

## TIMSS 2003 International Mathematics Report

Findings From IEA's Trends in International Mathematics and Science Study at the Fourth and Eighth Grades
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## Executive Summary

TIMSS 2003 is the third in a continuing cycle of international mathematics and science assessments conducted every four years. TIMSS assesses achievement in countries around the world and collects a rich array of information about the educational contexts for learning mathematics and science, with TIMSS 2003 involving more than 50 participants. This report contains the mathematics results for 46 countries and four benchmarking participants at the eighth grade and for 25 countries and three benchmarking participants at the fourth grade. Trend data are provided at the eighth and fourth grades for those countries that also participated in 1995 and 1999 (please see the Introduction for more information about TIMSS 2003.)

## Students' Mathematics Achievement in 2003

- At both the eighth and fourth grades, Singapore was the top-performing country having significantly higher average achievement in mathematics than the rest of the participating countries.
- At the eighth grade, with the exception of Singapore, the Republic of Korea, Hong Kong SAR, and Chinese Taipei had significantly higher average achievement than all of the other participating countries.
- At the fourth grade, Hong Kong, SAR had significantly higher performance than all countries except Singapore, and, in turn, Japan and Chinese Taipei outperformed the rest of the countries except Singapore and Hong Kong, SAR.


## Trends in Mathematics Achievement

- At the eighth grade, several countries showed significantly higher average achievement in 2003 compared to the previous assessments in 1995 and 1999. Korea, Hong Kong SAR, Latvia (LSS), ${ }^{1}$ Lithuania, and the United States, as well as the benchmarking Canadian province of Ontario, showed a pattern of improvement from assessment to assessment with significant change over the 8 -year period from 1995 to 2003. Of the countries participating only in the 1999 and 2003 assessments, Israel and the Philippines showed significant improvement.
- At the eighth grade, countries showing a decrease in average achievement in 2003 compared to previous assessments (1995, 1999, or both) included Japan, Belgium (Flemish), the Russian Federation, the Slovak Republic, Sweden, Bulgaria, Norway, Cyprus, Macedonia, Iran, and Tunisia as well as the benchmarking Canadian province of Quebec.
- At the fourth grade, many countries showed significant gains in average achievement between 1995 and 2003, including Hong Kong SAR, Latvia (LSS), England, Cyprus, New Zealand, and Slovenia as well as the benchmarking province of Ontario. The only significant declines were found in the Netherlands, Norway, and Quebec province.


## Gender Differences in Mathematics Achievement

- At the eighth grade, the gender difference in TIMSS 2003 was negligible in many countries. However, there were variations across countries with girls outperforming boys in the same number of countries that boys outperformed girls. The girls had significantly higher average achievement than boys in Serbia, Macedonia, Armenia, Moldova, Singapore, the Philippines, Cyprus, Jordan, and Bahrain.

In contrast, boys had higher achievement in the United States, Italy, Hungary, Lebanon, Belgium (Flemish), Morocco, Chile, Ghana, and Tunisia as well as in two benchmarking participants - the US state of Indiana and Quebec province.

- The trend results at the eighth grade show a few more countries with improvement for girls than for boys. Girls had improved performance and boys did not in four countries, whereas there was no country in which boys improved and girls did not. Both girls and boys improved in five countries and Ontario province. Reflecting declines in achievement across assessments, both genders had lower achievement in TIMSS 2003 in seven countries and Quebec province as did the girls in Belgium (Flemish).
- At the fourth grade, the TIMSS 2003 results by gender paralleled those at the eighth grade. Girls had significantly higher average achievement in Singapore, Moldova, the Philippines, and Armenia. Boys had higher average achievement in the Netherlands, the United States, Italy, Cyprus, Scotland, and in the two Canadian provinces.
- The fourth-grade trend results for the genders mirror the overall results, showing more countries with improvements than declines and consistency between girls and boys. Both boys and girls improved in six countries and Ontario province, while both declined only in Norway and Quebec province.


## Performance at the International Benchmarks in TIMSS 2003

TIMSS identified four benchmark levels to describe what students know and can do in mathematics and demonstrate the range of performance internationally - advanced, high, intermediate, and low. There were large differences across countries in the percentages of students reaching the various benchmarks.

At the eighth grade, students reaching the advanced benchmark used algebraic, geometric, and measurement concepts in complex
problem situations. At the other end of the performance continuum, those reaching the low benchmark demonstrated some basic mathematical knowledge.

- The highest performing countries - Singapore, Chinese Taipei, Korea and Hong Kong SAR - had about one-third of their students or more (from 31 to $44 \%$ ) reaching the advanced benchmark followed by Japan with 24 percent. In contrast, all other countries had 11 percent or less of their students reaching the advanced benchmark, including 19 of the lowest-performing countries with 1 percent or less.
- The nine highest-performing countries and the two Canadian provinces had 95 percent or more of their students reaching the low benchmark whereas the eight lowest-performing countries had less than half their students reaching the low benchmark.

At the fourth grade, students reaching the advanced benchmark used understanding of fractions and decimals, measurement concepts, and data interpretation in a wide variety of relatively complex situations. Those reaching the low benchmark demonstrated some mathematical knowledge.

- With fewer and more homogenous countries at the fourth grade, Singapore had 38 percent of its students reaching the advanced benchmark followed by 21 to 22 percent of the students in Hong Kong SAR and Japan. Five of the lowest-performing countries had 1 percent or less of their students reaching the advanced benchmark.
- Eight countries as well as the US state of Indiana had 95 percent or more their students reaching the low benchmark and all except four countries had at least three-fourths of their students reaching this level. In the four lowest-performing countries (the Philippines, Iran, Tunisia, and Morocco), less than half the students reached the low benchmark.


## Students' Home Context for Learning Mathematics

- At the eighth grade, students were asked about the level of their parents' schooling and their own expectations. Higher levels of parents' education were associated with higher student achievement in almost all countries. Also, students expecting to finish university had substantially greater average mathematics achievement than those without university expectations.
- At both the eighth and fourth grades, in general, students from homes where the language of the test was always or almost always spoken had higher average achievement than those who spoke it less frequently.
- At both the eighth and fourth grades, across countries on average, there was a clear-cut relationship between number of books in the home and mathematics achievement.
- Mathematics achievement was positively related to computer usage, particularly at eighth grade, with average achievement highest among students reporting using computers at home and at school. Next highest was achievement among students using computers at home but not school, followed by students using computers at school but not home, and then those using computers at other places or not using them at all. At both grades, the percentages of students reporting that they did not use a computer at all varied dramatically across countries - from one percent or less to as many as two-thirds at the eighth grade and three-fourths at the fourth grade.


## The Mathematics Curriculum

- Most countries had mathematics curricula defined at the national level (except Australia and the United States) and often supported by ministry directives, instructional guides, school inspections, and recommended textbooks.
- At the eighth grade, all participants emphasized understanding mathematical concepts and principles followed by mastering basic skills. At the fourth grade, mastering basic skills was emphasized most, followed by understanding concepts and principles.
- In relation to the TIMSS assessment at the eighth grade, on average, participants reported that nearly all the number topics ( $96 \%$ ) were included in their curricula, 78 percent of the measurement topics, 67 percent of the geometry topics, 63 percent of the algebra topics, and 39 percent of the data topics.
- At the fourth grade, on average, 81 percent of the measurement topics assessed were included in the participants' curricula, 68 percent of the number topics, 62 percent of the data topics, 54 percent of the patterns and relationships topics, and 38 percent of the geometry topics.
- At the eighth grade, across countries on average, teachers reported that 95 percent of the students had been taught the number topics, 78 percent the measurement topics, 69 percent the geometry topics, 66 percent the algebra topics, and 46 percent the data topics.
- At the fourth grade, across countries on average, teachers reported that 86 percent of the students had been taught the measurement topics, 80 percent the data topics, 79 percent the patterns and relationships topics, 77 percent the number topics, and 55 percent the geometry topics.


## Teachers of Mathematics

- Mathematics teachers reported considerable teaching experience. At both the eighth and fourth grades, on average, students were taught by teachers with 16 years of experience.
- On average, 76 percent of the eighth-grade students and 65 percent of the fourth-grade students were taught by teachers with at least a university degree.
- Seventy percent of the eighth-grade students, on average, had mathematics teachers with a mathematics major and more than half ( $54 \%$ ) with a major in mathematics education or both. At the fourth grade, teachers typically studied primary or elementary education ( $80 \%$ of the students with such teachers, on average).
- At both grades, schools reported that their professional development programs emphasized improving content knowledge and teaching skills. More than 80 percent of students were taught mathematics by teachers having at least some professional development training in these areas.
- Across the five mathematics content areas assessed, teachers reported being ready to teach nearly all the major topics tested by TIMSS. Almost all of the eighth-grade students were taught by such teachers - 90 percent or more for 15 out of 18 topics (all but three data topics). Similarly, 90 percent or more of the fourth-grade students were taught by teachers reporting readiness for teaching 14 of the 16 topics (exceptions were two geometry topics).


## Classroom Instruction

- At the eighth grade, on average, teachers reported that 27 percent of the instructional time was devoted to algebra, 26 percent to geometry, 21 percent to number, 10 percent to each of measurement and data, and 6 percent to other. At fourth grade, the profile was different, with number receiving 38 percent of the instructional time. Patterns and relationships, measurement, and geometry each were given 13 to 16 percent, data 9 percent, and other 6 percent.
- At the eighth grade, on average, teachers reported asking 62 percent of students to practice numerical operations and 43 percent to work on fractions and decimals in at least half their lessons. At the fourth grade, teachers reported an overwhelming emphasis on having stu-
dents practice numerical operations ( $82 \%$ of students in half or more of the lessons).
- At the eighth grade, on average, for 45 percent of students, teachers reported devoting some time in at least half their lessons to asking students to decide what procedures to use for solving complex problems.
- At both eighth and fourth grades, the textbook was often the foundation of mathematics instruction. On average, about two-thirds of students at both grades had teachers who reported using a textbook as the primary basis for their lessons, and another third as a supplementary resource.
- On average, the three most common instructional activities were teacher lecture, teacher-guided student practice, and students working on problems on their own (totaling $59 \%$ of the time at eighth grade and $61 \%$ at fourth grade).
- Policies about calculator usage varied dramatically from country to country. At the eighth grade, in 10 countries nearly all the students ( $98 \%$ or more) were permitted to use calculators. In contrast, less than half were permitted to use calculators in seven countries. At fourth grade, on average, more than half the students were not permitted to use calculators. Only five countries reported permitting widespread calculator usage (at least $90 \%$ of students).
- The percentages of eighth-grade students asked to use calculators in half their lessons averaged from 27 percent for checking answers to 14 percent for exploring number concepts. Relatively few fourthgrade students were asked to engage in any calculator activities in as many as half their lessons.
- At the eighth grade, on average, 56 percent of students were taught by teachers who used only or mostly constructed-response tests.

These students had higher average achievement than did students whose teachers used only multiple-choice tests or a combination.

## School Contexts for Learning and Instruction

- At the eighth grade, average mathematics achievement was 57 points higher for students in schools with few students from economically disadvantaged homes than for students attending schools with more than half their students from disadvantaged homes. At fourth grade, the difference was 47 points.
- At both eighth and fourth grades, there was a strong positive relationship between the principals' perception of school climate (based on seven questions about behaviors of teachers, parents, and students) and average mathematics achievement. Asked the same seven questions, teachers had a somewhat more gloomy view of school climate than principals, but the relationship with achievement still was positive.
- Teachers were asked about the safety of their schools' neighborhoods, how safe they felt in their schools, and the sufficiency of security policies and practices. On average, 72 percent of eighth-grade students and 75 percent of fourth-grade students attended schools characterized as safe by their teachers. At both grades, there was a positive relationship between school safety and mathematics achievement.



## Introduction

## What is TIMSS?

TIMSS 2003 is the most recent in a very ambitious series of international assessments conducted in nearly 50 countries to measure trends in mathematics and science learning. The aim of TIMSS, the Trends in International Mathematics and Science Study, is to improve the teaching and learning of mathematics and science by providing data about students' achievement in relation to different types of curricula, instructional practices, and school environments. The variation across the nearly 50 participating countries provides a unique opportunity to study different approaches to educational practices and how these can improve achievement.

TIMSS is a project of the International Association for the Evaluation of International Achievement (IEA), an independent international cooperative of national research institutions and government agencies that has been conducting studies of cross-national achievement since 1959. Conducted first in 1995 and then in 1999, the regular four-year cycle of TIMSS studies provides countries with an unprecedented opportunity to obtain comparative information about their students' achievement in mathematics and science.

Even more important, TIMSS also collects a rich array of contextual information about how mathematics and science learning takes place in each country. TIMSS asks students, their teachers, and their school principals to complete questionnaires about the curriculum,
schools, classrooms, and instruction. This data gives policy makers, curriculum specialists, and researchers a dynamic picture of implementation of educational policies and practices around the world, providing an invaluable perspective from which to consider educational reform and improvement. TIMSS results, which were first reported in 1996, have stirred debate and spurred reform efforts around the world. ${ }^{1}$

TIMSS 1995 compared the mathematics and science achievement of students in 41 countries at five grade levels. TIMSS 1999 was designed to provide trends in eighth-grade mathematics and science achievement. Also, 1999 represented four years since the first TIMSS, and the population of students originally assessed as fourth-graders had advanced to the eighth grade. Thus, TIMSS 1999 also provided information about whether the relative performance of these students had changed in the intervening years. TIMSS 2003 was administered at the eighth and fourth grades. For countries that participated in previous assessments, TIMSS 2003 provides three-cycle trends at the eighth grade $(1995,1999,2003)$ and data over two points in time at the fourth grade (1995 and 2003). In countries new to the study, the 2003 results can help policy makers and practitioners assess their comparative standing and gauge the rigor and effectiveness of the mathematics and science programs.

## Who Conducts TIMSS?

TIMSS is a major undertaking of the IEA, and together with PIRLS, comprises the core of IEA's regular cycle of studies. ${ }^{2}$ The IEA delegated responsibility for the overall direction and management of the project to the TIMSS \& PIRLS International Study Center at Boston College. Headed by Michael O. Martin and Ina V.S. Mullis, the study center is located in the Lynch School of Education. In carrying out the project, the TIMSS \& PIRLS International Study Center works closely with the IEA Secretariat in Amsterdam, the IEA Data Processing Center in Hamburg, Statistics Canada in Ottawa, and Educational Testing Service in Princeton, New Jersey.

1 Robitaille, D.F., Beaton, A.E., and Plomp, T., eds. (2000), The Impact of TIMSS on the Teaching and Learning of Mathematics and Science, Vancouver, BC: Pacific Educational Press.
2 PIRLS is the IEA's Progress in International Reading Literacy Study developed to assess students' reading achievement at fourth grade. Thirtyfive countries participated in PIRLS 2001, and nearly 50 countries are participating in PIRLS 2006.

To coordinate the TIMSS project nationally and to work with the international team, each participating country designates an individual to be the National Research Coordinator (NRC). The NRCs have the formidable task of implementing the TIMSS study in their countries in accordance with the TIMSS guidelines and procedures. The quality of the assessments depends on the work of the NRCs and their colleagues in carrying out the very complex sampling, data collection, and scoring tasks involved. Continuing the tradition of superlative work established in 1995 and 1999, the TIMSS 2003 NRCs performed their many tasks with great dedication, competence, and energy, and should be commended for their commitment to the project and the high quality of their work (see Appendix G for a list of the TIMSS 2003 NRCs).

## Which Countries Participated in TIMSS 2003?

Exhibit l shows the 49 countries that participated in TIMSS 2003. The decision to participate in any IEA study is coordinated through the IEA secretariat in Amsterdam and made solely by each member country according to its own data needs and resources. Exhibit 1 shows that 23 countries also participated in TIMSS 1995 and TIMSS 1999. For these participants, trend data across three-points in time are included in this report. Eleven countries participated in TIMSS 2003 and TIMSS 1999 only, while three countries participated in TIMSS 2003 and TIMSS 1995. These countries have trend data for two points in time. TIMSS 2003 is proud to welcome 12 new participating countries to the study. TIMSS 2003 is equally proud of its fledgling benchmarking program, whereby regions or localities of countries can participate in the study to compare to international standards. TIMSS 2003 included four benchmarking participants (one US state, two Canadian provinces, and Spain's Basque Country) in addition to its 49 countries.

At the eighth grade, results are presented for 46 countries and four benchmarking participants. At the fourth grade, results are presented for 25 countries and three benchmarking participants. Argentina was unable to complete the steps necessary to have its data available

## Exhibit 1: Countries Participating in TIMSS

2003, 1999, and 1995
Australia
Belgium (Flemish)
Bulgaria
Cyprus
England
Hong Kong, SAR
Hungary
Iran, Islamic Rep. of
Israel
Italy
Japan
Korea, Rep. of
Latvia
Lithuania
Netherlands
New Zealand
Romania
Russian Federation
Singapore
Slovak Republic
Slovenia
South Africa
United States
Ontario Province, Can.
Quebec Province, Can

## 2003 and 1999

Argentina
Chile
Chinese Taipe
Indonesia
Jordan
Macedonia, Rep. of
Malaysia
Moldova, Rep. of
Morocco
Philippines
Tunisia
Indiana State, US

## 2003 and 1995

Norway
Scotland
Sweden

## 2003

Armenia
Bahrain
Botswana
Egypt
Estonia
Ghana
Lebanon
Palestinian National Authority
Saudi Arabia
Serbia
Syrian Arab Republic
Yemen
Basque Country, Spain


Argentina administered the TIMSS 2003 data collection one year late, and did not score and process its data in time for inclusion in this report. Because the characteristics of their samples are not completely known, achievement data for Syria and Yemen are presented in Appendix F of this report.
for analysis for this report. Because the characteristics of their samples are not completely known, the results for Syrian Arab Republic and Yemen are presented in Appendix F.

For the sake of comparability across countries and across assessments, all testing was conducted at the end of the school year, except in Korea. As noted in the Exhibits in this report, Korea tested the same cohort of students as other countries, but later in 2003 at the beginning of the next school year. The seven countries on a Southern Hemisphere school schedule (Australia, Botswana, Chile, Malaysia, New Zealand, Singapore, and South Africa) tested in October through December of 2002, which was the end of the school year there. The remaining countries tested towards the end of the 2002-2003 school year, most often in April, May, or June of 2003.

## What Is the Comparability Across the Grades and Ages Tested?

Exhibit 2 contains information about the grade(s) tested in each country. Because TIMSS studies the effectiveness of curriculum and instruction on student learning, it is designed to assess mathematics and science achievement at the same point in schooling across countries. More specifically, TIMSS tries to assess students at two points - at the end of four years of formal schooling and at the end of eight years of formal schooling.

Exhibit 2 reveals that, with few exceptions, the grade(s) tested in each country represented the eighth year of formal schooling and the fourth year of formal schooling. Thus, solely for convenience, the report usually refers to the grade tested as the eighth or the fourth grade, respectively.

As can be seen from the first two columns in Exhibit 2, countries have different policies and practices about the age of entry to primary school. This information is extremely valuable and important in considering the achievement results, since differences in these policies can affect achievement through the grades. Everything else being equal,
students who start their formal schooling at a younger age will be younger than their counterparts at the grades assessed and those who start their schooling at an older age will be older. Again, everything else being equal, students who are older may be considered more mature. In many countries, students must be 6 years old to start school and they do start school at that age. In several countries, students must be six, but they do not need to start school at that age and can wait. In this case, students or their parents may wait, most often for economic reasons, so that the older students may come from disadvantaged backgrounds. Also, in a number of countries children must be 7 years old. On the other hand, in several countries some or all of the students are younger than six when they start school, including Australia, Cyprus, England, Jordan, Scotland, and Tunisia.

Besides the age of entry, policies on promotion and retention also can affect how old students are when they reach a particular grade. If students have been retained, they will be older when they are assessed. Most often, it is the lower achievers who are retained and consequently the older students have lower achievement. Consistent with most educational endeavors, the interaction between grade and age in school is complicated. As can be seen from Exhibit 2, the variation in policies and practices across the countries assessed resulted in a considerable range in the average age of the students assessed. At the eighth grade, for example, Scotland with an additional year of schooling because they start school at such a comparatively early age ( 4.5 to 5.5 years old), had the youngest students assessed - 13.7 years old on average. At the other end of the spectrum, students in Ghana start school closer to age 7 and may be retained because of attendance problems; as a result they were the oldest students assessed at 15.5 years old. Despite this wide range, however, eighth-grade students in most countries were between 14 and 15 years old. Similarly, fourth-grade students averaged between 10 and 11 years old, even though those in Scotland were 9.7 years old and those in Latvia had an average age of 11.1.

Exhibit 2: Information About the Grades Tested in TIMSS 2003


| Countries | Policy on Age of Entry to Primary School ${ }^{1}$ | Practice on Age of Entry to Primary School | Policy on Promotion / Retention | Country's <br> Name for Grade Tested | Years of Schooling ${ }^{2}$ | Average Age at Time of Testing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | Children must be 7 years old | 6.5 to 7 | Automatic | Grade 8 | 8 | 14.9 |
| Australia | Children must be 5 or 6 years old, depending on state or territory | 5 or 6 | Automatic | Year 8 | 8 or 9 | 13.9 |
| Bahrain | Children must be 6 years old | 6 | Automatic in grade 1, students in grades 2-8 must demonstrate a certain amount of academic progress | Second intermediate | 8 | 14.1 |
| Belgium (Flemish) | Children begin school during the calendar year in which they become 6 years old | 6 | Students must show progress, based on exam by teachers | Second grade of secondary education | 8 | 14.1 |
| Botswana | Children must be 6 years old by June | 6 to 7 | Students can be retained if found to be extremely deficient, after consultation with parents and teachers; students can repeat a maximum of 3 grades | Form 1 | 8 | 15.1 |
| Bulgaria | Children must be 6 years old by the end of June to begin school the following September | 7 | Students must demonstrate basic knowledge and skills | Grade 8 | 8 | 14.9 |
| Chile | Children must be 6 years old in March or before | 6 | Automatic in grades 1-4, dependent on marks and approval in grades 5-8 | Eighth grade of basic education | 8 | 14.2 |
| Chinese Taipei | Children must be 6 years old | 6 | Automatic | Junior high school, grade 2 | 8 | 14.2 |
| Cyprus | Children must be 5 years, 6 months old | 5 years, 6 months to 6 years, 5 months | Automatic in grades 1-6, dependent on progress in grades 7-8 | 2nd grade - gymnasium | 8 | 13.8 |


| Egypt | Children must be 6 years old, space permitting (otherwise 7) | 6 to 7 | Students in grades 1-5 must pass an exam but if retained are automatically promoted the following year, students in grades 6-8 must pass an exam and are not automatically promoted the following year | Preparatory 3 | 8 | 14.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| England | Children must begin school at the start of the term following their 5th birthday | 5 | Automatic | Year 9 | 9 | 14.3 |
| Estonia | Children must be 7 years old by October 1 | 7 | Students must have positive marks, and in grades 7-8 must also pass a school exam | Grade 8 | 8 | 15.2 |
| Ghana | Children must be 6 years old | 6 to 7 | Students are retained with parental consent if fail to satisfy certain conditions such as adequate attendance | Junior secondary school II (JSS II) | 8 | 15.5 |
| Hong Kong, SAR | Children must be 6 years old | 6 | Determined by schools but retention rate cannot exceed $3 \%$; in practice 99\% of students are promoted | Secondary 2 (S2) | 8 | 14.4 |
| Hungary | Children must be 6 years old | 6 or older | Automatic | Grade 8 | 8 | 14.5 |
| Indonesia | Children must be 6 years old | 6 | Based on student achievement, usually small number are retained | 2nd grade of junior secondary school | 8 | 14.5 |
| Iran, Islamic Rep. of | Children must be 6 years old | 6 | Students must pass a final examination | Third grade of guidance school | 8 | 14.4 |
| Israel | Children must be 6 years old | 6 | Mostly automatic, but students diagnosed as having difficulties are transferred to remedial classes | Grade 8 | 8 | 14.0 |
| Italy | Children may begin school when 5 years old if their birth date is before April 30 of the academic year, otherwise 6 | 6 | Students must demonstrate a certain amount of academic progress | Grade 8 (III media) | 8 | 13.9 |
| Japan | Children must be 6 years old | 6 | Automatic | 2nd grade at the lower secondary school | 8 | 14.4 |
| Jordan | Children must be 5 years, 8 months old | 5 years, 8 months | Retention rate cannot exceed 5\% | Grade 8 | 8 | 13.9 |
| * Korea, Rep. of | Children must be 6 years old | 6 | Automatic | Middle school, 2nd grade | 8 | 14.6 |
| Latvia | Children must be 7 years old in the calendar year | 7 | Automatic | Grade 8 | 8 | 15.0 |

[^0]2 Represents years of schooling counting from the first year of ISCED Level 1

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.

Exhibit 2: Information About the Grades Tested in TIMSS 2003 (Continued...)

| Countries | Policy on Age of Entry to Primary School ${ }^{1}$ | Practice on Age of Entry to Primary School | Policy on Promotion / Retention | Country's Name for Grade Tested | Years of Schooling ${ }^{2}$ | Average Age at Time of Testing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Lebanon | Children must be 6 or 7 years old | 6 or 7 | Dependent on final exams | Grade 8 | 8 | 14.6 |
| Lithuania | Children must be 6 or 7 years old, depending on child's development and parents' wishes | 7 or older | Students must have sufficient marks (at least 4 on a scale of 1-10) in all subjects, and approval by the School Teachers' Board | Grade 8 | 8 | 14.9 |
| Macedonia, Rep. of | Children must be 7 years old by September 1 | 6.5 to 7 | Automatic in grades 1-4; students in grades 5-8 must have marks of at least 3 (on a scale 1-5) in all subjects, but if do not finish grade 8 by age 17 are transferred to schools for adults | Grade 8 | 8 | 14.6 |
| Malaysia | Children must be 6 years old by January 1 of the academic year | 6 or older | Automatic | Form 2 | 8 | 14.3 |
| Moldova, Rep. of | Children must be 6 or 7 years old, parents decide | 6 or 7 | If students fail any subjects they are promoted with negative marks for those subjects, students with more than 5 negative marks are retained | Grade VIII | 8 | 14.9 |
| Morocco | Children must be 7 years old | 7 | Automatic except for students in grade 6 who must pass provincial exams | $2^{\circ}$ secondary | 8 | 15.2 |
| Netherlands | Children must be 6 years old | 6 | Essentially automatic, but students can be retained if have serious learning difficulties or fall behind because of illness | Grade 8 | 8 | 14.3 |
| New Zealand | Children must attend primary school from their 6th birthday, but have the right to be enrolled from age 5 | Almost all start on or near 5th birthday | Automatic | Year 9 | 8.5-9.5 | 14.1 |
| Norway | Children begin school the year they become 7 years old | 7 | Automatic | Grade 8 (these students started in Grade 2) | 7 | 13.8 |
| Palestinian Nat'l Auth. | Children must be 6 years old for governmental schools, 5.5 years old for special schools | 6 | Automatic in grades 1-4, students in grades 5-8 must have at least $50 \%$ passing marks in all subjects and if do not must pass exams in the relevant subjects | Grade 8 | 8 | 14.1 |
| Philippines | Children must be 6 years old | 6 to 7 | Students must repeat and pass any subjects they failed before being promoted | Second year high school | 8 | 14.8 |
| Romania | Children must be 7 years old | 7 | Students in grades 1-4 must receive a "satisfactory" grade in all subjects, students in grades 5-8 must receive grades of at least 5 (on a scale of 1 10) in all subjects | Grade 8 | 8 | 15.0 |
| Russian Federation | For 4-year primary schools, children must be 6 years old by September 1 but require special medical confirmation; for 3-year primary schools, children must be 7 years old by September 1 but parents have a right to keep children at home until age 8 | 6 or 7 | Automatic | Eighth grade | 7 or 8 | 14.2 |
| Saudi Arabia | Children must be 6 years old | 6 | Students must achieve a satisfactory level in all subjects | Second year of middle school | 8 | 14.1 |
| Scotland | Children can begin school between the ages of 4.5 and 6 ; those with a MarchAugust birth date automatically begin school in September following their 5th birthday; parents of children with a September-December birth date can defer school entry until the following year (most choose not to defer) | 4.5 to 5.5 | Automatic | Secondary 2 (S2) | 9 | 13.7 |
| Serbia | Children begin school during the calendar year in which they turn 7 , but may enter school earlier with parental consent if mature enough and ready for school | 7 | Students must have marks of at least 2 (on a scale 1-5) in all subjects | 8th grade of primary school | 8 | 14.9 |
| Singapore | Children must be 6 years old | 6 | Automatic in grades 1-5, students in grade 6 must satisfy basic requirements on national exam to be promoted to grade 7 | Secondary 2 | 8 | 14.3 |

[^1]2 Represents years of schooling counting from the first year of ISCED Level 1.

Exhibit 2: Information About the Grades Tested in TIMSS 2003 (...Continued)


| Countries | Policy on Age of Entry to Primary School ${ }^{1}$ | Practice on Age of Entry to Primary School | Policy on Promotion / Retention | Country's <br> Name for Grade Tested | Years of Schooling ${ }^{2}$ | Average Age at Time of Testing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Slovak Republic | Children must be 6 years old | 6 | Automatic | Grade 8 | 8 | 14.3 |
| Slovenia | For 8-year elementary schools, children must be 7 years old in the calendar year; for 9 -year elementary schools, children must be 7 years old in the calendar year, but are promoted from grade 5 of 8 -year elementary school directly to grade 7 of 9 -year elementary school | 6.5 | Automatic | Grade 7 of 8 -year elementary school; Grade 8 of 9 -year elementary school | 7 or 8 | 13.8 |
| South Africa | Children must be 6 years old by June 30 of the academic year, which begins in January | 7 | Automatic in grades 1-3, students in grades 4-8 must pass an exam | Grade 8 | 8 | 15.1 |
| Syrian Arab Republic | -- | -- | -- | Grade 8 | 8 | 14.0 |
| Sweden | Children begin school during the calendar year of their 7th birthday | 7 | Automatic | Year 8 | 8 | 14.9 |
| Tunisia | Children must be 6 years old | 5.5 to 6 | Students must demonstrate a certain amount of academic progress | 8th year of basic school | 8 | 14.8 |
| United States | Varies by state; 6 or 7 , depending on birth date | 6 or 7 | Automatic | Grade 8 | 8 | 14.2 |
| International Avg. |  |  |  |  | 8 | 14.5 |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | Children must be 6 years old | 6 | At the end of each cycle of 2 years, students with low achievement may be retained upon teachers' decision | 2nd year of compulsory secondary education | 8 | 14.1 |
| Indiana State, US | No official state policy | 6 to 7 | Promotion/retention decisions are made by individual schools | Grade 8 | 8 | 15.1 |
| Ontario Province, Can. | Children must be 6 years old by December 31 | 6 | Automatic | Grade 8 | 8 | 13.8 |
| Quebec Province, Can. | Children must be 7 years old by October 1 | 6 | Automatic | Secondary II | 8 | 14.2 |

[^2]2 Represents years of schooling counting from the first year of ISCED Level 1. A dash ( - ) indicates comparable data are not available.

| Countries | Policy on Age of Entry to Primary School ${ }^{1}$ | Practice on Age of Entry to Primary School | Policy on Promotion / Retention | Country's Name for Grade Tested | Years of Schooling ${ }^{2}$ | Average Age at Time of Testing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | Children must be 7 years old | 6.5 to 7 | Automatic | Grade 4 | 4 | 10.9 |
| Australia | Children must be 5 or 6 years old, depending on state or territory | 5 or 6 | Automatic | Year 4 | 4 or 5 | 9.9 |
| Belgium (Flemish) | Children begin school during the calendar year in which they become 6 years old | 6 | Students must show progress, based on exam by teachers | Fourth grade of primary education | 4 | 10.0 |
| Chinese Taipei | Children must be 6 years old | 6 | Automatic | Elementary school, grade 4 | 4 | 10.2 |
| Cyprus | Children must be 5 years, 8 months old | 5 years, 8 months to 6 years, 7 months | Automatic | 4th grade - primary | 4 | 9.9 |
| England | Children must begin school at the start of the term following their 5th birthday | 5 | Automatic | Year 5 | 5 | 10.3 |
| Hong Kong, SAR | Children must be 6 years old | 6 | Determined by schools but retention rate cannot exceed $3 \%$; in practice 99\% of students are promoted | Primary 4 (P4) | 4 | 10.2 |
| Hungary | Children must be 6 years old | 6 or older | Automatic | Grade 4 | 4 | 10.5 |
| Iran, Islamic Rep. of | Children must be 6 years old | 6 | Students must pass a final examination | Fourth grade of primary school | 4 | 10.4 |
| Italy | Children may begin school when 5 years old if their birth date is before April 30 of the academic year, otherwise 6 | 6 | Students must demonstrate a certain amount of academic progress | Grade 4 (IV elementare) | 4 | 9.8 |
| Japan | Children must be 6 years old | 6 | Automatic | 4th grade at the elementary school | 4 | 10.4 |
| Latvia | Children must be 7 years old in the calendar year | 7 | Automatic | Grade 4 | 4 | 11.1 |
| Lithuania | Children must be 6 or 7 years old, depending on child's development and parents' wishes | 7 or older | Students must have sufficient marks (at least 4 on a scale of 1-10) in all subjects, and approval by the School Teachers' Board | Grade 4 | 4 | 10.9 |
| Moldova, Rep. of | Children must be 6 or 7 years old, parents decide | 6 or 7 | If students fail any subjects they are promoted with negative marks for those subjects, students with more than 5 negative marks are retained | Grade IV | 4 | 11.0 |
| Morocco | Children must be 7 years old | 7 | Automatic | $4^{\circ}$ primary | 4 | 11.0 |
| Netherlands | Children must be 6 years old | 6 | Essentially automatic, but students can be retained if have serious learning difficulties or fall behind because of illness | Grade 4 | 4 | 10.2 |
| New Zealand | Children must attend primary school from their 6th birthday, but have the right to be enrolled from age 5 | Almost all start on or near 5th birthday | Automatic | Year 5 | 4.5-5.5 | 10.0 |
| Norway | Children begin school the year they become 6 years old, but the first year is called "Grade 1/Preschool" | 6 | Automatic | Grade 4 | 4 | 9.8 |
| Philippines | Children must be 6 years old | 6 to 7 | Students must repeat and pass any subjects they failed before being promoted | Grade 4 | 4 | 10.8 |
| Russian Federation | For 4-year primary schools, children must be 6 years old by September 1 but require special medical confirmation; for 3 -year primary schools, children must be 7 years old by September 1 but parents have a right to keep children at home until age 8 | 6 or 7 | Automatic | Fourth grade for 4-year primary school; Third grade for 3-year primary school | 3 or 4 | 10.6 |

[^3]Exhibit 2: Information About the Grades Tested in TIMSS 2003 (...Continued)


| Countries | Policy on Age of Entry to Primary School ${ }^{1}$ | Practice on Age of Entry to Primary School | Policy on Promotion / Retention | Country's <br> Name for Grade Tested | Years of Schooling ${ }^{2}$ | Average Age at Time of Testing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scotland | Children can begin school between the ages of 4.5 and 6; those with a MarchAugust birth date automatically begin school in September following their 5th birthday; parents of children with a September-December birth date can defer school entry until the following year (most choose not to defer) | 4.5 to 5.5 | Automatic | Primary 5 (P5) | 5 | 9.7 |
| Singapore | Children must be 6 years old | 6 | Automatic | Primary 4 | 4 | 10.3 |
| Slovenia | For 8-year elementary schools, children must be 7 years old in the calendar year; for 9 -year elementary schools, children must be 6 years old in the calendar year | 5.5 or 6.5 | Automatic | Grade 3 of 8 -year elementary school; Grade 4 of 9 -year elementary school | 3 or 4 | 9.8 |
| Tunisia | Children must be 6 years old | 5.5 to 6 | Students must demonstrate a certain amount of academic progress | 4th year of basic school | 4 | 10.4 |
| United States | Varies by state; 6 or 7 , depending on birth date | 6 or 7 | Automatic | Grade 4 | 4 | 10.2 |
| Yemen | Children must be 6 years old | 6 or older | Automatic | Grade 4 | 4 | 10.9 |
| International Avg. |  |  |  |  | 4 | 10.3 |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US | No official state policy | 6 to 7 | Promotion/retention decisions are made by individual schools | Grade 4 | 4 | 11.0 |
| Ontario Province, Can. | Children must be 6 years old by December 31 | 6 | Automatic | Grade 4 | 4 | 9.8 |
| Quebec Province, Can. | Children must be 7 years old by October 1 | 6 | Automatic | Second year of the second cycle | 4 | 10.1 |

Having valid and efficient samples in each country is crucial to the quality and integrity of the study. The accuracy of the survey results depends on the quality of the sampling information available, and particularly on the quality of the samples. TIMSS developed procedures and guidelines to ensure that the national samples were of the highest quality possible. Standards were established and well-documented for coverage of the target population and participation rates. For the most part, the national samples were drawn in accordance with the TIMSS standards, and achievement results can be compared with confidence. Countries that deviated from the guidelines are specially noted in this report.

## What Was the Nature of the Mathematics Test and Background Questionnaires?

A particular challenge for TIMSS 2003 was updating the set of frameworks underlying the assessments. The publication entitled TIMSS Assessment Frameworks and Specifications 2003 serves as the basis of TIMSS 2003 and beyond. ${ }^{3}$ It describes in some detail the mathematics and science content to be assessed in mathematics and science. Topic areas are elaborated with objectives specific to the eighth and fourth grades. In general, the mathematics topic areas are number, algebra, measurement, geometry, and data.

Developing the TIMSS tests for 2003 was a cooperative venture involving all of the NRCs during the entire process. The TIMSS \& PIRLS International Study Center began the process with an item-writing workshop for NRCs and their colleagues. Through a series of efforts, countries then submitted items that were reviewed by mathematics subject-matter specialists. Participating countries field-tested the items with representative samples of students, and all of the potential new items were reviewed by the Science and Mathematics Item Review Committee. The NRCs had several opportunities to review the items and scoring criteria. The resulting TIMSS 2003 mathematics tests contained 194 items at the eighth grade and 161 items at the fourth grade.

3 Mullis, I.V.S., Martin, M.O., Smith, T.A., Garden, R.A., Gregory, K.D., Gonzalez, E.J., Chrostowski, S.J., and O’Connor, K.M. (2003), TIMSS Assessment Frameworks and Specifications 2003 (2nd Edition), Chestnut Hill, MA: Boston College.
The TIMSS frameworks developed 1995 also were used for 1999. See, Robitaille, D.F., McKnight, C.C., Schmidt, W.H., Britton, E.D., Raisen, S.A., and Nicol, C. (1993), TIMSS Monograph No. 1: Curriculum Frameworks for Mathematics and Science, Vancouver, BC: Pacific Educational Press.

About one-third of the eighth-grade questions were in the con-structed-response format, requiring students to generate and write their answers. These questions, some of which required extended responses, were allotted about $40 \%$ of the testing time. At the fourth grade, more than two-fifths of the items were in constructed response format, accounting for almost half of the testing time. Chapter 2 of this report contains example items illustrating the range of mathematics concepts and processes covered in the TIMSS 2003 tests. Appendix A contains more information about test development for TIMSS 2003.

To guide questionnaire development, the TIMSS frameworks document also describes the contextual factors associated with students' learning in mathematics and science. A special effort was made for TIMSS 2003 to reduce burden for students, teachers, and schools and to address emerging policy concerns. In particular, TIMSS worked to examine curricular goals; the educational resources and facilities provided; the teaching force and how it is educated, equipped, and supported; classroom activities and characteristics; home support and involvement; and the experiences and attitudes that students themselves bring to the educational enterprise.

## How Do Country Characteristics Differ?

International studies of student achievement provide valuable comparative information about student performance, instructional practice, and curriculum. It is important, however, to consider the results in light of country-wide demographic and economic factors. Some selected demographic characteristics of the TIMSS 2003 countries are presented in Exhibit 3. As can be seen, countries range widely in population size and in geographic area. Countries also vary widely on indicators of health, such as life expectancy at birth and infant mortality rate. The economic indicators, such as gross national income per capita, reveal there is great disparity in the economic resources available to countries. Finally, there are differences in enrollment rates and pupilteacher ratios. For the enrollment rates, figures only were available
for primary and secondary school and not specifically for fourth and eighth grades. For the fourth grade, it can be seen that the countries generally had 90 percent or more of their children enrolled in primary school. The figures pertinent to the eighth grade in particular were not available, but they most certainly would be higher than those provided for the secondary school.


|  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |

1 Estimates are for mid-year 2002, includes all residents regardless of legal status or citizenship except refugees not permanently settled in the country of asylum as they are generally considered to be part of their country of origin. World Bank's 2004 World Development Indicators, p. 38-41.
2 Area is the total surface area in square kilometers, comprising all land area, inland bodies of waters, and some coastal water ways. World Bank's 2004 World Development Indicators, p. 14-17
3 Number of years a newborn infant would live if prevailing patterns of mortality at its birth were to stay the same throughout its life. World Bank's 2004 World Development Indicators, p. 108-111
4 Infant mortality rate is the number of deaths of infants under one year of age during 2002 per 1,000 live births in the same year. World Bank's 2004 Wor/d Development Indicators, p. 108-111.
5 GNI per Capita in U.S. dollars is converted using the World Bank's Atlas method. World Bank's 2004 World Development Indicators, p. 14-17.
6 An international dollar has the same purchasing power over GNI as a U.S. dollar in the United States. World Bank's 2004 World Development Indicators, p. 14-17

7 Ratio of the children of official school age who are enrolled in school to the population of the corresponding official school age. Based on the International Classification of Education 1997. World Bank's 2004 World Development Indicators, p. 76-79.
8 Primary pupil-teacher ratio is the number of pupils enrolled in primary school divided by the number of primary school teachers (regardless of their assignment). World Bank's 2004 World Development Indicators, p. 72-75 and Global Education Digest 2004 by UNESCO Institute for Statistics.
9 Data provided by the NRC of Chinese Taipei.
10 Figures for Belgium (Flemish) are for the whole country of Belgium.
11 Figures for England and Scotland are for the whole region of United Kingdom.
12 Data for Bahrain, Cyprus and Palestinian Nat'I Auth. was obtained from Global Education Digest 2004 by UNESCO Institute for Statistics and The World Fact Book 2004.
A dash $(-)$ indicates data are not available.

Exhibit 3: Selected Characteristics of TIMSS 2003 Countries


| GNI per Capita ${ }^{6}$ (Purchasing Power Parity) | Net Enrollment Ratio in Education ${ }^{7}$ (\% of Relevant Group) |  | Primary Pupil-Teacher | Countries |
| :---: | :---: | :---: | :---: | :---: |
|  | Primary | Secondary | Ratio ${ }^{8}$ |  |
| 10190 | 100 | 81 | 20.0 | Argentina |
| 3230 | 85 | 85 | 18.8 | Armenia |
| 27440 | 96 | 88 | 18.1 | Australia |
| - | 91 | 81 | 16.4 | 12 Bahrain |
| 28130 | 100 | - | 12.1 | 10 Belgium (Flemish) |
| 7740 | 81 | 55 | 26.6 | Botswana |
| 7030 | 90 | 87 | 16.8 | Bulgaria |
| 9420 | 89 | 75 | 32.2 | Chile |
| - | 98 | 93 | 18.6 | 9 Chinese Taipei |
| - | 95 | 88 | 17.2 | 12 Cyprus |
| 3810 | 90 | 78 | 22.3 | Egypt |
| 26580 | 100 | 95 | 18.2 | 11 England |
| 11630 | 98 | 92 | 14.1 | Estonia |
| 2080 | 60 | 30 | 32.1 | Ghana |
| 27490 | 98 | 72 | 20.0 | Hong Kong, SAR |
| 13070 | 90 | 87 | 10.5 | Hungary |
| 3070 | 92 | 47 | 20.9 | Indonesia |
| 6690 | 87 | - | 24.3 | Iran, Islamic Rep. of |
| 19000 | 100 | 88 | 12.2 | Israel |
| 26170 | 100 | 88 | 10.7 | Italy |
| 27380 | 100 | 100 | 20.4 | Japan |
| 4180 | 91 | 80 | 20.2 | Jordan |
| 16960 | 99 | 91 | 32.1 | Korea, Rep. of |
| 9190 | 91 | 89 | 15.0 | Latvia |
| 4600 | 90 | - | 16.8 | Lebanon |
| 10190 | 97 | 92 | 16.0 | Lithuania |
| 6420 | 93 | 82 | 18.0 | Macedonia, Rep. of |
| 8500 | 95 | 69 | 19.6 | Malaysia |
| 1600 | 78 | 68 | 19.5 | Moldova, Rep. of |
| 3730 | 88 | 31 | 28.3 | Morocco |
| 28350 | 99 | 90 | 9.8 | Netherlands |
| 20550 | 98 | 92 | 14.8 | New Zealand |
| 36690 | 100 | 95 | - | Norway |
| - | 95 | 81 | - | 12 Palestinian Nat'l Auth. |
| 4450 | 93 | 56 | 35.4 | Philippines |
| 6490 | 93 | 80 | 19.6 | Romania |
| 8080 | - | - | 17.1 | Russian Federation |
| 12660 | 59 | 53 | 12.3 | Saudi Arabia |
| 26580 | 100 | 95 | 18.2 | 11 Scotland |
| - | 75 | - | - | Serbia |
| 23730 | - | - | 25.4 | Singapore |
| 12590 | 89 | 75 | 19.0 | Slovak Republic |
| 18480 | 93 | 96 | 12.6 | Slovenia |
| 9810 | 90 | 62 | 37.1 | South Africa |
| 25820 | 100 | 96 | 11.4 | Sweden |
| 3470 | 98 | 39 | 24.0 | Syrian Arab Republic |
| 6440 | 97 | 68 | 21.9 | Tunisia |
| 36110 | 94 | 87 | 15.4 | United States |
| 800 | 67 | 35 | 29.8 | Yemen |

1 Estimates are for mid-year 2002, includes all residents regardless of legal status or citizenship except refugees not permanently settled in the country of asylum as they are generally considered to be part of their country of origin. World Bank's 2004 World Development Indicators, p. 38-41.
2 Area is the total surface area in square kilometers, comprising all land area, inland bodies of waters, and some coastal water ways. World Bank's 2004 World Development Indicators, p. 14-17
3 Number of years a newborn infant would live if prevailing patterns of mortality at its birth were to stay the same throughout its life. World Bank's 2004 Wor/d Development Indicators, p. 108-111.
4 Infant mortality rate is the number of deaths of infants under one year of age during 2002 per 1,000 live births in the same year. World Bank's 2004 World Development Indicators, p. 108-111.
5 GNI per Capita in U.S. dollars is converted using the World Bank Atlas method. World Bank's 2004 World Development Indicators, p. 14-17.
6 An international dollar has the same purchasing power over GNI as a U.S. dollar in the United States. World Bank's 2004 Wor/d Development Indicators, p. 14-17.

7 Ratio of the children of official school age who are enrolled in school to the population of the corresponding official school age. Based on the International Classification of Education 1997. World Bank's 2004 World Development Indicators, p. 76-79
8 Primary pupil-teacher ratio is the number of pupils enrolled in primary school divided by the number of primary school teachers (regardless of their assignment). World Bank's 2004 Wor/d Development Indicators, p. 72-75 and Global Education Digest 2004 by UNESCO Institute for Statistics.
Data provided by the NRC of Chinese Taipei.
10 Figures for Belgium (Flemish) are for the whole country of Belgium
Figures for England and Scotland are for the whole region of United Kingdom.
12 Data for Bahrain, Cyprus and Palestinian Nat'I Auth. was obtained from Global Education Digest 2004 by UNESCO Institute for Statistics and The World Fact Book 2004
A dash ( - ) indicates data are not available.


## Chapter 1

## International Student Achievement in Mathematics

Chapter 1 summarizes achievement for eighth- and fourth-grade students on the TIMSS 2003 mathematics assessment for each of the participating countries. It also shows trends in student performance at the eighth grade for those countries that also participated in TIMSS 1995 and 1999. At the fourth grade, trends are presented for those countries that participated in the 1995 assessment (no assessment was conducted at the fourth grade in 1999). Achievement differences by gender at both grades are also provided.

## How Do Countries Differ in Mathematics Achievement?

The first page of Exhibit 1.1 presents the distribution of student achievement ${ }^{1}$ for the 46 countries and four benchmarking entities that participated at the eighth grade in TIMSS 2003 and the second page presents the distribution of student achievement for the 25 countries and three benchmarking entities that participated at the fourth grade. ${ }^{2}$ Countries are shown in decreasing order of average (mean) scale score, together with an indication of whether the country average is significantly higher

[^4]or lower than the international average. The international average of 467 at the eighth grade was obtained by averaging across the mean scores for each of the 46 participating countries. The mean scores for the four benchmarking participants were not included in calculating the average. ${ }^{3}$ At the fourth grade, the international average of 495 was obtained by averaging across the mean scores for the 25 participating countries. It should be noted that the results for the eighth and fourth grades are not directly comparable. While the scales for the two grades are expressed in the same numerical units, they are not directly comparable in terms of being able to say how much achievement or learning at one grade equals how much achievement or learning at the other grade. Comparisons only can be made in terms of relative performance. ${ }^{4}$

At the eighth grade, with such a large number of participating countries, it is not surprising that the results reveal substantial differences in mathematics achievement between the highest- and lowestperforming countries, from an average of 605 for Singapore to 264 for South Africa. Twenty-six countries (including England) and the four benchmarking participants achieved average mathematics scores that were significantly above the international average and 18 countries scored below the international average. Romania and Moldova performed about the same as the international average. At the fourth grade, the range in achievement was from 594 in Singapore to 339 in Tunisia. Fourteen countries and the three benchmarking participants performed above the international average. Moldova, Australia, New Zealand, and Scotland performed at about the international average. Seven countries achieved below the international average.

For both the eighth and fourth grades, Exhibit 1.1 illustrates the broad range of achievement both within and across the countries assessed. It shows a graphical representation of the distribution of student performance within each country. Achievement for each country is shown for the 25 th and 75 th percentiles as well as for the 5 th and 95 th percentiles. ${ }^{5}$ Each percentile point indicates the percentage of students performing

[^5]below and above that point on the scale. For example, 25 percent of the eighth-grade students in each country performed below the 25th percentile for that country, and 75 percent performed above the 25 th percentile. The range between the 25 th and 75 th percentiles represents performance by the middle half of the students. In most countries, the range of performance for the middle group was between 100 and 130 scale-score points. In contrast, performance at the 5th and 95th percentiles represents the extremes in both lower and higher achievement. The range of performance between these two score points, which includes 90 percent of the population, is approximately 270 to 300 points in most countries. The dark boxes at the midpoints of the distributions show the 95 percent confidence intervals around the average achievement in each country. ${ }^{6}$

As well as showing the wide spread of student achievement within each country, the percentiles also provide a perspective on the size of the differences among countries. Even though performance generally differed very little between one country and the next higher- or lower-performing country, the range in performance across the participating countries was very large at both grades. For example, Singaporean students had the highest average achievement at both grades, with their average eighth-grade performance exceeding performance at the 95th percentile in the lower-performing countries such as Botswana, Saudi Arabia, Ghana, and South Africa. Similarly, at the fourth grade, average performance in Singapore exceeded performance at the 95th percentile in Iran, the Philippines, Morocco, and Tunisia. This means that only the most proficient students in the lower-performing countries approached the level of achievement of Singaporean students of average proficiency.

To aid in interpretation, Exhibit 1.1 also includes the years of formal schooling and average age of the students in each country. Equivalence of chronological age does not necessarily mean that students have received the same number of years of formal schooling or studied the same curriculum. For example, as described in the introduction,

6 See the "IRT Scaling and Data Analysis" section of Appendix A for more details about calculating standard errors and confidence intervals for the TIMSS statistics.

Exhibit 1.1: Distribution of Mathematics Achievement


* Represents years of schooling counting from the first year of ISCED Level 1.
** Taken from United Nations Development Programme's Human Development Report 2003, p. 237-240.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available


## Exhibit 1.1: Distribution of Mathematics Achievement

mathematics Grade



[^6]countries have different policies about the age at which students begin formal schooling and different policies about promotion and retention from grade to grade.

At the eighth grade, the aim was that the students assessed would have had eight years of formal schooling. Most notably, students in Norway, most of Slovenia, and parts of the Russian Federation had fewer years of formal schooling than their counterparts in other countries, while those in England, Scotland, New Zealand, and parts of Australia had more years of schooling. Even though the students assessed at the eighth grade typically averaged between 14 and 15 years old, the variety of countries assessed and their situations also resulted in a considerable range in the average age of the students assessed. To illustrate how education policies can affect the interaction between age and number of years of schooling, it is interesting to note that Scotland, one of the few countries with an additional year of schooling, starts formal schooling at an early age and had the youngest students assessed- 13.7 years old on average. Other countries assessing students younger than 14 years old included Slovenia, Norway, and Cyprus with 13.8 and Australia, Jordan, and Italy with 13.9. Students in the Balkans and some Eastern European countries start school later and tended to be older, particularly in Estonia with an average of $\mathbf{1 5 . 2}$. Students also were older in several African countries including Botswana and South Africa both averaging 15.1, Morocco averaging 15.2, and Ghana averaging 15.5. In these countries, it is not unusual for students to start school at an older age and also perhaps to find it necessary to interrupt their schooling.

At the fourth grade, the aim was to assess students having had four years of formal schooling and this was the case for the most part. However, some students in Slovenia and parts of the Russian Federation had only three years of formal schooling, and students in England and Scotland as well as some in Australia and New Zealand had five years. In terms of chronological age, students in most countries averaged between 10 and 11 years old. Consistent with the patterns at the eighth grade, students were somewhat younger in Scotland, averaging 9.7 years old; Italy,

Slovenia, and Norway, averaging 9.8; and Australia and Cyprus, averaging 9.9. The students in the Balkan and Eastern European countries were somewhat older, especially in Latvia with an average age of 11.1.

As a reminder that not all countries are equally well equipped to meet the challenge of educating their young people, Exhibit 1.1 includes the value for each country on the Human Development Index provided by the United Nations Development Programme (UNDP). ${ }^{7}$ The index has a minimum value of 0 and a maximum of 1.0. Countries with high values on the index enjoy long life expectancy, high levels of school enrollment and adult literacy, and a good standard of living as measured by per capita GDP. For example, TIMSS countries with index values greater than 0.9 included Australia, Belgium (Flemish), England, Israel, Italy, Japan, New Zealand, Norway, The Netherlands, Scotland, Sweden, and the United States. All except Norway have average eighth-grade mathematics achievement above the international average. However, not all countries above the international average had an index value as high as this.

Exhibit 1.2 shows how a country's average achievement in mathematics compares to achievement in the other countries. This figure shows whether or not the differences in average achievement between pairs of countries are statistically significant. Selecting a country of interest and reading across the table, a circle with a triangle pointing up indicates significantly higher performance than the comparison country listed across the top; absence of a symbol indicates no significant difference in performances; and a circle with triangle pointing down indicates significantly lower performance.

The data in Exhibit 1.2 reinforce the point that, when ordered by average achievement, adjacent countries usually did not significantly differ from each other, although the differences in achievement between the highperforming and low-performing countries were very large. Because of this wide range in performance, the pattern for a number of countries was one of having lower mean achievement than some countries, about the same mean achievement as other countries, and higher mean achievement than a third group of countries.

7 Human Development Report 2003, p. 237-240.

# Exhibit 1.2: Multiple Comparisons of Average Mathematics Achievement 

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


## Benchmarking Participants

| Basque Country, Spain | - | - | - | - | - | - | (1) | - | - | - |  | - | - | (1) | (1) | ) |  | - | © | - | () | - |  |  |  | 0 | 0 | 0 | - | - | - | - | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Indiana State, US | (-) | (-) | - | - | - | (-) | - | ( ${ }^{( }$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |  |  |  | 0 |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Ontario Province, Can. | (-) | - | - | - | - | - | - | - |  | 0 | 0 | - | 0 | $\bigcirc$ | 0 | 0 | - | - | 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | - | - | - | 0 | - | 0 |
| Quebec Province, Can. | (-) | (-) | (-) | (-) | - |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | - | - | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 |

[^7]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

|  |  | $\begin{aligned} & \text { ᄃ } \\ & \text { ¢ } \\ & \text { \% } \end{aligned}$ |  |  |  |  |  |  |  |  | $\begin{aligned} & \text { y } \\ & \frac{0}{0} \\ & \frac{0}{2} \\ & \frac{1}{2} \end{aligned}$ |  |  |  |  |  |  |  | Countries |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | - | 0 | 00 | 0 | 0 | 0 | 0 | Singapore |
| - | - | 0 | 0 | 0 | $\bigcirc$ | - | 0 | 0 | 0 | 0 | - | - | - | 00 | 0 | 0 | $\bigcirc$ | 0 | Korea, Rep. of |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 00 | 0 | 0 | 0 | 0 | Hong Kong, SAR |
| 0 | - | 0 | 0 | 0 | $\bigcirc$ | - | 0 | 0 | 0 | 0 | - | - | - | 00 | 0 | 0 | - | - | Chinese Taipei |
| 0 | - | 0 | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 0 | 0 | $\bigcirc$ | $\bigcirc$ | - | $0 \cdot$ | 0 | $\bigcirc$ | 0 | 0 | Japan |
| 0 | - | 0 | - | 0 | 0 | - | - | - | 0 | 0 | - | - | - | 00 | 0 | - | - |  | Belgium (Flemish) |
| 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | $\bigcirc$ | 0 | 0 | 0 | 0 | - | $\bigcirc$ | - | 00 | 0 | $\bigcirc$ | 0 |  | Netherlands |
| 0 | - | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | - | - | - | 00 | 0 | 0 | $\bigcirc$ | - | Estonia |
| 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 0 | 0 | $\bigcirc$ | $\bigcirc$ | - | 00 | 0 | $\bigcirc$ |  | $\checkmark$ | Hungary |
| 0 | - | - | - | 0 | 0 | - | - | 0 | 0 | 0 | - | - | - | 00 | 0 |  | - | - | Malaysia |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 00 | 0 |  | - | - | Latvia |
| 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 0 | 0 | - | - | - | 00 | 0 |  | - | - | Russian Federation |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 00 | 0 |  | (-) | - | Slovak Republic |
| 0 | 0 | - | - | 0 | 0 | - | - | - | 0 | 0 | - | - | - | 00 | 0 |  | - | - | Australia |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  | - | - | United States |
| 0 | 0 | - | - | 0 | $\bigcirc$ | - | - | - | 0 | - | - | - | - | 00 | 0 |  | - | - | Lithuania |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  | - | - | Sweden |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | - | - | 0 | 00 | 0 |  | - | - | England |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 00 | 0 |  | - | - | Scotland |
| 0 | 0 | - | 0 | 0 | 0 | - | 0 | - | 0 | 0 | - | - | - | 00 | 0 | - | - | - | Israel |
| 0 | 0 | - | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | $\bigcirc$ | - | 00 |  |  | $\checkmark$ | - | New Zealand |
| 0 | 0 | - | - | 0 | $\bigcirc$ | - | - | 0 | 0 | 0 | - | - | - | 00 |  | (1) | - | - | Slovenia |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | - | 00 |  | - | - | - | Italy |
| 0 | 0 | - | 0 | 0 | $\bigcirc$ | - | - | 0 | 0 | 0 | - | - | - | 00 | - | - | - | - | Armenia |
| 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | - | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 00 | (1) | - | - | - | Serbia |
| 0 | 0 | - | - | 0 | 0 | - | 0 | 0 | 0 | 0 | - | - | 0 | 00 | - | - | - | - | Bulgaria |
| 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 0 | - 0 | 0 | 0 | - | 00 | © | - | - | - | Romania |
| 0 | 0 | - | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | - | 0 | 0 | 00 | - | ( | - | - | Norway |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 00 | © | - | (1) | - | Moldova, Rep. of |
| 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 00 | - | - | - | - | Cyprus |
|  |  | 0 | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 00 | (1) | - | - | - | Macedonia, Rep. of |
|  |  |  | 0 | 0 | 0 | - | 0 | - | 0 | 0 | - | - | - | 00 | (1) | - | - | - | Lebanon |
| (1) |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 00 | (1) | $\checkmark$ | - | - | Jordan |
| ( | (-) | - |  |  |  |  | - | 0 | 0 | 0 | - | - | - | 0 | $\bigcirc$ | - | - | - | Iran, Islamic Rep. of |
| (-) | (-) | - |  |  |  |  |  | 0 | 0 | 0 | $\bigcirc$ | 0 | 0 | 00 | (1) | - | - | $\checkmark$ | Indonesia |
| (1) | (1) | - |  |  |  |  | - | 0 | 0 | 0 | - | - | - | 0 | - | - | - | - | Tunisia |
| (-) | (-) | - |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (1) | - | - | - | Egypt |
| (1) | (1) | (1) | - |  | - |  |  | 0 | 0 | 0 | - | - | - | 0 | (1) | - | (1) | - | Bahrain |
| (-) | - | - | (1) | - | - | - | (1) |  |  |  | 0 | 0 | 0 | 00 | (1) | - | - | - | Palestinian Nat I Auth. |
| - | - | - | - | - | - | - | - |  |  |  |  | $\bigcirc$ | - | 0 | (1) | - | - | - | Chile |
| - | (-) | (1) | - | - | - | - | - |  |  |  |  | $\bigcirc$ | 0 | 00 | © | - | - | - | Morocco |
| (-) | - | - | - | (1) | - | - | - | - |  |  |  |  | 0 | 00 | (1) | - | - | - | Philippines |
| - | - | - | - | - | - | - | - | - | - | - |  |  | $\bigcirc$ | 00 | © | - | - | - | Botswana |
| - | - | - | - | - | - | - | - | - | - | (1) | - | - |  | 00 | - | - | - | - | Saudi Arabia |
| (-) | - | - | (1) | - | - | - | () | (1) | - | (-) | (-) | - | (-) |  | (1) | - | - | - | Ghana |
| (-) | - | (-) | - | (-) | (1) | ( ) | - | (1) | - | (1) | ( ) | ( | (-) |  | - | - | - | - | South Africa |

- Average achievement significantly higher than comparison country
(-)
Average achievement significantly lower than comparison country


[^8]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


## Benchmarking Participants

| Indiana State, US | © | (1) | (1) | - | (1) | - |  |  |  |  |  | 0 | - | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | - | 0 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ontario Province, Can. | (1) | (1) | (1) | - | $\checkmark$ | (1) | - | - | - | - | - |  |  |  |  | $\bigcirc$ | 0 | 0 | 0 | 0 | 0 | - | 0 | - | - | 0 | © |  |  |
| Quebec Province, Can. |  | - | - | - | (1) | - | - | ( | - | - | - | - |  |  |  |  | - | 0 | 0 | 0 | - | - | - | - | 0 | 0 | - |  |  |

Average achievement significantly higher than comparison country
(-) Average achievement significantly lower than comparison country

At both the eighth and fourth grades, Singapore was the topperforming country having significantly higher mean achievement than the rest of the participating countries. At the eighth grade, the Republic of Korea, Hong Kong SAR, and Chinese Taipei had significantly higher mean achievement than all of the other participating countries except Singapore. Japan also performed very well, with significantly higher achievement than most other participating countries, as did Belgium (Flemish), the Netherlands, Estonia, and Hungary. At the fourth grade, in addition to Singapore, Hong Kong SAR, Japan, and Chinese Taipei had significantly higher average achievement than most of the other participating countries as did Belgium (Flemish).

How Has Mathematics Achievement Changed Since 1995 and $1999 ?$
Exhibit 1.3 shows the countries that have comparable data from previous TIMSS assessments at the eighth and fourth grades. At the eighth grade, 35 countries and three of the benchmarking participants have data from one or both of the previous TIMSS assessments conducted in 1995 and 1999. Well over half of the countries and two of the benchmarking entities, the Canadian provinces of Ontario and Quebec, have participated in all three assessments. Of these, 18 countries as well as Ontario and Quebec have trends in mathematics achievement for their eighth-grade students across three points in time-1995, 1999, and 2003. For several three-time participants, not all the results are presented because they were not strictly comparable. For example, changes in policy about age of school entry complicated trend data collection in Australia and Slovenia so their 1999 data are not shown. Also, the 1995 data are not shown for Israel, Italy, and South Africa since the characteristics of their samples were not completely known in that first assessment. Twelve countries and the US state of Indiana can monitor changes in performance between 1999 and 2003, and five countries between 1995 and 2003, including Australia, Sweden, Scotland, Slovenia, and Norway. At the fourth grade, 15 of the TIMSS 2003

Exhibit 1.3: Trends in Mathematics Achievement



- 2003 country average significantly higher than previous assessment year
(7) 2003 country average significantly lower than previous assessment year


[^9]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 1.3: Trends in Mathematics Achievement (Continued...)

- 2003 country average significantly higher than previous assessment year
(v) 2003 country average significantly lower than previous assessment year



## Exhibit 1.3: Trends in Mathematics Achievement (...Continued) <br> 

 in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995. Data for Latvia in this exhibit include Latvian-speaking schools only.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 1.3: Trends in Mathematics Achievement


Trend notes: Because of differences between 1995 and 2003 in population coverage, 1995 data are not shown for Italy. Data for Latvia in this exhibit include Latvian-speaking schools only. To be comparable with 1995, 2003 data for New Zealand in this exhibit include students in English medium instruction only (98\% of the estimated population).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
countries and Ontario and Quebec also participated in TIMSS 1995. Since TIMSS was not conducted at the fourth grade in 1999, these participants can track changes in student achievement over an eight-year period, between 1995 and 2003.

For the countries participating in assessments prior to TIMSS 2003, Exhibit 1.3 compares average achievement between the years. ${ }^{8}$ Countries are presented in descending order according to their average TIMSS 2003 achievements. At the eighth grade, a number of countries had significantly higher achievement in TIMSS 2003 than in previous assessments. Most notably, Korea, Hong Kong SAR, the US, Latvia (LSS), Lithuania, and Ontario have shown a pattern of improvement with significant change over the 8 -year period. For Lithuania, the increase between 1995 and 1999 also was significant. Israel and the Philippines showed significant improvement from 1999 to 2003. Countries showing a decrease at the eighth grade in TIMSS 2003, from 1995, 1999, or both, included Japan, Belgium (Flemish), the Russian Federation, the Slovak Republic, Sweden, Bulgaria, Norway, Cyprus, Macedonia, Iran, Tunisia, and Quebec.

At the fourth grade, many countries had significant increases in average achievement between 1995 and 2003. Participants showing improved performance included Hong Kong SAR, Latvia (LSS), England, Cyprus, New Zealand, Slovenia, and Ontario. Several participants showed significant declines, including the Netherlands, Norway, and Quebec.

A number of countries showed remarkable changes in mathematics achievement over the eight-year period covered by the TIMSS assessments, some of which may be the result of societal or educational changes during this time. For example, the political changes in Eastern Europe more than a decade ago spawned far-reaching educational reform initiatives that have changed the face of education in many countries in the region. The achievement growth in Latvia and Lithuania, as well as the strong performance of Estonia in its first TIMSS appearance, may reflect the efforts at improvement in those countries. In contrast, countries in the region where reform efforts seem to have been less successful
include Bulgaria, the Russian Federation, and the Slovak Republic, each of which show large decreases over the period.

## What Are the Gender Differences in Mathematics Achievement?

Exhibit 1.4 shows gender differences in eighth- and fourth-grade mathematics achievement in 2003. It presents average achievement separately for girls and boys for each of the TIMSS 2003 countries, as well as the difference between the means. Countries are shown in increasing order of this gender difference. The gender difference for each country is shown by a bar indicating the amount of the difference, whether the direction of the difference favored girls or boys, and whether the difference is statistically significant (indicated by a darkened bar).

On average, across all countries, there was essentially no difference in achievement between boys and girls at either the eighth or fourth grade, although the situation varied from country to country. In many countries the results paralleled the international pattern and the gender difference was negligible. However, at the eighth grade, countries where girls had significantly higher achievement included Serbia, Macedonia, Armenia, Moldova, Singapore, the Philippines, Cyprus, Jordan, and Bahrain. Participants where boys had significantly higher achievement included the United States, Italy, Hungary, Lebanon, Belgium (Flemish), Morocco, Chile, Ghana, Tunisia, US state of Indiana and Quebec province. At the fourth grade, girls had significantly higher average achievement in Singapore, Moldova, the Philippines, and Armenia. Boys had higher average achievement in the Netherlands, the United States, Italy, Cyprus, Scotland, and in the two Canadian provinces.

Achievement differences between TIMSS 2003 and 1995 and 1999 are presented separately for girls and for boys in Exhibit 1.5. At the eighth grade, both boys and girls had significantly higher achievement in 2003 in Israel, Lithuania, the Philippines, the United States, and Ontario. Girls showed improved performance compared to previous


Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9)
₹ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
Did not satisfy guidelines for sample participation rates (see Exhibit A.9). National Desired Population does not cover all of International Desired Population (see Exhibit A.6)

2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 1.4: Average Mathematics Achievement by Gender
матнематісs
Grade


$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries | Girls |  |  |  |  | Boys |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2003 Average Scale Score | $\begin{aligned} & 1999 \text { to } 2003 \\ & \text { Difference } \end{aligned}$ |  | $\begin{aligned} & 1995 \text { to } 2003 \\ & \text { Difference } \end{aligned}$ |  | 2003 Average Scale Score | $\begin{aligned} & 1999 \text { to } 2003 \\ & \text { Difference } \end{aligned}$ |  | $\begin{aligned} & 1995 \text { to } 2003 \\ & \text { Difference } \end{aligned}$ |  |
| Australia | 499 (5.8) | - - |  | -13 (7.1) |  | 511 (5.8) | - - |  | 4 (7.5) |  |
| Belgium (Flemish) | 532 (3.5) | -28 (7.7) | $\checkmark$ | -21 (8.9) | $\bigcirc$ | 542 (3.8) | -13 (9.0) |  | -4 (9.5) |  |
| Bulgaria | 476 (5.5) | -35 (8.1) | - | -57 (8.0) | $\checkmark$ | 477 (4.3) | -34 (8.2) | $\bigcirc$ | -45 (7.5) | (1) |
| Chile | 379 (3.5) | -9 (5.4) |  | $\checkmark>$ |  | 394 (4.3) | -3 (7.0) |  | $\diamond>$ |  |
| Chinese Taipei | 589 (4.9) | 5 (6.2) |  | $\checkmark>$ |  | 582 (5.2) | -5 (7.4) |  | $\checkmark>$ |  |
| Cyprus | 467 (1.9) | -11 (2.7) | (1) | -4 (3.3) |  | 452 (2.3) | -23 (3.6) | (\%) | -13 (4.2) | (1) |
| Hong Kong, SAR | 587 (3.8) | 4 (6.1) |  | 28 (7.9) | 0 | 585 (4.6) | 4 (7.5) |  | 8 (8.5) |  |
| Hungary | 526 (3.7) | -3 (5.4) |  | -1 (5.2) |  | 533 (3.5) | -2 (5.6) |  | 6 (5.1) |  |
| Indonesia | 411 (4.9) | 10 (7.2) |  | $\checkmark>$ |  | 410 (5.3) | 5 (7.3) |  | $\checkmark>$ |  |
| Iran, Islamic Rep. of | 417 (4.3) | 9 (6.0) |  | 12 (7.5) |  | 408 (4.2) | -24 (6.4) | $\bigcirc$ | -21 (6.3) | (1) |
| Israel | 492 (3.3) | 33 (5.4) | 0 | -- |  | 500 (4.5) | 25 (6.7) | 0 | - - |  |
| Italy | 481 (3.0) | 6 (5.3) |  | - - |  | 486 (3.9) | 2 (5.8) |  | - - |  |
| Japan | 569 (4.0) | -6 (4.7) |  | -8 (4.5) |  | 571 (3.6) | -11 (4.2) | $\bigcirc$ | -14 (4.2) | (\%) |
| Jordan | 438 (4.6) | 7 (6.7) |  | $\checkmark>$ |  | 411 (5.8) | -14 (8.3) |  | $\checkmark>$ |  |
| Korea, Rep. of | 586 (2.7) | 2 (4.1) |  | 15 (4.1) | 0 | 592 (2.6) | 2 (3.2) |  | 3 (3.8) |  |
| Latvia (LSS) | 509 (4.0) | 6 (5.3) |  | 22 (5.5) | 0 | 502 (4.4) | -6 (6.0) |  | 11 (6.1) |  |
| Lithuania | 503 (2.9) | 23 (5.4) | 0 | 32 (5.5) | 0 | 499 (3.0) | 16 (5.8) | 0 | 27 (5.5) | 0 |
| Macedonia, Rep. of | 439 (4.0) | -7 (6.5) |  | $\checkmark>$ |  | 431 (3.9) | -16 (5.8) | (1) | $\checkmark>$ |  |
| Malaysia | 512 (4.7) | -9 (6.7) |  | ১ ৪ |  | 505 (4.5) | -12 (7.4) |  | $\diamond \stackrel{\text { d }}{ }$ |  |
| Moldova, Rep. of | 465 (4.1) | -3 (5.8) |  | $\diamond>$ |  | 455 (4.8) | -16 (6.7) | (1) | $\checkmark>$ |  |
| Netherlands | 533 (4.1) | -4 (8.6) |  | 11 (7.8) |  | 540 (4.5) | -3 (8.4) |  | 5 (7.9) |  |
| New Zealand | 495 (4.8) | 0 (7.4) |  | -1 (7.2) |  | 493 (7.0) | 5 (10.2) |  | -12 (9.3) |  |
| Norway | 463 (2.7) | $\checkmark>$ |  | -35 (3.8) | ( | 460 (3.0) | $\checkmark>$ |  | -39 (4.1) | $\checkmark$ |
| Philippines | 383 (5.2) | 31 (8.4) | 0 | $\checkmark>$ |  | 370 (5.8) | 34 (8.7) | 0 | $\checkmark>$ |  |
| Romania | 477 (5.1) | 2 (8.0) |  | 5 (6.8) |  | 473 (5.0) | 3 (8.0) |  | -2 (7.3) |  |
| Russian Federation | 510 (3.5) | -16 (6.9) | ( | -15 (6.1) | - | 507 (4.4) | -20 (7.7) | $\bigcirc$ | -16 (7.5) | $\checkmark$ |
| Scotland | 500 (4.3) | $\checkmark>$ |  | 14 (6.8) | 0 | 495 (3.8) | $\checkmark>$ |  | -5 (7.9) |  |
| Singapore | 611 (3.3) | 7 (7.0) |  | 1 (5.9) |  | 601 (4.3) | -5 (8.6) |  | -7 (6.4) |  |
| Slovak Republic | 508 (3.4) | -24 (5.3) | (1) | -25 (4.7) | $\checkmark$ | 508 (4.0) | -28 (6.0) | - | -28 (5.3) | $\checkmark$ |
| Slovenia | 495 (2.6) | - - |  | 3 (3.9) |  | 491 (2.6) | - - |  | -6 (4.4) |  |
| South Africa | 262 (6.2) | -6 (9.4) |  | - - |  | 264 (6.4) | -19 (9.7) |  | - - |  |
| Sweden | 499 (3.0) | $\checkmark>$ |  | -43 (5.5) | (7) | 499 (2.7) | ১ > |  | -39 (5.4) | ( |
| Tunisia | 399 (2.6) | -37 (3.7) | (\%) | $\checkmark>$ |  | 423 (2.2) | -37 (3.8) | $\bigcirc$ | $\checkmark>$ |  |
| United States | 502 (3.4) | 3 (5.2) |  | 12 (5.8) | 0 | 507 (3.5) | 2 (5.9) |  | 12 (6.3) | 0 |
| \# England | 499 (5.3) | 12 (7.6) |  | 4 (6.7) |  | 498 (5.8) | -7 (7.7) |  | -2 (7.9) |  |
| International Avg. | 486 (0.7) | 0 (1.2) |  | -5 (1.3) | $\bigcirc$ | 485 (0.8) | -6 (1.4) | © | -9 (1.4) | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 502 (5.1) | -8 (8.6) |  | $\triangleleft>$ |  | 514 (5.8) | -6 (10.0) |  | $\checkmark>$ |  |
| Ontario Province, Can. | 520 (3.4) | 6 (4.7) |  | 20 (4.5) | 0 | 522 (3.4) | 3 (4.7) |  | 18 (4.8) | 0 |
| Quebec Province, Can. | 540 (3.7) | -27 (6.8) | (1) | -20 (7.7) | $\checkmark$ | 546 (3.3) | -19 (6.5) | (1) | -6 (7.2) |  |

Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia and Slovenia, and 1995 data are not shown for Israel, Italy, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995. Data for Latvia in this exhibit include Latvian-speaking schools only.

