations. Almost all participants achieved 100 percent coverage ( 36 out of 38), with Lithuania and Latvia the exceptions. Consequently, the results for Lithuania are annotated in exhibits in this report, and because coverage fell below 65 percent for Latvia, the Latvian results have been labeled "Latvia (Lss)," for Latvian-Speaking Schools. Although achieving 100 percent coverage of their populations in 1999, both Italy and Israel had less than complete coverage in 1995 - Italy because four of its provinces did not take part, and Israel because it did not test the Arabic-speaking population. Comparisons between 1995 and 1999 for these countries are based on the subsets of the 1999 populations that were comparable to the populations tested in 1995 .

Within the desired population, countries could define a population that excluded a small percentage (less than 10 percent) of certain kinds of schools or students that would be very difficult or resourceintensive to test (e.g., schools for students with special needs or schools that were very small or located in extremely rural areas). Exhibit A. 5 also shows that the degree of such exclusions was small. Only Israel exceeded the 10 percent limit, and this is annotated in the exhibits in this report.

Within countries, timss used a two-stage sample design, in which the first stage involved selecting about 150 public and private schools in each country. Within each school, countries were to use random procedures to select one mathematics class at the eighth grade. All of the students in that class were to participate in the timss testing. This approach was designed to yield a representative sample of about 3,750 students per country. Typically, between $45^{\circ}$ and $3,75^{\circ}$ students responded to each achievement item in each country, depending on the booklets in which the items appeared.

Exhibits A. 6 and A. 7 present achieved sample sizes for schools and students, respectively, for participating countries. Exhibit A. 8 shows the participation rates for schools, students, and overall, both with and without the use of replacement schools. All countries achieved the minimum acceptable participation rates -85 percent of both the schools
and students, or a combined rate (the product of school and student participation) of 75 percent - although Belgium (Flemish), England, Hong Kong, and the Netherlands did so only after including replacement schools.

Because of scheduling difficulties, Lithuania was unable to test its eighthgrade students in May 1999 as planned. Instead, the students were tested in September 1999, when they had moved into the ninth grade. The results for Lithuania are annotated accordingly in exhibits in this report.

Whereas all countries achieved a high degree of compliance with sampling guidelines in 1999, three of them (Israel, South Africa, and Thailand) had experienced difficulties with sampling at the classroom level in 1995. Accordingly, results for these three countries are reported in a separate panel of the exhibits in these reports that deal with trends from 1995.

|  | International Desired Population |  | National Desired Population |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coverage | Notes on Coverage | School-Level Exclusions | Within-Sample Exclusions | Overall Exclusions |
| Australia | 100\% |  | 1\% | 1\% | 2\% |
| Belgium (Flemish) | 100\% |  | 1\% | 0\% | 1\% |
| Bulgaria | 100\% |  | 5\% | 0\% | 5\% |
| Canada | 100\% |  | 4\% | 2\% | 6\% |
| Chile | 100\% |  | 3\% | 0\% | 3\% |
| Chinese Taipei | 100\% |  | 1\% | 1\% | 2\% |
| Cyprus | 100\% |  | 0\% | 1\% | 1\% |
| Czech Republic | 100\% |  | 5\% | 0\% | 5\% |
| England | 100\% |  | 2\% | 3\% | 5\% |
| Finland | 100\% |  | 3\% | 0\% | 4\% |
| Hong Kong, SAR | 100\% |  | 1\% | 0\% | 1\% |
| Hungary | 100\% |  | 4\% | 0\% | 4\% |
| Indonesia | 100\% |  | 0\% | 0\% | 0\% |
| Iran, Islamic Rep. of | 100\% |  | 4\% | 0\% | 4\% |
| Israel | 100\% |  | 8\% | 8\% | 16\% |
| Italy | 100\% |  | 4\% | 2\% | 7\% |
| Japan | 100\% |  | 1\% | 0\% | 1\% |
| Jordan | 100\% |  | 2\% | 1\% | 3\% |
| Korea, Rep. of | 100\% |  | 2\% | 2\% | 4\% |
| Latvia (LSS) | 61\% | Latvian-speaking students only | 4\% | 0\% | 4\% |
| Lithuania | 87\% | Lithuanian-speaking students only | 5\% | 0\% | 5\% |
| Macedonia, Rep. of | 100\% |  | 1\% | 0\% | 1\% |
| Malaysia | 100\% |  | 5\% | 0\% | 5\% |
| Moldova | 100\% |  | 2\% | 0\% | 2\% |
| Morocco | 100\% |  | 1\% | 0\% | 1\% |
| Netherlands | 100\% |  | 1\% | 0\% | 1\% |
| New Zealand | 100\% |  | 2\% | 1\% | 2\% |
| Philippines | 100\% |  | 3\% | 0\% | 3\% |
| Romania | 100\% |  | 4\% | 0\% | 4\% |
| Russian Federation | 100\% |  | 1\% | 1\% | 2\% |
| Singapore | 100\% |  | 0\% | 0\% | 0\% |
| Slovak Republic | 100\% |  | 7\% | 0\% | 7\% |
| Slovenia | 100\% |  | 3\% | 0\% | 3\% |
| South Africa | 100\% |  | 2\% | 0\% | 2\% |
| Thailand | 100\% |  | 3\% | 0\% | 3\% |
| Tunisia | 100\% |  | 0\% | 0\% | 0\% |
| Turkey | 100\% |  | 2\% | 0\% | 2\% |
| United States | 100\% |  | 0\% | 4\% | 4\% |


|  | Number of Schools in Original Sample | Number of Eligible Schools in Original Sample | Number of Schools in Original Sample That Participated | Number of Replacement Schools That Participated | Total Number of Schools That Participated |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Australia | 184 | 182 | 152 | 18 | 170 |
| Belgium (Flemish) | 150 | 150 | 106 | 29 | 135 |
| Bulgaria | 172 | 169 | 163 | 0 | 163 |
| Canada | 410 | 398 | 376 | 9 | 385 |
| Chile | 186 | 185 | 181 | 4 | 185 |
| Chinese Taipei | 150 | 150 | 150 | 0 | 150 |
| Cyprus | 61 | 61 | 61 | 0 | 61 |
| Czech Republic | 150 | 142 | 136 | 6 | 142 |
| England | 150 | 150 | 76 | 52 | 128 |
| Finland | 160 | 160 | 155 | 4 | 159 |
| Hong Kong, SAR | 180 | 180 | 135 | 2 | 137 |
| Hungary | 150 | 150 | 147 | 0 | 147 |
| Indonesia | 150 | 150 | 132 | 18 | 150 |
| Iran, Islamic Rep. of | 170 | 170 | 164 | 6 | 170 |
| Israel | 150 | 139 | 137 | 2 | 139 |
| Italy | 180 | 180 | 170 | 10 | 180 |
| Japan | 150 | 150 | 140 | 0 | 140 |
| Jordan | 150 | 147 | 146 | 1 | 147 |
| Korea, Rep. of | 150 | 150 | 150 | 0 | 150 |
| Latvia (LSS) | 150 | 148 | 143 | 2 | 145 |
| Lithuania | 150 | 150 | 150 | 0 | 150 |
| Macedonia, Rep. of | 150 | 150 | 149 | 0 | 149 |
| Malaysia | 150 | 150 | 148 | 2 | 150 |
| Moldova | 150 | 150 | 145 | 5 | 150 |
| Morocco | 174 | 174 | 172 | 1 | 173 |
| Netherlands | 150 | 148 | 86 | 40 | 126 |
| New Zealand | 156 | 156 | 145 | 7 | 152 |
| Philippines | 150 | 150 | 148 | 2 | 150 |
| Romania | 150 | 150 | 147 | 0 | 147 |
| Russian Federation | 190 | 190 | 186 | 3 | 189 |
| Singapore | 145 | 145 | 145 | 0 | 145 |
| Slovak Republic | 150 | 150 | 143 | 2 | 145 |
| Slovenia | 150 | 150 | 147 | 2 | 149 |
| South Africa | 225 | 219 | 183 | 11 | 194 |
| Thailand | 150 | 150 | 143 | 7 | 150 |
| Tunisia | 150 | 149 | 126 | 23 | 149 |
| Turkey | 204 | 204 | 202 | 2 | 204 |
| United States | 250 | 246 | 202 | 19 | 221 |