[^10]| Countries | Girls |  | Boys |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 2003 Average Scale Score | $\begin{aligned} & 1995 \text { to } 2003 \\ & \text { Difference } \end{aligned}$ | 2003 Average Scale Score | $\begin{gathered} 1995 \text { to } 2003 \\ \text { Difference } \end{gathered}$ |
| Australia | 497 (4.5) | 4 (5.9) | 500 (4.3) | 4 (6.0) |
| Cyprus | 505 (2.7) | 34 (4.5) | 514 (2.9) | 35 (4.8) - |
| England | 530 (3.9) | 51 (5.7) | 532 (4.5) | 44 (5.7) - |
| Hong Kong, SAR | 575 (3.4) | 17 (5.1) | 575 (3.4) | 18 (5.5) - |
| Hungary | 527 (3.8) | 8 (5.5) | 530 (3.3) | 6 (5.1) |
| Iran, Islamic Rep. of | 394 (6.5) | 15 (8.9) | 386 (5.5) | -8 (9.7) |
| Japan | 563 (1.8) | -1 (2.6) | 566 (2.1) | -5 (3.3) |
| Latvia (LSS) | 535 (3.2) | 30 (5.9) | 531 (3.9) | 38 (6.9) - |
| Netherlands | 537 (2.7) | -6 (4.4) | 543 (2.2) | -13 (4.2) © |
| New Zealand | 495 (2.8) | 22 (5.1) | 496 (2.4) | 31 (6.6) - |
| Norway | 449 (2.7) | -25 (5.0) | 454 (2.7) | -24 (4.5) 『 |
| Scotland | 485 (3.2) | -8 (5.2) | 496 (4.4) | 3 (6.5) |
| Singapore | 599 (5.5) | 4 (7.8) | 590 (6.2) | 4 (7.8) |
| Slovenia | 477 (3.0) | 19 (4.8) | 481 (3.5) | 15 (4.9) - |
| United States | 514 (2.4) | -2 (3.8) | 522 (2.7) | 3 (4.1) |
| ternation |  |  | 15 (1) |  |
| Benchmarking Participants |  |  |  |  |
| Ontario Province, Can. | 505 (3.6) | 19 (4.9) | 517 (4.7) | 26 (6.4) - |
| Quebec Province, Can. | 502 (2.7) | -46 (6.1) | 509 (2.8) | -42 (5.6) |

( 2003 significantly higher than 1995
(7) 2003 significantly lower than 1995
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
assessments in Hong Kong SAR, Korea, Latvia (LSS), and Scotland. There was no country in which boys showed improvement and girls did not. Both boys and girls had significantly lower average achievement in TIMSS 2003 in Bulgaria, Cyprus, Norway, the Russian Federation, the Slovak Republic, Sweden, Tunisia, and Quebec. In Belgium (Flemish), the girls showed a significant decrease but the boys did not. In Iran, Japan, Macedonia, and Moldova the boys had the significant decrease. At the fourth grade, changes in achievement were very consistent for both boys and girls. Both genders improved in Cyprus, England, Hong Kong, Latvia (LSS), New Zealand, Slovenia, and Ontario. In Norway and Quebec, both boys and girls showed declines. Only in the Netherlands did the genders behave differently, with boys showing a decline but not girls.


## Chapter 2 Performance at International Benchmarks

## How Do Countries Compare with International Benchmarks of Mathematics Achievement?

The TIMSS mathematics achievement scale summarizes student performance on test items designed to measure a wide range of student knowledge and proficiency. In order to provide meaningful descriptions of what performance on the scale could mean in terms of the mathematics that students know and can do, TIMSS identified four points on the scale for use as international benchmarks. Selected to represent the range of performance shown by students internationally, the advanced benchmark is 625 , the high benchmark is 550 , the intermediate benchmark is 475 , and the low benchmark is 400 . TIMSS worked with the Science and Mathematics Item Review Committee to conduct an ambitious scale-anchoring exercise to describe performance at these benchmarks.

Exhibit 2.1 summarizes what eighth- and fourth-grade students scoring at these benchmarks typically know and can do. At the eighth grade, performance ranged from using relatively complex algebraic and geometric concepts and relationships at the advanced
benchmark to having some basic mathematical knowledge at the low benchmark. At the fourth grade, students at the advanced benchmark showed the ability to solve a variety of problems whereas those at the low benchmark demonstrated an understanding of whole numbers, the properties of basic geometric shapes, and how to read simple bar graphs. More detailed descriptions appear in the remaining sections of the chapter, together with example test items illustrating performance at each benchmark.

Exhibit 2.2 displays the percentage of students in each participating country that reached each international benchmark. Both the eighth- and fourth-grade results are presented in decreasing order by percentage reaching the advanced benchmark. In general, the highperforming countries had greater percentages of students reaching each benchmark, and the low-performing countries had lesser percentages. Among the high performers at the eighth grade, for example, Singapore, Chinese Taipei, Korea, and Hong Kong SAR had about one-third or more of their students reaching the advanced benchmark, about two-thirds to three-fourths reaching the high benchmark, around 90 percent reaching the intermediate benchmark, and almost all (96 to 99 percent) reaching the low benchmark. In contrast, low-performing countries had almost no students reaching the advanced benchmark, from 0 to 4 percent reaching the high benchmark, less than 20 percent reaching the intermediate benchmark, and about half or fewer reaching the low benchmark. At the fourth grade, 38 percent of the Singaporean students performed at or above the advanced benchmark, followed by about one-fifth of the students from Hong Kong, SAR and Japan. In all three of these top-performing countries, nearly all fourthgrade students, from 97 to 99 percent, reached the low benchmark. For the lowest-performing countries, Tunisia and Morocco, very few, if any, fourth-grade students reached the advanced benchmark, about l percent reached the high benchmark, 8 to 9 percent the intermediate benchmark, and 28 to 29 percent the low benchmark.

Although Exhibit 2.2 is organized to draw particular attention to the percentage of high-achieving students in each country, it conveys information about the distribution of middle and low performers also. For example, even though the Netherlands does not have the highest percentages at the advanced benchmark ( 10 percent at eighth grade and 5 percent at fourth grade), it appears to do an excellent job of educating all of its students, since 97 percent of the eighth-grade students and 99 percent of the fourth-grade students reached the low benchmarks at their respective grades. It should be noted that at the eighth grade, a number of countries, as well as three of the benchmarking participants, have less than 6 percent of their eighth-grade students reaching the advanced benchmark but have 90 percent or more reaching the low benchmark.

Exhibits 2.3 and 2.4, for the eighth and fourth grades, respectively, provide information on the changes in student performance between the previous assessments and TIMSS 2003. The exhibits show the percentage of students reaching each international benchmark (advanced-625, high-550, intermediate-475, and low-400) in each of the years. In general, the patterns in overall achievement are reflected in the benchmarks. For example, at the eighth grade the decrease in performance in the Slovak Republic or in Bulgaria is also apparent at all four benchmarks, implying a decrease (at most levels) of the proficiency distribution. In Japan, however, the decrease is reflected at the three top benchmarks but not at the low benchmark. In contrast, the increase for Korea appears mainly at the two middle benchmarks, and for the Philippines at the two lower benchmarks. At the fourth grade, the general improvements between 1995 and 2003 also are reflected generally at the benchmarks. However, the pattern across the countries indicates more improvement at the lower parts of the distributions than at the advanced benchmark.

To help interpret the achievement results, the remaining sections of the chapter first describe eighth-grade mathematics achievement at each of the international benchmarks together with examples of the types of items typically answered correctly by students performing at the benchmark. It then describes fourth-grade achievement at each of the international benchmarks together with examples of the types of items typically answered correctly by students performing at the benchmark.

At both the eighth and fourth grades, the analysis of performance at these benchmarks in mathematics suggests that three primary factors appeared to differentiate performance among the four levels:

- The mathematical operation required;
- The complexity of the numbers or number system;
- The nature of the problem situation.

For example, there is evidence that students performing at the lower end of the scale could add, subtract, and multiply whole numbers. In contrast, students performing at the higher end of the scale solved non-routine problems involving relationships among fractions, decimals, and percents; various geometric properties; and algebraic rules.

## How Were the Benchmark Descriptions Developed?

To develop descriptions of achievement at the TIMSS 2003 international benchmarks, the TIMSS International Study Center used the scaleanchoring method. Scale anchoring is a way of describing students' performance at different points on the TIMSS 2003 achievement scales at eighth and fourth grades in terms of the types of items students at those grades, respectively, answered correctly. It involves an empirical component in which items that discriminate between successive points on the scale are identified, and a judgmental component in which subject matter experts examine the content of the items and generalize to students' knowledge and understandings.

For the scale-anchoring analysis, the results of students from all the TIMSS 2003 countries were pooled, so that the benchmark descriptions refer to all students achieving at that level. (That is, it does not matter which country the students are from, only how they performed on the test.) Criteria were applied to the TIMSS 2003 achievement scale results at the eighth grade to identify the sets of items that eighth-grade students reaching each international benchmark were likely to answer correctly and that those at the next lower benchmark were unlikely to answer correctly. ${ }^{1}$ Similarly, criteria were applied to the TIMSS 2003 achievement scale results at the fourth grade to identify the sets of items that fourth-grade students reaching each international benchmark were likely to answer correctly and that those at the next lower benchmark were unlikely to answer correctly.

The sets of items produced by the analysis represented the accomplishments of students reaching each successively higher benchmark, and were used by a panel of subject-matter experts from the TIMSS countries to develop the benchmark descriptions. ${ }^{2}$ The work of the panel involved developing a short description for each item of the mathematical understandings demonstrated by students answering it correctly, summarizing students' knowledge and understanding across the set of items for each benchmark to provide more general statements of achievement, and selecting example items illustrating the descriptions.

## How Should the Descriptions Be Interpreted?

In general, the parts of the descriptions that relate to the mathematical concepts or familiarity with procedures are relatively straightforward. It needs to be acknowledged, however, that the cognitive behavior necessary to answer some items correctly may vary according to students' experience. An item may require only simple recall for a student familiar with the item's content and context, but necessitate problem-solving strategies from a student unfamiliar with the material. Nevertheless, the descriptions are based on what the panel believed to be the way the

[^11]great majority of eighth- or fourth-grade students could be expected to perform when responding to the item.

It also needs to be emphasized that the descriptions of achievement characteristic of students at the international benchmarks are based solely on student performance on the TIMSS 2003 items. Since those items were developed in particular to sample the mathematics domains prescribed for this study, neither the set of items nor the descriptions based on them purport to be comprehensive. There are undoubtedly other mathematics curriculum elements on which students at the various benchmarks would have been successful if they had been included in the assessment.

Please note that at both grades, students reaching a particular benchmark demonstrated the knowledge and understandings characterizing that benchmark as well as the competencies of students at the lower benchmarks. The description of achievement at each higher benchmark is cumulative, building on the description of achievement demonstrated by students at the next lower benchmark.

Finally, it must be emphasized that the descriptions of the international benchmarks are provided as one possible way of beginning to examine student performance. Some students scoring below a benchmark may indeed know or understand some of the concepts that characterize a higher level. Thus, it is important to consider performance on the individual items and clusters of items in developing a profile of student achievement in each country.

Several example items are included for each benchmark to complement the descriptions by giving a more concrete notion of the abilities students were able to demonstrate. Each example item is accompanied by the percentage of correct responses for each country as well as the international average. In general, at each grade, the five or six countries scoring highest on the overall test also scored highest on each of the items used to illustrate benchmarks. Likewise, the five or six countries with the lowest mean achievement also tended to have consistently low percentages of correct responses on the illustrative items.

Not surprisingly, this was true for items assessing a range of cognitive skills - recall, ability to carry out routine procedures, and ability to solve routine and non-routine problems. The TIMSS 2003 results support the premise that successful problem solving is grounded in mastery of more fundamental knowledge and skills.

## Item Examples and Student Performance

Beginning with the eighth grade and then for the fourth grade, the remainder of this chapter describes each benchmark and presents two example items illustrating what students know and can do at that level. For each example item, the percent correct for each of the TIMSS 2003 countries is displayed, as well as the international average. The correct answer is circled for multiple-choice items. For open-ended items, the answers shown exemplify the types of student responses that were given full credit. The example items are ones that students reaching each benchmark were likely to answer correctly, and they represent the types of items used to develop the description of achievement at that benchmark. ${ }^{3}$

## Advanced International Benchmark - 625

Students can organize information, make generalizations, solve non-routine problems, and draw and justify conclusions from data. They can compute percent change and apply their knowledge of numeric and algebraic concepts and relationships to solve problems. Students can solve simultaneous linear equations and model simple situations algebraically. They can apply their knowledge of measurement and geometry in complex problem situations. They can interpret data from a variety of tables and graphs, including interpolation and extrapolation.

## High International Benchmark - 550

Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They can order, relate, and compute with fractions and decimals to solve word problems, operate with negative integers, and solve multi-step word problems involving proportions with whole numbers. Students can solve simple algebraic problems including evaluating expressions, solving simultaneous linear equations, and using a formula to determine the value of a variable. Students can find areas and volumes of simple geometric shapes and use knowledge of geometric properties to solve problems. They can solve probability problems and interpret data in a variety of graphs and tables.

## Intermediate International Benchmark - 475

Students can apply basic mathematical knowledge in straightforward situations. They can add, subtract, or multiply to solve one-step word problems involving whole numbers and decimals. They can identify representations of common fractions and relative sizes of fractions. They understand simple algebraic relationships and solve linear equations with one variable. They demonstrate understanding of properties of triangles and basic geometric concepts including symmetry and rotation. They recognize basic notions of probability. They can read and interpret graphs, tables, maps, and scales.

## Low International Benchmark - 400

Students have some basic mathematical knowledge.

## Advanced International Benchmark - 625

Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They demonstrate a developing understanding of fractions and decimals and the relationship between them. They can select appropriate information
to solve multi-step word problems involving proportions. They can formulate or select a rule for a relationship. They show understanding of area and can use measurement concepts to solve a variety of problems. They show some understanding of rotation.
They can organize, interpret, and represent data to solve problems.

## High International Benchmark - 550

Student can apply their knowledge and understanding to solve problems. Student can solve multistep word problems involving addition, multiplication, and division. They can use their understanding of place value and simple fractions to solve problems. They can identify a number sentence that represents situations. Students show understanding of three-dimensional objects, how shapes can make other shapes, and simple transformation in a plane. They demonstrate a variety of measurement skills and can interpret and use data in tables and graphs to solve problems.

## Intermediate International Benchmark - 475

Students can apply basic mathematical knowledge in straightforward situations. They can read, interpret, and use different representations of numbers. They can perform operations with threeand four-digit numbers and decimals. They can extend simple patterns. They are familiar with a range of two-dimensional shapes and read and interpret different representations of the same data.

## Low International Benchmark - 400

Students have some basic mathematical knowledge. Students demonstrate an understanding of whole numbers and can do simple computations with them. They demonstrate familiarity with the basic properties of triangles and rectangles. They can read information from simple bar graphs.

## Exhibit 2.2: Percentages of Students Reaching TIMSS 2003 International Benchmarks of Mathematics Achievement



[^12]
## Exhibit 2.2: Percentages of Students Reaching TIMSS 2003 International Benchmarks of

 Mathematics Achievement


[^13]
## Exhibit 2.3: Trends in Percentages of Students Reaching the TIMSS 2003 International Benchmarks of Mathematics Achievement in 1995, 1999, and 2003



| Countries | Advanced International Benchmark (625) |  |  |  | High International Benchmark (550) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $2003$ <br> Percent of Students | 1999 <br> Percent of Students | 1995 <br> Percent of Students |  | 2003 <br> Percent of Students | 1999 <br> Percent of <br> Students |  |  |  |
| Singapore | 44 (2.0) | 42 (3.5) | 40 (2.9) |  | 77 (2.0) | 77 (2.6) |  | 84 (1.8) | (7) |
| Chinese Taipei | 38 (2.0) | 37 (1.6) | $\checkmark>$ |  | 66 (1.8) | 67 (1.5) |  | $\checkmark>$ |  |
| Korea, Rep. of | 35 (1.3) | 32 (0.9) | 31 (1.1) | 0 | 70 (1.0) | 70 (1.0) |  | 67 (1.0) |  |
| Hong Kong, SAR | 31 (1.6) | 28 (2.1) | 23 (2.4) | 0 | 73 (1.8) | 70 (2.3) |  | 65 (3.2) | 0 |
| Japan | 24 (1.0) | 29 (0.9) - | 29 (1.0) | - | 62 (1.2) | 66 (1.0) | - | 67 (0.8) | ( ) |
| Hungary | 11 (1.0) | 13 (1.2) | 10 (0.8) |  | 41 (1.9) | 43 (1.9) |  | 40 (1.6) |  |
| Netherlands | 10 (1.5) | 11 (2.0) | 9 (1.9) |  | 44 (2.5) | 47 (4.1) |  | 41 (3.1) |  |
| Belgium (Flemish) | 9 (0.9) | 19 (1.5) (-) | 15 (1.5) | $\bigcirc$ | 47 (1.9) | 57 (1.7) | (-) | 54 (3.0) | ( |
| Slovak Republic | 8 (0.8) | 11 (1.2) | 11 (1.2) | - | 31 (1.7) | 42 (2.3) | $\checkmark$ | 43 (1.6) | ( |
| Australia | 7 (1.1) | - - | 7 (1.0) |  | 29 (2.4) | - - |  | 33 (1.8) |  |
| United States | 7 (0.7) | 7 (1.0) | 4 (0.7) | 0 | 29 (1.6) | 30 (1.6) |  | 26 (2.0) |  |
| Russian Federation | 6 (0.8) | 12 (1.6) | 9 (1.2) | ( ) | 30 (1.8) | 39 (2.8) | (7) | 38 (3.1) | (7) |
| Israel | 6 (0.6) | 4 (0.5) © | -- |  | 27 (1.5) | 19 (1.3) | 0 | - |  |
| Malaysia | 6 (1.0) | 10 (1.2) | $\rangle>$ |  | 30 (2.4) | 36 (2.4) |  | $\checkmark>$ |  |
| Lithuania | 5 (0.6) | 3 (0.6) - | 2 (0.5) | 0 | 28 (1.2) | 18 (2.0) | 0 | 17 (1.5) | 0 |
| New Zealand | 5 (1.3) | 6 (1.1) | 6 (1.0) |  | 24 (2.7) | 26 (2.4) |  | 28 (2.2) |  |
| Latvia (LSS) | 5 (0.9) | 6 (0.8) | 4 (0.7) |  | 27 (1.7) | 28 (1.8) |  | 22 (1.4) | 0 |
| Romania | 4 (0.6) | 4 (0.9) | 4 (0.6) |  | 21 (1.8) | 20 (2.0) |  | 21 (1.6) |  |
| Scotland | 4 (0.6) | $\checkmark>$ | 5 (1.4) |  | 25 (2.1) | $\checkmark>$ |  | 24 (2.7) |  |
| Bulgaria | 3 (0.7) | 9 (2.1) | 17 (2.0) | - | 19 (1.8) | 32 (3.0) | © | 40 (2.8) | ( |
| Sweden | 3 (0.5) | $\checkmark>$ | 12 (1.1) | - | 24 (1.2) | $\checkmark>$ |  | 46 (2.4) | ( ${ }^{\text {c }}$ |
| Slovenia | 3 (0.5) | -- | 4 (0.7) |  | 21 (1.0) | - |  | 22 (1.3) |  |
| Italy | 3 (0.6) | 4 (0.6) | - - |  | 19 (1.5) | 21 (1.5) |  | - - |  |
| Cyprus | 1 (0.2) | $2(0.4)$ (7) | 3 (0.4) | ( 7 | 13 (0.7) | 19 (0.9) | (1) | 19 (1.0) | (7) |
| Moldova, Rep. of | 1 (0.3) | 3 (0.6) (1) | ১ $\downarrow$ |  | 13 (1.2) | 18 (1.6) | (\%) | ১ > |  |
| Macedonia, Rep. of | 1 (0.2) | $2(0.4)$ (1) | $\diamond>$ |  | 9 (1.0) | 13 (1.0) | ( | $\diamond>$ |  |
| Jordan | 1 (0.2) | 3 (0.5) (\%) | $\diamond>$ |  | 8 (1.0) | 12 (1.0) | (-) | ৪ ৪ |  |
| Indonesia | 1 (0.2) | 2 (0.3) (-) | $\checkmark>$ |  | 6 (0.7) | 8 (0.9) |  | $\checkmark>$ |  |
| Norway | 0 (0.2) | $\checkmark>$ | 4 (0.4) | - | 10 (0.6) | $\checkmark>$ |  | 26 (1.3) | ( ${ }^{\text {c }}$ |
| Iran, Islamic Rep. of | 0 (0.2) | 1 (0.2) | 0 (0.2) |  | 3 (0.4) | 6 (0.9) | (\%) | 4 (0.6) |  |
| Chile | 0 (0.1) | 1 (0.4) | $\checkmark>$ |  | 3 (0.4) | 4 (1.1) |  | $\checkmark>$ |  |
| South Africa | 0 (0.1) | 0 (0.1) | -- |  | 2 (0.6) | 1 (0.5) |  | -- |  |
| Philippines | 0 (0.1) | 0 (0.1) | $\checkmark>$ |  | 3 (0.6) | 1 (0.6) |  | $\checkmark>$ |  |
| Tunisia | 0 (0.0) | 0 (0.1) | - |  | 1 (0.3) | 5 (0.5) | ( | $\checkmark>$ |  |
| \# England | 5 (1.0) | 6 (0.8) | 6 (1.0) |  | 26 (2.8) | 25 (2.0) |  | 27 (1.5) |  |
| International Avg. | 8 (0.2) | 10 (0.2) | 11 (0.3) | $\bigcirc$ | 28 (0.3) | 31 (0.3) | (1) | 37 (0.4) | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 5 (1.5) | 7 (1.6) | $\checkmark>$ |  | 27 (3.2) | 32 (3.9) |  | ১ |  |
| Ontario Province, Can. | 6 (0.7) | 6 (0.8) | 3 (0.4) | 0 | 34 (1.8) | 32 (1.8) |  | 26 (1.7) | 0 |
| Quebec Province, Can. | 8 (1.4) | 18 (4.4) | 14 (2.8) |  | 45 (2.2) | 60 (3.5) | (\%) | 54 (4.2) |  |
|  |  |  |  |  |  | 0 |  | 2003 significantly higher |  |

\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia and Slovenia, and 1995 data are not shown for Israel, Italy, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995. Data for Latvia in this exhibit include Latvian-speaking schools only.

[^14]
## Exhibit 2.3: Trends in Percentages of Students Reaching the TIMSS 2003 International

 Benchmarks of Mathematics Achievement in 1995, 1999, and 2003| Countries | Intermediate International Benchmark (475) |  |  |  | Low International Benchmark (400) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $2003$ <br> Percent of Students | 1999 <br> Percent of Students | $1995$ <br> Percent Studen |  | 2003 <br> Percent of Students | 1999 <br> Percent of Students | 1995 Percent Studen |  |
| Singapore | 93 (1.0) | 94 (1.2) | 98 (0.4) | (7) | 99 (0.2) | 99 (0.3) | 100 (0.0) | ( 7 |
| Chinese Taipei | 85 (1.2) | 85 (1.0) | $\diamond>$ |  | 96 (0.6) | 95 (0.5) | $\diamond>$ |  |
| Korea, Rep. of | 90 (0.5) | 91 (0.5) | 89 (0.7) | 0 | 98 (0.3) | 99 (0.2) | 97 (0.4) |  |
| Hong Kong, SAR | 93 (1.3) | 92 (1.3) | 88 (2.1) |  | 98 (0.6) | 98 (0.6) | 96 (1.1) |  |
| Japan | 88 (0.6) | 90 (0.5) $\bigcirc$ | 91 (0.5) | (7) | 98 (0.2) | 98 (0.2) | $98(0.2)$ |  |
| Hungary | 75 (1.6) | 75 (1.5) | 74 (1.6) |  | 95 (0.8) | 93 (1.0) | 94 (0.9) |  |
| Netherlands | 80 (2.0) | 82 (3.4) | 78 (2.9) |  | 97 (0.8) | 96 (1.5) | 95 (1.6) |  |
| Belgium (Flemish) | 82 (1.2) | 86 (1.2) $\bigcirc$ | 85 (2.7) |  | 95 (0.9) | 97 (0.6) | 96 (1.2) |  |
| Slovak Republic | 66 (1.7) | 79 (1.7) $\bigcirc$ | 79 (1.3) | (7) | 90 (1.1) | 96 (0.6) | 96 (0.6) | (7) |
| Australia | 65 (2.3) | - - | 68 (1.7) |  | 90 (1.4) | - - | 90 (1.0) |  |
| United States | 64 (1.6) | 62 (1.8) | 61 (2.4) |  | 90 (1.0) | 87 (1.1) | 86 (1.5) | 0 |
| Russian Federation | 66 (1.8) | 73 (2.7) $\bigcirc$ | 73 (2.4) | (7) | 92 (0.9) | 93 (1.4) | 93 (1.1) |  |
| Israel | 60 (1.8) | 49 (1.9) © | - - |  | 86 (1.2) | 76 (2.0) © | - - |  |
| Malaysia | 66 (2.1) | 70 (2.1) | $\checkmark>$ |  | 93 (0.9) | 93 (0.9) | $\checkmark>$ |  |
| Lithuania | 63 (1.4) | 53 (2.3) © | 50 (2.3) | 0 | 90 (0.8) | 85 (1.8) © | 81 (1.7) | 0 |
| New Zealand | 59 (2.5) | 57 (2.5) | 64 (2.2) |  | 88 (1.7) | 84 (1.5) | 89 (1.4) |  |
| Latvia (LSS) | 66 (2.2) | 65 (1.9) | 57 (1.8) | 0 | 92 (1.1) | 91 (0.9) | 87 (1.4) | 0 |
| Romania | 52 (2.2) | 51 (2.6) | 52 (2.2) |  | 79 (1.7) | 79 (2.1) | 79 (1.6) |  |
| Scotland | 63 (2.4) | $\diamond>$ | 60 (2.6) |  | 90 (1.1) | $\diamond>$ | 87 (1.4) |  |
| Bulgaria | 51 (2.1) | 67 (2.5) 『 | 69 (2.4) | (7) | 82 (1.6) | 90 (1.2) | 90 (1.1) | (7) |
| Sweden | 64 (1.5) | $\diamond>$ | 81 (1.8) | (7) | 91 (1.0) | $\checkmark>$ | 96 (0.8) | (7) |
| Slovenia | 60 (1.3) | - - | 60 (1.8) |  | 90 (0.9) | - - | 90 (0.9) |  |
| Italy | 56 (1.7) | 53 (2.1) | - |  | 86 (1.2) | 82 (1.6) | - |  |
| Cyprus | 45 (1.0) | 53 (1.2) ( 7 | 51 (1.3) | (7) | 77 (1.0) | 82 (0.9) | 77 (1.0) |  |
| Moldova, Rep. of | 45 (2.1) | 47 (2.1) | $\diamond \diamond$ |  | 77 (1.7) | 79 (1.7) | $\diamond>$ |  |
| Macedonia, Rep. of | 34 (1.7) | 40 (1.9) $\bigcirc$ | $\diamond>$ |  | 66 (1.7) | 70 (1.8) | $\diamond \diamond$ |  |
| Jordan | 30 (1.9) | 33 (1.6) | $\diamond \diamond$ |  | 60 (1.9) | 61 (1.4) | $\diamond>$ |  |
| Indonesia | 24 (1.7) | 23 (1.4) | $\diamond>$ |  | 55 (2.4) | 50 (2.1) | $\diamond>$ |  |
| Norway | 44 (1.6) | $\diamond>$ | 64 (1.3) | ( 7 | 81 (1.2) | $\diamond>$ | 90 (0.9) | ( 7 |
| Iran, Islamic Rep. of | 20 (1.1) | 26 (1.9) 『 | 24 (1.9) | (7) | 55 (1.4) | 61 (1.6) | 59 (1.8) | (7) |
| Chile | 15 (1.2) | 16 (1.9) | $\diamond>$ |  | 41 (1.8) | 46 (1.9) | $\diamond>$ |  |
| South Africa | 6 (1.3) | 6 (1.1) | - - |  | 10 (1.8) | 13 (2.0) | - |  |
| Philippines | 14 (1.7) | 9 (1.5) © | $\diamond>$ |  | 39 (2.7) | 29 (2.5) © | $\diamond \diamond$ |  |
| Tunisia | 15 (1.1) | 34 (1.5) $\bigcirc$ | $\diamond>$ |  | 55 (1.6) | 78 (1.2) | $\diamond>$ |  |
| \# England | 61 (2.9) | 60 (2.2) | 61 (1.5) |  | 90 (1.5) | 88 (1.2) | 87 (1.0) |  |
| International Avg. | 56 (0.3) | $57(0.3) \bigcirc$ | 69 (0.4) | (7) | 80 (0.3) | 80 (0.2) | 89 (0.3) | (7) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US | 68 (2.5) | 71 (3.5) | $\diamond>$ |  | 94 (1.0) | 93 (1.4) | $\diamond>$ |  |
| Ontario Province, Can. | 75 (1.7) | 72 (1.6) | 65 (1.7) | 0 | 97 (0.5) | 96 (0.6) | 91 (1.0) | 0 |
| Quebec Province, Can. | 88 (1.1) | 93 (1.1) $\bigcirc$ | 90 (2.6) |  | 99 (0.2) | 99 (0.4) | 99 (0.5) |  |

(7) 2003 significantly lower

[^15] 2003 and 1995. Data for Latvia in this exhibit include Latvian-speaking schools only.

[^16]
## Exhibit 2.4: Trends in Percentages of Students Reaching the TIMSS 2003 International Benchmarks of Mathematics Achievement in 1995 and 2003



| Countries | Advanced International Benchmark (625) |  |  | High International Benchmark (550) |  |  | Intermediate International Benchmark (475) |  |  | Low International <br> Benchmark (400) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $2003$ <br> Percent of Students | $1995$ <br> Percent of Students |  | $2003$ <br> Percent of Students | $1995$ <br> Percent of Students |  | $2003$ <br> Percent of Students | $1995$ <br> Percent of Students |  | $2003$ <br> Percent of Students |  |  |
| Singapore | 38 (2.9) | 38 (2.2) |  | 73 (2.4) | 70 (1.6) |  | 91 (1.3) | 89 (1.0) |  | 97 (0.6) | 96 (0.4) | 0 |
| Hong Kong, SAR | 22 (1.7) | 17 (1.7) |  | 67 (2.0) | 56 (2.2) | 0 | 94 (0.7) | 87 (1.3) | 0 | 99 (0.2) | 97 (0.6) | 0 |
| Japan | 21 (0.8) | 22 (1.0) |  | 60 (1.0) | 61 (1.1) |  | 89 (0.7) | 89 (0.7) |  | 98 (0.3) | 98 (0.2) |  |
| England | 14 (1.4) | 7 (0.8) | 0 | 43 (1.8) | 24 (1.5) | 0 | 75 (1.6) | 54 (1.6) | 0 | 93 (0.8) | 82 (1.1) | 0 |
| Hungary | 10 (1.0) | 11 (1.0) |  | 41 (1.6) | 38 (1.8) |  | 76 (1.6) | 72 (1.5) | 0 | 94 (0.8) | 91 (0.9) | 0 |
| Latvia (LSS) | 9 (0.9) | 6 (1.3) |  | 43 (2.1) | 27 (2.1) | 0 | 80 (1.4) | 61 (1.9) | 0 | 96 (0.8) | 88 (1.1) | 0 |
| Cyprus | 8 (0.7) | 5 (0.6) | 0 | 34 (1.2) | 21 (1.3) | 0 | 68 (1.2) | 52 (1.5) | 0 | 89 (0.7) | 79 (1.3) | 0 |
| United States | 7 (0.7) | 9 (0.9) |  | 35 (1.3) | 37 (1.6) |  | 72 (1.2) | 71 (1.3) |  | 93 (0.5) | 92 (0.7) |  |
| Netherlands | 5 (0.8) | 12 (1.1) | (1) | 44 (1.5) | 50 (1.9) | (1) | 89 (1.2) | 87 (1.4) |  | 99 (0.4) | 99 (0.4) |  |
| Australia | 5 (0.7) | 6 (0.6) |  | 26 (1.7) | 27 (1.4) |  | 64 (1.9) | 61 (1.6) |  | 88 (1.3) | 86 (1.1) |  |
| New Zealand | 5 (0.5) | 4 (0.6) |  | 27 (1.2) | 19 (1.4) | 0 | 62 (1.3) | 51 (1.9) | 0 | 86 (1.0) | 78 (1.7) | 0 |
| Scotland | 3 (0.4) | 7 (0.9) | (7) | 22 (1.4) | 27 (1.7) | (7) | 60 (1.6) | 60 (1.9) |  | 88 (1.2) | 85 (1.2) |  |
| Slovenia | 2 (0.4) | 2 (0.4) |  | 18 (1.0) | 14 (1.1) | 0 | 55 (1.5) | 45 (2.0) | - | 84 (1.0) | 77 (1.4) | 0 |
| Norway | 1 (0.2) | 2 (0.4) | (1) | 10 (1.0) | 16 (1.2) | (1) | 41 (1.3) | 53 (2.0) | (1) | 75 (1.2) | 84 (1.2) | (1) |
| Iran, Islamic Rep. of | 0 (0.1) | 0 (0.2) |  | 2 (0.3) | 3 (0.7) |  | 17 (1.3) | 15 (1.9) |  | 45 (2.2) | 44 (2.5) |  |
| International Avg. | 10 (0.3) | 10 (0.3) |  | 36 (0.4) | 33 (0.4) | © | 69 (0.4) | 63 (0.4) | © | 88 (0.3) | 85 (0.3) | - |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Ontario Province, Can. | 5 (1.1) | 4 (0.5) |  | 29 (2.2) | 22 (1.5) | 0 | 70 (1.7) | 59 (1.9) | 0 | 94 (0.9) | 86 (1.3) | 0 |
| Quebec Province, Can. | 3 (0.4) | 13 (1.9) | ( 7 | 25 (1.5) | 50 (3.4) | ( 7 | 69 (1.4) | 87 (1.7) | (1) | 94 (0.8) | 98 (0.7) | ( |
|  |  |  |  |  |  |  |  |  |  | 0 | 2003 significantly higher |  |
|  |  |  |  |  |  |  |  |  |  | (7) | significantly lo |  |

[^17]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Grade 8: Achievement at the Advanced International Benchmark

Exhibit 2.5 describes performance at the advanced international benchmark. Eighth-grade students reaching this benchmark demonstrated the ability to organize information in problem-solving situations, make generalizations, solve non-routine problems, and draw and justify conclusions from data. They typically demonstrated success on the knowledge and skills represented by this benchmark, as well as those demonstrated at the high, intermediate, and low benchmarks.

Example Item 1 in Exhibit 2.6 illustrates the type of algebra problem an eighth-grade student performing at the advanced benchmark generally answered correctly. The eighth-grade students reaching the advanced benchmark typically were able to apply a generalization in order to solve a sequence problem like the one shown in Exhibit 2.6. More specifically, they were asked to generalize from the first of several terms of a sequence growing in two dimensions to find a specified term. The problem was presented in three parts, A, B, and C. For parts A and B, students were given a geometric pattern and then asked to indicate how many triangles would be in the $3^{\text {rd }}, 4^{\text {th }}$, and $7^{\text {th }}$ figures, respectively, if the pattern were extended. In part C , students were asked to explain a way to find the number of triangles in the $50^{\text {th }}$ figure that did not involve drawing or counting it. The achievement results are shown for part C.

To receive full credit for Part C, students had to show or explain how their answer was obtained by providing a general expression or an equation and by calculating the correct number of triangles for the $50^{\text {th }}$ figure. Internationally, this was among the most difficult items in the assessment. On average, 14 percent of the students received full credit for their responses.

Unlike students performing at lower benchmarks, students reaching the advanced benchmark typically could correctly answer multi-step word problems. Example Item 2 from the data content area presented in Exhibit 2.7 requires students to select relevant infor-
mation from a table, calculate which of the two phone plans would be less expensive for Betty, and justify their answer in terms of the monthly fee and free minutes. With an international average of 21 percent correct (for full credit), this item was a challenge for many of the eighth-grade students participating in TIMSS 2003. In no country did the majority of eighth-grade students answer the item correctly, although Japan came very close with 49 percent. In Australia, Estonia, Korea and Singapore, from 40 to 44 percent of the eighth-grade students answered the item correctly.


Advanced International Benchmark - 625

## Summary

Students can organize information, make generalizations, solve non-routine problems, and draw and justify conclusions from data. They can compute percent change and apply their knowledge of numeric and algebraic concepts and relationships to solve problems. Students can solve simultaneous linear equations and model simple situations algebraically. They can apply their knowledge of measurement and geometry in complex problem situations. They can interpret data from a variety of tables and graphs, including interpolation and extrapolation.

Students can organize information, make generalizations, and solve non-routine problems. Students can solve multi-step problems involving computations with whole numbers, decimals, and rounding. They can use the distributive property of the product to identify different representations of a number. They can compute with integers using order of operations.

Students can solve problems involving operations with proper and improper fractions, including fractions with unlike denominators. Given two points on a number line representing unspecified fractions, students can identify the point that represents their product. They can convert mixed numbers to decimal fractions. They can solve word problems involving inverse operations, decimal place value, and a fraction of a whole number of currency units. They can order integers, decimals, and common fractions.

Given a number and the ratio of two of its parts, students can find the value of one part. They can, given the dimensions of two rectangles, express the ratio of their areas. They can identify equivalent ratios and determine the ratio of two parts of a whole. They can find the percent change, given the original and final quantities, and, given the original and reduced prices, determine the percent reduction. They also can solve a multi-step non-routine problem involving percents.

Students can extend number patterns to identify the numbers common to two different arithmetic sequences and identify the row in a table whose entries are used to solve a problem. Students can make generalizations to find terms in number patterns and can explain the process used to find those terms.

They can add three simple rational expressions with unlike numerical denominators, identify the sum of three consecutive whole numbers given the middle number in general terms, and evaluate an algebraic equation by using an equivalent form and substituting given values. They can identify algebraic expressions that model situations, a diagram that models an addition of two like algebraic terms, and what the variable represents in an equation for a given situation. They can solve a pair of linear, simultaneous equations, and given a linear equation in which $y$ is expressed in terms of $x$, they can solve for $x$.

Students can apply their knowledge of measurement in complex problem situations. They can solve area problems in which they have to find the length of a side, the perimeter of a figure, the area between two rectangles when one is inside the other, and the area of a trapezoid inscribed in a rectangle. They can draw a new rectangle based on a given rectangle and find its area. They can use their knowledge of the area of a circle and of average rate to solve a problem. They can apply their knowledge of number of milliliters in a liter to solve a word problem and solve a problem that involves filling a rectangular prism with spheres. Students can combine information about lengths of segments on a line to solve a distance problem. They can solve multi-step problems involving time, distance, and speed, and can relate different units of time to solve a problem. They can use knowledge of time, clocks, and angles to solve a problem.

Students can combine knowledge of geometric figures to solve problems that involve more than one step. This knowledge involves congruent triangles, the sum of angles in a triangle, interior and exterior angles, angle bisectors, and regular hexagons. They recognize that arcs of equal radii generate an equilateral triangle. Students can select coordinates on a line in a plane given the coordinates of two other points on the line. Students can justify that a triangle is a right triangle using the Pythagorean relationship.

Students can predict outcomes from data and use their understanding of probability to draw a spinner that could have produced the data in a given table. Students can interpret data from a variety of tables and graphs, including interpolation and extrapolation. They can derive information from given timetables to complete a table for a specified journey and check that it meets given conditions. They can draw and justify conclusions based on data.

## Exhibit 2.6: TIMSS 2003 Advanced International Benchmark (625) of Mathematics Achievement - Example Item 1 (Part C)

An Item That Students Reaching the Advanced International Benchmark Are Likely to Answer Correctly*

Content Area: Algebra
Description: Part C-Generalizing from the first several terms of a sequence growing in two dimensions, explains a way to find a specified term, e.g. the 50th.

The three figures below are divided into small congruent triangles.


Figure 1


Figure 2


Figure 3
A. Complete the table below. First, fill in how many small triangles make up Figure 3. Then, find the number of small triangles that would be needed for the 4th figure if the sequence of figures is extended.

B. The sequence of figures is extended to the 7th figure. How many small triangles would be needed for Figure 7?

C. The sequence of figures is extended to the 50 th figure. Explain a way to find the number of small triangles in the 50th figure that does not involve drawing it and counting the number of triangles.

* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

than international average
han international average



## Exhibit 2.7: TIMSS 2003 Advanced International Benchmark (625) of Mathematics Achievement - Example Item 2

An Item That Students Reaching the Advanced International Benchmark Are Likely to Answer Correctly*

## Content Area: Data

Description: Interpret data from a table, draws and justifies conclusions.

Betty, Frank, and Darlene have just moved to Zedland. They each need to get phone service. They received the following information from the telephone company about the two different phone plans it offers.

They must pay a set fee each month and there are different rates for each minute they talk. These rates depend on the time of the day or night they use the phone, and on which payment plan they choose. Both plans include time for which phone calls are free. Details of the two plans are shown in the table below.


Betty talks for less than 2 hours per month. Which plan would be less expensive for her?

Less expensive plan


Explain your answer in terms of both the monthly fee and free minutes.
she talks for less than 2 hours and Plan B has less monthly fees


## Grade 8: Achievement at the High International Benchmark

Exhibit 2.8 describes performance at the high benchmark. Eighth-grade students performing at this level applied their mathematical knowledge and understanding in a wide variety of relatively complex situations. For example, they demonstrated facility with fractions in a variety of formats, as illustrated by Example Item 3 shown in Exhibit 2.9. This item required students to divide or reason with a unit fraction to solve a one-step word problem. Internationally, 38 percent of the students, on average, were able to provide a correct response. About three-fourths or more of the students in Singapore, Hong Kong SAR, Chinese Taipei, and the Netherlands answered the question correctly.

Eighth-grade students reaching the high benchmark generally were able to apply knowledge of geometric properties. In Example Item 4 in Exhibit 2.10, students needed to use their knowledge of the properties of congruent triangles to find the measure of an angle. About fourfifths or more of the students in Korea, Hong Kong SAR, Japan, and Singapore answered the item correctly. Internationally, however, just under half the eighth-grade students (46 percent, on average) did so.

# Exhibit 2.8: Description of TIMSS 2003 High International Benchmark (550) of Mathematics Achievement 

## High International Benchmark - 550

## Summary


#### Abstract

Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They can order, relate, and compute with fractions and decimals to solve word problems, operate with negative integers, and solve multi-step word problems involving proportions with whole numbers. Students can solve simple algebraic problems including evaluating expressions, solving simultaneous linear equations, and using a formula to determine the value of a variable. Students can find areas and volumes of simple geometric shapes and use knowledge of geometric properties to solve problems. They can solve probability problems and interpret data in a variety of graphs and tables.


Students can apply their understanding and knowledge in a wide variety of relatively complex situations. Students can solve word problems by determining a number between two given numbers that is divisible by only one of two other numbers, and by estimating the product of whole numbers. They can identify the prime factorization of a given number. Students can solve word problems by using the patterns in a two-column table to determine the number in the second column that corresponds to a number midway between two entries in the first column. They demonstrate understanding of the effects of operations involving negative integers by identifying the largest number produced. They can identify the number that gives a specified result when divided by a given negative integer.

Students demonstrate some facility with fractions and decimals through computation, ordering, rounding, and use in word problems. They can identify the fraction of an hour representing a given time interval and three fractions with denominators less than 10 . Students can solve one-step word problems involving division of a whole number by a unit fraction and multi-step word problems involving multiplication of whole numbers by fractions. They can select a fraction representing the comparison of parts to a whole, given each of two parts, and identify the percent equivalent of a given fraction with a denominator that is a factor of 100 . They can round four-place decimals to the nearest hundredth. They can multiply two-place decimal numbers by three-place decimal numbers without calculators.

Students can identify one proportional share of an amount divided into three unequal parts. They can solve word problems by finding the missing term in a proportion. They can select the statement that describes the effect of adding the same amount to both terms of a ratio, and can determine the simplified ratio of the shaded to unshaded parts of a shape. They can calculate the new price of an item given the percent increase in price.

Given the first several terms of a sequence in numeric and pictorial form, students can extend the sequence to find specified terms. Students can solve simple algebraic problems. They can simplify an algebraic expression by combining like terms, and can find the value of an expression involving multiplication of negative integers. Students can identify an algebraic expression that corresponds to a situation, subtract algebraic expressions with the same numeric denominators, and recognize the product of two algebraic expressions in one variable that involves exponents.

Students can solve a linear equation with parentheses, solve simple, simultaneous linear equations, and identify the quantity that satisfies two inequalities represented using a balance. They can identify the linear equation that describes the relationship between the first and second terms in a set of ordered pairs. They can use a formula to determine the value of one variable given the value of the other.

Students can compare volumes by visualizing and counting cubes, find the number of cubes needed to a fill a hole in a given shape, and calculate the volume of a rectangular prism given its net. Students can solve a variety of problems involving area. For example, they can find the perimeter of a square given its area, find the area of a rectangle enclosing two touching circles with a given radius, find the area of an irregular figure formed by rectangles, and find the area of a triangle, on the same base and with the same height as a square, when the length of a side of the square is known. From a set of times expressed variously in days, hours, minutes, and seconds, students can determine which is least. Given the start time and the duration of an event expressed as a fraction of an hour, students can determine the end time. They can solve word problems involving average speed, distance, and time.

Students can use properties of lines and angles to solve routine problems that involve supplementary, adjacent, and vertical angles and measures of angles. They can use properties of triangles to find the measure of an angle. Students can produce a drawing that meets specific angle specifications. They can identify a pair of similar triangles given the length of their sides and identify a false statement about congruent triangles. They show understanding of transformations (rotations and reflections) in a plane. They can select a center of rotation when given a figure and its image. Students can visualize a figure cut from a folded piece of paper.

Students understand elementary concepts of probability, including estimating outcomes from sample data. They can solve simple problems involving the relationship between successful and unsuccessful outcomes and probabilities. They also recognize that when outcomes are expressed as fractions of a whole, the least likely outcome corresponds to a smallest fraction. They can read and interpret data in pie graphs, line graphs, and frequency tables to solve problems. They can compare and integrate several sets of data to determine which meet given conditions.

## Exhibit 2.9: TIMSS 2003 High International Benchmark (550) of Mathematics Achievement - Example Item 3

An Item That Students Reaching the High International Benchmark Are Likely to Answer Correctly*


The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
2 National Defined Population covers less than 90\% of National Desired Population (see Exhibit A.6)

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 2.10: TIMSS 2003 High International Benchmark (550) of Mathematics Achievement - Example Item 4
An Item That Students Reaching the High International Benchmark Are Likely to Answer Correctly*



* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
2 National Defined Population covers less than 90\% of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


## Grade 8: Achievement at the Intermediate International Benchmark

Eighth-grade students at the intermediate benchmark demonstrated the ability to apply basic mathematical knowledge in straightforward situations (see Exhibit 2.11). For example, as shown by Example Item 5 in Exhibit 2.12, students showed that they could subtract a twoplace decimal number from another. The international average percent correct for this item was 61 percent. Singapore and Korea outperformed other countries with 87 to 88 percent correct.

Example Item 6 shown in Exhibit 2.13 illustrates students' emerging familiarity with algebraic representation. Internationally, on average, nearly two-thirds of the eighth-grade students were able to solve the equation for a missing number in a proportion. About threefourths or more of the students were able to do so in 13 countries up to and including 93 percent in Singapore.

## Exhibit 2.11: TIMSS 2003 Intermediate International Benchmark (475) of Mathematics Achievement



Intermediate International Benchmark - 475

## Summary

Students can apply basic mathematical knowledge in straightforward situations. They can add, subtract, or multiply to solve one-step word problems involving whole numbers and decimals. They can identify representations of common fractions and relative sizes of fractions. They understand simple algebraic relationships and solve linear equations with one variable. They demonstrate understanding of properties of triangles and basic geometric concepts including symmetry and rotation. They recognize basic notions of probability. They can read and interpret graphs, tables, maps, and scales.

Students can apply basic mathematical knowledge in straightforward situations. They can arrange four given digits in descending and ascending order to form the largest and smallest possible numbers, and find the difference between those two numbers. They can solve word problems involving addition and multiplication of two-digit whole numbers. Students can approximate the quantity remaining after an amount is reduced by a given percent. They can select the statement that describes the effect of adding the same amount to both terms of a ratio. They can use knowledge of exponent notation to select approximations to two squared whole numbers.

Students show some understanding of decimals and fractions. They can solve word problems involving addition of numbers with up to three decimal places, and subtraction with up to two decimal places. They can select a two-place decimal closest to a given whole number and round two-place decimals to whole numbers. Students can identify the decimal number that is equivalent to the sum of two fractions whose denominators are powers of 10. They can select the smallest fraction from a set of commonly used fractions and can also write a fraction less than a given fraction. They can identify a circular model of a fraction that best approximates a given rectangular model of the same fraction.

Students at this level know the meaning of simple algebraic expressions involving multiplication and addition and can identify the expression that represents a situation. They can solve linear equations with one variable. Using the properties of a balance, they can reason to find an unknown weight. Students are able to recognize and extend number patterns. Given two straight line graphs, they can select the one that models a situation described in words, and interpret the graphs and use their intersection to solve a problem.

Students can identify a value of unlabeled marks on circular and linear scales. They can solve problems by comparing distances on a map drawn to scale.

Students can use knowledge of basic geometric properties to identify corresponding parts of congruent figures and to divide an isosceles triangle into congruent triangles. They can use properties of triangles to locate points on a grid. They can relate twodimensional representations to three-dimensional objects and identify a three-dimensional figure after a rotation. Students can use the concept of line symmetry to complete geometric patterns and they can locate points in the Cartesian plane.

Students can locate and interpret data presented in bar graphs, pie graphs, and line graphs. They can construct a pie chart representing given data. Given a table of values for two variables, they can select the graph that represents the given data. They can calculate and compare averages, and have some understanding of the likelihood of an event.

* The item was answered correctly by a majority of students reaching this benchmark.
† Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 2.13: TIMSS 2003 Intermediate International Benchmark (475) of Mathematics Achievement - Example Item 6
An Item That Students Reaching the Intermediate International Benchmark Are Likely to Answer Correctly*


## Grade 8: Achievement at the Low International Benchmark

As shown in Exhibit 2.14, the very few items anchoring at the low benchmark provided evidence that students performing at this level have some basic mathematical knowledge. Essentially, however, students performing at the 400 level or lower had considerable difficulty with many of the TIMSS 2003 items. The one example item that is available for public release is presented in Exhibit 2.15. Students answering Example Item 7 demonstrated some understanding of decimal place values, by correctly selecting 9.99 as the two-place decimal closest to 10 . The international average was 77 percent correct, and 15 countries as well as three benchmarking participants had 90 percent or more of their students choosing the correct answer. In five countries - the Netherlands, Sweden, Estonia, Singapore, and Lithuania - 95 percent or more of the students gave the correct response.

## Exhibit 2.14: Description of TIMSS 2003 Low International Benchmark (400) of Mathematics Achievement

## Low International Benchmark - 400

## Summary

Students have some basic mathematical knowledge.

The few items at this level provide some evidence that students can do basic computations with whole numbers without a calculator. They can select the two-place decimal closest to a whole number. They can multiply two-place decimal numbers by three-place decimal numbers with calculators available. They recognize some basic terminology and read information from a line on a graph.

## Exhibit 2.15: TIMSS 2003 Low International Benchmark (400) of Mathematics Achievement - Example Item 7 <br> An Item That Students Reaching the Low International Benchmark Are Likely to Answer Correctly*



The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
2 National Defined Population covers less than 90\% of National Desired Population (see Exhibit A.6)

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


## Grade 4: Achievement at the Advanced International Benchmark

At the fourth grade, students reaching the advanced benchmark demonstrated that they could apply their understanding and knowledge in a wide variety of relatively complex situations (see Exhibit 2.16). In the content area of number, fourth-grade students reaching the advanced level exhibited a developing understanding of fractions and decimals and the relationship between them. For example, as illustrated by Example Item 1 in Exhibit 2.17, students at this level were able to identify " 0.7 " as the decimal representation for a fraction with a denominator of 10 . Internationally, on average, 43 percent of the fourth-grade students answered this item correctly. By far the best performance was in Singapore, where 95 percent of the students answered correctly. The next highest achievement was in Hong Kong, SAR with 78 percent answering correctly.

In measurement, fourth-grade students reaching the advanced level were able to determine the area of a figure composed of squares and half squares (see Example Item 2 in Exhibit 2.18). Further, the students had to draw the irregular figure on a grid so that it had the correct area. This was relatively difficult for the fourth-grade students in TIMSS 2003, with 29 percent answering correctly, on average, internationally. About two-thirds of the fourth-grade students in Japan and Chinese Taipei responded correctly.

## Exhibit 2.16: Description of TIMSS 2003 Advanced International Benchmark (625) of Mathematics Achievement

Advanced International Benchmark - 625

## Summary

Students can apply their understanding and knowledge in a wide variety of relatively complex situations. They demonstrate a developing understanding of fractions and decimals and the relationship between them. They can select appropriate information to solve multi-step word problems involving proportions. They can formulate or select a rule for a relationship. They show understanding of area and can use measurement concepts to solve a variety of problems. They show some understanding of rotation. They can organize, interpret, and represent data to solve problems.

Students at this level demonstrate a developing understanding of fractions and decimals and the relationship between them. They can determine the fraction of a figure that is shaded. Given a fraction, they can identify a larger fraction with a different denominator. They can use tiles to represent one half. They can identify the decimal representation of fractions with denominators of 10 and subtract a one-place decimal from a two-place decimal. They can solve simple ratio problems and problems that involve halving whole numbers and fractions. They can select appropriate information to solve multi-step word problems involving proportions.

Students can identify the number that satisfies a number sentence with two terms on each side involving addition or division. They can identify a two-step rule for a linear relationship between the first and second numbers in a set of ordered pairs and between adjacent terms in a sequence of numbers. They can formulate a rule for a multiplicative relationship between the first and second numbers in a set of ordered pairs.

Students can use their knowledge of measurement to solve problems including conversion of metric units for capacity and time units. They can solve simple problems involving distance, time, and speed and problems involving two operations. They can estimate the length of a curved line next to the middle of a ruler. Students can use maps drawn to scale to solve problems, including locating a point between two specified points and estimating distance. Students show an understanding of area in that they can determine the area of a figure composed of squares and half squares. Students also can complete an irregular figure on a grid so that it has a given area, and recognize that area does not change when a figure is cut into parts and rearranged.

Student can draw angles greater than 90 degrees. They show some understanding of rotation in a plane and in space. For example, they can identify the position of a shape after a half-turn rotation in a plane and recognize the equivalent threedimensional figure after rotation.

Students can organize, interpret, and represent data to solve problems. They can organize data and complete a tally chart to represent the data. They can solve problems that involve relating and interpreting values from two sets of data from a graph.

Exhibit 2.17: TIMSS 2003 Advanced International Benchmark (625) of
Mathematics Achievement - Example Item 1
An Item That Students Reaching the Advanced International Benchmark Are Likely to Answer Correctly*


* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.18: TIMSS 2003 Advanced International Benchmark (625) of Mathematics Achievement - Example Item 2

An Item That Students Reaching the Advanced International Benchmark Are Likely to Answer Correctly*


|  |  |  |
| :--- | :--- | :--- | :--- |
|  | Percent |  |
| Full Credit |  |  |

Country average significantly higher than international average
Country average significantly lower than international average

* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Grade 4: Achievement at the High International Benchmark

As detailed in Exhibit 2.19, fourth-grade students reaching the high benchmark were able to apply their knowledge and understanding to solve problems. For example, Exhibit 2.20 containing Example Item 3 shows that these fourth-grade students were able to select the expression that represented the situation in a word problem involving multiplication. The international average was 58 percent, with Singaporean students having the highest achievement (86\%) followed by Chinese Taipei (81\%).

In geometry, students used the simple properties of triangles and rectangles to solve problems. Example Item 4 presented in Exhibit 2.21 shows that students can compose triangles to make other shapes, including a larger triangle and a square. Students were given square tiles divided diagonally into one white and one black triangle and ask to use the tiles in answering a set a of questions. In part A, students were asked to make a large triangle and in part B to make a black square. The achievement results are presented for part B. Forty-two percent of the fourth-grade students, on average, internationally performed this task correctly. Japan had the best performance, with 71 percent correct. The next highest performance was in the Netherlands with 60 percent correct.

## Exhibit 2.19: Description of TIMSS 2003 High International Benchmark (550) of Mathematics Achievement

High International Benchmark - 550

## Summary

Student can apply their knowledge and understanding to solve problems. Student can solve multi-step word problems involving addition, multiplication, and division. They can use their understanding of place value and simple fractions to solve problems. They can identify a number sentence that represents situations. Students show understanding of threedimensional objects, how shapes can make other shapes, and simple transformation in a plane. They demonstrate a variety of measurement skills and can interpret and use data in tables and graphs to solve problems.

Students at this level can solve multi-step word problems involving addition, multiplication, and division. They can solve word problem involving division of three-digit by one-digit whole numbers. They can use their understanding of place value to solve problems. For example, they can arrange single digits to create the largest and smallest possible numbers and to create sums and differences of numbers that meet specified criteria (i.e., sum closest to a given value, largest sum, and largest difference). They can round three-digit whole numbers to the nearest hundred, select the two-place decimal closest to a given whole number, and estimate the product of two two-digit numbers.

Students can solve problems involving $1 / 2$ and $3 / 4$ and by finding a fractional part of a set of objects. They can recognize the figure illustrating a simple ratio and select appropriate information to solve a simple proportional problem.

Students can extend entries in a table according to numeric rules described in a situation. They can select an expression that represents a situation involving multiplication. They can identify a number sentence that represents a situation involving division and can identify a number that satisfies such a number sentence. Students can identify the result of a specified sequence of operations on a given number and identify the missing number in a square whose rows and columns have the same sum.

Students can calculate the volume of a rectangular solid given the volume of one layer and the number of layers. Students can locate a point on a map drawn to scale between two given distances and can read scales when the interval scale represents more than one unit (e.g., 5 units). Students can solve multi-step problems involving time and temperature. They can solve a word problem involving conversion between hours and minutes and read a thermometer to solve problems involving change in temperatures. Students can select an appropriate type of metric unit to measure weight (mass).

Students can use simple properties of triangles and rectangles to solve problems. They can compose and decompose shapes to make other simple shapes. They can identify two triangles that have the same shape but different sizes in a complex figure. Students have basic knowledge of transformations in a plane. For example, they can draw the reflection of a figure on a grid and identify a figure in which a line of symmetry is shown. Students demonstrate some familiarity with three-dimensional objects. They can identify a solid with curved and flat surfaces and recognize a net of a triangular prism.

Students can interpret and use data in tables and graphs to solve problems. They can use data from bar graphs, tally charts, and tables. They can compare data from two tables to draw conclusions. They can identify the label for a bar graph based on data in a tally chart.

## Exhibit 2.20: TIMSS 2003 High International Benchmark (550) of Mathematics Achievement - Example Item 3

An Item That Students Reaching the High International Benchmark Are Likely to Answer Correctly*

* The item was answered correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.21: TIMSS 2003 High International Benchmark (550) of Mathematics Achievement - Example Item 4 (Part B) <br> An Item That Students Reaching the High International Benchmark Are Likely to Answer Correctly*



* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Grade 4: Achievement at the Intermediate International Benchmark
Exhibit 2.22 presents the description of student achievement at the intermediate benchmark. At the intermediate benchmark, fourth-grade students could apply basic mathematical knowledge in straightforward situations. In comparison to the high benchmark, the mathematics and the problem situations were less complex.

In the number content area, students demonstrated the ability to recognize and translate between different representations of whole numbers, including number line, pictorial representations, and expanded notation. As illustrated by Example Item 5 in Exhibit 2.23, fourth-grade students reaching the intermediate benchmark recognized which figure had two-thirds shaded parts. Fifty-seven percent of the fourth-grade students, on average, internationally answered the question correctly. In Singapore, 93 percent answered correctly followed by 86 percent in Hong Kong, SAR.

In the data content area, the fourth-grade students completed a bar graph based on the solution of a word problem (see Example Item 6 in Exhibit 2.24). Indeed fourth-grade students in many of the participating countries performed this task successfully. In 15 countries and three benchmarking participants, 80 percent or more of the students answered correctly.

## Exhibit 2.22: Description of TIMSS 2003 Intermediate International Benchmark (475) of

 Mathematics Achievement
## Intermediate International Benchmark - 475

## Summary

Students can apply basic mathematical knowledge in straightforward situations. They can read, interpret, and use different representations of numbers. They can perform operations with three- and four-digit numbers and decimals. They can extend simple patterns. They are familiar with a range of two-dimensional shapes and read and interpret different representations of the same data.

Students at this level demonstrate an understanding of and can order and operate with whole numbers. They can recognize and translate between different representations of whole numbers, including number line, pictorial representations, and expanded notation. They can identify the appropriate operations to solve multiplication and division problems. They can solve problems that involve the addition of four-digit numbers, multiplication of a three-digit by a one-digit whole number, multiplication of two two-digit numbers, and division of a three-digit by a one-digit whole number. Students can add and subtract two-place decimals. They can recognize the fractional part of a set of objects or a region, can identify the fraction that represents a given part-whole situation, and select information to solve a simple proportion problem.

Students show understanding of patterns. They can generalize from the first several terms of a numeric sequence to select another number (e.g., the tenth) that is also in the sequence. They can extend sequences based on geometric patterns or patterns involving time. They can identify the next terms in an alternating number pattern involving counting forward and backward by ones. Students can identify an expression that represents a situation involving multiplication and a number sentence that represents a situation involving subtraction.

Students have some basic knowledge of area. For example, they recognize that area does not change when parts of a figure are rearranged and the inverse relationship between the size and number of units needed to cover an area. They can read a one-month calendar and use the fact that a week has seven days to solve a problem. They can select a reasonable weight, given in metric units, for an adult.

Students are familiar with a range of two-dimensional shapes. They can draw a line to divide a rectangle into two triangles and can name common geometrical shapes in a picture. They also can identify a three-dimensional object given the pictorial representation of its faces. They can locate position on a grid and describe the movement from one position to another. Students can draw a line parallel to an oblique line on a grid, and identify a pattern generated by a quarter-turn clockwise.

Students can read and interpret different representations of the same data. For example, they can match data in pie charts to tables and bar graphs. Given verbal descriptions of data or problem situations, they can use that information to complete bar graphs and a two-by-two table. They can also use information to identify the number of symbols needed to complete a pictograph when the symbol represents more than one unit.

## Exhibit 2.23: TIMSS 2003 Intermediate International Benchmark (475) of Mathematics Achievement - Example Item 5

An Item That Students Reaching the Intermediate International Benchmark Are Likely to Answer Correctly*

[^18]1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.24: TIMSS 2003 Intermediate International Benchmark (475) of Mathematics Achievement - Example Item 6

An Item That Students Reaching the Intermediate International Benchmark Are Likely to Answer Correctly*


Country average significantly higher
than international average
Country average significantly lowe than international average

* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Grade 4: Achievement at the Low International Benchmark

As can be seen from the description presented in Exhibit 2.25, fourthgrade students reaching the low benchmark have some basic mathematical knowledge. For example, they demonstrate an understanding of computation with whole numbers as shown in Exhibit 2.26. In Example Item 7, fourth-grade students were asked to multiply a two-digit whole number (15) by a one-digit whole number (9). Students in many of the participating countries and benchmarking entities answered this open-ended question correctly. The international average was 72 percent, and 90 percent or more of the fourth-graders answered correctly in Chinese Taipei, Singapore, Hong Kong SAR, and the Russian Federation.

Exhibit 2.27 contains Example Item 8 asking the fourth-grade students to draw a triangle on a grid such that the line $A B$ is the base and the two new sides are the same length as each other. Two-thirds of the fourth-grade students, on average, internationally completed this task correctly. Ninety-five percent of the students in Hong Kong, SAR did so, as did 80 to 84 percent of the fourth-graders in Latvia, Japan, and New Zealand.

## Exhibit 2.25: Description of TIMSS 2003 Low International Benchmark (400) of

 Mathematics Achievement
## Low International Benchmark - 400

## Summary

Students have some basic mathematical knowledge. Students demonstrate an understanding of whole numbers and can do simple computations with them. They demonstrate familiarity with the basic properties of triangles and rectangles. They can read information from simple bar graphs.

Students at this level demonstrate an understanding of whole numbers. They are familiar with numbers into the thousands They demonstrate understanding of place value and can translate between representations of whole numbers. They can add a four-digit and a three-digit whole number, multiply a two-digit by a one-digit whole number, and subtract two fractions with the same denominator. They can solve problems involving addition. Students can find the missing number in a number sentence involving multiplication by a one-digit whole number.

Students can compare areas by counting squares, identify two figures with the same shape, and draw a line to divide a rectangle into two rectangles. Students demonstrate familiarity with triangles. For example, they can identify two triangles with the same size and shape in a complex figure, recognize triangles in a set of polygons, and identify that a triangle has three sides. Given the base on a grid, students can draw a triangle whose other two sides are each the same length. Students can read information from simple bar graphs.

Exhibit 2.26: TIMSS 2003 Low International Benchmark (400) of Mathematics Achievement - Example Item 7
An Item That Students Reaching the Low International Benchmark Are Likely to Answer Correctly*

* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 2.27: TIMSS 2003 Low International Benchmark (400) of Mathematics Achievement - Example Item 8 <br> An Item That Students Reaching the Low International Benchmark Are Likely to Answer Correctly*



| Country | Percent Full Cred |  |
| :---: | :---: | :---: |
| ${ }^{\dagger}$ Hong Kong, SAR | 95 (0.9) | 0 |
| Latvia | 84 (1.4) | 0 |
| Japan | 80 (1.8) | 0 |
| New Zealand | 80 (1.8) | 0 |
| Singapore | 77 (1.8) | 0 |
| Russian Federation | 77 (2.3) | 0 |
| Belgium (Flemish) | 77 (1.8) | 0 |
| ${ }^{\dagger}$ Australia | 77 (2.1) | 0 |
| Italy | 77 (1.9) | 0 |
| ${ }^{1}$ Lithuania | 74 (1.9) | 0 |
| $\dagger$ England | 73 (2.1) | 0 |
| Hungary | 72 (2.0) | 0 |
| $\dagger$ Scotland | 71 (2.2) |  |
| Chinese Taipei | 70 (1.5) |  |
| Moldova, Rep. of | 67 (2.8) |  |
| International Avg. | 67 (0.4) |  |
| Slovenia | 64 (2.7) |  |
| † United States | 63 (1.4) | - |
| Norway | 58 (2.3) | $\checkmark$ |
| Cyprus | 57 (2.1) | - |
| Armenia | 56 (2.0) | ( |
| Iran, Islamic Rep. of | 48 (2.7) | ( |
| Philippines | 45 (2.7) | ( |
| Morocco | 42 (2.6) | ( |
| Tunisia | 28 (1.7) | ( |
| Benchmarking Participants |  |  |
| Indiana State, US | 64 (2.9) |  |
| Ontario Province, Can. | 76 (2.2) | 0 |
| Quebec Province, Can. | 68 (2.2) |  |

[^19]Country average significantly lower than international average than interna

* The item was answered fully correctly by a majority of students reaching this benchmark.
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## What Issues Emerge from the Benchmark Descriptions?

At both grades, the benchmark descriptions and example items strongly suggest a gradation in achievement, from the top-performing students' ability to generalize and solve non-routine or contextualized problems to the lower-performing students being able primarily to use routine, mainly numeric procedures. The fact that, even at the intermediate benchmark, students demonstrate only limited achievement in problem solving beyond straightforward one-step problems may suggest a need to reconsider the role, or priority, of problem solving in mathematics curricula.

In looking across the item-level results, it also is important to note the variation in performance across the topics covered. For example, on just the few items (15) presented in this chapter, there was a substantial range in performance for many countries. While some countries consistently registered high or low performance, and others had results consistently near the international average, a number of countries performed significantly above the international average on at least one item, and significantly below the international average on at least one item. Such results may reflect intended differences in emphasis in national curricula. It is likely, however, that such results may be unintended, and the findings will provide important information about strengths and weaknesses in intended or implemented curricula. At the very least, an in-depth examination of the TIMSS 2003 results may reveal aspects of curricula that merit further investigation.


## Chapter 3

## Average Achievement in the

 Mathematics Content AreasChapter 3 presents results by the major content areas in mathematics to provide information about the possible effects of curricular variation on average achievement. Average performance is provided for five content areas at the eighth and fourth grades: number, algebra (patterns and relationships at the fourth grade), measurement, geometry, and data. Relative achievement is shown among the content areas for each country and results are presented by gender. Trends from 1999 are shown for the eighth grade (insufficient items are available from 1995 to report trends within content areas).

The TIMSS 2003 mathematics assessments at the eighth and fourth grades were designed to allow as fair comparisons as possible among participating countries. Considerable effort was devoted to updating the mathematics framework newly published in the TIMSS Assessment Frameworks and Specifications 2003. ${ }^{1}$ IEA gratefully acknowledges the generous support of the US National Science Foundation in helping to fund this work, which took about two years, including a special international expert panel, iterative reviews by the NRCs, and a curriculum questionnaire completed by the countries. The effort focused on specifying the particular topics and subtopics to be assessed at each grade within each content area. Following on the framework

[^20]development, also with additional funding from the US National Science Foundation, an enormous, collaborative test development effort involving the participating countries occurred at both grades to reflect the framework and its new emphasis on problem solving. Nevertheless, curriculum data collected as part of TIMSS ${ }^{2}$ indicate differences in the grade level at which particular topics are introduced and in the teaching emphases given some topics. In addition, within countries there can be variation among teachers in the relative emphasis given particular topics.

The TIMSS 2003 mathematics tests for the eighth and fourth grades were designed to enable reporting by five content areas in accordance with the TIMSS mathematics framework. These areas, with their main topics, are:

## Number

1. whole numbers
2. fractions and decimals
3. integers
4. ratio, proportion, and percent.

At grade 4, integers are not included and the last topic includes only simple proportional reasoning

## Algebra

1. patterns
2. algebraic expressions
3. equations and formulas
4. relationships

At grade 4, algebraic expressions is not included.

## Measurement

1. attributes and units
2. tools, techniques, and formula

## Geometry

1. lines and angles
2. two- and three-dimensional shapes
3. congruence and similarity
4. locations and spatial relationships
5. symmetry and transformations.

## Data

1. data collection and organization
2. data representation
3. data interpretation
4. uncertainty and probability.

At grade 4, uncertainty and probability is not included.

## How Does Achievement Differ Across Mathematics Content Areas?

Exhibit 3.1 presents average achievement in each of the five mathematics content areas at the eighth grade and the fourth grade. Countries are displayed in alphabetical order, and symbols indicate whether a country's performance is statistically significantly above or below the international average. To provide a basis of comparison for the performance of each country in each content area, the international average for each content area was scaled to be 467 , the same as the overall international average.

| © Country verage significanty higher than intermational average <br> (8) Country average iginificanty lywer than intermational average | Countries | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Number |  | Algebra |  | Measurement |  | Geometry |  | Data |  |
|  | Armenia | 473 (3.1) | 0 | 489 (2.6) | 0 | 488 (3.3) | 0 | 481 (3.1) | 0 | 419 (2.7) | $\bigcirc$ |
|  | Australia | 498 (4.6) | 0 | 499 (4.4) | 0 | 511 (4.3) | 0 | 491 (4.8) | 0 | 531 (3.8) | 0 |
|  | Bahrain | 380 (1.9) | - | 411 (2.5) | - | 388 (2.1) | - | 438 (2.1) | - | 414 (2.1) | $\bigcirc$ |
|  | Belgium (Flemish) | 539 (2.7) | 0 | 523 (2.8) | 0 | 535 (2.5) | 0 | 527 (3.1) | 0 | 546 (2.9) | 0 |
|  | Botswana | 382 (2.2) | - | 377 (2.7) | - | 377 (2.0) | - | 335 (3.9) | - | 375 (2.7) | - |
|  | Bulgaria | 477 (4.1) | 0 | 481 (4.0) | 0 | 473 (4.6) |  | 484 (4.5) | 0 | 458 (3.9) | - |
|  | Chile | 390 (3.1) | - | 384 (3.1) | - | 404 (2.9) | - | 378 (3.3) | - | 412 (3.4) | - |
|  | Chinese Taipei | 585 (4.6) | 0 | 585 (4.9) | 0 | 574 (4.4) | 0 | 588 (5.1) | 0 | 568 (3.4) | 0 |
|  | Cyprus | 464 (1.5) | - | 455 (1.7) | - | 459 (2.2) | - | 457 (2.4) | - | 458 (1.7) | - |
|  | Egypt | 421 (3.0) | - | 408 (3.9) | - | 401 (3.3) | - | 408 (3.6) | - | 393 (3.2) | - |
|  | Estonia | 523 (3.1) | 0 | 528 (2.6) | 0 | 528 (3.0) | 0 | 540 (2.6) | 0 | 535 (2.8) | 0 |
|  | Ghana | 289 (5.1) | - | 288 (4.8) | - | 262 (3.7) | - | 278 (4.3) | - | 293 (4.1) | - |
|  | ${ }^{\dagger}$ Hong Kong, SAR | 586 (3.2) | 0 | 580 (3.2) | 0 | 584 (3.3) | 0 | 588 (3.6) | 0 | 566 (3.0) | 0 |
|  | Hungary | 529 (3.6) | 0 | 534 (3.1) | 0 | 525 (3.1) | 0 | 515 (3.1) | 0 | 526 (2.9) | - |
|  | ${ }^{1}$ Indonesia | 421 (4.6) | - | 418 (4.5) | - | 394 (4.9) | - | 413 (4.6) | - | 418 (4.0) | - |
|  | Iran, Islamic Rep. of | 416 (2.3) | - | 412 (3.1) | - | 399 (2.6) | - | 437 (3.1) | - | 404 (2.6) | - |
|  | ${ }^{2}$ Israel | 504 (3.3) | 0 | 498 (3.2) | 0 | 480 (3.4) | 0 | 488 (3.7) | 0 | 492 (3.3) | 0 |
|  | Italy | 480 (3.2) | 0 | 477 (3.4) | 0 | 500 (3.2) | 0 | 469 (3.5) |  | 490 (3.0) | 0 |
|  | Japan | 557 (2.3) | 0 | 568 (2.0) | 0 | 559 (2.0) | 0 | 587 (2.1) | 0 | 573 (1.9) | - |
|  | Jordan | 413 (4.4) | - | 434 (4.4) | - | 418 (4.4) | - | 446 (4.0) | - | 430 (3.5) | - |
|  | - Korea, Rep. of | 586 (2.1) | 0 | 597 (2.2) | 0 | 577 (2.0) | 0 | 598 (2.6) | 0 | 569 (2.0) | 0 |
|  | Latvia | 507 (3.2) | 0 | 508 (3.2) | 0 | 500 (3.0) | 0 | 515 (3.3) | 0 | 506 (3.8) | 0 |
|  | Lebanon | 430 (3.3) | - | 448 (3.1) | - | 430 (3.7) | - | 459 (3.0) | - | 394 (4.0) | - |
|  | ${ }^{1}$ Lithuania | 500 (2.7) | 0 | 501 (2.4) | 0 | 492 (3.0) | 0 | 506 (2.5) | 0 | 502 (2.5) | 0 |
|  | ${ }^{2}$ Macedonia, Rep. of | 438 (3.5) | - | 442 (3.6) | $\bigcirc$ | 434 (3.6) | $\bigcirc$ | 442 (3.7) | - | 419 (3.6) | $\bigcirc$ |
|  | Malaysia | 524 (4.0) | 0 | 495 (3.9) | 0 | 504 (4.5) | 0 | 495 (4.8) | 0 | 505 (3.2) | 0 |
|  | Moldova, Rep. of | 463 (3.8) |  | 464 (4.2) |  | 468 (4.0) |  | 463 (4.7) |  | 428 (3.4) | - |
|  | 1 \# Morocco | 384 (2.7) | - | 400 (2.8) | - | 376 (3.4) | $\bigcirc$ | 415 (2.3) | - | 374 (2.5) | - |
|  | ${ }^{\dagger}$ Netherlands | 539 (3.6) | 0 | 514 (4.0) | 0 | 549 (3.7) | 0 | 513 (4.1) | 0 | 560 (3.1) | 0 |
|  | New Zealand | 481 (6.0) | 0 | 490 (5.2) | 0 | 500 (4.8) | 0 | 488 (4.6) | 0 | 526 (5.1) | 0 |
|  | Norway | 456 (2.3) | - | 428 (2.7) | - | 481 (2.9) | 0 | 461 (2.8) | - | 498 (2.5) | 0 |
|  | Palestinian Nat'l Auth. | 385 (3.6) | - | 392 (3.5) | - | 386 (2.8) | - | 423 (3.1) | - | 390 (2.8) | © |
|  | Philippines | 393 (5.1) | - | 400 (5.2) | - | 372 (4.8) | - | 344 (5.3) | $\bigcirc$ | 390 (4.5) | - |
|  | Romania | 474 (4.9) |  | 480 (4.7) | 0 | 485 (4.7) | 0 | 476 (4.9) | 0 | 445 (4.6) | - |
|  | Russian Federation | 505 (4.0) | 0 | 516 (3.2) | 0 | 507 (3.9) | 0 | 515 (4.2) | 0 | 484 (3.2) | 0 |
|  | Saudi Arabia | 307 (5.3) | - | 331 (4.7) | $\bigcirc$ | 338 (3.4) | - | 382 (4.3) | ${ }^{\circ}$ | 339 (3.8) | ${ }^{(1)}$ |
|  | ${ }^{+}$Scotland | 484 (4.2) | 0 | 488 (3.9) | 0 | 508 (3.6) | 0 | 491 (3.3) | 0 | 531 (3.7) | 0 |
|  | ${ }^{1}$ Serbia | 477 (2.8) | 0 | 488 (2.5) | 0 | 475 (2.5) | 0 | 471 (3.0) |  | 456 (2.6) | - |
|  | Singapore | 618 (3.5) | 0 | 590 (3.5) | 0 | 611 (3.6) | 0 | 580 (3.7) | 0 | 579 (3.2) | 0 |
|  | Slovak Republic | 514 (3.3) | 0 | 505 (3.3) | 0 | 508 (3.7) | 0 | 501 (3.6) | 0 | 495 (2.9) | 0 |
|  | Slovenia | 498 (2.0) | 0 | 487 (2.3) | 0 | 496 (2.3) | 0 | 483 (2.5) | 0 | 494 (2.3) | 0 |
|  | South Africa | 274 (5.4) | - | 275 (5.1) | - | 298 (4.7) | - | 247 (5.4) | - | 296 (5.3) | - |
|  | Sweden | 496 (2.6) | 0 | 480 (3.0) | 0 | 512 (2.6) | 0 | 467 (3.4) |  | 539 (2.9) | 0 |
|  | Tunisia | 419 (2.3) | $\bigcirc$ | 405 (2.4) | - | 407 (2.2) | - | 427 (2.0) | © | 387 (2.2) | - |
|  | $\ddagger$ United States | 508 (3.4) | 0 | 510 (3.1) | 0 | 495 (3.2) | 0 | 472 (3.1) |  | 527 (3.2) | 0 |
|  | $\ddagger$ England | 485 (5.0) | 0 | 492 (4.5) | 0 | 505 (4.3) | 0 | 492 (4.5) | 0 | 535 (4.1) | 0 |
|  | International Avg. | 467 (0.5) |  | 467 (0.5) |  | 467 (0.5) |  | 467 (0.5) |  | 467 (0.5) |  |
|  | Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
|  | Basque Country, Spain | 490 (2.6) | 0 | 490 (2.7) | 0 | 488 (2.4) | 0 | 456 (3.2) | - | 499 (2.7) | 0 |
|  | Indiana State, US | 516 (5.8) | 0 | 510 (5.3) | 0 | 503 (5.5) | 0 | 468 (5.1) |  | 528 (4.9) | 0 |
|  | Ontario Province, Can. | 516 (3.4) | 0 | 515 (2.6) | 0 | 520 (2.8) | 0 | 513 (3.2) | 0 | 538 (2.7) | 0 |
|  | Quebec Province, Can. | 546 (3.4) | 0 | 529 (3.2) | 0 | 541 (3.6) | 0 | 542 (3.3) | 0 | 544 (2.6) | 0 |

$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9)
Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
National Desired Population does not cover all of International Desired Population (see Exhibit A.6)

2 National Defined Population covers less than 90\% of National Desired Population (see Exhibit A.6)

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number |  | Patterns and Relationships |  | Measurement |  | Geometry |  | Data |  |
| Armenia | 473 (3.0) | (1) | 461 (4.1) | ( ) | 465 (3.1) | ( | 431 (3.8) | (1) | 417 (3.6) | ( |
| ${ }^{\dagger}$ Australia | 479 (4.3) | ( | 495 (3.7) |  | 514 (3.7) | 0 | 524 (3.7) | 0 | 525 (3.6) | 0 |
| Belgium (Flemish) | 549 (1.9) | 0 | 542 (1.9) | 0 | 550 (1.4) | 0 | 533 (1.8) | 0 | 548 (2.2) | 0 |
| Chinese Taipei | 568 (1.8) | 0 | 555 (2.4) | 0 | 557 (1.6) | 0 | 553 (2.5) | 0 | 564 (2.3) | 0 |
| Cyprus | 514 (2.7) | 0 | 519 (2.4) | 0 | 506 (2.3) | 0 | 505 (2.3) | 0 | 509 (2.3) | 0 |
| $\dagger$ England | 519 (4.1) | 0 | 523 (3.9) | 0 | 535 (3.3) | 0 | 542 (3.7) | 0 | 552 (3.4) | 0 |
| ${ }^{\dagger}$ Hong Kong, SAR | 574 (3.3) | 0 | 568 (3.5) | 0 | 563 (2.7) | 0 | 557 (2.9) | 0 | 562 (2.3) | 0 |
| Hungary | 524 (2.9) | 0 | 545 (3.7) | 0 | 532 (2.7) | 0 | 514 (3.3) | 0 | 513 (3.2) | 0 |
| Iran, Islamic Rep. of | 410 (3.7) | - | 394 (3.9) | ( $\downarrow$ | 398 (3.2) | - | 416 (3.9) | - | 356 (4.4) | ( |
| Italy | 502 (3.6) | 0 | 496 (4.3) |  | 504 (3.4) | 0 | 522 (3.5) | 0 | 497 (3.0) |  |
| Japan | 556 (2.0) | 0 | 554 (1.4) | 0 | 568 (1.6) | 0 | 559 (1.9) | 0 | 593 (1.6) | 0 |
| Latvia | 531 (2.6) | 0 | 532 (3.4) | 0 | 545 (2.6) | 0 | 523 (2.2) | 0 | 526 (2.7) | 0 |
| ${ }^{1}$ Lithuania | 535 (2.9) | 0 | 531 (3.0) | 0 | 540 (2.7) | 0 | 524 (2.2) | 0 | 517 (2.5) | 0 |
| Moldova, Rep. of | 507 (4.7) | 0 | 521 (5.1) | 0 | 505 (4.0) | 0 | 501 (4.9) |  | 477 (4.3) | ( |
| Morocco | 359 (4.7) | (1) | 360 (4.7) | (1) | 345 (5.5) | - | 362 (4.9) | - | 355 (5.0) | - |
| ${ }^{+}$Netherlands | 536 (2.2) | 0 | 527 (2.4) | 0 | 545 (2.2) | 0 | 521 (3.2) | 0 | 553 (2.4) | 0 |
| New Zealand | 475 (2.3) | - | 495 (2.9) |  | 503 (2.0) | 0 | 517 (1.8) | 0 | 522 (2.0) | 0 |
| Norway | 440 (2.2) | (7) | 439 (2.7) | (1) | 475 (2.2) | ( 7 | 478 (2.2) | ( | 479 (2.3) | (7) |
| Philippines | 380 (7.4) | (1) | 382 (7.0) | (1) | 330 (7.8) | ( - | 335 (8.8) | - | 384 (7.5) | (1) |
| Russian Federation | 532 (4.6) | 0 | 531 (5.0) | 0 | 538 (3.8) | 0 | 528 (4.8) | 0 | 505 (4.1) | 0 |
| + Scotland | 475 (3.3) | - | 495 (2.9) |  | 499 (3.1) |  | 511 (2.5) | 0 | 516 (2.7) | 0 |
| Singapore | 612 (6.0) | 0 | 579 (5.4) | 0 | 566 (4.6) | 0 | 570 (5.5) | 0 | 575 (3.9) | 0 |
| Slovenia | 461 (2.7) | ( | 490 (2.7) | ( - | 497 (2.8) |  | 498 (2.2) |  | 486 (2.7) | (1) |
| Tunisia | 360 (4.1) | ( | 330 (4.7) | (-) | 308 (5.5) | ( ${ }^{\text {c }}$ | 346 (5.1) | ( | 308 (4.7) | (1) |
| † United States | 516 (2.6) | 0 | 524 (2.7) | 0 | 500 (2.1) |  | 518 (2.2) | 0 | 549 (2.0) | 0 |
| International Avg. | 495 (0.7) |  | 495 (0.7) |  | 495 (0.7) |  | 495 (0.7) |  | 495 (0.6) |  |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 531 (3.4) | 0 | 535 (3.4) | 0 | 515 (3.0) | 0 | 525 (3.5) | 0 | 557 (2.9) | 0 |
| Ontario Province, Can. | 494 (5.0) |  | 513 (3.4) | 0 | 512 (3.8) | 0 | 535 (3.8) | 0 | 544 (3.5) | 0 |
| Quebec Province, Can. | 508 (2.5) | 0 | 499 (2.6) |  | 504 (2.1) | 0 | 522 (2.3) | 0 | 506 (2.3) | 0 |

(土 Country average significantly higher than international average
(7) Country average significantly lower than international average

[^21]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

At both grades, the countries scoring highest in the overall mathematics assessments also tended to be the highest-scoring countries (though not always in the same rank order) in each of the major content areas. Correspondingly, countries scoring lowest on the overall tests tended to have low-average performance across all five content areas.

At the eighth grade, the differences in average achievement between the highest- and lowest-performing countries were greatest for geometry and measurement ( 351 and 349 scale-score points, respectively), next for number (344), then algebra (322), and least for data (286). In contrast to the consistency in performance across content areas displayed by the higher- and lower-performing countries overall, performance varied substantially for some middle-performing countries. For example, Armenia performed significantly above the international average in all the content areas except data, where, in contrast, it performed below the international average.

At the fourth grade, with fewer and less variable countries, the differences in achievement within the content areas were smaller between the highest- and lowest-performing countries. Interestingly, the largest difference by far - 285 scale-score points - was in data (which had the least difference at the eighth grade). Countries did report considerable differences in instructional emphasis given to this content area, especially at the fourth grade. For the other four content areas, the differences were 260 for measurement, 253 for number, 249 for patterns and relationships, and 245 for geometry.

In Appendix B, Exhibits B. 1 through B. 5 for the eighth grade and Exhibits B. 6 through B. 10 for the fourth grade compare average achievement among individual countries for each of the content areas, respectively. The exhibits show whether or not the differences in average achievement between pairs of countries are statistically significant.

## In Which Content Areas Are Countries Relatively Strong or Weak?

To highlight relative strengths and weaknesses within each country, Exhibit 3.2 profiles the relative average achievement in mathematics content areas within each country at the eighth and fourth grades. For each country, Exhibit 3.2 displays the difference between average performance in each content area and average performance overall. The profiles reveal that many countries performed relatively better or worse in several content areas than they did overall. At the eighth grade, for example, it can be seen that Botswana performed relatively worse in geometry than in the other four content areas. At the fourth grade, Norway performed relatively less well in number and in patterns and relationships, and relatively better in the areas of measurement, geometry, and data.

Differences in relative performance may be related to one or more of a number of factors, such as emphases in intended curricula or widely used textbooks, strengths or weaknesses in curriculum implementation, and the grade level at which topics are introduced. Differences in the match between the implemented curriculum and content measured by the test may also be a factor.

The profiles of relative performance reveal more variation across the content areas in some countries than in others. Average achievement across content areas showed considerable variation in several countries. For example, at the eighth grade, considerable variation of 60 or more scale-score points (one area at least 30 above and one 30 below) was found in Lebanon, Norway, Saudi Arabia, Sweden, and the US state of Indiana. At the fourth grade, no countries had such large differences even though several had a particular strength or weakness. On the other hand, there were only a small number of scale points of difference between highest and lowest content area means in some countries, with the best example being Cyprus at both grades. For the latter countries, the TIMSS 2003 data indicate a greater balance in mathematics content covered through the grades.

Exhibit 3.2: Profiles of Within-Country Relative Performance in Mathematics Content Areas

$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).

2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.

Exhibit 3.2: Profiles of Within-Country Relative Performance in Mathematics Content Areas
(Continued...)

$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

- Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

Exhibit 3.2: Profiles of Within-Country Relative Performance in Mathematics Content Areas
(...Continued)


[^22]Exhibit 3.2: Profiles of Within-Country Relative Performance in Mathematics Content Areas
(Continued...)

1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6). (see Exhibit A.9).

Exhibit 3.2: Profiles of Within-Country Relative Performance in Mathematics Content Areas
(...Continued)


[^23]
## What Are the Gender Differences in Achievement for the Content Areas?

Exhibit 3.3 displays average achievement in mathematics content areas by gender for the eighth and fourth grades. The most striking results at the eighth grade were the large number of significant differences favoring girls in algebra compared to those in measurement favoring boys. ${ }^{3}$ In algebra, girls had higher average achievement than boys in 22 countries and one benchmarking participant compared to the boys having higher achievement in only 3 countries. On average internationally, the girls had an advantage of 9 points. In measurement, boys had higher average achievement than the girls in 13 countries and 2 benchmarking participants compared to the girls having higher achievement in only 2 countries. The overall difference was 6 points higher for boys, on average. For each TIMSS assessment, examining item statistics to detect any gender bias is an important stage of item selection. It is therefore reasonable to assume that where significant differences do occur, they result from differences in performance rather than problem situations favoring one gender or the other. For the other three content areas, there were essentially no gender differences, on average, internationally, even though there were differences within particular countries. In number, girls performed significantly higher in 10 countries and boys in 12 countries and 2 benchmarking participants. Girls had significantly higher achievement in 8 countries in both geometry and data, whereas boys had the better performance in 13 and 9 entities, respectively.

At the fourth grade, the gender pattern was the same as the eighth grade in measurement. Boys had significantly higher achievement than girls in 12 countries and 2 benchmarking participants, whereas girls did not outperform boys in any country. The difference in achievement across countries was 5 points higher for boys. However, for patterns and relationships (the fourth grade equivalent for algebra), the results did not mirror those at eighth grade. Essentially, girls had higher achievement in 3 participating entities and so did boys. At the fourth grade, interestingly, the content area in which girls did better

3 The results for TIMSS 2003 show many more significant differences than TIMSS 1999 because a Bonferroni procedure was applied in 1999 across countries leading to extremely conservative estimates given the large number of countries.

Exhibit 3.3: Average Achievement in Mathematics Content Areas by Gender


[^24]2 National Defined Population covers less than 90\% of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 3.3: Average Achievement in Mathematics Content Areas by Gender

| Countries |  | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Geometry |  |  |  | Data |  |  |  |
|  |  | Girls |  | Boys |  | Girls |  | Boys |  |
|  | Armenia | 485 (3.4) | - | 476 (3.5) |  | $527 \text { (4.8) }$ |  | 412 (3.3) |  |
|  | Australia | 485 (5.7) |  | 497 (6.1) |  |  |  | 536 (4.3) |  |
|  | Bahrain | 453 (2.4) | - | 422 (2.8) |  | 427 (2.2) - |  | 401 (2.7) |  |
|  | Belgium (Flemish) | 522 (3.7) |  | 533 (5.0) |  | 541 (3.8) |  | 552 (4.2) | 0 |
|  | Botswana | 328 (4.9) |  | 343 (4.2) | 0 | 375 (3.6) |  | 374 (3.3) |  |
|  | Bulgaria | 483 (5.4) |  | 486 (4.8) |  | 454 (4.8) |  | 462 (5.0) |  |
|  | Chile | 369 (3.9) |  | 386 (4.6) | 0 | 405 (3.9) |  | 419 (4.1) | 0 |
|  | Chinese Taipei | 595 (5.9) | 0 | 581 (5.6) |  | 570 (3.6) |  | 566 (4.0) |  |
|  | Cyprus | 464 (3.2) | 0 | 451 (2.7) |  | 465 (2.5) | 0 | 451 (2.0) |  |
|  | Egypt | 407 (4.9) |  | 409 (5.3) |  | 393 (4.2) |  | 394 (4.7) |  |
|  | Estonia | 539 (3.0) |  | 540 (3.2) |  |  |  | 532 (3.2) |  |
|  | Ghana | 259 (6.0) |  | 293 (4.2) | 0 | $\begin{aligned} & 538 \text { (3.2) } \\ & 286 \text { (4.5) } \end{aligned}$ |  | 299 (4.6) | 0 |
|  | ${ }^{\dagger}$ Hong Kong, SAR | 587 (4.3) |  | 589 (4.8) |  | 568 (3.3) |  | 564 (4.1) |  |
|  | Hungary | 510 (4.0) |  | 521 (3.5) | 0 | 523 (3.6) |  | 528 (3.3) |  |
|  | Indonesia | 408 (4.5) |  | 419 (5.8) | 0 | $417 \text { (4.8) }$ |  | 420 (4.6) |  |
|  | Iran, Islamic Rep. of | 446 (4.8) |  | 432 (4.7) |  | 407 (4.5) |  | 403 (4.4) |  |
|  | Israel | 487 (3.8) |  | 488 (4.8) |  | 486 (3.7) |  | 497 (4.4) | 0 |
|  | Italy | 466 (3.4) |  | 472 (4.0) | 0 | 484 (3.0) |  | 496 (3.6) | 0 |
|  | Japan | 588 (3.9) |  | 585 (3.5) |  | 570 (3.4) |  | 575 (2.3) |  |
|  | Jordan | 455 (4.4) | 0 | 438 (5.8) |  | 441 (3.7) | 0 | 420 (4.7) |  |
|  | - Korea, Rep. of | 593 (3.9) |  | 601 (2.4) - |  | 564 (2.8) |  | 574 (2.7) | 0 |
|  | Latvia | 518 (3.9) |  | 512 (3.6) |  | 513 (3.7) | 0 | 500 (4.5) |  |
|  | Lebanon | 453 (3.2) |  | 467 (4.2) | 0 | 391 (5.2) |  | 398 (4.6) |  |
|  | Lithuania | 508 (3.2) |  | 505 (4.8) |  | 501 (3.2) |  | 503 (3.0) |  |
|  | ${ }^{2}$ Macedonia, Rep. of | 445 (4.2) |  | 438 (4.4) |  | 421 (4.8) |  | 416 (4.9) |  |
|  | Malaysia | 494 (6.0) |  | 495 (5.2) |  | 507 (3.8) |  | 503 (3.6) |  |
|  | Moldova, Rep. of | 467 (4.6) | 0 | 458 (5.5) |  | 431 (3.7) |  | 425 (4.2) |  |
| 1 | $\ddagger$ Morocco | 408 (3.9) |  | 423 (3.6) | 0 | 364 (3.8) |  | 384 (3.8) | 0 |
|  | $\dagger$ Netherlands | 512 (4.3) |  | 514 (5.1) |  | 556 (3.6) |  | 564 (4.0) |  |
|  | New Zealand | 490 (4.5) |  | 486 (5.8) |  | 530 (4.7) |  | 522 (6.7) |  |
|  | Norway | 463 (3.9) |  | 459 (3.7) |  | 500 (2.8) |  | 497 (3.4) |  |
|  | Palestinian Nat'l Auth. | 426 (4.2) |  | 419 (4.8) |  | 397 (3.9) | 0 | 382 (5.2) |  |
|  | Philippines | 344 (5.4) |  | 346 (6.3) |  | 395 (4.2) | 0 | 384 (5.7) |  |
|  | Romania | 474 (5.3) |  | 479 (5.5) |  | 445 (5.2) |  | 445 (4.9) |  |
|  | Russian Federation | 517 (4.2) |  | 513 (4.7) |  | 483 (3.4) |  | 485 (3.9) |  |
|  | Saudi Arabia | 381 (7.2) |  | 382 (4.9) |  | 345 (5.9) |  | 334 (5.3) |  |
|  | + Scotland | 493 (4.4) |  | 488 (3.6) |  | 533 (4.3) |  | 529 (3.9) |  |
|  | ${ }^{1}$ Serbia | 475 (3.2) | 0 | 467 (3.7) |  | 454 (3.1) |  | 458 (3.4) |  |
|  | Singapore | 584 (3.8) | 0 | 575 (4.5) |  | 581 (3.0) |  | 578 (4.0) |  |
|  | Slovak Republic | 497 (3.9) |  | 505 (4.8) |  | 488 (3.5) |  | 502 (3.9) | 0 |
|  | Slovenia | 486 (4.0) |  | 480 (3.6) |  | 495 (2.9) |  | 492 (3.0) |  |
|  | South Africa | 246 (6.0) |  | 245 (6.4) |  | 297 (6.2) |  | 294 (5.7) |  |
|  | Sweden | 469 (4.0) |  | 465 (3.3) |  | 540 (3.6) |  | 539 (3.6) |  |
|  | Tunisia | 419 (2.4) |  | 437 (2.4) | 0 | 373 (2.1) |  | 402 (3.5) | 0 |
|  | $\ddagger$ United States | 469 (3.0) |  | 475 (3.8) | 0 | 526 (3.3) |  | 527 (3.5) |  |
|  | \# England | 490 (5.6) |  | 494 (5.9) |  | 535 (4.7) |  | 535 (5.4) |  |
|  | International Avg. | 466 (0.6) |  | 467 (0.6) |  | 467 (0.5) |  | 467 (0.6) |  |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
|  | Basque Country, Spain | 457 (3.2) |  | 454 (4.2) |  | 500 (3.6) |  | 498 (3.4) |  |
|  | Indiana State, US | 462 (5.9) |  | 474 (5.5) | 0 | 526 (4.9) |  | 530 (5.8) |  |
|  | Ontario Province, Can. | 511 (3.5) |  | 514 (3.7) |  | 536 (3.1) |  | 540 (3.3) |  |
|  | Quebec Province, Can. | 538 (3.9) |  | 545 (3.7) | 0 | $541 \text { (3.0) }$ |  | 546 (3.2) |  |

- $\begin{gathered}\text { Significantly } \\ \text { higher than }\end{gathered}$ other gender
$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).

2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

- Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


| Countries | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number |  |  |  | Patterns and Relationships |  |  |  | Measurement |  |  |
|  | Girls |  | Boys |  | Girls |  | Boys |  | Girls | Boys |  |
| Armenia | 480 (3.3) | 0 | 467 (3.2) |  | 468 (4.6) | 0 | 453 (4.6) |  | 468 (3.3) | 463 (3.9) |  |
| ${ }^{\dagger}$ Australia | 476 (5.1) |  | 481 (5.0) |  | 493 (4.5) |  | 497 (4.3) |  | 510 (4.4) | 517 (4.1) |  |
| Belgium (Flemish) | 547 (2.1) |  | 550 (2.5) |  | 542 (2.7) |  | 543 (2.2) |  | 547 (1.7) | 552 (2.1) | 0 |
| Chinese Taipei | 568 (2.5) |  | 567 (2.1) |  | 555 (2.4) |  | 555 (2.9) |  | 556 (2.0) | 558 (1.9) |  |
| Cyprus | 510 (3.1) |  | 517 (3.0) | 0 | 516 (3.4) |  | 522 (2.9) |  | 498 (2.4) | 513 (3.1) | 0 |
| + England | 520 (4.4) |  | 518 (4.8) |  | 523 (4.1) |  | 524 (4.5) |  | 531 (3.5) | 539 (3.8) | 0 |
| ${ }^{\dagger}$ Hong Kong, SAR | 575 (3.5) |  | 573 (3.6) |  | 568 (4.4) |  | 568 (3.6) |  | 561 (3.0) | 564 (2.9) |  |
| Hungary | 522 (3.5) |  | 525 (3.4) |  | 550 (4.1) | 0 | 539 (4.9) |  | 527 (3.5) | 538 (2.8) | 0 |
| Iran, Islamic Rep. of | 415 (6.1) |  | 407 (5.0) |  | 402 (6.5) |  | 389 (5.3) |  | 401 (5.5) | 397 (4.3) |  |
| Italy | 499 (4.0) |  | 506 (3.7) | 0 | 496 (5.3) |  | 496 (5.3) |  | 496 (3.8) | 512 (3.8) | 0 |
| Japan | 553 (2.5) |  | 558 (2.3) |  | 551 (1.9) |  | 557 (2.0) | 0 | 567 (2.0) | 569 (2.0) |  |
| Latvia | 532 (3.1) |  | 530 (3.3) |  | 533 (3.9) |  | 530 (3.8) |  | 542 (3.1) | 548 (3.0) |  |
| ${ }^{1}$ Lithuania | 536 (3.5) |  | 536 (3.6) |  | 531 (3.5) |  | 533 (4.1) |  | 539 (2.9) | 544 (3.7) |  |
| Moldova, Rep. of | 513 (5.0) | 0 | 501 (4.8) |  | 527 (5.6) | 0 | 515 (5.3) |  | 506 (4.4) | 504 (4.3) |  |
| Morocco | 355 (6.0) |  | 363 (4.8) |  | 356 (5.9) |  | 365 (5.2) |  | 336 (6.5) | 353 (5.7) | 0 |
| $\dagger$ Netherlands | 531 (2.6) |  | 541 (2.8) | 0 | 527 (3.6) |  | 528 (2.5) |  | 540 (2.6) | 549 (2.3) | 0 |
| New Zealand | 473 (3.4) |  | 477 (2.6) |  | 496 (4.0) |  | 493 (3.7) |  | 501 (3.2) | 505 (2.1) |  |
| Norway | 437 (3.2) |  | 444 (2.4) | 0 | 439 (3.0) |  | 438 (3.0) |  | 469 (2.9) | 480 (2.9) | 0 |
| Philippines | 388 (8.9) | 0 | 372 (6.3) |  | 384 (8.2) |  | 380 (6.7) |  | 332 (9.4) | 328 (7.4) |  |
| Russian Federation | 532 (5.1) |  | 531 (4.7) |  | 531 (5.6) |  | 531 (5.3) |  | 533 (4.3) | 544 (4.0) | 0 |
| + Scotland | 471 (3.6) |  | 479 (4.5) |  | 492 (2.7) |  | 498 (4.2) |  | 492 (3.2) | 507 (3.9) | 0 |
| Singapore | 617 (5.9) | 0 | 608 (6.7) |  | 583 (5.4) |  | 575 (6.0) |  | 569 (4.5) | 564 (5.2) |  |
| Slovenia | 458 (3.4) |  | 465 (3.4) |  | 487 (3.0) |  | 493 (4.9) |  | 493 (3.1) | 501 (3.5) | 0 |
| Tunisia | 361 (4.8) |  | 360 (4.1) |  | 331 (5.4) |  | 329 (5.4) |  | 311 (6.3) | 306 (5.5) |  |
| $\dagger$ United States | 513 (2.5) |  | 520 (3.2) | 0 | 521 (2.7) |  | 526 (3.1) | 0 | 494 (2.0) | 505 (2.7) | 0 |
| International Avg. | 495 (0.8) |  | 496 (0.8) |  | 496 (0.8) |  | 495 (0.8) |  | 493 (0.8) | 498 (0.7) | $\triangle$ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 529 (3.5) |  | 532 (4.5) |  | 535 (3.4) |  | 536 (4.6) |  | 515 (3.8) | 515 (3.7) |  |
| Ontario Province, Can. | 490 (4.2) |  | 498 (6.7) |  | 508 (4.0) |  | 517 (4.3) | 0 | 506 (3.6) | 517 (4.8) | 0 |
| Quebec Province, Can. | 503 (2.9) |  | 514 (3.0) | 0 | 499 (3.5) |  | 499 (3.1) |  | 499 (2.7) | 508 (2.9) | 0 |

[^25]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 3.3: Average Achievement in Mathematics Content Areas by Gender

| Countries | Average Scale Scores for Mathematics Content Areas |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Geometry |  |  | Data |  |  |  |
|  | Girls |  | Boys | Girls |  | Boys |  |
| Armenia | 437 (3.9) | 0 | 425 (4.4) | 424 (4.0) | 0 | 411 (4.0) |  |
| ${ }^{\dagger}$ Australia | 529 (3.6) | 0 | 519 (4.9) | 529 (4.3) |  | 521 (4.7) |  |
| Belgium (Flemish) | 534 (2.0) |  | 531 (2.3) | 547 (2.8) |  | 549 (2.9) |  |
| Chinese Taipei | 554 (2.6) |  | 552 (2.7) | 568 (2.1) | 0 | 560 (3.3) |  |
| Cyprus | 506 (2.5) |  | 504 (2.7) | 506 (2.4) |  | 513 (3.1) | 0 |
| $\dagger$ England | 545 (4.4) |  | 538 (4.4) | 554 (4.3) |  | 549 (4.3) |  |
| ${ }^{\dagger}$ Hong Kong, SAR | 559 (3.8) |  | 555 (2.9) | 563 (2.6) |  | 561 (2.7) |  |
| Hungary | 515 (4.1) |  | 513 (3.7) | 515 (4.6) |  | 512 (3.8) |  |
| Iran, Islamic Rep. of | 430 (5.9) | 0 | 407 (4.7) | 360 (7.3) |  | 354 (5.4) |  |
| Italy | 523 (4.2) |  | 521 (3.4) | 495 (3.9) |  | 499 (3.5) |  |
| Japan | 562 (1.9) |  | 557 (2.7) | 595 (2.4) |  | 591 (2.4) |  |
| Latvia | 525 (2.0) | 0 | 520 (2.9) | 529 (3.2) |  | 522 (3.5) |  |
| ${ }^{1}$ Lithuania | 525 (2.7) |  | 526 (2.7) | 519 (3.3) |  | 518 (3.3) |  |
| Moldova, Rep. of | 505 (5.5) | 0 | 496 (4.8) | 483 (4.9) | 0 | 470 (4.3) |  |
| Morocco | 362 (7.3) |  | 362 (5.2) | 356 (6.2) |  | 354 (4.9) |  |
| $\dagger$ Netherlands | 522 (4.1) |  | 519 (3.1) | 552 (2.8) |  | 554 (3.1) |  |
| New Zealand | 521 (2.4) | 0 | 514 (2.5) | 524 (2.9) |  | 519 (2.9) |  |
| Norway | 482 (2.7) | 0 | 473 (2.9) | 480 (2.8) |  | 478 (3.0) |  |
| Philippines | 336 (10.6) |  | 334 (7.8) | 393 (8.8) | 0 | 374 (7.2) |  |
| Russian Federation | 528 (5.2) |  | 528 (4.9) | 502 (4.8) |  | 508 (4.3) |  |
| + Scotland | 513 (2.8) |  | 509 (3.3) | 513 (3.2) |  | 519 (3.6) |  |
| Singapore | 573 (5.4) |  | 566 (6.1) | 579 (3.8) | 0 | 571 (4.4) |  |
| Slovenia | 502 (3.1) |  | 495 (2.5) | 486 (3.6) |  | 487 (3.9) |  |
| Tunisia | 351 (6.2) |  | 342 (5.4) | 311 (5.3) |  | 305 (5.0) |  |
| † United States | 517 (2.5) |  | 519 (2.4) | 546 (1.9) |  | 551 (2.5) | 0 |
| International Avg. | 498 (0.8) | © | 493 (0.8) | 497 (0.8) | © | 494 (0.7) |  |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | 524 (3.4) |  | 526 (5.0) | 557 (4.4) |  | 558 (3.6) |  |
| Ontario Province, Can. | 532 (3.6) |  | 537 (5.2) | 542 (4.4) |  | 546 (4.5) |  |
| Quebec Province, Can. | 525 (2.1) |  | 519 (3.6) | 505 (3.0) |  | 508 (3.4) |  |

$\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
than boys across countries was geometry. The girls had higher achievement in 7 countries and the boys none. Internationally, there was a 5 -point difference favoring girls. The results were relatively similar for the genders in number ( 4 countries favoring girls and 6 entities favoring boys) and in data ( 5 countries favoring girls and 2 favoring boys). In data, however, the small difference between in the international averages was significantly higher for girls.

In some respects, the patterns in the performance of girls and boys found in TIMSS 2003 are consistent with previous IEA mathematics assessments. Girls tended to perform better than boys in algebra in both previous TIMSS assessments and the Second International Mathematics Study (SIMS), ${ }^{4}$ while boys were markedly stronger in measurement in previous studies.

## What Changes Have Occurred in Content Area Achievement?

To examine changes in achievement in the mathematics content areas, Exhibit 3.4 shows the average percent correct for eighth-grade students in 2003 and 1999 for items given in both the 2003 and 1999 TIMSS assessments. If achievement improved significantly between assessments, the 1999 result is annotated with an up arrow or down arrow. This content area trend analysis uses average percent correct rather than average scale score because there were insufficient items to reliably link the results for both assessments to the TIMSS scale in all of the five different content areas. The first column in the table shows overall trends in the average percentage correct metric. For the most part, significant differences agree with those in the overall scale score (and the direction is always consistent).

During the four years between 1999 and 2003, countries were consistent in either showing improvements or declines. No country showed statistically significant improvements in some areas while showing declines in other areas. Israel had statistically significant improvements in all five content areas. Lithuania improved in three areas. Participants improving in two areas included the Philippines,

4 Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Gregory, K.D., Garden, R.A., O'Connor, K.M., Chrostowki, S.J., and Smith, T.A. (2000), TIMSS 1999 International Mathematics Report: Findings from IEA's Repeat of the Third International Mathematics and Science Study at the Eighth Grade, Chestnut Hill: MA: Boston College. Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A. (1996), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study (TIMSS), Chestnut Hill, MA: Boston College. Robitaille D.F. (1989), "Student's Achievements: Population A" in D.F. Robitaille and R.A. Garden (eds.), The IEA Study of Mathematics II: Contexts and Outcomes of School Mathematics, New York: Pergamon Press, p. 121
the United States, and the Canadian province of Ontario. On the other hand, Bulgaria, Japan, the Slovak Republic, and Tunisia had statistically significant decreases in all five content areas. In Belgium (Flemish), Iran, and Jordan average achievement showed statistically significant decreases in four content areas. Cyprus and Malaysia showed significant decreases in three content areas, Macedonia in two areas, and the Russian Federation in one.

| Countries | Average Percent Correct for Mathematics Content Areas |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Total Mathematics Trend Items (79 items) |  |  | Number Trend Items (25 items) |  |  | Algebra Trend Items (16 items) |  |  |
|  | 2003 | 1999 |  | 2003 | 1999 |  | 2003 | 1999 |  |
| Australia | 52 (1.0) | - - |  | 53 (1.0) | - - |  | 47 (1.3) | - - |  |
| Belgium (Flemish) | 60 (0.7) | 64 (0.8) | (1) | 61 (0.8) | 64 (1.0) | ( | 52 (0.8) | 56 (1.0) | ( |
| Bulgaria | 45 (1.0) | 53 (1.5) | ( | 47 (1.0) | 54 (1.5) | ( | 43 (1.1) | 53 (1.6) | ( ) |
| Chile | 29 (0.6) | 29 (0.8) |  | 31 (0.6) | 32 (0.9) |  | 23 (0.7) | 24 (0.9) |  |
| Chinese Taipei | 69 (1.0) | 70 (0.9) |  | 70 (1.1) | 73 (0.9) |  | 66 (1.2) | 68 (1.1) |  |
| Cyprus | 43 (0.4) | 46 (0.4) | ( | 46 (0.5) | 49 (0.5) | ( - | 38 (0.6) | 40 (0.7) |  |
| Hong Kong, SAR | 70 (0.7) | 71 (1.1) |  | 69 (0.8) | 71 (1.2) |  | 68 (0.9) | 69 (1.3) |  |
| Hungary | 57 (0.9) | 59 (0.8) |  | 59 (1.0) | 60 (0.9) |  | 56 (1.0) | 57 (0.9) |  |
| Indonesia | 32 (0.8) | 34 (0.8) |  | 35 (0.9) | 36 (0.8) |  | 30 (0.8) | 32 (0.9) |  |
| Iran, Islamic Rep. of | 32 (0.5) | 35 (0.7) | ( | 36 (0.5) | 39 (0.7) | $\stackrel{\rightharpoonup}{*}$ | 29 (0.6) | 31 (0.8) | - |
| Israel | 50 (0.9) | 43 (0.9) | 0 | 52 (0.9) | 44 (0.9) | 0 | 48 (0.9) | 42 (1.1) | 0 |
| Italy | 47 (0.9) | 48 (0.9) |  | 48 (0.9) | 49 (0.9) |  | 42 (1.1) | 41 (0.9) |  |
| Japan | 66 (0.6) | 70 (0.5) | ( | 65 (0.7) | 70 (0.6) | ( - | 64 (0.7) | 69 (0.7) | ( |
| Jordan | 33 (0.8) | 36 (0.6) | ( 7 | 35 (0.8) | 38 (0.7) | ( 7 | 31 (0.9) | 33 (0.8) | ( |
| Korea, Rep. of | 72 (0.5) | 71 (0.5) |  | 73 (0.6) | 72 (0.5) |  | 71 (0.6) | 68 (0.7) | 0 |
| Latvia (LSS) | 51 (1.0) | 51 (0.8) |  | 53 (1.1) | 53 (0.9) |  | 48 (1.2) | 47 (0.9) |  |
| Lithuania | 50 (0.7) | 47 (1.0) | 0 | 51 (0.7) | 50 (1.1) |  | 46 (0.8) | 44 (1.2) |  |
| Macedonia, Rep. of | 36 (0.7) | 38 (0.8) |  | 38 (0.8) | 37 (0.9) |  | 35 (0.9) | 38 (1.0) | ( |
| Malaysia | 52 (1.1) | 56 (1.2) | ( ) | 57 (1.1) | 62 (1.2) | ( | 42 (1.0) | 46 (1.0) | ( |
| Moldova, Rep. of | 43 (0.9) | 44 (1.0) |  | 47 (1.0) | 46 (1.1) |  | 40 (1.0) | 41 (1.0) |  |
| Netherlands | 60 (1.0) | 58 (2.0) |  | 60 (1.0) | 58 (2.1) |  | 51 (1.1) | 51 (2.3) |  |
| New Zealand | 48 (1.2) | 47 (1.3) |  | 47 (1.2) | 47 (1.3) |  | 43 (1.4) | 43 (1.4) |  |
| Philippines | 27 (0.8) | 25 (0.7) | 0 | 31 (0.8) | 30 (0.8) |  | 27 (1.0) | 20 (0.9) | 0 |
| Romania | 45 (1.2) | 46 (1.3) |  | 46 (1.1) | 46 (1.4) |  | 44 (1.4) | 44 (1.5) |  |
| Russian Federation | 53 (1.0) | 55 (1.3) |  | 54 (1.1) | 57 (1.4) | - | 52 (1.0) | 54 (1.3) |  |
| Singapore | 74 (1.0) | 76 (1.4) |  | 78 (0.9) | 80 (1.2) |  | 69 (1.1) | 69 (1.6) |  |
| Slovak Republic | 52 (0.9) | 59 (1.1) | ( | 55 (1.0) | 62 (1.2) | - | 49 (1.0) | 55 (1.3) | ( ${ }^{\text {c }}$ |
| Slovenia | 50 (0.7) | -- |  | 53 (0.7) | - - |  | 45 (0.9) | - - |  |
| South Africa | 18 (0.7) | 19 (0.7) |  | 20 (0.7) | 22 (0.7) |  | 14 (0.7) | 15 (0.7) |  |
| Tunisia | 30 (0.4) | 39 (0.5) | ( | 33 (0.5) | 41 (0.5) | ( - | 26 (0.5) | 33 (0.6) | ( |
| United States | 51 (0.9) | 50 (0.9) |  | 54 (0.9) | 54 (1.0) |  | 50 (1.0) | 47 (1.0) | 0 |
| ま England | 49 (1.1) | 47 (1.1) |  | 49 (1.1) | 47 (1.1) |  | 43 (1.2) | 42 (1.2) |  |
| International Avg. | 48 (0.2) | 50 (0.2) | $\bigcirc$ | 50 (0.2) | 51 (0.2) | $\bigcirc$ | 45 (0.2) | 46 (0.2) | (1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 52 (1.3) | 52 (1.7) |  | 56 (1.4) | 56 (1.8) |  | 49 (1.3) | 49 (1.8) |  |
| Ontario Province, Can. | 55 (0.8) | 53 (0.8) |  | 55 (0.9) | 56 (1.0) |  | 51 (0.9) | 48 (0.9) |  |
| Quebec Province, Can. | 61 (0.8) | 65 (1.5) | (1) | 62 (0.9) | 65 (1.8) |  | 56 (1.0) | 60 (1.2) | ( |

* Applies only to items that appeared on both the 1999 and 2003 assessments. Fourth grade data are not available.
ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
rend notes: Because of differences in population coverage, 1999 data are not shown for Australia and
Slovenia. Korea tested later in 2003 than in 1999, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003. Data for Latvia in this exhibit include Latvian-speaking schools only.

[^26]A dash ( - ) indicates comparable data are not available.

Exhibit 3.4: Trends in Average Percent Correct in Mathematics Content Areas*

| Countries | Average Percent Correct for Mathematics Content Areas |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Measurement Trend Items (16 items) |  |  | Geometry Trend Items (12 items) |  |  | Data Trend Items (10 items) |  |  |
|  | 2003 | 1999 |  | 2003 | 1999 |  | 2003 | 1999 |  |
| Australia | 47 (1.2) | - |  | 50 (1.1) | - - |  | 71 (1.1) | - - |  |
| Belgium (Flemish) | 54 (0.8) | 60 (0.8) | (\%) | 61 (0.9) | 64 (1.0) | (1) | 79 (0.7) | 81 (0.8) |  |
| Bulgaria | 35 (1.2) | 45 (1.5) | (\%) | 50 (0.9) | 58 (1.6) | - | 58 (1.1) | 62 (1.6) | © |
| Chile | 21 (0.6) | 19 (0.8) |  | 30 (0.7) | 32 (0.9) |  | 44 (1.0) | 45 (1.0) |  |
| Chinese Taipei | 61 (1.1) | 64 (1.0) |  | 71 (1.0) | 72 (0.9) |  | 79 (0.8) | 80 (0.7) |  |
| Cyprus | 34 (0.6) | 40 (0.6) | © | 45 (0.5) | 47 (0.6) | $\checkmark$ | 61 (0.7) | 61 (1.0) |  |
| Hong Kong, SAR | 66 (0.9) | 66 (1.2) |  | 73 (0.8) | 72 (1.1) |  | 76 (0.6) | 78 (0.9) |  |
| Hungary | 51 (1.0) | 53 (1.0) |  | 55 (1.0) | 55 (1.1) |  | 69 (1.0) | 71 (0.9) |  |
| Indonesia | 21 (0.8) | 22 (0.8) |  | 36 (0.8) | 37 (1.0) |  | 47 (1.1) | 47 (1.1) |  |
| Iran, Islamic Rep. of | 20 (0.5) | 22 (0.8) |  | 36 (0.6) | 39 (0.8) | (7) | 46 (0.8) | 49 (1.0) | (1) |
| Israel | 39 (0.9) | 32 (0.9) | 0 | 51 (1.1) | 44 (0.9) | 0 | 65 (1.1) | 59 (1.1) | 0 |
| Italy | 43 (1.0) | 44 (1.0) |  | 46 (1.0) | 47 (1.0) |  | 64 (0.9) | 64 (1.2) |  |
| Japan | 58 (0.7) | 63 (0.7) | (\%) | 74 (0.6) | 75 (0.6) | ( | 76 (0.5) | 79 (0.5) | ( ) |
| Jordan | 23 (0.8) | 27 (0.8) | (\%) | 37 (0.8) | 41 (0.7) | (\%) | 46 (1.1) | 49 (0.7) |  |
| Korea, Rep. of | 63 (0.7) | 64 (0.6) |  | 75 (0.6) | 74 (0.6) |  | 80 (0.4) | 82 (0.4) | ( ) |
| Latvia (LSS) | 38 (1.0) | 40 (1.1) |  | 57 (1.2) | 59 (1.0) |  | 67 (1.4) | 63 (1.0) | 0 |
| Lithuania | 38 (0.8) | 34 (1.2) | 0 | 54 (0.8) | 49 (1.3) | 0 | 68 (0.8) | 64 (1.2) | 0 |
| Macedonia, Rep. of | 27 (0.9) | 29 (1.0) |  | 39 (0.7) | 42 (1.0) | - | 49 (1.0) | 48 (1.0) |  |
| Malaysia | 45 (1.3) | 51 (1.4) | ( ) | 51 (1.2) | 53 (1.3) |  | 67 (1.0) | 68 (1.0) |  |
| Moldova, Rep. of | 36 (1.1) | 37 (1.3) |  | 46 (1.3) | 47 (1.2) |  | 49 (1.0) | 50 (1.1) |  |
| Netherlands | 58 (1.2) | 56 (2.0) |  | 57 (1.2) | 58 (1.7) |  | 79 (1.0) | 75 (2.4) |  |
| New Zealand | 42 (1.5) | 42 (1.5) |  | 49 (1.3) | 48 (1.3) |  | 66 (1.4) | 65 (1.4) |  |
| Philippines | 18 (0.8) | 15 (0.6) | 0 | 25 (0.7) | 25 (0.8) |  | 40 (0.9) | 39 (0.9) |  |
| Romania | 39 (1.4) | 40 (1.4) |  | 45 (1.3) | 48 (1.3) |  | 55 (1.4) | 54 (1.3) |  |
| Russian Federation | 44 (1.2) | 47 (1.6) |  | 56 (1.1) | 58 (1.5) |  | 64 (1.2) | 65 (1.3) |  |
| Singapore | 74 (1.1) | 76 (1.6) |  | 71 (1.1) | 73 (1.6) |  | 79 (0.8) | 81 (1.2) |  |
| Slovak Republic | 44 (1.1) | 53 (1.5) | (\%) | 53 (1.0) | 61 (1.2) | ( ) | 64 (1.0) | 71 (1.1) | (1) |
| Slovenia | 42 (0.9) | - - |  | 50 (0.9) | - - |  | 67 (0.9) | - - |  |
| South Africa | 12 (0.7) | 13 (0.6) |  | 19 (0.8) | 21 (0.8) |  | 29 (1.1) | 30 (0.9) |  |
| Tunisia | 20 (0.5) | 32 (0.7) | (1) | 34 (0.6) | 46 (0.6) | ( | 39 (0.6) | 52 (0.7) | ( |
| United States | 42 (1.0) | 40 (1.1) |  | 45 (0.9) | 44 (1.0) |  | 72 (0.8) | 68 (0.9) | 0 |
| 泰 England | 45 (1.3) | 43 (1.3) |  | 50 (1.3) | 47 (1.3) | 0 | 69 (1.3) | 66 (1.4) |  |
| International Avg. | 41 (0.2) | 42 (0.2) | (1) | 50 (0.2) | 51 (0.2) | $\bigcirc$ | 62 (0.2) | 62 (0.2) |  |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 42 (1.7) | 43 (2.0) |  | 44 (1.7) | 44 (1.9) |  | 72 (1.3) | 72 (1.9) |  |
| Ontario Province, Can. | 47 (0.9) | 45 (1.1) |  | 56 (1.1) | 52 (1.0) | 0 | 75 (0.8) | 71 (0.9) | 0 |
| Quebec Province, Can. | 54 (1.1) | 60 (2.0) | (1) | 64 (0.9) | 68 (2.0) |  | 74 (0.6) | 77 (1.4) | (1) |

* Applies only to items that appeared on both the 1999 and 2003 assessments. Fourth grade data are not available.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
rend notes: Because of differences in population coverage, 1999 data are not shown for Australia and Slovenia. Korea tested later in 2003 than in 1999, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003. Data for Latvia in this exhibit include Latvian-speaking schools only
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates comparable data are not available.



## Chapter 4

## Students' Backgrounds and Attitudes Towards Mathematics

With its overarching goal of improving student learning in mathematics and science, TIMSS focuses primarily on curricular, instructional, and school resource factors in presenting information on the context in which learning takes place. However, as documented extensively by previous IEA studies of mathematics achievement, ${ }^{1}$ student achievement also is related to home background factors, and to students' activities and attitudes. Since information on such factors is indispensable for interpreting the achievement results, this chapter provides detailed information about students' home backgrounds and resources for learning, how they spend their time out of school, their self-confidence in learning mathematics, and the value they place on mathematics. Also provided is information on trends in attitudes to learning mathematics across 1995, 1999, and 2003.

## What Educational Resources Do Students Have in Their Homes?

IEA's ongoing assessments of student achievement in mathematics and science (TIMSS) and reading literacy (PIRLS) have shown that in almost every country students from homes with extensive educational resources have higher achievement in mathematics and other subjects

1 For results from TIMSS 1999, see Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Gregory, K.D., Garden, R.A., O’Connor, K.M., Chrostowski, S.J., and Smith, T.A., (2000), TIMSS 1999 International Mathematics Report: Findings from IEA's Repeat of the Third International Mathematics and Science Study at the Eighth Grade, Chestnut Hill, MA: Boston College. For TIMSS 1995 results, see Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A.(1996), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study, Chestnut Hill, MA: Boston College;
than those from less advantaged backgrounds. For the 2003 data presented in this report, TIMSS has focused on just a few central variables: level of parental education, students' educational aspirations, speaking the language of the test at home, having a range of study aids in the home, and computer use at home and at school.

Because for most children, parents are their first and probably most important educators, the level of education of the parents may be the most important educational resource in the home. Exhibit 4.1 summarizes eighth-grade students' reports of the highest level of education attained by their parents. Ordered alphabetically by country, this two-page display shows the percentages of students in each of five categories of parents' educational level, together with their average mathematics achievement. Standard errors for percentages and averages also are shown. The education level of the parent with most education was used in assigning students to categories.

Although response rates to questions in the TIMSS questionnaires generally were high, students in some countries had difficulty in answering specific questions, particularly those about their parents' level of education. The exhibits in this chapter have special notations on this point. For a country where responses are available for at least 70 but less than 85 percent of the students, an " $r$ " is included next to its data. Where responses are available for at least 50 but less than 70 percent of the students, an " $s$ " is included. Where responses are available for less than 50 percent, an " $x$ " replaces the data.

Exhibit 4.1 reveals great diversity in levels of parental education within and across the TIMSS countries. On average across countries, the percentages of eighth-grade students reporting that the highest level of education attained by either parent was as follows: finished university - $28 \%$; finished post-secondary education but not university - 17\%; finished upper secondary - $28 \%$; finished lower secondary - $15 \%$; and no more than primary (includes not attending school at all) $-12 \%$. Countries with the highest percentages ( $40 \%$ or more) of students reporting university-educated parents included Armenia, Estonia,

Israel, Japan, Latvia, Norway, the Russian Federation, Sweden, and the United States. Among benchmarking participants, Indiana and Ontario were included. In contrast, countries reporting the highest percentages $(40 \%$ or more) of parents with no more than primary education included Botswana, Iran, Morocco, Saudi Arabia, and Tunisia.

The different educational approaches, structures, and organizations across the TIMSS countries make comparisons of educational levels difficult, and this is exacerbated by high levels of 'do not know' and missing responses in some countries. Nonetheless, Exhibit 4.1 makes it clear that higher levels of parents' education are associated with higher eighth-grade student achievement in mathematics in almost all countries. At 503 score points, the average mathematics achievement of students with university-educated parents was more than 90 points greater than the average of students whose parents had no more than primary education.

As shown in Exhibit 4.2, students generally had high expectations for university education, particularly those who had a parent with a university education. More than half the eighth-grade students (54\% on average across countries) reported that they expect to finish university, 30 percent do not expect to complete a university education, and a further 15 percent do not know. Students expecting to finish university had substantially greater average mathematics achievement than those without university expectations. Among those expecting to finish university, the average achievement of those students with a parent who finished university ( $21 \%$ of students) was 30 points greater than those without a university-educated parent ( $33 \%$ ).

Although speaking more than one language has advantages, TIMSS 1999 showed that, with some exceptions, countries with large proportions of students from homes where the language of the test (and consequently the language of instruction) is not often spoken had lower average mathematics achievement at eighth grade than those who spoke it more often. Exhibit 4.3, which presents students' reports of how frequently they spoke the language of the TIMSS test at home

| Countries |  | Finished University or Equivalent or Higher |  | Finished Post-secondary Vocational/Technical Education but Not University |  | Finished Upper Secondary Schooling |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia |  | 51 (1.5) | 492 (3.6) | 22 (0.9) | 473 (4.4) | 24 (1.1) | 467 (4.0) |
| Australia | $r$ | 29 (1.3) | 543 (5.6) | 27 (1.0) | 517 (5.8) | 25 (1.1) | 493 (6.1) |
| Bahrain |  | 33 (0.7) | 427 (2.5) | 7 (0.5) | 410 (5.7) | 23 (0.6) | 409 (2.9) |
| Belgium (Flemish) | s | 25 (1.4) | 568 (3.9) | 26 (1.0) | 565 (3.0) | 31 (1.1) | 535 (3.5) |
| Botswana |  | 10 (0.7) | 411 (7.1) | 14 (0.6) | 378 (4.0) | 16 (0.8) | 361 (3.5) |
| Bulgaria |  | 28 (1.3) | 516 (6.2) | 36 (1.4) | 475 (4.7) | 29 (1.4) | 457 (5.3) |
| Chile |  | 16 (1.0) | 465 (4.7) | 10 (0.5) | 418 (5.5) | 32 (1.1) | 391 (3.7) |
| Chinese Taipei |  | 17 (1.4) | 643 (5.1) | 11 (0.6) | 618 (5.3) | 46 (1.0) | 583 (4.3) |
| Cyprus |  | 28 (0.8) | 486 (2.6) | 14 (0.7) | 475 (3.0) | 36 (0.9) | 459 (2.8) |
| Egypt |  | 24 (1.1) | 464 (4.5) | 0 (0.0) | ~ | 11 (0.6) | 433 (5.7) |
| Estonia |  | 40 (1.4) | 555 (3.4) | 39 (1.1) | 525 (3.3) | 19 (0.7) | 512 (3.8) |
| Ghana |  | 10 (0.7) | 320 (8.1) | 17 (0.9) | 296 (6.7) | 22 (1.0) | 292 (5.8) |
| Hong Kong, SAR |  | 12 (1.0) | 612 (7.0) | 12 (0.5) | 598 (5.2) | 36 (0.9) | 587 (3.0) |
| Hungary | $r$ | 37 (1.6) | 573 (3.4) | 0 (0.0) | ~ | 49 (1.6) | 515 (3.0) |
| Indonesia |  | 9 (0.9) | 457 (8.4) | 6 (0.5) | 433 (7.7) | 24 (1.1) | 422 (5.9) |
| Iran, Islamic Rep. of |  | 10 (0.8) | 456 (6.6) | 10 (0.7) | 429 (5.2) | 15 (0.8) | 434 (4.2) |
| Israel | $r$ | 45 (1.3) | 531 (3.7) | 24 (0.9) | 493 (4.0) | 18 (0.9) | 474 (4.9) |
| Italy |  | 21 (1.3) | 509 (5.6) | 5 (0.4) | 500 (6.4) | 40 (0.9) | 495 (3.1) |
| Japan | $r$ | 45 (1.4) | 601 (2.9) | 18 (0.7) | 569 (3.8) | 36 (1.1) | 548 (2.5) |
| Jordan |  | 35 (1.8) | 458 (6.8) | 15 (0.8) | 439 (4.8) | 30 (1.0) | 419 (3.3) |
| Korea, Rep. of |  | 35 (1.2) | 619 (3.0) | 15 (0.6) | 589 (3.6) | 41 (1.0) | 580 (2.2) |
| Latvia | $r$ | 43 (1.8) | 532 (4.0) | 0 (0.0) | ~ | 34 (1.4) | 512 (4.2) |
| Lebanon |  | 19 (1.2) | 465 (4.8) | 21 (1.0) | 448 (4.5) | 19 (0.7) | 436 (4.4) |
| Lithuania | $r$ | 36 (1.6) | 538 (2.9) | 31 (1.0) | 502 (3.2) | 30 (1.3) | 473 (3.3) |
| Macedonia, Rep. of |  | 22 (1.3) | 479 (5.4) | 19 (0.9) | 459 (3.9) | 43 (1.2) | 435 (3.6) |
| Malaysia |  | 11 (0.9) | 544 (7.4) | 20 (0.9) | 522 (4.9) | 27 (0.9) | 519 (4.6) |
| Moldova, Rep. of |  | 34 (1.4) | 485 (4.0) | 18 (1.0) | 463 (5.5) | 21 (1.1) | 457 (5.1) |
| Morocco | $r$ | 16 (1.3) | 406 (4.8) | 0 (0.0) | $\sim \sim$ | 17 (0.8) | 398 (5.3) |
| Netherlands | r | 22 (1.6) | 569 (5.7) | 32 (1.3) | 563 (4.2) | 43 (1.9) | 526 (4.3) |
| New Zealand | s | 28 (1.9) | 535 (8.0) | 30 (1.5) | 502 (6.3) | 34 (1.9) | 492 (5.3) |
| Norway | s | 66 (1.4) | 485 (2.6) | 16 (1.0) | 459 (5.7) | 12 (0.9) | 451 (4.9) |
| Palestinian Nat'l Auth. |  | 27 (0.9) | 426 (4.5) | 12 (0.5) | 401 (6.1) | 36 (0.8) | 396 (3.3) |
| Philippines |  | 19 (1.2) | 425 (8.5) | 22 (0.8) | 394 (5.4) | 33 (0.9) | 372 (5.8) |
| Romania |  | 17 (1.8) | 533 (5.7) | 16 (1.0) | 493 (5.8) | 47 (1.5) | 479 (4.2) |
| Russian Federation |  | 44 (2.3) | 530 (3.6) | 26 (1.5) | 513 (3.7) | 24 (1.2) | 484 (4.8) |
| Saudi Arabia |  | 27 (1.9) | 363 (6.3) | 0 (0.0) | ~ | 12 (0.5) | 339 (7.6) |
| Scotland |  | x x | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x |
| Serbia |  | 20 (1.2) | 529 (4.0) | 68 (1.2) | 475 (2.4) | 2 (0.2) | ~ ~ |
| Singapore | $r$ | 16 (0.6) | 651 (3.3) | 4 (0.3) | 624 (5.9) | 21 (0.8) | 621 (3.6) |
| Slovak Republic | $r$ | 34 (1.9) | 549 (3.8) | 0 (0.0) | (5.9) | 65 (1.9) | 502 (3.4) |
| Slovenia | $r$ | 26 (1.3) | 522 (3.5) | 31 (0.8) | 498 (2.9) | 34 (1.1) | 486 (3.5) |
| South Africa | r | 11 (1.0) | 352 (16.6) | 13 (0.7) | 294 (10.0) | 30 (0.9) | 266 (6.0) |
| Sweden | s | 48 (1.8) | 525 (3.5) | 18 (1.1) | 513 (3.9) | 22 (1.3) | 489 (4.6) |
| Tunisia |  | 11 (0.9) | 437 (5.8) | 12 (0.8) | 437 (4.1) | 16 (0.6) | 419 (3.7) |
| United States | $r$ | 56 (1.3) | 530 (3.6) | 9 (0.4) | 495 (3.6) | 26 (0.9) | 488 (3.0) |
| $\ddagger$ England |  | x x | x x | $\mathrm{x} \times$ | x x | x x | x x |
| International Avg. |  | 28 (0.2) | 503 (0.9) | 17 (0.1) | 480 (0.9) | 28 (0.2) | 463 (0.7) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 34 (2.1) | 508 (4.0) | 14 (1.1) | 492 (4.2) | 21 (1.1) | 482 (4.1) |
| Indiana State, US | $r$ | 46 (2.1) | 529 (7.4) | 10 (0.8) | 505 (4.6) | 33 (1.3) | 505 (5.4) |
| Ontario Province, Can. | s | 46 (2.3) | 552 (3.8) | 37 (1.6) | 517 (3.2) | 13 (1.1) | 510 (4.8) |
| Quebec Province, Can. | r | 33 (1.6) | 562 (4.7) | 34 (0.9) | 547 (4.0) | 21 (1.1) | 529 (2.7) |

Background data provided by students.

* Based on countries' categorizations to UNESCO's International Standard Classification of Education (Operational Manual for ISCED-1997).
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. $A n$ " $x$ " indicates data are available for less than $50 \%$ of the students.

Exhibit 4.1: Highest Level of Education of Either Parent*

| Countries |  | Finished Lower Secondary Schooling |  | No More Than Primary Schooling |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia |  | 2 (0.4) | ~ | 1 (0.2) | ~ ~ |
| Australia | r | 15 (0.9) | 482 (5.2) | 3 (0.4) | 429 (13.3) |
| Bahrain |  | 20 (0.7) | 387 (3.6) | 17 (0.7) | 385 (3.5) |
| Belgium (Flemish) | s | 11 (0.7) | 524 (5.8) | 6 (0.7) | 462 (12.7) |
| Botswana |  | 20 (0.8) | 366 (3.1) | 41 (1.2) | 356 (3.0) |
| Bulgaria |  | 6 (0.7) | 443 (11.5) | 2 (0.4) | ~ |
| Chile |  | 31 (1.0) | 354 (3.2) | 11 (0.9) | 334 (5.3) |
| Chinese Taipei |  | 21 (1.1) | 553 (5.6) | 6 (0.5) | 537 (7.8) |
| Cyprus |  | 15 (0.7) | 430 (4.0) | 7 (0.4) | 412 (6.1) |
| Egypt |  | 29 (0.9) | 398 (4.0) | 36 (1.4) | 387 (3.7) |
| Estonia |  | 2 (0.3) | ~ | 0 (0.1) | ~ ~ |
| Ghana |  | 37 (1.2) | 261 (5.7) | 14 (1.0) | 246 (5.5) |
| Hong Kong, SAR |  | 25 (0.8) | 586 (3.5) | 15 (0.7) | 578 (5.0) |
| Hungary | $r$ | 14 (1.3) | 473 (7.2) | 0 (0.1) | ~ ~ |
| Indonesia |  | 22 (0.9) | 392 (7.5) | 39 (1.6) | 406 (5.1) |
| Iran, Islamic Rep. of |  | 22 (0.8) | 408 (2.8) | 43 (1.6) | 395 (2.6) |
| Israel | $r$ | 8 (0.6) | 457 (7.9) | 5 (0.6) | 455 (11.1) |
| Italy |  | 30 (1.1) | 459 (4.1) | 5 (0.4) | 425 (6.5) |
| Japan | $r$ | 2 (0.3) | ~~ | 0 (0.0) | ~~ |
| Jordan |  | 12 (0.9) | 403 (5.9) | 8 (0.6) | 377 (5.7) |
| Korea, Rep. of |  | 6 (0.4) | 551 (4.9) | 3 (0.4) | 516 (9.8) |
| Latvia | $r$ | 23 (1.1) | 502 (4.5) | 0 (0.1) | ~~ |
| Lebanon |  | 15 (0.8) | 418 (4.6) | 26 (1.7) | 405 (3.9) |
| Lithuania | $r$ | 2 (0.3) | ~ ~ | 1 (0.2) | ~ |
| Macedonia, Rep. of |  | 11 (0.8) | 384 (5.9) | 5 (0.6) | 367 (12.6) |
| Malaysia |  | 24 (1.0) | 496 (4.9) | 18 (1.0) | 485 (5.0) |
| Moldova, Rep. of |  | 17 (0.9) | 450 (7.2) | 10 (0.8) | 420 (8.3) |
| Morocco | $r$ | 17 (1.1) | 372 (5.6) | 50 (1.7) | 385 (3.0) |
| Netherlands | r | 0 (0.0) | ~ | 3 (0.4) | 502 (11.2) |
| New Zealand | s | 5 (0.7) | 475 (10.8) | 2 (0.4) | ~~ |
| Norway | 5 | 4 (0.5) | 419 (9.4) | 2 (0.3) | ~ ~ |
| Palestinian Nat'l Auth. |  | 18 (0.8) | 368 (4.2) | 6 (0.5) | 339 (6.3) |
| Philippines |  | 13 (0.5) | 348 (6.1) | 14 (0.9) | 339 (5.3) |
| Romania |  | 13 (1.6) | 465 (9.8) | 7 (0.8) | 392 (9.5) |
| Russian Federation |  | 6 (0.5) | 471 (8.4) | 0 (0.1) | ~ ~ |
| Saudi Arabia |  | 19 (1.7) | 322 (6.2) | 41 (1.7) | 320 (4.3) |
| Scotland |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x |
| Serbia |  | 9 (0.9) | 425 (6.0) | 1 (0.2) | ~ ~ |
| Singapore | r | 48 (0.8) | 600 (3.9) | 11 (0.5) | 571 (6.0) |
| Slovak Republic | $r$ | 1 (0.3) | ~ | 0 (0.1) | ~~ |
| Slovenia | $r$ | 8 (0.7) | 458 (5.5) | 1 (0.2) | $\sim$ |
| South Africa | r | 18 (0.7) | 244 (4.0) | 28 (1.1) | 223 (4.4) |
| Sweden | s | 9 (0.8) | 478 (6.0) | 3 (0.5) | 441 (11.8) |
| Tunisia |  | 17 (0.7) | 406 (2.8) | 44 (1.5) | 397 (2.4) |
| United States | $r$ | 6 (0.4) | 457 (5.6) | 3 (0.3) | 436 (7.5) |
| \# England |  | $\mathrm{x} \times$ | x x | $\mathrm{x} \times$ | x x |
| International Avg. |  | 15 (0.1) | 434 (1.1) | 12 (0.1) | 410 (1.4) |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain |  | 20 (1.5) | 475 (3.6) | 11 (0.8) | 457 (5.7) |
| Indiana State, US | r | 7 (0.9) | 470 (8.0) | 4 (0.5) | 487 (15.0) |
| Ontario Province, Can. | s | 3 (0.5) | 511 (9.6) | 2 (0.4) | ~ ~ |
| Quebec Province, Can. |  | 10 (0.7) | 527 (3.8) | 1 (0.3) | ~ ~ |

[^27]A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

| Countries |  | Finish University and Either Parent Went to University or Equivalent |  | Finish University but Neither Parent Went to University or Equivalent |  | Not Finish University Regardless of Parents' Education |  | Do Not Know Regardless of Parents' Education |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | r | 36 (1.5) | 510 (3.5) | 18 (0.9) | 492 (4.0) | 37 (1.5) | 456 (4.2) | 9 (0.5) | 471 (5.7) |
| Australia | s | 22 (1.3) | 555 (6.2) | 22 (1.0) | 537 (6.3) | 45 (1.4) | 483 (4.4) | 11 (0.7) | 506 (6.4) |
| Bahrain |  | 28 (0.7) | 440 (2.4) | 39 (0.8) | 420 (2.5) | 16 (0.7) | 357 (4.2) | 16 (0.6) | 379 (4.1) |
| Belgium (Flemish) | s | 16 (1.2) | 583 (4.0) | 17 (0.9) | 578 (3.3) | 46 (1.6) | 528 (3.4) | 21 (0.8) | 530 (4.8) |
| Botswana |  | 8 (0.6) | 424 (6.4) | 36 (0.9) | 395 (2.8) | 45 (1.0) | 344 (3.1) | 12 (0.6) | 340 (5.7) |
| Bulgaria |  | 23 (1.3) | 527 (6.3) | 28 (1.1) | 490 (4.6) | 37 (1.7) | 445 (5.8) | 12 (0.9) | 462 (5.6) |
| Chile |  | 15 (1.0) | 473 (4.5) | 43 (1.1) | 397 (3.9) | 36 (1.0) | 350 (3.3) | 7 (0.4) | 350 (6.8) |
| Chinese Taipei |  | 15 (1.3) | 650 (5.0) | 56 (1.0) | 607 (3.4) | 16 (0.9) | 500 (4.8) | 14 (0.6) | 543 (6.6) |
| Cyprus |  | 23 (0.8) | 500 (2.9) | 40 (0.9) | 482 (2.3) | 18 (0.8) | 406 (3.1) | 19 (0.6) | 427 (3.5) |
| Egypt | r | 23 (1.1) | 479 (4.4) | 44 (1.2) | 423 (3.5) | 18 (0.8) | 369 (3.9) | 14 (0.8) | 411 (5.0) |
| Estonia |  | 25 (1.2) | 571 (3.6) | 19 (0.7) | 549 (3.3) | 37 (1.1) | 513 (3.6) | 19 (0.6) | 512 (3.7) |
| Ghana |  | 6 (0.6) | 351 (8.6) | 21 (1.4) | 318 (6.8) | 67 (1.5) | 263 (3.9) | 7 (0.6) | 247 (6.9) |
| Hong Kong, SAR |  | 11 (0.9) | 619 (6.0) | 63 (1.1) | 599 (2.6) | 19 (1.0) | 547 (5.9) | 8 (0.4) | 583 (6.2) |
| Hungary | 5 | 38 (1.8) | 583 (3.1) | 36 (1.2) | 542 (3.5) | 19 (1.4) | 454 (4.7) | 8 (0.7) | 491 (10.1) |
| Indonesia |  | 8 (0.9) | 467 (8.4) | 46 (1.3) | 425 (5.1) | 25 (1.2) | 390 (7.3) | 21 (1.0) | 395 (5.8) |
| Iran, Islamic Rep. of |  | 7 (0.6) | 472 (8.3) | 37 (0.9) | 430 (2.8) | 16 (0.8) | 385 (3.4) | 39 (1.1) | 398 (2.4) |
| Israel | r | 35 (1.1) | 540 (4.0) | 29 (0.9) | 499 (4.1) | 23 (0.8) | 455 (4.8) | 14 (0.6) | 489 (4.7) |
| Italy |  | 15 (1.1) | 522 (5.7) | 35 (1.1) | 507 (2.8) | 38 (1.2) | 458 (3.8) | 12 (0.6) | 455 (6.1) |
| Japan | r | 29 (1.3) | 622 (2.9) | 17 (0.7) | 594 (3.3) | 37 (1.2) | 540 (2.3) | 18 (0.7) | 550 (4.1) |
| Jordan |  | 27 (1.6) | 472 (7.7) | 35 (1.2) | 437 (3.9) | 13 (0.8) | 375 (4.6) | 24 (1.0) | 409 (3.9) |
| Korea, Rep. of |  | 31 (1.2) | 626 (2.8) | 48 (0.9) | 593 (2.1) | 11 (0.5) | 514 (4.3) | 9 (0.4) | 559 (5.2) |
| Latvia | s | 35 (1.7) | 540 (3.7) | 34 (1.5) | 522 (3.3) | 16 (1.3) | 506 (7.1) | 15 (0.9) | 489 (6.3) |
| Lebanon |  | 16 (1.1) | 473 (5.4) | 52 (1.2) | 439 (3.6) | 16 (0.9) | 403 (3.8) | 16 (0.9) | 407 (4.8) |
| Lithuania | r | 33 (1.6) | 546 (3.0) | 42 (1.3) | 503 (2.9) | 26 (1.2) | 461 (3.9) | 0 (0.0) | ~ ~ |
| Macedonia, Rep. of |  | 20 (1.3) | 489 (5.2) | 40 (1.1) | 463 (3.0) | 30 (1.1) | 394 (5.2) | 10 (0.8) | 401 (6.7) |
| Malaysia |  | 10 (0.9) | 549 (7.6) | 54 (1.5) | 516 (3.9) | 26 (1.3) | 486 (5.2) | 10 (0.7) | 509 (6.1) |
| Moldova, Rep. of | r | 23 (1.3) | 495 (4.1) | 23 (1.0) | 477 (5.3) | 37 (1.4) | 446 (5.3) | 17 (0.9) | 440 (5.6) |
| Morocco | r | 13 (1.2) | 414 (5.2) | 38 (1.2) | 398 (3.8) | 20 (1.1) | 376 (4.1) | 29 (1.3) | 382 (3.5) |
| Netherlands | r | 13 (1.3) | 585 (6.0) | 16 (1.5) | 589 (5.1) | 55 (2.5) | 527 (3.8) | 16 (1.1) | 541 (6.6) |
| New Zealand | s | 17 (1.6) | 558 (7.8) | 22 (1.3) | 519 (7.2) | 36 (1.9) | 484 (5.4) | 25 (1.3) | 494 (6.8) |
| Norway | S | 47 (1.3) | 490 (2.8) | 13 (0.9) | 469 (5.7) | 19 (1.0) | 437 (5.1) | 21 (0.8) | 467 (4.5) |
| Palestinian Nat'l Auth. |  | 20 (0.8) | 440 (4.4) | 34 (0.9) | 412 (3.1) | 19 (0.8) | 350 (4.3) | 26 (0.8) | 379 (3.6) |
| Philippines |  | 15 (1.2) | 438 (7.9) | 26 (1.2) | 400 (5.4) | 44 (1.7) | 352 (5.8) | 15 (0.9) | 365 (6.3) |
| Romania |  | 14 (1.6) | 550 (5.0) | 30 (1.2) | 520 (4.0) | 41 (1.7) | 450 (4.9) | 16 (1.2) | 438 (7.3) |
| Russian Federation |  | 35 (2.2) | 543 (3.5) | 30 (1.4) | 515 (4.5) | 21 (1.2) | 475 (5.7) | 13 (0.6) | 474 (3.9) |
| Saudi Arabia | $r$ | 24 (1.9) | 374 (6.3) | 45 (1.6) | 337 (5.5) | 13 (1.0) | 310 (5.2) | 19 (1.7) | 324 (6.3) |
| Scotland |  | x x | x x | x x | x x | x x | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x |
| Serbia |  | 15 (1.1) | 547 (3.7) | 27 (0.9) | 524 (2.8) | 48 (1.3) | 445 (2.9) | 10 (0.6) | 429 (5.2) |
| Singapore | r | 13 (0.5) | 655 (3.3) | 43 (1.1) | 627 (2.9) | 28 (1.0) | 566 (5.0) | 15 (0.5) | 603 (5.1) |
| Slovak Republic | r | 25 (1.8) | 570 (3.9) | 27 (1.1) | 542 (3.8) | 36 (1.5) | 479 (3.1) | 13 (0.8) | 471 (5.8) |
| Slovenia | r | 18 (1.1) | 544 (3.5) | 26 (0.9) | 525 (3.0) | 42 (1.1) | 464 (2.7) | 14 (0.8) | 486 (4.9) |
| South Africa | r | 8 (1.0) | 391 (16.2) | 26 (0.9) | 293 (7.8) | 54 (1.2) | 240 (3.7) | 12 (0.8) | 232 (6.5) |
| Sweden | s | 32 (1.4) | 536 (3.8) | 14 (0.8) | 513 (5.4) | 33 (1.5) | 482 (3.5) | 21 (0.9) | 502 (4.2) |
| Tunisia |  | 8 (0.7) | 453 (5.7) | 46 (1.1) | 417 (2.8) | 26 (0.8) | 396 (2.7) | 21 (0.7) | 406 (2.5) |
| United States | $r$ | 48 (1.3) | 535 (3.7) | 27 (0.8) | 496 (3.3) | 16 (0.7) | 458 (3.3) | $9(0.3)$ | 494 (4.1) |
| $\ddagger$ England |  | x x | x x | $\times \mathrm{x}$ | x x | x x | x x | $\mathrm{x} \times$ | x x |
| International Avg. |  | 21 (0.2) | 516 (0.9) | 33 (0.2) | 485 (0.7) | 30 (0.2) | 434 (0.7) | 15 (0.1) | 447 (0.8) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 23 (1.7) | 519 (4.3) | 27 (1.3) | 503 (4.2) | 18 (1.2) | 461 (4.4) | 32 (1.3) | 469 (3.1) |
| Indiana State, US | r | 40 (2.4) | 535 (7.5) | 33 (1.5) | 512 (5.0) | 16 (1.5) | 472 (4.9) | 11 (1.0) | 497 (7.2) |
| Ontario Province, Can. | s | 39 (2.2) | 558 (3.3) | 26 (1.4) | 534 (3.5) | 22 (1.7) | 491 (3.4) | 13 (0.9) | 519 (4.4) |
| Quebec Province, Can. | $r$ | 26 (1.6) | 568 (4.8) | 28 (1.1) | 551 (4.0) | 35 (1.9) | 525 (2.4) | 11 (0.7) | 550 (4.6) |

Background data provided by students.

* Based on countries' categorizations to UNESCO's International Standard Classification of Education (Operational Manual for ISCED-1997).
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. $A n$ " $x$ " indicates data are available for less than $50 \%$ of the students.
in relation to their average mathematics achievement, shows that this remains true for the TIMSS 2003 countries, and holds also for mathematics achievement at the fourth grade. At both eighth and fourth grades, students from homes where the language of the test is always or almost always spoken had higher average achievement than those who spoke it less frequently.

Whereas in most countries a large majority of students at each grade are from homes where the language of the test is spoken frequently, on average, internationally about 21 percent of students were from homes where the language of the test was spoken only sometimes, or never. Countries where the majority of students speak the language of the test so infrequently included Botswana, Ghana, Indonesia, Lebanon, the Philippines, Singapore, and South Africa at the eighth grade, and Morocco, the Philippines, and Singapore at the fourth grade. Even though most of these countries had relatively low mathematics achievement, Singapore was a notable exception, with average achievement among those sometimes or never speaking the language of the test at home well above the international average for students always speaking the language of the test at home.