|  | Within- <br> School Student Participation (Weighted Percentage) | Number of Sampled Students in Participating Schools | Number of Students Withdrawn from Class/School | Number of Students Excluded | Number of Eligible Students | Number of Students Absent | Number of Students Assessed |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Australia | 90\% | 4600 | 96 | 53 | 4451 | 419 | 4032 |
| Belgium (Flemish) | 97\% | 5387 | 12 | 0 | 5375 | 116 | 5259 |
| Bulgaria | 96\% | 3461 | 63 | 0 | 3398 | 126 | 3272 |
| Canada | 96\% | 9490 | 84 | 245 | 9161 | 391 | 8770 |
| Chile | 96\% | 6283 | 119 | 18 | 6146 | 239 | 5907 |
| Chinese Taipei | 99\% | 5889 | 30 | 42 | 5817 | 45 | 5772 |
| Cyprus | 97\% | 3296 | 38 | 32 | 3226 | 110 | 3116 |
| Czech Republic | 96\% | 3640 | 24 | 0 | 3616 | 163 | 3453 |
| England | 90\% | 3400 | 27 | 115 | 3258 | 298 | 2960 |
| Finland | 96\% | 3060 | 17 | 13 | 3030 | 110 | 2920 |
| Hong Kong, SAR | 98\% | 5310 | 18 | 1 | 5291 | 112 | 5179 |
| Hungary | 95\% | 3350 | 0 | 0 | 3350 | 167 | 3183 |
| Indonesia | 97\% | 6162 | 106 | 1 | 6055 | 207 | 5848 |
| Iran, Islamic Rep. of | 98\% | 5497 | 104 | 0 | 5393 | 92 | 5301 |
| Israel | 94\% | 4670 | 29 | 187 | 4454 | 259 | 4195 |
| Italy | 97\% | 3531 | 23 | 86 | 3422 | 94 | 3328 |
| Japan | 95\% | 4996 | 15 | 12 | 4969 | 224 | 4745 |
| Jordan | 99\% | 5300 | 130 | 42 | 5128 | 76 | 5052 |
| Korea, Rep. of | 100\% | 6285 | 29 | 128 | 6128 | 14 | 6114 |
| Latvia (LSS) | 93\% | 3128 | 16 | 4 | 3108 | 235 | 2873 |
| Lithuania | 89\% | 2668 | 0 | 0 | 2668 | 307 | 2361 |
| Macedonia, Rep. of | 98\% | 4096 | 0 | 0 | 4096 | 73 | 4023 |
| Malaysia | 99\% | 5713 | 98 | 0 | 5615 | 38 | 5577 |
| Moldova | 98\% | 3824 | 23 | 0 | 3801 | 90 | 3711 |
| Morocco | 92\% | 5841 | 42 | 0 | 5799 | 397 | 5402 |
| Netherlands | 95\% | 3099 | 12 | 0 | 3087 | 125 | 2962 |
| New Zealand | 94\% | 3966 | 96 | 22 | 3848 | 235 | 3613 |
| Philippines | 92\% | 7591 | 461 | 0 | 7130 | 529 | 6601 |
| Romania | 98\% | 3514 | 36 | 0 | 3478 | 53 | 3425 |
| Russian Federation | 97\% | 4557 | 48 | 34 | 4475 | 143 | 4332 |
| Singapore | 98\% | 5100 | 37 | 0 | 5063 | 97 | 4966 |
| Slovak Republic | 98\% | 3695 | 149 | 0 | 3546 | 49 | 3497 |
| Slovenia | 95\% | 3287 | 0 | 4 | 3283 | 174 | 3109 |
| South Africa | 93\% | 9071 | 256 | 0 | 8815 | 669 | 8146 |
| Thailand | 99\% | 5831 | 59 | 0 | 5772 | 40 | 5732 |
| Tunisia | 98\% | 5189 | 45 | 0 | 5144 | 93 | 5051 |
| Turkey | 99\% | 7972 | 49 | 0 | 7923 | 82 | 7841 |
| United States | 94\% | 9981 | 115 | 142 | 9724 | 652 | 9072 |


|  | School Participation |  | Student Participation | Overall Participation |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Before Replacement | After Replacement |  | Before Replacement | After Replacement |
| Australia | 83\% | 93\% | 90\% | 75\% | 84\% |
| Belgium (Flemish) | 72\% | 89\% | 97\% | 70\% | 87\% |
| Bulgaria | 97\% | 97\% | 96\% | 93\% | 93\% |
| Canada | 92\% | 95\% | 96\% | 88\% | 92\% |
| Chile | 98\% | 100\% | 96\% | 94\% | 96\% |
| Chinese Taipei | 100\% | 100\% | 99\% | 99\% | 99\% |
| Cyprus | 100\% | 100\% | 97\% | 97\% | 97\% |
| Czech Republic | 94\% | 100\% | 96\% | 90\% | 96\% |
| England | 49\% | 85\% | 90\% | 45\% | 77\% |
| Finland | 97\% | 100\% | 96\% | 93\% | 96\% |
| Hong Kong, SAR | 75\% | 76\% | 98\% | 74\% | 75\% |
| Hungary | 98\% | 98\% | 95\% | 93\% | 93\% |
| Indonesia | 84\% | 100\% | 97\% | 81\% | 97\% |
| Iran, Islamic Rep. of | 96\% | 100\% | 98\% | 95\% | 98\% |
| Israel | 98\% | 100\% | 94\% | 93\% | 94\% |
| Italy | 94\% | 100\% | 97\% | 91\% | 97\% |
| Japan | 93\% | 93\% | 95\% | 89\% | 89\% |
| Jordan | 99\% | 100\% | 99\% | 98\% | 99\% |
| Korea, Rep. of | 100\% | 100\% | 100\% | 100\% | 100\% |
| Latvia (LSS) | 96\% | 98\% | 93\% | 89\% | 91\% |
| Lithuania | 100\% | 100\% | 89\% | 89\% | 89\% |
| Macedonia, Rep. of | 99\% | 99\% | 98\% | 98\% | 98\% |
| Malaysia | 99\% | 100\% | 99\% | 98\% | 99\% |
| Moldova | 96\% | 100\% | 98\% | 94\% | 98\% |
| Morocco | 99\% | 99\% | 92\% | 91\% | 92\% |
| Netherlands | 62\% | 85\% | 95\% | 59\% | 81\% |
| New Zealand | 93\% | 97\% | 94\% | 87\% | 91\% |
| Philippines | 98\% | 100\% | 92\% | 91\% | 92\% |
| Romania | 98\% | 98\% | 98\% | 97\% | 97\% |
| Russian Federation | 98\% | 100\% | 97\% | 95\% | 97\% |
| Singapore | 100\% | 100\% | 98\% | 98\% | 98\% |
| Slovak Republic | 95\% | 96\% | 98\% | 93\% | 94\% |
| Slovenia | 98\% | 99\% | 95\% | 93\% | 94\% |
| South Africa | 85\% | 91\% | 93\% | 79\% | 84\% |
| Thailand | 93\% | 100\% | 99\% | 93\% | 99\% |
| Tunisia | 84\% | 100\% | 98\% | 82\% | 98\% |
| Turkey | 99\% | 100\% | 99\% | 98\% | 99\% |
| United States | 83\% | 90\% | 94\% | 78\% | 85\% |

## Data Collection

Each participating country was responsible for carrying out all aspects of the data collection, using standardized procedures developed for the study. Training manuals were created for school coordinators and test administrators that explained procedures for receipt and distribution of materials as well as for the activities related to the testing sessions. These manuals covered procedures for test security, standardized scripts to regulate directions and timing, rules for answering students' questions, and steps to ensure that identification on the test booklets and questionnaires corresponded to the information on the forms used to track students.

Each country was responsible for conducting quality control procedures and describing this effort in the NRC's report documenting procedures used in the study. In addition, the International Study Center considered it essential to monitor compliance with standardized procedures. nRCs were asked to nominate one or more persons unconnected with their national center, such as retired school teachers, to serve as quality control monitors for their countries. The International Study Center developed manuals for the monitors and briefed them in twoday training sessions about timss, the responsibilities of the national centers in conducting the study, and their own roles and responsibilities. In all, 71 quality control monitors participated in this training.

The quality control monitors interviewed the nRCs about data collection plans and procedures. They also visited a sample of 15 schools where they observed testing sessions and interviewed school coordinators. ${ }^{8}$ Quality control monitors interviewed school coordinators in all 38 countries, and observed a total of $55^{\circ}$ testing sessions.

The results of the interviews indicate that, in general, nRCs had prepared well for data collection and, despite the heavy demands of the schedule and shortages of resources, were able to conduct the data collection efficiently and professionally. Similarly, the timss tests appeared to have been administered in compliance with international procedures, including the activities before the testing session, those during testing, and the school-level activities related to receiving, distributing, and returning material from the national centers.

[^99]
## Scoring the Free-Response Items

Because about one-third of the written test time was devoted to freeresponse items, timss needed to develop procedures for reliably evaluating student responses within and across countries. Scoring used two-digit codes with rubrics specific to each item. The first digit designates the correctness level of the response. The second digit, combined with the first, represents a diagnostic code identifying specific types of approaches, strategies, or common errors and misconceptions. Although not used in this report, analyses of responses based on the second digit should provide insight into ways to help students better understand mathematics concepts and problem-solving approaches. Because of the burden of maintaining scoring consistency across time, no free-response items were used to measure trends from 1995 to 1999 . However, samples of student responses from each country to selected items in 1999 have been scanned using advanced imaging technology in preparation for studying trends to 2003 and beyond.

To ensure reliable scoring procedures based on the timss rubrics, the International Study Center prepared detailed guides containing the rubrics and explanations of how to implement them, together with example student responses for the various rubric categories. These guides, along with training packets containing extensive examples of student responses for practice in applying the rubrics, were used as a basis for intensive training in scoring the free-response items. The training sessions were designed to help representatives of national centers who would then be responsible for training personnel in their countries to apply the twodigit codes reliably.

To gather and document empirical information about the within-country agreement among scorers, TIMss arranged to have systematic subsamples of at least 1 oo students' responses to each item coded independently by two readers. Exhibit A. 9 shows the average and range of the within-country exact percent of agreement between scorers on the free-response items in the mathematics test for 37 of the 38 countries. A high percentage of exact agreement was observed, with an overall average of 99 percent across the 37 countries. The timss data from the reliability studies indicate that scoring procedures were robust for the mathematics items, especially for the correctness score used for the analyses in this report.


## Exhibit A. 9 TIMSS 1999 Within-Country Free-Response Scoring Reliability Data for Mathematics Items

|  | Correctness Score Agreement |  |  | Diagnostic Score Agreement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average of Exact Percent Agreement | Range of Exact Percent Agreement |  | Average of Exact Percent Agreement | Range of Exact Percent Agreement |  |
|  |  |  |  |  | Min | Max |
| Australia | 98 | 94 | 100 | 95 | 80 | 100 |
| Belgium (Flemish) | 99 | 92 | 100 | 98 | 91 | 100 |
| Bulgaria | 99 | 94 | 100 | 96 | 73 | 100 |
| Canada | 98 | 88 | 100 | 94 | 80 | 99 |
| Chile | 99 | 94 | 100 | 97 | 88 | 100 |
| Chinese Taipei | 100 | 98 | 100 | 99 | 93 | 100 |
| Cyprus | - | - | - | - | - | - |
| Czech Republic | 97 | 81 | 100 | 92 | 63 | 99 |
| England | 99 | 96 | 100 | 97 | 87 | 100 |
| Finland | 99 | 97 | 100 | 97 | 90 | 100 |
| Hong Kong, SAR | 98 | 84 | 100 | 95 | 80 | 100 |
| Hungary | 98 | 87 | 100 | 96 | 76 | 100 |
| Indonesia | 99 | 92 | 100 | 94 | 79 | 100 |
| Iran, Islamic Rep. | 99 | 93 | 100 | 94 | 74 | 100 |
| Israel | 98 | 92 | 100 | 95 | 81 | 100 |
| Italy | 99 | 95 | 100 | 97 | 89 | 100 |
| Japan | 99 | 90 | 100 | 96 | 88 | 100 |
| Jordan | 99 | 96 | 100 | 96 | 89 | 100 |
| Korea, Rep. of | 98 | 88 | 100 | 96 | 73 | 100 |
| Latvia (LSS) | 99 | 96 | 100 | 96 | 79 | 100 |
| Lithuania | 99 | 90 | 100 | 98 | 88 | 100 |
| Macedonia, Rep. of | 99 | 97 | 100 | 98 | 95 | 100 |
| Malaysia | 100 | 98 | 100 | 99 | 97 | 100 |
| Moldova | 97 | 92 | 100 | 94 | 86 | 99 |
| Morocco | 97 | 84 | 100 | 88 | 65 | 99 |
| Netherlands | 99 | 85 | 100 | 94 | 79 | 100 |
| New Zealand | 99 | 95 | 100 | 95 | 88 | 100 |
| Philippines | 99 | 97 | 100 | 95 | 84 | 100 |
| Romania | 99 | 96 | 100 | 97 | 92 | 100 |
| Russian Federation | 100 | 98 | 100 | 98 | 92 | 100 |
| Singapore | 99 | 94 | 100 | 97 | 87 | 100 |
| Slovak Republic | 99 | 97 | 100 | 99 | 96 | 100 |
| Slovenia | 100 | 99 | 100 | 96 | 83 | 100 |
| South Africa | 99 | 93 | 100 | 96 | 85 | 99 |
| Thailand | 100 | 100 | 100 | 100 | 100 | 100 |
| Tunisia | 98 | 92 | 100 | 96 | 88 | 100 |
| Turkey | 100 | 97 | 100 | 99 | 97 | 100 |
| United States | 99 | 96 | 100 | 97 | 89 | 100 |
| International Avg. | 99 | 93 | 100 | 96 | 85 | 100 |

## Test Reliability

"「
Exhibit A. 10 displays the mathematics test reliability coefficient for each country. This coefficient is the median KR-2o reliability across the eight test booklets. Median reliabilities ranged from 0.76 in the Philippines to 0.94 in Chinese Taipei. The international median, o.89, is the median of the reliability coefficients for all countries.

## Data Processing

To ensure the availability of comparable, high-quality data for analysis, timss took rigorous quality control steps to create the international database. ${ }^{9}$ Timss prepared manuals and software for countries to use in entering their data, so that the information would be in a standardized international format before being forwarded to the iea Data Processing Center in Hamburg for creation of the international database. Upon arrival at the Data Processing Center, the data underwent an exhaustive cleaning process. This involved several iterative steps and procedures designed to identify, document, and correct deviations from the international instruments, file structures, and coding schemes. The process also emphasized consistency of information within national data sets and appropriate linking among the many student, teacher, and school data files.

Throughout the process, the data were checked and double-checked by the iea Data Processing Center, the International Study Center, and the national centers. The national centers were contacted regularly and given multiple opportunities to review the data for their countries. In conjunction with the iea Data Processing Center, the International Study Center reviewed item statistics for each cognitive item in each country to identify poorly performing items. On the mathematics test, one item was deleted for all countries. In addition, 14 countries had one or more items deleted (in most cases, one). Usually the poor statistics (negative point-biserials for the key, large item-by-country interactions, and statistics indicating lack of fit with the model) were a result of translation, adaptation, or printing deviations.

[^100]|  | Reliability Coefficient ${ }^{1}$ |
| :---: | :---: |
| Australia | 0.90 |
| Belgium (Flemish) | 0.89 |
| Bulgaria | 0.90 |
| Canada | 0.88 |
| Chile | 0.83 |
| Chinese Taipei | 0.94 |
| Cyprus | 0.87 |
| Czech Republic | 0.90 |
| England | 0.90 |
| Finland | 0.86 |
| Hong Kong, SAR | 0.89 |
| Hungary | 0.91 |
| Indonesia | 0.87 |
| Iran, Islamic Rep. | 0.83 |
| Israel | 0.90 |
| Italy | 0.89 |
| Japan | 0.91 |
| Jordan | 0.89 |
| Korea, Rep. of | 0.91 |
| Latvia (LSS) | 0.89 |
| Lithuania | 0.89 |
| Macedonia, Rep. of | 0.88 |
| Malaysia | 0.90 |
| Moldova | 0.88 |
| Morocco | 0.69 |
| Netherlands | 0.89 |
| New Zealand | 0.91 |
| Philippines | 0.76 |
| Romania | 0.90 |
| Russian Federation | 0.91 |
| Singapore | 0.90 |
| Slovak Republic | 0.89 |
| Slovenia | 0.90 |
| South Africa | 0.77 |
| Thailand | 0.87 |
| Tunisia | 0.79 |
| Turkey | 0.86 |
| United States | 0.90 |
| International Median | 0.89 |

[^101]
## IRT Scaling and Data Analysis

The general approach to reporting the timss achievement data was based primarily on item response theory (IRT) scaling methods. ${ }^{10}$ The mathematics results were summarized using a family of 2 -parameter and 3 parameter IRT models for dichotomously-scored items (right or wrong), and generalized partial credit models for items with 0,1 , or 2 available score points. The irt scaling method produces a score by averaging the responses of each student to the items that he or she took in a way that takes into account the difficulty and discriminating power of each item. The methodology used in timss includes refinements that enable reliable scores to be produced even though individual students responded to relatively small subsets of the total mathematics item pool. Achievement scales were produced for each of the five mathematics content areas (fractions and number sense, measurement, data representation, analysis, and probability, geometry, and algebra), as well as for mathematics overall.

The IRT methodology was preferred for developing comparable estimates of performance for all students, since students answered different test items depending upon which of the eight test booklets they received. The IRT analysis provides a common scale on which performance can be compared across countries. In addition to providing a basis for estimating mean achievement, scale scores permit estimates of how students within countries vary and provide information on percentiles of performance. To provide a reliable measure of student achievement in both 1999 and 1995, the overall mathematics scale was calibrated using students from the countries that participated in both years. When all countries participating in 1995 at the eighth grade are treated equally, the timss scale average over those countries is 500 and the standard deviation is 100 . Since the countries varied in size, each country was weighted to contribute equally to the mean and standard deviation of the scale. The average and standard deviation of the scale scores are arbitrary and do not affect scale interpretation. When the metric of the scale had been established, students from the countries that tested in 1999 but not 1995 were assigned scores on the basis of the new scale.

IRT scales were also created for each of the five mathematics content areas for the 1999 data. However, insufficient items were used both in 1995 and in 1999 to establish reliable IRT content area scales for trend purposes. The trend exhibits presented in Chapter 3 were based on the average percentage of students responding correctly to the common items in each content area.

[^102]To allow more accurate estimation of summary statistics for student subpopulations, the timss scaling made use of plausible-value technology, whereby five separate estimates of each student's score were generated on each scale, based on the student's responses to the items in the student's booklet and the student's background characteristics. The five score estimates are known as "plausible values," and the variability between them encapsulates the uncertainty inherent in the score estimation process.

## Estimating Sampling Error

Because the statistics presented in this report are estimates of national performance based on samples of students, rather than the values that could be calculated if every student in every country had answered every question, it is important to have measures of the degree of uncertainty of the estimates. The jackknife procedure was used to estimate the standard error associated with each statistic presented in this report. ${ }^{11}$ The jackknife standard errors also include an error component due to variation between the five plausible values generated for each student. The use of confidence intervals, based on the standard errors, provides a way to make inferences about the population means and proportions in a manner that reflects the uncertainty associated with the sample estimates. An estimated sample statistic plus or minus two standard errors represents a 95 percent confidence interval for the corresponding population result.