Many countries tested in more than one language in order to cover their whole student population. These included Bahrain (Arabic and English), Egypt (Arabic, English, and French), Estonia (Estonian and Russian), Hong Kong SAR (Chinese and English), Israel (Hebrew and Arabic), Latvia (Latvian and Russian), Lebanon (French and English), Macedonia (Macedonian and Albanian), Moldova (Moldavian and Russian), New Zealand (English and Maori at grade 4 only), Norway (Bokmål and Nynorsk), the Palestinian National Authority (Arabic and English), Romania (Romanian and Hungarian), the Slovak Republic (Slovak and Hungarian), and South Africa (English and Afrikaans). Among benchmarking participants, the Basque Country, Spain tested in Basque and Castilian, and the Canadian provinces of Ontario and Quebec in English and French. However, in countries like Botswana, Ghana, Indonesia, Morocco,

| Countries | Always |  | Almost Always |  | Sometimes |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 80 (1.0) | 477 (3.3) | 16 (0.8) | 491 (4.0) | 4 (0.5) | 461 (8.4) | 0 (0.1) | ~ ~ |
| Australia | 80 (2.3) | 503 (4.1) | 12 (1.1) | 510 (10.9) | 7 (1.3) | 534 (15.1) | 1 (0.4) | ~ |
| Bahrain | 66 (1.1) | 398 (2.2) | 15 (0.7) | 424 (3.4) | 15 (0.7) | 399 (3.7) | 4 (0.5) | 384 (5.9) |
| Belgium (Flemish) | 77 (1.3) | 547 (2.7) | 11 (0.6) | 527 (6.9) | 9 (0.8) | 483 (8.3) | 4 (0.6) | 513 (8.0) |
| Botswana | 5 (0.3) | 375 (10.3) | 6 (0.4) | 402 (8.0) | 80 (0.8) | 367 (2.6) | 9 (0.6) | 329 (6.2) |
| Bulgaria | 81 (2.0) | 477 (4.0) | 10 (0.8) | 493 (9.5) | 8 (1.4) | 454 (12.1) | 1 (0.3) | ~ ~ |
| Chile | 87 (0.7) | 390 (3.3) | 9 (0.5) | 386 (4.5) | 4 (0.4) | 334 (8.2) | 0 (0.1) | ~ ~ |
| Chinese Taipei | 44 (1.5) | 609 (3.9) | 36 (1.0) | 586 (4.7) | 19 (1.2) | 537 (8.6) | 1 (0.2) | ~ |
| Cyprus | 79 (0.8) | 460 (1.8) | 14 (0.6) | 469 (4.6) | 6 (0.4) | 447 (6.7) | 2 (0.2) | ~ ~ |
| Egypt | 61 (1.3) | 403 (3.7) | 14 (0.8) | 428 (5.6) | 22 (1.0) | 415 (4.4) | 3 (0.3) | 389 (10.6) |
| Estonia | 90 (0.6) | 532 (3.2) | 8 (0.4) | 532 (4.5) | 2 (0.3) | ~ ~ | 1 (0.2) | ~ ~ |
| Ghana | 23 (1.1) | 272 (5.3) | 10 (0.7) | 295 (8.7) | 63 (1.3) | 285 (4.6) | 5 (0.9) | 189 (12.2) |
| Hong Kong, SAR | 77 (0.8) | 596 (2.8) | 15 (0.6) | 566 (6.1) | 7 (0.5) | 541 (8.5) | 1 (0.2) | ~~ |
| Hungary | 95 (0.4) | 529 (3.2) | 4 (0.4) | 533 (9.3) | 0 (0.1) | ~ | 0 (0.1) | ~ |
| Indonesia | 22 (2.0) | 406 (7.1) | 11 (0.7) | 420 (7.5) | 57 (2.0) | 410 (5.3) | 10 (0.8) | 412 (7.0) |
| Iran, Islamic Rep. of | 55 (3.2) | 422 (3.0) | 9 (0.6) | 428 (4.8) | 21 (1.8) | 392 (3.4) | 15 (1.9) | 391 (5.4) |
| Israel | 79 (1.0) | 496 (3.6) | 15 (0.7) | 506 (5.8) | 5 (0.5) | 484 (6.1) | 1 (0.2) | ~ ~ |
| Italy | 94 (0.5) | 486 (3.1) | 3 (0.3) | 475 (8.2) | 3 (0.3) | 424 (10.2) | 1 (0.2) | ~ ~ |
| Japan | 94 (0.4) | 572 (2.1) | 4 (0.3) | 542 (6.8) | 1 (0.2) | ~ ~ | 0 (0.1) | ~~ |
| Jordan | 72 (1.2) | 420 (3.8) | 13 (0.7) | 459 (7.6) | 11 (0.7) | 424 (5.8) | 4 (0.5) | 423 (17.7) |
| Korea, Rep. of | 71 (0.8) | 588 (2.5) | 28 (0.8) | 595 (2.9) | 1 (0.2) | $\sim \sim$ | 0 (0.0) | ~~ |
| Latvia | 77 (1.9) | 511 (3.4) | 14 (0.9) | 509 (4.1) | 6 (1.3) | 486 (8.0) | 2 (0.5) | ~ |
| Lebanon | 5 (0.5) | 425 (8.1) | 12 (0.7) | 442 (5.1) | 68 (1.1) | 433 (3.2) | 15 (0.8) | 428 (5.0) |
| Lithuania | 89 (1.0) | 501 (2.6) | 9 (0.5) | 508 (5.5) | 2 (0.4) | ~ | 1 (0.2) | ~ ~ |
| Macedonia, Rep. of | 89 (1.4) | 438 (3.5) | 4 (0.4) | 429 (8.8) | 5 (0.9) | 394 (12.2) | 2 (0.6) | ~ ~ |
| Malaysia | 51 (2.1) | 490 (4.1) | 14 (0.8) | 510 (4.5) | 28 (1.9) | 530 (6.3) | 7 (0.8) | 551 (9.7) |
| Moldova, Rep. of | 68 (1.6) | 461 (4.6) | 18 (0.9) | 466 (5.3) | 13 (1.2) | 448 (5.7) | 1 (0.2) | ~ ~ |
| Morocco | 35 (1.8) | 375 (3.3) | 18 (0.9) | 403 (4.4) | 39 (1.4) | 391 (3.2) | 8 (0.8) | 394 (6.6) |
| Netherlands | 83 (1.3) | 542 (3.8) | 12 (1.0) | 518 (7.4) | 4 (0.5) | 491 (12.2) | 1 (0.2) | ~~ |
| New Zealand | 80 (1.3) | 495 (5.4) | 12 (0.8) | 487 (7.2) | 6 (0.8) | 508 (13.4) | 1 (0.3) | ~ ~ |
| Norway | 85 (0.8) | 463 (2.4) | 10 (0.5) | 463 (5.2) | 3 (0.4) | 427 (8.8) | 1 (0.2) | ~ |
| Palestinian Nat'l Auth. | 73 (1.3) | 391 (3.2) | 11 (0.6) | 410 (5.9) | 13 (1.0) | 382 (5.6) | 2 (0.3) | ~ ~ |
| Philippines | 2 (0.3) | ~ ~ | 4 (0.3) | 386 (10.8) | 80 (1.0) | 383 (5.3) | 14 (0.9) | 351 (5.7) |
| Romania | 86 (1.8) | 475 (4.9) | 8 (0.6) | 493 (7.0) | 4 (1.0) | 453 (17.3) | 2 (1.0) | ~~ |
| Russian Federation | 86 (2.0) | 507 (3.9) | 10 (1.0) | 524 (6.5) | 4 (1.1) | 492 (15.0) | 1 (0.3) | $\sim \sim$ |
| Saudi Arabia | 100 (0.0) | 332 (4.6) | 0 (0.0) | ~ ~ | 0 (0.0) | ~ ~ | 0 (0.0) | ~ |
| Scotland | 92 (0.6) | 499 (3.7) | 5 (0.5) | 508 (8.0) | 3 (0.3) | 446 (10.4) | 1 (0.2) | ~ ~ |
| Serbia | 93 (0.7) | 477 (2.6) | 5 (0.4) | 486 (7.1) | 2 (0.4) | ~ ~ | 0 (0.1) | ~ ~ |
| Singapore | 23 (0.6) | 625 (3.8) | 19 (0.6) | 620 (3.5) | 49 (0.8) | 595 (4.3) | 8 (0.4) | 581 (5.7) |
| Slovak Republic | 79 (1.6) | 509 (3.5) | 12 (0.7) | 518 (5.8) | 7 (1.0) | 480 (8.0) | 2 (0.4) | ~~ |
| Slovenia | 80 (1.3) | 497 (2.4) | 11 (0.7) | 488 (3.8) | 6 (0.7) | 464 (7.1) | 2 (0.5) | ~ ~ |
| South Africa | 18 (1.7) | 349 (14.6) | 9 (0.7) | 319 (13.0) | 57 (1.7) | 247 (3.1) | 15 (1.0) | 192 (3.9) |
| Sweden | 84 (1.3) | 504 (2.5) | 10 (0.8) | 491 (5.0) | 5 (0.7) | 457 (8.8) | 1 (0.2) | ~ ~ |
| Tunisia | 51 (1.7) | 408 (2.6) | 13 (0.8) | 429 (5.1) | 28 (1.3) | 406 (2.7) | 9 (0.9) | 411 (5.3) |
| United States | 83 (0.9) | 509 (3.1) | 10 (0.5) | 496 (5.7) | 5 (0.4) | 464 (6.8) | 1 (0.2) | ~ ~ |
| \# England | 87 (1.6) | 501 (5.3) | 10 (1.3) | 504 (6.3) | 2 (0.6) | ~ | 1 (0.2) | ~ ~ |
| International Avg. | 68 (0.2) | 472 (0.7) | 11 (0.1) | 477 (1.0) | 17 (0.1) | 441 (1.4) | 4 (0.1) | 396 (2.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 65 (1.6) | 487 (3.3) | 25 (1.1) | 490 (3.5) | 8 (0.7) | 485 (5.1) | 3 (0.5) | 476 (10.2) |
| Indiana State, US | 88 (0.9) | 509 (5.1) | 7 (0.8) | 514 (9.0) | 4 (0.4) | 488 (11.6) | 1 (0.2) | ~ |
| Ontario Province, Can. | 72 (2.0) | 520 (2.8) | 16 (1.1) | 517 (4.8) | 9 (0.9) | 530 (9.2) | 2 (0.3) | $\sim \sim$ |
| Quebec Province, Can. | 72 (1.8) | 545 (3.2) | 19 (0.9) | 540 (5.0) | 7 (0.9) | 532 (5.8) | 2 (0.4) | $\sim \sim$ |

Did not satisfy guidelines for sample participation rates (see Exhibit A.9)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries | Always |  | Almost Always |  | Sometimes |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 84 (1.0) | 459 (3.6) | 11 (0.7) | 470 (5.7) | 4 (0.4) | 427 (11.3) | 1 (0.2) | ~ |
| Australia | 80 (1.7) | 500 (4.3) | 11 (0.9) | 510 (6.1) | 8 (1.0) | 488 (7.2) | 1 (0.2) | ~ |
| Belgium (Flemish) | 68 (1.4) | 558 (1.7) | 16 (0.9) | 550 (2.9) | 12 (1.2) | 517 (5.2) | 4 (0.5) | 533 (6.7) |
| Chinese Taipei | 31 (1.2) | 581 (2.3) | 41 (0.8) | 563 (1.7) | 26 (1.1) | 548 (2.7) | 1 (0.1) | ~ |
| Cyprus | 72 (1.1) | 510 (2.4) | 14 (0.7) | 526 (4.4) | 11 (0.6) | 497 (5.8) | 3 (0.3) | 488 (9.6) |
| England | 82 (1.3) | 534 (3.9) | 12 (0.8) | 540 (5.9) | 5 (0.7) | 476 (7.9) | 1 (0.2) | ~ ~ |
| Hong Kong, SAR | 51 (1.3) | 592 (3.4) | 24 (0.8) | 568 (3.3) | 21 (1.0) | 554 (3.8) | 4 (0.4) | 521 (5.1) |
| Hungary | 91 (0.6) | 530 (3.0) | 8 (0.6) | 536 (6.2) | 1 (0.2) | ~ ~ | 0 (0.1) | ~ ~ |
| Iran, Islamic Rep. of | 53 (3.4) | 407 (4.6) | 6 (0.5) | 405 (9.9) | 21 (1.9) | 379 (6.0) | 20 (2.5) | 354 (6.8) |
| Italy | 88 (0.7) | 508 (3.7) | 3 (0.3) | 487 (9.5) | 6 (0.5) | 470 (7.1) | 2 (0.3) | ~ ~ |
| Japan | 91 (0.5) | 568 (1.6) | 8 (0.5) | 546 (5.2) | 1 (0.2) | ~ ~ | 0 (0.1) | ~ ~ |
| Latvia | 78 (1.5) | 537 (2.8) | 15 (0.8) | 546 (4.6) | 6 (0.8) | 511 (7.9) | 2 (0.4) | ~ ~ |
| Lithuania | 83 (1.0) | 534 (3.1) | 13 (0.8) | 556 (5.2) | 3 (0.6) | 494 (10.7) | 0 (0.1) | ~ ~ |
| Moldova, Rep. of | 76 (1.8) | 508 (5.4) | 14 (1.0) | 501 (7.8) | 9 (1.1) | 502 (8.2) | 1 (0.3) | ~ ~ |
| Morocco | 35 (2.3) | 344 (5.9) | 11 (0.8) | 344 (7.1) | 28 (1.6) | 362 (6.2) | 27 (2.5) | 350 (8.9) |
| Netherlands | 75 (1.2) | 547 (1.9) | 17 (0.9) | 532 (3.7) | 7 (0.8) | 503 (7.1) | 1 (0.3) | ~ ~ |
| New Zealand | 76 (1.0) | 500 (2.2) | 13 (0.6) | 509 (4.8) | 11 (0.8) | 443 (7.1) | 1 (0.2) | ~ ~ |
| Norway | 78 (1.0) | 455 (2.4) | 15 (0.8) | 458 (3.8) | 5 (0.5) | 410 (8.3) | 1 (0.2) | ~ ~ |
| Philippines | 6 (0.6) | 321 (10.9) | 8 (0.9) | 336 (21.1) | 59 (1.8) | 382 (8.5) | 27 (2.1) | 325 (6.8) |
| Russian Federation | 81 (2.3) | 531 (4.7) | 8 (0.7) | 546 (7.1) | 8 (1.7) | 532 (15.2) | 2 (0.5) | ~ ~ |
| Scotland | 78 (1.3) | 495 (3.2) | 10 (0.6) | 501 (6.2) | 9 (0.8) | 466 (6.0) | 3 (0.4) | 439 (12.7) |
| Singapore | 24 (1.2) | 610 (6.2) | 22 (1.0) | 625 (4.9) | 47 (1.5) | 580 (5.7) | 7 (0.6) | 551 (8.6) |
| Slovenia | 72 (1.3) | 480 (2.8) | 18 (1.1) | 496 (3.9) | 8 (1.0) | 459 (5.5) | 2 (0.3) | ~ ~ |
| Tunisia | 43 (2.5) | 342 (6.9) | 9 (0.8) | 341 (9.4) | 36 (2.2) | 347 (5.3) | 12 (1.5) | 353 (9.9) |
| United States | 73 (1.1) | 526 (2.4) | 13 (0.5) | 525 (4.0) | 12 (0.8) | 477 (4.8) | 2 (0.1) | ~ ~ |
| International Avg. | 67 (0.3) | 499 (0.9) | 14 (0.2) | 501 (1.4) | 15 (0.2) | 471 (1.6) | 5 (0.2) | 435 (2.9) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US | 83 (0.9) | 534 (2.8) | 11 (0.7) | 550 (5.8) | 5 (0.7) | 502 (8.3) | 1 (0.2) | ~ ~ |
| Ontario Province, Can. | 63 (1.7) | 510 (3.5) | 24 (1.1) | 526 (5.1) | 13 (1.1) | 492 (6.8) | 1 (0.2) | ~ ~ |
| Quebec Province, Can. | 67 (1.3) | 505 (2.6) | 24 (0.9) | 515 (3.7) | 8 (0.8) | 490 (5.0) | 2 (0.3) | $\sim \sim$ |

the Philippines, Singapore, and South Africa, testing in all possible dialects and languages was prohibitive.

Earlier IEA studies have shown that students from homes with extensive literacy resources have higher achievement than those from less advantaged backgrounds. For example, TIMSS 1999 has shown a consistent relationship between number of books in the home and student achievement in both mathematics and science at the eighth grade, ${ }^{2}$ and PIRLS 2001 demonstrated a similar relationship with reading literacy at the fourth grade. ${ }^{3}$ Providing further information on this topic, Exhibit 4.4 shows for each country at both eighth and fourth grades the percentage of students at each of five ranges of numbers of books in the home in relation to average mathematics achievement. This exhibit reveals a wide range both across and within each country. For example, the percentage of eighth-grade students reporting more than 200 books in their homes exceeded 30 percent in Australia, Estonia, Hungary, and Sweden, whereas in Botswana, Egypt, Ghana, Indonesia, Iran, Morocco, the Philippines, and South Africa, more than 30 percent of students were from homes with 10 books or less. The situation among fourth-grade students was similar.

Across countries, on average, 15 percent of eighth-grade student were from homes with more than 200 books, 13 percent from homes with 101-200 books, 27 percent from homes with 26-100 books, 26 percent from homes with 11-25 books, and 18 percent with 0-10 books. There also was a clear-cut relationship, on average, between number of books in the home and mathematics achievement. Eighthgrade students reporting more than 200 books in their homes had an average score of 498 on the mathematics scale, compared with an average of just 429 for students reporting 10 books or less, a difference of 69 points. If anything, the difference at fourth grade was even larger, ranging from 521 for students reporting more than 200 books to 457 for students reporting 10 books or less.

In addition to literacy resources such as books, TIMSS has found that having study aids such as a computer or a study desk or table at

3 Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., and Kennedy, A.M. (2003), PIRLS 2001 International Report: IEA's Study of Reading Literacy Achievement in Primary Schools in 35 Countries, Chestnut Hill, MA: Boston College
home was associated with higher student achievement. Exhibit 4.5 shows the percentage of eighth- and fourth-grade students in each country that had a computer or study desk or table, together with their average mathematics achievement. About 60 percent of eighthgrade students, on average, reported having a computer at home, and a slightly greater percentage of fourth-grade students ( $65 \%$ ). However, there were great differences between countries. For 17 of the participants - Australia, Belgium (Flemish), Chinese Taipei, England, Hong Kong SAR, Israel, Korea, the Netherlands, New Zealand, Norway, Scotland, Singapore, Sweden, the United States, Indiana, Ontario, and Quebec - virtually all eighth-grade students ( $90 \%$ or more) reported having a computer at home. In contrast, less than 20 percent of eighthgrade students in Armenia, Botswana, Egypt, Indonesia, Moldova, and Morocco reported having a computer. The mathematics achievement difference between students with a computer at home and those without was substantial on average - 39 scale score points at eighth grade and 27 points at fourth grade.

Perhaps not surprisingly, somewhat greater percentages of students reported having a study desk or table at home -83 percent and 80 percent at eighth and fourth grades, respectively. In many countries (20 at eighth grade and 9 at fourth grade), more than 90 percent of students reported having a study desk. Having such a study facility was associated with higher average mathematics achievement at both grades - a 35 point difference at eighth grade and a 27 point difference at fourth grade.

Because having a computer at home does not necessarily mean that students have access to it, TIMSS also asked students where they actually use a computer - at home, at school, or some other place. Exhibit 4.6 summarizes these responses, presenting countries in order of the percentage of students that reported using a computer both at home and at school. At the eighth grade, 39 percent of the students, on average, across countries reported using a computer both at home and at school. Eighteen percent reported using a computer at home

| Countries | More than 200 Books |  | 101-200 Books |  | 26-100 Books |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 20 (1.0) | 497 (4.1) | 13 (0.6) | 497 (4.8) | 28 (0.7) | 483 (3.4) |
| Australia | 31 (1.4) | 526 (5.0) | 23 (0.8) | 514 (4.6) | 30 (1.0) | 501 (6.0) |
| Bahrain | 17 (0.5) | 416 (3.1) | 14 (0.6) | 426 (3.7) | 31 (0.8) | 407 (2.1) |
| Belgium (Flemish) | 12 (0.6) | 560 (4.6) | 15 (0.6) | 558 (3.6) | 34 (0.9) | 544 (2.9) |
| Botswana | 4 (0.5) | 401 (12.5) | 5 (0.3) | 400 (6.9) | 13 (0.6) | 386 (5.8) |
| Bulgaria | 28 (1.3) | 502 (6.3) | 18 (0.9) | 492 (5.3) | 25 (1.1) | 472 (4.3) |
| Chile | 5 (0.4) | 461 (5.9) | 7 (0.4) | 444 (5.1) | 27 (0.9) | 415 (3.7) |
| Chinese Taipei | 15 (1.0) | 639 (4.9) | 14 (0.6) | 622 (4.8) | 30 (0.7) | 600 (4.7) |
| Cyprus | 11 (0.5) | 492 (4.6) | 16 (0.7) | 478 (3.6) | 35 (0.8) | 472 (2.5) |
| Egypt | 6 (0.4) | 433 (8.8) | 6 (0.4) | 426 (9.5) | 18 (0.7) | 426 (4.8) |
| Estonia | 45 (1.2) | 549 (3.3) | 18 (0.6) | 534 (3.6) | 23 (0.7) | 515 (3.5) |
| Ghana | 10 (0.6) | 275 (7.2) | 6 (0.4) | 300 (9.6) | 16 (0.7) | 294 (7.8) |
| Hong Kong, SAR | 9 (0.6) | 608 (6.3) | 8 (0.4) | 611 (4.6) | 27 (0.6) | 595 (3.6) |
| Hungary | 31 (1.2) | 567 (3.3) | 22 (0.7) | 543 (3.7) | 29 (1.0) | 516 (3.5) |
| Indonesia | 1 (0.2) | ~ ~ | 3 (0.3) | 443 (10.2) | 19 (0.7) | 423 (5.8) |
| Iran, Islamic Rep. of | 7 (0.5) | 456 (5.8) | 5 (0.3) | 452 (5.2) | 17 (0.8) | 432 (3.6) |
| Israel | 22 (0.9) | 520 (4.6) | 22 (0.7) | 514 (3.9) | 33 (0.8) | 492 (4.2) |
| Italy | 19 (0.9) | 516 (4.7) | 14 (0.6) | 501 (4.2) | 25 (0.7) | 489 (3.8) |
| Japan | 17 (0.7) | 604 (3.5) | 17 (0.5) | 587 (3.5) | 32 (0.8) | 571 (2.4) |
| Jordan | 9 (0.6) | 456 (9.1) | 8 (0.5) | 463 (7.7) | 28 (0.9) | 445 (4.8) |
| Korea, Rep. of | 19 (0.8) | 636 (3.3) | 22 (0.7) | 608 (2.9) | 33 (0.8) | 586 (2.4) |
| Latvia | 28 (1.3) | 528 (4.3) | 25 (0.8) | 515 (4.2) | 31 (1.1) | 505 (3.3) |
| Lebanon | 8 (0.6) | 447 (6.6) | 8 (0.8) | 465 (6.5) | 25 (1.0) | 457 (3.9) |
| Lithuania | 12 (0.8) | 540 (5.2) | 15 (0.7) | 532 (3.9) | 34 (0.9) | 509 (2.4) |
| Macedonia, Rep. of | 8 (0.7) | 452 (8.2) | 8 (0.6) | 475 (6.6) | 28 (0.9) | 465 (3.8) |
| Malaysia | 5 (0.5) | 555 (8.0) | 9 (0.6) | 539 (6.0) | 28 (0.8) | 524 (4.4) |
| Moldova, Rep. of | 8 (0.8) | 488 (6.7) | 9 (0.6) | 483 (7.0) | 23 (1.0) | 471 (4.6) |
| Morocco | 5 (0.6) | 396 (11.4) | 4 (0.3) | 403 (6.6) | 21 (0.9) | 391 (4.5) |
| Netherlands | 21 (1.4) | 565 (5.3) | 19 (0.9) | 558 (4.6) | 31 (1.3) | 539 (3.8) |
| New Zealand | 25 (1.5) | 527 (8.0) | 22 (1.1) | 508 (4.4) | 31 (1.0) | 489 (5.2) |
| Norway | 27 (1.2) | 481 (3.2) | 22 (0.7) | 477 (3.1) | 33 (0.9) | 460 (3.0) |
| Palestinian Nat'l Auth. | 7 (0.5) | 402 (7.9) | 6 (0.4) | 420 (7.1) | 24 (0.7) | 413 (4.2) |
| Philippines | 3 (0.3) | 372 (9.4) | 4 (0.3) | 403 (12.4) | 17 (0.8) | 410 (7.2) |
| Romania | 12 (1.2) | 529 (6.6) | 13 (1.1) | 517 (5.1) | 29 (1.2) | 489 (4.1) |
| Russian Federation | 21 (1.3) | 534 (4.4) | 26 (0.9) | 521 (3.6) | 32 (1.4) | 505 (4.4) |
| Saudi Arabia | 10 (0.7) | 347 (8.5) | 9 (0.9) | 355 (9.0) | 25 (1.0) | 347 (5.7) |
| Scotland | 17 (1.0) | 539 (5.6) | 16 (0.7) | 527 (4.0) | 29 (0.8) | 504 (3.8) |
| Serbia | 6 (0.5) | 519 (5.8) | 9 (0.5) | 534 (4.9) | 27 (1.0) | 500 (3.2) |
| Singapore | 14 (0.5) | 642 (3.5) | 16 (0.5) | 627 (3.7) | 33 (0.7) | 617 (3.2) |
| Slovak Republic | 12 (0.8) | 551 (5.4) | 18 (0.8) | 543 (3.9) | 41 (0.9) | 514 (3.1) |
| Slovenia | 13 (0.7) | 517 (5.3) | 15 (0.7) | 513 (4.4) | 38 (0.9) | 501 (2.1) |
| South Africa | 6 (0.5) | 324 (17.5) | 5 (0.4) | 325 (19.5) | 14 (0.7) | 304 (11.7) |
| Sweden | 32 (1.3) | 531 (2.7) | 21 (0.6) | 513 (3.1) | 27 (0.9) | 485 (3.4) |
| Tunisia | 4 (0.4) | 453 (7.8) | 6 (0.5) | 436 (6.6) | 22 (0.9) | 422 (3.4) |
| United States | 24 (0.9) | 541 (4.4) | 18 (0.5) | 528 (3.4) | 28 (0.6) | 506 (3.0) |
| ま England | 24 (1.1) | 539 (6.9) | 18 (1.0) | 518 (6.7) | 27 (1.0) | 494 (5.5) |
| International Avg. | 15 (0.1) | 498 (1.0) | 13 (0.1) | 492 (1.0) | 27 (0.1) | 476 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 25 (1.4) | 509 (3.5) | 20 (0.9) | 497 (3.6) | 36 (1.3) | 486 (3.1) |
| Indiana State, US | 19 (1.6) | 541 (8.8) | 17 (0.9) | 526 (6.8) | 32 (1.0) | 514 (4.6) |
| Ontario Province, Can. | 28 (1.6) | 544 (3.4) | 21 (0.9) | 532 (3.5) | 31 (1.1) | 513 (3.7) |
| Quebec Province, Can. | 13 (0.8) | 561 (4.9) | 16 (0.9) | 563 (5.5) | 33 (0.9) | 547 (3.1) |

[^28]丰 Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 4.4: Books in the Home

| Countries | 11-25 Books |  | 0-10 Books |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 24 (0.9) | 466 (4.2) | 15 (0.9) | 449 (4.5) |
| Australia | 11 (0.8) | 477 (7.1) | 5 (0.5) | 448 (10.8) |
| Bahrain | 26 (0.8) | 384 (3.4) | 11 (0.5) | 376 (3.9) |
| Belgium (Flemish) | 25 (0.8) | 527 (4.0) | 14 (0.7) | 497 (5.9) |
| Botswana | 30 (0.9) | 368 (4.1) | 48 (1.3) | 355 (2.6) |
| Bulgaria | 15 (0.7) | 453 (5.7) | 14 (1.6) | 441 (11.2) |
| Chile | 37 (0.9) | 374 (3.1) | 23 (1.2) | 342 (3.8) |
| Chinese Taipei | 24 (0.9) | 564 (4.8) | 17 (0.9) | 513 (5.3) |
| Cyprus | 27 (0.7) | 441 (3.4) | 11 (0.5) | 410 (4.2) |
| Egypt | 38 (0.8) | 408 (3.8) | 33 (1.2) | 398 (3.5) |
| Estonia | 11 (0.6) | 503 (4.4) | 3 (0.3) | 476 (6.8) |
| Ghana | 34 (1.0) | 285 (6.0) | 34 (1.5) | 264 (4.7) |
| Hong Kong, SAR | 28 (0.7) | 583 (3.9) | 28 (0.7) | 567 (4.4) |
| Hungary | 13 (0.6) | 481 (4.7) | 5 (0.7) | 433 (9.1) |
| Indonesia | 45 (0.9) | 404 (5.2) | 32 (1.0) | 408 (5.7) |
| Iran, Islamic Rep. of | 31 (0.8) | 411 (2.7) | 39 (1.3) | 391 (2.7) |
| Israel | 17 (0.8) | 466 (4.4) | 6 (0.4) | 465 (7.0) |
| Italy | 29 (0.7) | 464 (3.9) | 13 (0.7) | 450 (4.8) |
| Japan | 22 (0.6) | 553 (3.2) | 13 (0.7) | 533 (3.7) |
| Jordan | 33 (0.9) | 416 (3.8) | 23 (0.8) | 398 (4.2) |
| Korea, Rep. of | 10 (0.6) | 555 (3.8) | 15 (0.7) | 534 (3.4) |
| Latvia | 12 (0.7) | 480 (5.6) | 4 (0.4) | 453 (8.2) |
| Lebanon | 36 (1.1) | 422 (3.5) | 23 (1.4) | 410 (3.0) |
| Lithuania | 30 (1.1) | 477 (3.0) | 10 (0.7) | 455 (5.9) |
| Macedonia, Rep. of | 40 (1.2) | 427 (3.6) | 17 (0.8) | 388 (5.2) |
| Malaysia | 40 (1.0) | 498 (4.0) | 17 (0.9) | 477 (4.7) |
| Moldova, Rep. of | 37 (1.2) | 457 (4.8) | 23 (1.1) | 438 (6.2) |
| Morocco | 38 (1.0) | 385 (3.2) | 33 (1.4) | 387 (3.2) |
| Netherlands | 19 (1.2) | 504 (6.5) | 10 (0.8) | 490 (6.2) |
| New Zealand | 14 (0.8) | 464 (5.2) | 8 (0.7) | 439 (8.9) |
| Norway | 11 (0.6) | 425 (4.2) | 7 (0.4) | 408 (7.2) |
| Palestinian Nat'l Auth. | 36 (0.8) | 387 (3.6) | 27 (1.0) | 371 (3.5) |
| Philippines | 34 (0.8) | 382 (4.8) | 43 (1.0) | 361 (5.4) |
| Romania | 27 (1.4) | 454 (5.1) | 20 (1.7) | 430 (8.1) |
| Russian Federation | 17 (1.1) | 476 (5.3) | 4 (0.5) | 457 (9.1) |
| Saudi Arabia | 33 (1.1) | 321 (5.1) | 23 (1.4) | 318 (4.6) |
| Scotland | 21 (1.0) | 471 (4.4) | 16 (0.9) | 450 (4.8) |
| Serbia | 38 (1.0) | 466 (2.9) | 21 (1.1) | 435 (4.5) |
| Singapore | 24 (0.7) | 580 (5.1) | 12 (0.7) | 554 (5.2) |
| Slovak Republic | 24 (1.1) | 465 (3.8) | 5 (0.5) | 424 (7.3) |
| Slovenia | 27 (0.7) | 474 (3.6) | 8 (0.6) | 444 (5.4) |
| South Africa | 31 (0.9) | 261 (5.0) | 44 (1.3) | 241 (3.1) |
| Sweden | 14 (0.7) | 460 (4.0) | 6 (0.6) | 447 (6.3) |
| Tunisia | 44 (1.1) | 404 (2.2) | 23 (1.1) | 400 (2.3) |
| United States | 18 (0.6) | 473 (3.5) | 13 (0.6) | 449 (4.2) |
| き England | 17 (0.9) | 480 (5.9) | 13 (1.1) | 446 (5.7) |
| International Avg. | 26 (0.1) | 449 (0.7) | 18 (0.1) | 429 (1.0) |
| Benchmarking Participants |  |  |  |  |
| Basque Country, Spain | 15 (0.8) | 458 (3.4) | 5 (0.5) | 430 (7.5) |
| Indiana State, US | 19 (1.0) | 484 (5.9) | 14 (1.2) | 467 (5.4) |
| Ontario Province, Can. | 14 (0.9) | 494 (4.2) | 7 (0.6) | 482 (6.7) |
| Quebec Province, Can. | 24 (1.1) | 529 (2.5) | 14 (0.7) | 521 (3.4) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 4.4: Books in the Home





## Exhibit 4.4: Books in the Home

| Countries |  | 11-25 Books |  | 0-10 Books |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | r | 22 (0.9) | 456 (5.2) | 17 (1.2) | 434 (6.3) |
| Australia |  | 13 (0.9) | 477 (5.7) | 6 (0.8) | 437 (9.6) |
| Belgium (Flemish) |  | 23 (0.9) | 537 (3.0) | 8 (0.5) | 512 (5.2) |
| Chinese Taipei |  | 24 (0.8) | 555 (2.1) | 17 (0.8) | 527 (2.8) |
| Cyprus |  | 29 (1.0) | 506 (3.3) | 11 (0.7) | 467 (5.1) |
| England |  | 17 (1.0) | 497 (4.5) | 8 (0.8) | 466 (5.9) |
| Hong Kong, SAR |  | 30 (0.8) | 572 (3.4) | 25 (1.4) | 561 (4.0) |
| Hungary |  | 22 (0.9) | 500 (3.8) | 8 (0.7) | 469 (6.0) |
| Iran, Islamic Rep. of |  | 22 (1.2) | 410 (4.4) | 55 (2.1) | 374 (4.0) |
| Italy |  | 33 (1.0) | 498 (4.4) | 18 (0.9) | 489 (7.0) |
| Japan |  | 28 (0.8) | 549 (2.7) | 12 (0.8) | 528 (3.8) |
| Latvia |  | 18 (0.9) | 517 (4.4) | 6 (0.7) | 488 (7.6) |
| Lithuania |  | 34 (1.1) | 526 (3.4) | 13 (0.9) | 491 (5.0) |
| Moldova, Rep. of |  | 31 (1.4) | 502 (6.8) | 30 (1.4) | 477 (6.3) |
| Morocco | $r$ | 26 (1.5) | 352 (5.4) | 60 (2.1) | 352 (6.4) |
| Netherlands |  | 21 (1.1) | 529 (3.0) | 9 (0.8) | 500 (6.5) |
| New Zealand |  | 17 (0.6) | 464 (4.4) | 9 (0.7) | 430 (4.8) |
| Norway |  | 17 (0.8) | 428 (5.6) | 7 (0.5) | 400 (5.4) |
| Philippines |  | 27 (1.1) | 391 (8.7) | 48 (2.1) | 332 (5.2) |
| Russian Federation |  | 27 (1.5) | 522 (5.1) | 10 (0.7) | 499 (8.4) |
| Scotland |  | 20 (1.1) | 469 (4.1) | 11 (0.7) | 445 (5.3) |
| Singapore |  | 22 (0.9) | 569 (4.9) | 11 (0.8) | 528 (8.7) |
| Slovenia |  | 28 (1.1) | 466 (3.7) | 7 (0.6) | 422 (6.1) |
| Tunisia | $r$ | 29 (1.5) | 359 (5.2) | 41 (2.3) | 321 (5.5) |
| United States |  | 22 (0.6) | 496 (2.7) | 13 (0.6) | 473 (3.0) |
| International Avg. |  | 24 (0.2) | 486 (1.0) | 18 (0.2) | 457 (1.2) |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US |  | 19 (1.2) | 515 (3.7) | 10 (0.8) | 490 (6.7) |
| Ontario Province, Can. |  | 16 (1.3) | 494 (4.2) | 7 (0.9) | 463 (5.7) |
| Quebec Province, Can. |  | 27 (0.8) | 496 (2.9) | 11 (0.7) | 478 (4.7) |


| Countries | Have Computer |  | Do Not Have Computer |  | Have Study Desk/Table |  | Do Not Have Study Desk/Table |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 19 (0.7) | 479 (4.4) | 81 (0.7) | 479 (3.3) | 64 (1.1) | 489 (3.1) | 36 (1.1) | 461 (4.0) |
| Australia | 96 (0.3) | 508 (4.6) | 4 (0.3) | 448 (9.6) | 92 (0.5) | 508 (4.8) | 8 (0.5) | 484 (5.8) |
| Bahrain | 81 (0.6) | 407 (1.6) | 19 (0.6) | 379 (3.7) | 80 (0.7) | 407 (1.9) | 20 (0.7) | 382 (3.5) |
| Belgium (Flemish) | 95 (0.5) | 541 (2.7) | 5 (0.5) | 476 (8.7) | 95 (0.4) | 540 (2.7) | 5 (0.4) | 495 (6.2) |
| Botswana | 16 (0.8) | 370 (7.2) | 84 (0.8) | 369 (2.3) | 68 (0.8) | 376 (2.7) | 32 (0.8) | 354 (3.6) |
| Bulgaria | 37 (1.5) | 493 (5.7) | 63 (1.5) | 470 (4.7) | 79 (1.2) | 482 (4.4) | 21 (1.2) | 458 (7.6) |
| Chile | 39 (1.4) | 423 (3.6) | 61 (1.4) | 365 (3.2) | 56 (1.0) | 403 (3.3) | 44 (1.0) | 368 (3.8) |
| Chinese Taipei | 91 (0.8) | 592 (4.4) | 9 (0.8) | 512 (6.0) | 93 (0.5) | 589 (4.5) | 7 (0.5) | 537 (6.9) |
| Cyprus | 82 (0.6) | 470 (1.5) | 18 (0.6) | 417 (4.2) | 95 (0.3) | 464 (1.5) | 5 (0.3) | 391 (6.6) |
| Egypt | 16 (0.8) | 443 (5.5) | 84 (0.8) | 403 (3.6) | 80 (1.0) | 423 (3.4) | 20 (1.0) | 360 (4.0) |
| Estonia | 67 (1.1) | 540 (3.1) | 33 (1.1) | 515 (3.3) | 93 (0.6) | 531 (3.1) | 7 (0.6) | 532 (5.6) |
| Ghana | 24 (1.1) | 272 (6.4) | 76 (1.1) | 284 (4.8) | 60 (1.5) | 298 (4.8) | 40 (1.5) | 258 (5.1) |
| Hong Kong, SAR | 97 (0.3) | 588 (3.3) | 3 (0.3) | 560 (8.5) | 75 (0.8) | 590 (3.4) | 25 (0.8) | 577 (4.0) |
| Hungary | 75 (1.0) | 542 (3.0) | 25 (1.0) | 497 (4.9) | 98 (0.3) | 531 (3.1) | 2 (0.3) | ~~ |
| Indonesia | 17 (1.3) | 431 (5.4) | 83 (1.3) | 412 (4.9) | 75 (1.2) | 418 (4.7) | 25 (1.2) | 393 (5.6) |
| Iran, Islamic Rep. of | 27 (1.4) | 433 (4.0) | 73 (1.4) | 407 (2.3) | 50 (1.6) | 426 (2.5) | 50 (1.6) | 399 (2.7) |
| Israel | 92 (0.7) | 501 (3.4) | 8 (0.7) | 442 (9.3) | 97 (0.3) | 498 (3.5) | 3 (0.3) | 464 (9.4) |
| Italy | 84 (0.7) | 490 (3.2) | 16 (0.7) | 453 (4.4) | 88 (0.6) | 486 (3.2) | 12 (0.6) | 467 (4.8) |
| Japan | 82 (0.8) | 576 (2.1) | 18 (0.8) | 542 (3.1) | 96 (0.3) | 572 (2.0) | 4 (0.3) | 537 (8.0) |
| Jordan | 41 (1.7) | 454 (5.8) | 59 (1.7) | 407 (3.6) | 73 (1.3) | 435 (4.3) | 27 (1.3) | 400 (5.2) |
| Korea, Rep. of | 98 (0.3) | 591 (2.1) | 2 (0.3) | ~ | 97 (0.3) | 592 (2.1) | 3 (0.3) | 516 (9.0) |
| Latvia | 43 (1.6) | 523 (3.4) | 57 (1.6) | 499 (3.5) | 94 (0.6) | 510 (3.3) | 6 (0.6) | 498 (6.3) |
| Lebanon | 59 (1.5) | 444 (3.5) | 41 (1.5) | 419 (3.6) | 71 (1.2) | 440 (3.3) | 29 (1.2) | 418 (3.5) |
| Lithuania | 48 (1.6) | 522 (2.9) | 52 (1.6) | 482 (2.6) | 97 (0.3) | 502 (2.6) | 3 (0.3) | 471 (12.0) |
| Macedonia, Rep. of | 42 (1.6) | 452 (4.9) | 58 (1.6) | 427 (3.4) | 87 (0.8) | 442 (3.6) | 13 (0.8) | 401 (6.5) |
| Malaysia | 57 (1.4) | 525 (4.8) | 43 (1.4) | 487 (3.9) | 87 (0.6) | 511 (4.2) | 13 (0.6) | 489 (5.8) |
| Moldova, Rep. of | 18 (1.0) | 465 (5.7) | 82 (1.0) | 460 (4.1) | 80 (1.2) | 463 (4.2) | 20 (1.2) | 449 (5.2) |
| Morocco | 18 (1.2) | 391 (4.6) | 82 (1.2) | 388 (2.7) | 73 (1.4) | 392 (2.6) | 27 (1.4) | 379 (4.4) |
| Netherlands | 98 (0.3) | 538 (3.9) | 2 (0.3) | ~ ~ | 99 (0.2) | 537 (3.9) | 1 (0.2) | ~ |
| New Zealand | 91 (0.7) | 497 (5.5) | 9 (0.7) | 471 (7.6) | 87 (0.8) | 499 (5.3) | 13 (0.8) | 465 (7.2) |
| Norway | 96 (0.4) | 464 (2.4) | 4 (0.4) | 415 (9.5) | 98 (0.3) | 463 (2.4) | 2 (0.3) | ~~ |
| Palestinian Nat'l Auth. | 41 (1.2) | 409 (4.1) | 59 (1.2) | 380 (3.0) | 77 (1.3) | 396 (3.2) | 23 (1.3) | 377 (4.4) |
| Philippines | 21 (1.1) | 391 (8.1) | 79 (1.1) | 376 (5.1) | 75 (1.1) | 386 (5.4) | 25 (1.1) | 358 (5.6) |
| Romania | 32 (1.9) | 507 (5.8) | 68 (1.9) | 465 (4.6) | 77 (1.8) | 492 (4.3) | 23 (1.8) | 432 (6.9) |
| Russian Federation | 30 (2.0) | 533 (4.8) | 70 (2.0) | 498 (3.6) | 92 (0.5) | 511 (3.8) | 8 (0.5) | 484 (5.9) |
| Saudi Arabia | 57 (1.9) | 342 (5.5) | 43 (1.9) | 320 (3.7) | 61 (1.5) | 341 (5.2) | 39 (1.5) | 321 (4.2) |
| Scotland | 91 (0.7) | 502 (3.7) | 9 (0.7) | 464 (6.3) | 82 (0.8) | 503 (3.8) | 18 (0.8) | 475 (5.3) |
| Serbia | 44 (1.4) | 499 (3.5) | 56 (1.4) | 463 (2.5) | 91 (0.6) | 481 (2.6) | 9 (0.6) | 442 (6.6) |
| Singapore | 94 (0.4) | 610 (3.4) | 6 (0.4) | 538 (7.4) | 91 (0.5) | 609 (3.4) | 9 (0.5) | 570 (6.2) |
| Slovak Republic | 67 (1.2) | 519 (3.5) | 33 (1.2) | 485 (3.7) | 88 (0.8) | 512 (3.3) | 12 (0.8) | 477 (4.9) |
| Slovenia | 86 (0.9) | 498 (2.1) | 14 (0.9) | 469 (4.5) | 97 (0.4) | 494 (2.1) | 3 (0.4) | 455 (11.5) |
| South Africa | 37 (1.3) | 289 (10.6) | 63 (1.3) | 251 (4.3) | 58 (1.5) | 281 (8.5) | 42 (1.5) | 245 (3.6) |
| Sweden | 98 (0.3) | 500 (2.6) | 2 (0.3) | ~ ~ | 98 (0.3) | 500 (2.6) | 2 (0.3) | ~ ~ |
| Tunisia | 22 (1.4) | 432 (4.5) | 78 (1.4) | 404 (2.0) | 73 (1.2) | 415 (2.4) | 27 (1.2) | 398 (2.5) |
| United States | 93 (0.4) | 509 (3.3) | 7 (0.4) | 453 (4.9) | 86 (0.5) | 510 (3.3) | 14 (0.5) | 475 (4.0) |
| \# England | 94 (0.5) | 503 (5.1) | 6 (0.5) | 460 (8.1) | 87 (1.0) | 505 (4.9) | 13 (1.0) | 472 (6.4) |
| International Avg. | 60 (0.2) | 479 (0.7) | 40 (0.2) | 440 (0.9) | 83 (0.1) | 473 (0.6) | 17 (0.1) | 438 (1.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 89 (0.7) | 490 (2.9) | 11 (0.7) | 464 (4.8) | 93 (0.6) | 489 (2.8) | 7 (0.6) | 462 (6.9) |
| Indiana State, US | 92 (0.9) | 511 (5.3) | 8 (0.9) | 479 (8.0) | 84 (0.9) | 512 (5.3) | 16 (0.9) | 490 (7.1) |
| Ontario Province, Can. | 97 (0.4) | 522 (3.0) | 3 (0.4) | 479 (9.1) | 91 (0.7) | 523 (3.0) | 9 (0.7) | 497 (5.4) |
| Quebec Province, Can. | 93 (0.5) | 545 (3.2) | 7 (0.5) | 520 (3.2) | 91 (0.6) | 545 (3.2) | 9 (0.6) | 528 (3.9) |


| Countries | Have Computer |  | Do Not Have Computer |  | Have Study Desk/Table |  | Do Not Have Study Desk/Table |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | 28 (1.2) | 462 (4.5) | 72 (1.2) | 460 (3.8) | 60 (1.5) | 467 (3.9) | 40 (1.5) | 449 (4.2) |
| Australia | 92 (0.9) | 503 (3.8) | 8 (0.9) | 461 (7.1) | 85 (1.1) | 504 (3.6) | 15 (1.1) | 479 (6.8) |
| Belgium (Flemish) | 90 (0.5) | 553 (1.8) | 10 (0.5) | 534 (3.5) | 91 (0.5) | 551 (1.8) | $9(0.5)$ | 547 (3.5) |
| Chinese Taipei | 89 (0.7) | 568 (1.8) | 11 (0.7) | 535 (3.0) | 87 (0.6) | 567 (1.8) | 13 (0.6) | 549 (3.0) |
| Cyprus | 75 (0.7) | 517 (2.6) | 25 (0.7) | 496 (3.5) | 90 (0.5) | 516 (2.4) | 10 (0.5) | 470 (4.3) |
| England | 91 (0.6) | 537 (3.8) | 9 (0.6) | 494 (5.4) | 80 (1.1) | 537 (3.9) | 20 (1.1) | 514 (5.0) |
| Hong Kong, SAR | 85 (1.0) | 577 (3.2) | 15 (1.0) | 565 (3.7) | 71 (1.1) | 574 (3.2) | 29 (1.1) | 578 (3.8) |
| Hungary | 71 (1.2) | 542 (3.0) | 29 (1.2) | 509 (4.1) | 96 (0.5) | 532 (2.9) | 4 (0.5) | 477 (10.5) |
| Iran, Islamic Rep. of | 25 (1.7) | 411 (5.4) | 75 (1.7) | 385 (4.3) | 40 (1.8) | 420 (4.3) | 60 (1.8) | 373 (4.7) |
| Italy | 79 (0.7) | 506 (3.4) | 21 (0.7) | 497 (5.6) | 72 (0.9) | 508 (3.8) | 28 (0.9) | 492 (4.5) |
| Japan | 77 (0.8) | 570 (1.8) | 23 (0.8) | 549 (2.5) | 94 (0.4) | 566 (1.6) | 6 (0.4) | 547 (5.5) |
| Latvia | 42 (1.4) | 545 (3.7) | 58 (1.4) | 533 (3.0) | 91 (0.7) | 537 (2.9) | 9 (0.7) | 526 (5.5) |
| Lithuania | 45 (1.4) | 548 (4.1) | 55 (1.4) | 526 (3.0) | 97 (0.3) | 537 (3.0) | 3 (0.3) | 503 (13.3) |
| Moldova, Rep. of | 20 (1.1) | 507 (6.9) | 80 (1.1) | 507 (4.8) | 81 (1.2) | 509 (5.1) | 19 (1.2) | 488 (5.8) |
| Morocco | 20 (1.2) | 354 (7.4) | 80 (1.2) | 352 (5.2) | 52 (1.8) | 361 (5.8) | 48 (1.8) | 344 (6.1) |
| Netherlands | 93 (0.6) | 543 (2.0) | 7 (0.6) | 511 (6.3) | 94 (0.5) | 542 (2.1) | 6 (0.5) | 524 (6.1) |
| New Zealand | 87 (0.7) | 502 (2.1) | 13 (0.7) | 464 (5.5) | 80 (0.7) | 501 (2.2) | 20 (0.7) | 475 (4.2) |
| Norway | 91 (0.5) | 458 (2.3) | 9 (0.5) | 412 (5.0) | 92 (0.5) | 458 (2.4) | 8 (0.5) | 405 (7.0) |
| Philippines | 26 (1.7) | 400 (16.5) | 74 (1.7) | 348 (5.8) | 69 (1.3) | 372 (7.8) | 31 (1.3) | 338 (9.5) |
| Russian Federation | 23 (1.1) | 540 (6.3) | 77 (1.1) | 530 (4.7) | 83 (0.9) | 535 (4.9) | 17 (0.9) | 521 (5.5) |
| Scotland | 89 (0.8) | 496 (3.2) | 11 (0.8) | 468 (5.1) | 77 (1.1) | 498 (3.1) | 23 (1.1) | 471 (4.7) |
| Singapore | 89 (0.8) | 601 (5.4) | 11 (0.8) | 546 (6.5) | 90 (0.7) | 600 (5.4) | 10 (0.7) | 547 (8.5) |
| Slovenia | 77 (1.0) | 492 (2.9) | 23 (1.0) | 454 (3.8) | 91 (0.6) | 480 (2.7) | 9 (0.6) | 474 (7.0) |
| Tunisia | 26 (1.3) | 365 (6.6) | 74 (1.3) | 336 (4.7) | 64 (1.8) | 357 (5.3) | 36 (1.8) | 325 (6.1) |
| United States | 92 (0.4) | 523 (2.3) | 8 (0.4) | 478 (4.2) | 77 (0.8) | 528 (2.3) | 23 (0.8) | 492 (3.3) |
| International Avg. | 65 (0.2) | 505 (1.1) | 35 (0.2) | 478 (0.9) | 80 (0.2) | 502 (0.8) | 20 (0.2) | 476 (1.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US | 90 (0.8) | 537 (2.8) | 10 (0.8) | 505 (4.8) | 80 (0.9) | 538 (2.8) | 20 (0.9) | 517 (4.6) |
| Ontario Province, Can. | 92 (0.6) | 515 (3.9) | 8 (0.6) | 473 (6.0) | 83 (1.1) | 516 (3.9) | 17 (1.1) | 490 (4.2) |
| Quebec Province, Can. | 89 (0.8) | 509 (2.4) | 11 (0.8) | 484 (4.2) | 86 (0.9) | 511 (2.3) | 14 (0.9) | 480 (4.9) |



[^29]
## Exhibit 4.6: Use of Computer

| Countries | Use Computer Only at Places Other than Home and School |  | Do Not Use Computers at All |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Hong Kong, SAR | 0 (0.1) | ~ ~ | 0 (0.1) | ~ |
| Chinese Taipei | 0 (0.1) | $\sim$ | 0 (0.1) | ~ ~ |
| Australia | 1 (0.1) | ~ ~ | 1 (0.2) | ~ ~ |
| Singapore | 1 (0.1) | $\sim \sim$ | 1 (0.1) | $\sim \sim$ |
| United States | 1 (0.1) | ~ ~ | 1 (0.1) | ~ ~ |
| Netherlands | 0 (0.1) | $\sim \sim$ | 2 (0.3) | $\sim$ |
| Sweden | 1 (0.2) | ~ ~ | 2 (0.3) | ~ ~ |
| Scotland | 1 (0.2) | $\sim \sim$ | 1 (0.2) | $\sim \sim$ |
| Israel | 2 (0.3) | $\sim \sim$ | 1 (0.1) | $\sim \sim$ |
| New Zealand | 2 (0.3) | $\sim \sim$ | 2 (0.3) | $\sim \sim$ |
| Norway | 1 (0.2) | ~ ~ | 2 (0.2) | ~ ~ |
| Cyprus | 2 (0.2) | ~ | 5 (0.4) | 420 (5.3) |
| Belgium (Flemish) | 5 (0.3) | 527 (7.8) | 1 (0.2) | ~ ~ |
| Hungary | 2 (0.4) | $\sim$ | 3 (0.4) | 503 (9.2) |
| Japan | 1 (0.2) | $\sim \sim$ | 2 (0.2) | ~ |
| Slovenia | 3 (0.4) | 450 (6.8) | 4 (0.4) | 454 (7.7) |
| Estonia | 6 (0.5) | 515 (5.9) | 4 (0.5) | 501 (10.0) |
| Lebanon | 14 (1.2) | 408 (4.9) | 10 (1.2) | 417 (4.9) |
| Italy | 5 (0.4) | 448 (7.3) | 9 (0.5) | 456 (5.4) |
| Jordan | 7 (0.8) | 393 (6.9) | 4 (0.5) | 412 (7.7) |
| Korea, Rep. of | 2 (0.2) | ~ ~ | 0 (0.1) | ~ ~ |
| Bahrain | 10 (0.6) | 377 (4.7) | 6 (0.4) | 379 (6.5) |
| Slovak Republic | 13 (0.8) | 480 (3.6) | 12 (1.1) | 476 (4.8) |
| Lithuania | 13 (1.0) | 482 (4.2) | 4 (0.6) | 472 (10.3) |
| Malaysia | 14 (1.0) | 478 (5.1) | 11 (1.1) | 479 (5.1) |
| Palestinian Nat'l Auth. | 13 (1.1) | 379 (4.8) | 10 (0.9) | 397 (5.4) |
| Latvia | 12 (0.9) | 492 (5.7) | 5 (0.7) | 461 (8.0) |
| Chile | 10 (0.7) | 370 (4.5) | 8 (0.6) | 350 (4.9) |
| Egypt | 8 (0.6) | 393 (6.5) | 7 (0.7) | 437 (6.8) |
| South Africa | 27 (1.3) | 247 (5.5) | 28 (2.0) | 258 (5.4) |
| Serbia | 19 (1.2) | 451 (4.3) | 20 (1.1) | 453 (3.5) |
| Moldova, Rep. of | 8 (0.8) | 459 (7.7) | 9 (1.4) | 469 (7.3) |
| Morocco | 28 (1.2) | 393 (3.5) | 20 (1.5) | 393 (4.2) |
| Romania | 24 (1.4) | 460 (4.8) | 20 (1.8) | 453 (5.9) |
| Macedonia, Rep. of | 32 (1.8) | 429 (4.4) | 10 (1.0) | 405 (6.6) |
| Russian Federation | 21 (1.1) | 505 (5.7) | 21 (1.7) | 482 (5.7) |
| Saudi Arabia | 12 (0.7) | 311 (4.8) | 25 (1.9) | 321 (6.5) |
| Philippines | 14 (0.9) | 391 (7.5) | 44 (1.6) | 357 (5.1) |
| Ghana | 26 (1.5) | 285 (7.2) | 34 (2.5) | 291 (6.2) |
| Armenia | 18 (1.1) | 484 (5.0) | 45 (2.1) | 475 (3.0) |
| Indonesia | 19 (1.3) | 372 (7.4) | 40 (2.8) | 407 (6.9) |
| Tunisia | 23 (1.1) | 413 (2.6) | 36 (1.7) | 399 (2.3) |
| Bulgaria | 40 (1.8) | 465 (4.7) | 24 (1.6) | 473 (6.4) |
| Botswana | 5 (0.4) | 376 (7.3) | 61 (2.5) | 374 (2.9) |
| Iran, Islamic Rep. of | 12 (0.8) | 415 (4.5) | 68 (1.7) | 403 (2.5) |
| 末 England | 1 (0.2) | ~ ~ | 1 (0.2) | $\sim \sim$ |
| International Avg. | 10 (0.1) | 422 (1.2) | 14 (0.2) | 420 (1.3) |
| Benchmarking Participants |  |  |  |  |
| Basque Country, Spain | 2 (0.5) | ~ ~ | 1 (0.2) | $\sim \sim$ |
| Indiana State, US | 1 (0.3) | $\sim \sim$ | 1 (0.3) | $\sim \sim$ |
| Ontario Province, Can. | 0 (0.1) | $\sim \sim$ | 0 (0.1) | $\sim \sim$ |
| Quebec Province, Can. | 2 (0.2) | $\sim \sim$ | 1 (0.2) | $\sim \sim$ |

[^30]
## Exhibit 4.6: Use of Computer



| Countries | Use Computer Both at Home and at School |  | Use Computer at Home but Not at School |  | Use Computer at School but Not at Home |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Chinese Taipei | 81 (1.5) | 570 (1.7) | 5 (1.3) | 564 (5.3) | 12 (0.7) | 531 (2.8) |
| Australia | 80 (1.6) | 508 (3.7) | 7 (0.8) | 481 (6.7) | 11 (1.1) | 458 (8.5) |
| England | 79 (1.0) | 540 (3.9) | 8 (0.6) | 516 (7.5) | 11 (0.8) | 489 (5.2) |
| Netherlands | 79 (2.0) | 544 (1.9) | 12 (1.7) | 535 (4.7) | 4 (0.4) | 517 (10.6) |
| Scotland | 78 (1.0) | 497 (3.2) | 8 (0.7) | 463 (7.3) | 12 (0.7) | 470 (5.3) |
| Hong Kong, SAR | 76 (1.3) | 581 (3.2) | 9 (0.9) | 548 (5.6) | 11 (0.9) | 571 (4.6) |
| United States | 73 (1.2) | 530 (2.2) | 12 (0.9) | 503 (5.6) | 11 (0.6) | 477 (4.2) |
| Singapore | 71 (1.4) | 607 (5.4) | 17 (1.0) | 577 (5.7) | 8 (0.6) | 549 (8.4) |
| New Zealand | 71 (1.1) | 507 (2.2) | 12 (0.8) | 479 (5.6) | 13 (0.7) | 459 (5.2) |
| Belgium (Flemish) | 66 (1.4) | 556 (1.8) | 21 (1.5) | 547 (3.4) | 6 (0.6) | 538 (4.9) |
| Norway | 60 (1.7) | 461 (2.4) | 28 (1.6) | 456 (3.4) | 5 (0.5) | 416 (8.5) |
| Japan | 54 (1.1) | 578 (1.9) | 9 (0.7) | 566 (4.8) | 31 (1.0) | 547 (2.7) |
| Cyprus | 36 (1.6) | 522 (3.7) | 27 (1.6) | 519 (4.0) | 16 (0.9) | 493 (3.7) |
| Slovenia | 33 (1.9) | 483 (4.5) | 46 (2.0) | 487 (3.1) | 6 (0.7) | 463 (7.4) |
| Italy | 30 (1.8) | 511 (4.2) | 38 (1.9) | 506 (4.7) | 12 (1.0) | 487 (6.0) |
| Hungary | 24 (2.1) | 550 (5.3) | 43 (2.1) | 535 (3.5) | 9 (1.0) | 500 (7.8) |
| Morocco | 16 (1.2) | 339 (9.1) | 25 (1.8) | 355 (5.9) | 7 (0.7) | 336 (10.0) |
| Philippines | 16 (2.0) | 400 (25.4) | 11 (0.8) | 393 (9.5) | 8 (0.7) | 379 (19.2) |
| Lithuania | 11 (1.2) | 551 (7.2) | 35 (1.5) | 548 (4.0) | 18 (1.6) | 519 (5.1) |
| Latvia | 10 (1.1) | 545 (6.8) | 27 (1.4) | 546 (4.0) | 17 (1.8) | 536 (6.0) |
| Moldova, Rep. of | 8 (0.8) | 455 (12.1) | 14 (1.1) | 507 (8.4) | 10 (1.4) | 508 (7.2) |
| Tunisia | 7 (0.8) | 331 (10.5) | 24 (1.4) | 364 (6.4) | 7 (1.1) | 326 (10.0) |
| Armenia | 6 (0.5) | 441 (7.3) | 30 (1.2) | 454 (4.3) | 9 (1.2) | 455 (6.3) |
| Russian Federation | 4 (0.6) | 524 (13.9) | 20 (1.0) | 537 (6.7) | 11 (1.6) | 528 (7.7) |
| Iran, Islamic Rep. of | 2 (0.4) | ~ | 11 (1.4) | 437 (5.7) | 2 (0.4) | ~ |
| International Avg. | 43 (0.3) | 505 (1.6) | 20 (0.3) | 497 (1.2) | 11 (0.2) | 481 (1.6) |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US | 79 (1.3) | 540 (2.8) | 8 (0.7) | 508 (5.2) | 10 (0.9) | 512 (5.1) |
| Ontario Province, Can. | 78 (2.0) | 517 (3.9) | 12 (1.6) | 500 (8.1) | 7 (0.6) | 482 (5.4) |
| Quebec Province, Can. | 75 (1.5) | 511 (2.6) | 12 (1.1) | 495 (3.8) | 10 (0.7) | 493 (4.6) |

[^31]A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.

## Exhibit 4.6: Use of Computer

| Countries |  | Use Computer Only at Places Other than Home and School |  | Do Not Use Computers at All |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Chinese Taipei |  | 0 (0.1) | $\sim \sim$ | 1 (0.1) | $\sim \sim$ |
| Australia |  | 1 (0.2) | $\sim \sim$ | 1 (0.1) | $\sim \sim$ |
| England |  | 1 (0.2) | $\sim \sim$ | 1 (0.2) | ~ ~ |
| Netherlands |  | 1 (0.2) | $\sim \sim$ | 5 (0.5) | 530 (7.0) |
| Scotland |  | 1 (0.2) | $\sim \sim$ | 1 (0.2) | $\sim \sim$ |
| Hong Kong, SAR |  | 1 (0.2) | $\sim \sim$ | 2 (0.3) | $\sim \sim$ |
| United States |  | 2 (0.2) | $\sim \sim$ | 2 (0.1) | $\sim \sim$ |
| Singapore |  | 2 (0.2) | $\sim \sim$ | 2 (0.2) | $\sim \sim$ |
| New Zealand |  | 3 (0.3) | 443 (8.1) | 2 (0.3) | $\sim \sim$ |
| Belgium (Flemish) |  | 1 (0.2) | ~ ~ | 5 (0.4) | 541 (4.5) |
| Norway |  | 2 (0.3) | $\sim \sim$ | 5 (0.6) | 422 (7.9) |
| Japan |  | 2 (0.3) | $\sim \sim$ | 3 (0.4) | 542 (5.5) |
| Cyprus |  | 8 (0.6) | 481 (5.4) | 14 (0.7) | 504 (4.2) |
| Slovenia |  | 5 (0.6) | 448 (9.0) | 12 (0.9) | 464 (5.5) |
| Italy |  | 8 (0.6) | 490 (9.3) | 12 (0.7) | 497 (7.1) |
| Hungary |  | 12 (0.8) | 495 (5.7) | 12 (0.8) | 526 (4.8) |
| Morocco | $r$ | 15 (1.2) | 353 (6.5) | 37 (3.2) | 353 (7.3) |
| Philippines |  | 9 (0.8) | 374 (10.6) | 56 (2.5) | 341 (5.7) |
| Lithuania |  | 24 (1.1) | 532 (3.7) | 13 (1.0) | 527 (5.1) |
| Latvia |  | 25 (1.5) | 532 (4.0) | 22 (1.6) | 530 (4.0) |
| Moldova, Rep. of |  | 25 (1.6) | 517 (6.7) | 43 (2.5) | 512 (6.5) |
| Tunisia |  | 15 (1.1) | 376 (6.3) | 46 (2.1) | 323 (6.3) |
| Armenia |  | 24 (1.0) | 456 (4.8) | 32 (1.5) | 468 (5.0) |
| Russian Federation |  | 30 (1.4) | 531 (5.9) | 35 (1.6) | 534 (4.8) |
| Iran, Islamic Rep. of |  | 8 (0.9) | 407 (6.6) | 76 (1.9) | 382 (4.3) |
| International Avg. |  | 9 (0.2) | 460 (1.8) | 18 (0.3) | 470 (1.4) |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US |  | 1 (0.2) | $\sim \sim$ | 2 (0.3) | $\sim \sim$ |
| Ontario Province, Can. |  | 2 (0.4) | $\sim \sim$ | 1 (0.2) | $\sim \sim$ |
| Quebec Province, Can. |  | 1 (0.2) | $\sim \sim$ | 2 (0.3) | $\sim \sim$ | some totals may appear inconsistent.

A tilde ( ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.
but not at school, 19 percent using one at school but not at home, and 10 percent at some other place. Fourteen percent of eighth-grade students reported that they do not use a computer at all. At fourth grade, the results were similar to the eighth grade. Forty-three percent of the fourth-grade students reported using a computer both at home and at school, 20 percent at home but not at school, 11 percent at school but not at home, and 9 percent some other place. Eighteen percent reported that they did not use a computer at all.

Interestingly, at both grades, the data indicate that students were somewhat more likely to use a computer at home than at school. Also, it should be highlighted that at both grades percentages of students reporting that they did not use a computer at all varied dramatically across countries. For example at the eighth grade, it varied from 0 percent in several countries (Hong Kong SAR and Chinese Taipei) to about one-third ( 34 to $45 \%$ ) in the Philippines, Ghana, Armenia, Indonesia, and Tunisia to about two-thirds (61-68\%) in Botswana and Iran.

Mathematics achievement was positively related to computer usage, particularly at eighth grade, with average achievement highest among students reporting using computers at home and at school (485 points). Next highest was achievement among students using computers at home but not school (470 points), followed by students using computers at school but not home ( 441 points). Countries with the greatest percentages of eighth-grade students using computers at home and at school included Hong Kong SAR, Chinese Taipei, Australia, England, and Indiana ( $80 \%$ or more), as well as Singapore, the United States, the Netherlands, Sweden, Scotland, Israel, New Zealand, Norway, and Cyprus ( $70 \%$ or more). At the fourth grade, countries with the greatest percentages ( $80 \%$ or more) of students using computers at home and at school included Chinese Taipei and Australia, as well as England, the Netherlands, Scotland, Hong Kong SAR, the United States, Singapore, and New Zealand.

## How Much of Their Out-of-School Time Do Students Spend on Homework During the School Week?

One of the major ways that students can consolidate and extend classroom learning is to spend time out of school studying or doing homework in school subjects. Well-chosen homework assignments can reinforce classroom learning, and, by providing a challenge, can encourage students to extend their understanding of the subject matter. Homework also provides students who are having trouble keeping up with their classmates an opportunity to review material taught in class.

To summarize the amount of time typically devoted to mathematics homework in each country, TIMSS constructed an index of the time students spend doing mathematics homework that assigns students to a high, medium, or low level on the basis of the frequency and amount of mathematics homework they are assigned each week. Students at the high level reported that they were assigned more than 30 minutes of mathematics homework at least 3-4 times per week. Students at the low level were reportedly assigned not more than 30 minutes of mathematics homework twice per week. The middle level included all other response combinations.

Exhibit 4.7 presents the percentages of eighth- and fourth-grade students at the various levels of this index across countries, and their average mathematics achievement. Countries are ordered by the percentage of students at the high level of the index. At the eighth grade across countries, on average, 26 percent of students were at the high level of the time spent on mathematics homework index, 54 percent at the medium level, and 19 percent at the low level. Students at the low level, on average, had lower achievement than the students in the high and medium categories. Countries with the greatest emphasis on homework the eighth grade included Romania, Italy, and the Russian Federation, where 50 percent or more of the students were at the high level of the index. In these countries, homework seems to be an important part of teachers' instructional strategy. In contrast, there seems to be relatively little emphasis on homework in Scotland, Japan, Sweden,

## Exhibit 4.7: Index of Time Students Spend Doing Mathematics Homework (TMH) in a Normal

 School WeekIndex of Time
Students Spend Doing
Mathematics Homework

Index based on students reports on the frequency and amount of mathematics homework they are given. High level indicates more than 30 minutes of mathematics homework assigned 3-4 times a week. Low level indicates no more than 30 minutes of mathematics homework no more than twice a week. Medium level includes all other possible combinations of responses.


## Background data provided by students.

末 Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
A tilde (~) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 4.7: Index of Time Students Spend Doing Mathematics Homework (TMH) in a Normal School Week



| Countries |  | High TMH |  | Medium TMH |  | Low <br> TMH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Singapore |  | 40 (1.5) | 604 (6.0) | 49 (1.3) | 595 (5.8) | 11 (0.6) | 575 (7.2) |
| Russian Federation |  | 38 (1.3) | 531 (5.3) | 59 (1.2) | 537 (4.7) | 2 (0.4) | ~ ~ |
| Armenia | $r$ | 33 (1.3) | 467 (5.1) | 65 (1.3) | 465 (3.5) | 2 (0.3) | ~ ~ |
| Moldova, Rep. of |  | 31 (2.0) | 518 (6.3) | 66 (1.9) | 504 (5.4) | 3 (0.6) | 494 (10.9) |
| Iran, Islamic Rep. of |  | 31 (2.3) | 404 (5.1) | 52 (1.8) | 391 (5.0) | 17 (2.3) | 376 (8.1) |
| Lithuania |  | 29 (1.2) | 527 (3.8) | 66 (1.3) | 545 (3.1) | 5 (0.6) | 510 (10.7) |
| Latvia |  | 25 (1.1) | 525 (4.1) | 71 (1.1) | 546 (2.7) | 4 (0.6) | 517 (9.1) |
| Hong Kong, SAR |  | 24 (1.0) | 575 (3.8) | 71 (0.9) | 580 (3.2) | 5 (0.5) | 530 (5.6) |
| Italy |  | 24 (1.1) | 496 (5.2) | 52 (1.1) | 504 (4.5) | 24 (1.6) | 512 (3.6) |
| Morocco | s | 22 (1.3) | 362 (5.9) | 58 (1.9) | 365 (4.8) | 20 (2.1) | 353 (12.3) |
| Tunisia | s | 22 (2.2) | 373 (8.6) | 50 (2.8) | 365 (6.3) | 28 (3.0) | 365 (8.0) |
| Hungary |  | 17 (0.9) | 515 (4.9) | 78 (1.1) | 538 (3.1) | 5 (0.9) | 535 (10.6) |
| Philippines |  | 17 (0.8) | 349 (7.0) | 52 (1.7) | 362 (6.7) | 31 (1.9) | 372 (15.7) |
| Cyprus |  | 14 (0.6) | 494 (4.6) | 76 (0.9) | 521 (2.4) | 10 (0.6) | 497 (5.3) |
| Slovenia |  | 14 (0.9) | 466 (6.7) | 76 (1.2) | 490 (2.6) | 10 (0.9) | 455 (8.6) |
| United States |  | 12 (0.6) | 504 (4.0) | 63 (1.3) | 524 (2.7) | 25 (1.5) | 520 (3.5) |
| Norway |  | 12 (1.0) | 447 (4.7) | 56 (1.8) | 462 (3.2) | 32 (2.1) | 467 (4.0) |
| Chinese Taipei |  | 11 (0.6) | 546 (3.5) | 62 (1.1) | 569 (2.0) | 27 (1.2) | 561 (2.7) |
| Belgium (Flemish) |  | 9 (0.7) | 538 (3.9) | 48 (1.7) | 549 (2.7) | 43 (2.0) | 557 (2.0) |
| Japan |  | 8 (0.6) | 543 (4.6) | 57 (1.8) | 568 (2.3) | 35 (2.1) | 565 (2.7) |
| New Zealand |  | 7 (0.4) | 489 (6.7) | 41 (1.1) | 491 (3.3) | 52 (1.3) | 504 (3.1) |
| Australia |  | 7 (0.8) | 486 (13.0) | 43 (2.1) | 500 (4.6) | 50 (2.1) | 505 (4.4) |
| Scotland |  | 6 (0.8) | 477 (6.8) | 40 (2.0) | 488 (4.2) | 54 (2.2) | 498 (3.4) |
| England |  | 4 (0.6) | 489 (14.3) | 37 (1.8) | 531 (4.8) | 59 (1.9) | 540 (4.2) |
| Netherlands |  | 1 (0.2) | ~ ~ | 10 (0.8) | 508 (6.6) | 89 (0.9) | 546 (1.8) |
| International Avg. |  | 18 (0.2) | 489 (1.3) | 56 (0.3) | 500 (0.9) | 26 (0.3) | 494 (1.6) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 15 (1.6) | 531 (5.6) | 65 (2.6) | 537 (2.7) | 21 (3.0) | 525 (5.9) |
| Ontario Province, Can. |  | 16 (0.9) | 514 (6.3) | 53 (1.7) | 511 (3.4) | 31 (2.0) | 513 (6.4) |
| Quebec Province, Can. |  | 10 (0.9) | 487 (3.8) | 44 (1.5) | 505 (2.9) | 46 (1.7) | 514 (3.0) |

## Background data provided by students.

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students.