## Making Multiple Comparisons

This report makes extensive use of statistical hypothesis-testing to provide a basis for evaluating the significance of differences in percentages and in average achievement scores. Each separate test follows the usual convention of holding to 0.05 the probability that reported differences could be due to sampling variability alone. However, in exhibits where statistical significance tests are reported, the results of many tests are reported simultaneously, usually at least one for each country in the exhibit. The significance tests in these exhibits are based on a Bonferroni procedure for multiple comparisons that hold to 0.05 the probability of erroneously declaring a statistic (mean or percentage)

[^103]for one country to be different from that for another country. In the multiple comparison charts (Exhibit 1.2 and those in Appendix B), the Bonferroni procedure adjusts for the number of countries in the chart, minus one. In exhibits where a country statistic is compared to the international average, the adjustment is for the number of countries. ${ }^{12}$

## Setting International Benchmarks of Student Achievement

International benchmarks of student achievement were computed at each grade level for both mathematics and science. The benchmarks are points in the weighted international distribution of achievement scores that separate the 10 percent of students located on top of the distribution, the top 25 percent of students, the top 50 percent, and the bottom 25 percent. The percentage of students in each country meeting or exceeding the international benchmarks is reported. The benchmarks correspond to the goth, $75^{\text {th }}$, 5 oth, and $25^{\text {th }}$ percentiles of the international distribution of achievement. When computing these percentiles, each country contributed as many students to the distribution as there were students in the target population in the country. That is, each country's contribution to setting the international benchmarks was proportional to the estimated population enrolled at the eighth grade.

In order to interpret the timss scale scores and analyze achievement at the international benchmarks, timss conducted a scale anchoring analysis to describe achievement of students at those four points on the scale. Scale anchoring is a way of describing students' performance at different points on a scale in terms of what they know and can do. It involves a statistical component, in which items that discriminate between successive points on the scale are identified, and a judgmental component in which subject-matter experts examine the items and generalize to students' knowledge and understandings. ${ }^{13}$

[^104]
## Mathematics Curriculum Questionnaire

In an effort to collect information about the content of the intended curriculum in mathematics, timss asked National Research
Coordinators to complete a questionnaire about the structure, organization, and content coverage of their national curricula. NRCS reviewed $5^{6}$ mathematics topics and reported the percentage of their eighthgrade students for which each topic was intended in their curriculum. Although most topic descriptions were used without modification, there were occasions when NRCs found it necessary to expand on or qualify the topic description to describe their situation accurately.
These country-specific adaptations to the mathematics curriculum questionnaire are presented in Exhibit A. 11.

|  | Topic |
| :---: | :---: |
| Bulgaria | Geometry: Congruence and similarity |
| Czech Republic | Measurement: Volume of other solids (e.g., pyramids, cylinders, cones, spheres) |
|  | Geometry: Congruence and similarity |
| Finland | Fractions and Number Sense: Concepts of ratio and proportion; ratio and proportion problems |
|  | Geometry: Symmetry and transformations (reflection and rotation) |
|  | Algebra: Representing situations algebraically; formulas |
| Israel | Fractions and Number Sense: Whole numbers - including place values, factorization and operations ( $+,-, x, \div$ ) |
|  | Fractions and Number Sense: Computations with common fractions |
|  | Fractions and Number Sense: Computations with decimal fractions |
|  | Measurement: Estimates of measurement; accuracy of measurement |
|  | Geometry: Simple two dimensional geometry - angles on a straight line, parallel lines, triangles and quadrilaterals |
|  | Geometry: Congruence and similarity |
| Japan | Fractions and Number Sense: Prime factors, highest common factor, lowest common multiple, rules for divisibility |
| Korea, Rep. of | Fractions and Number Sense: Number lines |
|  | Geometry: Cartesian coordinates of points in a plane |
| Morocco | Geometry: Symmetry and transformations (reflection and rotation) |
| Netherlands | Geometry: Congruence and similarity |
| New Zealand | Fractions and Number Sense: Computations with common fractions |
|  | Fractions and Number Sense: Square roots (of perfect squares less than 144), small integer exponents |
|  | Algebra: Representing situations algebraically; formulas |
|  | Algebra: Using the graph of a relationship to interpolate/extrapolate |
| Russian Federation | Measurement: Perimeter and area of simple shapes triangles, rectangles, and circles |
|  | Geometry: Congruence and similarity |
| South Africa | Measurement: Volume of other solids (e.g., pyramids, cylinders, cones, spheres) |
| Tunisia | Geometry: Symmetry and transformations (reflection and rotation) |


| Response | Comments |
| :---: | :---: |
| All or almost all of the students (at least 90\%) | Similarity not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Volume of pyramids, cones, \& spheres not included in curriculum through grade 8 . |
| All or almost all of the students (at least 90\%) | Similarity not included in curriculum through grade 8. |
| Not included in curriculum through grade 8 | Concepts of ratio and proportion included in curriculum through grade 8 . |
| Not included in curriculum through grade 8 | Symmetry included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Formulas not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Factorization not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Division with common fractions not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Division with decimal fractions is not included in curriculum through grade 8. |
| Only the most advanced students ( $10 \%$ or less) | Accuracy of measurement is not included in curriculum through grade 8. |
| About half of the students | Quadrilaterals not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Similarity not included in curriculum through grade 8. |
| Not included in curriculum through grade 8 | Highest common factor and lowest common multiple included in curriculum through grade 8 . |
| All or almost all of the students (at least 90\%) | Whole number and integer number lines included in curriculum through grade 8. The real number line is taught in grade 9. |
| Not included in curriculum through grade 8 | Linear function and its graph is included in curriculum through grade 8 . |
| All or almost all of the students (at least 90\%) | Transformations (reflection \& rotation) not included in curriculum through grade 8. |
| Not included in curriculum through grade 8 | Symmetry taught to all or almost all of the students. |
| All or almost all of the students (at least 90\%) | Division with common fractions is not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Small integer exponents taught to about half of the students. |
| About half of the students | Formulas not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Using the graph of a relationship to extrapolate not included in curriculum through grade 8. |
| About half of the students | Perimeter and area of rectangles and circles included in curriculum through grade 8. |
| About half of the students | Congruence included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Volume of pyramids, cones, \& spheres not included in curriculum through grade 8. |
| All or almost all of the students (at least 90\%) | Rotation not included in curriculum through grade 8. |

## APPENDIX B

Multiple Comparisons of Average Achievement in Mathematics
Content Areas

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries


Average achievement significantly higher than comparison country

- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

[^105]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Average achievement significantly higher than comparison country

- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

Significance tests adjusted for multiple comparisons

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Average achievement significantly higher than comparison country

- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

Significance tests adjusted for multiple comparisons

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Average achievement significantly higher than comparison country

- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

[^106]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Average achievement significantly higher than comparison country

- No statistically significant difference from comparison country

Average achievement significantly lower than comparison country

[^107]
## APPENDIX C

The Test-Curriculum Matching Analysis:
Mathematics


When comparing student achievement across countries, it is important that the comparisons be as fair as possible. lss has worked toward this goal in a number of ways, including providing detailed procedures for standardizing the population definitions, sampling, test translations, test administration, scoring, and database formation. Similar to the procedures used for developing the original timss instruments, developing the Timss 1999 tests involved a series of reviews by representatives of the participating countries, experts in mathematics, and testing specialists. ${ }^{1}$ The National Research Coordinators (NRCs) from each country formally approved the timss 1999 tests, thus accepting them as being sufficiently fair to compare their students' mathematics achievement with that of students from other countries.

Although the tests were developed to represent a set of agreed-upon mathematics content, differences among the curricula of participating countries result in various topics being taught at different grades. To restrict test items to topics included in the curricula of all participating countries and covered in the same sequence would severely limit test coverage and restrict the research questions that the study is designed to address. The tests, therefore, inevitably have some items measuring topics unfamiliar to some students in some countries.

The Test-Curriculum Matching Analysis (тсма) was conducted to investigate the appropriateness of the timss 1999 mathematics test for the eighth-grade students in the participating countries. tCma also shows how student performance for individual countries varies when based only on the test questions that are judged to be relevant to their own curricula. ${ }^{2}$

To gather data about the extent to which the timss 1999 tests were relevant to the curricula of the participating countries, each NRC reported whether each item was in that country's intended curriculum at the grade tested. The nRC was asked to choose a person or persons who were very familiar with the curriculum at the grade tested to make this determination. Since an item might be in the curriculum for some but not all students in a country, an item was determined appropriate if it was in the intended curriculum for more than 50 percent of the students. The nrcs had considerable flexibility in selecting items and may have considered items inappropriate for other reasons. All participating countries returned the information for analysis.

Exhibits C. 1 and C. 2 present the tcma results for the timss 1999 tests. Exhibit C. 1 shows the average percent correct for each country on items selected as appropriate and on the test as a whole. Exhibit C. 2 shows the standard errors corresponding to the percentages presented in Exhibit C.ı.

[^108]In Exhibit C. 1, the last row of the exhibit indicates that the countries varied substantially in the number of items (score points) identified as appropriate. ${ }^{3}$ The percentages ranged from 100 percent ( 169 score points) in Chinese Taipei, the Slovak Republic, Latvia (Lss), the United States, Lithuania, Moldova, and Indonesia to $5^{8}$ percent ( 98 score points) in Chile. Thirty-four of the 38 countries indicated that the items representing three-quarters or more of the score points ( 127 out of a possible 169) were appropriate.

Since most countries indicated that some items were not included in their intended curriculum at the grade tested, the data were analyzed to determine whether the inclusion of these items had any effect on the international performance comparisons. ${ }^{4}$

The first column in Exhibit C. 1 shows the average percent correct on all test items for each country. The countries are presented in order of their overall performance based on overall percent correct, from highest to lowest. To interpret this exhibit, reading across a row provides the average percent correct for the students in that country on the items selected by each of the countries listed across the top of the exhibit. For example, Singapore, where the average percent correct was 77 percent on its own set of items, also had 78 percent correct for the items selected by Korea, 77 percent for the items selected by Hong Kong, and so forth. The column for a country listed across the top shows how each of the other countries performed on the subset of items selected as appropriate for its own students. Using the set of items selected by Finland as an example, on average 77 percent of these items were answered correctly by students in Singapore, 73 percent by students in Korea, 72 percent by those in Hong Kong, and so forth. The shaded diagonal element in the exhibit shows how each country performed on the subset of items that it selected based on its own curriculum. Thus, Finnish students averaged 56 percent correct on the set of items identified by Finland for the analysis.

The international averages of each country's selected items are presented across the second to the last row of the exhibit. They show that the selection of items for the participating countries varied somewhat in average difficulty, ranging from 48 to 54 percent. Despite these differences, the overall picture presented by Exhibit C. 1 reveals that different item selections do not make a major difference in how well countries perform relative to one another. The items selected by some countries were more difficult than those selected by others. The relative performance of countries on various item selections did vary somewhat, but generally not in a statistically significant manner. ${ }^{5}$

3 Of the 162 items in the test, some items were assigned more score points than others. In particular, some items had two parts, and some extended-response items were scored on a two-point scale. The total number of score points available for analysis was 169. The TCMA uses score points in order to give the same weight to items given them in test scoring.

4 It should be noted that the performance levels presented in Exhibit C. 1 are based on average percents, which are different from the average scale scores that are presented in Chapter 1.

5 small differences in performance shown in this exhibit are not statistically significant. The standard errors for the estimated average percent correct statistics are in Exhibit C.2. It can be said with 95 percent confidence that the value for the entire population falls between the sample estimate plus or minus two standard errors.

Comparing the diagonal element for a country with the overall average percent correct shows the difference between performance on the subset of items chosen as appropriate and performance on the test as a whole. In general, there were only small increases in each country's performance on its own subset of items. To illustrate, the average percent correct for Singapore was 77 percent. The diagonal element shows that Singaporean students had the same percent correct ( 77 percent) based on the smaller set of items selected as they did overall. All countries had a difference of less than five percentage points between the two performance measures, with the largest difference four percent for the Netherlands ( 65 percent compared with 61 percent).

It is clear that the selection of items does not have a major effect on the general relationship among countries. Countries that had substantially higher or lower relative performance on all items also had higher or lower relative performance on the different sets of items selected for the тсma. For example, Singapore had the highest average percent correct on the test as a whole and on most of the different item selections, with Korea, Hong Kong, and Chinese Taipei among the four highestperforming countries in all cases. Although there are some changes in the ordering of countries based on the items selected for the тсма, most of these differences are within the boundaries of sampling error. As an example, consider the 149 score points selected by Jordan. The Jordanian students did better on these items than on the test as a whole, with $4^{1}$ percent correct on these items, on average, compared with 38 percent correct on all items. However, most other countries also did better on these particular items, with an international average of 54 percent correct on the items selected by Jordan. All 30 countries that performed better than Jordan on the overall test also performed better on the items selected by Jordan.

The tcma results provide evidence that the timss 1999 mathematics test provides a reasonable basis for comparing achievement of the participating countries. This result is not unexpected, since making the test as fair as possible was a major consideration in test development. The fact that the majority of countries indicated that most items were appropriate for their students means that the different average percent correct estimates were based on essentially the same items. Insofar as countries rejected items that would be difficult for their students, these items tended to be difficult for students in other countries as well. The analysis shows that omitting such items tends to improve the results for that country, but also tends to improve the results for all other countries, so that the overall pattern of results is largely unaffected.

## Exhibit C. 1 Average Percent Correct for Test-Curriculum Matching Analysis - Mathematics <br> Based on Subsets of Items Specially Identified by Each Country as Addressing its Curriculum (See Exhibit C. 2 for corresponding standard errors)

Instructions: Read across the row to compare that country's performance based on the test items included by each of the countries across the top.






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Of the 162 items in the mathematics test, some items had two parts and some
extended-response items were scored on a two-point scale, resulting in 169 total score
points.



## APPENDIX D

Percentiles and
Standard Deviations
of Mathematics
Achievement

|  | 5th Percentile | 25th Percentile | 50th Percentile | 75th Percentile | 95th Percentile |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Australia | 387 (6.5) | 472 (5.6) | 529 (6.2) | 581 (4.5) | 648 (7.3) |
| Belgium (Flemish) | 423 (14.1) | 511 (4.0) | 563 (3.6) | 611 (3.2) | 675 (5.5) |
| Bulgaria | 367 (6.3) | 454 (5.8) | 512 (7.0) | 567 (10.8) | 649 (11.9) |
| Canada | 406 (4.6) | 484 (3.8) | 533 (2.6) | 581 (2.1) | 646 (6.0) |
| Chile | 253 (7.5) | 336 (4.3) | 391 (2.9) | 448 (5.7) | 533 (13.1) |
| Chinese Taipei | 396 (6.4) | 524 (6.1) | 595 (4.4) | 656 (3.5) | 739 (5.1) |
| Cyprus | 335 (6.9) | 422 (4.0) | 481 (2.0) | 534 (2.4) | 603 (4.0) |
| Czech Republic | 392 (9.9) | 467 (5.0) | 517 (5.7) | 573 (6.0) | 653 (9.9) |
| England | 360 (6.4) | 442 (4.8) | 496 (5.1) | 551 (3.5) | 632 (6.4) |
| Finland | 408 (4.0) | 479 (3.9) | 523 (2.4) | 565 (3.1) | 623 (4.6) |
| Hong Kong, SAR | 456 (11.0) | 538 (5.8) | 587 (3.7) | 632 (3.8) | 693 (4.1) |
| Hungary | 386 (6.4) | 476 (3.4) | 536 (3.7) | 590 (4.1) | 667 (5.1) |
| Indonesia | 239 (8.4) | 337 (7.8) | 401 (4.8) | 469 (4.3) | 574 (8.8) |
| Iran, Islamic Rep. | 284 (4.7) | 367 (2.9) | 423 (4.0) | 478 (4.9) | 556 (7.9) |
| Israel | 300 (6.9) | 402 (6.6) | 473 (7.2) | 534 (2.6) | 614 (3.7) |
| Italy | 331 (8.8) | 423 (5.3) | 482 (3.3) | 540 (4.8) | 615 (5.8) |
| Japan | 441 (2.8) | 529 (2.4) | 583 (1.8) | 633 (1.9) | 702 (4.1) |
| Jordan | 258 (4.3) | 357 (3.8) | 429 (3.6) | 498 (4.3) | 596 (4.2) |
| Korea, Rep. of | 448 (5.8) | 538 (3.6) | 592 (2.3) | 640 (2.0) | 710 (3.2) |
| Latvia (LSS) | 377 (5.1) | 453 (4.0) | 505 (4.6) | 557 (3.7) | 631 (4.3) |
| Lithuania | 354 (9.1) | 429 (3.9) | 482 (4.2) | 534 (3.4) | 608 (7.5) |
| Macedonia, Rep. of | 287 (7.2) | 386 (5.1) | 451 (5.0) | 510 (3.5) | 594 (5.5) |
| Malaysia | 387 (6.0) | 464 (5.0) | 519 (5.3) | 577 (6.8) | 648 (4.3) |
| Moldova | 331 (6.4) | 412 (4.6) | 468 (4.8) | 528 (4.4) | 607 (4.8) |
| Morocco | 181 (7.1) | 277 (3.9) | 340 (2.8) | 401 (2.6) | 477 (4.8) |
| Netherlands | 410 (9.1) | 495 (9.0) | 545 (6.1) | 590 (5.6) | 653 (9.7) |
| New Zealand | 341 (5.5) | 430 (5.9) | 493 (7.0) | 554 (6.5) | 632 (7.4) |
| Philippines | 185 (7.3) | 278 (5.7) | 345 (6.4) | 414 (7.5) | 504 (10.2) |
| Romania | 312 (11.7) | 412 (5.6) | 477 (4.7) | 537 (7.2) | 616 (7.4) |
| Russian Federation | 385 (12.0) | 471 (8.0) | 526 (6.9) | 584 (6.1) | 666 (13.4) |
| Singapore | 464 (7.5) | 555 (5.7) | 608 (6.6) | 658 (8.9) | 728 (6.5) |
| Slovak Republic | 407 (7.4) | 485 (4.2) | 534 (6.0) | 585 (4.8) | 656 (4.9) |
| Slovenia | 392 (4.4) | 476 (3.6) | 531 (3.1) | 587 (4.8) | 663 (5.7) |
| South Africa | 113 (9.6) | 200 (5.5) | 263 (6.6) | 337 (9.9) | 485 (11.1) |
| Thailand | 328 (9.1) | 412 (4.7) | 465 (4.5) | 524 (7.6) | 609 (7.0) |
| Tunisia | 341 (7.1) | 406 (2.5) | 449 (2.9) | 491 (2.9) | 551 (2.9) |
| Turkey | 290 (5.9) | 371 (3.8) | 428 (3.5) | 486 (6.7) | 572 (7.1) |
| United States | 356 (4.3) | 442 (4.7) | 504 (4.3) | 562 (3.7) | 642 (6.6) |