## Exhibit 4.8 How Students Spend Their Leisure Time on a Normal School Day

| Countries | Average Hours Spent Each Day* |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Watch Television and Videos | $\begin{aligned} & \text { Play } \\ & \text { Computer } \\ & \text { Games } \end{aligned}$ | Play or Talk with Friends | Do Jobs at Home | Play Sports | Read a Book for Enjoyment | Use the Internet | Work at a Paid Job |
| Armenia | 1.8 (0.03) | r 0.9 (0.03) | r 1.6 (0.03) | r 0.4 (0.02) | 1.2 (0.03) | 1.6 (0.03) | r 0.7 (0.03) | 1.0 (0.04) |
| Australia | 2.0 (0.03) | 0.9 (0.02) | 1.7 (0.04) | 1.0 (0.02) | 1.6 (0.03) | 0.7 (0.02) | 1.3 (0.04) | 0.4 (0.03) |
| Bahrain | 2.0 (0.03) | 1.2 (0.02) | 1.6 (0.03) | 1.2 (0.02) | 1.5 (0.03) | 0.9 (0.02) | 1.4 (0.03) | 0.6 (0.02) |
| Belgium (Flemish) | 2.1 (0.03) | 1.0 (0.03) | 1.9 (0.03) | 0.9 (0.02) | 1.6 (0.03) | 0.5 (0.01) | 1.3 (0.03) | 0.2 (0.02) |
| Botswana | 1.4 (0.03) | 0.5 (0.02) | 2.1 (0.04) | 2.3 (0.03) | 1.5 (0.02) | 1.8 (0.03) | 0.7 (0.02) | 0.6 (0.03) |
| Bulgaria | 2.5 (0.04) | 1.1 (0.04) | 2.6 (0.05) | 1.5 (0.03) | 1.2 (0.04) | 0.7 (0.03) | 1.0 (0.04) | 0.3 (0.02) |
| Chile | 2.2 (0.02) | 0.7 (0.02) | 2.3 (0.02) | 1.5 (0.02) | 1.8 (0.03) | 0.6 (0.01) | 0.7 (0.02) | 0.3 (0.02) |
| Chinese Taipei | 1.7 (0.03) | 1.4 (0.04) | 1.4 (0.03) | 0.7 (0.01) | 1.0 (0.02) | 1.0 (0.02) | 1.4 (0.04) | 0.2 (0.01) |
| Cyprus | 2.1 (0.03) | 1.3 (0.02) | 2.1 (0.03) | 1.0 (0.03) | 1.7 (0.03) | 0.9 (0.02) | 1.2 (0.02) | 0.6 (0.02) |
| Egypt | 0.8 (0.02) | 0.7 (0.02) | 0.8 (0.02) | 1.3 (0.03) | 1.1 (0.02) | 1.0 (0.02) | 0.6 (0.02) | 0.6 (0.02) |
| Estonia | 2.3 (0.03) | 1.1 (0.03) | 2.8 (0.03) | 1.1 (0.02) | 1.4 (0.03) | 0.7 (0.02) | 1.5 (0.04) | 0.4 (0.02) |
| Ghana | 0.7 (0.02) | 0.6 (0.02) | 1.2 (0.03) | 1.5 (0.03) | 1.3 (0.02) | 1.7 (0.03) | 0.8 (0.03) | 0.8 (0.03) |
| Hong Kong, SAR | 2.3 (0.03) | 2.0 (0.04) | 1.6 (0.03) | 0.7 (0.01) | 1.0 (0.02) | 1.1 (0.02) | 2.0 (0.03) | 0.1 (0.01) |
| Hungary | 2.1 (0.03) | 1.1 (0.03) | 2.2 (0.03) | 1.1 (0.02) | 1.5 (0.03) | 0.8 (0.02) | 0.6 (0.03) | 0.2 (0.02) |
| Indonesia | 1.5 (0.03) | 0.5 (0.02) | 1.3 (0.03) | 2.2 (0.03) | 1.1 (0.02) | 1.1 (0.02) | 0.3 (0.02) | 0.8 (0.03) |
| Iran, Islamic Rep. of | 1.6 (0.03) | 0.4 (0.02) | 1.4 (0.03) | 1.5 (0.03) | 1.4 (0.04) | 1.0 (0.02) | 0.2 (0.02) | 0.7 (0.05) |
| Israel | 2.5 (0.04) | 1.9 (0.03) | 2.3 (0.03) | 1.4 (0.03) | 1.6 (0.03) | 0.9 (0.02) | 1.8 (0.04) | 0.6 (0.02) |
| Italy | 1.8 (0.03) | 1.0 (0.02) | 2.6 (0.03) | 1.1 (0.03) | 1.8 (0.03) | 0.7 (0.02) | 0.6 (0.02) | 0.9 (0.02) |
| Japan | 2.7 (0.03) | 0.9 (0.02) | 1.6 (0.04) | 0.6 (0.01) | 1.3 (0.03) | 0.9 (0.02) | 0.6 (0.02) | 0.1 (0.01) |
| Jordan | 1.5 (0.03) | 0.9 (0.03) | 1.2 (0.03) | 1.3 (0.03) | 1.2 (0.03) | 0.9 (0.02) | 0.6 (0.03) | 0.6 (0.03) |
| Korea, Rep. of | 1.7 (0.03) | 1.5 (0.03) | 1.8 (0.03) | 0.7 (0.01) | 0.7 (0.02) | 0.6 (0.01) | 1.7 (0.03) | 0.1 (0.01) |
| Latvia | 2.4 (0.03) | 1.0 (0.02) | 2.8 (0.03) | 1.6 (0.03) | 1.3 (0.03) | 0.8 (0.03) | 0.8 (0.03) | 0.5 (0.02) |
| Lebanon | 1.8 (0.04) | 1.3 (0.03) | 1.6 (0.04) | 1.3 (0.03) | 1.6 (0.03) | 1.0 (0.02) | 1.0 (0.03) | 0.8 (0.03) |
| Lithuania | 2.1 (0.03) | 1.1 (0.03) | 2.6 (0.04) | 1.6 (0.04) | 1.1 (0.03) | 0.6 (0.02) | 0.7 (0.03) | 0.3 (0.02) |
| Macedonia, Rep. of | 2.3 (0.04) | 1.3 (0.03) | 2.2 (0.03) | 1.6 (0.03) | 1.8 (0.03) | 1.0 (0.02) | 0.9 (0.03) | 0.7 (0.03) |
| Malaysia | 2.1 (0.04) | 0.8 (0.03) | 1.5 (0.03) | 1.7 (0.02) | 1.1 (0.02) | 1.2 (0.02) | 0.6 (0.02) | 0.3 (0.02) |
| Moldova, Rep. of | 1.9 (0.04) | 0.7 (0.03) | 2.0 (0.04) | 2.2 (0.06) | 1.3 (0.03) | 1.1 (0.03) | 0.7 (0.03) | 0.5 (0.03) |
| Morocco | 1.3 (0.04) | 2.3 (0.06) | 1.3 (0.03) | 1.8 (0.03) | 1.5 (0.03) | 1.3 (0.03) | r 2.6 (0.06) | 2.8 (0.06) |
| Netherlands | 2.1 (0.05) | 1.2 (0.04) | 2.0 (0.05) | 0.8 (0.02) | 1.7 (0.04) | 0.5 (0.02) | 1.5 (0.04) | 0.8 (0.05) |
| New Zealand | 2.1 (0.04) | 1.0 (0.04) | 1.8 (0.05) | 1.0 (0.02) | 1.5 (0.03) | 0.7 (0.03) | 1.3 (0.04) | 0.6 (0.03) |
| Norway | 2.2 (0.03) | 1.2 (0.03) | 2.7 (0.03) | 1.0 (0.03) | 1.8 (0.03) | 0.6 (0.02) | 1.2 (0.03) | 0.7 (0.02) |
| Palestinian Nat'l Auth. | 1.2 (0.02) | 0.7 (0.02) | 1.3 (0.03) | 1.5 (0.03) | 1.1 (0.03) | 1.0 (0.02) | 0.5 (0.02) | 0.6 (0.03) |
| Philippines | 1.6 (0.04) | 0.6 (0.02) | 1.7 (0.03) | 1.9 (0.03) | 1.4 (0.02) | 1.2 (0.02) | 0.5 (0.03) | 0.8 (0.04) |
| Romania | 2.0 (0.04) | 0.9 (0.03) | 2.1 (0.03) | 1.7 (0.05) | 1.3 (0.03) | 1.0 (0.03) | 0.8 (0.04) | 0.5 (0.04) |
| Russian Federation | 2.0 (0.03) | 1.0 (0.03) | 2.5 (0.04) | 1.6 (0.03) | 1.3 (0.02) | 1.1 (0.03) | 0.4 (0.02) | 0.2 (0.02) |
| Saudi Arabia | 1.6 (0.05) | 1.1 (0.03) | 1.3 (0.03) | 1.5 (0.04) | 1.2 (0.04) | 0.9 (0.02) | 0.8 (0.05) | 0.8 (0.03) |
| Scotland | 2.2 (0.03) | 1.4 (0.04) | 2.7 (0.03) | 0.8 (0.02) | 1.7 (0.03) | 0.6 (0.02) | 1.4 (0.03) | 0.5 (0.03) |
| Serbia | 2.1 (0.03) | 1.0 (0.03) | 2.1 (0.03) | 1.3 (0.03) | 1.7 (0.03) | 0.8 (0.02) | 0.6 (0.03) | 0.3 (0.02) |
| Singapore | 2.3 (0.02) | 1.4 (0.02) | 1.7 (0.02) | 0.7 (0.02) | 1.4 (0.02) | 0.9 (0.02) | 1.6 (0.02) | 0.2 (0.02) |
| Slovak Republic | 2.5 (0.03) | 1.1 (0.03) | 2.8 (0.03) | 1.5 (0.03) | 1.9 (0.04) | 0.9 (0.02) | 0.6 (0.03) | 0.4 (0.02) |
| Slovenia | 2.2 (0.03) | 1.3 (0.03) | 2.0 (0.03) | 1.2 (0.03) | 1.7 (0.03) | 0.8 (0.02) | 1.1 (0.03) | 0.4 (0.02) |
| South Africa | 1.5 (0.03) | 0.7 (0.02) | 2.0 (0.03) | 1.8 (0.03) | 1.6 (0.02) | 1.6 (0.03) | 0.8 (0.02) | 0.8 (0.02) |
| Sweden | 2.1 (0.03) | 1.1 (0.03) | 2.8 (0.03) | 1.0 (0.02) | 1.6 (0.03) | 0.6 (0.02) | 1.7 (0.04) | 0.4 (0.02) |
| Tunisia | 1.4 (0.02) | 0.8 (0.03) | 1.5 (0.02) | 1.9 (0.03) | 1.5 (0.02) | 1.3 (0.02) | 0.7 (0.02) | 0.6 (0.02) |
| United States | 2.2 (0.03) | 1.1 (0.02) | 2.4 (0.03) | 1.2 (0.02) | 1.8 (0.02) | 0.7 (0.01) | 1.8 (0.03) | 0.6 (0.02) |
| ま England | 2.0 (0.04) | 1.1 (0.04) | 2.4 (0.05) | 0.8 (0.03) | 1.4 (0.05) | 0.5 (0.02) | 1.4 (0.04) | 0.5 (0.04) |
| International Avg. | 1.9 (0.00) | 1.1 (0.00) | 1.9 (0.00) | 1.3 (0.00) | 1.4 (0.00) | 0.9 (0.00) | 1.0 (0.00) | 0.6 (0.00) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 1.6 (0.04) | 0.9 (0.03) | 2.4 (0.04) | 0.9 (0.03) | 1.5 (0.03) | 0.7 (0.02) | 0.8 (0.03) | 0.4 (0.03) |
| Indiana State, US | 2.2 (0.06) | 1.0 (0.04) | 2.4 (0.06) | 1.2 (0.04) | 1.8 (0.04) | 0.7 (0.03) | 1.7 (0.04) | 0.6 (0.05) |
| Ontario Province, Can. | 2.1 (0.04) | 1.2 (0.04) | 2.0 (0.04) | 0.9 (0.02) | 1.7 (0.03) | 0.8 (0.02) | 1.9 (0.04) | 0.6 (0.03) |
| Quebec Province, Can. | 2.0 (0.03) | 1.4 (0.03) | 2.0 (0.04) | 0.9 (0.02) | 1.7 (0.04) | 0.6 (0.02) | 1.5 (0.04) | 0.6 (0.02) |

[^32][^33]| Countries | Average Hours Spent Each Day* |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Watch Television and Videos |  | $\begin{aligned} & \text { Play } \\ & \text { Computer } \\ & \text { Games } \end{aligned}$ |  | ay or Talk with Friends |  | Do Jobs at Home |  | Play Sports |  | Read a Book for Enjoyment |  | the Internet |
| Armenia | r 1.6 (0.04) | $r$ | 1.0 (0.04) | $r$ | 1.3 (0.03) | s | 0.5 (0.05) | $r$ | 1.4 (0.03) | $r$ | 1.9 (0.04) | 5 | 0.5 (0.04) |
| Australia | 1.9 (0.04) |  | 1.1 (0.03) |  | 1.8 (0.04) |  | 1.3 (0.03) |  | 1.8 (0.04) |  | 1.2 (0.03) |  | 0.9 (0.04) |
| Belgium (Flemish) | 1.8 (0.03) |  | 1.0 (0.02) |  | 2.0 (0.03) |  | 1.2 (0.02) |  | 1.6 (0.03) |  | 0.9 (0.02) |  | 0.8 (0.02) |
| Chinese Taipei | 1.3 (0.03) |  | 1.0 (0.03) |  | 1.0 (0.02) |  | 0.9 (0.02) |  | 1.3 (0.02) |  | 1.1 (0.02) |  | 1.0 (0.03) |
| Cyprus | 1.9 (0.03) |  | 1.1 (0.03) |  | 2.1 (0.03) |  | 1.3 (0.03) |  | 1.7 (0.03) |  | 1.2 (0.02) |  | 0.6 (0.02) |
| England | 2.0 (0.04) |  | 1.5 (0.04) |  | 2.1 (0.04) |  | 1.0 (0.03) |  | 1.9 (0.03) |  | 1.0 (0.03) |  | 1.0 (0.03) |
| Hong Kong, SAR | 1.9 (0.03) |  | 1.2 (0.03) |  | 1.2 (0.03) |  | 0.9 (0.02) |  | 1.1 (0.02) |  | 1.0 (0.02) |  | 0.9 (0.03) |
| Hungary | 1.9 (0.03) |  | 1.2 (0.03) |  | 2.2 (0.03) |  | 1.3 (0.03) |  | 1.7 (0.03) |  | 1.0 (0.02) |  | 0.4 (0.02) |
| Iran, Islamic Rep. of | 1.1 (0.04) |  | 0.3 (0.03) |  | 1.2 (0.05) |  | 1.6 (0.05) |  | 1.4 (0.04) |  | 1.3 (0.04) |  | 0.2 (0.02) |
| Italy | 1.4 (0.03) |  | 0.8 (0.02) |  | 1.9 (0.03) |  | 1.3 (0.03) |  | 1.6 (0.02) |  | 0.9 (0.02) |  | 0.4 (0.02) |
| Japan | 2.0 (0.03) |  | 0.9 (0.02) |  | 1.9 (0.03) |  | 0.8 (0.02) |  | 1.3 (0.02) |  | 0.8 (0.02) |  | 0.4 (0.01) |
| Latvia | 2.0 (0.04) |  | 0.9 (0.03) |  | 2.6 (0.04) |  | 1.7 (0.04) |  | 1.5 (0.03) |  | 1.1 (0.03) |  | 0.5 (0.03) |
| Lithuania | 1.7 (0.04) |  | 1.1 (0.03) |  | 2.7 (0.03) |  | 1.8 (0.04) |  | 1.2 (0.03) |  | 1.1 (0.02) |  | 0.5 (0.02) |
| Moldova, Rep. of | 1.6 (0.04) | $r$ | 0.6 (0.03) |  | 1.8 (0.05) |  | 1.9 (0.05) |  | 1.2 (0.03) |  | 1.2 (0.03) | $r$ | 0.4 (0.03) |
| Morocco | r 1.0 (0.05) | $r$ | 0.8 (0.05) | $r$ | 1.2 (0.05) | $r$ | 1.3 (0.04) | $r$ | 1.2 (0.04) | $r$ | 1.1 (0.05) | $r$ | 0.8 (0.04) |
| Netherlands | 1.6 (0.04) |  | 1.2 (0.03) |  | 2.4 (0.05) |  | 0.9 (0.03) |  | 1.7 (0.04) |  | 0.8 (0.03) |  | 0.8 (0.04) |
| New Zealand | 1.9 (0.03) |  | 1.1 (0.03) |  | 1.8 (0.03) |  | 1.3 (0.03) |  | 1.6 (0.03) |  | 1.3 (0.03) |  | 1.0 (0.02) |
| Norway | 1.5 (0.02) |  | 1.0 (0.02) |  | 2.4 (0.04) |  | 1.1 (0.02) |  | 1.5 (0.03) |  | 1.0 (0.03) |  | 0.6 (0.02) |
| Philippines | 1.2 (0.04) |  | 0.8 (0.03) |  | 1.3 (0.03) |  | 1.5 (0.05) |  | 1.4 (0.04) |  | 1.4 (0.04) |  | 0.7 (0.04) |
| Russian Federation | 1.5 (0.03) |  | 0.8 (0.03) |  | 2.2 (0.04) |  | 1.5 (0.03) |  | 1.2 (0.03) |  | 1.2 (0.02) |  | 0.3 (0.02) |
| Scotland | 2.0 (0.04) |  | 1.6 (0.04) |  | 2.1 (0.04) |  | 1.1 (0.03) |  | 2.0 (0.04) |  | 1.0 (0.02) |  | 1.1 (0.03) |
| Singapore | 2.0 (0.02) |  | 1.2 (0.02) |  | 1.2 (0.02) |  | 1.0 (0.03) |  | 1.5 (0.03) |  | 1.3 (0.02) |  | 0.9 (0.02) |
| Slovenia | 1.6 (0.05) |  | 1.3 (0.04) |  | 1.7 (0.04) |  | 1.5 (0.04) |  | 1.9 (0.04) |  | 1.2 (0.03) |  | 0.6 (0.02) |
| Tunisia | r 0.8 (0.03) | $r$ | 0.8 (0.04) | $r$ | 0.9 (0.04) | $r$ | 1.5 (0.04) | $r$ | 1.4 (0.04) | $r$ | 1.3 (0.05) | $r$ | 0.8 (0.05) |
| United States | 2.1 (0.03) |  | 1.1 (0.02) |  | 2.0 (0.02) |  | 1.2 (0.01) |  | 1.9 (0.02) |  | 1.2 (0.02) |  | 1.2 (0.02) |
| International Avg. | 1.7 (0.01) |  | 1.0 (0.01) |  | 1.8 (0.01) |  | 1.3 (0.01) |  | 1.5 (0.01) |  | 1.1 (0.01) |  | 0.7 (0.01) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 2.0 (0.04) |  | 1.1 (0.03) |  | 2.2 (0.03) |  | 1.1 (0.03) |  | 2.0 (0.03) |  | 1.1 (0.03) |  | 1.2 (0.04) |
| Ontario Province, Can. | 2.0 (0.04) |  | 1.2 (0.04) |  | 1.8 (0.05) |  | 1.2 (0.02) |  | 1.7 (0.04) |  | 1.2 (0.03) |  | 1.2 (0.03) |
| Quebec Province, Can. | 1.8 (0.03) |  | 1.2 (0.03) |  | 2.0 (0.04) |  | 1.4 (0.03) |  | 2.2 (0.03) |  | 1.0 (0.02) |  | 1.2 (0.03) |

Background data provided by students.

* Number of hours based on: No time $=0$; Less than 1 hour $=0.5 ; 1-2$ hours $=1.5$; More than 2 but less than 4 hours $=3 ; 4$ or more hours $=4.5$. Activities are not necessarily exclusive; students may have reported engaging in more than one activity at the same time.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An " " " indicates data are available for at least 50 but less than $70 \%$ of the students.
and England, where less than ten percent of students were at the high level of the index.

In general, fourth-grade students reported being given less mathematics homework than did students at the eighth grade. Eighteen percent of fourth-grade students, on average, were at the high level of the index, 56 percent at the middle level, and 26 percent at the low level. Singapore was the country with the highest percentage of students in the high category- 40 percent. Despite this, across countries, fourth-grade students in the medium category had the highest average mathematics achievement. This pattern suggests that, compared with their higher-achieving counterparts, the lower-performing students may be assigned more homework as a remedial strategy in an effort to keep up academically.

To provide a fuller picture of how students spend their out-of-school time on a school day, Exhibit 4.8 gives students' reports on how they spend their daily leisure time. The two most popular activities were watching television or videos and playing or talking with friends (each about two hours per day at eighth grade and a little less at fourth grade). Students reported spending more than one hour per day playing sports and working at jobs at home, and about one hour playing computer games and using the Internet.

## How Confident Are Students in Their Ability to Learn Mathematics?

To investigate how students think of their abilities in mathematics, TIMSS created an index of students' self-confidence in learning mathematics. This index is based on students' responses to four statements about their mathematics ability:

- I usually do well in mathematics;
- Mathematics is more difficult for me than for many of my classmates;*
- Mathematics is not one of my strengths;*
- I learn things quickly in mathematics.

Students who agreed a little or agreed a lot with all four statements, on average, were assigned to the high level of the index, while students who disagreed a little or disagreed a lot with all four, on average, were assigned to the low level. The medium level includes all other possible combinations of responses. The percentages of students at each level of this index, and their average mathematics achievement, are presented in Exhibit 4.9 for both eighth and fourth grades.

On average, internationally, 40 percent of the eighth-grade students had high self-confidence in learning mathematics. The percentages ranged from a high of 59 percent in Israel to a low of 17 percent in Japan. Although there was a clear positive association between selfconfidence in learning mathematics and mathematics achievement, internationally and in every country, at the country level the relationship was more complex. It is noteworthy that the four countries with lowest percentages of students in the high self-confidence category - Chinese Taipei, Hong Kong SAR, Japan, and Korea - all had high average mathematics achievement. Since all of these are Asian Pacific countries, they may share cultural traditions that encourage modest self-confidence.

At fourth grade, on average, internationally, 55 percent of students were at the high level of the self-confidence in learning mathematics index, compared with 33 percent at the medium and just 11 percent at the low. The countries with the greatest percentages included Slovenia, and Cyprus, each with 70 percent or more. Countries with relatively lower percentages included Japan and the Philippines, each with less than 40 percent at the high level. Again, there was a positive relationship, on average, between self-confidence in learning mathematics and mathematics achievement.

| Index of Students' Self-Confidence in Learning Mathematics | Countries | High SCM |  | Medium SCM |  | $\begin{aligned} & \text { Low } \\ & \text { SCM } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on students' responses to four statements about mathematics:1)। usually do well in mathematics; 2) Mathematics is more difficult for me than for many of my classmates (Reversed); 3) Mathematics is not one of my strengths (Reversed); 4) I learn things quickly in mathematics. | Israel | 59 (1.2) | 526 (3.5) | 30 (0.9) | 461 (3.8) | 11 (0.7) | 451 (5.7) |
|  | Egypt | 58 (1.0) | 437 (3.3) | 35 (0.9) | 383 (3.7) | 7 (0.4) | 374 (5.3) |
|  | Scotland | 52 (1.5) | 524 (3.9) | 32 (1.0) | 477 (3.8) | 15 (0.9) | 456 (5.0) |
|  | United States | 51 (0.8) | 534 (3.3) | 29 (0.6) | 483 (3.5) | 20 (0.6) | 461 (3.6) |
|  | Australia | 50 (1.7) | 542 (4.5) | 31 (1.1) | 483 (3.7) | 19 (1.2) | 451 (6.4) |
|  | Jordan | 49 (1.2) | 463 (4.7) | 38 (1.0) | 400 (3.7) | 13 (0.7) | 390 (4.4) |
|  | Sweden | 49 (1.3) | 534 (2.6) | 36 (0.9) | 477 (3.1) | 16 (0.9) | 446 (3.4) |
|  | Norway | 46 (1.1) | 502 (2.0) | 32 (0.8) | 445 (2.9) | 21 (0.8) | 405 (3.4) |
|  | Cyprus | 46 (0.8) | 503 (2.0) | 32 (0.8) | 437 (2.2) | 22 (0.7) | 407 (3.6) |
|  | Italy | 46 (0.9) | 521 (3.3) | 29 (0.9) | 466 (3.6) | 25 (1.0) | 439 (3.4) |
| Average is computed across the four items based on a 4-point scale: 1. Agree a lot; 2. Agree a little; 3. Disagree a little; 4. Disagree a lot. | Belgium (Flemish) | 45 (0.9) | 556 (3.2) | 30 (0.7) | 526 (3.0) | 25 (0.8) | 518 (3.5) |
|  | Netherlands | 45 (1.4) | 557 (4.4) | 33 (1.0) | 527 (4.7) | 23 (1.0) | 511 (4.8) |
|  | Serbia | 44 (1.1) | 530 (2.8) | 26 (0.7) | 458 (3.2) | 30 (1.1) | 422 (3.4) |
|  | Bahrain | 44 (0.9) | 437 (2.0) | 38 (0.9) | 379 (2.4) | 18 (0.6) | 366 (3.2) |
|  | Tunisia | 44 (1.0) | 436 (2.7) | 36 (0.8) | 399 (2.5) | 20 (0.9) | 384 (2.2) |
| Students agreeing a little or a lot on average across the four statements are assigned to the high level. Students disagreeing a little or a lot on average are assigned to the low level. All other students are assigned to the middle level. | Hungary | 44 (1.0) | 574 (3.3) | 32 (1.0) | 507 (3.9) | 24 (0.8) | 479 (3.9) |
|  | Ghana | 43 (1.4) | 306 (5.6) | 44 (1.2) | 265 (4.8) | 12 (0.7) | 265 (7.5) |
|  | Palestinian Nat'I Auth. | 43 (1.0) | 428 (3.9) | 41 (0.9) | 370 (2.9) | 16 (0.6) | 355 (3.6) |
|  | Russian Federation | 43 (1.1) | 548 (3.0) | 30 (0.8) | 492 (4.1) | 27 (0.8) | 466 (4.6) |
|  | New Zealand | 43 (1.4) | 534 (6.4) | 36 (1.1) | 475 (5.4) | 21 (0.9) | 452 (4.1) |
|  | Lebanon | 43 (1.4) | 462 (3.6) | 44 (1.1) | 416 (3.1) | 13 (0.7) | 403 (4.4) |
|  | Saudi Arabia | 41 (1.4) | 361 (4.8) | 43 (1.1) | 321 (5.4) | 16 (0.9) | 303 (5.8) |
|  | Armenia | 41 (1.1) | 505 (4.0) | 40 (1.0) | 468 (3.7) | 19 (0.9) | 462 (4.1) |
|  | Estonia | 41 (0.9) | 569 (3.2) | 32 (0.7) | 520 (3.1) | 28 (0.8) | 489 (3.5) |
|  | Slovak Republic | 40 (1.1) | 556 (3.7) | 35 (1.0) | 487 (3.9) | 25 (1.0) | 462 (4.1) |
|  | Slovenia | 40 (0.9) | 533 (3.2) | 39 (1.0) | 474 (2.5) | 20 (0.9) | 453 (2.8) |
|  | Morocco | 40 (1.3) | 413 (4.1) | 41 (1.4) | 377 (2.6) | 19 (1.2) | 368 (4.5) |
|  | Singapore | $39(0.8)$ | 639 (3.0) | 34 (0.7) | 594 (3.9) | 27 (0.7) | 571 (4.6) |
|  | Malaysia | 39 (1.2) | 546 (4.2) | 45 (1.0) | 490 (3.7) | 16 (0.7) | 471 (4.4) |
|  | Botswana | 38 (0.9) | 390 (2.8) | 45 (0.8) | 361 (2.5) | 17 (0.8) | 352 (3.4) |
|  | South Africa | 37 (0.9) | 300 (8.3) | 48 (0.9) | 242 (3.9) | 15 (0.8) | 255 (9.9) |
|  | Lithuania | 36 (1.0) | 552 (3.1) | 37 (0.9) | 486 (2.8) | 26 (0.9) | 456 (2.7) |
|  | Iran, Islamic Rep. of | 35 (0.9) | 447 (3.5) | 49 (0.8) | 399 (2.6) | 16 (0.7) | 377 (3.4) |
|  | Chile | 35 (0.9) | 427 (3.9) | 42 (0.7) | 369 (3.4) | 23 (0.7) | 361 (3.9) |
|  | Latvia | $34(1.0)$ | 555 (3.4) | 33 (0.9) | 499 (3.2) | 33 (1.0) | 473 (3.4) |
|  | Bulgaria | 33 (1.3) | 519 (5.5) | 39 (1.4) | 467 (4.2) | 28 (1.2) | 445 (4.8) |
|  | Macedonia, Rep. of | 33 (1.0) | 482 (4.0) | 37 (1.0) | 418 (4.7) | 31 (1.0) | 424 (3.9) |
|  | Korea, Rep. of | 30 (0.7) | 650 (2.8) | 36 (0.6) | 592 (2.5) | 34 (0.8) | 534 (2.3) |
|  | Moldova, Rep. of | 30 (1.2) | 494 (5.0) | 50 (0.9) | 451 (4.5) | 20 (1.1) | 441 (5.3) |
|  | Romania | 30 (1.2) | 533 (4.6) | 45 (1.1) | 465 (4.5) | 25 (0.9) | 442 (5.4) |
|  | Hong Kong, SAR | 30 (0.9) | 627 (2.9) | 38 (0.7) | 581 (4.1) | 33 (0.9) | 556 (4.0) |
|  | Philippines | 29 (0.7) | 405 (6.1) | 59 (0.7) | 369 (4.8) | 12 (0.5) | 366 (6.5) |
|  | Indonesia | 27 (1.1) | 420 (6.6) | 59 (0.8) | 408 (4.5) | 15 (0.9) | 416 (4.7) |
|  | Chinese Taipei | 26 (1.0) | 661 (4.1) | 30 (0.7) | 593 (5.1) | 44 (1.1) | 534 (4.0) |
|  | Japan | 17 (0.6) | 634 (3.1) | 38 (0.7) | 580 (2.7) | 45 (0.8) | 538 (2.3) |
|  | F England | 47 (1.5) | 526 (5.8) | 34 (1.2) | 485 (4.7) | 19 (1.1) | 468 (5.5) |
|  | International Avg. | 40 (0.2) | 504 (0.6) | 38 (0.1) | 453 (0.6) | 22 (0.1) | 433 (0.7) |
|  | Benchmarking Participants |  |  |  |  |  |  |
|  | Basque Country, Spain | 46 (1.6) | 518 (3.1) | 29 (1.1) | 471 (3.1) | 24 (1.4) | 449 (2.9) |
|  | Indiana State, US | 50 (1.7) | 536 (6.0) | 28 (1.0) | 493 (4.8) | 22 (1.2) | 470 (4.4) |
|  | Ontario Province, Can. | 63 (1.2) | 549 (3.0) | 22 (0.9) | 484 (3.2) | 15 (0.8) | 460 (3.6) |
|  | Quebec Province, Can. | 59 (1.3) | 566 (3.3) | 24 (0.9) | 521 (2.9) | 16 (0.8) | 498 (3.2) |

[^34]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries |  | High SCM |  | Medium SCM |  | Low <br> SCM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Slovenia |  | 77 (1.0) | 499 (2.6) | 18 (0.8) | 424 (4.2) | 5 (0.5) | 409 (5.8) |
| Cyprus |  | 71 (1.0) | 531 (2.6) | 24 (0.9) | 466 (3.5) | 5 (0.4) | 443 (6.5) |
| Netherlands |  | 67 (1.0) | 556 (2.3) | 22 (0.9) | 516 (2.8) | 11 (0.6) | 498 (4.4) |
| Norway |  | 65 (0.9) | 472 (2.4) | 28 (0.8) | 426 (3.0) | 8 (0.6) | 399 (5.7) |
| United States |  | 64 (0.7) | 541 (2.3) | 25 (0.5) | 486 (2.8) | 11 (0.4) | 475 (2.7) |
| Hungary |  | 64 (0.8) | 556 (3.1) | 26 (0.8) | 487 (3.8) | 9 (0.5) | 473 (5.2) |
| Australia |  | 64 (0.9) | 522 (3.7) | 25 (0.9) | 471 (5.2) | 11 (0.8) | 436 (8.1) |
| Scotland |  | 64 (0.8) | 508 (3.5) | 26 (0.9) | 468 (3.7) | 11 (0.6) | 451 (5.8) |
| Belgium (Flemish) |  | 62 (0.8) | 569 (1.8) | 26 (0.7) | 526 (2.7) | 13 (0.6) | 510 (3.1) |
| Italy |  | 62 (1.0) | 523 (3.9) | 29 (0.8) | 479 (5.0) | 9 (0.5) | 458 (6.1) |
| Lithuania |  | 61 (1.2) | 559 (3.0) | 31 (1.0) | 505 (3.9) | 8 (0.6) | 489 (8.0) |
| England |  | 59 (1.1) | 556 (4.1) | 30 (0.9) | 505 (4.3) | 11 (0.6) | 480 (5.3) |
| Tunisia | r | 56 (1.8) | 367 (4.9) | 37 (1.6) | 321 (5.5) | 7 (0.7) | 305 (9.4) |
| New Zealand |  | 54 (1.1) | 526 (2.5) | 36 (1.0) | 464 (2.9) | 9 (0.5) | 446 (4.3) |
| Morocco | $r$ | 54 (1.8) | 372 (5.0) | 40 (1.5) | 342 (6.4) | 6 (0.6) | 324 (10.6) |
| Russian Federation |  | 53 (1.4) | 558 (4.8) | 32 (1.1) | 513 (5.1) | 15 (0.7) | 500 (5.5) |
| Moldova, Rep. of |  | 52 (1.5) | 535 (5.9) | 40 (1.4) | 478 (4.5) | 8 (0.7) | 461 (8.6) |
| Latvia |  | 50 (1.1) | 566 (3.2) | 34 (0.9) | 513 (3.6) | 16 (0.8) | 492 (4.1) |
| Singapore |  | 49 (1.6) | 629 (5.0) | 35 (1.1) | 573 (5.3) | 16 (0.9) | 540 (6.2) |
| Armenia | s | 43 (1.1) | 495 (4.5) | 44 (1.1) | 453 (4.6) | 13 (0.8) | 446 (5.7) |
| Iran, Islamic Rep. of |  | 42 (1.6) | 418 (4.8) | 51 (1.6) | 374 (4.3) | 7 (0.5) | 349 (8.9) |
| Chinese Taipei |  | 41 (0.9) | 591 (2.2) | 39 (0.9) | 549 (2.2) | 20 (0.6) | 539 (2.1) |
| Hong Kong, SAR |  | 40 (1.1) | 601 (3.1) | 42 (0.9) | 562 (3.6) | 19 (0.8) | 548 (3.7) |
| Japan |  | 39 (0.9) | 600 (2.2) | 40 (0.9) | 550 (2.3) | 21 (0.8) | 532 (2.2) |
| Philippines |  | 34 (1.2) | 395 (11.7) | 53 (1.2) | 351 (6.8) | 12 (0.7) | 326 (7.4) |
| International Avg. |  | 55 (0.2) | 522 (0.9) | 33 (0.2) | 472 (0.9) | 11 (0.1) | 453 (1.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 64 (1.5) | 551 (3.1) | 22 (0.9) | 511 (3.5) | 14 (1.0) | 493 (6.2) |
| Ontario Province, Can. |  | 67 (1.4) | 531 (4.2) | 23 (1.2) | 480 (3.4) | 10 (0.7) | 463 (5.3) |
| Quebec Province, Can. |  | 70 (1.1) | 525 (2.2) | 22 (0.9) | 471 (3.2) | 8 (0.5) | 448 (5.0) |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## What Value Do Students Place on Mathematics?

Students' motivation to learn mathematics can be affected by whether they find the subject enjoyable, place value on the subject, and think it is important for success in school and for future career aspirations. In addition, developing such positive attitudes towards mathematics among students is an important goal of mathematics education in many countries. To gain some understanding about the value eighth- and fourth-grade students place on mathematics, TIMSS created an index of students valuing mathematics. Students were asked to state their agreement with the following seven statements about mathematics:

- I would like to take more mathematics in school;
- I enjoy learning mathematics;
- I think learning mathematics will help me in my daily life;
- I need mathematics to learn other school subjects;
- I need to do well in mathematics to get into the university of my choice;
- I would like a job that involved using mathematics;
- I need to do well in mathematics to get the job I want.

Students who agreed a little or agreed a lot on average with all seven statements were assigned to the high level of the index, while students who on average disagreed a little or disagreed a lot with all seven were assigned to the low level. Students between these extremes were placed in the medium category. The percentages of students at each level of this index, and their average mathematics achievement, are presented in Exhibit 4.10 for both eighth and fourth grades.

Across the participating countries, on average, students generally placed a high value on mathematics, with 55 percent in the high category, and a further 35 percent in the medium category. Only 10 percent of students were in the low category. Countries with large percentages of
students at the high level included Morocco, Botswana, Ghana, Egypt, and Jordan, with 80 percent or more in this category. Among countries where students reported placing less value on mathematics were Korea, Japan, and the Netherlands with less than 20 percent. Since these are countries with high average mathematics achievement, it may be that the students follow a demanding mathematics curriculum, one that leads to high achievement but little enthusiasm for the subject matter. Despite some high percentages for low performing countries and low percentages for high performing countries, students in the high category had higher average mathematics achievement than those in the medium and low categories.

To provide more information on changes from 1995 and 1999 in an important component of the students valuing mathematics index, Exhibit 4.11 displays the percentages of eighth-grade students in 2003, 1999, and 1995 that "agree a lot," "agree a little," or "disagree" that they enjoy learning mathematics. Comparable data at fourth grade are shown for 2003 and 1995 only.

At the eighth grade, on average, internationally, there was a significant increase from 1995 and 1999 in the average percentage of students agreeing a lot that they enjoy learning mathematics, from 17 percent in 1995 to 25 percent in 1999 to 29 percent in 2003. Nevertheless, the upward trend from 1995 to 1999 in the percentage of students agreeing a lot that they enjoy learning mathematics appears to have leveled somewhat off in 2003. Participants showing a significant increase in 2003 over either 1995 or 1999 included Australia, Belgium (Flemish), Chile, Hungary, Iran, Japan, Jordan, Korea, Lithuania, Macedonia, Moldova, New Zealand, the Russian Federation, Singapore, the Slovak Republic, Tunisia, the United States, Ontario, and Quebec. At fourth grade, the average percentage of students agreeing a lot that they enjoy learning mathematics increased from 46 percent in 1995 to 50 percent in 2003. Countries showing a significant increase included Australia, Hungary, Iran, Japan, New Zealand, Norway, Singapore, and the United States.

Index of Students' Valuing Mathematics

Index based on students' responses to seven statements about mathematics: 1) I would like to take more mathematics in school; 2) I enjoy learning mathematics; 3) I think learning mathematics will help me in my daily life; 4) I need mathematics to learn other school subjects; 5) I need to do well in mathematics to get into the university of my choice; 6) I would like a job that involved using mathematics; 7) I need to do well in mathematics to get the job I want.

Average is computed across the seven items based on a 4 point scale: 1. Agree a lot; 2. Agree a little; 3. Disagree a little; 4. Disagree a lot.

Students agreeing a little or a lot on average across the seven statements are assigned to the high level. Students disagreeing a little or a lot on average are assigned to the low level. All other students are assigned to the middle level.

| Countries | High SVM |  | Medium SVM |  | Low <br> SVM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Morocco | 85 (1.0) | 391 (2.6) | 12 (0.8) | 377 (5.2) | 3 (0.4) | 380 (9.8) |
| Botswana | 84 (0.7) | 378 (2.7) | 14 (0.7) | 331 (2.8) | 2 (0.2) | ~~ |
| Ghana | 82 (1.2) | 293 (4.8) | 16 (1.1) | 227 (4.8) | 1 (0.2) | ~ |
| Egypt | 82 (0.7) | 418 (3.3) | 16 (0.7) | 386 (4.7) | 2 (0.3) | ~ ~ |
| Jordan | 81 (0.9) | 436 (3.8) | 16 (0.8) | 398 (8.0) | 3 (0.3) | 395 (8.1) |
| Tunisia | 79 (0.9) | 417 (2.2) | 17 (0.7) | 395 (3.2) | 4 (0.4) | 385 (3.8) |
| South Africa | 79 (0.9) | 271 (5.6) | 17 (0.8) | 243 (9.1) | 4 (0.3) | 241 (11.4) |
| Malaysia | 78 (1.0) | 515 (4.1) | 21 (0.9) | 486 (5.0) | 1 (0.1) | ~ ~ |
| Palestinian Nat'l Auth. | 77 (1.0) | 403 (3.1) | 19 (0.9) | 355 (4.2) | 4 (0.4) | 344 (8.5) |
| Philippines | 73 (1.1) | 390 (5.1) | 25 (1.0) | 347 (6.1) | 2 (0.2) | ~~ |
| Indonesia | 71 (1.1) | 411 (5.1) | 28 (1.1) | 415 (4.4) | 1 (0.1) | ~ ~ |
| Lebanon | 71 (1.2) | 442 (3.2) | 24 (1.1) | 413 (5.0) | 4 (0.4) | 409 (7.4) |
| Iran, Islamic Rep. of | 70 (0.9) | 415 (2.6) | 24 (0.8) | 407 (3.1) | 6 (0.4) | 393 (6.1) |
| Bahrain | 70 (0.9) | 407 (2.2) | 25 (0.7) | 393 (2.5) | 6 (0.5) | 381 (6.0) |
| Chile | 66 (1.0) | 388 (3.6) | 29 (0.9) | 385 (3.7) | 5 (0.3) | 389 (6.0) |
| Singapore | 63 (0.8) | 616 (3.4) | 32 (0.6) | 592 (4.0) | 5 (0.3) | 558 (7.9) |
| Saudi Arabia | 63 (1.5) | 339 (5.2) | 26 (1.0) | 330 (4.4) | 11 (0.8) | 323 (5.7) |
| Moldova, Rep. of | 61 (1.4) | 468 (4.4) | 35 (1.2) | 452 (4.7) | 4 (0.5) | 441 (11.5) |
| Armenia | 59 (1.1) | 488 (3.7) | 30 (0.9) | 473 (3.4) | 11 (0.7) | 469 (5.4) |
| United States | 58 (0.8) | 512 (3.6) | 34 (0.7) | 498 (3.4) | 8 (0.4) | 485 (4.6) |
| Israel | 56 (1.3) | 499 (4.1) | 35 (1.1) | 500 (4.2) | 9 (0.6) | 487 (5.5) |
| New Zealand | 56 (1.3) | 499 (5.3) | 36 (1.2) | 493 (6.0) | 8 (0.7) | 480 (6.9) |
| Russian Federation | 55 (1.1) | 522 (4.3) | 39 (1.0) | 496 (3.3) | 7 (0.5) | 482 (4.6) |
| Macedonia, Rep. of | 55 (1.0) | 437 (4.1) | 31 (0.8) | 443 (4.4) | 14 (0.8) | 443 (4.9) |
| Scotland | 54 (1.3) | 503 (4.1) | 37 (1.0) | 497 (3.9) | 9 (0.7) | 479 (6.6) |
| Cyprus | 53 (0.8) | 476 (2.2) | 36 (0.9) | 443 (2.6) | 11 (0.5) | 439 (4.4) |
| Lithuania | 53 (1.0) | 515 (2.7) | 40 (1.0) | 489 (3.2) | 7 (0.4) | 473 (4.4) |
| Romania | 53 (1.3) | 493 (5.0) | 35 (1.1) | 469 (4.5) | 12 (0.8) | 451 (8.4) |
| Australia | 51 (1.3) | 517 (4.9) | 37 (1.0) | 499 (4.9) | 12 (0.6) | 481 (7.4) |
| Latvia | 50 (1.2) | 519 (3.9) | 43 (1.0) | 502 (3.3) | 8 (0.6) | 484 (6.6) |
| Bulgaria | 48 (1.5) | 488 (4.7) | 39 (1.1) | 472 (5.0) | 14 (1.1) | 461 (5.9) |
| Slovak Republic | 47 (1.3) | 519 (3.9) | 44 (1.2) | 500 (3.8) | 9 (0.5) | 498 (4.7) |
| Hungary | 47 (1.0) | 540 (3.8) | 44 (0.9) | 519 (3.7) | 9 (0.6) | 527 (5.3) |
| Norway | 45 (1.2) | 475 (3.0) | 42 (1.0) | 458 (2.2) | 13 (0.8) | 432 (4.4) |
| Serbia | 43 (1.2) | 488 (3.5) | 39 (1.0) | 473 (3.1) | 18 (0.9) | 471 (4.3) |
| Estonia | 38 (1.2) | 540 (3.6) | 49 (1.1) | 531 (3.5) | 13 (0.7) | 508 (4.0) |
| Hong Kong, SAR | 35 (1.0) | 607 (3.4) | 55 (0.8) | 581 (3.4) | 10 (0.5) | 544 (6.1) |
| Italy | 32 (1.0) | 505 (3.9) | 52 (0.9) | 480 (3.4) | 16 (0.8) | 454 (3.7) |
| Belgium (Flemish) | 29 (1.0) | 557 (3.7) | 47 (0.8) | 535 (2.7) | 24 (0.9) | 521 (3.7) |
| Sweden | 29 (1.1) | 514 (3.8) | 60 (1.1) | 496 (2.8) | 11 (0.7) | 479 (3.5) |
| Chinese Taipei | 25 (1.0) | 630 (5.3) | 50 (0.8) | 587 (4.7) | 24 (1.0) | 536 (5.0) |
| Slovenia | 25 (1.1) | 510 (3.7) | 58 (1.0) | 491 (2.6) | 17 (1.0) | 478 (3.5) |
| Korea, Rep. of | 18 (0.7) | 633 (3.4) | 59 (0.7) | 593 (2.5) | 23 (0.8) | 546 (2.9) |
| Japan | 17 (0.6) | 597 (3.1) | 61 (0.8) | 574 (2.2) | 22 (0.8) | 539 (3.3) |
| Netherlands | 16 (1.0) | 526 (7.9) | 59 (1.3) | 540 (4.1) | 25 (1.2) | 534 (4.3) |
| き England | 39 (1.5) | 508 (6.2) | 46 (1.3) | 500 (4.8) | 15 (0.8) | 486 (6.7) |
| International Avg. | 55 (0.2) | 479 (0.6) | 35 (0.1) | 458 (0.6) | 10 (0.1) | 458 (1.0) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 42 (1.7) | 500 (3.3) | 39 (1.2) | 484 (3.3) | 19 (1.0) | 467 (3.5) |
| Indiana State, US | 57 (1.6) | 518 (6.3) | 34 (1.3) | 500 (4.3) | 9 (0.9) | 487 (5.7) |
| Ontario Province, Can. | 69 (1.4) | 532 (3.3) | 25 (1.0) | 501 (3.7) | 6 (0.7) | 481 (5.1) |
| Quebec Province, Can. | 55 (1.1) | 551 (3.6) | 39 (0.9) | 536 (2.9) | 6 (0.4) | 519 (5.1) |

[^35]A tilde (~) indicates insufficient data to report achievement.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries | Agree A Lot |  |  |  |  | Agree A Little |  |  |  |  | Disagree |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2003 <br> Percent of Students |  |  | 1995 Percent of Students |  | $2003$ <br> Percent of Students |  |  |  |  | 2003 <br> Percent of Students | 1999 Percent of Students |  | 1995 Percent Student |  |
| Armenia | 45 (1.2) | $\checkmark>$ |  | $\checkmark>$ |  | 28 (0.8) | $\checkmark>$ |  | $\checkmark>$ |  | 28 (1.1) | $\checkmark>$ |  | ২ $\downarrow$ |  |
| Australia | 18 (1.2) | -- |  | 13 (0.7) | 0 | 39 (1.0) | -- |  | 52 (0.6) | ( | 42 (1.4) | - |  | 35 (0.9) | 0 |
| Bahrain | 40 (0.9) | >> |  | \gg |  | 33 (0.9) | ১ > |  | ১ > |  | 26 (1.0) | >> |  | ১ > |  |
| Belgium (Flemish) | 20 (0.9) | 14 (0.6) | 0 | 14 (1.0) | 0 | 37 (0.9) | 37 (0.8) |  | 41 (1.2) | - | 43 (1.3) | 49 (1.0) | ( | 45 (1.3) |  |
| Botswana | 65 (1.0) | $\checkmark>$ |  | $\checkmark>$ |  | 22 (0.8) | $\checkmark>$ |  | ১ $\downarrow$ |  | 14 (0.7) | $\checkmark>$ |  | ১ ১ |  |
| Bulgaria | 22 (1.1) | 21 (1.4) |  | - |  | 39 (1.1) | 35 (1.2) | 0 | -- |  | 38 (1.5) | 44 (2.1) | (7) | - |  |
| Chile | 34 (1.1) | 30 (1.1) | 0 | ৪ |  | 37 (0.7) | 45 (0.7) | (1) | ১ ৪ |  | 30 (1.2) | 26 (1.0) | 0 | ১ ৪ |  |
| Chinese Taipei | 13 (0.6) | 16 (0.7) | (7) | $\checkmark>$ |  | 29 (1.0) | 42 (0.7) | (1) | $\checkmark>$ |  | 58 (1.4) | 42 (1.0) | 0 | $\checkmark>$ |  |
| Cyprus | 36 (0.8) | 38 (1.2) |  | 38 (1.1) |  | 34 (0.9) | 46 (1.0) | (1) | 45 (0.8) | ( | 30 (0.7) | 17 (1.0) | 0 | 17 (0.9) | 0 |
| Egypt | 61 (1.0) | ৪ |  | $\checkmark>$ |  | 27 (0.8) | $\checkmark>$ |  | $\checkmark>$ |  | 12 (0.6) | $\checkmark>$ |  | ২ |  |
| Estonia | 14 (0.7) | $\triangleleft \stackrel{ }{*}$ |  | $\checkmark \stackrel{\text { d }}{ }$ |  | 39 (0.8) | $\diamond \stackrel{\text { d }}{ }$ |  | $\diamond \stackrel{\text { d }}{ }$ |  | 48 (1.0) | $\checkmark>$ |  | $\diamond \stackrel{\text { d }}{ }$ |  |
| Ghana | 53 (1.2) | $\checkmark>$ |  | $\checkmark>$ |  | 30 (0.8) | $\checkmark>$ |  | $\checkmark>$ |  | 16 (0.9) | $\checkmark>$ |  | $\checkmark>$ |  |
| Hong Kong, SAR | 15 (0.7) | 19 (0.7) | (1) | 15 (0.8) |  | 45 (1.0) | 50 (0.8) | (1) | 50 (1.1) | - | 41 (1.1) | 31 (1.1) | 0 | 35 (1.3) | 0 |
| Hungary | 17 (0.9) | 8 (0.5) | 0 | 8 (0.7) | 0 | 36 (0.9) | 30 (1.1) | 0 | 31 (1.2) | 0 | 47 (1.2) | 62 (1.2) | (7) | 61 (1.3) | - |
| Indonesia | 21 (0.9) | 25 (1.4) | - | $\checkmark>$ |  | 62 (0.9) | 67 (1.2) | (1) | $\checkmark>$ |  | 17 (0.9) | 7 (0.6) | 0 | $\checkmark>$ |  |
| Iran, Islamic Rep. of | 58 (1.0) | 50 (0.9) | 0 | 39 (1.2) | 0 | 26 (0.8) | 40 (0.9) | - | 43 (1.2) | © | 16 (0.7) | 11 (0.6) | 0 | 18 (1.1) |  |
| Israel | 27 (1.1) | 31 (1.4) | - | - - |  | 34 (0.8) | 42 (0.9) | (1) | - - |  | 39 (1.1) | 28 (1.4) | 0 | - - |  |
| Italy | 16 (0.8) | 21 (0.9) | ( | -- |  | 43 (1.2) | 45 (1.1) |  | - - |  | 41 (1.2) | 34 (1.3) | 0 | - - |  |
| Japan | 9 (0.6) | 6 (0.4) | 0 | 5 (0.3) | 0 | 30 (0.8) | 33 (1.0) | (1) | 41 (1.3) | ( | 61 (1.1) | 61 (1.1) |  | 54 (1.5) | 0 |
| Jordan | 50 (1.3) | 46 (1.2) | 0 | $\checkmark>$ |  | 31 (1.0) | 37 (0.8) | (1) | $\checkmark>$ |  | 19 (1.0) | 18 (0.9) |  | $\checkmark>$ |  |
| Korea, Rep. of | 9 (0.5) | 5 (0.3) | 0 | 8 (0.6) |  | 34 (0.8) | 27 (0.7) | 0 | 33 (1.0) |  | 57 (1.0) | 68 (0.7) | - | 59 (1.1) |  |
| Latvia | 14 (0.9) | - - |  | - - |  | 33 (0.9) | - - |  | - - |  | 53 (1.3) | - - |  | - - |  |
| Lebanon | 50 (1.4) | $\checkmark>$ |  | $\checkmark>$ |  | 28 (1.0) | $\checkmark>$ |  | $\checkmark>$ |  | 23 (1.0) | $\checkmark>$ |  | $\checkmark>$ |  |
| Lithuania | 18 (0.9) | 13 (0.9) | 0 | 12 (0.9) | 0 | 36 (0.9) | 46 (1.3) | (1) | 33 (1.3) |  | 46 (1.2) | 40 (1.5) | 0 | 55 (1.3) | - |
| Macedonia, Rep. of | 36 (1.1) | 29 (0.9) | 0 | $\checkmark>$ |  | 31 (0.9) | 39 (0.9) | (1) | $\checkmark>$ |  | 33 (1.0) | 33 (1.1) |  | ১ ৪ |  |
| Malaysia | 41 (1.1) | 43 (1.0) |  | $\checkmark>$ |  | 45 (0.9) | 50 (0.9) | (1) | ১ |  | 14 (0.7) | 6 (0.4) | 0 | ২ |  |
| Moldova, Rep. of | 23 (1.0) | 18 (1.0) | 0 | $\checkmark>$ |  | 51 (1.1) | 49 (1.2) |  | $\diamond \diamond$ |  | 26 (1.2) | 33 (1.4) | $\bigcirc$ | ২ |  |
| Morocco | 60 (1.5) | -- |  | $\checkmark>$ |  | 23 (1.0) | - - |  | $\checkmark>$ |  | 17 (0.9) | - |  | $\checkmark>$ |  |
| Netherlands | 6 (0.5) | 14 (1.1) | (1) | 10 (1.1) | (1) | 26 (1.2) | 44 (1.4) | (1) | 46 (1.9) | ( | 69 (1.4) | 43 (1.8) | 0 | 44 (2.4) | 0 |
| New Zealand | 23 (1.2) | 20 (1.0) | 0 | 20 (1.0) | 0 | 38 (1.1) | 53 (0.9) | (1) | 54 (0.9) | ( | 39 (1.3) | 27 (1.1) | 0 | 26 (1.0) | 0 |
| Norway | 22 (1.0) | $\checkmark>$ |  | 20 (0.9) |  | 40 (0.9) | $\diamond \diamond$ |  | 55 (1.0) | (-) | 38 (1.3) | $\diamond \diamond$ |  | 24 (1.1) | 0 |
| Palestinian Nat'l Auth. | 45 (1.2) | $\checkmark>$ |  | $\checkmark>$ |  | 33 (0.9) | $\checkmark>$ |  | $\diamond>$ |  | 22 (1.0) | $\checkmark>$ |  | ২ |  |
| Philippines | 38 (0.9) | 45 (1.0) | (1) | $\checkmark>$ |  | 44 (0.7) | 46 (1.0) |  | ১> |  | 18 (0.8) | 9 (0.6) | 0 | ২ ১ |  |
| Romania | 21 (1.0) | 19 (0.9) |  | 25 (1.1) | (\%) | 39 (1.0) | 49 (1.1) | (1) | 48 (1.1) | ( 7 | 39 (1.2) | 32 (1.4) | 0 | 27 (1.2) | 0 |
| Russian Federation | 17 (0.7) | 16 (0.8) |  | 14 (0.8) | 0 | 38 (1.0) | 41 (1.2) | - | 40 (1.3) |  | 45 (1.2) | 43 (1.5) |  | 46 (1.4) |  |
| Saudi Arabia | 34 (1.5) | $\checkmark>$ |  | $\checkmark>$ |  | 34 (1.0) | $\checkmark>$ |  | $\checkmark>$ |  | 32 (1.4) | $\checkmark>$ |  | ১ |  |
| Scotland | 18 (0.8) | $\checkmark>$ |  | -- |  | 40 (1.2) | ১ ৪ |  | -- |  | 42 (1.5) | ৪ |  | -- |  |
| Serbia | 23 (1.1) | $\checkmark>$ |  | $\checkmark>$ |  | 29 (0.8) | $\diamond>$ |  | $\checkmark>$ |  | 49 (1.2) | $\checkmark>$ |  | $\checkmark>$ |  |
| Singapore | 33 (0.7) | 28 (0.9) | 0 | 25 (1.0) | 0 | 42 (0.7) | 52 (0.9) | (1) | 53 (0.8) | ( | 25 (0.8) | 20 (1.0) | 0 | 22 (1.0) | 0 |
| Slovak Republic | 13 (0.9) | 11 (0.8) |  | 10 (0.6) | 0 | 40 (1.2) | 48 (1.2) | (1) | 48 (1.2) | ( | 47 (1.4) | 41 (1.5) | 0 | 42 (1.3) | 0 |
| Slovenia | 7 (0.6) | - - |  | 10 (0.7) | (1) | 28 (1.1) | - - |  | 39 (1.4) | ( | 65 (1.2) | - - |  | 51 (1.6) | 0 |
| South Africa | 56 (1.2) | 54 (1.1) |  | - - |  | 24 (0.8) | 34 (1.0) | (1) | - |  | 20 (1.0) | 12 (0.6) | 0 | -- |  |
| Sweden | 15 (0.9) | $\checkmark>$ |  | 17 (1.1) |  | 51 (1.1) | $\checkmark>$ |  | 57 (1.2) | ( | 34 (1.3) | $\checkmark>$ |  | 26 (1.2) | 0 |
| Tunisia | 45 (1.1) | 38 (1.0) | 0 | $\checkmark>$ |  | 31 (0.8) | 44 (0.8) | (1) | $\checkmark>$ |  | 24 (1.0) | 18 (0.8) | 0 | ২ |  |
| United States | 22 (0.6) | 22 (0.9) |  | 20 (0.7) | 0 | 38 (0.7) | 47 (0.6) | (1) | 50 (0.9) | ( | 40 (0.8) | 31 (1.1) | 0 | 30 (0.9) | 0 |
| \# England | 14 (1.1) | 25 (1.1) | (7) | 22 (1.1) | ( 7 | 39 (1.2) | 54 (1.2) | (1) | 59 (1.5) | ( | 47 (1.5) | 21 (1.0) | 0 | 20 (1.3) | 0 |
| International Avg. | 29 (0.1) | 25 (0.2) | © | 17 (0.2) | © | 36 (0.1) | 44 (0.2) | $\bigcirc$ | 46 (0.3) | $\bigcirc$ | 35 (0.2) | 31 (0.2) | © | 37 (0.3) | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 18 (1.3) | $\checkmark>$ |  | $\diamond>$ |  | 31 (1.4) | $\checkmark>$ |  | $\checkmark>$ |  | 51 (1.8) | $\checkmark>$ |  | ২ ৪ |  |
| Indiana State, US | 22 (1.0) | 19 (1.4) |  | $\checkmark>$ |  | 37 (1.2) | 50 (1.1) | (1) | $\checkmark>$ |  | 41 (1.5) | 30 (1.8) | 0 | $\checkmark$ - |  |
| Ontario Province, Can. | 30 (1.1) | 27 (1.4) | 0 | 24 (1.2) | 0 | 40 (1.1) | 47 (1.1) | (1) | 54 (1.5) | ( | 30 (1.3) | 26 (1.2) | 0 | 22 (1.6) | 0 |
| Quebec Province, Can. | 19 (0.8) | 10 (2.3) | 0 | 20 (2.3) |  | 52 (0.9) | 37 (4.2) | 0 | 51 (1.8) |  | 28 (1.1) | 53 (2.3) |  | 28 (2.1) |  |

- 2003 significantly higher
(7) 2003 significantly lower

Background data provided by students.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia, Latvia, Morocco, and Slovenia, and 1995 data are not shown for Israel, Italy, Latvia, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995.

[^36]
## Exhibit 4.11: Trends in "I Enjoy Learning Mathematics"



| Countries | Agree A Lot |  |  | Agree A Little |  |  | Disagree |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2003 <br> Percent of Students | $1995$ <br> Percent of Students |  | 2003 <br> Percent of Students | $1995$ <br> Percent of Students |  | $2003$ <br> Percent of Students |  |  |
| Armenia | 71 (1.1) | $\checkmark$ - |  | 8 (0.7) | $\checkmark>$ |  | 20 (0.9) | $\checkmark>$ |  |
| Australia | 52 (1.4) | 41 (1.1) | 0 | 27 (1.2) | 42 (0.9) | ( $\downarrow$ | 20 (0.9) | 17 (0.7) | 0 |
| Belgium (Flemish) | 27 (0.8) | $\checkmark>$ |  | 38 (0.7) | ২ ৪ |  | 35 (1.2) | ৪ |  |
| Chinese Taipei | 31 (0.9) | $\checkmark>$ |  | 35 (0.8) | $\rangle>$ |  | 34 (1.0) | $\checkmark>$ |  |
| Cyprus | 57 (1.2) | 73 (1.2) | (1) | 24 (0.7) | 22 (1.1) |  | 19 (0.9) | 5 (0.5) | 0 |
| England | 43 (1.2) | 53 (1.4) | (1) | 27 (0.8) | 31 (1.0) | - | 30 (1.3) | 16 (1.0) | 0 |
| Hong Kong, SAR | 30 (1.2) | 34 (1.6) | (1) | 42 (0.8) | 49 (1.2) | (1) | 28 (1.0) | 17 (1.0) | 0 |
| Hungary | 49 (1.3) | 32 (1.3) | 0 | 27 (0.9) | 45 (1.2) | ( | 24 (1.2) | 23 (1.5) |  |
| Iran, Islamic Rep. of | 81 (1.4) | 72 (1.7) | 0 | 11 (1.1) | 22 (1.3) | (1) | 7 (0.8) | 5 (0.7) |  |
| Italy | 40 (1.2) | - - |  | 41 (0.9) | -- |  | 19 (1.0) | - |  |
| Japan | 29 (1.0) | 16 (0.8) | 0 | 36 (0.8) | 56 (1.0) | (1) | 35 (1.2) | 28 (1.1) | 0 |
| Latvia | 49 (1.1) | - - |  | 30 (0.8) | - - |  | 21 (0.9) | - - |  |
| Lithuania | 58 (1.0) | ৪ ৪ |  | 25 (0.8) | $\checkmark>$ |  | 17 (0.8) | $\checkmark>$ |  |
| Moldova, Rep. of | 49 (1.3) | ২১ |  | 38 (1.1) | $\stackrel{\rightharpoonup}{*}$ |  | 12 (0.8) | $\rangle>$ |  |
| Morocco | 71 (1.5) | $\checkmark \diamond$ |  | 18 (1.2) | $\checkmark>$ |  | 11 (0.7) | $\checkmark>$ |  |
| Netherlands | 30 (1.3) | 28 (1.2) |  | 39 (1.0) | 40 (1.3) |  | 31 (1.4) | 32 (1.5) |  |
| New Zealand | 52 (1.1) | 45 (1.4) | 0 | 29 (1.0) | 37 (1.2) | $\stackrel{\rightharpoonup}{*}$ | 19 (0.7) | 18 (1.0) |  |
| Norway | 52 (1.5) | 52 (1.9) |  | 28 (0.9) | 34 (1.4) | - | 20 (1.1) | 14 (1.2) | 0 |
| Philippines | 50 (1.6) | $\checkmark\rangle$ |  | 30 (1.2) | $\checkmark\rangle$ |  | 20 (1.2) | $\checkmark>$ |  |
| Russian Federation | 50 (1.3) | $\checkmark>$ |  | 29 (1.1) | $\checkmark>$ |  | 21 (1.0) | $\checkmark>$ |  |
| Scotland | 50 (1.3) | -- |  | 26 (1.0) | -- |  | 24 (1.1) | -- |  |
| Singapore | 57 (0.8) | 48 (1.0) | 0 | 27 (0.5) | 44 (0.8) | (1) | 15 (0.6) | 8 (0.6) | 0 |
| Slovenia | 49 (1.5) | 59 (1.7) | ( ${ }^{\text {c }}$ | 26 (1.1) | 31 (1.4) | (1) | 24 (1.4) | 10 (0.9) | 0 |
| Tunisia | 70 (1.5) | $\checkmark>$ |  | 18 (1.0) | $\checkmark>$ |  | 12 (0.9) | $\checkmark>$ |  |
| United States | 54 (0.9) | 47 (1.6) | 0 | 25 (0.5) | 38 (1.0) | (1) | 20 (0.6) | 15 (0.9) | 0 |
| International Avg. | 50 (0.2) | 46 (0.4) | © | 28 (0.2) | 38 (0.3) | (1) | 22 (0.2) | 16 (0.3) | © |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 53 (1.7) | $\checkmark>$ |  | 26 (1.0) | $\checkmark>$ |  | 21 (1.4) | $\checkmark>$ |  |
| Ontario Province, Can. | 48 (1.5) | 48 (1.1) |  | 31 (1.1) | 41 (1.0) | ( | 21 (1.2) | 11 (0.8) | 0 |
| Quebec Province, Can. | 56 (1.2) | 57 (2.7) |  | 32 (1.0) | 35 (2.8) |  | 12 (0.8) | 8 (1.4) | 0 |

- 2003 significantly higher
(7) 2003 significantly lower

Background data provided by students.
Trend notes: Because of differences between 1995 and 2003 in population coverage, 1995 data are not shown for Italy and Latvia. 1995 data for New Zealand in this exhibit include students in English medium instruction only (>98\% of the estimated population).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. A diamond (') indicates the country did not participate in the assessment.


## Chapter 5

## The Mathematics Curriculum

The first part of Chapter 5 presents information about the curricular goals in the TIMSS 2003 countries, referred to as the intended curriculum. Data are provided about whether the participating countries have national curricula and public examinations in mathematics, how the curriculum is supported and monitored within each country, whether countries differentiate the curriculum for students with different levels of ability, and the approaches and processes that are emphasized in the intended curriculum. The second part of the chapter presents data about the coverage of the TIMSS mathematics topics in the intended curriculum for each country, as well as teachers' reports about the mathematics topics actually taught to their students, also known as the implemented curriculum.

In comparing achievement across countries, it is important to consider differences in students' curricular experiences and how they may affect the mathematics they have studied. Students' opportunity to learn the content, skills, and processes tested in the TIMSS 2003 mathematics assessment depends to a large degree on the curricular goals and intentions inherent in each country's policies for mathematics education. Just as important as what students are expected to learn, however, is what their teachers choose to teach them. The lessons provided by the teacher ultimately determine the mathematics students are taught.

This chapter presents information about the curricular goals in mathematics in the TIMSS 2003 countries and teachers' reports about the mathematics studied. Teachers' instructional programs for their classes are usually guided by an "official curriculum" that describes the mathematics education that should be provided. The official curriculum can be communicated by means of documents or statements of various types (often called guides, guidelines, or frameworks) prepared by the education ministry or by national or regional education departments. These documents or statements, together with supporting material such as instructional guides or mandated textbooks, are referred to as the intended curriculum. To collect information about the intended mathematics curriculum in each of the TIMSS 2003 countries, the National Research Coordinators (NRCs) responsible for implementing the study completed curriculum questionnaires, often with the assistance of curriculum specialists, and responded to followup queries.

In many cases, teachers need to interpret and adapt the intended curriculum according to their perceptions of the needs, abilities, and interests of their students, and this evolves into the implemented curriculum. Research has shown that the implemented curriculum, even in highly regulated educational systems, is not identical to the intended curriculum. To collect data about the implemented curriculum, the mathematics teachers of the students tested in TIMSS 2003 completed questionnaires about whether the students had been taught the various mathematics topics included in the assessment.

## Which Countries Have a National Curriculum and Public Examinations in Mathematics?

A common feature of many countries' educational systems is that curricular decisions are made at the national level, with the ministry of education (or highest authority in the system) being primarily responsible for the major decisions governing the direction of education. Some countries, on the other hand, have less centralized systems, with
such decisions made at the regional or local level. Centralized decision making can add coherence and uniformity to curriculum coverage, whereas less centralized decision making may give a school or teacher more flexibility in tailoring instruction to the needs of students.

Exhibit 5.1 shows that, of the 47 countries that participated in TIMSS 2003 at the eighth grade, ${ }^{1}$ all but 3 reported that the specifications for students' curricular goals in mathematics at this level were developed as national curricula. In Australia and the United States, curricula were determined at the state level. In Belgium (Flemish), although there was no national curriculum, there were officially defined final attainment levels, and school boards developed their own curricula based on these. Among benchmarking participants, the US state of Indiana and the Canadian provinces of Ontario and Quebec had system-wide curricula determined at the state and provincial level, respectively, while in the Basque Country of Spain, 55 percent of the curriculum was determined at the national level and 45 percent at the community level.

In the recent past, it has become common for countries' intended curricula to be updated regularly. At the time of the TIMSS 2003 testing, the official eighth-grade mathematics curriculum in 27 of the participants had been in place for five years or less, and more than half of those were in revision. Of the 24 participants with an eighthgrade mathematics curriculum of more than five years standing, 18 were revising it at the time of the assessment. For Australia and the United States, with less centralized educational systems, curriculum renewal varies by state and is a generally ongoing process.

At the fourth grade, Exhibit 5.1 shows that of the 26 countries that participated in TIMSS 2003 at this level, all but 3 reported having national curricula in fourth-grade mathematics. Similar to the eighth grade, fourth-grade mathematics curricula in Australia and the United States were determined at the state level, and school boards in Belgium (Flemish) developed their own curricula based on officially defined final attainment levels. Among benchmarkers, Indiana,

1 Curriculum data are presented for the Syrian Arab Republic at the eighth grade, and for Yemen at the fourth grade, because these data are not dependent upon the countries' samples.

Exhibit 5.1: Intended Mathematics Curriculum


| Countries | National Curriculum | Year Curriculum Introduced | Curriculum Under Revision | Public Exams with Consequences for Individual Students | Grades Tested in Public Exams |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bigcirc$ | 2000 | $\bigcirc$ | - | 3,8,10 | Country reported Yes |
| Australia | $\bigcirc$ | Varies by state; generally ongoing process | - | - | 12 | for the particular option |
| Bahrain | $\bigcirc$ | 2000-2001 | - | - | 9,10,11,12 |  |
| 1 Belgium (Flemish) | $\bigcirc$ | 1997 | $\bigcirc$ | $\bigcirc$ | - | Country reported No for the particular option |
| Botswana | - | 1996 | $\bigcirc$ | - | 7,10,12 |  |
| Bulgaria | - | 1998 | $\bigcirc$ | - | 7,12 |  |
| Chile | $\bigcirc$ | 2002 | $\bigcirc$ | - | 12 |  |
| Chinese Taipei | - | 1997 | - | - | 9,12 |  |
| Cyprus | - | 1997 | $\bigcirc$ | - | 7-12 |  |
| Egypt | $\bigcirc$ | 2002 | - | - | 5,8,10,11 |  |
| England | - | 2000 | $\bigcirc$ | - | 10,11,12 |  |
| Estonia | - | 1997, revised 2002 | - | - | 9,12 |  |
| Ghana | - | 1987, revised 2001 | $\bigcirc$ | - | 9 |  |
| Hong Kong, SAR | - | 2002 | $\bigcirc$ | - | 11,13 |  |
| Hungary | - | 2000 | $\bigcirc$ | - | 12 |  |
| Indonesia | - | 1994 | - | - | 6,9,12 |  |


| Iran, Islam |
| :---: |
| 2 Israel |
| 2 Italy |

Japan
Jordan
Korea, Rep. of
Latvia
Lebanon
Lithuania
Macedonia
Malaysia
Moldova, Rep. of
Morocco
Netherlands
New Zealand
Norway
Palestinian Nat'l Auth.
Philippines
Romania
Russian Federation
Saudi Arabia
Scotland
Serbia
Singapore
Slovak Republic
Slovenia

| South Africa | - | 2001 (introduced in 1998 for prior grades) | - | $\bullet$ | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sweden | - | 1994, revised 2000 | $\bigcirc$ | $\bigcirc$ | - |
| Syrian Arab Republic | - | 1984 | - | - | 9,12 |
| Tunisia | - | 2000 | - | - | 9,12 |
| United States | $\bigcirc$ | Varies by state; generally ongoing process | - | $\bigcirc$ | - |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | - | 1992 | - | $\bigcirc$ | - |
| Indiana State, US | - | 2000 | $\bigcirc$ | $\bigcirc$ | 10 |
| Ontario Province, Can. | - | 1997 | - | - | 3,6,9 |
| Quebec Province, Can. | - | 1995 | - | - | 10,11 |

[^37]2 Italy: Beginning with the 2004-05 academic year, students in grade 5 will not be tested in public examinations.
A dash ( - ) indicates comparable data are not available.


| Countries | National Curriculum | Year Curriculum Introduced | Curriculum Under Revision | Public Exams with Consequences for Individual Students | Grades Tested in Public Exams |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bigcirc$ | 2000 | $\bigcirc$ | - | 3,8,10 |
| Australia | $\bigcirc$ | Varies by state; generally ongoing process | - | - | 12 |
| 1 Belgium (Flemish) | $\bigcirc$ | 1998-1999 | $\bigcirc$ | $\bigcirc$ | - |
| Chinese Taipei | - | 2002 | - | - | 9,12 |
| Cyprus | - | 1995 | $\bigcirc$ | - | 7-12 |
| England | - | 2000 | $\bigcirc$ | - | 10,11,12 |
| Hong Kong, SAR | - | 1983 | $\bigcirc$ | - | 11,13 |
| Hungary | - | 2000 | $\bigcirc$ | - | 12 |
| Iran, Islamic Rep. of | - | 1983 | $\bigcirc$ | - | 5,8,11,12 |
| 2 Italy | - | 1985, revised 2002 | - | - | 5,8,13 |
| Japan | - | 2002 | $\bigcirc$ | $\bigcirc$ | - |
| Latvia | - | 2001 | $\bigcirc$ | - | 6,9,12 |
| Lithuania | - | 1997, revised 2003 | $\bigcirc$ | - | 10,12 |
| Moldova, Rep. of | - | 1999-2000 | $\bigcirc$ | - | 4,9,11,12 |
| Morocco | - | 2002-2003 | - | - | 12 |
| Netherlands | - | 1998 | - | - | 10,11,12 |
| New Zealand | - | Introduced 1993, implemented 1994 | - | - | 10,11,12 |
| Norway | - | 1997 | $\bigcirc$ | $\bigcirc$ | - |
| Philippines | - | 2002 (pilot) | - | $\bigcirc$ | - |
| Russian Federation | - | 2001 | $\bigcirc$ | - | 9,11 |
| Scotland | $\bigcirc$ | 1991 | $\bigcirc$ | - | 10,11,12 |
| Singapore | - | 1999 | - | - | 6,10,12 |
| Slovenia | - | 1999 for sample of schools; 2003 for all schools | - | - | 3,6,9,12 |
| Tunisia | - | 2000 | - | - | 9,12 |
| United States | $\bigcirc$ | Varies by state; generally ongoing process | - | $\bigcirc$ | - |
| Yemen | - | 2000-2001 | $\bigcirc$ | - | 9,12 |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US | - | 2000 | $\bigcirc$ | - | 10 |
| Ontario Province, Can. | - | 1997 | - | - | 3,6,9 |
| Quebec Province, Can. | - | 2001 | $\bigcirc$ | - | 10,11 |

Country reported Yes for the particular option
Country reported No for the particular option

2 Italy: Beginning with the 2004-05 academic year, students in grade 5 will not be tested in public examinations.
A dash ( - ) indicates comparable data are not available

Ontario, and Quebec had system-wide curricula determined at the state and provincial level, respectively.

At the time of the TIMSS 2003 assessment, the official fourthgrade mathematics curriculum had been in place for five years or less in 20 of the participants, and nearly half of those were in revision. Of the nine participating entities with a fourth-grade mathematics curriculum of more than five years standing, five were revising it at the time of the assessment. As at the eighth grade, curriculum renewal in Australia and the United States varied by state and was generally an ongoing process.

Public examinations with consequences for individual students are another common feature of many countries' educational systems. Although public examinations can provide information of interest to national and regional policy makers, their main purpose is to make decisions about individual students, such as promotion from one grade to another, entry to a higher school system, or graduation from secondary school. Among all TIMSS 2003 participants, 39 countries and one benchmarking entity reported having public examinations in mathematics at one or more grades. Grade 12 was the most prevalent, with 33 countries giving students public examinations in mathematics at this level.

## How Do Countries Support and Monitor Curriculum Implementation?

Education systems use different ways to achieve the best match between the intended and the implemented curriculum. The use of public examinations as a mechanism to support and monitor implementation of the intended curriculum is prevalent among many countries, as noted above. Another way to help ensure alignment is to develop instructional materials, such as textbooks, instructional guides, and ministry notes, tailored to the curriculum. In addition, countries can also monitor curriculum implementation by means of national assessments
based on student samples, and by systems of school inspection or audit. The different methods used by the TIMSS 2003 countries are shown in Exhibit 5.2, first for countries that participated at the eighth grade and then for those at the fourth grade.

Of the methods for supporting and monitoring curriculum implementation shown in Exhibit 5.2, at the eighth grade, 12 participants reported using all 7 , and an additional 22 used 5 or 6 . The most widely used methods were ministry notes and directives (42 participants), instructional or pedagogical guides (41 participants), and a system of school or audit (40 participants)

The use of mandated or recommended textbooks as a means of supporting eighth-grade mathematics curriculum implementation was reported by 38 participants. Curriculum evaluation during or after implementation was used by 35 participating entities, and the use of specifically developed or recommended instructional activities by 33 participants. The least widely used method was national assessments based on student samples ( 25 participants).

At the fourth grade, four participants reported using all seven methods shown in Exhibit 5.2 to support and monitor curriculum implementation, and 16 participants used five or six. The most widely used methods were instructional or pedagogical guides (24 participants), ministry notes and directives ( 24 participants), and curriculum evaluation during or after implementation ( 23 participants).

A system of school inspection or audit as a means of monitoring fourth-grade mathematics curriculum implementation was used by 21 participants. The use of specifically developed or recommended instructional activities was reported by 21 participants and mandated or recommended textbooks by 20 participants. Similar to the eighth grade, the least widely used method at the fourth grade was national assessments based on student samples ( 12 participants).

An additional method countries often use to support curriculum implementation is to provide mathematics teachers with specific

Exhibit 5.2: Methods Used to Support or Monitor Implementation of the Intended

| Countries |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Australia | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Bahrain | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Belgium (Flemish) | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Botswana | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Bulgaria | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| Chile | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Chinese Taipei | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Cyprus | $\bullet$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| Egypt | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| England | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Estonia | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Ghana | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Hong Kong, SAR | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Hungary | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Indonesia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Iran, Islamic Rep. of | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Israel | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| Italy | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Japan | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Jordan | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Korea, Rep. of | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Latvia | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Lebanon | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Lithuania | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Macedonia, Rep. of | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Malaysia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Moldova, Rep. of | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Morocco | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Netherlands | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| New Zealand | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| Norway | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| Palestinian Nat'l Auth. | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Philippines | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Romania | $\bullet$ | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Russian Federation | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Saudi Arabia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| Scotland | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Serbia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Singapore | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Slovak Republic | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| Slovenia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ |
| South Africa | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Sweden | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Syrian Arab Republic | - | - | - | - | - | - | - |
| Tunisia | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| United States | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Basque Country, Spain | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Indiana State, US | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Ontario Province, Can. | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | - | $\bigcirc$ |
| Quebec Province, Can. | $\bigcirc$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |

Background data provided by National Research Coordinators.
A dash $(-)$ indicates comparable data are not available.

| Countries |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Australia | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Belgium (Flemish) | $\bigcirc$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Chinese Taipei | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Cyprus | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| England | $\bigcirc$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Hong Kong, SAR | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Hungary | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Iran, Islamic Rep. of | - | $\bullet$ | - | $\bullet$ | $\bullet$ | - | $\bullet$ |
| Italy | $\bigcirc$ | $\bullet$ | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Japan | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Latvia | $\bullet$ | $\bigcirc$ | - | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ |
| Lithuania | - | $\bullet$ | - | - | - | - | - |
| Moldova, Rep. of | $\bigcirc$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Morocco | - | - | - | $\bigcirc$ | - | $\bigcirc$ | $\bullet$ |
| Netherlands | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| New Zealand | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | - |
| Norway | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| Philippines | - | - | - | - | $\bullet$ | - | - |
| Russian Federation | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | - | $\bigcirc$ | - |
| Scotland | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | - | - | - |
| Singapore | $\bullet$ | $\bullet$ | - | $\bullet$ | - | $\bigcirc$ | - |
| Slovenia | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ |
| Tunisia | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bullet$ |
| United States | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Yemen | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | $\bullet$ | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | - |
| Ontario Province, Can. | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | - | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bigcirc$ | - | $\bigcirc$ | for the particular option

preparation in how to teach the intended curriculum as part of their pre-service and/or in-service education. These data are given in Exhibit 6.5 of the next chapter.

## How Much Instructional Time is Intended for Mathematics?

Many countries designate in their intended curriculum the percentage of total instructional time that should be devoted to mathematics and other subjects at different grade levels. The percentage of instructional time designated for mathematics in the intended curriculum for grades 2, 4, 6, and 8 is shown in Exhibit 5.3 for all TIMSS 2003 participants. These data provide a good estimate of students' intended instructional time for mathematics across the primary and middle school years. The general pattern across countries shows that the percentage of time remains the same or decreases from grade 2 to grade 4 , from grade 4 to grade 6 , and from grade 6 to grade 8 , with the largest decline usually between grades 6 and 8 . Interestingly, the reverse pattern holds for science. ${ }^{2}$ Where increases occurred in the percentage of instructional time designated for mathematics, they generally were between grades 2 and 4 . Not all countries conformed to this general pattern, however. The percentage of total instructional time specified for mathematics ranged from 10 to 25 percent at second grade, from 12 to 29 percent at fourth grade, from 11 to 25 percent at sixth grade, and from 8 to 25 percent at eighth grade. Schools' and teachers' reports of the percentage of instructional time actually devoted to mathematics at grades 4 and 8, shown in Exhibit 7.3, generally correspond with the intended percentages reported in Exhibit 5.3, although slightly more so at eighth grade than at fourth grade.


Background data provided by National Research Coordinators.
A dash (-) indicates comparable data are not available.

1 Sweden: Figure shown represents an average across the nine years of compulsory school.

## Do Countries Differentiate the Intended Mathematics Curriculum for Students with Different Levels of Ability?

The challenge of maximizing opportunity to learn for students with widely varying abilities is met differently in different countries. Exhibit 5.4 indicates how countries addressed this issue in organizing the intended mathematics curriculum, first for countries that participated at the eighth grade and then for those at the fourth grade.

The most common approach at the eighth grade, reported by 38 participants, was to have the same intended curriculum for all students with no grouping of students. Nine countries reported having one curriculum for all students, but at different difficulty levels for groups of students with different ability levels. Four countries - Belgium (Flemish), the Netherlands, the Russian Federation, and Singapore - had different curricula for different groups of students according to their ability level.

At the fourth grade, all participants reported having just one curriculum for all students, and in most cases with no grouping by ability level. Five countries, Australia, England, New Zealand, Scotland, and the United States, had just one curriculum for all students, but provided different levels of difficulty for students of differing ability levels.