|  | Overall |  | Girls |  | Boys |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Standard Deviation | Mean | Standard <br> Deviation | Mean | Standard <br> Deviation |
| Australia | 525 (4.8) | 80 (2.9) | 524 (5.7) | 77 (3.8) | 526 (5.7) | 83 (3.3) |
| Belgium (Flemish) | 558 (3.3) | 77 (2.8) | 560 (7.2) | 74 (4.8) | 556 (8.3) | 79 (5.6) |
| Bulgaria | 511 (5.8) | 86 (3.8) | 510 (5.9) | 84 (3.5) | 511 (6.9) | 88 (4.7) |
| Canada | 531 (2.5) | 73 (1.7) | 529 (2.5) | 72 (1.9) | 533 (3.2) | 74 (1.7) |
| Chile | 392 (4.4) | 85 (3.5) | 388 (4.3) | 82 (2.9) | 397 (5.8) | 89 (4.2) |
| Chinese Taipei | 585 (4.0) | 104 (1.8) | 583 (3.9) | 98 (2.4) | 587 (5.3) | 110 (2.1) |
| Cyprus | 476 (1.8) | 82 (1.7) | 479 (2.1) | 77 (2.2) | 474 (2.7) | 85 (1.9) |
| Czech Republic | 520 (4.2) | 79 (2.4) | 512 (4.0) | 78 (2.6) | 528 (5.8) | 80 (2.9) |
| England | 496 (4.1) | 83 (2.2) | 487 (5.4) | 79 (3.5) | 505 (5.0) | 86 (2.8) |
| Finland | 520 (2.7) | 65 (1.3) | 519 (3.0) | 63 (1.7) | 522 (3.5) | 68 (1.7) |
| Hong Kong, SAR | 582 (4.3) | 73 (3.0) | 583 (4.7) | 69 (2.8) | 581 (5.9) | 77 (4.4) |
| Hungary | 532 (3.7) | 85 (2.0) | 529 (4.0) | 82 (2.3) | 535 (4.3) | 88 (2.6) |
| Indonesia | 403 (4.9) | 101 (2.9) | 401 (5.4) | 102 (3.4) | 405 (5.0) | 101 (3.1) |
| Iran, Islamic Rep. | 422 (3.4) | 83 (2.3) | 408 (4.2) | 81 (2.5) | 432 (4.8) | 83 (2.5) |
| Israel | 466 (3.9) | 96 (2.6) | 459 (4.2) | 90 (2.4) | 474 (4.8) | 100 (3.8) |
| Italy | 479 (3.8) | 87 (2.3) | 475 (4.5) | 85 (2.8) | 484 (4.3) | 88 (2.8) |
| Japan | 579 (1.7) | 80 (1.1) | 575 (2.4) | 76 (2.1) | 582 (2.3) | 82 (1.3) |
| Jordan | 428 (3.6) | 103 (1.6) | 431 (4.7) | 96 (2.3) | 425 (5.9) | 109 (2.2) |
| Korea, Rep. of | 587 (2.0) | 79 (1.0) | 585 (3.1) | 79 (1.3) | 590 (2.2) | 80 (1.6) |
| Latvia (LSS) | 505 (3.4) | 78 (2.0) | 502 (3.8) | 75 (2.6) | 508 (4.4) | 81 (2.4) |
| Lithuania | 482 (4.3) | 78 (2.6) | 480 (4.7) | 76 (3.2) | 483 (4.8) | 80 (3.2) |
| Macedonia, Rep. of | 447 (4.2) | 93 (2.5) | 446 (5.3) | 92 (3.0) | 447 (4.3) | 94 (2.8) |
| Malaysia | 519 (4.4) | 81 (2.0) | 521 (4.7) | 79 (2.2) | 517 (6.0) | 83 (2.6) |
| Moldova | 469 (3.9) | 85 (2.1) | 468 (4.1) | 83 (2.6) | 471 (4.7) | 87 (2.6) |
| Morocco | 337 (2.6) | 91 (2.0) | 326 (5.3) | 90 (3.5) | 344 (4.1) | 91 (2.0) |
| Netherlands | 540 (7.1) | 73 (4.2) | 538 (7.6) | 73 (4.4) | 542 (7.0) | 74 (4.3) |
| New Zealand | 491 (5.2) | 89 (2.3) | 495 (5.5) | 87 (2.9) | 487 (7.6) | 91 (3.0) |
| Philippines | 345 (6.0) | 97 (2.8) | 352 (6.9) | 96 (4.1) | 337 (6.5) | 98 (2.8) |
| Romania | 472 (5.8) | 93 (3.5) | 475 (6.3) | 90 (3.8) | 470 (6.2) | 96 (3.8) |
| Russian Federation | 526 (5.9) | 86 (3.0) | 526 (6.0) | 83 (3.0) | 526 (6.4) | 90 (3.8) |
| Singapore | 604 (6.3) | 79 (2.9) | 603 (6.1) | 76 (3.0) | 606 (7.5) | 82 (3.3) |
| Slovak Republic | 534 (4.0) | 75 (1.6) | 532 (4.2) | 72 (1.9) | 536 (4.5) | 79 (2.3) |
| Slovenia | 530 (2.8) | 83 (2.0) | 529 (3.0) | 79 (1.9) | 531 (3.6) | 86 (2.8) |
| South Africa | 275 (6.8) | 109 (4.7) | 267 (7.5) | 110 (5.1) | 283 (7.3) | 108 (4.7) |
| Thailand | 467 (5.1) | 85 (2.5) | 469 (5.7) | 84 (2.8) | 465 (5.5) | 86 (2.9) |
| Tunisia | 448 (2.4) | 64 (0.9) | 436 (2.4) | 64 (1.2) | 460 (2.9) | 61 (1.3) |
| Turkey | 429 (4.3) | 86 (2.0) | 428 (4.7) | 83 (2.1) | 429 (4.4) | 87 (2.4) |
| United States | 502 (4.0) | 88 (2.4) | 498 (3.9) | 84 (2.1) | 505 (4.8) | 91 (3.0) |

$\qquad$


## APPENDIX E

Acknowledgments


TIMSS 1999 was truly a collaborative effort among hundreds of individuals around the world. Staff from the national research centers in each participating country, the International Association for the Evaluation for Educational Achievement (iea), the International Study Center (Isc) at Boston College, advisors, and funding agencies worked closely to develop and implement timss 1999. The project would not have been possible without the tireless efforts of all involved. Inside, the individuals and organizations are acknowledged for their contributions. Given that implementing timss 1999 has spanned approximately four years and involved so many people and organizations, this list may not pay heed to all who contributed throughout the life of the project. Any omission is inadvertent. TIMSS 1999 also acknowledges the students, teachers, and school principals who contributed their time and effort to the study. This report would not be possible without them.

## Funding Agencies

Funding for the international coordination of timss 1999 was provided by the National Center for Education Statistics of the U.S. Department of Education, the U.S. National Science Foundation, the World Bank, and participating countries. Valena Plisko, Eugene Owen, and Patrick Gonzales of the National Center for Education Statistics; Larry Suter, Elizabeth VanderPutten, and Janice Earle of the National Science Foundation; and Marlaine Lockheed of the World Bank each played a crucial role in making timss 1999 possible and for ensuring the quality of the study. Each participating country was responsible for funding national project costs and implementing timss 1999 in accordance with the international procedures.

## Management and Operations

timss 1999 was conducted under the auspices of the iea. The study was co-directed by Michael O. Martin and Ina V.S. Mullis, and managed centrally by the staff of the International Study Center at Boston College, Lynch School of Education. Although the study was directed by the International Study Center and its staff members implemented various parts of timss 1999, important activities also were carried out in centers around the world. In the iea Secretariat, Hans Wagemaker, Executive Director, was responsible for overseeing fundraising and country participation. The iea Secretariat also coordinated translation verification and recruiting of quality control monitors. The data were processed centrally by the iea Data Processing Center in Hamburg. Statistics Canada was responsible for collecting and evaluating the sampling documentation from each country and for calculating the sampling weights. Educational Testing Service in Princeton, New Jersey conducted the scaling of the achievement data.