## Exhibit 5.4: The Way the Intended Mathematics Curriculum Addresses the Issue of Students with Different Levels of Ability



|  | One Curriculum <br> One Curriculum <br> for All Students, <br> but Students <br> with No Grouping |
| :---: | :---: |
| but Diferent <br> Groups of Students <br> Have Different <br> Difficulty Levels |  |
|  |  |




Exhibit 5.4: The Way the Intended Mathematics Curriculum Addresses the Issue of Students with Different Levels of Ability


| Countries | One Curriculum for All Students with No Grouping | One Curriculum for All Students, but Different Groups of Students Have Different Difficulty Levels | Different Curricula for Different Groups of Students According to Ability Level |
| :---: | :---: | :---: | :---: |
| Armenia | - | $\bigcirc$ | $\bigcirc$ |
| Australia | $\bigcirc$ | - | $\bigcirc$ |
| Belgium (Flemish) | - | $\bigcirc$ | $\bigcirc$ |
| Chinese Taipei | - | $\bigcirc$ | $\bigcirc$ |
| Cyprus | - | $\bigcirc$ | $\bigcirc$ |
| England | $\bigcirc$ | - | $\bigcirc$ |
| Hong Kong, SAR | - | $\bigcirc$ | $\bigcirc$ |
| Hungary | - | $\bigcirc$ | $\bigcirc$ |
| Iran, Islamic Rep. of | - | $\bigcirc$ | $\bigcirc$ |
| Italy | - | $\bigcirc$ | $\bigcirc$ |
| Japan | - | $\bigcirc$ | $\bigcirc$ |
| Latvia | - | $\bigcirc$ | $\bigcirc$ |
| Lithuania | - | $\bigcirc$ | $\bigcirc$ |
| Moldova, Rep. of | - | $\bigcirc$ | $\bigcirc$ |
| Morocco | - | $\bigcirc$ | $\bigcirc$ |
| Netherlands | - | $\bigcirc$ | $\bigcirc$ |
| New Zealand | $\bigcirc$ | - | $\bigcirc$ |
| Norway | - | $\bigcirc$ | $\bigcirc$ |
| Philippines | - | $\bigcirc$ | $\bigcirc$ |
| Russian Federation | - | $\bigcirc$ | $\bigcirc$ |
| Scotland | $\bigcirc$ | - | $\bigcirc$ |
| Singapore | - | $\bigcirc$ | $\bigcirc$ |
| Slovenia | - | $\bigcirc$ | $\bigcirc$ |
| Tunisia | - | $\bigcirc$ | $\bigcirc$ |
| United States | $\bigcirc$ | - | $\bigcirc$ |
| Yemen | - | $\bigcirc$ | $\bigcirc$ |
| Benchmarking Participants |  |  |  |
| Indiana State, US | - | $\bigcirc$ | $\bigcirc$ |
| Ontario Province, Can. | - | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | - | $\bigcirc$ | $\bigcirc$ |

## What Approaches and Processes Do Countries Emphasize in their Intended Mathematics Curriculum?

Exhibit 5.5 indicates the relative emphasis given to various aspects of mathematics instruction in the intended curriculum of participating countries, for both eighth and fourth grade. At the eighth grade, as might be anticipated for students at this point in their education, "a lot of emphasis" was most commonly placed on understanding mathematical concepts and principles (32 participants) and mastering basic skills (30 participants). Not a single participant reported giving "very little" or "no" emphasis in the intended curriculum to understanding mathematical concepts and principles, and mastering basic skills received very little or no emphasis in only five countries.

Applying mathematics in real-life contexts was given a lot of emphasis in the intended eighth-grade curriculum of 17 participants. Botswana, the Netherlands, and South Africa reported placing more emphasis on this approach than on mastering basic skills or understanding mathematics concepts. Communicating mathematically received a lot of emphasis in 13 participating entities, and reasoning mathematically in 14 entities.

Relative to the other approaches and processes, participants reported placing less emphasis on integrating mathematics with other subjects, deriving formal proofs, and incorporating the experiences of different ethnic/ cultural groups. Only two countries - Ghana and South Africa - reported placing a lot of emphasis on this multicultural approach in the intended curriculum.

In the intended mathematics curriculum at the fourth grade, most emphasis was placed on mastering basic skills and understanding mathematical concepts and principles, with applying mathematics in real-life contexts next in terms of emphasis. Communicating mathematically and reasoning mathematically were given a lot of emphasis in about half the participants. Integrating mathematics with other subjects and incorporating the experiences of different ethnic/cultural groups were given least emphasis in the fourth-grade mathematics curriculum.

Exhibit 5.5: Emphasis on Approaches and Processes in the Intended Mathematics Curriculum

| Countries | $\left\lvert\, \begin{array}{\|c\|} \text { Mastering Basic } \\ \text { Skills } \end{array}\right.$ | Understanding Mathematical Concepts and Principles | Applying Mathematics in Real-life Contexts | Communicating Mathematically | Reasoning Mathematically | Integrating Mathematics with Other Subjects | Deriving Formal <br> Proofs | Incorporating the Experiences of Different Ethnic/Cultural Groups |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bullet$ | - | - | - | - | - | - | $\bigcirc$ |
| Australia | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | - | - | $\bigcirc$ | $\odot$ |
| Bahrain | $\bullet$ | $\bullet$ | - | - | - | - | $\bullet$ | $\bigcirc$ |
| Belgium (Flemish) | - | $\bigcirc$ | $\bullet$ | - | 0 | 0 | - | $\bigcirc$ |
| Botswana | - | - | - | - | - | $\bullet$ | - | - |
| Bulgaria | - | - | - | $\odot$ | $\bullet$ | - | $\bullet$ | $\bigcirc$ |
| Chile | $\bullet$ | - | - | $\bigcirc$ | - | - | $\odot$ | - |
| Chinese Taipei | $\bullet$ | $\bullet$ | - | - | $\odot$ | $\odot$ | - | $\bigcirc$ |
| Cyprus | $\bullet$ | $\bullet$ | $\bullet$ | $\odot$ | - | - | - | $\bigcirc$ |
| Egypt | $\bullet$ | $\bigcirc$ | - | - | - | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| England | $\bullet$ | $\bullet$ | - | - | - | - | - | - |
| Estonia | $\bullet$ | - | - | $\odot$ | - | - | - | $\bigcirc$ |
| Ghana | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | - | - | $\bigcirc$ | $\bullet$ |
| Hong Kong, SAR | $\bullet$ | - | - | - | - | $\odot$ | $\odot$ | $\bigcirc$ |
| Hungary | $\bigcirc$ | - | $\bigcirc$ | - | $\odot$ | $\bigcirc$ | - | $\bigcirc$ |
| Indonesia | - | - | $\odot$ | $\odot$ | $\odot$ | $\odot$ | - | - |
| Iran, Islamic Rep. of | - | $\bullet$ | $\odot$ | $\bigcirc$ | - | $\odot$ | $\odot$ | $\bigcirc$ |
| Israel | - | $\bullet$ | - | - | - | - | $\bullet$ | $\bigcirc$ |
| Italy | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | - |
| Japan | $\bullet$ | $\bullet$ | - | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| Jordan | - | $\bullet$ | - | - | - | - | - | - |
| Korea, Rep. of | - | $\bullet$ | - | - | - | $\bigcirc$ | $\bullet$ | $\bigcirc$ |
| Latvia | - | - | - | $\bullet$ | - | - | - | $\bigcirc$ |
| Lebanon | - | - | - | $\odot$ | - | $\odot$ | - | $\odot$ |
| Lithuania | $\bigcirc$ | $\bullet$ | - | $\bigcirc$ | $\odot$ | $\odot$ | $\bigcirc$ | $\bigcirc$ |
| Macedonia, Rep. of | - | $\bullet$ | - | - | - | - | $\bullet$ | - |
| Malaysia | $\bullet$ | - | - | - | - | - | - | - |
| Moldova, Rep. of | $\bullet$ | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ |
| Morocco | $\odot$ | - | - | $\bigcirc$ | - | $\odot$ | $\bullet$ | $\bigcirc$ |
| Netherlands | - | - | $\bullet$ | - | - | - | $\bigcirc$ | - |
| New Zealand | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | - | $\bigcirc$ | - |
| Norway | $\bullet$ | - | $\bullet$ | - | - | 0 | $\bigcirc$ | $\bigcirc$ |
| Palestinian Nat'I Auth. | - | $\bullet$ | - | - | - | - | - | $\bigcirc$ |
| Philippines | $\bullet$ | $\bullet$ | - | - | - | $\bullet$ | - | - |
| Romania | - | - | - | - | - | - | - | $\bigcirc$ |
| Russian Federation | $\bullet$ | $\bullet$ | $\odot$ | $\odot$ | - | $\odot$ | - | $\bigcirc$ |
| Saudi Arabia | $\bullet$ | $\bullet$ | - | - | $\bullet$ | - | $\bullet$ | - |
| Scotland | - | $\bullet$ | $\bigcirc$ | - | $\bigcirc$ | - | - | - |
| Serbia | $\bullet$ | $\bullet$ | - | - | - | - | - | - |
| Singapore | $\bullet$ | $\bullet$ | - | - | - | - | - | - |
| Slovak Republic | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | - | - | $\bigcirc$ |
| Slovenia | $\bigcirc$ | $\bullet$ | $\bullet$ | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| South Africa | - | - | - | - | - | - | - | - |
| Sweden | $\bullet$ | $\bullet$ | $\bullet$ | - | $\bullet$ | - | $\bigcirc$ | $\odot$ |
| Syrian Arab Republic | - | $\bullet$ | $\odot$ | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Tunisia | - | - | - | $\odot$ | - | $\odot$ | $\odot$ | $\bigcirc$ |
| United States | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\odot$ | $\odot$ | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain | - | $\bullet$ | - | - | - | - | - | - |
| Indiana State, US | - | $\bullet$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Ontario Province, Can. | - | $\bullet$ | $\bullet$ | $\bullet$ | - | $\odot$ | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | - | - | - | - | - | - | ๑ | - |
|  | - A Lot of Emphasis |  | Some Emphasis |  | - Very Little Emphasis |  | O No Emphasis |  |


| Countries | Mastering Basic Skills | Understanding Mathematical Concepts and Principles | Applying Mathematics in Real-life Contexts | Communicating Mathematically | Reasoning Mathematically | Integrating Mathematics with Other Subjects | Incorporating the Experiences of Different Ethnic/Cultural Groups |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | - | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Australia | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - |
| Belgium (Flemish) | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Chinese Taipei | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Cyprus | - | - | - | - | $\bigcirc$ | - | $\bigcirc$ |
| England | - | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hong Kong, SAR | - | - | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Hungary | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Iran, Islamic Rep. of | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Italy | - | - | - | - | - | - | - |
| Japan | - | - | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Latvia | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Lithuania | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Moldova, Rep. of | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Morocco | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Netherlands | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| New Zealand | - | - | - | - | - | - | $\bigcirc$ |
| Norway | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Philippines | - | - | - | - | - | - | $\bigcirc$ |
| Russian Federation | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Scotland | - | - | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Singapore | - | - | - | - | - | - | - |
| Slovenia | $\bigcirc$ | - | - | - | - | - | $\bigcirc$ |
| Tunisia | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| United States | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Yemen | - | - | - | $\bigcirc$ | - | - | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | - | - | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Ontario Province, Can. | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  |  |  | - A Lot of Emphas | - Some Em | mphasis $\bigcirc$ Ve | Little Emphasis | O No Emphasis |

[^38]
## Are the TIMSS Mathematics Topics Included in the Intended Curriculum?

The ability of policy makers to make sound judgments about relative strengths and weaknesses of mathematics and science education in their systems depends on achievement measures being based, as closely as possible, on what students in their systems have actually been taught. The TIMSS Assessment Frameworks and Specifications: 2003 served as the basis for the TIMSS 2003 mathematics assessment. ${ }^{3}$ It delineates the mathematics content and skills to be assessed at both the eighth and fourth grades, and represents a consensus among the countries participating in TIMSS 2003 about the mathematics students at these grades should be expected to have learned. Content and topic areas are elaborated in the frameworks, with each topic area presented as a comprehensive list of objectives specific to the target grades covered in a majority of participating countries. However, the frameworks do not consist solely of content and behaviors included in the intended curricula of most participating countries. The aim was to ensure that goals of mathematics education regarded as important in a significant number of countries be included. Hence, not all topics included in the TIMSS 2003 assessment are in all participating countries' intended curriculum, and consequently the curricula of some countries align more closely than others with the TIMSS frameworks. ${ }^{4}$

National Research Coordinators were asked to indicate whether each of the TIMSS 2003 mathematics topics was included in their countries' intended curriculum through the target grade (eighth or fourth grade), and if so, whether the topics were intended to be taught to "all or almost all students" or "only the more able students." They were also asked to indicate the grade(s) at which each topic was primarily intended to be taught to students.

Exhibit 5.6 shows that, for most countries, a great deal of the mathematics content addressed by the TIMSS 2003 assessment was included in their intended curricula. On average, across participants at
the eighth grade, 70 percent of the assessment topics were intended for all or almost all students, and a further six percent for only the more able students. In only six countries were less than half of the topics included in the eighth-grade curriculum: Botswana, Indonesia, Lebanon, Morocco, the Philippines, and Tunisia.

Not surprisingly, at this level, the content area with the greatest coverage was number, with 96 percent of the topics, on average, included in participants' intended curriculum for all or almost all students. For all but three participants, at least nine of the ten topics in number ( $90 \%$ ) were included in the curriculum. The mathematics content area with the next greatest coverage was measurement, with 78 percent of the topics, on average, included in the intended curriculum for all or almost all students. Sixteen participants included all eight measurement topics in their curricula, and a further 30 participants included seven of the eight topics. Countries with low emphasis on measurement in the curriculum included Botswana, Indonesia, Lebanon, Morocco, South Africa, and Tunisia, where at least half of the measurement topics were not included in the curriculum.

Geometry and algebra had similar levels of coverage across participating countries, with about two-thirds of the topics ( 67 percent of the geometry topics and 63 percent of the algebra topics) included in the intended curriculum for all or almost all students. In geometry, relatively high levels of coverage ( 11 of 13 percent of the topics) were reported for the intended curricula of 21 participants, although there also were several (Botswana, Indonesia, Latvia, Morocco, the Philippines, South Africa, Sweden, and Tunisia) where fewer than half of the geometry topics were included in the eighth-grade curriculum. For algebra, most of the topics (5 out of 6) were included in the intended curricula of 22 participants. However, in 14 of the TIMSS participants, no more than half of the algebra topics were included. One country, Chile, included none of the algebra topics in its intended curriculum.

The content area with the least coverage was data, with only 39 percent of the topics on average included in the intended curriculum for all or almost all students. All eight topics were included in the curriculum of just two countries (New Zealand and the United States) and two benchmarking participants (Indiana and Ontario). In contrast, 30 participants had no more than half of the data topics in their curricula, and in four countries - Chinese Taipei, the Philippines, Syria, and Tunisia - none of the data topics was included.

Consistent with few countries indicating that they had different curricula for students of different ability levels, the percentages of topics that were included in the intended curriculum for only the more able students were generally low, with only 6 percent of eighth-grade mathematics topics, on average, intended for the top track of students. The percentage ranged from 2 percent for number to 10 percent for data.

Although the relationship between inclusion in the intended curriculum and student achievement was not perfect, it was notable that several of the higher-performing countries reported high levels of emphasis on the mathematics topics in their intended curricula and that those with the lowest levels of curricular coverage came from the lower half of the achievement distribution. For example, five of the six top-performing countries (Chinese Taipei being the exception) included 80 percent or more of the topics for all or almost all of their students, while the six countries with fewer than half of the topics in their curricula all had average mathematics achievement below the international mean. However, high-performing Chinese Taipei and the Netherlands had relatively low coverage of the mathematics topics ( 69 and 53 percent, respectively) in their intended curricula, whereas lower-performing Ghana and Bahrain had 96 and 89 percent of topics, respectively, included in their intended curricula. Clearly the intended curriculum is only one of the factors that impact achievement.

At fourth grade, Exhibit 5.6 shows that on average, internationally, 59 percent of the TIMSS 2003 mathematics topics were included in the intended curricula for all or almost all students, and a further

[^39]9 percent for only the more able students. More than eighty percent of the mathematics topics were included in the intended curriculum for all or almost all students in Armenia, England, Italy, Moldova, the United States, Indiana, and Ontario.

Although measurement had fewer topics than number at the fourth grade ( 6 vs 12 ), it had a greater percentage of topics included in the intended curricula of participating countries -81 percent for all or almost all students compared with 68 percent. Nineteen of the twentynine fourth-grade participants included at least five of the six measurement topics in their curricula. Comparable coverage of number topics ( 10 out of 12 topics) was reported in just 10 of the 29 participants.

The data content area was next at fourth grade in terms of inclusion in the intended curriculum, with 62 percent of its topics, on average, intended for all or almost all students. Five or more of the seven data topics were included in the intended curricula of 19 participants for all or almost all students. For patterns and relationships, on average, 54 percent of the topics were included in the intended curriculum for all or almost all students. At least four of the six topics in patterns and relationships were included in the intended curricula of 14 participants for all or almost all students. The content area with the least coverage was geometry, with only 38 percent of the topics on average included in the intended curriculum for all or almost all students. In 17 of the 29 participants, fewer than half of the 11 geometry topics were included in the curriculum.

As at the eighth grade, the percentages of topics included in the intended curriculum for only the more able students at fourth grade were generally low, consistent with few countries indicating that they had different curricula for different groups of students depending on ability level. Only 9 percent of fourth-grade mathematics topics on average were intended for the top track of students, with a range of 8 percent for measurement and geometry to 11 percent for patterns and relationships.

| Countries | Percentage of TIMSS Mathematics Topics Intended to be Taught Up to and Including Eighth Grade* |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Overall (45 topics) |  |  | Number (10 topics) |  |  | Algebra (6 topics) |  |  |
|  | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 |
| Armenia | 69 | 31 | 0 | 90 | 10 | 0 | 67 | 33 | 0 |
| Australia | 69 | 29 | 2 | 90 | 0 | 10 | 50 | 50 | 0 |
| Bahrain | 89 | 0 | 11 | 100 | 0 | 0 | 67 | 0 | 33 |
| Belgium (Flemish) | 80 | 13 | 7 | 100 | 0 | 0 | 83 | 0 | 17 |
| Botswana | 44 | 0 | 56 | 90 | 0 | 10 | 17 | 0 | 83 |
| Bulgaria | 78 | 0 | 22 | 100 | 0 | 0 | 83 | 0 | 17 |
| Chile | 64 | 0 | 36 | 100 | 0 | 0 | 0 | 0 | 100 |
| Chinese Taipei | 69 | 0 | 31 | 100 | 0 | 0 | 67 | 0 | 33 |
| Cyprus | 64 | 27 | 9 | 100 | 0 | 0 | 50 | 33 | 17 |
| Egypt | 87 | 0 | 13 | 100 | 0 | 0 | 100 | 0 | 0 |
| England | 89 | 11 | 0 | 100 | 0 | 0 | 100 | 0 | 0 |
| Estonia | 73 | 0 | 27 | 100 | 0 | 0 | 100 | 0 | 0 |
| Ghana | 96 | 0 | 4 | 100 | 0 | 0 | 100 | 0 | 0 |
| Hong Kong, SAR | 82 | 0 | 18 | 100 | 0 | 0 | 50 | 0 | 50 |
| Hungary | 82 | 0 | 18 | 100 | 0 | 0 | 83 | 0 | 17 |
| Indonesia | 49 | 0 | 51 | 100 | 0 | 0 | 67 | 0 | 33 |
| Iran, Islamic Rep. of | 73 | 0 | 27 | 100 | 0 | 0 | 50 | 0 | 50 |
| Israel | 69 | 7 | 24 | 100 | 0 | 0 | 83 | 0 | 17 |
| Italy | 87 | 0 | 13 | 100 | 0 | 0 | 67 | 0 | 33 |
| Japan | 80 | 0 | 20 | 100 | 0 | 0 | 100 | 0 | 0 |
| Jordan | 76 | 0 | 24 | 100 | 0 | 0 | 83 | 0 | 17 |
| Korea, Rep. of | 84 | 0 | 16 | 90 | 0 | 10 | 83 | 0 | 17 |
| Latvia | 67 | 0 | 33 | 100 | 0 | 0 | 83 | 0 | 17 |
| Lebanon | 36 | 0 | 64 | 90 | 0 | 10 | 17 | 0 | 83 |
| Lithuania | 76 | 2 | 22 | 100 | 0 | 0 | 67 | 0 | 33 |
| Macedonia, Rep. of | 78 | 2 | 20 | 100 | 0 | 0 | 100 | 0 | 0 |
| Malaysia | 73 | 0 | 27 | 100 | 0 | 0 | 33 | 0 | 67 |
| Moldova, Rep. of | 82 | 0 | 18 | 100 | 0 | 0 | 100 | 0 | 0 |
| Morocco | 33 | 0 | 67 | 70 | 0 | 30 | 17 | 0 | 83 |
| Netherlands | 53 | 22 | 24 | 90 | 10 | 0 | 50 | 33 | 17 |
| New Zealand | 76 | 22 | 2 | 60 | 40 | 0 | 33 | 67 | 0 |
| Norway | 71 | 0 | 29 | 90 | 0 | 10 | 33 | 0 | 67 |
| Palestinian Nat'l Auth. | 76 | 0 | 24 | 100 | 0 | 0 | 50 | 0 | 50 |
| Philippines | 47 | 0 | 53 | 100 | 0 | 0 | 50 | 0 | 50 |
| Romania | 84 | 0 | 16 | 100 | 0 | 0 | 100 | 0 | 0 |
| Russian Federation | 76 | 0 | 24 | 100 | 0 | 0 | 83 | 0 | 17 |
| Saudi Arabia | 64 | 0 | 36 | 100 | 0 | 0 | 67 | 0 | 33 |
| Scotland | 58 | 29 | 13 | 70 | 30 | 0 | 17 | 50 | 33 |
| Serbia | 76 | 7 | 18 | 100 | 0 | 0 | 83 | 17 | 0 |
| Singapore | 80 | 9 | 11 | 100 | 0 | 0 | 83 | 17 | 0 |
| Slovak Republic | 62 | 33 | 4 | 100 | 0 | 0 | 50 | 33 | 17 |
| Slovenia | 80 | 0 | 20 | 100 | 0 | 0 | 100 | 0 | 0 |
| South Africa | 33 | 20 | 47 | 90 | 10 | 0 | 33 | 17 | 50 |
| Sweden | 53 | 13 | 33 | 90 | 0 | 10 | 0 | 33 | 67 |
| Syrian Arab Republic | 49 | 2 | 49 | 90 | 10 | 0 | 33 | 0 | 67 |
| Tunisia | 42 | 0 | 58 | 100 | 0 | 0 | 33 | 0 | 67 |
| United States | 98 | 2 | 0 | 100 | 0 | 0 | 83 | 17 | 0 |
| International Avg. | 70 | 6 | 24 | 96 | 2 | 2 | 63 | 9 | 29 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 49 | 29 | 22 | 90 | 10 | 0 | 17 | 67 | 17 |
| Indiana State, US | 96 | 0 | 4 | 100 | 0 | 0 | 100 | 0 | 0 |
| Ontario Province, Can. | 98 | 0 | 2 | 100 | 0 | 0 | 83 | 0 | 17 |
| Quebec Province, Can. | 78 | 2 | 20 | 100 | 0 | 0 | 50 | 17 | 33 |

Background data provided by National Research Coordinators.

[^40]See Exhibits 5.8 through 5.12 for data on individual topics.

Exhibit 5.6: Summary of TIMSS Mathematics Topics in the Intended Curriculum

| Countries | Percentage of TIMSS Mathematics Topics Intended to be Taught Up to and Including Eighth Grade |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Measurement (8 topics) |  |  | Geometry <br> (13 topics) |  |  | Data (8 topics) |  |  |
|  | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 8 |
| Armenia | 38 | 63 | 0 | 77 | 23 | 0 | 63 | 38 | 0 |
| Australia | 88 | 13 | 0 | 54 | 46 | 0 | 63 | 38 | 0 |
| Bahrain | 100 | 0 | 0 | 92 | 0 | 8 | 75 | 0 | 25 |
| Belgium (Flemish) | 88 | 13 | 0 | 85 | 0 | 15 | 38 | 63 | 0 |
| Botswana | 50 | 0 | 50 | 38 | 0 | 62 | 13 | 0 | 88 |
| Bulgaria | 100 | 0 | 0 | 85 | 0 | 15 | 13 | 0 | 88 |
| Chile | 100 | 0 | 0 | 54 | 0 | 46 | 50 | 0 | 50 |
| Chinese Taipei | 100 | 0 | 0 | 69 | 0 | 31 | 0 | 0 | 100 |
| Cyprus | 88 | 13 | 0 | 69 | 23 | 8 | 0 | 75 | 25 |
| Egypt | 75 | 0 | 25 | 100 | 0 | 0 | 50 | 0 | 50 |
| England | 88 | 13 | 0 | 85 | 15 | 0 | 75 | 25 | 0 |
| Estonia | 88 | 0 | 13 | 62 | 0 | 38 | 25 | 0 | 75 |
| Ghana | 100 | 0 | 0 | 100 | 0 | 0 | 75 | 0 | 25 |
| Hong Kong, SAR | 100 | 0 | 0 | 92 | 0 | 8 | 50 | 0 | 50 |
| Hungary | 63 | 0 | 38 | 92 | 0 | 8 | 63 | 0 | 38 |
| Indonesia | 50 | 0 | 50 | 15 | 0 | 85 | 25 | 0 | 75 |
| Iran, Islamic Rep. of | 88 | 0 | 13 | 85 | 0 | 15 | 25 | 0 | 75 |
| Israel | 63 | 0 | 38 | 46 | 8 | 46 | 63 | 25 | 13 |
| Italy | 100 | 0 | 0 | 85 | 0 | 15 | 75 | 0 | 25 |
| Japan | 88 | 0 | 13 | 77 | 0 | 23 | 38 | 0 | 63 |
| Jordan | 75 | 0 | 25 | 77 | 0 | 23 | 38 | 0 | 63 |
| Korea, Rep. of | 100 | 0 | 0 | 92 | 0 | 8 | 50 | 0 | 50 |
| Latvia | 88 | 0 | 13 | 38 | 0 | 62 | 38 | 0 | 63 |
| Lebanon | 13 | 0 | 88 | 23 | 0 | 77 | 25 | 0 | 75 |
| Lithuania | 88 | 0 | 13 | 69 | 8 | 23 | 50 | 0 | 50 |
| Macedonia, Rep. of | 75 | 0 | 25 | 100 | 0 | 0 | 0 | 13 | 88 |
| Malaysia | 100 | 0 | 0 | 77 | 0 | 23 | 38 | 0 | 63 |
| Moldova, Rep. of | 100 | 0 | 0 | 92 | 0 | 8 | 13 | 0 | 88 |
| Morocco | 13 | 0 | 88 | 38 | 0 | 62 | 13 | 0 | 88 |
| Netherlands | 63 | 13 | 25 | 23 | 38 | 38 | 50 | 13 | 38 |
| New Zealand | 100 | 0 | 0 | 77 | 15 | 8 | 100 | 0 | 0 |
| Norway | 88 | 0 | 13 | 54 | 0 | 46 | 88 | 0 | 13 |
| Palestinian Nat'l Auth. | 100 | 0 | 0 | 69 | 0 | 31 | 50 | 0 | 50 |
| Philippines | 100 | 0 | 0 | 0 | 0 | 100 | 0 | 0 | 100 |
| Romania | 75 | 0 | 25 | 92 | 0 | 8 | 50 | 0 | 50 |
| Russian Federation | 88 | 0 | 13 | 85 | 0 | 15 | 13 | 0 | 88 |
| Saudi Arabia | 75 | 0 | 25 | 62 | 0 | 38 | 13 | 0 | 88 |
| Scotland | 75 | 13 | 13 | 62 | 15 | 23 | 50 | 50 | 0 |
| Serbia | 75 | 13 | 13 | 92 | 8 | 0 | 13 | 0 | 88 |
| Singapore | 88 | 0 | 13 | 85 | 15 | 0 | 38 | 13 | 50 |
| Slovak Republic | 50 | 38 | 13 | 62 | 38 | 0 | 38 | 63 | 0 |
| Slovenia | 88 | 0 | 13 | 77 | 0 | 23 | 38 | 0 | 63 |
| South Africa | 13 | 38 | 50 | 23 | 15 | 62 | 0 | 25 | 75 |
| Sweden | 100 | 0 | 0 | 23 | 15 | 62 | 50 | 25 | 25 |
| Syrian Arab Republic | 63 | 0 | 38 | 46 | 0 | 54 | 0 | 0 | 100 |
| Tunisia | 38 | 0 | 63 | 31 | 0 | 69 | 0 | 0 | 100 |
| United States | 100 | 0 | 0 | 100 | 0 | 0 | 100 | 0 | 0 |
| International Avg. | 78 | 5 | 17 | 67 | 6 | 27 | 39 | 10 | 51 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 75 | 13 | 13 | 38 | 31 | 31 | 13 | 38 | 50 |
| Indiana State, US | 88 | 0 | 13 | 92 | 0 | 8 | 100 | 0 | 0 |
| Ontario Province, Can. | 100 | 0 | 0 | 100 | 0 | 0 | 100 | 0 | 0 |
| Quebec Province, Can. | 75 | 0 | 25 | 85 | 0 | 15 | 63 | 0 | 38 |

[^41]* Percentages may not add to 100 due to rounding.


| Countries | Percentage of TIMSS Mathematics Topics Intended to be Taught Up to and Including Fourth Grade |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Overall <br> (42 topics) |  |  | $\begin{aligned} & \text { Number } \\ & \text { (12 topics) } \end{aligned}$ |  |  | Patterns and Relationships (6 topics) |  |  |
|  | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 |
| Armenia | 81 | 14 | 5 | 83 | 17 | 0 | 83 | 17 | 0 |
| Australia | 74 | 0 | 26 | 67 | 0 | 33 | 83 | 0 | 17 |
| Belgium (Flemish) | 38 | 31 | 31 | 58 | 42 | 0 | 33 | 33 | 33 |
| Chinese Taipei | 57 | 0 | 43 | 83 | 0 | 17 | 50 | 0 | 50 |
| Cyprus | 45 | 48 | 7 | 75 | 25 | 0 | 83 | 17 | 0 |
| England | 81 | 12 | 7 | 92 | 0 | 8 | 50 | 50 | 0 |
| Hong Kong, SAR | 52 | 0 | 48 | 100 | 0 | 0 | 17 | 0 | 83 |
| Hungary | 69 | 0 | 31 | 58 | 0 | 42 | 83 | 0 | 17 |
| Iran, Islamic Rep. of | 60 | 0 | 40 | 67 | 0 | 33 | 50 | 0 | 50 |
| Italy | 86 | 0 | 14 | 92 | 0 | 8 | 67 | 0 | 33 |
| Japan | 69 | 0 | 31 | 67 | 0 | 33 | 100 | 0 | 0 |
| Latvia | 52 | 0 | 48 | 50 | 0 | 50 | 50 | 0 | 50 |
| Lithuania | 48 | 12 | 40 | 33 | 25 | 42 | 50 | 33 | 17 |
| Moldova, Rep. of | 81 | 0 | 19 | 92 | 0 | 8 | 100 | 0 | 0 |
| Morocco | 21 | 67 | 12 | 8 | 92 | 0 | 0 | 83 | 17 |
| Netherlands | 43 | 0 | 57 | 42 | 0 | 58 | 0 | 0 | 100 |
| New Zealand | 69 | 24 | 7 | 50 | 33 | 17 | 83 | 17 | 0 |
| Norway | 55 | 0 | 45 | 75 | 0 | 25 | 50 | 0 | 50 |
| Philippines | 48 | 0 | 52 | 92 | 0 | 8 | 0 | 0 | 100 |
| Russian Federation | 50 | 0 | 50 | 50 | 0 | 50 | 83 | 0 | 17 |
| Scotland | 52 | 12 | 36 | 58 | 17 | 25 | 33 | 17 | 50 |
| Singapore | 71 | 0 | 29 | 100 | 0 | 0 | 33 | 0 | 67 |
| Slovenia | 71 | 0 | 29 | 58 | 0 | 42 | 67 | 0 | 33 |
| Tunisia | 19 | 0 | 81 | 25 | 0 | 75 | 17 | 0 | 83 |
| United States | 83 | 17 | 0 | 100 | 0 | 0 | 83 | 17 | 0 |
| Yemen | 57 | 0 | 43 | 92 | 0 | 8 | 50 | 0 | 50 |
| International Avg. | 59 | 9 | 32 | 68 | 10 | 22 | 54 | 11 | 35 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 83 | 2 | 14 | 100 | 0 | 0 | 83 | 17 | 0 |
| Ontario Province, Can. | 88 | 0 | 12 | 75 | 0 | 25 | 100 | 0 | 0 |
| Quebec Province, Can. | 79 | 0 | 21 | 75 | 0 | 25 | 67 | 0 | 33 |

Exhibit 5.6: Summary of TIMSS Mathematics Topics in the Intended Curriculum

| Countries | Percentage of TIMSS Mathematics Topics Intended to be Taught Up to and Including Fourth Grade |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Measurement (6 topics) |  |  | Geometry <br> (11 topics) |  |  | Data (7 topics) |  |  |
|  | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 | Topics for All or Almost All Students | Topics for Only the More Able Students (top track) | Not Included in the Curriculum Through Grade 4 |
| Armenia | 100 | 0 | 0 | 55 | 27 | 18 | 100 | 0 | 0 |
| Australia | 100 | 0 | 0 | 45 | 0 | 55 | 100 | 0 | 0 |
| Belgium (Flemish) | 67 | 33 | 0 | 27 | 18 | 55 | 0 | 29 | 71 |
| Chinese Taipei | 50 | 0 | 50 | 27 | 0 | 73 | 71 | 0 | 29 |
| Cyprus | 50 | 50 | 0 | 0 | 73 | 27 | 29 | 71 | 0 |
| England | 100 | 0 | 0 | 73 | 9 | 18 | 86 | 14 | 0 |
| Hong Kong, SAR | 83 | 0 | 17 | 9 | 0 | 91 | 43 | 0 | 57 |
| Hungary | 100 | 0 | 0 | 36 | 0 | 64 | 100 | 0 | 0 |
| Iran, Islamic Rep. of | 83 | 0 | 17 | 45 | 0 | 55 | 57 | 0 | 43 |
| Italy | 100 | 0 | 0 | 73 | 0 | 27 | 100 | 0 | 0 |
| Japan | 83 | 0 | 17 | 27 | 0 | 73 | 100 | 0 | 0 |
| Latvia | 100 | 0 | 0 | 9 | 0 | 91 | 86 | 0 | 14 |
| Lithuania | 83 | 0 | 17 | 18 | 0 | 82 | 86 | 0 | 14 |
| Moldova, Rep. of | 83 | 0 | 17 | 64 | 0 | 36 | 71 | 0 | 29 |
| Morocco | 17 | 83 | 0 | 64 | 27 | 9 | 0 | 57 | 43 |
| Netherlands | 83 | 0 | 17 | 27 | 0 | 73 | 71 | 0 | 29 |
| New Zealand | 67 | 33 | 0 | 82 | 9 | 9 | 71 | 29 | 0 |
| Norway | 67 | 0 | 33 | 55 | 0 | 45 | 14 | 0 | 86 |
| Philippines | 67 | 0 | 33 | 9 | 0 | 91 | 57 | 0 | 43 |
| Russian Federation | 100 | 0 | 0 | 18 | 0 | 82 | 29 | 0 | 71 |
| Scotland | 67 | 17 | 17 | 36 | 9 | 55 | 71 | 0 | 29 |
| Singapore | 100 | 0 | 0 | 45 | 0 | 55 | 71 | 0 | 29 |
| Slovenia | 100 | 0 | 0 | 64 | 0 | 36 | 86 | 0 | 14 |
| Tunisia | 67 | 0 | 33 | 0 | 0 | 100 | 0 | 0 | 100 |
| United States | 100 | 0 | 0 | 64 | 36 | 0 | 71 | 29 | 0 |
| Yemen | 100 | 0 | 0 | 18 | 0 | 82 | 29 | 0 | 71 |
| International Avg. | 81 | 8 | 10 | 38 | 8 | 54 | 62 | 9 | 30 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 100 | 0 | 0 | 45 | 0 | 55 | 100 | 0 | 0 |
| Ontario Province, Can. | 100 | 0 | 0 | 100 | 0 | 0 | 71 | 0 | 29 |
| Quebec Province, Can. | 67 | 0 | 33 | 91 | 0 | 9 | 86 | 0 | 14 |

[^42]* Percentages may not add to 100 due to rounding.

At the fourth grade, as at the eighth grade, the relationship between the coverage of the TIMSS mathematics topics in participants' intended curricula and student achievement in mathematics is a moderately positive one. Higher-performing countries had generally greater levels of coverage, and lower-performing countries lesser levels. For example, high-performing Singapore and Japan had 71 and 69 percent, respectively, of mathematics topics included in their intended curricula for all or almost all students, whereas low-performing Morocco and Tunisia had just 21 and 19 percent, respectively. However, as at the eighth grade, this relationship did not hold true for all countries at the fourth grade. For example, higher-performing Hong Kong, SAR and Belgium (Flemish) had 52 and 38 percent, respectively, of mathematics topics overall included in their intended curricula for all or almost all students, and lower-performing Iran had 60 percent included in its intended curriculum.

## Are the TIMSS Mathematics Topics Taught in School?

The previous section described the coverage of the TIMSS mathematics topics in participating countries' intended curricula at the eighth and fourth grades, with a focus on the percentage of topics that were included in countries' intended curricula for all or almost all students. This section describes the coverage of the TIMSS topics in countries' implemented curricula at the eighth and fourth grades, based on teachers' reports of the percentage of students actually taught these topics.

To gather information about mathematics coverage in the implemented curricula of participating countries, the mathematics teachers ${ }^{5}$ of the students assessed were asked to indicate whether each of the TIMSS 2003 mathematics topics was "mostly taught before this year," "mostly taught this year," or "not yet taught or just introduced." Exhibit 5.7 presents for eighth and fourth grade the percentage of students whose teachers reported that the students had been taught the TIMSS mathematics topics either prior to or during the year of the assessment. The
exhibit shows for each TIMSS participant, averaged across mathematics content areas, the percentage of students whose teachers reported that the students had been taught each topic. The topics were listed in a questionnaire completed by the mathematics teachers of the students who took the TIMSS 2003 test. ${ }^{6}$ Although generally teacher participation was high, sometimes teachers did not complete the questionnaire assigned to them, so most countries had some percentage of students for whom no teacher questionnaire information is available. The exhibits in this chapter have special notations on this point. For a country where teacher responses are available for at least 70 but less than 85 percent of the students, an " $r$ " is included next to its data. Where teacher responses are available for at least 50 but less than 70 percent of students, an "s" is included. Where teacher responses are available for less than 50 percent, an " $x$ " replaces the data.

Exhibit 5.7 shows that, according to their teachers, on average 72 percent of the eighth-grade students tested in TIMSS 2003 had been taught the TIMSS mathematics topics. In Armenia and Macedonia almost all students ( $90 \%$ or more) had been taught the topics, as had the majority of students in every country except Botswana.

Consistent with the information on the intended curriculum presented in the previous section, number was the content area with the greatest coverage, with 95 percent of students across countries having been taught the TIMSS number topics by the eighth grade. This was followed by measurement ( $78 \%$ ), geometry ( $69 \%$ ), algebra ( $66 \%$ ), and data $(46 \%)$. All but 5 countries had 90 percent or more of their students taught the number topics, while 25 participating entities had less than half their students taught the data topics.

The agreement between the average percentages of TIMSS topics in countries' eighth-grade intended mathematics curricula and the percentages of students actually taught the TIMSS mathematics topics by the eighth grade is rather striking. The differences in these percentages were a mere two percentage points for the mathematics topics overall, one percentage point for number, three percentage points for algebra,

| Countries | Average Percentage of Students Taught the TIMSS Mathematics Topics |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Overall (45 topics) |  | Number (10 topics) |  | Algebra (6 topics) |  | Measurement (8 topics) |  | Geometry <br> (13 topics) |  | Data (8 topics) |
| Armenia | $r$ | 90 (0.7) | $r$ | 100 (0.2) | $r$ | 93 (1.0) | $r$ | 95 (0.8) | $r$ | 92 (0.8) | s | 65 (3.0) |
| Australia |  | 71 (1.1) |  | 95 (0.7) |  | 61 (2.1) |  | 79 (1.4) |  | 61 (1.7) |  | 57 (2.7) |
| Bahrain |  | 66 (0.6) |  | 100 (0.1) |  | 42 (1.6) |  | 69 (1.8) |  | 72 (0.8) |  | 28 (1.3) |
| Belgium (Flemish) |  | 62 (1.0) |  | 93 (0.8) |  | 42 (1.9) |  | 69 (1.9) |  | 61 (1.0) |  | 35 (2.0) |
| Botswana |  | 40 (1.1) |  | 88 (0.6) |  | 26 (2.0) |  | 49 (2.4) |  | 26 (1.8) |  | 6 (1.3) |
| Bulgaria |  | 75 (0.7) |  | 99 (0.3) |  | 86 (1.3) |  | 93 (1.1) |  | 70 (0.9) |  | 24 (2.0) |
| Chile |  | 66 (1.2) |  | 93 (0.8) |  | 55 (1.9) |  | 59 (2.4) |  | 64 (1.3) |  | 47 (2.6) |
| Chinese Taipei |  | 72 (0.7) |  | 99 (0.6) |  | 89 (1.1) |  | 88 (1.5) |  | 73 (1.3) |  | 6 (1.6) |
| Cyprus |  | 53 (0.5) |  | 89 (0.8) |  | 34 (1.1) |  | 62 (1.2) |  | 59 (0.5) |  | 4 (0.7) |
| Egypt |  | 88 (0.6) |  | 99 (0.4) |  | 91 (1.0) |  | 92 (1.4) |  | 94 (0.6) |  | 60 (1.8) |
| Estonia |  | 80 (0.8) |  | 98 (0.9) |  | 82 (1.2) |  | 92 (1.0) |  | 69 (1.1) |  | 62 (2.5) |
| Ghana |  | 60 (1.6) |  | 83 (1.6) |  | 59 (2.2) |  | 53 (2.9) |  | 51 (2.4) |  | 55 (2.7) |
| Hong Kong, SAR |  | 77 (1.0) |  | 98 (0.5) |  | 66 (2.1) |  | 86 (1.8) |  | 81 (1.3) |  | 45 (2.5) |
| Hungary |  | 85 (0.8) |  | 100 (0.1) |  | 93 (1.2) |  | 98 (0.5) |  | 83 (1.0) |  | 54 (2.7) |
| Indonesia |  | 79 (1.0) |  | 98 (0.7) |  | 72 (1.8) |  | 88 (1.4) |  | 69 (1.3) |  | 68 (2.5) |
| Iran, Islamic Rep. of |  | 75 (1.0) |  | 95 (0.8) |  | 65 (2.2) |  | 64 (2.2) |  | 91 (0.8) |  | 43 (2.2) |
| Israel |  | 61 (1.2) |  | 96 (0.6) |  | 69 (1.5) |  | 60 (2.5) |  | 45 (1.4) |  | 41 (2.4) |
| Italy |  | 79 (0.8) |  | 99 (0.2) |  | 62 (1.9) |  | 88 (1.2) |  | 85 (0.9) |  | 50 (2.3) |
| Japan |  | 74 (0.8) |  | 98 (0.8) |  | 92 (1.0) |  | 79 (1.9) |  | 75 (0.8) |  | 21 (2.3) |
| Jordan |  | 77 (0.9) |  | 99 (0.4) |  | 63 (1.7) |  | 89 (1.8) |  | 80 (1.0) |  | 44 (2.4) |
| Korea, Rep. of | s | 81 (1.2) | $s$ | 92 (1.1) | s | 87 (1.4) | 5 | 81 (1.9) | $s$ | 85 (1.5) | s | 59 (2.5) |
| Latvia | s | 67 (1.1) | 5 | 98 (0.5) | s | 52 (2.4) | s | 63 (2.4) | s | 61 (1.7) | s | 48 (3.0) |
| Lebanon |  | 68 (1.4) |  | 92 (1.1) |  | 58 (2.7) |  | 72 (2.1) |  | 71 (1.6) |  | 38 (3.0) |
| Lithuania |  | 82 (0.8) |  | 99 (0.2) |  | 69 (2.0) |  | 92 (0.9) |  | 76 (1.1) |  | 69 (2.0) |
| Macedonia, Rep. of |  | 95 (0.7) |  | 99 (0.7) |  | 98 (0.6) |  | 90 (1.6) |  | 99 (0.5) |  | - |
| Malaysia |  | 72 (1.1) |  | 99 (0.3) |  | 54 (2.1) |  | 72 (1.9) |  | 80 (1.4) |  | 40 (2.5) |
| Moldova, Rep. of | $r$ | 82 (1.3) | $r$ | 94 (1.9) | $r$ | 89 (1.8) | $r$ | 81 (1.8) | $r$ | 82 (1.5) | $r$ | 57 (3.7) |
| Morocco | s | 63 (1.4) | 5 | 96 (0.9) | $s$ | 46 (3.2) | s | 76 (3.0) | $s$ | 56 (2.0) |  | $\mathrm{x} \times$ |
| Netherlands |  | 71 (1.1) |  | 93 (1.0) |  | 71 (2.7) |  | 81 (1.6) |  | 64 (1.8) |  | 43 (2.1) |
| New Zealand |  | 75 (1.5) |  | 94 (1.0) |  | 67 (2.5) |  | 80 (2.2) |  | 62 (1.8) |  | 69 (2.5) |
| Norway |  | 55 (1.1) |  | 87 (1.4) |  | 23 (1.5) |  | 66 (2.3) |  | 41 (1.4) |  | 53 (2.6) |
| Palestinian Nat'l Auth. |  | 71 (0.9) |  | 98 (0.7) |  | 42 (2.1) |  | 77 (2.0) |  | 71 (1.0) |  | 54 (1.6) |
| Philippines |  | 60 (1.7) |  | 98 (1.0) |  | 85 (1.9) |  | 67 (2.9) |  | 33 (3.2) |  | 30 (3.1) |
| Romania |  | 89 (0.7) |  | 100 (0.0) |  | 94 (1.2) |  | 94 (1.0) |  | 95 (0.5) |  | 59 (2.6) |
| Russian Federation |  | - - |  | -- |  | -- |  | - |  | - - |  | -- |
| Saudi Arabia |  | 62 (1.3) |  | 92 (1.6) |  | 55 (2.3) |  | 66 (3.1) |  | 65 (1.3) |  | 18 (2.1) |
| Scotland |  | 68 (1.3) |  | 93 (1.0) |  | 47 (2.9) |  | 79 (1.6) |  | 56 (1.7) |  | 62 (2.1) |
| Serbia |  | 89 (1.3) |  | 94 (2.2) |  | 95 (1.0) |  | 93 (1.5) |  | 92 (1.9) |  | 65 (2.7) |
| Singapore |  | 83 (0.5) |  | 100 (0.1) |  | 89 (0.8) |  | 86 (0.7) |  | 82 (1.0) |  | 54 (1.1) |
| Slovak Republic |  | 69 (0.6) |  | 100 (0.1) |  | 54 (1.4) |  | 90 (1.1) |  | 71 (0.8) |  | 18 (1.9) |
| Slovenia |  | 66 (0.7) |  | 92 (0.5) |  | 40 (1.9) |  | 81 (1.6) |  | 69 (0.9) |  | 31 (1.8) |
| South Africa | $r$ | 55 (1.6) | r | 77 (1.9) | r | 57 (2.4) | $r$ | 49 (2.5) | $r$ | 48 (2.0) | $r$ | 40 (2.6) |
| Sweden |  | 60 (0.9) |  | 93 (0.5) |  | 43 (2.1) |  | 78 (1.1) |  | 40 (1.3) |  | 47 (1.9) |
| Syrian Arab Republic |  | - - |  | - - |  | -- |  | -- |  | -- |  | -- |
| Tunisia |  | 64 (1.1) |  | 93 (0.9) |  | 44 (2.2) |  | 75 (2.0) |  | 60 (1.2) |  | 37 (2.3) |
| United States |  | 83 (0.8) |  | 100 (0.2) |  | 80 (1.3) |  | 84 (1.2) |  | 72 (1.6) |  | 83 (1.3) |
| $\ddagger$ England | $s$ | 83 (1.5) | s | 99 (0.5) | s | 73 (3.1) | s | 84 (2.3) | 5 | 77 (2.1) | $s$ | 79 (2.2) |
| International Avg. |  | 72 (0.2) |  | 95 (0.1) |  | 66 (0.3) |  | 78 (0.3) |  | 69 (0.2) |  | 46 (0.4) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 67 (1.4) |  | 98 (0.4) |  | 57 (3.0) |  | 76 (2.0) |  | 65 (2.1) |  | 30 (3.5) |
| Indiana State, US |  | 81 (1.8) |  | 99 (0.3) |  | 74 (2.9) |  | 86 (2.0) |  | 66 (3.5) |  | 82 (2.7) |
| Ontario Province, Can. |  | 80 (1.0) |  | 93 (1.1) |  | 60 (2.2) |  | 86 (1.2) |  | 75 (2.1) |  | 82 (2.3) |
| Quebec Province, Can. |  | 68 (1.2) |  | 99 (0.5) |  | 58 (2.6) |  | 66 (2.0) |  | 66 (2.0) |  | 42 (2.4) |

[^43]"An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for ess than $50 \%$ of the students.
See Exhibits 5.8 through 5.12 for data on individual topics.

| Countries | Average Percentage of Students Taught the TIMSS Mathematics Topics |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Overall (42 topics) |  | Number (12 topics) |  | Patterns and Relationships (6 topics) |  | Measurement (6 topics) |  | Geometry <br> (11 topics) |  | $\begin{aligned} & \text { Data } \\ & \text { (7 topics) } \end{aligned}$ |
| Armenia | $r$ | 73 (1.1) | $r$ | 91 (0.9) | $r$ | 86 (1.4) | r | 93 (1.3) | $r$ | 38 (2.5) | $r$ | 67 (2.4) |
| Australia |  | 77 (1.5) |  | 74 (1.7) |  | 79 (3.1) |  | 89 (1.5) |  | 69 (1.5) |  | 81 (2.4) |
| Belgium (Flemish) |  | 81 (1.0) |  | 93 (1.1) |  | 83 (1.6) |  | 93 (1.0) |  | 62 (1.8) |  | 79 (1.6) |
| Chinese Taipei |  | 78 (1.1) |  | 86 (1.0) |  | 80 (1.8) |  | 96 (1.0) |  | 53 (2.3) |  | 89 (1.9) |
| Cyprus |  | 86 (0.9) |  | 95 (0.7) |  | 87 (1.4) |  | 95 (1.0) |  | 72 (1.9) |  | 86 (1.7) |
| England | $r$ | 88 (0.9) | $r$ | 87 (1.2) | $r$ | 80 (1.9) | $r$ | 95 (0.9) | $r$ | 87 (1.5) | $r$ | 89 (1.5) |
| Hong Kong, SAR |  | 73 (1.2) |  | 90 (1.1) |  | 55 (2.7) |  | 84 (2.1) |  | 53 (2.5) |  | 83 (1.9) |
| Hungary |  | 73 (1.2) |  | 68 (1.1) |  | 92 (1.0) |  | 89 (1.3) |  | 61 (2.1) |  | 74 (2.9) |
| Iran, Islamic Rep. of |  | 68 (1.4) |  | 70 (1.4) |  | 65 (2.3) |  | 85 (1.8) |  | 58 (1.9) |  | 68 (2.4) |
| Italy |  | 78 (0.9) |  | 88 (1.0) |  | 73 (1.7) |  | 71 (2.0) |  | 72 (1.6) |  | 83 (1.7) |
| Japan |  | 54 (1.0) |  | 59 (1.4) |  | 63 (1.9) |  | 80 (1.7) |  | 21 (1.1) |  | 69 (2.0) |
| Latvia | s | 72 (1.4) | s | 67 (2.1) | $s$ | 89 (1.7) | s | 93 (1.1) | 5 | 45 (2.7) | s | 87 (1.9) |
| Lithuania |  | 78 (1.2) |  | 77 (1.4) |  | 83 (1.6) |  | 93 (0.9) |  | 63 (1.9) |  | 87 (1.8) |
| Moldova, Rep. of | $r$ | 88 (0.9) | $r$ | 94 (0.9) | $r$ | 93 (1.3) | $r$ | 98 (0.5) | $r$ | 71 (2.1) | $r$ | 89 (1.8) |
| Morocco |  | x x |  | $\mathrm{x} \times$ |  | x x |  | x x |  | x x |  | $\mathrm{x} \times$ |
| Netherlands |  | 54 (1.1) |  | 63 (1.5) |  | 67 (2.2) |  | 78 (1.9) |  | 13 (1.6) |  | 67 (2.6) |
| New Zealand |  | 77 (1.0) |  | 76 (1.2) |  | 84 (1.7) |  | 85 (1.4) |  | 65 (1.7) |  | 87 (1.4) |
| Norway |  | 52 (1.3) |  | 54 (1.6) |  | 53 (2.2) |  | 78 (2.1) |  | 32 (2.5) |  | 54 (2.8) |
| Philippines |  | 79 (1.9) |  | 95 (0.9) |  | 73 (3.2) |  | 78 (3.2) |  | 71 (2.8) |  | 72 (3.1) |
| Russian Federation |  | -- |  | - |  | - |  | -- |  | - |  | - - |
| Scotland | $r$ | 75 (1.2) | $r$ | 67 (1.8) | $r$ | 84 (1.9) | r | 86 (2.6) | $r$ | 65 (1.8) | r | 86 (1.9) |
| Singapore |  | 82 (0.8) |  | 97 (0.5) |  | 87 (1.5) |  | 95 (0.9) |  | 51 (1.8) |  | 90 (1.5) |
| Slovenia |  | 59 (1.1) |  | 54 (0.9) |  | 86 (1.5) |  | 59 (1.9) |  | 34 (1.5) |  | 84 (2.1) |
| Tunisia | r | 58 (1.0) | $r$ | 40 (0.9) | $r$ | 85 (1.9) | $r$ | 82 (1.9) | $r$ | 43 (1.6) | $r$ | 71 (2.7) |
| United States |  | 82 (0.8) |  | 83 (1.1) |  | 89 (1.0) |  | 81 (1.3) |  | 74 (1.5) |  | 90 (1.2) |
| Yemen |  | - |  | - - |  | - |  | - |  | - - |  | - - |
| International Avg. |  | 73 (0.2) |  | 77 (0.3) |  | 79 (0.4) |  | 86 (0.3) |  | 55 (0.4) |  | 80 (0.4) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 75 (1.5) |  | 79 (2.1) |  | 84 (2.2) |  | 78 (3.2) |  | 57 (3.5) |  | 87 (1.7) |
| Ontario Province, Can. |  | 80 (1.1) |  | 75 (2.1) |  | 83 (1.7) |  | 86 (1.8) |  | 75 (2.3) |  | 91 (1.9) |
| Quebec Province, Can. |  | 68 (1.3) |  | 67 (1.6) |  | 83 (1.5) |  | 70 (2.6) |  | 59 (1.8) |  | 69 (2.9) |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.
See Exhibits 5.13 through 5.17 for data on individual topics.
no difference for measurement, two percentage points for geometry, and seven percentage points for data.

Although there was great agreement between coverage in the intended curriculum and the implemented curriculum internationally at the eighth grade, there was wide variation among individual countries. Agreement between the percentage of TIMSS mathematics topics included in a country's intended curriculum and the percentage of students taught the TIMSS mathematics topics in that country by the eighth grade was within 5 percentage points in 19 countries spanning the entire spectrum of achievement: Australia, Botswana, Bulgaria, Chile, Chinese Taipei, Egypt, Hong Kong SAR, Hungary, Iran, Jordan, Korea, Latvia, Malaysia, Moldova, New Zealand, the Palestinian National Authority, Romania, Saudi Arabia, and Singapore. However, there were also several participants where the level of agreement between coverage of the intended and implemented curricula was much less.

At the fourth grade, Exhibit 5.7 shows that internationally, on average, 73 percent of the students tested in TIMSS 2003 had been taught the TIMSS mathematics topics, with the percentage ranging from 88 percent in England and Moldova to 52 percent in Norway. The majority of students in every country had been taught the topics.

Consistent with the data reported on the intended mathematics curriculum at the fourth grade (Exhibit 5.6), measurement was the content area with the greatest percentage of students taught the topics ( $86 \%$ ). The percentages of fourth-grade students internationally, on average, taught the TIMSS mathematics topics in the content areas of data, patterns and relationships, and number were rather similar. A full 80 percent of the students across countries had been taught the data topics by the fourth grade, 79 percent of students had been taught the patterns and relationships topics, and 77 percent of students had been taught the number topics. Across countries, the range for data was from 90 percent in the United States to 54 percent in Norway, for patterns and relationships from 93 percent in Moldova to 53 percent in Norway, and for number from 97 percent in Singapore to 40 percent in Tunisia.

5 At fourth grade there was one teacher questionnaire that asked about both mathematics and science, and at eighth grade there were separate questionnaires for mathematics teachers and science teachers.

There was much less agreement at fourth grade than at eighth grade between the average percentages of TIMSS topics in countries' intended mathematics curricula and the percentages of students actually taught the TIMSS mathematics topics.

## Which TIMSS Mathematics Topics Are in the Intended and Implemented Curriculum?

For first the eighth grade and then the fourth grade, this section presents information about the coverage of each individual mathematics topic in each country's intended and implemented curriculum. For each topic, the exhibits indicate whether the topic was intended to be taught and if so, to all or only the more able students; the grade(s) at which the topic was primarily intended to be taught; and the percentage of students actually taught the topic. Exhibits 5.8 through 5.12 present these data for the mathematics content areas at eighth grade, and Exhibits 5.13 through 5.17 for those at fourth grade.

Exhibit 5.8 presents information on the ten number topics at eighth grade. As shown in this exhibit, the TIMSS number topics were included in the intended curriculum of almost all participants. In particular, three topics - "common fractions," "decimal fractions," and "computations with decimals" - were included by all participants for all or almost all students. Exhibit 5.8 shows, however, that there was great variation among participants in the grade(s) at which the number topics were primarily intended to be taught. Also, while some countries reported that topics were intended to be taught primarily at a single grade, many provided a range of grades in which they are taught. According to the exhibit, teachers reported that the TIMSS number topics had been taught to almost all students, with more than 90 percent of students taught each of the topics except "ratios," where the figure was 86 percent.

| Number | Whole numbers including place value， factorization，and the four operations |  |  | Computations， estimations，or approximations involving whole numbers |  |  | Common fractions |  |  | Decimal fractions |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | － | －－ | r 100 （0．0） | － | －－ | r 98 （1．2） | － | －－ | r 100 （0．0） | － | －－ | r 100 （0．0） |  |
| Australia | $\bigcirc$ | 3－6 | 100 （0．1） | － | 5－8 | 96 （2．1） | $\bigcirc$ | 5－8 | 100 （0．2） | － | 5－8 | 98 （0．9） |  |
| Bahrain | － | 1－6 | 100 （0．0） | － | 1－6 | 99 （0．6） | － | 3－4 | 100 （0．0） | － | 5 | 100 （0．0） |  |
| Belgium（Flemish） | － | －－ | 99 （0．5） | － | －－ | 100 （0．0） | － | －－ | 98 （1．1） | － | －－ | 90 （2．3） |  |
| Botswana | － | 8 | 100 （0．0） | － | 8 | 94 （2．1） | － | 6 | 99 （0．6） | － | 8 | 99 （0．7） |  |
| Bulgaria | － | 4 | 99 （0．9） | $\bigcirc$ | 4 | 88 （3．0） | － | 5 | 100 （0．0） | － | 5 | 100 （0．0） | $\stackrel{\text { \＃}}{\text { ¢ }}$ |
| Chile | － | 4 | 99 （0．9） | － | 4 | 98 （0．9） | － | 5 | 97 （1．1） | － | 8 | 98 （1．0） | $\leqq$ |
| Chinese Taipei | － | 7 | 99 （0．6） | － | 7 | 99 （0．6） | － | 7 | 99 （0．6） | $\bigcirc$ | 7 | 99 （0．6） | n |
| Cyprus | － | 4－7 | 87 （1．8） | $\bigcirc$ | 4－7 | 62 （2．3） | － | 4－7 | 96 （1．2） | － | 4－7 | 84 （1．7） |  |
| Egypt | － | 1－4 | 100 （0．0） | － | 1－5 | 100 （0．0） | － | 4－5 | 100 （0．0） | － | 5 | 96 （1．6） | － |
| Estonia | － | 5 | 98 （1．1） | － | 5 | 98 （1．1） | － | 6 | 98 （1．0） | － | 6 | 98 （1．0） | نّ |
| Ghana | － | －－ | 96 （1．8） | － | －－ | 77 （3．9） | － | －－ | 91 （2．8） | － | －－ | 89 （3．2） | $\stackrel{\text { cren }}{\substack{3}}$ |
| Hong Kong，SAR | － | 1－4 | 99 （0．9） | － | 4 | 97 （1．5） | － | 4 | 97 （1．7） | － | 5 | 99 （1．1） | $\bigcirc$ |
| Hungary | － | 4 | 100 （0．0） | － | 4 | 99 （0．7） | － | 5 | 100 （0．0） | － | 6 | 100 （0．0） |  |
| Indonesia | － | 4－6 | 98 （1．3） | － | 5－8 | 96 （2．1） | － | 6－8 | 98 （1．5） | － | 6－8 | 99 （1．3） | \％ |
| Iran，Islamic Rep．of | － | 1－9 | 93 （2．2） | － | 1－9 | 90 （2．8） | － | 5－6 | 98 （1．1） | － | 6 | 95 （1．7） | $\frac{0}{5}$ |
| Israel | － | 1－3 | 98 （1．0） | － | 1－3 | 95 （1．2） | － | 4－5 | 98 （1．0） | － | 5－7 | 98 （1．0） | ¢ |
| Italy | － | 2－6 | 100 （0．0） | － | 1－6 | 99 （0．7） | － | 4－7 | 100 （0．0） | － | 4－7 | 100 （0．0） | － |
| Japan | － | 1－4 | 100 （0．0） | － | 4－6 | 97 （1．6） | － | 5 | 98 （1．4） | － | 5 | 98 （1．4） | $\stackrel{\square}{\square}$ |
| Jordan | － | 1－6 | 100 （0．0） | － | 1－6 | 99 （0．8） | － | 2－5 | 99 （0．8） | － | 4－8 | 99 （0．8） | O |
| Korea，Rep．of | $\bigcirc$ | 9 | s 71 （3．3） | － | －－ | 99 （0．8） | － | －－ | s 95 （1．4） | － | －－ | s 99 （0．9） | ¢ |
| Latvia | － | 6－7 | s 100 （0．0） | － | 6－7 | 85 （4．5） | － | 6 | s 100 （0．0） | － | 6－7 | s 100 （0．0） | $\xi$ |
| Lebanon | － | 8 | 99 （1．0） | $\bigcirc$ | 9－10 | 88 （3．0） | － | －－ | 98 （1．2） | － | －－ | 95 （1．8） | ， |
| Lithuania | － | 1－6 | 100 （0．0） | － | 1－5 | 97 （1．3） | － | 6 | 100 （0．0） | － | 6 | 100 （0．0） | 此 |
| Macedonia，Rep．of | － | 1－5 | 99 （1．0） | － | 1－5 | 99 （0．7） | － | 5 | 99 （0．7） | － | 5 | 99 （1．0） | $\stackrel{\text { U }}{\sim}$ |
| Malaysia | － | 1－7 | 97 （1．6） | － | 3－7 | 99 （0．7） | － | 4 | 100 （0．0） | － | 4－7 | 99 （1．0） | $\stackrel{ \pm}{ \pm}$ |
| Moldova，Rep．of | － | 5－6 | r 94 （2．3） | － | 5－6 | r 94 （2．2） | － | 5 | r 92 （2．5） | － | 5－6 | r 92 （2．7） | \％ |
| Morocco | － | －－ | s 99 （0．7） | － | －－ | 99 （1．0） | － | －－ | s 100 （0．0） | － | －－ | S 97 （2．1） | $\frac{\square}{3}$ |
| Netherlands | － | K－6 | 65 （4．2） | － | K－6 | 94 （2．0） | － | K－6 | 98 （1．3） | － | K－6 | 97 （1．6） | $\stackrel{\square}{\text { ¢ }}$ |
| New Zealand | － | 2－7 | 100 （0．1） | － | 4－7 | 95 （2．7） | － | 4－9 | 99 （0．8） | － | 5－9 | 98 （1．2） | $\stackrel{\square}{2}$ |
| Norway | － | 2－10 | 99 （0．7） | － | 3－10 | 98 （1．3） | － | 4－10 | 90 （2．6） | － | 4－10 | 94 （2．0） | 2 |
| Palestinian Nat＇l Auth． | － | 1－5 | 99 （0．6） | － | 1－6 | 95 （2．1） | － | 1－5 | 98 （1．4） | － | 1－6 | 100 （0．0） | $\bigcirc$ |
| Philippines | － | 7 | 98 （1．2） | － | 7 | 98 （1．4） | － | －－ | 98 （1．3） | － | －－ | 99 （1．0） | n |
| Romania | － | 1－5 | 100 （0．0） | － | 1－5 | 100 （0．0） | － | 4－6 | 100 （0．0） | － | 5－7 | 100 （0．0） | － |
| Russian Federation | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | $\stackrel{\text { ¢ }}{4}$ |
| Saudi Arabia | － | 1－7 | 90 （3．5） | － | 4 | 88 （3．7） | － | 4－5 | 98 （1．2） | － | 4－6 | 94 （4．3） | $\stackrel{\square}{0}$ |
| Scotland | － | －－ | 96 （1．7） | － | －－ | 99 （0．6） | － | －－ | 95 （1．4） | － | －－ | 97 （1．6） | －0 |
| Serbia | － | 6 | 94 （2．2） | － | 6 | 94 （2．2） | － | 5 | 94 （2．2） | － | 5 | 95 （2．1） | $\stackrel{\square}{\circ}$ |
| Singapore | － | 1－5 | 100 （0．0） | $\bigcirc$ | 1－5 | 99 （0．4） | － | 3－5 | 100 （0．0） | － | 4－5 | 100 （0．3） | $\stackrel{\square}{ \pm}$ |
| Slovak Republic | － | 6 | 100 （0．0） | $\bigcirc$ | 5 | 100 （0．0） | － | 6 | 100 （0．0） | － | 5 | 100 （0．0） | $\stackrel{\text { ¢ }}{+}$ |
| Slovenia | － | 8 | 99 （0．7） | － | 5 | 97 （1．4） | － | 6 | 100 （0．0） | － | 7 | 100 （0．0） | ঠิ |
| South Africa | － | －－ | r 87 （2．5） | － | －－ | r 73 （3．3） | － | －－ | 89 （2．5） | － | －－ | r 77 （3．2） |  |
| Sweden | － | 7 | 100 （0．4） | － | 7 | 99 （0．7） | － | 7 | 98 （0．7） | － | 7 | 98 （0．8） | － |
| Syrian Arab Republic | $\bigcirc$ | －－ | －－ | － | －－ | － | － | －－ | －－ | － | －－ | －－ | ニ |
| Tunisia | $\bigcirc$ | －－ | 99 （0．6） | － | －－ | 96 （1．7） | － | －－ | 98 （1．1） | － | －－ | 97 （1．4） | ¢ |
| United States | － | －－ | 100 （0．0） | － | －－ | 99 （0．5） | － | －－ | 100 （0．3） | － | －－ | 100 （0．1） | 云 |
| ま England | $\bigcirc$ | K－7 | s 100 （0．0） | $\bigcirc$ | K－8 | 100 （0．0） | － | 2－5 | s 100 （0．0） | $\bigcirc$ | 3－6 | s 99 （1．4） | $\overline{\bar{T}}$ |
| International Avg． |  |  | 97 （0．2） |  |  | 95 （0．3） |  |  | 98 （0．2） |  |  | 97 （0．2） | 苂 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  | $\frac{\text { E }}{10}$ |
| Basque Country，Spain | $\odot$ | 10 | 100 （0．0） | － | －－ | 100 （0．5） | － | －－ | 100 （0．0） | － | －－ | 98 （1．3） | ¢ |
| Indiana State，US | － | －－ | 100 （0．0） | － | －－ | 100 （0．0） | － | －－ | 100 （0．0） | － | －－ | 100 （0．0） | $\overline{\text { ¢ }}$ |
| Ontario Province，Can． | － | 6－8 | 100 （0．1） | － | 1－6 | 100 （0．0） | － | 5－6 | 96 （2．0） | － | 4－7 | 97 （1．7） | － |
| Quebec Province，Can． | － | 1－6 | 97 （1．6） | － | 1－6 | 98 （1．6） | － | 4－7 | 98 （1．4） | － | 2－7 | 97 （1．9） |  |

[^44]| Number | Representing decimals and fractions |  |  | Computations with fractions |  |  | Computations with decimals |  |  | Integers including words，numbers， or models |  |  | $\stackrel{\text { On }}{\substack{\text { N }}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  | 槀 |
| Armenia | $\bullet$ | －－ | r 99 （0．7） | $\bullet$ | －－ | 100 （0．0） | $\bullet$ | －－ | r 100 （0．0） | $\bullet$ | －－ | r 99 （0．7） |  |
| Australia | $\bullet$ | 5－8 | 98 （1．1） | $\bullet$ | 5－8 | 97 （1．1） | － | 5－8 | 98 （0．9） | $\bullet$ | 8 | 97 （1．2） |  |
| Bahrain | － | 4－6 | 100 （0．5） | － | 4－7 | 100 （0．0） | － | 5－7 | 100 （0．0） | － | 7 | 100 （0．0） |  |
| Belgium（Flemish） | $\bullet$ | －－ | 92 （1．9） | $\bullet$ | －－ | 98 （1．1） | － | －－ | 99 （0．9） | $\bullet$ | －－ | 90 （1．5） |  |
| Botswana | － | 6 | 89 （2．9） | $\bullet$ | 8 | 95 （1．7） | － | 8 | 97 （1．4） | $\bullet$ | 8 | 95 （2．1） |  |
| Bulgaria | $\bullet$ | 6 | 100 （0．2） | $\bullet$ | 5 | 100 （0．0） | $\bullet$ | 5 | 100 （0．0） | $\bullet$ | 6 | 100 （0．0） |  |
| Chile | － | 8 | 96 （1．4） | － | 5－6 | 97 （1．0） | － | 6－7 | 98 （0．9） | － | 8 | 96 （1．6） |  |
| Chinese Taipei | $\bullet$ | 7 | 99 （0．9） | $\bullet$ | 7 | 99 （0．6） | － | 7 | 99 （0．6） | － | 7 | 99 （0．7） |  |
| Cyprus | $\bullet$ | 4－7 | 82 （1．9） | － | 4－7 | 99 （0．6） | － | 4－7 | 91 （1．3） | － | 4－8 | 94 （1．3） |  |
| Egypt | $\bullet$ | 5 | 99 （0．9） | $\bullet$ | 5 | 99 （0．9） | $\bullet$ | 5 | 98 （1．3） | － | 7 | 99 （0．5） |  |
| Estonia | － | 6 | 98 （1．0） | － | 6 | 98 （1．0） | － | 5 | 98 （1．0） | － | 6－7 | 97 （1．3） |  |
| Ghana | － | －－ | 90 （3．1） | $\bullet$ | －－ | 82 （4．2） | － | －－ | 72 （3．9） | $\bullet$ | －－ | 92 （2．7） |  |
| Hong Kong，SAR | $\bullet$ | 7 | 95 （1．9） | $\bullet$ | 6 | 99 （0．7） | $\bullet$ | 5 | 99 （0．7） | － | 7－9 | 98 （1．3） | － |
| Hungary | － | 6 | 100 （0．0） | $\bullet$ | 7 | 100 （0．0） | $\bullet$ | 7 | 100 （0．0） | $\bullet$ | 7 | 100 （0．0） |  |
| Indonesia | － | 6－8 | 98 （1．1） | － | 5－8 | 100 （0．0） | － | 6－8 | 100 （0．0） | － | 4－8 | 98 （1．2） |  |
| Iran，Islamic Rep．of | － | 6 | 98 （1．3） | $\bullet$ | 6 | 99 （0．7） | － | 6 | 98 （1．0） | $\bullet$ | 6 | 99 （0．8） | － |
| Israel | $\bullet$ | 4－7 | 96 （1．3） | － | 5－7 | 98 （0．5） | － | 5－7 | 98 （1．0） | － | 2－7 | 99 （0．8） | ᄃ |
| Italy | － | 4－6 | 100 （0．3） | $\bullet$ | 4－8 | 100 （0．0） | $\bullet$ | 4－8 | 100 （0．0） | － | 6 －8 | 100 （0．3） | － |
| Japan | － | 4 | 98 （1．2） | － | 5－6 | 100 （0．0） | － | 4－5 | 100 （0．0） | － | 7 | 99 （0．6） | － |
| Jordan | $\bullet$ | 4－7 | 100 （0．0） | $\bullet$ | 4－7 | 99 （0．8） | $\bullet$ | 4－7 | $99(0.8)$ | $\bullet$ | 7－10 | 99 （0．5） | 5 |
| Korea，Rep．of | $\bullet$ | －－ | s 96 （1．3） | － | －－ | 94 （2．0） | $\bullet$ | －－ | s 96 （1．8） | － | －－ | s 95 （1．5） | ¢ |
| Latvia | $\bullet$ | 6－7 | s 100 （0．0） | － | 6 | 100 （0．0） | $\bullet$ | 6 | s 100 （0．0） | － | 6－7 | s 100 （0．0） | E |
| Lebanon | $\bullet$ | 8 | 92 （2．4） | － | －－ | 97 （1．4） | － | －－ | 97 （1．5） | － | －－ | 96 （1．8） | $\frac{}{3}$ |
| Lithuania | $\bullet$ | 4－6 | 100 （0．0） | － | 6 | 100 （0．0） | $\bullet$ | 5－6 | 100 （0．0） | － | 6－8 | 100 （0．0） |  |
| Macedonia，Rep．of | － | 5－6 | 99 （0．7） | － | 5 | 99 （0．7） | $\bullet$ | 6 | $99(0.7)$ | － | 6－7 | 99 （0．9） | 。 |
| Malaysia | $\bullet$ | 4－7 | 99 （0．7） | $\bullet$ | 4－7 | 100 （0．0） | － | 4－7 | 100 （0．0） | － | 7 | 100 （0．0） | $\stackrel{\sim}{ \pm}$ |
| Moldova，Rep．of | $\bullet$ | 5 | 95 （2．2） | － | 5－7 | 95 （2．0） | － | 5，7 | 95 （2．1） | $\bullet$ | 6 | r 94 （2．2） | $\bigcirc$ |
| Morocco | $\bigcirc$ | －－ | s 93 （3．2） | $\bullet$ | －－ | 100 （0．0） | $\bullet$ | －－ | s 100 （0．0） | $\bullet$ | －－ | s $99(0.9)$ | $\stackrel{\square}{0}$ |
| Netherlands | － | K－6 | 95 （2．0） | $\bullet$ | K－6 | 95 （2．1） | $\bullet$ | K－6 | 97 （1．5） | － | K－6 | 97 （2．7） | $\stackrel{\square}{\square}$ |
| New Zealand | $\bullet$ | 2－5 | 98 （1．1） | $\bigcirc$ | 8－9 | 95 （1．5） | － | 5－9 | 98 （0．9） | $\bigcirc$ | 6－9 | 95 （2．3） | $\stackrel{\square}{\circ}$ |
| Norway | $\bullet$ | 4－10 | 84 （3．1） | $\bullet$ | 5－10 | 85 （2．8） | $\bullet$ | 5－10 | 97 （1．4） | － | 6－10 | 98 （1．2） | 2 |
| Palestinian Nat＇l Auth． | $\bullet$ | 3－6 | 99 （0．7） | － | 3－6 | 99 （1．1） | $\bullet$ | 3－6 | 98 （1．2） | － | 6－7 | 99 （1．1） | $\bigcirc$ |
| Philippines | $\bullet$ | －－ | 97 （1．5） | － | －－ | 99 （0．8） | $\bullet$ | －－ | 97 （1．6） | － | 7 | 98 （1．2） |  |
| Romania | $\bullet$ | 5－8 | 100 （0．0） | $\bullet$ | 4－6 | 100 （0．0） | $\bullet$ | 5－7 | 100 （0．0） | － | 5－9 | 100 （0．0） | 0 |
| Russian Federation | － | －－ | －－ | － | －－ | －－ | $\bullet$ | －－ | －－ | － | －－ | －－ | $\stackrel{\square}{3}$ |
| Saudi Arabia | $\bullet$ | 4－6 | 95 （1．7） | － | 4－8 | 100 （0．4） | $\bullet$ | 4－6 | 97 （1．9） | － | 7 | 98 （1．1） | ¢ |
| Scotland | $\bullet$ | －－ | 96 （2．0） | － | －－ | 78 （3．6） | $\bullet$ | －－ | 98 （1．1） | － | －－ | 90 （2．6） | $\frac{\square}{0}$ |
| Serbia | $\bullet$ | 5 | 93 （2．4） | $\bullet$ | 5 | 93 （2．4） | $\bullet$ | 5 | $94(2.2)$ | $\bullet$ | 6 | 94 （2．2） | \％ |
| Singapore | － | 4－5 | 100 （0．3） | $\bullet$ | 4－7 | 100 （0．0） | $\bullet$ | 4－5 | 100 （0．0） | － | 7 | 99 （0．5） | $\stackrel{\square}{\square}$ |
| Slovak Republic | $\bullet$ | 6 | 100 （0．0） | $\bullet$ | 7 | 100 （0．0） | $\bullet$ | 5 | 100 （0．0） | $\bullet$ | 6 | 100 （0．0） | $\stackrel{\text { F }}{ }$ |
| Slovenia | $\bullet$ | 7 | 100 （0．0） | － | 7 | 100 （0．0） | － |  | $99(0.6)$ | $\bullet$ | 4 | 99 （0．8） | 츧 |
| South Africa | $\bullet$ | －－ | r 76 （3．3） | － | －－ | r 71 （3．8） | $\bullet$ | －－ | r 68 （3．9） | $\bullet$ | －－ | r 94 （1．7） |  |
| Sweden | $\bullet$ | 7 | 96 （1．0） | $\bigcirc$ | 9 | 94 （1．3） | $\bullet$ | 7 | 99 （0．4） | － | 5 | 98 （0．9） | $\bigcirc$ |
| Syrian Arab Republic | $\bullet$ | －－ | －－ | $\bullet$ | －－ | － | $\bullet$ | －－ | －－ | － | －－ | －－ |  |
| Tunisia | $\bullet$ | －－ | 95 （1．9） | $\bullet$ | －－ | 99 （0．6） | $\bullet$ | －－ | 100 （0．0） | － | －－ | 99 （0．6） | \％ |
| United States | － | －－ | 100 （0．0） | － | －－ | 100 （0．3） | － | －－ | 100 （0．3） | － | －－ | 99 （0．5） | 考 |
| F England | $\bullet$ | 3－5 | s 100 （0．0） | $\bullet$ | 6－8 | 98 （1．5） | $\bullet$ | 4－8 | s 99 （0．6） | $\bullet$ | K－7 | s 100 （0．0） | $\bar{\sim}$ |
| International Avg． |  |  | 96 （0．2） |  |  | 97 （0．2） |  |  | 97 （0．2） |  |  | 98 （0．2） | \％ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  | $\frac{E}{1}$ |
| Basque Country，Spain | $\bullet$ | －－ | 96 （2．3） | $\bullet$ | －－ | 100 （0．0） | $\bullet$ | －－ | $99(0.8)$ | $\bullet$ | －－ | 100 （0．0） | \％ |
| Indiana State，US | $\bullet$ | －－ | 99 （1．1） | $\bullet$ | －－ | 100 （0．0） | $\bullet$ | －－ | 99 （0．5） | $\bullet$ | －－ | 98 （1．2） | ¢ |
| Ontario Province，Can． | $\bullet$ | 4－6 | 97 （1．8） | － | 7－8 | 96 （2．0） | － | 4－8 | $99(1.0)$ | － | 7－8 | 88 （3．0） | $\bigcirc$ |
| Quebec Province，Can． | $\bullet$ | 4－7 | 99 （1．0） | $\bullet$ | 5－7 | 100 （0．0） | $\bullet$ | 4－7 | $99(0.8)$ | $\bullet$ | 6－8 | 100 （0．2） |  |

Background data on intended curriculum provided by National Research Coordinators，and on imple－ mented curriculum by teachers at the time of testing．
\＃Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
（ ）Standard errors appear in parentheses．Because results are rounded to the nearest whole number， some totals may appear inconsistent．

A dash（－）indicates comparable data are not available．
An＂$r$＂indicates data are available for at least 70 but less than $85 \%$ of the students．An＂$s$＂indicates data are available for at least 50 but less than $70 \%$ of the students．


Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

The algebra topics were included in their intended eighth-grade curricula by somewhat fewer participants, as shown in Exhibit 5.9. The most frequently reported topic - "sums, products, and powers of expressions containing variables" - was included for all or almost all students in 42 of the participating entities. In contrast, "attributes of a graph" was included in the intended curriculum of just 19 participants. Although when most topics were included, they were intended for all or almost all students, "simple linear equations and equalities, and simultaneous (two variables) equations" and "proportional, linear, and nonlinear relationships" were intended for the top-track students only in 9 and 7 entities, respectively. Countries frequently indicated that algebra topics would primarily be taught in later grades. Exhibit 5.9 also shows that the percentages of students whose teachers reported having taught the algebra topics generally is in line with the inclusion of the topics in the intended curriculum. The percentage of students ranged from 88 percent for "sums, products, and powers of expressions containing variables" to 44 percent for "attributes of a graph."

As noted earlier in this chapter, most TIMSS participants included good coverage of measurement in their eighth-grade intended curriculum. Exhibit 5.10 provides more detail, showing that five of the eight measurement topics are included in the intended curriculum of at least 40 of the participants. These topics include standard units of measure, relationship among conversion units, using standard measurement tools, estimation of measurements, and measurement formulas. Also, teachers reported that these topics had been well covered in the classroom, with more than 80 percent of students having been taught each one, on average. The other three topics were included in fewer participants' curricula and had received less attention in the classroom. "Precision of measurements" was included in the intended curriculum of just 22 participants, and on average, 57 percent of students had teachers reporting that the topic had been taught.

With 13 topics, geometry was the TIMSS mathematics content area with the most topics. However, as shown in Exhibit 5.11, just three

| Algebra | Numeric, algebraic, and geometric patterns or sequences |  |  |  | Sums, products, and powers of expressions containing variables |  |  | Simple linear equations and equalities, and simultaneous (two variables) equations |  |  |  | Equivalent representations of functions as ordered pairs, tables, graphs, words, or equations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | $\bullet$ | -- | r | 98 (0.9) | $\bullet$ | -- | 100 (0.0) | $\bullet$ | -- | r | 99 (0.5) | $\bigcirc$ | -- | r | 88 (2.6) |
| Australia | $\bullet$ | 5-7 |  | 89 (2.7) | $\bullet$ | 8-9 | 76 (3.3) | $\bigcirc$ | 9-10 |  | 42 (3.9) | $\bullet$ | 7-9 |  | 72 (3.7) |
| Bahrain | $\bullet$ | 1-8 |  | 58 (3.2) | $\bullet$ | 7-9 | 97 (1.4) | $\bullet$ | 7-9 |  | 28 (3.5) | $\bigcirc$ | 9-12 |  | 48 (3.3) |
| Belgium (Flemish) | $\bullet$ | -- |  | 56 (3.8) | $\bullet$ | -- | 78 (2.4) | $\bullet$ | -- |  | 28 (3.4) | $\bullet$ | -- |  | 40 (4.2) |
| Botswana | - | 8 |  | 70 (4.2) | $\bigcirc$ | 9 | 47 (4.8) | $\bigcirc$ | 9 |  | 16 (3.7) | $\bigcirc$ | 11 |  | 13 (3.2) |
| Bulgaria | $\bigcirc$ | -- |  | 47 (4.5) | $\bullet$ | 7-8 | 99 (0.9) | - | 6-8 |  | 98 (1.2) | $\bullet$ | 8 |  | 97 (0.8) |
| Chile | $\bigcirc$ | 9 |  | 67 (3.3) | $\bigcirc$ | - | 76 (3.1) | $\bigcirc$ | 10 |  | 58 (3.6) | $\bigcirc$ | 10 |  | 54 (3.4) |
| Chinese Taipei | $\bigcirc$ | 9 |  | 76 (3.4) | $\bullet$ | 8 | 99 (0.6) | $\bullet$ | 8 |  | 98 (1.4) | $\bullet$ | 8 |  | 97 (1.4) |
| Cyprus | - | 4-8 |  | 25 (2.3) | $\bullet$ | 6-8 | 85 (2.3) | $\bigcirc$ | 7-9 |  | 72 (2.8) | - | 5-8 |  | 9 (1.9) |
| Egypt | $\bullet$ | 8 |  | 84 (3.0) | $\bullet$ | 6-7 | 99 (0.8) | $\bullet$ | 6-8 |  | 99 (0.7) | $\bullet$ | 8 |  | 98 (1.3) |
| Estonia | - | 4-9 |  | 58 (3.9) | $\bullet$ | 8-9 | 99 (1.0) | - | 7-8 |  | 98 (1.1) | - | 7,9 |  | 88 (2.9) |
| Ghana | $\bullet$ | -- |  | 81 (3.8) | $\bullet$ | -- | 88 (2.8) | - | -- |  | 77 (3.8) | $\bullet$ | -- |  | 54 (4.1) |
| Hong Kong, SAR | - | 7-9 |  | 76 (3.8) | $\bullet$ | 7-9 | 95 (1.8) | - | 7-9 |  | 89 (2.2) | $\bigcirc$ | 12 |  | 70 (4.4) |
| Hungary | - | 4 |  | 82 (3.3) | $\bullet$ | 5 | 96 (1.6) | - | 7-10 |  | 92 (2.2) | - | 8 |  | 97 (1.4) |
| Indonesia | - | 7-8 |  | 60 (4.3) | $\bullet$ | 7-8 | 81 (3.6) | - | 7-8 |  | 100 (0.2) | - | 8-9 |  | 97 (1.4) |
| Iran, Islamic Rep. of | $\bullet$ | 8-9 |  | 64 (4.1) | $\bullet$ | 6-7,9 | 93 (2.0) | $\bullet$ | 8-9 |  | 91 (2.3) | $\bigcirc$ | 9-11 |  | 67 (4.2) |
| Israel | - | 4-9 |  | 91 (2.1) | $\bullet$ | $8-9$ | 89 (1.9) | - | $8-9$ |  | 93 (1.8) | - | $8-9$ |  | 58 (3.8) |
| Italy | $\bullet$ | 8-9 |  | 62 (3.5) | $\bullet$ | 8-10 | 89 (2.6) | - | 8-10 |  | 59 (4.0) | $\bullet$ | 8-10 |  | 69 (3.4) |
| Japan | $\bullet$ | 7 |  | 77 (3.5) | - | 7-8 | 96 (1.3) | - | 7-8 |  | 95 (1.9) | - | 7-8 |  | 93 (1.8) |
| Jordan | $\bullet$ | 4-11 |  | 49 (4.4) | $\bullet$ | 7-11 | 99 (0.7) | $\bullet$ | 6-9 |  | 97 (1.5) | $\bullet$ | 8-10 |  | 99 (1.1) |
| Korea, Rep. of | - | -- | 5 | 62 (3.7) | $\bullet$ | -- | 92 (1.9) | - | -- | 5 | 97 (0.9) | - | -- | s | 97 (1.0) |
| Latvia | $\bigcirc$ | 9 | 5 | 3 (1.7) | $\bullet$ | 7 | 95 (0.5) | $\bullet$ | 7 | $s$ | 64 (4.7) | $\bullet$ | 7 | s | 53 (5.5) |
| Lebanon | $\bigcirc$ | 11-12 |  | 70 (4.3) | - | 8 | 97 (1.5) | $\bigcirc$ | 9 |  | 49 (4.5) | $\bigcirc$ | 9-12 |  | 56 (4.4) |
| Lithuania | $\bigcirc$ | 11-12 |  | 37 (4.1) | $\bullet$ | 8-12 | 98 (1.3) | - | $4-8$ |  | 82 (3.6) | - | 8-12 |  | 73 (3.8) |
| Macedonia, Rep. of | - | 7 | r | 87 (3.1) | $\bullet$ | 7 | 98 (1.0) | $\bullet$ | 5-8 |  | 99 (0.8) | - | 5-8 |  | 100 (0.0) |
| Malaysia | $\bullet$ | 7 |  | 83 (3.1) | $\bigcirc$ | 9 | 89 (2.3) | $\bullet$ | 8-10 |  | 58 (4.3) | $\bigcirc$ | 9 |  | 50 (4.5) |
| Moldova, Rep. of | - | 6-7 | s | 85 (3.6) | - | 7 | 97 (1.4) | - | 7-8 | r | 93 (2.4) | - | 7-8 | r | 92 (2.5) |
| Morocco | $\bigcirc$ | -- |  | $\mathrm{x} \times$ | $\bullet$ | -- | 94 (3.1) | $\bigcirc$ | -- | s | 48 (6.5) | $\bigcirc$ | -- | 5 | 28 (5.8) |
| Netherlands | $\bigcirc$ | -- |  | 67 (5.2) | $\bigcirc$ | -- | 78 (3.9) | $\bigcirc$ | -- |  | 68 (4.6) | - | -- |  | 77 (4.3) |
| New Zealand | $\bullet$ | 8-9 |  | 92 (2.8) | $\bigcirc$ | 8-9 | 92 (2.6) | $\odot$ | 8-10 |  | 47 (4.8) | $\bullet$ | 4-9 |  | 75 (3.9) |
| Norway | $\bigcirc$ | 9-10 |  | 48 (4.2) | $\bullet$ | 8-10 | 30 (4.3) | $\bullet$ | 8-10 |  | 6 (1.7) | $\bigcirc$ | 9-10 |  | 30 (3.8) |
| Palestinian Nat'l Auth. | $\bullet$ | 6-8 |  | 46 (4.3) | $\bullet$ | 7-8 | 97 (1.7) | - | 7-8 |  | 44 (4.5) | $\bigcirc$ | 9 |  | 39 (4.6) |
| Philippines | - | 8 |  | 65 (4.5) | - | 8 | 94 (2.4) | - | 8 |  | 98 (1.3) | $\bigcirc$ | 10 |  | 93 (2.4) |
| Romania | $\bullet$ | 6-9 |  | 83 (3.5) | $\bullet$ | 6-9 | 95 (1.8) | - | 7-9 |  | 100 (0.0) | $\bullet$ | 7-11 |  | 98 (1.1) |
| Russian Federation | $\bigcirc$ | 9 |  | (35) | $\bullet$ | -- | - | $\bullet$ | -- |  | (1) | - | -- |  | (1) |
| Saudi Arabia | $\bigcirc$ | 11 |  | 59 (5.9) | $\bullet$ | 8 | 96 (1.8) | - | 7-8 |  | 40 (4.8) | $\bullet$ | 8 |  | 85 (3.6) |
| Scotland | - | -- |  | 82 (3.2) | $\odot$ | -- | 60 (4.8) | $\odot$ | -- | r | 32 (4.6) | $\bigcirc$ | -- |  | 38 (5.1) |
| Serbia | - | 7 |  | 83 (3.2) | $\bullet$ | 7 | 95 (2.1) | - | 8 |  | 99 (0.9) | - | 8 |  | 98 (1.2) |
| Singapore | - | 6-8 |  | 97 (1.0) | - | 7-10 | 96 (1.1) | - | 7-8 |  | 92 (1.4) | - | 8-10 |  | 92 (1.4) |
| Slovak Republic | $\bigcirc$ | 9 |  | 28 (3.6) | $\bullet$ | 8 | 99 (0.5) | - | 7 |  | 62 (4.7) | $\bigcirc$ | 9 |  | 25 (3.5) |
| Slovenia | - | 4 |  | 45 (4.6) | $\bullet$ | 6 | 84 (3.1) | - | 7 |  | 18 (3.4) | - | 7 |  | 44 (4.3) |
| South Africa | $\bullet$ | -- | r | 76 (3.8) | $\bullet$ | -- | 92 (2.2) | $\bigcirc$ | -- | r | 59 (3.9) | $\bigcirc$ | -- | $r$ | 50 (3.8) |
| Sweden | $\bigcirc$ | 9 |  | 64 (3.9) | $\bigcirc$ | 9 | 61 (4.0) | $\bigcirc$ | 7-9 |  | 28 (3.5) | $\bigcirc$ | 9 |  | 37 (3.8) |
| Syrian Arab Republic | $\bullet$ | 10 |  | - | $\bullet$ | -- | - | $\bigcirc$ | 9 |  | - | $\bigcirc$ | 9 |  | - |
| Tunisia | $\bullet$ | -- |  | 76 (3.8) | $\bullet$ | -- | 81 (3.5) | $\bigcirc$ | 11 |  | 23 (3.5) | $\bigcirc$ | 11 |  | 36 (4.0) |
| United States | $\bullet$ | -- |  | 95 (1.3) | $\bullet$ | -- | 93 (1.2) | $\bigcirc$ | -- |  | 80 (2.4) | - | -- |  | 85 (1.9) |
| England | $\bullet$ | 6-8 | 5 | 95 (2.4) | $\bullet$ | 6-7 | 86 (3.8) | $\bullet$ | 6-9 | s | 63 (5.5) | $\bullet$ | 6-7 | s | 81 (4.4) |
| International Avg. |  |  |  | 68 (0.5) |  |  | 88 (0.4) |  |  |  | 68 (0.5) |  |  |  | 68 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | $\bullet$ | -- |  | 70 (4.6) | $\odot$ | 10 | 86 (3.5) | $\odot$ | 10 |  | 65 (5.6) | $\odot$ | 10 |  | 40 (5.4) |
| Indiana State, US | $\bullet$ | -- |  | 92 (3.5) | $\bullet$ | -- | 94 (2.3) | $\bullet$ | -- |  | 72 (5.5) | $\bullet$ | -- |  | 78 (3.8) |
| Ontario Province, Can. | - | 6-8 |  | 89 (2.6) | $\bullet$ | 7-8 | 86 (3.5) | - | 7-8 |  | 64 (4.0) | - | 8 |  | 60 (4.8) |
| Quebec Province, Can. | $\bullet$ | 1-7 |  | 92 (2.8) | $\bullet$ | 8-11 | 68 (4.7) | $\bullet$ | 8-11 |  | 22 (3.9) | $\bigcirc$ | 9-11 |  | 66 (4.8) |

Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
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A dash (-) indicates comparable data are not available.
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| AlgebraCountries | Proportional, linear, and nonlinear relationships |  |  | Attributes of a graph |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
| Armenia | $\bigcirc$ | -- | r 98 (0.9) | $\bigcirc$ | -- | r 76 (3.6) |
| Australia | $\bigcirc$ | 9-11 | 46 (3.8) | $\bigcirc$ | 9-11 | 39 (4.6) |
| Bahrain | - | 6-9 | 18 (2.9) | $\bigcirc$ | 10-12 | 4 (1.2) |
| Belgium (Flemish) | - | -- | 39 (3.5) | $\bigcirc$ | -- | 10 (1.8) |
| Botswana | $\bigcirc$ | 9 | 7 (2.5) | $\bigcirc$ | 9 | 1 (1.0) |
| Bulgaria | - | 8 | 93 (2.1) | - | 8 | 80 (3.2) |
| Chile | $\bigcirc$ | 11 | 45 (4.0) | $\bigcirc$ | -- | 30 (3.8) |
| Chinese Taipei | - | 8 | 86 (3.1) | $\bigcirc$ | 9 | 75 (3.4) |
| Cyprus | $\bigcirc$ | 6-9 | 6 (2.2) | $\bigcirc$ | 9 | 4 (1.5) |
| Egypt | - | 5,11 | 70 (3.2) | - | 8 | 98 (0.9) |
| Estonia | - | 7,9 | 93 (2.2) | - | 6-7, 9 | 58 (3.2) |
| Ghana | - | -- | 28 (4.3) | - | -- | 27 (4.3) |
| Hong Kong, SAR | $\bigcirc$ | 10-11 | 42 (4.9) | $\bigcirc$ | 12 | 21 (3.4) |
| Hungary | - | 8 | 97 (1.3) | $\bigcirc$ | 11 | 90 (2.5) |
| Indonesia | $\bigcirc$ | 10 | 56 (4.3) | $\bigcirc$ | 10 | 38 (4.0) |
| Iran, Islamic Rep. of | $\bigcirc$ | 9-11 | 42 (4.2) | $\bigcirc$ | 10-11 | 32 (3.9) |
| Israel | $\bigcirc$ | 9 | 49 (3.6) | - | 8-9 | 30 (3.5) |
| Italy | $\bigcirc$ | 9-10 | 59 (3.6) | $\bigcirc$ | 9-13 | 38 (3.3) |
| Japan | - | 7-8 | 92 (2.1) | - | 8 | 97 (1.5) |
| Jordan | - | 7-9 | 24 (3.9) | $\bigcirc$ | 10-12 | 14 (3.1) |
| Korea, Rep. of | $\bigcirc$ | 9 | s 80 (3.5) | - | -- | 91 (2.0) |
| Latvia | - | 7 | s 75 (4.4) | - | 7,9 | 26 (4.7) |
| Lebanon | $\bigcirc$ | 9 | 37 (4.4) | $\bigcirc$ | 10-12 | 36 (4.8) |
| Lithuania | - | 8-12 | 79 (3.2) | $\bigcirc$ | 9-12 | 44 (4.0) |
| Macedonia, Rep. of | - | 7-8 | 98 (1.1) | - | 7-8 | 99 (0.6) |
| Malaysia | $\bigcirc$ | 9 | 27 (3.7) | $\bigcirc$ | 9 | 14 (3.0) |
| Moldova, Rep. of | - | 7 | r 86 (3.2) | - | 8 | r 79 (3.4) |
| Morocco | $\bigcirc$ | -- | $\mathrm{x} \times$ | $\bigcirc$ | -- | 10 (4.2) |
| Netherlands | - | -- | 62 (4.9) | - | -- | 75 (4.5) |
| New Zealand | $\bigcirc$ | 8-10 | 54 (4.9) | $\bigcirc$ | 9 | 43 (4.7) |
| Norway | $\bigcirc$ | 9-10 | 8 (2.0) | $\bigcirc$ | 12-13 | 15 (2.7) |
| Palestinian Nat'l Auth. | $\bigcirc$ | 9-10 | 14 (3.0) | $\bigcirc$ | 10 | 12 (2.8) |
| Philippines | $\bigcirc$ | 10 | 76 (4.3) | $\bigcirc$ | 10 | 81 (3.6) |
| Romania | - | 7-11 | 91 (2.7) | - | 7-11 | 94 (2.1) |
| Russian Federation | - | -- | - | - | 8-9 | - - |
| Saudi Arabia | - | 8 | 33 (5.0) | $\bigcirc$ | 10,12 | 14 (2.4) |
| Scotland | $\bigcirc$ | -- | 40 (4.5) | $\bigcirc$ | -- | 26 (4.2) |
| Serbia | - | 7 | 96 (1.7) | $\bigcirc$ | 8 | 98 (1.1) |
| Singapore | - | 8-10 | 88 (1.7) | - | 8-10 | 65 (2.3) |
| Slovak Republic | - | 7 | 98 (0.8) | $\bigcirc$ | 9 | 10 (2.2) |
| Slovenia | - | 7 | 38 (4.0) | - | 7 | 9 (2.7) |
| South Africa | $\bigcirc$ | -- | r 32 (3.8) | $\bigcirc$ | -- | r 34 (3.6) |
| Sweden | $\bigcirc$ | 8-9 | 49 (3.9) | $\bigcirc$ | 9 | 18 (2.8) |
| Syrian Arab Republic | $\bigcirc$ | 9 | - - | $\bigcirc$ | 12 | - - |
| Tunisia | $\bigcirc$ | 11 | 20 (3.2) | $\bigcirc$ | 11 | 21 (3.7) |
| United States | - | -- | 62 (2.5) | - | -- | 67 (2.2) |
| $\ddagger$ England | $\bigcirc$ | 7-12 | s 57 (6.0) | $\bigcirc$ | 7-11 | 54 (5.2) |
| International Avg. |  |  | 57 (0.5) |  |  | 44 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | $\bigcirc$ | 10 | 60 (5.2) | $\bigcirc$ | 11 | 20 (4.6) |
| Indiana State, US | $\bigcirc$ | -- | 54 (5.4) | - | -- | 54 (4.6) |
| Ontario Province, Can. | - | 8 | 27 (4.7) | $\bigcirc$ | 9 | 34 (4.4) |
|  |  | 10-11 | 54 (4.3) | $\bigcirc$ | 9 | 44 (4.5) |

Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

| Measurement | Standard units for measures of length，area，volume，perimeter， circumference，time，speed， density，angle，mass／weight |  |  | Relationships among units of conversions within systems of units，and for rates |  |  | Use standard tools to measure length，time，speed，angle， and temperature |  |  | Estimations of length， circumference，area，volume， weight，time，angle，and a speed in problem situations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | $\bigcirc$ | －－ | r 100 （0．3） | $\bigcirc$ | －－ | r 97 （1．4） | $\bigcirc$ | －－ | r 99 （0．9） | $\bigcirc$ | －－ |  | 99 （0．5） |
| Australia | － | 5－8 | 98 （1．0） | － | 5－8 | 92 （2．2） | － | 5－8 | 93 （2．1） | $\bigcirc$ | 5－8 |  | 90 （2．1） |
| Bahrain | $\bigcirc$ | 3－8 | 88 （2．6） | － | 4－6 | 85 （3．2） | － | 3－8 | 60 （3．4） | － | 2－8 |  | 69 （3．7） |
| Belgium（Flemish） | － | －－ | 94 （1．7） | － | －－ | 71 （3．2） | － | －－ | 70 （3．7） | － | －－ |  | 73 （3．6） |
| Botswana | － | 7 | 74 （3．8） | － | 8 | 79 （4．1） | － | 8 | 81 （3．6） | － | 8 |  | 43 （4．5） |
| Bulgaria | － | 4 | 100 （0．3） | － | 4 | 100 （0．3） | － | 4 | 96 （1．5） | － | 6 |  | 97 （1．5） |
| Chile | － | 1－8 | 78 （3．1） | － | 1－8 | 72 （3．6） | － | 1－8 | 64 （3．7） | － | 1－8 |  | 59 （3．9） |
| Chinese Taipei | $\bigcirc$ | 6 | 89 （2．6） | $\bigcirc$ | 6 | 91 （2．4） | － | 6 | 89 （2．7） | － | 6 |  | 92 （2．1） |
| Cyprus | － | 4－7 | 98 （0．8） | － | 4－8 | 74 （2．6） | － | 4－8 | 29 （2．4） | － | 4－8 |  | 87 （2．1） |
| Egypt | － | 3－5 | 97 （1．7） | － | 3－5 | 86 （2．9） | － | 3－5 | 86 （3．1） | － | 3－5 |  | 91 （2．6） |
| Estonia | － | 1－4 | 99 （0．5） | － | 4－6 | 96 （1．4） | － | 1－6 | 99 （0．8） | $\bigcirc$ | －－ |  | 96 （1．6） |
| Ghana | － | －－ | 74 （4．4） | － | －－ | 55 （4．7） | － | －－ | 64 （5．0） | － | －－ |  | 56 （4．1） |
| Hong Kong，SAR | － | 6 | 93 （2．3） | － | 5 | 92 （2．6） | － | 6 | 87 （3．0） | － | 6 |  | 89 （2．9） |
| Hungary | － | 7 | 99 （0．7） | － | 2－5 | 100 （0．0） | － | 2－6 | 99 （0．8） | $\bigcirc$ | －－ |  | 99 （0．9） |
| Indonesia | － | 5－8 | 99 （0．8） | － | 8－9 | 79 （4．0） | － | 7－8 | 83 （3．2） | － | 7－9 |  | 98 （1．1） |
| Iran，Islamic Rep．of | － | 5，7－8 | 77 （3．5） | － | 5，7 | 62 （4．0） | － | 3－5 | 61 （3．9） | － | 7－8 |  | 75 （3．3） |
| Israel | － | 2－8 | 80 （2．9） | － | 4，7 | 77 （3．1） | － | 3－6 | 63 （4．1） | $\bigcirc$ | －－ |  | 66 （3．8） |
| Italy | － | 6－7 | 100 （0．0） | － | 4－7 | 85 （2．6） | － | 4－7 | 92 （1．9） | － | 8－10 |  | 90 （2．3） |
| Japan | － | 2－6 | 96 （1．7） | － | 2－6 | 91 （2．5） | － | 2－6 | 90 （2．6） | － | 5－6 |  | 89 （2．4） |
| Jordan | $\bigcirc$ | 4－8 | 96 （2．1） | － | 5－6 | 98 （1．3） | $\bigcirc$ | 4－7 | 89 （3．1） | $\bigcirc$ | －－ |  | 91 （2．7） |
| Korea，Rep．of | － | －－ | S 89 （2．6） | － | －－ | 79 （3．1） | － | －－ | 69 （3．9） | － | －－ | s | 82 （3．1） |
| Latvia | － | 6－7 | S 83 （4．4） | － | －－ | 84 （4．3） | － | 6 | s 93 （2．7） | － | －－ | s | 64 （6．2） |
| Lebanon | $\bigcirc$ | －－ | 91 （2．4） | $\bigcirc$ | －－ | 74 （3．6） | $\bigcirc$ | －－ | 76 （4．0） | $\bigcirc$ | －－ |  | 76 （3．1） |
| Lithuania | $\bigcirc$ | 4－12 | 99 （0．8） | － | 5－6 | 98 （1．3） | － | 5－8 | 97 （1．4） | － | 5－12 |  | 91 （2．4） |
| Macedonia，Rep．of | － | 3－8 | 97 （1．5） | － | 5－8 | 96 （1．8） | － | 4－8 | 94 （2．0） | － | 7－8 |  | 91 （2．1） |
| Malaysia | － | 3－7 | 93 （2．1） | － | 4－7 | 87 （2．9） | － | 4－8 | 91 （2．5） | － | 4－8 |  | 85 （3．4） |
| Moldova，Rep．of | － | 5－6 | r 91 （2．9） | － | 6 | r 90 （2．7） | － | 6 | r 93 （2．5） | － | 6 | $r$ | 83 （4．0） |
| Morocco | $\bigcirc$ | －－ | S 85 （3．9） | － | －－ | 90 （4．1） | $\bigcirc$ | －－ | 82 （5．4） | $\bigcirc$ | －－ | s | 87 （3．4） |
| Netherlands | － | －－ | 93 （2．7） | $\bigcirc$ | －－ | 78 （4．0） | － | －－ | 92 （2．6） | － | －－ |  | 88 （3．5） |
| New Zealand | － | 4－7 | 96 （2．5） | － | 6－9 | 93 （2．5） | － | 4－7 | 92 （2．9） | － | 6－9 |  | 81 （4．5） |
| Norway | － | 2－10 | 80 （3．6） | － | 8－10 | 83 （3．6） | － | 2－10 | 80 （3．2） | － | 8－10 |  | 72 （3．8） |
| Palestinian Nat＇l Auth． | － | 2－6 | 96 （1．7） | － | 3－6 | 88 （2．5） | － | 4－6 | 78 （3．7） | － | 4－6 |  | 79 （3．6） |
| Philippines | － | 7 | 82 （3．3） | － | 7 | 82 （3．0） | － | 7 | 75 （3．7） | － | 7 |  | 72 （4．1） |
| Romania | － | 2－5 | 100 （0．0） | － | 2－5 | 100 （0．0） | － | 2－6 | 99 （0．8） | － | 3－8 |  | 97 （1．5） |
| Russian Federation | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | － | －－ |  | －－ |
| Saudi Arabia | － | 4－6 | 87 （2．8） | － | 4－6 | 80 （4．3） | － | 3－6 | 69 （5．9） | $\bigcirc$ | －－ |  | 65 （6．0） |
| Scotland | － | －－ | 95 （1．9） | － | －－ | 89 （2．7） | － | －－ | 94 （2．2） | － | －－ |  | 80 （3．5） |
| Serbia | － | 4－7 | 94 （2．1） | － | 6 | 94 （2．0） | － | 4－7 | 91 （2．6） | － | 7 |  | 95 （1．8） |
| Singapore | － | 2－7 | 99 （0．5） | － | 3－8 | 98 （0．7） | － | 2－6 | 94 （1．5） | － | 2－6 |  | 96 （1．0） |
| Slovak Republic | － | 8 | 100 （0．0） | － | 7 | 100 （0．0） | － | 7 | 98 （1．1） | － | 7 |  | 97 （1．3） |
| Slovenia | － | 3－5 | 100 （0．0） | － | 6 | 95 （1．9） | － | 5－6 | 99 （0．7） | － | 5－6 |  | 80 （3．5） |
| South Africa | － | －－ | r 69 （3．6） | $\bigcirc$ | －－ | r 50 （4．1） | $\bigcirc$ | －－ | r 63 （4．2） | $\bigcirc$ | －－ | $r$ | 58 （4．2） |
| Sweden | － | 8 | 97 （1．2） | － | 7 | 82 （2．6） | $\bigcirc$ | 7 | 91 （1．8） | － | 8 |  | 90 （1．9） |
| Syrian Arab Republic | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | － | －－ |  | －－ |
| Tunisia | － | －－ | 92 （2．4） | $\bigcirc$ | 12 | 87 （2．7） | － | －－ | 84 （2．9） | $\bigcirc$ | 9 |  | 80 （3．1） |
| United States | － | －－ | 96 （1．2） | － | －－ | 92 （1．4） | － | －－ | 95 （1．2） | － | －－ |  | 90 （1．8） |
| $\ddagger$ England | $\bigcirc$ | K－8 | s 96 （2．6） | $\bigcirc$ | 3－8 | 89 （3．9） | $\bigcirc$ | K－6 | s 96 （2．6） | $\bigcirc$ | 1－8 | s | 88 （3．4） |
| International Avg． |  |  | 92 （0．3） |  |  | 86 （0．4） |  |  | 84 （0．4） |  |  |  | 83 （0．5） |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country，Spain | － | －－ | 93 （2．4） | － | －－ | 91 （2．9） | $\bigcirc$ | 10 | 89 （2．9） | $\bigcirc$ | 9 |  | 83 （3．5） |
| Indiana State，US | － | －－ | 97 （1．6） | － | －－ | 96 （2．0） | － | －－ | 96 （1．6） | － | －－ |  | 86 （3．6） |
| Ontario Province，Can． | － | 2－8 | 99 （0．4） | － | 4－8 | 89 （2．8） | － | 2－8 | 97 （1．6） | － | 2－9 |  | 95 （1．7） |
| Quebec Province，Can． | － | 1－9 | 71 （4．7） | － | 4－9 | 93 （2．5） | － | 2－6 | 81 （3．6） | － | 2－8 |  | 67 （4．6） |

Background data on intended curriculum provided by National Research Coordinators，and on implemented curriculum by teachers at the time of testing．
$\ddagger$ Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
（）Standard errors appear in parentheses．Because results are rounded to the nearest whole number，some totals may appear inconsistent．

A dash（－）indicates comparable data are not available．
An＂$r$＂indicates data are available for at least 70 but less than $85 \%$ of the students．An＂s＂indi－ cates data are available for at least 50 but less than $70 \%$ of the students．


Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. $A n$ " $x$ " indicates data are available for less than $50 \%$ of the students.

| Geometry | Angles－acute，right，straight， obtuse，reflex，complementary， and supplementary |  |  | Relationships for angles at a point，angles on a line， vertically opposite angles， angles associated with a transversal cutting parallel lines， and perpendicularity |  |  | Properties of angle bisectors and perpendicular bisectors of lines |  |  | Properties of geometric shapes： triangles and quadrilaterals |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | － | －－ | r 100 （0．0） | $\bigcirc$ | －－ | r 99 （0．6） | － | －－ | r 100 （0．0） | － | －－ | r 99 （0．5） | ${ }^{\text {N }}$ |
| Australia | － | 7－8 | 93 （1．8） | － | 8 | 83 （3．1） | $\bigcirc$ | 9 | 50 （4．0） | － | 7－8 | 89 （2．6） | T |
| Bahrain | － | 4－5 | 100 （0．0） | － | 5－7 | 100 （0．0） | － | 7－9 | 95 （1．6） | － | 5－9 | 99 （0．3） | $\stackrel{\square}{0}$ |
| Belgium（Flemish） | － | －－ | 98 （0．8） | － | －－ | 86 （1．8） | － | －－ | 82 （2．0） | － | －－ | 90 （2．0） | － |
| Botswana | － | 8 | 70 （3．9） | － | 8 | 49 （5．0） | $\bigcirc$ | 9 | 11 （2．7） | $\bigcirc$ | 9 | 60 （4．6） | $\stackrel{5}{5}$ |
| Bulgaria | － | 7 | 100 （0．0） | － | 7 | 100 （0．0） | － | 7 | 100 （0．0） | － | 7 | 100 （0．0） | n |
| Chile | － | 3－8 | 98 （1．1） | － | 8 | 96 （1．5） | $\bigcirc$ | －－ | 84 （2．3） | $\bigcirc$ | 5－6 | 93 （1．6） | $\stackrel{\cong}{\square}$ |
| Chinese Taipei | － | 8 | 99 （0．8） | － | 8 | 79 （3．0） | $\bigcirc$ | 8 | 93 （2．2） | $\bigcirc$ | 9 | 93 （2．3） | 先 |
| Cyprus | － | 4－8 | 98 （0．9） | － | 4－7 | 98 （0．9） | $\bigcirc$ | 8 | 95 （1．2） | $\bigcirc$ | 5－8 | 92 （1．7） |  |
| Egypt | － | 4－6 | 100 （0．0） | － | 6 | 99 （0．9） | － | 6 | 100 （0．0） | $\bigcirc$ | 5－8 | 100 （0．0） | $\stackrel{y}{5}$ |
| Estonia | － | 5，8 | 96 （1．5） | － | 5，8 | 97 （1．3） | － | 6 | 97 （1．4） | $\bigcirc$ | 6，8 | 98 （1．3） | $\bigcirc$ |
| Ghana | － | －－ | 85 （3．8） | $\bigcirc$ | －－ | 73 （4．8） | － | －－ | 74 （3．8） | － | －－ | 75 （4．3） |  |
| Hong Kong，SAR | － | 7－9 | 97 （1．4） | － | 7－9 | 98 （1．2） | － | 7－9 | 75 （4．2） | － | 7－9 | 89 （2．7） |  |
| Hungary | － | 5－6 | 100 （0．0） | $\bigcirc$ | 6 | 98 （1．2） | － | 6 | 100 （0．0） | － | 6 | 100 （0．0） |  |
| Indonesia | － | 7－8 | 98 （1．1） | $\bigcirc$ | 9 | 96 （1．5） | $\bigcirc$ | 10 | 95 （1．9） | $\bigcirc$ | 9 | 92 （2．4） |  |
| Iran，Islamic Rep．of | － | 5－6 | 100 （0．0） | － | 6－7 | 97 （1．5） | － | 5－6 | 99 （0．6） | － | 6－8 | 100 （0．5） | \％ |
| Israel | － | 4－8 | 98 （1．0） | － | 8 | 78 （2．9） | － | 7－8 | 88 （2．6） | － | 7－9 | 74 （3．0） | 5 |
| Italy | － | 4－9 | 100 （0．0） | － | 6－9 | 98 （1．2） | － | 6－9 | 93 （2．0） | － | 4－10 | 100 （0．0） | 声 |
| Japan | － | 8 | 91 （2．3） | － | 8 | 98 （1．1） | － | 7 | 98 （1．2） | － | 8 | 97 （1．5） | － |
| Jordan | － | 4－5，7 | 99 （0．7） | $\bigcirc$ | 5，7 | 97 （1．6） | － | 8－10 | 95 （2．0） | $\bigcirc$ | 6－8 | 100 （0．0） | 万 |
| Korea，Rep．of | － | －－ | s 94 （1．7） | － | －－ | 95 （1．7） | － | －－ | 94 （1．7） | － | －－ | s 96 （1．6） | O |
| Latvia | － | 7 | s 99 （1．0） | － | 7 | 100 （0．0） | － | 7 | s 62 （5．3） | $\bigcirc$ | 7 | s 99 （0．9） | $\stackrel{+}{\square}$ |
| Lebanon | $\bigcirc$ | －－ | 96 （1．8） | $\bigcirc$ | －－ | 97 （1．4） | $\bigcirc$ | －－ | 96 （1．6） | － | －－ | 98 （1．2） | $\frac{3}{7}$ |
| Lithuania | － | 5－7 | 100 （0．0） | － | 5－8 | 98 （1．1） | － | 7－8 | 95 （2．0） | － | 7－10 | 100 （0．0） | 止 |
| Macedonia，Rep．of | － | 6－7 | 99 （0．7） | － | 6－7 | 99 （0．7） | － | 6 | 99 （0．7） | － | 6－7 | 99 （0．7） | Ј |
| Malaysia | － | 7 | 88 （2．8） | － | 7 | 88 （2．8） | － | 7 | 96 （1．8） | － | 7，9 | 97 （1．5） | $\stackrel{ \pm}{\ddagger}$ |
| Moldova，Rep．of | － | 8 | r 95 （2．0） | － | 8 | r 85 （3．6） | － | 8 | r 94 （2．2） | － | 8 | r 95 （2．1） | $\stackrel{\square}{\square}$ |
| Morocco | － | －－ | s 98 （2．0） | $\bigcirc$ | －－ | 96 （2．7） | － | －－ | s 99 （0．9） | $\bigcirc$ | －－ | $\mathrm{x} \times$ | ¢ |
| Netherlands | $\bigcirc$ | －－ | 94 （2．4） | $\bigcirc$ | －－ | 85 （3．3） | $\bigcirc$ | －－ | 52 （5．0） | $\bigcirc$ | －－ | 84 （4．1） | 근 |
| New Zealand | － | 6－9 | 96 （2．3） | － | 6－8 | 86 （4．2） | $\bigcirc$ | 8－9 | 45 （5．4） | － | 4－8 | 89 （2．5） | $\stackrel{\square}{+}$ |
| Norway | － | 8－10 | 90 （2．5） | － | 8－10 | 56 （3．9） | － | 8－10 | 90 （2．6） | － | 8－10 | 89 （2．8） | 2 |
| Palestinian Nat＇l Auth． | － | 3－7 | 98 （1．1） | － | 5－7 | 98 （1．0） | － | 5－7 | 86 （3．1） | － | 2－8 | 99 （0．9） | $\bigcirc$ |
| Philippines | $\bigcirc$ | 9 | 52 （4．5） | $\bigcirc$ | 9 | 36 （4．5） | $\bigcirc$ | 9 | 28 （4．1） | $\bigcirc$ | 9 | 35 （4．7） |  |
| Romania | － | 6－7 | 100 （0．0） | － | 6－8 | 100 （0．0） | － | 6－7 | 100 （0．0） | － | 6－7 | 100 （0．0） | $\stackrel{\sim}{c}$ |
| Russian Federation | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | － | －－ | －－ | $\stackrel{\text { ® }}{\text { ¢ }}$ |
| Saudi Arabia | － | 4－7 | 100 （0．2） | － | 8 | 100 （0．0） | － | 7 | 99 （0．9） | － | 7－8 | 100 （0．2） | 艺 |
| Scotland | － | －－ | 97 （1．1） | － | －－ | 92 （1．8） | $\bigcirc$ | －－ | 24 （3．8） | － | －－ | 87 （3．2） | $\frac{0}{0}$ |
| Serbia | － | 5 | 94 （2．2） | － | 5 | 94 （2．2） | － | 5－6 | 94 （2．3） | － | 6 | 94 （2．2） | $\stackrel{\square}{\circ}$ |
| Singapore | － | 3－7 | 96 （1．1） | － | 5－8 | 97 （0．9） | － | 7 | 84 （1．9） | － | 5－7 | 99 （0．7） | $\stackrel{\text { ¢ }}{ }$ |
| Slovak Republic | － | 5 | 99 （0．8） | － | 6 | 99 （0．9） | － | 6 | 99 （0．8） | － | 6 | 100 （0．0） | $\stackrel{\Perp}{ \pm}$ |
| Slovenia | － | 6 | 100 （0．1） | － | 6 | 99 （0．7） | － | 5 | 99 （0．8） | － | 6 | 100 （0．0） | त |
| South Africa | － | －－ | r 90 （2．2） | $\bigcirc$ | －－ | r 88 （2．5） | $\bigcirc$ | －－ | r 46 （4．1） | － | －－ | r 74 （3．5） | $\bigcirc$ |
| Sweden | － | 8 | 91 （2．1） | $\bigcirc$ | 8 | 55 （3．4） | $\bigcirc$ | 8－9 | 20 （2．6） | － | 8 | 94 （1．6） | $\bigcirc$ |
| Syrian Arab Republic | － | －－ | －－ | $\bigcirc$ | －－ | －－ | － | －－ | －－ | $\bigcirc$ | －－ | －－ |  |
| Tunisia | － | －－ | 100 （0．0） | － | －－ | 100 （0．0） | － | －－ | 100 （0．0） | － | －－ | 96 （1．6） | － |
| United States | － | －－ | 91 （1．8） | － | －－ | 74 （2．5） | － | －－ | 47 （2．9） | － | －－ | 87 （2．2） | $\stackrel{\text { 글 }}{ }$ |
| \＃England | $\bullet$ | 2－6 | s 100 （0．3） | $\bullet$ | 4－6 | 96 （1．7） | $\bullet$ | 7 | s 66 （5．9） | $\bullet$ | K－7 | S 94 （3．2） | $\stackrel{\square}{\bar{\sigma}}$ |
| International Avg． |  |  | 95 （0．3） |  |  | 90 （0．3） |  |  | 81 （0．4） |  |  | 92 （0．3） | \＃ |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  | $\underline{\text { E }}$ |
| Basque Country，Spain | － | －－ | 92 （2．3） | $\bigcirc$ | 9 | 86 （3．6） | $\bigcirc$ | 10 | 76 （3．7） | － | －－ | 91 （2．7） | － |
| Indiana State，US | － | 4 | 85 （3．7） | $\bigcirc$ | －－ | 70 （4．7） | － | －－ | 51 （4．7） | $\bigcirc$ | －－ | 81 （4．1） | ¢ |
| Ontario Province，Can． | － | 4－8 | 97 （2．1） | － | 7－8 | 88 （3．6） | － | 7－8 | 72 （4．7） | － | 1－6 | 97 （1．9） | － |
| Quebec Province，Can． | － | 4－7 | 94 （2．7） | － | 7－8 | 83 （4．3） | － | 7 | 86 （3．9） | － | 4－6 | 89 （3．4） |  |

Background data on intended curriculum provided by National Research Coordinators，and on imple－ mented curriculum by teachers at the time of testing
$\ddagger$ Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
（）Standard errors appear in parentheses．Because results are rounded to the nearest whole number， some totals may appear inconsistent．

A dash（－）indicates comparable data are not available．
An＂$r$＂indicates data are available for at least 70 but less than $85 \%$ of the students．An＂$s$＂indicates data are available for at least 50 but less than $70 \%$ of the students．An＂$x$＂indicates data are available for less than $50 \%$ of the students．

| Geometry | Properties of other polygons |  |  | Construct or draw triangles and rectangles of given dimensions |  |  | Pythagorean theorem to find length of a side |  |  | Congruent figures and their corresponding measures |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | - | -- | r 99 (0.7) | - | -- | r 98 (1.2) | - | -- | r 99 (1.0) | $\bigcirc$ | -- | r | 99 (1.1) |
| Australia | - | 7-8 | 65 (4.2) | - | 8 | 72 (3.1) | $\bigcirc$ | 9 | 51 (3.1) | $\bigcirc$ | 9 |  | 43 (4.5) |
| Bahrain | - | 7 | 83 (2.5) | - | 4-5 | 96 (0.1) | $\bigcirc$ | 8 | 97 (1.0) | - | 8 |  | 99 (0.7) |
| Belgium (Flemish) | - | -- | 21 (2.5) | - | -- | 93 (1.7) | $\bigcirc$ | -- | 3 (1.4) | - | -- |  | 82 (2.0) |
| Botswana | - | 8 | 47 (4.5) | $\bigcirc$ | 9 | 17 (3.5) | $\bigcirc$ | 10 | 2 (1.1) | $\bigcirc$ | 9 |  | 14 (3.2) |
| Bulgaria | - | 6-9 | 76 (3.9) | - | 7 | 97 (1.5) | $\bigcirc$ | 9 | 2 (0.8) | - | 7 |  | 99 (0.6) |
| Chile | - | 8 | 74 (3.1) | - | 8 | 88 (2.1) | - | 8 | 66 (3.0) | $\bigcirc$ | 9 |  | 72 (3.3) |
| Chinese Taipei | $\bigcirc$ | 9 | 94 (2.1) | - | 8 | 93 (2.2) | - | 8 | 98 (1.2) | $\bigcirc$ | 9 |  | 80 (3.3) |
| Cyprus | - | 5-8 | 44 (2.7) | - | 4-8 | 84 (1.7) | - | 6 | 100 (0.0) | $\bigcirc$ | 6-8 |  | 91 (1.3) |
| Egypt | - | 7 | $\mathrm{x} \times$ | - | 4-6 | 99 (0.9) | - | 7 | 100 (0.0) | - | 7 |  | 100 (0.0) |
| Estonia | - | 8 | 75 (3.6) | - | 6 | 98 (1.3) | $\bigcirc$ | 9 | 3 (1.3) | - | 6 |  | 67 (3.0) |
| Ghana | - | -- | 35 (4.2) | - | -- | 74 (3.6) | - | -- | 27 (4.1) | - | -- |  | 48 (4.5) |
| Hong Kong, SAR | $\bigcirc$ | -- | 77 (3.5) | - | 7-9 | 80 (3.8) | - | 7-9 | 94 (2.0) | - | 7-9 |  | 87 (3.1) |
| Hungary | - | 8 | 95 (1.8) | - | 6 | 100 (0.0) | $\bigcirc$ | 8 | 97 (1.6) | - | 6-7 |  | 92 (2.3) |
| Indonesia | $\bigcirc$ | 10 | 35 (4.4) | $\bigcirc$ | 11 | 71 (4.3) | - | 8 | 98 (0.7) | $\bigcirc$ | 9 |  | 63 (4.4) |
| Iran, Islamic Rep. of | $\bigcirc$ | 10 | 89 (2.5) | - | 5-6 | 96 (1.8) | - | 8 | 99 (0.6) | - | 6 |  | 98 (1.0) |
| Israel | $\bigcirc$ | -- | 22 (3.0) | $\bigcirc$ | -- | 37 (3.4) | $\bigcirc$ | 9 | 12 (2.6) | - | 8 |  | 68 (3.2) |
| Italy | - | 4-10 | 96 (1.4) | - | 6-7 | 96 (1.4) | - | 7-9 | 100 (0.0) | - | 7-9 |  | 100 (0.3) |
| Japan | - | 8 | 94 (1.9) | - | 7-8 | 92 (1.9) | $\bigcirc$ | 9 | 2 (0.0) | - | 8 |  | 97 (1.5) |
| Jordan | - | 7 | 88 (3.1) | - | 5-6 | 99 (0.9) | - | 8 | 98 (1.2) | - | 7 |  | 100 (0.0) |
| Korea, Rep. of | - | -- | S 87 (2.5) | - | -- | 91 (2.2) | $\bigcirc$ | 9 | s 28 (3.8) | - | -- | s | 97 (1.4) |
| Latvia | $\bigcirc$ | -- | s 22 (4.3) | $\bigcirc$ | 9 | 85 (3.2) | $\bigcirc$ | 9 | S 92 (2.9) | - | 7 | $s$ | 78 (4.7) |
| Lebanon | $\bigcirc$ | -- | 29 (4.4) | $\bigcirc$ | -- | 96 (1.6) | - | -- | 86 (3.0) | $\bigcirc$ | -- |  | 91 (2.6) |
| Lithuania | $\bigcirc$ | 9-10 | 24 (3.4) | $\bigcirc$ | 6-8 | 97 (1.2) | - | 8 | 99 (1.0) | - | 7 |  | 99 (0.9) |
| Macedonia, Rep. of | - | 7 | 99 (0.9) | - | 6 | 99 (0.7) | - | 7-8 | 100 (0.0) | - | 6 |  | 100 (0.0) |
| Malaysia | $\bigcirc$ | 9 | 62 (4.2) | - | 8 | 90 (2.8) | - | 8 | 95 (1.9) | - | 8 |  | 88 (2.9) |
| Moldova, Rep. of | - | 8 | r 83 (3.0) | - | 8 | 96 (1.7) | - | 8 | r 97 (1.6) | - | 8 | $r$ | 96 (1.8) |
| Morocco | $\bigcirc$ | -- | s 29 (6.2) | - | -- | 87 (4.5) | $\bigcirc$ | -- | $\mathrm{x} \times$ | $\bigcirc$ | -- |  | $\mathrm{x} \times$ |
| Netherlands | $\bigcirc$ | -- | 38 (4.6) | $\bigcirc$ | -- | 88 (3.2) | - | -- | 91 (2.9) | $\bigcirc$ | -- |  | 46 (4.9) |
| New Zealand | - | 6-8 | 64 (4.8) | - | 6-9 | 62 (4.8) | $\bigcirc$ | 9-10 | 23 (3.9) | $\bigcirc$ | 6-9 |  | 40 (5.0) |
| Norway | $\bigcirc$ | 9-10 | 13 (2.8) | - | 8-10 | 94 (1.9) | $\bigcirc$ | 9-10 | 5 (2.0) | $\bigcirc$ | 10 |  | 10 (2.6) |
| Palestinian Nat'l Auth. | - | 6 | 76 (4.0) | - | 6-7 | 97 (1.6) | - | 7 | 100 (0.0) | - | 7 |  | 99 (0.8) |
| Philippines | $\bigcirc$ | 9 | 32 (4.4) | $\bigcirc$ | 9 | 30 (3.9) | $\bigcirc$ | 9 | 34 (4.4) | $\bigcirc$ | 9 |  | 29 (4.1) |
| Romania | - | 7 | 93 (2.1) | - | 3-7 | 100 (0.0) | - | 7-9 | 100 (0.0) | - | -- |  | 100 (0.0) |
| Russian Federation | $\bigcirc$ | 9 | -- | - | -- | -- | - | -- | - - | - | -- |  | - - |
| Saudi Arabia | $\bigcirc$ | 10 | 52 (5.4) | - | 5-8 | 99 (0.8) | $\bigcirc$ | 9 | 8 (2.6) | - | 8 |  | 98 (1.3) |
| Scotland | $\bigcirc$ | -- | 37 (4.4) | - | -- | 87 (2.6) | $\bigcirc$ | -- | 33 (4.6) | - | -- |  | 44 (5.2) |
| Serbia | - | 7 | 94 (2.2) | - | 6 | 94 (2.2) | - | 7 | 96 (1.8) | - | 6 |  | 95 (2.0) |
| Singapore | - | 8 | 97 (0.9) | - | 5-7 | 92 (1.4) | $\bigcirc$ | 8 | 64 (3.2) | - | 8-9 |  | 81 (2.1) |
| Slovak Republic | $\bigcirc$ | 9 | 75 (3.1) | - | 7 | 100 (0.0) | - | 7 | 100 (0.0) | - | 7 |  | 96 (1.8) |
| Slovenia | - | 8 | 88 (2.7) | - | 7 | 100 (0.1) | - | 8 | 37 (4.0) | - | 7 |  | 82 (3.1) |
| South Africa | $\bigcirc$ | -- | r 44 (4.2) | $\bigcirc$ | -- | r 58 (4.1) | $\bigcirc$ | -- | r 54 (3.6) | $\bigcirc$ | -- | $r$ | 32 (4.0) |
| Sweden | $\bigcirc$ | 9 | 31 (3.8) | - | 8 | 92 (1.9) | $\bigcirc$ | 9 | 7 (1.7) | $\bigcirc$ | 11 |  | 36 (3.8) |
| Syrian Arab Republic | - | 8 | - - | - | -- | - - | $\bigcirc$ | 9 | -- | $\bigcirc$ | 10 |  | - - |
| Tunisia | $\bigcirc$ | 9 | 49 (4.2) | $\bigcirc$ | 9 | 98 (1.2) | $\bigcirc$ | 10 | 7 (1.9) | $\bigcirc$ | 10 |  | 90 (2.6) |
| United States | $\bigcirc$ | -- | 77 (2.4) | - | -- | 64 (3.2) | - | -- | 81 (2.5) | - | -- |  | 81 (2.7) |
| England | $\bigcirc$ | 7-10 | s 85 (4.2) | $\bigcirc$ | 4-8 | 89 (3.8) | $\bigcirc$ | 8-10 | r 71 (5.3) | $\bigcirc$ | 6-10 | s | 60 (5.3) |
| International Avg. |  |  | 63 (0.5) |  |  | 86 (0.4) |  |  | 63 (0.4) |  |  |  | 77 (0.4) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | - | -- | 84 (3.3) | - | -- | 81 (4.2) | $\bigcirc$ | 9 | 88 (3.2) | - | -- |  | 84 (3.6) |
| Indiana State, US | $\bigcirc$ | -- | 68 (5.8) | - | -- | 61 (5.1) | - | -- | 71 (5.1) | - | -- |  | 67 (5.0) |
| Ontario Province, Can. | - | 6-8 | 86 (2.7) | - | 5-6 | 84 (3.8) | - | 8 | 71 (4.6) | - | 2-7 |  | 85 (3.7) |
| Quebec Province, Can. | - | 7-8 | 66 (4.6) | - | 7 | 90 (3.2) | $\bigcirc$ | 9-11 | 9 (2.6) | - | 8-9 |  | 69 (4.8) |

Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Geometry | Translation，reflection， rotation，and enlargement |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |
| Armenia | $\bigcirc$ | －－ | r 60 （3．8） |  |
| Australia | $\bigcirc$ | 9 | 58 （3．6） |  |
| Bahrain | $\bigcirc$ | 7－9 | 16 （2．7） |  |
| Belgium（Flemish） | － | －－ | 85 （2．3） |  |
| Botswana | － | 8 | 15 （3．6） |  |
| Bulgaria | － | 8 | 65 （4．6） |  |
| Chile | $\bigcirc$ | 9－10 | 16 （2．2） |  |
| Chinese Taipei | － | 8 | 25 （3．6） |  |
| Cyprus | $\bigcirc$ | 4－6，10 | 8 （1．6） |  |
| Egypt | － | 8 | 94 （2．1） |  |
| Estonia | $\bigcirc$ | －－ | 53 （4．0） |  |
| Ghana | － | －－ | 22 （3．8） |  |
| Hong Kong，SAR | － | 7－9 | 83 （3．1） |  |
| Hungary | － | 7－9 | 79 （3．2） |  |
| Indonesia | $\bigcirc$ | 9 | 4 （1．4） |  |
| Iran，Islamic Rep．of | － | 7－11 | 89 （2．6） | 0 |
| Israel | $\bigcirc$ | －－ | 16 （2．8） | \％ |
| Italy | $\bigcirc$ | 9－10 | 47 （3．4） | 苛 |
| Japan | $\bigcirc$ | 9 | 67 （4．2） | － |
| Jordan | $\bigcirc$ | 9 | 15 （3．5） | 万 |
| Korea，Rep．of | － | －－ | s 65 （3．5） | 을 |
| Latvia | $\bigcirc$ | －－ | S 28 （5．1） | E |
| Lebanon | $\bigcirc$ | 9－11 | 42 （4．5） | $\frac{3}{3}$ |
| Lithuania | $\bigcirc$ | －－ | 35 （4．0） | 足 |
| Macedonia，Rep．of | － | 5，7 | 99 （0．7） | Ј |
| Malaysia | － | 8－9 | 76 （3．5） | $\stackrel{ \pm}{ \pm}$ |
| Moldova，Rep．of | － | 7，11 | r 48 （5．0） | $\bigcirc$ |
| Morocco | $\bigcirc$ | －－ | － | O |
| Netherlands | $\bigcirc$ | －－ | 69 （4．6） | － |
| New Zealand | － | 2－9 | 82 （2．7） | 敬 |
| Norway | － | 2－10 | 13 （2．6） | 2 |
| Palestinian Nat＇l Auth． | $\bigcirc$ | 9 | 5 （1．9） |  |
| Philippines | $\bigcirc$ | 9 | 10 （2．8） |  |
| Romania | － | 4－10 | 47 （4．1） | 艺 |
| Russian Federation | － | 8 or 9 | － | $\stackrel{\text { O}}{3}$ |
| Saudi Arabia | － | 5－8 | 68 （5．1） | 令 |
| Scotland | － | －－ | 50 （4．6） | － |
| Serbia | $\bigcirc$ | 5－6 | 81 （3．4） | $\stackrel{\square}{\circ}$ |
| Singapore | $\bigcirc$ | 8－10 | 54 （3．1） | $\stackrel{\square}{\square}$ |
| Slovak Republic | $\bigcirc$ | 9 | 22 （3．3） | $\pm$ |
| Slovenia | － | 7 | 83 （3．2） | 入 |
| South Africa | $\bigcirc$ | －－ | r 21 （3．0） | $\bigcirc$ |
| Sweden | $\bigcirc$ | 9 | 11 （2．3） | $\bigcirc$ |
| Syrian Arab Republic | $\bigcirc$ | 11 | －－ | ص |
| Tunisia | $\bigcirc$ | 10 | 11 （2．7） | ¢ |
| United States | － | －－ | 64 （3．1） | 旁 |
| $\ddagger$ England | － | 2－10 | S 89 （3．2） | $\stackrel{\sim}{\bar{\pi}}$ |
| International Avg． |  |  | 47 （0．5） | 苂 |
| Benchmarking Participants |  |  |  | $\frac{E}{10}$ |
| Basque Country，Spain | $\bigcirc$ | 10 | 14 （3．8） | \％ |
| Indiana State，US | － | －－ | 60 （6．0） | $\overline{\text { ¢ }}$ |
| Ontario Province，Can． | － | 2－8 | 62 （4．5） | ， |
| Quebec Province，Can． | － | 4－8 | 94 （2．2） |  |

Background data on intended curriculum provided by National Research Coordinators，and on imple－ mented curriculum by teachers at the time of testing．
$\ddagger$ Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
（）Standard errors appear in parentheses．Because results are rounded to the nearest whole number some totals may appear inconsistent．

A dash（－）indicates comparable data are not available
An＂$r$＂indicates data are available for at least 70 but less than $85 \%$ of the students．An＂$s$＂indicates data are available for at least 50 but less than $70 \%$ of the students．
of these topics were included in the intended curricula of almost all participants and taught to virtually all students ( $90 \%$ or more). These topics were: "angles - acute, right, straight, obtuse, reflex, complementary, and supplementary," "relationships for angles on a point or on a line," and "properties of geometric shapes: triangles and quadrilaterals." Two other topics were included in most participants' curricula and taught to more than 80 percent of students: "construct or draw triangles or rectangles of given dimensions," and "properties of angle bisectors and perpendicular bisectors of lines." Inclusion of the other geometry topics in the intended curriculum was more varied, as was the percentage of students taught the topics. The topics with least coverage in the classroom were "translation, reflection, rotation, and enlargement," and "relationships between two-dimensional and three-dimensional shapes," where less than half the students ( $47 \%$ and $41 \%$, respectively) were taught the topics. In countries where geometry topics were not in the intended curriculum at eighth grade, they often were intended primarily for later grades.

As shown in Exhibit 5.12, only two of the eight TIMSS data topics - "organizing a set of data by one or more characteristics using a tally chart, table, or graph" and "drawing and interpreting graphs, tables, pictographs, bar graphs, pie charts, and line graphs" - were included in the intended eighth-grade mathematics curriculum for more than half of the participants. These topics also were the only ones taught to more than half of the students ( 68 and 72 percent, respectively). TIMSS participants varied considerably in the extent to which they included the other data topics in their intended curriculum and taught them in the classroom. The two topics receiving least attention, in both the intended and implemented curriculum, were "sources of error in collecting and organizing data" and "evaluating interpretations of data with respect to correctness and completeness of interpretation." These were included in the curriculum of just a few countries, and had been taught to relatively few students, on average ( $32 \%$ and 29\%, respectively).

At the fourth grade, 12 of the 42 TIMSS mathematics topics were in the number content area. As shown in Exhibit 5.13, there was generally good coverage of the topics both in the intended curriculum and in the classroom. Five of the topics - "whole numbers including place value and ordering," "represent whole numbers using words, diagrams, or symbols," "properties of whole numbers," "computation with whole numbers," and "estimation with whole numbers" - appear in the intended curricula of almost all participants and have been taught to almost all students (more than $90 \%$ ). Four of the number topics appear in the intended curricula of less than half the participants - "equivalent fractions," "compare and order fractions," "adding and subtracting fractions with the same denominator," and "simple and proportional reasoning." These topics were taught to between one half and twothirds of the students, on average.

As shown in Exhibit 5.14, of the six TIMSS patterns and relationships topics, only "missing number in an equation" was included in the intended fourth-grade curriculum of almost all TIMSS participants. Practically all students had been taught this topic, including those in the countries where it was not part of the intended curriculum! "Patterns of numbers or shapes" and "pairs of numbers following a given rule" were in the intended curriculum of at least half of the participants, and were taught to 81 percent and 76 percent of students, respectively. "Simple equations" and "finding a rule for a relationship given some pairs of numbers" were included in the curriculum of relatively few participants ( 10 and 12 , respectively) but were taught to surprisingly large percentages of students ( $87 \%$ and $71 \%$ ).

As described earlier in this chapter, the fourth-grade mathematics curriculum included a strong emphasis on measurement topics in many countries. Exhibit 5.15 shows that four of the six TIMSS measurement topics were included in the intended curriculum of almost all participating entities. These included "standard units to measure length, area, mass/weight, angle, and time," "non-standard units to measure length, area, volume, and time," conversion factors between standard

| Data | Organizing a set of data by one or more characteristics using a tally chart，table， or graph |  |  | Sources of error in collecting and organizing data |  |  | Data collection methods |  |  | Drawing and interpreting graphs，tables，pictographs， bar graphs，pie charts， and line graphs |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | － | －－ | r 83 （3．2） | － | －－ | 60 （4．8） | $\bigcirc$ | －－ | S 72 （4．1） | $\bigcirc$ | －－ | r 74 （3．6） | ${ }_{\square}^{\text {¢ }}$ |
| Australia | － | 4－7 | 83 （3．5） | $\bigcirc$ | 9－10 | 45 （4．5） | － | 5－8 | 66 （3．9） | － | 5－8 | 86 （3．1） | $\stackrel{5}{0}$ |
| Bahrain | － | 1－8 | 75 （3．2） | $\bigcirc$ | －－ | 5 （1．7） | － | 7－8 | 11 （2．2） | － | 4－8，10 | 87 （2．9） | ¢ |
| Belgium（Flemish） | － | －－ | 73 （3．2） | $\bigcirc$ | －－ | 8 （2．2） | － | －－ | 7 （2．0） | － | －－ | 73 （3．7） | 은 |
| Botswana | $\bigcirc$ | 7 | 12 （2．5） | $\bigcirc$ | Tertiary | 3 （1．7） | $\bigcirc$ | Tertiary | 8 （2．4） | $\bigcirc$ | 9 | 13 （3．0） |  |
| Bulgaria | － | 5－6 | 59 （4．3） | $\bigcirc$ | －－ | 18 （3．8） | $\bigcirc$ | －－ | 19 （3．5） | $\bigcirc$ | 10－11 | 56 （4．5） | $\stackrel{H}{5}$ |
| Chile | － | 6－7 | 68 （3．6） | $\bigcirc$ | －－ | 36 （3．5） | － | 6 | 57 （3．4） | － | 7－8 | 67 （3．6） | － |
| Chinese Taipei | $\bigcirc$ | 9 | 12 （2．9） | $\bigcirc$ | 11 | 9 （2．5） | $\bigcirc$ | 11 | 7 （2．1） | $\bigcirc$ | 11 | 8 （2．3） | ¢ |
| Cyprus | $\bigcirc$ | 4－6，12 | 8 （1．5） | $\bigcirc$ | 12 | 2 （1．1） | $\bigcirc$ | 12 | 3 （1．5） | $\bigcirc$ | 4－6，12 | 1 （0．6） | $\stackrel{\sim}{4}$ |
| Egypt | － | 2－5 | 96 （1．7） | $\bigcirc$ | －－ | 24 （3．3） | $\bigcirc$ | －－ | 29 （3．4） | － | 3－5 | 83 （3．2） | $\stackrel{4}{4}$ |
| Estonia | － | 6，12 | 84 （2．9） | $\bigcirc$ | 12 | 59 （4．5） | $\bigcirc$ | 12 | 62 （4．1） | － | 6，12 | 90 （2．5） | 山 |
| Ghana | － | －－ | 76 （3．7） | $\bigcirc$ | －－ | 52 （4．3） | $\bigcirc$ | －－ | 65 （4．3） | $\bigcirc$ | －－ | 73 （3．6） | $\stackrel{\sim}{\square}$ |
| Hong Kong，SAR | － | 6－8 | 75 （3．7） | $\bigcirc$ | 10－11 | 45 （4．2） | $\bigcirc$ | －－ | 69 （4．0） | － | 6－9 | 79 （3．3） |  |
| Hungary | － | 6 | 80 （3．5） | $\bigcirc$ | －－ | 39 （4．4） | $\bigcirc$ | －－ | 39 （4．4） | － | 6 | 85 （3．0） |  |
| Indonesia | － | 8－9 | 87 （2．7） | $\bigcirc$ | 10 | 45 （4．3） | $\bigcirc$ | 11 | 64 （4．1） | － | 8－11 | 93 （2．3） |  |
| Iran，Islamic Rep．of | － | 6－10 | 71 （3．9） | $\bigcirc$ | 10 | 34 （4．2） | $\bigcirc$ | 10 | 35 （3．8） | － | 6，8，10 | 74 （3．2） | \％ |
| Israel | － | 3－10 | 68 （3．9） | $\bigcirc$ | －－ | 25 （3．3） | － | 3－10 | 37 （3．8） | － | 3－10 | 54 （3．9） | ¢ |
| Italy | － | 6 | 78 （3．4） | $\bigcirc$ | 9－13 | 24 （3．1） | － | 6－7 | 60 （3．5） | － | 4，7－9 | 86 （3．0） | － |
| Japan | － | 3－5 | 24 （3．9） | $\bigcirc$ | 10－12 | 12 （2．9） | $\bigcirc$ | 10－12 | 19 （3．4） | － | 3－5 | 55 （4．5） | － |
| Jordan | $\bigcirc$ | 9 | 58 （4．8） | $\bigcirc$ | 11 | 16 （3．4） | $\bigcirc$ | 11 | 26 （3．6） | － | 6－7 | 85 （3．2） |  |
| Korea，Rep．of | － | －－ | 84 （2．7） | $\bigcirc$ | －－ | 55 （3．7） | $\bigcirc$ | －－ | s 59 （3．8） | － | －－ | s 74 （3．2） | $\stackrel{\text { O}}{+}$ |
| Latvia | － | 7 | s 70 （5．2） | $\bigcirc$ | －－ | 27 （5．0） | $\bigcirc$ | －－ | s 37 （4．9） | － | 6－7 | s 94 （2．0） | $\underline{5}$ |
| Lebanon | － | －－ | 63 （4．8） | $\bigcirc$ | －－ | 29 （4．2） | $\bigcirc$ | －－ | 47 （4．9） | $\bigcirc$ | 8 | 49 （5．0） | $\frac{5}{3}$ |
| Lithuania | － | 4－10 | 96 （1．6） | $\bigcirc$ | －－ | 54 （4．0） | $\bigcirc$ | －－ | 85 （2．8） | － | 6－12 | 96 （1．4） | 年 |
| Macedonia，Rep．of | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | $\stackrel{\sim}{\circ}$ |
| Malaysia | － | 8 | 69 （4．1） | $\bigcirc$ | 10 | 33 （4．3） | $\bigcirc$ | 10 | 49 （4．0） | － | 6，8－9 | 80 （3．8） | $\stackrel{\text { F }}{\ddagger}$ |
| Moldova，Rep．of | $\bigcirc$ | －－ | r 75 （4．3） | $\bigcirc$ | －－ | r 51 （5．4） | $\bigcirc$ | －－ | r 69 （4．3） | $\bigcirc$ | －－ | r 74 （4．7） | $\bigcirc$ |
| Morocco | － | －－ | s 53 （6．0） | $\bigcirc$ | －－ | x x | $\bigcirc$ | －－ | $\mathrm{x} \times$ | $\bigcirc$ | －－ | s 61 （5．5） | O |
| Netherlands | － | －－ | 83 （3．9） | $\bigcirc$ | －－ | 11 （3．7） | $\bigcirc$ | －－ | 28 （5．1） | － | －－ | 96 （1．8） | $\stackrel{\text { V }}{ }$ |
| New Zealand | － | 3－9 | 90 （2．4） | － | 6－9 | 52 （3．8） | $\bigcirc$ | 6－9 | 73 （4．3） | － | 3－9 | 88 （2．4） | \＃ |
| Norway | － | 7－10 | 71 （4．1） | － | 8－10 | 48 （4．9） | － | 8－10 | 54 （4．5） | － | 6－10 | 83 （3．2） | $z$ |
| Palestinian Nat＇l Auth． | － | 2－6 | 64 （4．0） | $\bigcirc$ | 10 | 12 （2．9） | $\bigcirc$ | 10 | 28 （4．1） | － | 3－8 | 97 （1．7） | $\bigcirc$ |
| Philippines | $\bigcirc$ | 10 | 42 （4．7） | $\bigcirc$ | 10 | 29 （4．2） | $\bigcirc$ | 10 | 30 （4．2） | $\bigcirc$ | 10 | 50 （4．1） |  |
| Romania | － | 4－12 | 89 （2．8） | $\bigcirc$ | 11－12 | 44 （4．3） | $\bigcirc$ | 10－12 | 61 （4．7） | － | 4－12 | 81 （3．2） | $\stackrel{4}{c}$ |
| Russian Federation | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | － | －－ | －－ | $\stackrel{9}{3}$ |
| Saudi Arabia | $\bigcirc$ | 10 | 41 （6．2） | $\bigcirc$ | －－ | 7 （2．8） | $\bigcirc$ | 10 | 9 （3．0） | － | 5－6 | 40 （5．1） | $\stackrel{\sim}{\sim}$ |
| Scotland | － | －－ | 96 （1．5） | $\bigcirc$ | －－ | 31 （4．5） | － | －－ | 74 （3．9） | － | －－ | 95 （1．6） | － |
| Serbia | － | 8 | 86 （3．1） | $\bigcirc$ | 12 | 58 （3．7） | $\bigcirc$ | 12 | 56 （3．8） | $\bigcirc$ | 12 | 90 （2．5） | \％ |
| Singapore | － | 1－8 | 92 （1．2） | $\bigcirc$ | －－ | 30 （2．1） | $\bigcirc$ | －－ | 62 （2．8） | － | 3－8 | 94 （1．0） | $\varepsilon$ |
| Slovak Republic | $\bigcirc$ | 9 | 25 （4．0） | $\bigcirc$ | 9 | 10 （2．8） | $\bigcirc$ | 9 | 15 （3．2） | － | 7 | 42 （4．3） | $\stackrel{\text { f }}{\ddagger}$ |
| Slovenia | － | 3－4 | 71 （4．2） | $\bigcirc$ | －－ | 18 （2．9） | － | 4－5 | 31 （3．6） | － | 3－4 | 76 （3．7） | ते |
| South Africa | $\bigcirc$ | －－ | r 55 （3．9） | $\bigcirc$ | －－ | r 36 （3．7） | $\bigcirc$ | －－ | r 44 （3．7） | $\bigcirc$ | －－ | r 55 （3．8） |  |
| Sweden | － | 8 | 75 （3．0） | $\bigcirc$ | 8 | 23 （3．5） | － | 8 | 45 （3．7） | － | 8 | 84 （2．8） | $\bullet$ |
| Syrian Arab Republic | $\bigcirc$ | 11 | －－ | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ | $\bigcirc$ | －－ | －－ |  |
| Tunisia | $\bigcirc$ | －－ | 58 （3．9） | $\bigcirc$ | －－ | 23 （3．3） | $\bigcirc$ | －－ | 33 （3．9） | $\bigcirc$ | －－ | 55 （4．3） | ¢ |
| United States | － | －－ | 96 （1．2） | － | －－ | 65 （2．6） | $\bigcirc$ | －－ | 80 （2．3） | $\bigcirc$ | －－ | 97 （1．0） | 云 |
| $\ddagger$ England | － | K－6 | s $99(0.8)$ | $\bigcirc$ | 8－10 | 55 （6．6） | － | 6－10 | S 80 （5．4） | － | 6－10 | s 100 （0．0） | $\overline{\bar{\sigma}}$ |
| International Avg． |  |  | 68 （0．5） |  |  | 32 （0．6） |  |  | 44 （0．6） |  |  | 72 （0．5） | 苟 |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  | $\frac{\varepsilon}{10}$ |
| Basque Country，Spain | － | －－ | 45 （5．2） | $\bigcirc$ | 10 | 17 （4．6） | $\bigcirc$ | 10 | 39 （5．9） | $\odot$ | 9 | 43 （5．4） | ¢ |
| Indiana State，US | － | －－ | 92 （2．9） | － | －－ | 69 （5．7） | － | －－ | 80 （4．2） | － | －－ | 94 （2．2） | ¢ |
| Ontario Province，Can． | － | 1－8 | 97 （1．7） | － | 5－8 | 76 （3．9） | － | 3－8 | 91 （3．0） | － | 1－8 | 94 （2．4） | － |
| Quebec Province，Can． | $\bigcirc$ | 1－7，9－10 | 84 （3．6） | $\bigcirc$ | 10－11 | 23 （3．7） | $\bigcirc$ | 1－6，10 | 50 （5．2） | $\bigcirc$ | 1－7，10 | 81 （4．0） |  |

[^45]A dash（－）indicates comparable data are not available．
An＂$r$＂indicates data are available for at least 70 but less than $85 \%$ of the students．An＂ s ＂indicates data are available for at least 50 but less than $70 \%$ of the students．$A n$＂$x$＂indicates data are available for less than $50 \%$ of the students．


Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indiates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| NumberCountries | Whole numbers including place value and ordering |  |  | Represent whole numbers using words, diagrams, or symbols |  |  |  | Properties of whole numbers such as odd and even, multiples, or factors |  |  | Computation with whole numbers |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | - | -- | r 100 (0.0) | - | -- | r | 92 (2.1) | - | -- | r 95 (1.6) | - | -- | r 99 (1.1) |
| Australia | - | -- | 100 (0.3) | - | -- |  | 96 (1.4) | - | -- | 97 (1.1) | - | -- | 100 (0.1) |
| Belgium (Flemish) | - | -- | 99 (0.6) | - | -- |  | 94 (1.9) | - | -- | 97 (1.4) | - | -- | 100 (0.0) |
| Chinese Taipei | - | 3 | 100 (0.0) | - | 1 |  | 92 (2.4) | - | 4 | 53 (4.1) | - | 3 | 100 (0.0) |
| Cyprus | - | 3-7 | 100 (0.3) | - | 2-7 |  | 99 (0.7) | - | 2-7 | 93 (2.3) | $\bigcirc$ | 6 | 99 (0.7) |
| England | - | K-4 | r 100 (0.0) | $\bigcirc$ | K-4 | $r$ | 95 (2.1) | $\bigcirc$ | K-4 | r 100 (0.0) | $\bigcirc$ | K-4 | r 100 (0.0) |
| Hong Kong, SAR | - | 3 | 100 (0.0) | - | 3 |  | 83 (3.5) | - | 4 | 99 (0.8) | - | 3 | 100 (0.0) |
| Hungary | - | 1 | 99 (0.6) | - | 1 |  | 98 (1.2) | - | 3 | 100 (0.0) | - | 4 | 99 (0.6) |
| Iran, Islamic Rep. of | - | 4 | 99 (0.6) | - | 2-3 |  | 98 (1.2) | - | 3-4 | 90 (3.0) | - | 2-4 | 84 (2.9) |
| Italy | - | 2-5 | 99 (0.6) | - | 1-5 |  | 97 (1.2) | - | 1-8 | 95 (1.3) | - | 1-8 | 100 (0.4) |
| Japan | - | 1-4 | 100 (0.0) | - | 1-3 |  | 84 (3.2) | $\bigcirc$ | 5-6 | 24 (3.4) | - | 1-4 | 100 (0.0) |
| Latvia | - | -- | s 96 (2.4) | - | -- | s | 96 (1.8) | $\bigcirc$ | -- | S 95 (1.6) | - | -- | s $99(1.0)$ |
| Lithuania | - | 1-4 | 99 (0.5) | - | 1-6 |  | 91 (2.4) | $\bigcirc$ | 5-6 | 91 (1.8) | - | 1 | 100 (0.5) |
| Moldova, Rep. of | - | -- | $r 96$ (1.7) | - | -- | $r$ | 93 (2.3) | $\bigcirc$ | -- | r 97 (1.7) | - | -- | $r \quad 97$ (1.6) |
| Morocco | $\bigcirc$ | -- | x x | $\bigcirc$ | -- |  | x X | $\bigcirc$ | -- | x x | $\bigcirc$ | -- | x x |
| Netherlands | - | -- | 99 (0.7) | - | -- | $r$ | 83 (3.9) | $\bigcirc$ | 6 | 88 (3.1) | $\bigcirc$ | -- | 100 (0.0) |
| New Zealand | - | K-5 | 100 (0.0) | - | K-5 |  | 98 (1.0) | $\bigcirc$ | 3 | 93 (1.5) | - | K-5 | 100 (0.2) |
| Norway | - | 2-7 | 100 (0.3) | - | 2-7 |  | 74 (3.6) | $\bigcirc$ | 2-7 | 88 (2.7) | - | 2-7 | 100 (0.0) |
| Philippines | - | -- | 100 (0.0) | - | -- |  | 97 (1.7) | - | -- | 98 (1.3) | - | -- | 99 (1.1) |
| Russian Federation | - | -- | - - | - | -- |  | - - | - | -- | - - | - | -- | - - |
| Scotland | - | -- | r 100 (0.0) | - | -- | s | 87 (3.7) | - | -- | r 99 (0.8) | - | -- | r 100 (0.3) |
| Singapore | - | 1-5 | 100 (0.0) | - | 1-5 |  | 98 (1.0) | - | 3-4 | 99 (0.9) | - | 1-5 | 100 (0.0) |
| Slovenia | - | 2 | 99 (0.9) | - | 2 |  | 97 (1.3) | - | 3 | 98 (1.3) | - | 2 | 100 (0.0) |
| Tunisia | - | -- | r 98 (1.3) | $\bigcirc$ | 7 | r | 91 (2.6) | - | -- | 98 (1.0) | - | -- | r 98 (1.4) |
| United States | - | -- | 100 (0.0) | - | -- |  | 98 (0.7) | - | -- | 98 (0.8) | - | -- | 100 (0.0) |
| Yemen | - | -- | - - | - | -- |  | - - | - | 2,5 | - - | - | -- | - - |
| International Avg. |  |  | $99(0.2)$ |  |  |  | 93 (0.5) |  |  | 91 (0.4) |  |  | 99 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | - | -- | 100 (0.0) | - | -- |  | 100 (0.0) | - | -- | 97 (2.0) | - | -- | 100 (0.0) |
| Ontario Province, Can. | - | 1-6 | 100 (0.0) | - | 1-6 |  | 99 (1.0) | - | 3,6-7 | 93 (2.5) | - | 1-6 | 100 (0.0) |
| Quebec Province, Can. | - | 1-6 | 99 (0.8) | - | 1-6 |  | 100 (0.2) | - | 1-6 | 90 (2.9) | - | 1-6 | 100 (0.1) |
|  | - All or almost all students |  |  | - Only the more able students |  |  |  | Not included in the curriculum through fourth grade |  |  |  |  |  |

[^46]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

Exhibit 5.13: Intended and Taught TIMSS Number Topics (Continued...)
mathematics
Grade


[^47]Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 5.13: Intended and Taught TIMSS Number Topics (...Continued)


Grade


[^48]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " x " indicates data are available for less than $50 \%$ of the students.
units," and "instruments to measure length, area, mass/weight, angle, and time." Less often included in participants' intended curricula were "calculating areas and perimeters of squares" and "estimating length, area, volume, weight, and time." Regardless of whether they were in the intended curriculum or not, the measurement topics were widely taught, with no fewer than 80 percent of students being taught each one.