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## National Research Coordinators

The timss 1999 National Research Coordinators and their staff had the enormous task of implementing the timss 1999 design. This required obtaining funding for the project; participating in the development of the instruments and procedures; conducting field tests; participating in and conducting training sessions; translating the instruments and procedural manuals into the local language; selecting the sample of schools and students; working with the schools to arrange for the testing; arranging for data collection, coding, and data entry; preparing the data files for submission to the iea Data Processing Center; contributing to the development of the international reports; and preparing national reports. The way in which the national centers operated
and the resources that were available varied considerably across the timss 1999 countries. In some countries, the tasks were conducted centrally, while in others, various components were subcontracted to other organizations. In some countries, resources were more than adequate, while in some cases, the national centers were operating with limited resources. Of course, across the life of the project, some nrcs have changed. This list attempts to include all past NRCs who served for a significant period of time as well as all the present nrcs. All of the timss 1999 National Research Coordinators and their staff members are to be commended for their professionalism and their dedication in conducting all aspects of timss.

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The International Study Center at Boston College was supported in its work by advisory committees. The Subject Matter Item Replacement Committee was instrumental in developing the timss 1999 tests, and the Questionnaire Item Review Committee revised the timss questionnaires. The Scale Anchoring Panel developed the descriptions of the international benchmarks in mathematics and science.

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[^0]:    1 Because coverage of the target population falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

[^1]:    1 Robitaille, D.F., Beaton, A.E., and Plomp, T., eds. (2000), The Impact of TIMSS on the Teaching and Learning of Mathematics and Science, Vancouver, BC: Pacific Educational Press.

[^2]:    2 Sponsored by the United States, the TIMSS-R Videotape Classroom Study builds on the work of the first TIMSS videotape study of mathematics (Stigler, J.W., Gonzales, P., Kawanaka, T., Knoll S., and Serrano, A. (1999), The TIMSS Videotape Classroom Study: Methods and Findings from an Exploratory Research Project on Eighth-Grade Mathematics Instruction in Germany, Japan, and the United States, NCES 1999-074, Washington, DC: National Center for Education Statistics). The first data from the Videotape Classroom Study are anticipated in late 2001.

[^3]:    3 Hong Kong became a Special Administrative Region of the People's Republic of China in 1999, and is labeled "Hong Kong, SAR" in the exhibits in this report.

    4 Italy was unable to complete the steps necessary to have its data available for reporting in 1996, but all scoring and database tasks were completed subsequently. Indonesia and the Philippines participated in 1995, but were unable to complete the steps necessary for their 1995 data to be reported comparably to those of other countries.

    5 Israel and Thailand also participated at the fourth grade in 1995, but did not satisfy guidelines for sampling procedures at the classroom level and were not included in the comparisons for fourth and eighth grade.
    6 Please see Appendix E for a list of the TIMSS 1999 National Research Coordinators and the TIMSS 1999 advisory committees.

[^4]:    7 The TIMSS 1999 sampling requirements and the outcomes of the sampling procedures are described in Appendix A.

[^5]:    8 The TIMSS 1999 item replacement procedures are described in Appendix A.
    9 Robitaille, D.F., McKnight, C.C., Schmidt, W.H., Britton, E.D., Raisen, S.A., and Nicol, C. (1993), TIMSS Monograph No. 1: Curriculum Frameworks for Mathematics and Science, Vancouver, BC: Pacific Educational Press.

[^6]:    10 See Appendix A for more information about the translation procedures.
    11 Results of the Test-Curriculum Matching Analysis are presented in Appendix C.

[^7]:    12 Appendix A contains an overview of the procedures used. More detailed information is provided in Martin, M.O., Gregory, K.A., and Stemler, S.E., eds., (2000), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

    13 See Chapter 5 for information about the official mathematics curriculum for each country participating in TIMSS 1999.

[^8]:    1 TIMSS used item response theory (IRT) methods to summarize the achievement results on a scale with a mean of 500 and a standard deviation of 100 . Given the matrix-sampling approach, scaling averages students' responses in a way that accounts for differences in the difficulty of different subsets of items. It allows students' performance to be summarized on a common metric even though individual students responded to different items in the mathematics test. For more detailed information, see the "IRT Scaling and Data Analysis" section of Appendix A.
    2 The significance tests in Exhibits 1.1 and 1.2 are based on a Bonferroni procedure for multiple comparisons that holds to 5 percent the probability of erroneously stating the mean of one country to be different from that of another country.
    3 Tables of the percentile values and standard deviations for all countries are presented in Appendix D.
    4 See the "IRT Scaling and Data Analysis" section of Appendix A for more details about calculating standard errors and confidence intervals for the TIMSS statistics.

[^9]:    6 TIMSS used IRT methods to place the eighth-grade results from 1995 and 1999 on the same scale. See Appendix A for more detailed information.

    7 Because coverage of its eighth-grade population falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.
    8 The mathematics achievement scale for fourth grade is not comparable to that for eighth grade, and so results for fourth grade and eighth grade may be compared only in relative terms, for example with reference to the international average for countries that participated in 1995 at both the fourth and eighth grades.

[^10]:    § Average across the subset of TIMSS 1999 countries that participated and met sampling guidelines in () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, 1995 at both the fourth and eighth grades.

[^11]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.
    2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).

[^12]:    1 For example, for the Top $10 \%$ Benchmark, an item was included if at least 65 percent of students scoring at the scale point correspon ding to this benchmark answered the item correctly and less than 50 percent of students scoring at the Upper Quarter Benchmark answered it correctly. Similarly, for the Upper Quarter Benchmark, an item was included if at least 65 percent of students scoring at that point answered the item correctly and less than 50 percent of students at the Median Benchmark answered it correctly.

    2 The participants in the scale anchoring process are listed in Appendix E.

[^13]:    3 Some of the items used to develop the benchmark descriptions are being kept secure to measure achievement trends in future TIMSS assessments and are not available for publication.

[^14]:    * The item was answered fully correctly by a majority of students reaching this benchmark.
    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian-Speaking Schools only.

[^15]:    2 National Defined Population covers less than 90 percent of National Desired Population (see Exhibit A.5).
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^16]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning

    Internationally comparable data are unavailable for Morocco, Thailand, and Tunisia.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number
    of the next school year. some totals may appear inconsistent.

[^17]:    1 Please see Appendix A for more information about the test development process. Appendix C provides an analysis of the match between the test and curriculum in different TIMSS 1999 countries and the effect of this match on the results.

    2 Proportionality was included as a reporting category in TIMSS 1995, but only 11 items were classified in this content area. To improve the stability of trend comparisons with TIMSS 1995 and for TIMSS 1999 reporting, these items were allocated to other content categories for which they were suitable, mainly fractions and number sense.

[^18]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.8).
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.5) Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian-Speaking Schools only.
    2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.5).

[^19]:    3 See Appendix C for information about the extent to which the TIMSS 1999 tests were judged to be relevant to the curriculum of the participating countries.

[^20]:    4 Robitaille D.F. (1989), "Student's Achievements: Population A" in D.F. Robitaille and R.A. Garden (eds.), The IEA Study of Mathematics II: Contexts and Outcomes of School Mathematics, New York: Pergamon Press, p.121; Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A. (1996a), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study (TIMSS), Chestnut Hill, MA: Boston College.

[^21]:    1 Martin, M.O., Mullis, I.V.S., Gregory, K.D., Hoyle, C.D., and Shen, C. (2000), Effective Schools in Science and Mathematics: IEA's Third International Mathematics and Science Study, Chestnut Hill, MA: Boston College.

    2 Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A. (1996), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study, Chestnut Hill, MA: Boston College.

[^22]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number,

[^23]:    Background data provided by students.
    $\mp$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year

[^24]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    A tilde ( $\sim$ ) indicates insufficient data to report achievement.
    $A n$ " $r$ " indicates a $70-84 \%$ student response rate. An "s" indicates a $50-69 \%$ student response rate.

[^25]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent

[^26]:    Background data provided by students.
    1 Average hours based on: No time $=0$; less than 1 hour $=.5 ; 1-2$ hours $=1.5 ; 3-5$ hours $=4$; more than 5 hours=7.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^27]:    4 The response categories for this statement were reversed in constructing the index.
    5 Additional information on students' liking mathematics, one of the components of the index, is provided in Exhibit R1. 15 in the reference section.

[^28]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^29]:    Background data provided by National Research Coordinators.
    1 Canada: Public examinations are administered in 5 of 10 provinces.

[^30]:    Background data provided by National Research Coordinators.
    1 Public examinations are also used for system-wide assessment purposes in these countries: Malaysia, Morocco, Netherlands, Philippines, Singapore, Tunisia and Turkey

[^31]:    1 Martin, M.O., Mullis, I.V.S., Gonzalez, E.J., Gregory, K.D., Smith, T.A., Chrostowski, S.J., Garden, R.A., and O'Connor, K.M. (2000), TIMSS 1999 International Science Report: Findings from IEA's Repeat of the Third International Mathematics and Science Study at the Eighth Grade, Chestnut Hill, MA: Boston College.

[^32]:    Background data provided by National Research Coordinators.
    1 England: While there is one "programme of study" for grades 6-8, the document identifies nine per-formance-levels describing the types and range of performance that pupils working at a particular level should demonstrate

[^33]:    * The use of calculators on TIMSS was not allowed in 1995 or in 1999

[^34]:    Background data provided by teachers.

    * Taught before or during this school year
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^35]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    A dash $(-)$ indicates data are not available.
    An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

[^36]:    2 Livingstone, I.D., (1986), Second International Mathematics Study: Perceptions of the Intended and Implemented Mathematics Curriculum, Washington, D.C., Center for Statistics, U.S. Department of Education.

[^37]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^38]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

[^39]:    Background data provided by teachers.
    1 Teachers having mathematics as the major area of study are those who reported having a bachelor's degree (BA) or equivalent, master's degree (MA), or teacher training certificate in mathematics or mathematics education.
    2 Includes teachers certified to teach any subject.
    3 Italy: Teacher training certificate not required but teachers must excel on a national exam.

[^40]:    1 Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A. (1996), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study, Chestnut Hill MA: Boston College.

[^41]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

[^42]:    2 Stigler, J.W., Gonzales, P., Kawanaka, T., Knoll, S., and Serrano, A., (1999), The TIMSS Videotape Classroom Study: Methods and Findings from an Exploratory Research Project on Eighth-Grade Mathematics Instruction in Germany, Japan, and the United States, NCES 1999-074, Washington DC: National Center for Education Statistics.

[^43]:    Mathematics instructional time provided by teachers, and total instructional time provided by schools.
    1 Computed as the ratio of mathematics instructional time to total instructional time averaged across students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year.

[^44]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available.
    An " $r$ " indicates school and/or teacher response data available for $70-84 \%$ of students. An " $s$ " indicates school and/or teacher response data available for $50-69 \%$ of students. An "x" indicates school and/or teacher response data available for $<50 \%$ of students.

[^45]:    A dash (-) indicates data are not available. A tilde (~) indicates insufficient data to report achievement.
    An " $r$ " indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for 50-69\% of students.

[^46]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^47]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    A dash ( - ) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement.
    An " $r$ " indicates a $70-84 \%$ student response rate.

[^48]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A tilde ( $\sim$ ) indicates insufficient data to report achievement.

[^49]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^50]:    A tilde ( ) indicates insufficient data to report achievement.
    An " $r$ " indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for 50-69\% of students.

[^51]:    Background data provided by teachers.

    * The use of calculators on TIMSS was not allowed in 1995 or in 1999
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^52]:    A dash (-) indicates data are not available. A tilde (~) indicates insufficient data to report achievement.
    An "r" indicates teacher and/or student response data available for $70-84 \%$ of students. An "s" indicates teacher and/or student response data available for 50-69\% of students.

[^53]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^54]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

    A dash (-) indicates data are not available.
    $A n$ " $r$ " indicates a $70-84 \%$ student response rate. An " $s$ " indicates a $50-69 \%$ student response rate.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^55]:    3 Robitaille, D.F., (1997), National Contexts for Mathematics and Science Education: An Encyclopedia of the Education Systems Participating in TIMSS, Vancouver, BC: Pacific Educational Press.

[^56]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent

[^57]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^58]:    A dash (-) indicates data are not available.
    An " r " indicates teacher response data available for $70-84 \%$ of students. An " s " indicates teacher response data available for $50-69 \%$ of students.

[^59]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number,

[^60]:    1 Activities reported by principals are not necessarily exclusive; principals may have reported engaging in more than one activity at the same time.

[^61]:    Background data provided by schools
    1 Serve on committees which select school personnel or review school finances.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year

[^62]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^63]:    Background data provided by schools.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^64]:    A dash (-) indicates data are not available.
    An " r " indicates school response data available for $70-84 \%$ of students. An " $s$ " indicates school response data available for $50-69 \%$ of students.

[^65]:    Background data provided by schools.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^66]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^67]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

[^68]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^69]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    A tilde ( ) indicates insufficient data to report achievement.

[^70]:    - 1999 significantly higher than 1995

    No significant difference between 1995 and 1999
    v 1999 significantly lower than 1995

    Significance tests adjusted for multiple comparisons

[^71]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    An " r " indicates a $70-84 \%$ student response rate

[^72]:    Background data provided by students.
    † Countries with unapproved sampling procedures at the classroom level in 1995.
    § International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

    Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

[^73]:    1 Average scale value based on: Strongly disagree=4; disagree=3; agree=2; strongly agree=1.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^74]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    A dash ( - ) indicates data are not available. A tilde $(\sim)$ indicates insufficient data to report achievement.
    An " $r$ " indicates a $70-84 \%$ student response rate.

[^75]:    Background data provided by schools.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^76]:    SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1998-1999

[^77]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    A dash $(-)$ indicates data are not available.
    An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

[^78]:    Background data provided by teachers.
    1 Does not include students whose teachers report that they do not teach the topic.
    Percentage of students averaged across topics.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^79]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole numbe some totals may appear inconsistent.
    A dash (-) indicates data are not available.
    An " r " indicates teacher response data available for $70-84 \%$ of students.

[^80]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    A tilde ( ) indicates insufficient data to report achievement.
    An " r " indicates school response data available for $70-84 \%$ of students.

[^81]:    An " r " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

[^82]:    Background data provided by schools.
    1 Days reported averaged across students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year

[^83]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

    An "r" indicates teacher response data available for $70-84 \%$ of students. An "s" indicates teacher response data available for $50-69 \%$ of students.

[^84]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^85]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash ( - ) indicates data are not available. A tilde $(\sim)$ indicates insufficient data to report achievement. An " r " indicates a $70-84 \%$ student response rate.

[^86]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    A dash ( - ) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement. An " $r$ " indicates a $70-84 \%$ student response rate.

[^87]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    An " $r$ " indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for $50-69 \%$ of students.

[^88]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^89]:    Background data provided by schools.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^90]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

    An " $r$ " indicates school response data available for 70-84\% of students.

[^91]:    Background data provided by schools
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^92]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    An " $r$ " indicates school response data available for $70-84 \%$ of students. An "s" indicates schoo response data available for $50-69 \%$ of students.

[^93]:    Background data provided by schools.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^94]:    1 Results for 41 countries are reported in the 1995 international reports. Italy also completed the 1995 testing, but too late to be included in the international reports. It is counted as a 1995 country in this report and included in all trend exhibits in the 1999 international reports. Unweighted data for the Philippines were reported in an appendix to the international reports in 1995. These data were not included in trend exhibits in the 1999 international reports.

    2 Two of the 19 countries with fourth-grade data from 1995 (Israel and Thailand) did not satisfy guidelines for sampling procedures at the classroom level and were not included in the comparisons for fourth and eighth grade

[^95]:    3 The complete TIMSS curriculum frameworks can be found in Robitaille, D.F., et al. (1993), TIMSS Monograph No.1: Curriculum Frameworks for Mathematics and Science, Vancouver, BC: Pacific Educational Press.

[^96]:    4 For a full discussion of the TIMSS 1999 test development effort, please see Garden, R.A. and Smith, T.A. (2000), "TIMSS Test Development" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^97]:    5 The 1999 TIMSS test design is identical to the design for 1995, which is fully documented in Adams, R. and Gonzalez, E. (1996), "TIMSS Test Design" in M.O. Martin and D.L. Kelly (eds.), Third International Mathematics and Science Study Technical Report, Volume I, Chestnut Hill, MA: Boston College.

[^98]:    6 More details about the translation verification procedures can be found in O'Connor, K., and Malak, B. (2000), "Translation and Cultural Adaptation of the TIMSS Instruments" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

    7 The sample design for TIMSS is described in detail in Foy, P., and Joncas, M. (2000), "TIMSS Sample Design" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^99]:    8 Steps taken to ensure high-quality data collection in TIMSS are described in detail in O'Connor, K., and Stemler, S. (2000), "Quality Control in the TIMSS Data Collection" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^100]:    9 These steps are detailed in Hastedt, D., and Gonzalez, E. (2000), "Data Management and Database Construction" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^101]:    1 The reliability coefficient for each country is the median KR-20 reliability across the eight test booklets.

[^102]:    10 For a detailed description of the TIMSS scaling, see Yamamoto, K., and Kulick, E. (2000), "Scaling Methods and Procedures for the TIMSS Mathematics and Science Scales" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^103]:    11 Procedures for computing jackknifed standard errors are presented in Gonzalez, E. and Foy, P. (2000), "Estimation of Sampling Variance" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

[^104]:    12 The application of the Bonferroni procedures is described in Gonzalez, E., and Gregory, K. (2000), "Reporting Student Achievement in Mathematics and Science" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College.

    13 The scale-anchoring procedure is described fully in Gregory, K., and Mullis, I. (2000), "Describing International Benchmarks of Student Achievement" in M.O. Martin, K.D. Gregory and S.E. Stemler (eds.), TIMSS 1999 Technical Report, Chestnut Hill, MA: Boston College. An application of the procedure to the 1995 TIMSS data may be found in Kelly, D.L., Mullis, I.V.S., and Martin, M.O. (2000), Profiles of Student Achievement in Mathematics at the TIMSS International Benchmarks: U.S. Performance and Standards in an International Context, Chestnut Hill, MA: Boston College.

[^105]:    Significance tests adjusted for multiple comparisons

[^106]:    Significance tests adjusted for multiple comparisons

[^107]:    Significance tests adjusted for multiple comparisons

[^108]:    1 See Appendix A for more information on test development.
    2 Because there may also be curriculum areas covered in some countries that are not covered by the TIMSS 1999 tests, the TCMA does not provide complete information about how well the tests cover the curricula of the countries.