Although there are 11 geometry topics in the TIMSS fourthgrade mathematics assessment, their inclusion in participants' curricula varies widely, as does the percentage of students taught each of the topics. Exhibit 5.16 shows that only one geometry topic - "angles greater than, equal to, or less than a right angle" - was included in the intended curriculum of more than half the participants, and that three topics - "congruent triangles," "similar triangles," and "translation, reflection, and rotation" - were included by very few participants indeed. The percentage of students taught the geometry topics also was generally lower than in areas such as number or measurement. Percentages ranged from 74 percent for the aforementioned angles topic to just 33 percent for "translation, reflection, and rotation." For many countries, geometry topics not included in the fourth-grade curriculum were intended for later grades.

As shown in Exhibit 5.17, three of the seven TIMSS data topics were included in the intended fourth-grade mathematics curriculum of more than half the participating entities. Furthermore, these three topics, "organizing a set of data by one characteristic," "reading data directly from tables, pictographs, and bar graphs," and "display data using tables, pictographs, and bar graphs," were each taught to more than 85 percent of students. "Comparing and matching different representations of the same data" was in the curriculum of the fewest participants (11), yet was taught to 65 percent of students, on average.


Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " x " indicates data are available for less than $50 \%$ of the students.

| Patterns and Relationships | Pairs of numbers following a given rule |  |  |  | Finding a rule for a relationship given some pairs of numbers |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |
| Armenia | - | -- | r | 92 (2.1) | - | -- | $r$ | 91 (2.2) |
| Australia | - | -- |  | 62 (4.9) | $\bigcirc$ | 5 |  | 62 (4.8) |
| Belgium (Flemish) | $\bigcirc$ | 6 |  | 80 (2.9) | $\bigcirc$ | 6 |  | 78 (3.2) |
| Chinese Taipei | $\bigcirc$ | 5 |  | 72 (3.7) | $\bigcirc$ | 5 |  | 76 (3.5) |
| Cyprus | - | 4-7 |  | 86 (2.4) | - | 4-7 |  | 72 (3.8) |
| England | - | 4 | $r$ | 78 (4.1) | - | 4 | $r$ | 75 (4.6) |
| Hong Kong, SAR | $\bigcirc$ | 7-9 |  | 40 (4.8) | $\bigcirc$ | 7-9 |  | 45 (4.9) |
| Hungary | - | 2 |  | 97 (1.4) | - | 2 |  | 99 (0.7) |
| Iran, Islamic Rep. of | $\bigcirc$ | 8 |  | 69 (4.1) | $\bigcirc$ | 8 |  | 50 (4.8) |
| Italy | $\bigcirc$ | 3-4 |  | 76 (3.4) | - | 3-4 |  | 81 (2.9) |
| Japan | - | 4 |  | 43 (3.5) | - | 4 |  | 41 (3.8) |
| Latvia | - | -- | s | 84 (4.0) | $\bigcirc$ | -- | S | 88 (3.7) |
| Lithuania | $\bigcirc$ | 4 |  | 81 (3.1) | $\bigcirc$ | 11-12 |  | 70 (3.7) |
| Moldova, Rep. of | - | -- | $r$ | 94 (2.1) | $\bigcirc$ | -- | $r$ | 88 (3.0) |
| Morocco | $\bigcirc$ | -- |  | x x | $\bigcirc$ | -- |  | x x |
| Netherlands | $\bigcirc$ | 7 |  | 65 (4.4) | $\bigcirc$ | 6 |  | 56 (4.6) |
| New Zealand | - | 4 |  | 78 (2.5) | - | 4 |  | 79 (2.9) |
| Norway | $\bigcirc$ | 9-10 |  | 40 (4.0) | $\bigcirc$ | 9-10 |  | 34 (3.8) |
| Philippines | $\bigcirc$ | -- |  | 68 (4.4) | $\bigcirc$ | -- |  | 66 (4.8) |
| Russian Federation | - | -- |  | - - | $\bigcirc$ | -- |  | - - |
| Scotland | $\bigcirc$ | -- | $r$ | 80 (3.6) | $\bigcirc$ | -- | $r$ | 75 (4.7) |
| Singapore | $\bigcirc$ | 7 |  | 91 (2.2) | $\bigcirc$ | 7 |  | 73 (3.7) |
| Slovenia | - | 4 |  | 92 (2.4) | $\bigcirc$ | 4 |  | 75 (4.2) |
| Tunisia | $\bigcirc$ | 7 | r | 83 (3.2) | $\bigcirc$ | 7 | r | 77 (3.9) |
| United States | - | -- |  | 86 (1.8) | $\bigcirc$ | -- |  | 85 (2.0) |
| Yemen | $\bigcirc$ | 6-7 |  | - - | $\bigcirc$ | -- |  | - - |
| International Avg. |  |  |  | 76 (0.7) |  |  |  | 71 (0.8) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US | - | -- |  | 82 (4.5) | - | -- |  | 68 (6.0) |
| Ontario Province, Can. | - | 3-6 |  | 76 (3.7) | - | 4-9 |  | 84 (3.8) |
| Quebec Province, Can. | $\bigcirc$ | 3-4 |  | 76 (3.6) | - | 3-4 |  | 69 (4.5) |

[^49][^50]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.


[^51]Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| MeasurementCountries | Calculating areas and perimeters of squares |  |  |  | Estimating length, area, volume, weight, and time |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
| Armenia | - | -- | r | 100 (0.3) | - | -- | r | 96 (1.6) |
| Australia | - | -- |  | 79 (3.5) | - | -- |  | 86 (4.0) |
| Belgium (Flemish) | $\bigcirc$ | 5 |  | 78 (3.6) | $\bigcirc$ | 5 |  | 91 (2.5) |
| Chinese Taipei | $\bigcirc$ | 5 |  | 93 (2.2) | $\bigcirc$ | 5 |  | 93 (2.1) |
| Cyprus | - | -- |  | 98 (1.2) | $\bigcirc$ | 6 |  | 91 (2.4) |
| England | - | 3-4 | $r$ | 97 (1.5) | - | 1-3 | $r$ | 95 (2.4) |
| Hong Kong, SAR | - | 4 |  | 82 (3.5) | $\bigcirc$ | 7-9 |  | 81 (3.4) |
| Hungary | - | 4 |  | 81 (3.3) | - | 1 |  | 84 (3.4) |
| Iran, Islamic Rep. of | - | 3-4 |  | 96 (1.5) | $\bigcirc$ | 6 |  | $\mathrm{x} \times$ |
| Italy | - | 4-6 |  | 60 (3.2) | - | 4-10 |  | 47 (3.4) |
| Japan | - | 4 |  | 88 (2.4) | $\bigcirc$ | 6 |  | 47 (4.4) |
| Latvia | - | -- | s | 99 (0.7) | - | -- | $s$ | 98 (1.6) |
| Lithuania | - | 3-4 |  | 100 (0.0) | - | 1-4 |  | 94 (1.7) |
| Moldova, Rep. of | - | -- | $r$ | 100 (0.0) | - | -- | $r$ | 99 (0.7) |
| Morocco | $\bigcirc$ | -- |  | $\mathrm{x} \times$ | $\bigcirc$ | -- |  | $\mathrm{x} \times$ |
| Netherlands | $\bigcirc$ | 5 |  | 65 (4.9) | - | -- |  | 61 (5.0) |
| New Zealand | $\bigcirc$ | 5 |  | 71 (3.0) | - | K-5 |  | 82 (2.5) |
| Norway | $\bigcirc$ | 5-7 |  | 67 (4.4) | - | 3-7 |  | 59 (4.9) |
| Philippines | $\bigcirc$ | -- |  | 80 (4.1) | $\bigcirc$ | -- |  | 72 (4.1) |
| Russian Federation | - | -- |  | - - | - | -- |  | - - |
| Scotland | $\bigcirc$ | -- | $r$ | 69 (4.6) | $\bigcirc$ | -- | $r$ | 87 (3.0) |
| Singapore | - | 3-4 |  | 97 (1.5) | - | 1-4 |  | 93 (2.2) |
| Slovenia | - | 4-5 |  | 0 (0.0) | - | 4 |  | 63 (4.0) |
| Tunisia | - | -- |  | $\mathrm{x} \times$ | $\bigcirc$ | 6 | r | 88 (2.9) |
| United States | - | -- |  | 87 (1.7) | - | -- |  | 76 (2.5) |
| Yemen | - | -- |  | - - | - | 4-6 |  | - - |
| International Avg. |  |  |  | 81 (0.6) |  |  |  | 81 (0.7) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US | - | -- |  | 79 (4.6) | - | -- |  | 67 (5.3) |
| Ontario Province, Can. | - | 4-5 |  | 90 (2.8) | - | 3-8 |  | 83 (3.7) |
| Quebec Province, Can. | $\bigcirc$ | 5-7 |  | 77 (3.8) | - | 1-6 |  | 62 (4.1) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.


[^52]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 5.16: Intended and Taught TIMSS Geometry Topics (Continued...)



[^53]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 5.16: Intended and Taught TIMSS Geometry Topics (...Continued)

| Geometry | Symmetry about a line |  |  |  | Two-dimensional symmetrical figures |  |  |  | Translation, reflection, and rotation |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | $\bigcirc$ | -- | $r$ | 22 (4.0) | - | -- | r | 18 (3.5) | - | -- | $r$ | 7 (2.0) |
| Australia | - | -- |  | 87 (2.9) | - | -- |  | 86 (2.9) | $\bigcirc$ | 6 |  | 68 (4.4) |
| Belgium (Flemish) | - | -- |  | 68 (3.5) | $\bigcirc$ | 5 |  | 55 (4.2) | $\bigcirc$ | 6 |  | 27 (3.4) |
| Chinese Taipei | $\bigcirc$ | 5 |  | 25 (3.9) | $\bigcirc$ | 5 |  | 33 (4.4) | $\bigcirc$ | 6 |  | 13 (2.9) |
| Cyprus | $\bigcirc$ | 7 |  | 94 (1.5) | $\bigcirc$ | 7 |  | 65 (3.8) | $\bigcirc$ | 7 |  | 33 (3.8) |
| England | $\bigcirc$ | K-4 | $r$ | 95 (2.4) | $\bigcirc$ | 1-4 | $r$ | 91 (3.1) | $\bigcirc$ | 2-4 | $r$ | 65 (4.6) |
| Hong Kong, SAR | $\bigcirc$ | 6 |  | 69 (4.4) | $\bigcirc$ | 7-9 |  | 67 (4.2) | $\bigcirc$ | 7-9 |  | 13 (2.9) |
| Hungary | $\bigcirc$ | 6 |  | 75 (3.7) | $\bigcirc$ | 6 |  | 86 (3.1) | $\bigcirc$ | 7 |  | 45 (4.2) |
| Iran, Islamic Rep. of | - | 4,5,7 |  | 78 (3.7) | - | 4,5,7 |  | 56 (5.0) | $\bigcirc$ | 7,11 |  | 32 (5.0) |
| Italy | - | 4-6,9 |  | 80 (2.9) | - | 4-6,9 |  | 69 (3.5) | $\bigcirc$ | 5-10 |  | 55 (3.7) |
| Japan | $\bigcirc$ | 7 |  | 1 (1.0) | $\bigcirc$ | 7 |  | 1 (0.7) | $\bigcirc$ | -9 |  | 1 (0.7) |
| Latvia | $\bigcirc$ | -- | $s$ | 39 (5.5) | $\bigcirc$ | -- | 5 | 43 (5.0) | $\bigcirc$ | -- | $s$ | 20 (3.9) |
| Lithuania | $\bigcirc$ | 8 |  | 68 (4.0) | $\bigcirc$ | 8 |  | 67 (4.1) | $\bigcirc$ | -- |  | 23 (3.2) |
| Moldova, Rep. of | - | -- | $r$ | 84 (3.0) | $\bigcirc$ | -- | $r$ | 64 (4.3) | $\bigcirc$ | -- | $r$ | 42 (4.7) |
| Morocco | - | -- |  | $\mathrm{x} \times$ | - | -- |  | $\mathrm{x} \times$ | $\bigcirc$ | -- |  | $\mathrm{x} \times$ |
| Netherlands | - | -- |  | 14 (3.3) | - | -- |  | 19 (3.2) | $\bigcirc$ | 7 |  | 34 (4.3) |
| New Zealand | - | K-5 |  | 84 (2.4) | - | K-5 |  | 85 (2.3) | - | K-5 |  | 80 (2.3) |
| Norway | - | 2-7 |  | 59 (4.2) | - | 2-7 |  | 39 (4.2) | - | 4-7 |  | 44 (4.2) |
| Philippines | $\bigcirc$ | -- |  | 61 (5.0) | $\bigcirc$ | -- |  | 53 (4.6) | $\bigcirc$ | -- |  | 44 (4.9) |
| Russian Federation | $\bigcirc$ | 5 |  | - - | $\bigcirc$ | 5 |  | - | $\bigcirc$ | 8-9 |  | - |
| Scotland | $\bigcirc$ | -- | $r$ | 94 (2.6) | - | -- | $r$ | 83 (4.0) | $\bigcirc$ | -- | $r$ | 28 (4.2) |
| Singapore | - | 4 |  | 90 (2.4) | - | 4 |  | 73 (3.6) | $\bigcirc$ | 8 |  | 11 (2.3) |
| Slovenia | - | 2 |  | 22 (3.6) | - | 2 |  | 34 (3.7) | $\bigcirc$ | 7 |  | 12 (3.0) |
| Tunisia | $\bigcirc$ | 10 | r | 34 (4.0) | $\bigcirc$ | 10 |  | 34 (4.1) | $\bigcirc$ | 10 | $r$ | 6 (2.1) |
| United States | $\bigcirc$ | -- |  | 81 (2.3) | - | -- |  | 74 (2.6) | - | -- |  | 64 (2.9) |
| Yemen | $\bigcirc$ | 7,10 |  | - - | $\bigcirc$ | -- |  | - - | $\bigcirc$ | 7 |  | - - |
| International Avg. |  |  |  | 62 (0.7) |  |  |  | 56 (0.8) |  |  |  | 33 (0.8) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | $\bigcirc$ | 5 |  | 65 (5.7) | $\bigcirc$ | 5 |  | 58 (6.1) | $\bigcirc$ | 6 |  | 41 (6.0) |
| Ontario Province, Can. | - | 2-5 |  | 81 (3.9) | - | 2-5 |  | 84 (3.7) | - | 2-7 |  | 58 (5.0) |
| Quebec Province, Can. | - | 3-4 |  | 59 (4.8) | - | 3-4 |  | 66 (4.0) | - | 3-7 |  | 34 (4.3) |

All or almost all students Only the more able students $\quad \bigcirc$ Not included in the curriculum through fourth grade

[^54]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.


Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 5.17: Intended and Taught TIMSS Data Topics (...Continued)

All or almost all students $\quad$ Only the more able students $\quad$ Not included in the curriculum through fourth grade

[^55]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.


## Chapter 6

## Teachers of Mathematics

Since the teacher is central in creating a classroom environment that supports learning mathematics, Chapter 6 presents information about the preparation and background of mathematics teachers in the participating countries. The chapter begins with information about the licensing and/or certification requirements for teaching mathematics at the eighth and fourth grades in the TIMSS countries. The National Research Coordinators were responsible for providing this information as part of completing the Curriculum Questionnaire.

The remaining sections of the chapter include information about the demographic characteristics of the teaching force and about teachers' educational background and preparation, including opportunities for professional development. To collect information from teachers, TIMSS administered a two-part questionnaire in which teachers were asked to provide information about their background and training and their instructional practices. Chapter 6 essentially presents teachers' responses to the first part of the questionnaire, while Chapter 7 presents information from the second part about classroom instruction.

Because the sampling for the teacher questionnaires was based on participating students, teachers' responses do not necessarily represent all eighth-grade or all fourth-grade mathematics teachers in each country. Rather, they represent teachers of the representative
samples of students assessed. It is important to note that when information from the teacher questionnaire is being reported, the student is always the unit of analysis. That is, the data shown are the percentages of students whose teachers reported on various characteristics or instructional strategies. Using the student as the unit of analysis makes it possible to describe the instruction received by representative samples of students and the characteristics of the teachers delivering that instruction. Although this perspective may differ from that obtained by simply collecting information from teachers, it is consistent with the TIMSS goals of providing information about the educational contexts and performance of students.

The teachers who completed the questionnaires were the mathematics teachers of the students who took the TIMSS 2003 test. At the eighth grade, the general sampling procedure was to sample a mathematics class from each participating school, administer the test to those students, and ask their teacher to complete the questionnaire. At the fourth grade, students often only have one teacher for all subjects, so this teacher is their mathematics teacher and the one who completed the questionnaire. In either case, the information about teachers' characteristics and instruction is tied directly to the students tested. Sometimes, however, teachers did not complete the questionnaire assigned to them, so most countries had some percentage of students for whom no teacher questionnaire information is available. The exhibits in this chapter have special notations on this point. For a country where teacher responses are available for at least 70 but less than 85 percent of the students, an " r " is included next to its data. Where teacher responses are available for at least 50 but less than 70 percent of the students, an " $s$ " is included. Where teacher responses are available for less than 50 percent, an " $x$ " replaces the data.

## What Are the Requirements for Being a Mathematics Teacher?

Exhibit 6.1 presents the country-level responses about the requirements for being certified or licensed to teach mathematics at the eighth and
fourth grades. Countries were asked about five requirements, including supervised practical experience (practicum), passing an examination, obtaining a university degree, completion of a probationary period, and completion of an induction program. At the eighth grade, 70 percent of the TIMSS countries ( 33 out of 47) and three benchmarking entities required a university degree (or equivalent) and just as many participants required fulfillment of some type of practicum for certification as a mathematics teacher. In more than half of the countries ( 28 out of 47) and all of the benchmarking participants, certification required passing an examination. A probationary period was required in 23 countries and two benchmarking entities. Of the TIMSS countries, 11 required completion of an induction program as did two of the benchmarking entities. For the United States and Canada, it should be noted that requirements for certification vary across states and provinces.

At the fourth grade, most of the TIMSS countries (19 out of 26) and all three of the benchmarking participants required some type of practicum for certification. Eighteen of the countries participating at the fourth grade and all three of the benchmarking participants required two or more of the following for certification - passing an examination, a university degree, or completion of a probationary period. Similar to the eighth grade, the fewest number of fourth grade participants required completion of an induction program.

Exhibit 6.2 contains participants' reports about the organization or authority responsible for granting certification for mathematics teachers. Across participants at the eighth grade, universities or colleges were most likely to be responsible for granting certification (55\% of the countries and Quebec province). The next most prevalent procedure was for the ministry of education to grant certification. A handful of participants reported using licensing boards and three (New Zealand, Scotland, and Syria) reported granting certification through a teacher organization. The responses at the fourth grade were similar, with ministries of education and universities/colleges being the organizations most often responsible for granting certification.

| Countries | Pre-practicum and Supervised Practicum | Passing an Examination | University Degree or Equivalent | Completion of a Probationary Teaching Period | Completion of an Induction Program |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Australia | - | $\bigcirc$ | - | - | $\bigcirc$ |
| Bahrain | - | - | - | - | $\bigcirc$ |
| Belgium (Flemish) | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Botswana | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Bulgaria | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Chile | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Chinese Taipei | - | $\bigcirc$ | - | - | $\bigcirc$ |
| Cyprus | $\bigcirc$ | $\bigcirc$ | - | - | $\bigcirc$ |
| Egypt | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| England | - | - | - | - | - |
| Estonia | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Ghana | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hong Kong, SAR | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hungary | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Indonesia | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Iran, Islamic Rep. of | - | $\bigcirc$ | $\bigcirc$ | - | - |
| Israel | - | $\bigcirc$ | - | - | - |
| Italy | $\bigcirc$ | - | - | - | $\bigcirc$ |
| Japan | - | - | - | - | - |
| Jordan | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Korea, Rep. of | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Latvia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Lebanon | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - |
| Lithuania | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Macedonia, Rep. of | $\bigcirc$ | $\bigcirc$ | - | - | $\bigcirc$ |
| Malaysia | - | - | $\bigcirc$ | - | - |
| Moldova, Rep. of | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Morocco | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Netherlands | - | - | $\bigcirc$ | - | $\bigcirc$ |
| New Zealand | - | $\bigcirc$ | - | - | $\bigcirc$ |
| Norway | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Palestinian Nat'l Auth. | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Philippines | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Romania | - | - | - | - | - |
| Russian Federation | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Saudi Arabia | - | - | - | - | - |
| Scotland | - | - | - | - | - |
| Serbia | - | - | - | - | - |
| Singapore | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Slovak Republic | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Slovenia | - | $\bigcirc$ | - | - | - |
| South Africa | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Sweden | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Syrian Arab Republic | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Tunisia | - | - | $\bigcirc$ | - | $\bigcirc$ |
| United States | - | $\bigcirc$ | - | - | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | $\bigcirc$ | - | - | $\bigcirc$ | $\bigcirc$ |
| Indiana State, US | - | - | $\bigcirc$ | - | - |
| Ontario Province, Can. | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | - | - | - | - | - |

Country reported Yes for the particular option

Country reported No
for the particular option

## Exhibit 6.1: Current Requirements for Being a Mathematics Teacher



Countries
Pre-practicum
and Supervised
Practicum

| Passing an |  |  |
| :---: | :---: | :---: |
| Examination | University <br> Degree or <br> Equivalent | Completion of <br> a Probationary <br> Teaching Period |

Completion of
an Induction
Program

| Countries | Minister/ Ministry of Education | National/State Licensing Board | Universities/ Colleges | Teacher Organization |
| :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Australia | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Bahrain | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Belgium (Flemish) | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Botswana | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Bulgaria | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Chile | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Chinese Taipei | $\bigcirc$ | - | - | $\bigcirc$ |
| Cyprus | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Egypt | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| England | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Estonia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Ghana | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Hong Kong, SAR | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hungary | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Indonesia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Iran, Islamic Rep. of | - | $\bigcirc$ | - | $\bigcirc$ |
| Israel | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Italy | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Japan | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Jordan | - | $\bigcirc$ | - | $\bigcirc$ |
| Korea, Rep. of | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Latvia | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Lebanon | - | $\bigcirc$ | - | $\bigcirc$ |
| Lithuania | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Macedonia, Rep. of | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Malaysia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Moldova, Rep. of | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Morocco | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Netherlands | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| New Zealand | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Norway | - | - | - | $\bigcirc$ |
| Palestinian Nat'l Auth. | - | $\bigcirc$ | - | $\bigcirc$ |
| Philippines | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Romania | - | $\bigcirc$ | - | $\bigcirc$ |
| Russian Federation | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Saudi Arabia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Scotland | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Serbia | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Singapore | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Slovak Republic | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Slovenia | - | $\bigcirc$ | - | $\bigcirc$ |
| South Africa | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Sweden | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Syrian Arab Republic | - | - | - | - |
| Tunisia | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| United States | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |
| Basque Country, Spain | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Indiana State, US | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Ontario Province, Can. | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |

[^56] for the particular option

Country reported No for the particular option

| Countries | Minister/ Ministry of Education | National/State Licensing Board | Universities/ Colleges | Teacher Organization |
| :---: | :---: | :---: | :---: | :---: |
| Armenia | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Australia | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Belgium (Flemish) | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Chinese Taipei | $\bigcirc$ | - | - | $\bigcirc$ |
| Cyprus | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| England | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hong Kong, SAR | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Hungary | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Iran, Islamic Rep. of | - | $\bigcirc$ | - | $\bigcirc$ |
| Italy | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Japan | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Latvia | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Lithuania | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Moldova, Rep. of | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Morocco | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Netherlands | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| New Zealand | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Norway | - | - | $\bigcirc$ | $\bigcirc$ |
| Philippines | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Russian Federation | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Scotland | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Singapore | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Slovenia | - | $\bigcirc$ | - | $\bigcirc$ |
| Tunisia | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| United States | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Yemen | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Benchmarking Participants |  |  |  |  |
| Indiana State, US | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Ontario Province, Can. | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Quebec Province, Can. | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
|  |  |  |  | Country reported Yes for the particular option <br> Country reported No for the particular option |

## What Are the Background Characteristics of Mathematics Teachers?

Exhibit 6.3 presents a considerable amount of information about the background characteristics of mathematics teachers at the eighth and fourth grades, including their gender, age, certification status, and number of years of teaching experience. Typically, larger percentages of students were taught mathematics by female teachers than male teachers, particularly at the fourth grade. At the eighth grade, on average, internationally, 58 percent of the students were taught mathematics by females and 42 percent by males, and similar percentages were found in a number of countries. However, at least 85 percent of students had female teachers in Armenia, Bulgaria, Estonia, Hungary, Latvia, Lithuania, Moldova, the Russian Federation, and Slovenia. By contrast, only in Egypt and Ghana were as many as 85 percent of the students taught mathematics by male teachers. At the fourth grade, on average, internationally, four-fifths of the mathematics teaching force was female. Across the participants, in each country, with the exception of Morocco and Tunisia at least 50 percent, and often a much higher percentage, of the fourth-grade students were taught by female teachers.

Looking to the last column of Exhibit 6.3, it can be seen that, in general, the mathematics teaching force around the world is quite experienced. At both the eighth and fourth grades, mathematics teachers reported 16 years of teaching experience, on average, internationally.

Given their years of teaching experience, it follows that the majority of the eighth-grade and the fourth-grade students were taught mathematics by teachers in their 30 s and 40 s. If there was a steady replenishing of the teaching force, one might expect approximately equivalent percentages of students taught by teachers in their 20s, $30 \mathrm{~s}, 40 \mathrm{~s}$, and 50 s. Very few countries, however, had a comparatively younger teaching force at either the eighth or fourth grades. At the eighth grade, on average, internationally, only 17 percent of students were taught by teachers younger than age 30 . The five countries with
the most students (more than 40 percent) taught by younger teachers were Botswana, Ghana, the Palestinian National Authority, Saudi Arabia, and Singapore. The pattern was very similar at the fourth grade. On average, internationally, 19 percent of the students were taught by teachers younger than 30 years old, and with the exception of Singapore $(41 \%)$, this percentage was usually well under 40 percent.

At the other end of the age distribution, 23 percent of the eighth-grade students and 21 percent of the fourth-grade students internationally were taught by teachers age 50 or older. At the eighth grade, interestingly, the teaching force was relatively older in several countries. More than half of the students in Italy, Moldova, and Serbia had teachers at least 50 years of age.

Finally, from Exhibit 6.3, it can be seen that teachers at both the eighth and fourth grades, reported having full certification rather than provisional or emergency credentials. Given the potential problem of teacher shortages for a variety of reasons, it is interesting to note that, on average, internationally, 88 percent of the eighth-grade students and 85 percent of the fourth-grade students were taught mathematics by certified teachers. Of course, the situation varied dramatically across the TIMSS countries. For example, in South Africa only 45 percent of the eighth-grade students and in Tunisia only 21 percent of the fourthgrade students were taught mathematics by a fully certified teacher.

Exhibit 6.3: Mathematics Teachers' Gender, Age, Certification, and Number of Years of Teaching

| Countries | Percentage of Students by Teacher Characteristics |  |  |  |  |  |  | Number of Years of Teaching |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Gender |  | Age |  |  |  | Have Full Certificate* |  |  |
|  | Female | Male | 29 Years or Under | 30-39 Years | 40-49 Years | 50 Years or Older |  |  |  |
| Armenia | 87 (2.4) | 13 (2.4) | 3 (0.9) | 35 (3.6) | 37 (3.5) | 25 (3.0) | 94 (1.9) | r | 19 (0.7) |
| Australia | 49 (4.7) | 51 (4.7) | 13 (2.6) | 26 (4.4) | 37 (5.1) | 24 (3.7) | 89 (2.9) |  | 16 (0.8) |
| Bahrain | 50 (0.5) | 50 (0.5) | 36 (3.3) | 44 (4.0) | 17 (3.3) | 3 (1.4) | 84 (3.1) |  | 11 (0.7) |
| Belgium (Flemish) | 75 (2.6) | 25 (2.6) | 24 (3.1) | 22 (2.9) | 36 (3.6) | 18 (2.9) | - - |  | 18 (0.8) |
| Botswana | 27 (4.0) | 73 (4.0) | 49 (4.4) | 45 (4.3) | 4 (1.8) | 2 (1.2) | 96 (1.7) | r | 6 (0.5) |
| Bulgaria | 88 (3.0) | 12 (3.0) | 5 (1.9) | 15 (2.9) | 46 (3.9) | 34 (3.6) | 100 (0.0) |  | 21 (0.7) |
| Chile | 54 (3.7) | 46 (3.7) | 7 (1.7) | 15 (2.9) | 38 (3.5) | 39 (3.1) | 87 (2.3) |  | 22 (0.7) |
| Chinese Taipei | 46 (4.1) | 54 (4.1) | 19 (2.9) | 42 (4.2) | 21 (3.4) | 18 (3.3) | 96 (1.4) |  | 14 (0.9) |
| Cyprus | 63 (3.0) | 37 (3.0) | 5 (1.2) | 37 (3.3) | 31 (2.8) | 27 (2.7) | - |  | 12 (0.6) |
| Egypt | 14 (2.9) | 86 (2.9) | 11 (2.3) | 56 (4.0) | 31 (4.0) | 1 (0.4) | 99 (0.3) |  | 14 (0.4) |
| Estonia | 89 (2.5) | 11 (2.5) | 12 (2.6) | 16 (3.4) | 32 (3.6) | 40 (4.3) | 91 (2.2) |  | 22 (1.2) |
| Ghana | 11 (3.3) | 89 (3.3) | 48 (3.9) | 31 (4.3) | 17 (3.5) | 5 (1.9) | 71 (4.4) |  | 8 (0.6) |
| Hong Kong, SAR | 53 (4.3) | 47 (4.3) | 29 (3.7) | 41 (4.4) | 19 (3.1) | 10 (2.3) | 77 (3.3) |  | 12 (0.7) |
| Hungary | 85 (2.6) | 15 (2.6) | 5 (1.4) | 21 (3.1) | 39 (3.6) | 35 (3.8) | - - |  | 22 (0.8) |
| Indonesia | 53 (4.0) | 47 (4.0) | 12 (3.0) | 49 (3.8) | 32 (3.6) | 7 (1.9) | 100 (0.0) |  | 14 (0.6) |
| Iran, Islamic Rep. of | 39 (4.2) | 61 (4.2) | 23 (2.8) | 41 (3.8) | 29 (3.8) | 6 (1.8) | 69 (3.5) |  | 14 (0.5) |
| Israel | 79 (2.6) | 21 (2.6) | 14 (2.4) | 35 (3.3) | 35 (2.8) | 16 (2.6) | 96 (1.3) |  | 16 (0.6) |
| Italy | 80 (3.0) | 20 (3.0) | 3 (1.0) | 7 (2.1) | 31 (3.1) | 59 (3.1) | 95 (1.6) |  | 23 (0.6) |
| Japan | 32 (3.8) | 68 (3.8) | 13 (2.6) | 35 (3.9) | 35 (4.0) | 16 (3.1) | 99 (0.7) |  | 17 (0.7) |
| Jordan | 49 (2.0) | 51 (2.0) | 31 (4.0) | 47 (4.8) | 19 (3.6) | 3 (1.5) | 76 (3.9) |  | 11 (0.6) |
| Korea, Rep. of | r 67 (3.6) | 33 (3.6) | 17 (2.7) | 39 (3.3) | 36 (3.6) | 7 (1.9) | 98 (0.8) | s | 13 (0.5) |
| Latvia | 92 (2.5) | 8 (2.5) | 5 (2.0) | 23 (3.8) | 39 (4.1) | 33 (4.0) | - |  | 22 (0.9) |
| Lebanon | 46 (4.6) | 54 (4.6) | 22 (3.1) | 31 (4.1) | 29 (4.0) | 18 (3.1) | 51 (4.6) |  | 15 (0.8) |
| Lithuania | 91 (2.5) | 9 (2.5) | 7 (2.0) | 26 (3.5) | 40 (4.0) | 26 (3.4) | 100 (0.0) |  | 20 (0.8) |
| Macedonia, Rep. of | 68 (3.8) | 32 (3.8) | 2 (0.6) | 25 (3.6) | 36 (3.9) | 38 (3.4) | x x |  | 21 (0.9) |
| Malaysia | 72 (3.9) | 28 (3.9) | 26 (3.4) | 44 (4.2) | 28 (3.5) | 2 (1.3) | 80 (3.5) |  | 11 (0.6) |
| Moldova, Rep. of | 87 (3.0) | 13 (3.0) | 11 (2.5) | 13 (2.9) | 24 (4.5) | 52 (4.8) | 91 (2.4) | $r$ | 26 (0.9) |
| Morocco | s 15 (4.6) | 85 (4.6) | 8 (3.9) | 21 (5.0) | 60 (6.8) | 11 (3.8) | s 100 (0.0) |  | x x |
| Netherlands | 32 (4.7) | 68 (4.7) | 17 (3.3) | 14 (3.1) | 45 (4.6) | 25 (3.8) | - |  | 17 (1.0) |
| New Zealand | 45 (4.7) | 55 (4.7) | 12 (3.9) | 28 (4.6) | 34 (4.9) | 26 (3.0) | 79 (4.8) |  | 14 (1.0) |
| Norway | 36 (3.8) | 64 (3.8) | 13 (2.6) | 22 (3.3) | 21 (3.3) | 43 (4.2) | 96 (1.9) |  | 18 (1.0) |
| Palestinian Nat'l Auth. | 49 (3.1) | 51 (3.1) | 41 (4.3) | 29 (4.1) | 27 (3.6) | 3 (1.5) | 70 (3.8) |  | 10 (0.7) |
| Philippines | 73 (3.9) | 27 (3.9) | 18 (3.6) | 44 (4.7) | 24 (3.5) | 14 (2.9) | 93 (2.3) |  | 11 (0.7) |
| Romania | 51 (4.2) | 49 (4.2) | 13 (3.0) | 17 (3.4) | 22 (3.3) | 48 (4.1) | 96 (1.8) |  | 24 (1.0) |
| Russian Federation | 95 (1.6) | 5 (1.6) | 9 (1.8) | 19 (2.3) | 33 (4.3) | 40 (3.7) | 97 (1.4) |  | 24 (0.9) |
| Saudi Arabia | 42 (3.1) | 58 (3.1) | 43 (5.8) | 38 (5.9) | 14 (3.1) | 5 (2.0) | 96 (1.3) |  | 10 (0.8) |
| Scotland | 50 (4.7) | 50 (4.7) | 15 (3.8) | 22 (4.0) | 34 (4.1) | 29 (3.9) | -- | $r$ | 16 (1.0) |
| Serbia | 58 (3.9) | 42 (3.9) | 7 (2.2) | 17 (3.3) | 21 (3.5) | 55 (4.0) | 89 (2.6) |  | 22 (0.9) |
| Singapore | 67 (2.3) | 33 (2.3) | 43 (2.5) | 22 (2.2) | 15 (1.8) | 20 (2.1) | 97 (0.7) |  | 12 (0.7) |
| Slovak Republic | 79 (3.6) | 21 (3.6) | 11 (2.6) | 22 (3.9) | 28 (3.9) | 39 (4.3) | 91 (2.1) |  | 21 (1.1) |
| Slovenia | 87 (3.1) | 13 (3.1) | 8 (2.4) | 24 (3.4) | 48 (4.4) | 20 (3.6) | 91 (2.4) |  | 20 (0.8) |
| South Africa | 40 (3.3) | 60 (3.3) | 19 (2.7) | 55 (3.4) | 21 (3.1) | 5 (1.6) | 45 (3.2) |  | 11 (0.6) |
| Sweden | 44 (3.6) | 56 (3.6) | 13 (2.7) | 28 (3.1) | 22 (2.8) | 37 (3.2) | 86 (2.5) |  | 14 (0.8) |
| Tunisia | 32 (4.0) | 68 (4.0) | 23 (3.2) | 42 (3.8) | 23 (3.1) | 12 (2.5) | 91 (2.5) | s | 12 (0.9) |
| United States | 65 (2.7) | 35 (2.7) | 13 (2.0) | 26 (2.8) | 29 (2.9) | 32 (2.9) | 93 (1.8) |  | 15 (0.7) |
| ま England | 54 (6.2) | 46 (6.2) | 24 (5.0) | 19 (5.0) | 36 (6.5) | 20 (4.9) | - - | $r$ | 15 (1.5) |
| International Avg. | 58 (0.5) | 42 (0.5) | 17 (0.4) | 30 (0.6) | 30 (0.6) | 23 (0.5) | 88 (0.4) |  | 16 (0.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 74 (5.0) | 26 (5.0) | 5 (2.4) | 20 (4.0) | 38 (4.9) | 36 (4.3) | - - |  | 21 (0.9) |
| Indiana State, US | 60 (5.9) | 40 (5.9) | 22 (5.2) | 29 (5.1) | 12 (3.6) | 38 (6.3) | 99 (0.0) |  | -- |
| Ontario Province, Can. | 46 (5.0) | 54 (5.0) | 24 (4.4) | 42 (4.9) | 16 (3.0) | 18 (3.3) | 96 (1.7) |  | 11 (0.9) |
| Quebec Province, Can. | 47 (5.1) | 53 (5.1) | 21 (4.1) | 36 (4.7) | 15 (3.5) | 28 (3.9) | 92 (3.0) |  | 15 (1.0) |

[^57][^58]Exhibit 6.3: Mathematics Teachers' Gender, Age, Certification, and Number of Years of Teaching


| Countries | Percentage of Students by Teacher Characteristics |  |  |  |  |  |  |  |  | Number of Years of Teaching |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Gender |  | Age |  |  |  | Have Full Certificate* |  |  |  |
|  | Female | Male | 29 Years or Under | 30-39 Years | 40-49 Years | 50 Years or Older |  |  |  |  |
| Armenia | 88 (2.6) | 12 (2.6) | 8 (1.9) | 25 (3.2) | 38 (3.8) | 30 (4.0) | r | 92 (2.2) |  | 20 (0.9) |
| Australia | 75 (4.2) | 25 (4.2) | 21 (3.5) | 14 (2.4) | 46 (4.4) | 19 (3.0) | $r$ | 91 (2.4) |  | 17 (0.9) |
| Belgium (Flemish) | 78 (2.7) | 22 (2.7) | 23 (2.9) | 37 (3.1) | 27 (2.9) | 14 (2.1) |  | 100 (0.0) |  | 16 (0.7) |
| Chinese Taipei | 80 (2.9) | 20 (2.9) | 26 (3.4) | 44 (4.0) | 23 (3.0) | 7 (2.2) |  | 88 (2.6) |  | 11 (0.7) |
| Cyprus | 79 (3.3) | 21 (3.3) | 39 (4.3) | 50 (4.3) | 5 (1.7) | 7 (2.2) |  | - |  | 11 (0.7) |
| England | 73 (4.2) | 27 (4.2) | 30 (4.7) | 24 (4.4) | 25 (3.8) | 21 (3.5) |  | - | $r$ | 12 (1.0) |
| Hong Kong, SAR | 73 (4.3) | 27 (4.3) | 34 (4.5) | 34 (4.3) | 15 (2.8) | 17 (3.9) |  | 89 (2.6) |  | 13 (1.1) |
| Hungary | 94 (1.8) | 6 (1.8) | 8 (2.1) | 33 (3.7) | 40 (3.7) | 19 (3.2) |  | - - |  | 19 (0.8) |
| Iran, Islamic Rep. of | 51 (4.8) | 49 (4.8) | 14 (3.4) | 39 (4.2) | 39 (4.4) | 8 (2.6) |  | 33 (4.2) |  | 16 (0.7) |
| Italy | 96 (1.2) | 4 (1.2) | 3 (1.4) | 18 (2.4) | 39 (3.6) | 39 (3.3) |  | 97 (1.3) |  | 21 (0.6) |
| Japan | 63 (3.8) | 37 (3.8) | 11 (2.8) | 27 (3.3) | 39 (4.1) | 23 (3.6) |  | 99 (1.0) |  | 19 (0.8) |
| Latvia | 99 (0.6) | 1 (0.6) | 6 (1.8) | 38 (3.9) | 31 (4.0) | 25 (3.5) |  | - - |  | 20 (0.9) |
| Lithuania | 99 (0.6) | 1 (0.6) | 12 (2.2) | 37 (3.1) | 32 (3.1) | 19 (2.6) |  | 100 (0.0) |  | 19 (0.7) |
| Moldova, Rep. of | 98 (1.2) | 2 (1.2) | 15 (2.8) | 30 (4.0) | 35 (4.2) | 20 (3.5) |  | 64 (4.6) |  | 21 (0.9) |
| Morocco | r 36 (4.5) | 64 (4.5) | 24 (3.7) | 20 (4.1) | 47 (4.6) | 9 (2.4) | s | 96 (1.8) | s | 15 (0.7) |
| Netherlands | 64 (4.6) | 36 (4.6) | 30 (4.4) | 18 (3.7) | 24 (4.3) | 28 (3.9) |  | - |  | 16 (1.1) |
| New Zealand | 81 (2.5) | 19 (2.5) | 24 (2.8) | 26 (3.2) | 31 (2.9) | 19 (2.3) |  | 85 (2.5) |  | 12 (0.6) |
| Norway | 81 (2.4) | 19 (2.4) | 13 (2.7) | 24 (3.3) | 31 (4.1) | 31 (3.4) |  | 97 (1.3) |  | 16 (0.9) |
| Philippines | 87 (2.9) | 13 (2.9) | 14 (3.1) | 39 (5.1) | 24 (4.2) | 22 (4.0) |  | 89 (2.9) |  | 13 (0.9) |
| Russian Federation | 99 (0.8) | 1 (0.8) | 11 (2.6) | 36 (3.4) | 28 (3.5) | 25 (3.7) |  | 98 (0.9) |  | 21 (0.7) |
| Scotland | 93 (2.2) | 7 (2.2) | 22 (3.8) | 27 (3.6) | 22 (3.9) | 29 (4.3) |  | - - | $r$ | 16 (0.9) |
| Singapore | 82 (3.1) | 18 (3.1) | 41 (3.8) | 38 (3.6) | 7 (2.2) | 15 (2.6) |  | 97 (1.4) |  | 10 (0.9) |
| Slovenia | 97 (1.6) | 3 (1.6) | 11 (3.0) | 32 (4.3) | 36 (4.6) | 21 (3.7) | $r$ | 89 (3.1) |  | 19 (0.8) |
| Tunisia | 46 (4.3) | 54 (4.3) | 11 (2.5) | 46 (4.6) | 24 (3.6) | 19 (3.3) | r | 21 (3.5) | $r$ | 18 (0.8) |
| United States | 85 (2.0) | 15 (2.0) | 20 (1.8) | 28 (2.1) | 21 (2.2) | 31 (2.7) |  | 91 (1.6) |  | 14 (0.6) |
| International Avg. | 80 (0.6) | 20 (0.6) | 19 (0.6) | 31 (0.7) | 29 (0.7) | 21 (0.7) |  | 85 (0.6) |  | 16 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US | 88 (3.6) | 12 (3.6) | 16 (3.8) | 22 (4.9) | 22 (5.2) | 40 (5.3) |  | 100 (0.0) |  | - |
| Ontario Province, Can. | 76 (3.8) | 24 (3.8) | 22 (4.1) | 23 (3.9) | 27 (4.6) | 28 (4.5) |  | 92 (3.0) |  | 13 (0.9) |
| Quebec Province, Can. | 93 (2.0) | 7 (2.0) | 14 (3.3) | 31 (4.1) | 19 (3.6) | 36 (4.4) |  | 84 (3.6) |  | 18 (0.9) |

## Background data provided by teachers.

*Does not include provisional or emergency certificate
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

## What Preparation Do Teachers Have for Teaching Mathematics?

Exhibits 6.4 through 6.8 present teachers' reports about their preparation to teach mathematics, including educational experiences before actually teaching and opportunities for developing their expertise after entering the profession (often referred to as pre-service and in-service training).

Exhibit 6.4 presents teacher's highest level of education. Even though the percentages were somewhat higher at the eighth grade than the fourth grade, approximately two-thirds of the eighth- and fourth-grade students were taught mathematics by teachers having at least a university degree or equivalent. At the eighth grade, 59 percent of the students were taught by teachers with a university degree and another 17 percent by teachers who had coursework beyond the initial university degree. At the fourth grade, 52 percent of the students were taught by teachers with a university degree and another 13 percent by teachers with coursework beyond that degree.

Despite a relatively well-educated teaching force, on average, the situation varied dramatically among countries. At the eighth grade, for example, at least half the students were taught by teachers with work beyond the initial university degree in Armenia, Australia, Bulgaria, the Russian Federation, Tunisia, and the United States. In contrast, 72 percent of the eighth-grade students in Morocco were taught by teachers only having completed secondary school.

According to the results of the Curriculum Questionnaire, almost all of the students participating in TIMSS 2003 were supposed to be learning mathematics according to a national (for most countries) or regional curriculum. To gather some information about coherence between the intended curriculum and teacher preparation, the Curriculum Questionnaire also asked about specific teacher training in how to teach this curriculum - as part of either teachers' pre-service or inservice education. Exhibit 6.5 has the results. The majority of countries and benchmarking participants reported preparation in how to teach
the intended curriculum as part of both pre- and in-service training, and most reported coverage in at least one of these places. Countries reporting no specific training in how to teach the intended curriculum included Chile, Korea, Moldova, Morocco, Norway, and Sweden.

Teachers' reports about their major area or areas of study during their postsecondary education can be found also, in Exhibit 6.5. At the eighth grade, on average, internationally, the majority studied mathematics education (54\%) or mathematics ( $70 \%$ ) or both (since teachers often reported that their study was focused in more than one area). For example, it was not uncommon for teachers in some countries to report pedagogy as a major area of study and mathematics as another major area. As might be considered, the situation was different at the fourth grade. Here teachers typically studied primary or elementary education (approximately 80 percent, on average). On average, for the primary education majors, about one-fourth ( $26 \%$ ) reported specializing in mathematics, 4 percent in science, and half ( $50 \%$ ) not having any particular specialization. Countries with more than half the fourthgrade students being taught by mathematics specialists were Latvia, Moldova, and the Russian Federation.

In today's fast-paced world of frequent important discoveries and new technologies in the fields of pedagogy and mathematics, it is very important for teachers to continually update their knowledge. To provide context for considering this important part of teacher training in the TIMSS countries, Exhibits 6.6 through 6.8 contain information about teachers' opportunities for and participation in professional development activities.

Exhibit 6.6 presents schools' reports about the opportunities provided to teachers in five major areas: supporting implementation of the official curriculum, supporting school-level goals, improving content knowledge, improving teaching skills, and using technology. Within each area, schools reported the frequency of teachers' involvement. At both grades, schools reported that their professional development programs emphasized improving content knowledge and teaching skills.


Background data provided by teachers
*Based on countries categorizations to UNESCO's International Standard Classification of Education (Operational Manual for ISCED-1997).
**For example, doctorate, master's, postgraduate diploma, and honors bachelor's degree.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

| Countries |  | Percentage of Students by Their Teachers' Educational Level |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Beyond Initial University Degree** | Finished University or Equivalent | Finished Post Secondary Education but Not University | Finshed Upper Secondary Schooling | Did Not Complete Upper Secondary Schooling |
| Armenia |  | 79 (2.9) | 12 (2.4) | 6 (1.9) | 2 (1.1) | 0 (0.0) |
| Australia |  | 27 (4.1) | 49 (4.4) | 24 (3.4) | 0 (0.0) | 0 (0.0) |
| Belgium (Flemish) |  | 0 (0.0) | 0 (0.0) | 100 (0.0) | 0 (0.0) | 0 (0.0) |
| Chinese Taipei |  | 5 (1.8) | 77 (3.8) | 12 (2.8) | 6 (2.2) | 0 (0.0) |
| Cyprus |  | 19 (3.1) | 81 (3.1) | 1 (0.4) | 0 (0.0) | 0 (0.0) |
| England | $r$ | 4 (1.9) | 96 (1.9) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| Hong Kong, SAR |  | 4 (1.8) | 51 (4.9) | 44 (5.0) | 0 (0.0) | 1 (0.0) |
| Hungary |  | 3 (1.3) | 97 (1.3) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| Iran, Islamic Rep. of |  | 2 (1.9) | 21 (4.2) | 34 (4.7) | 34 (3.9) | 8 (2.2) |
| Italy |  | 1 (0.5) | 13 (2.2) | 3 (1.0) | 84 (2.3) | 0 (0.0) |
| Japan |  | 3 (1.4) | 83 (3.1) | 14 (2.9) | 0 (0.0) | 0 (0.0) |
| Latvia |  | 0 (0.0) | 84 (3.2) | 3 (1.4) | 13 (3.0) | 0 (0.0) |
| Lithuania |  | 16 (2.4) | 75 (3.2) | 8 (2.1) | 0 (0.0) | 1 (0.5) |
| Moldova, Rep. of |  | 0 (0.0) | 65 (4.2) | 21 (4.0) | 12 (2.9) | 2 (1.0) |
| Morocco | s | 1 (0.8) | 23 (4.6) | 4 (2.9) | 54 (5.7) | 18 (3.5) |
| Netherlands |  | 1 (0.5) | - - | 98 (1.0) | 1 (0.9) | 0 (0.0) |
| New Zealand |  | 10 (2.0) | 54 (3.2) | 36 (3.3) | 0 (0.0) | 0 (0.0) |
| Norway |  | 1 (0.6) | 57 (3.9) | 38 (3.9) | 2 (1.1) | 2 (0.8) |
| Philippines |  | 7 (2.3) | 93 (2.3) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| Russian Federation |  | 44 (3.8) | 26 (3.4) | 29 (3.5) | 0 (0.0) | 0 (0.0) |
| Scotland | r | 12 (3.1) | 88 (3.1) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| Singapore |  | 3 (1.7) | 40 (4.0) | 41 (3.9) | 16 (3.1) | 0 (0.0) |
| Slovenia |  | 34 (4.4) | 56 (4.8) | 3 (1.4) | 7 (2.3) | 0 (0.0) |
| Tunisia | r | 2 (1.2) | 7 (2.4) | 43 (4.2) | 48 (4.0) | 1 (0.9) |
| United States |  | 52 (2.6) | 47 (2.6) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| International Avg. |  | 13 (0.4) | 52 (0.7) | 22 (0.5) | 11 (0.4) | 1 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US |  | - - | - - | - - | - - | - - |
| Ontario Province, Can. |  | 9 (2.8) | 84 (3.6) | 7 (2.3) | 0 (0.0) | 0 (0.0) |
| Quebec Province, Can. |  | 9 (2.6) | 88 (2.9) | 4 (1.1) | 0 (0.0) | 0 (0.0) |

## Background data provided by teachers.

*Based on countries categorizations to UNESCO's International Standard Classification of Education (Operational Manual for ISCED-1997).
**For example, doctorate, master's, postgraduate diploma, and honors bachelor's degree
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


[^59]A dash ( - ) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| Countries | Teachers Receive Specific Preparation in How to Teach the Intended Mathematics Curriculum |  | Teachers' Major Area of Study in Their Postsecondary Education |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Primary/Elementary Education with a Major or Specialization in Mathematics | Primary/Elementary Education with a Major or Specialization in Science but Not in Mathematics | Mathematics or Science Major or Specialization without a Major in Primary/Elementary Education | Primary/Elementary Education without a Major or Specialization in Mathematics or Science | Other |
|  | As Part of Pre-Service Education | As Part of In-Service Education | Percent of Students | Percent of Students | Percent of Students | Percent of Students | Percent of Students |
| Armenia | - | - | 9 (2.3) | 0 (0.0) | 86 (2.7) | 2 (0.9) | 3 (1.1) |
| Australia | $\bigcirc$ | - | 17 (3.5) | 6 (1.7) | 1 (0.5) | 72 (4.1) | 4 (1.4) |
| Belgium (Flemish) | - | - | 34 (3.5) | 3 (1.2) | 2 (1.1) | 59 (3.2) | 1 (0.6) |
| Chinese Taipei | - | - | 29 (3.7) | 3 (1.3) | 11 (2.8) | 36 (4.2) | 22 (3.4) |
| Cyprus | - | $\bigcirc$ | 18 (2.8) | 11 (2.3) | 1 (0.5) | 68 (3.6) | 2 (1.0) |
| England | - | - | 8 (3.1) | 7 (2.6) | 5 (1.8) | 64 (4.3) | 16 (2.7) |
| Hong Kong, SAR | - | - | 37 (4.4) | 1 (0.9) | 11 (3.2) | 34 (4.7) | 17 (3.5) |
| Hungary | - | - | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x | $\mathrm{x} \times$ |
| Iran, Islamic Rep. of | - | - | s $\quad 50(5.5)$ | 2 (1.2) | 5 (2.5) | 32 (5.2) | 11 (2.8) |
| Italy | $\bigcirc$ | - | s 0 (0.0) | 0 (0.0) | 6 (1.8) | 5 (2.1) | 88 (2.8) |
| Japan | - | - | 15 (3.0) | 7 (2.1) | 1 (0.7) | 56 (3.9) | 22 (3.4) |
| Latvia | - | - | 63 (3.7) | 2 (1.2) | 3 (1.4) | 24 (3.4) | 7 (2.6) |
| Lithuania | - | - | 14 (2.5) | 2 (1.1) | 3 (1.0) | 78 (3.2) | 4 (1.3) |
| Moldova, Rep. of | $\bigcirc$ | $\bigcirc$ | 51 (4.6) | 2 (1.3) | 5 (1.7) | 32 (4.4) | 10 (2.5) |
| Morocco | - | - | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x | x x | $\mathrm{x} \times$ |
| Netherlands | - | - | 12 (3.1) | 9 (2.7) | - - | 76 (3.7) | 2 (1.7) |
| New Zealand | - | - | 21 (2.6) | 10 (2.3) | 1 (0.5) | 63 (3.2) | 6 (1.4) |
| Norway | $\bigcirc$ | $\bigcirc$ | - | - - | -- | - - | - - |
| Philippines | - | - | 24 (4.0) | 7 (2.2) | 4 (2.2) | 54 (4.3) | 11 (2.9) |
| Russian Federation | - | - | 57 (3.5) | 2 (1.3) | 1 (0.8) | 35 (3.7) | 5 (1.6) |
| Scotland | - | - | r 8 (2.4) | 5 (1.9) | 1 (0.1) | 79 (3.6) | 7 (2.3) |
| Singapore | - | - | 48 (4.2) | 4 (1.6) | 8 (2.1) | 24 (2.7) | 16 (3.1) |
| Slovenia | - | - | 34 (4.2) | 2 (1.6) | 0 (0.0) | 63 (4.4) | 0 (0.0) |
| Tunisia | - | - | 15 (3.0) | 0 (0.4) | 6 (1.8) | 67 (4.1) | 12 (2.7) |
| United States | - | -- | 8 (1.5) | 6 (1.4) | 3 (0.8) | 72 (2.8) | 12 (1.9) |
| International Avg. |  |  | 26 (0.7) | 4 (0.3) | 7 (0.4) | 50 (0.8) | 13 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | - | $\bigcirc$ | -- | -- | -- | - - | - - |
| Ontario Province, Can. | - | $\bigcirc$ | 6 (2.2) | 4 (1.5) | 5 (2.1) | 63 (5.1) | 21 (4.0) |
| Quebec Province, Can. | - | - | 15 (2.9) | 2 (0.9) | 4 (1.7) | 68 (4.2) | 12 (2.7) |
| Country reported Yes for the particular option |  |  |  |  |  |  |  |
| Country reported No for the particular option |  |  |  |  |  |  |  |

Background data provided by National Research Coordinators and by teachers
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science


Grade 0

| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Supporting the Implementation of the National or Regional Curriculum |  |  | Designing or Supporting the School's Own Improvement Goals |  |  |  |
|  | 3 Times or More a Year | 1-2 Times a Year | Never |  | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | $r \quad 4$ (1.8) | 34 (4.2) | 63 (4.5) | r | 21 (4.6) | 35 (4.8) | 44 (4.7) |
| Australia | 48 (5.0) | 38 (5.1) | 14 (2.9) |  | 60 (4.5) | 35 (4.3) | 4 (1.9) |
| Bahrain | 60 (0.2) | 23 (0.2) | 16 (0.1) |  | 66 (0.2) | 19 (0.1) | 16 (0.1) |
| Belgium (Flemish) | 11 (2.7) | 67 (4.2) | 22 (3.7) |  | 12 (3.2) | 62 (4.5) | 26 (3.9) |
| Botswana | 30 (4.3) | 38 (4.7) | 32 (3.8) |  | 43 (4.7) | 42 (4.7) | 15 (3.0) |
| Bulgaria | 2 (1.1) | 30 (4.2) | 68 (4.3) |  | 11 (2.8) | 36 (4.2) | 53 (4.5) |
| Chile | 27 (4.0) | 55 (4.7) | 19 (3.4) |  | 50 (3.8) | 39 (3.8) | 11 (2.3) |
| Chinese Taipei | 11 (2.8) | 46 (4.3) | 43 (4.2) |  | 43 (4.3) | 46 (4.1) | 11 (2.7) |
| Cyprus | 10 (0.2) | 90 (0.2) | 0 (0.0) |  | 50 (0.3) | 47 (0.3) | 3 (0.0) |
| Egypt | 88 (2.7) | 8 (2.4) | 3 (1.5) |  | 88 (2.4) | 9 (2.0) | 3 (1.2) |
| Estonia | 20 (3.6) | 62 (4.0) | 18 (3.3) |  | 25 (3.6) | 46 (4.5) | 29 (4.3) |
| Ghana | 17 (3.7) | 33 (4.4) | 50 (5.1) |  | 45 (4.3) | 29 (4.4) | 26 (3.5) |
| Hong Kong, SAR | 47 (4.6) | 46 (4.4) | 7 (2.5) |  | 44 (5.1) | 51 (5.1) | 5 (2.0) |
| Hungary | 15 (3.1) | 32 (3.7) | 53 (3.8) |  | 69 (3.5) | 28 (3.6) | 3 (1.5) |
| Indonesia | 16 (3.2) | 34 (4.4) | 50 (4.7) |  | 26 (4.0) | 49 (4.3) | 25 (4.0) |
| Iran, Islamic Rep. of | 20 (3.4) | 48 (4.1) | 32 (3.7) |  | 31 (4.1) | 43 (3.9) | 25 (3.3) |
| Israel | 91 (2.0) | 6 (1.8) | 3 (1.2) |  | 81 (3.7) | 17 (3.4) | 2 (1.3) |
| Italy | 28 (3.4) | 34 (3.5) | 38 (3.5) |  | 35 (3.7) | 38 (3.7) | 27 (3.4) |
| Japan | 15 (3.1) | 28 (3.8) | 57 (4.3) |  | 31 (3.8) | 40 (3.8) | 29 (3.8) |
| Jordan | 39 (4.2) | 41 (4.1) | 20 (3.3) |  | 41 (4.6) | 40 (3.6) | 19 (3.6) |
| Korea, Rep. of | 9 (2.3) | 73 (3.8) | 18 (3.6) |  | 9 (2.1) | 55 (3.9) | 36 (3.7) |
| Latvia | 11 (3.0) | 42 (4.7) | 46 (5.0) |  | 28 (3.4) | 59 (4.0) | 13 (2.9) |
| Lebanon | 24 (3.9) | 37 (4.6) | 39 (4.0) |  | 38 (4.2) | 34 (4.2) | 28 (3.7) |
| Lithuania | 5 (2.1) | 35 (4.1) | 60 (4.3) |  | 53 (4.6) | 45 (4.6) | 2 (1.2) |
| Macedonia, Rep. of | 26 (4.1) | 54 (4.0) | 20 (3.3) |  | 41 (4.3) | 44 (3.6) | 15 (3.2) |
| Malaysia | 49 (4.3) | 43 (4.3) | 8 (2.0) |  | 55 (4.2) | 40 (4.1) | 5 (2.0) |
| Moldova, Rep. of | 40 (4.9) | 46 (4.9) | 14 (3.5) | $r$ | 50 (5.1) | 42 (4.8) | 8 (2.7) |
| Morocco | 12 (3.7) | 24 (5.1) | 64 (5.1) | s | 2 (1.8) | 32 (5.3) | 66 (5.6) |
| Netherlands | 2 (1.2) | 43 (4.5) | 56 (4.6) |  | 23 (4.1) | 52 (5.0) | 25 (4.2) |
| New Zealand | 41 (5.3) | 53 (5.3) | 5 (2.4) |  | 47 (5.8) | 48 (6.2) | 5 (2.1) |
| Norway | 10 (2.5) | 43 (5.2) | 47 (5.1) |  | 10 (2.8) | 36 (4.5) | 54 (4.6) |
| Palestinian Nat'l Auth. | 56 (4.4) | 33 (3.7) | 11 (2.9) |  | 58 (4.3) | 32 (4.3) | 10 (2.5) |
| Philippines | 58 (3.9) | 38 (4.1) | 4 (1.7) |  | 70 (3.7) | 26 (3.4) | 4 (1.9) |
| Romania | 61 (4.1) | 25 (3.6) | 14 (3.1) |  | 78 (3.4) | 17 (3.0) | 5 (2.0) |
| Russian Federation | 16 (2.9) | 63 (3.5) | 22 (4.9) |  | 17 (2.7) | 60 (4.6) | 24 (4.3) |
| Saudi Arabia | 20 (4.2) | 27 (4.0) | 54 (5.4) |  | 37 (5.2) | 28 (4.2) | 35 (5.4) |
| Scotland | s $\quad 33$ (5.8) | 60 (5.7) | 7 (3.0) | s | 55 (5.6) | 42 (5.4) | 3 (2.0) |
| Serbia | 13 (2.8) | 33 (3.7) | 54 (4.0) |  | 46 (4.4) | 38 (4.2) | 17 (3.2) |
| Singapore | 56 (0.0) | 42 (0.0) | 2 (0.0) |  | 67 (0.0) | 31 (0.0) | 2 (0.0) |
| Slovak Republic | 13 (3.1) | 38 (4.8) | 49 (4.4) |  | 7 (2.0) | 27 (3.9) | 65 (4.0) |
| Slovenia | 58 (4.3) | 38 (4.1) | 4 (1.7) |  | 39 (4.5) | 58 (4.4) | 3 (1.3) |
| South Africa | 55 (3.6) | 27 (3.4) | 18 (2.4) |  | 49 (3.2) | 33 (3.2) | 18 (3.0) |
| Sweden | 11 (2.6) | 41 (4.4) | 49 (4.6) |  | 17 (3.1) | 52 (4.0) | 30 (4.1) |
| Tunisia | 27 (3.6) | 26 (3.5) | 47 (4.1) |  | 31 (4.1) | 33 (4.4) | 37 (4.2) |
| United States | 63 (3.6) | 34 (3.5) | 4 (1.4) |  | 72 (3.0) | 25 (3.0) | 3 (1.4) |
| \# England | 68 (6.0) | 27 (5.9) | 4 (2.1) | 5 | 46 (7.6) | 48 (7.4) | 6 (3.0) |
| International Avg. | 31 (0.5) | 40 (0.6) | 29 (0.5) |  | 42 (0.6) | 39 (0.6) | 20 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Basque Country, Spain | 20 (4.4) | 23 (4.4) | 57 (5.4) |  | 49 (5.1) | 26 (5.0) | 25 (4.6) |
| Indiana State, US | 64 (5.5) | 31 (5.7) | 5 (3.1) |  | 67 (6.7) | 32 (6.7) | 1 (0.0) |
| Ontario Province, Can. | 31 (4.6) | 58 (4.8) | 11 (2.8) |  | 40 (4.8) | 53 (4.9) | 8 (2.6) |
| Quebec Province, Can. | 15 (3.5) | 51 (4.8) | 34 (4.3) |  | 24 (4.5) | 45 (5.1) | 30 (4.6) |

Background data provided by schools.
き Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science (Continued...)


| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Improving the Content Knowledge |  |  | Improving Teaching Skills |  |  |  |
|  | 3 Times or More a Year | $\begin{aligned} & \text { 1-2 Times } \\ & \text { a Year } \end{aligned}$ | Never |  | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | 32 (4.4) | 35 (4.8) | 34 (4.3) | r | 33 (4.3) | 37 (4.6) | 30 (4.4) |
| Australia | 40 (4.6) | 48 (4.6) | 12 (3.6) |  | 50 (4.5) | 47 (4.2) | 3 (1.4) |
| Bahrain | 67 (0.2) | 26 (0.1) | 7 (0.1) |  | 87 (0.2) | 7 (0.0) | 6 (0.2) |
| Belgium (Flemish) | 16 (3.5) | 66 (4.1) | 18 (3.1) |  | 14 (3.1) | 60 (4.3) | 26 (4.1) |
| Botswana | 32 (4.2) | 36 (4.9) | 33 (4.3) |  | 40 (4.6) | 36 (4.3) | 25 (3.4) |
| Bulgaria | 41 (4.5) | 39 (4.0) | 20 (3.6) |  | 42 (4.7) | 42 (4.1) | 17 (3.0) |
| Chile | 38 (4.0) | 49 (4.3) | 12 (2.5) |  | 46 (4.3) | 45 (4.6) | 9 (2.2) |
| Chinese Taipei | 61 (4.2) | 36 (4.1) | 3 (1.4) |  | 55 (4.1) | 43 (3.9) | 2 (1.1) |
| Cyprus | 32 (0.3) | 59 (0.3) | 10 (0.2) |  | 41 (0.3) | 58 (0.3) | 1 (0.0) |
| Egypt | 94 (2.0) | 5 (1.8) | 2 (0.9) |  | 95 (1.7) | 3 (1.4) | 1 (1.0) |
| Estonia | 56 (3.9) | 43 (3.8) | 1 (0.8) |  | 35 (4.5) | 61 (4.4) | 4 (1.8) |
| Ghana | 49 (4.6) | 29 (4.1) | 21 (3.8) |  | 48 (4.5) | 35 (4.6) | 17 (3.0) |
| Hong Kong, SAR | 55 (4.9) | 43 (5.0) | 2 (1.1) |  | 51 (4.8) | 46 (4.7) | 3 (1.3) |
| Hungary | 55 (3.8) | 38 (4.0) | 8 (2.3) |  | 66 (3.6) | 27 (3.9) | 7 (2.0) |
| Indonesia | 42 (4.2) | 47 (4.3) | 11 (2.8) |  | 43 (4.1) | 47 (4.1) | 10 (2.9) |
| Iran, Islamic Rep. of | 34 (3.6) | 49 (3.7) | 17 (3.0) |  | 25 (3.5) | 57 (4.1) | 18 (3.2) |
| Israel | 87 (2.9) | 12 (2.8) | 1 (1.0) |  | 83 (3.4) | 13 (2.9) | 4 (1.7) |
| Italy | 26 (3.4) | 33 (3.8) | 41 (3.9) |  | 39 (3.9) | 33 (3.8) | 28 (3.4) |
| Japan | 44 (3.8) | 49 (4.1) | 7 (2.2) |  | 42 (3.7) | 49 (4.1) | 9 (2.1) |
| Jordan | 51 (4.3) | 40 (4.1) | 9 (2.7) |  | 49 (3.9) | 41 (4.1) | 10 (2.5) |
| Korea, Rep. of | 18 (3.3) | 75 (3.7) | 6 (2.0) |  | 21 (3.0) | 68 (3.9) | 11 (2.8) |
| Latvia | 40 (4.4) | 58 (4.4) | 2 (1.3) |  | 44 (4.6) | 54 (4.4) | 3 (1.6) |
| Lebanon | 39 (4.3) | 33 (4.3) | 28 (3.4) |  | 47 (4.4) | 30 (4.2) | 24 (3.7) |
| Lithuania | 59 (5.0) | 41 (5.1) | 1 (0.6) |  | 61 (4.6) | 39 (4.6) | 0 (0.0) |
| Macedonia, Rep. of | 32 (3.7) | 56 (3.9) | 12 (3.0) |  | 28 (3.8) | 55 (4.1) | 17 (3.3) |
| Malaysia | 68 (3.6) | 32 (3.7) | 1 (0.8) |  | 62 (4.3) | 36 (4.3) | 2 (1.2) |
| Moldova, Rep. of | 61 (4.9) | 37 (4.9) | 2 (1.1) | $r$ | 78 (4.5) | 20 (4.2) | 3 (1.5) |
| Morocco | $\mathrm{s} \quad 12$ (3.2) | 33 (5.3) | 55 (5.6) | 5 | 23 (4.4) | 43 (5.0) | 35 (4.5) |
| Netherlands | 9 (2.7) | 70 (4.3) | 21 (4.2) |  | 18 (3.7) | 54 (5.5) | 28 (4.8) |
| New Zealand | 36 (5.6) | 60 (5.7) | 4 (1.3) |  | 35 (4.8) | 56 (4.8) | 8 (3.0) |
| Norway | 15 (3.4) | 68 (4.1) | 17 (3.1) |  | 9 (2.5) | 58 (4.5) | 33 (4.3) |
| Palestinian Nat'l Auth. | 62 (4.5) | 34 (4.2) | 5 (1.9) |  | 67 (4.1) | 26 (3.5) | 6 (2.4) |
| Philippines | 73 (3.7) | 24 (3.6) | 3 (1.6) |  | 85 (3.1) | 14 (3.0) | 1 (0.9) |
| Romania | 83 (3.2) | 14 (2.9) | 4 (1.7) |  | 86 (3.2) | 13 (2.9) | 2 (1.3) |
| Russian Federation | 44 (3.4) | 50 (3.4) | 7 (1.8) |  | 43 (3.5) | 51 (3.6) | 6 (1.9) |
| Saudi Arabia | 41 (5.4) | 30 (4.3) | 30 (5.3) |  | 39 (5.5) | 38 (5.0) | 22 (5.1) |
| Scotland | $5 \quad 41$ (4.9) | 50 (4.9) | 9 (3.3) | s | 35 (4.7) | 59 (5.3) | 6 (2.9) |
| Serbia | 45 (3.8) | 49 (3.7) | 6 (2.0) |  | 37 (3.6) | 51 (3.9) | 13 (3.2) |
| Singapore | 59 (0.0) | 40 (0.0) | 0 (0.0) |  | 68 (0.0) | 32 (0.0) | 0 (0.0) |
| Slovak Republic | 46 (4.4) | 42 (4.3) | 12 (2.9) |  | 44 (4.0) | 49 (3.9) | 7 (2.0) |
| Slovenia | 40 (4.8) | 53 (5.0) | 7 (2.5) |  | 36 (4.2) | 53 (4.3) | 11 (2.5) |
| South Africa | 60 (3.2) | 29 (3.3) | 12 (2.3) |  | 63 (3.0) | 24 (3.1) | 13 (2.2) |
| Sweden | 16 (2.9) | 62 (4.0) | 22 (3.6) |  | 15 (3.2) | 47 (4.4) | 38 (3.6) |
| Tunisia | 59 (4.0) | 25 (3.4) | 16 (2.7) |  | 62 (4.5) | 23 (3.7) | 15 (3.1) |
| United States | 56 (3.3) | 37 (3.4) | 7 (1.8) |  | 59 (3.4) | 36 (3.5) | 6 (1.6) |
| \# England | s $\quad 55$ (7.2) | 36 (6.8) | 9 (4.0) | 5 | 68 (6.5) | 30 (6.3) | 2 (0.1) |
| International Avg. | 46 (0.6) | 42 (0.6) | 12 (0.4) |  | 48 (0.6) | 40 (0.6) | 12 (0.4) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Basque Country, Spain | 33 (4.9) | 37 (4.7) | 30 (5.0) |  | 41 (5.1) | 42 (5.1) | 17 (4.1) |
| Indiana State, US | 50 (6.0) | 41 (5.9) | 9 (4.2) |  | 47 (6.6) | 46 (6.4) | 7 (3.5) |
| Ontario Province, Can. | 23 (4.2) | 62 (4.6) | 15 (3.7) |  | 29 (4.0) | 58 (4.6) | 13 (3.5) |
| Quebec Province, Can. | 14 (3.6) | 45 (5.0) | 41 (5.0) |  | 21 (4.6) | 58 (4.4) | 21 (3.6) |

Background data provided by schools.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science (...Continued)

| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |
| :---: | :---: | :---: | :---: |
|  | Using Information and Communication Technology for Educational Purposes |  |  |
|  | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | 23 (4.0) | 31 (4.9) | 46 (4.9) |
| Australia | 46 (3.9) | 50 (3.5) | 4 (1.7) |
| Bahrain | 44 (0.2) | 35 (0.2) | 22 (0.2) |
| Belgium (Flemish) | 29 (4.0) | 64 (4.3) | 7 (2.3) |
| Botswana | 23 (3.8) | 21 (4.2) | 56 (5.1) |
| Bulgaria | 18 (3.9) | 30 (4.2) | 52 (4.5) |
| Chile | 47 (3.9) | 40 (3.6) | 13 (2.7) |
| Chinese Taipei | 46 (4.2) | 50 (4.3) | 4 (1.7) |
| Cyprus | 30 (0.3) | 45 (0.3) | 24 (0.2) |
| Egypt | 85 (2.8) | 9 (2.3) | 6 (2.1) |
| Estonia | 25 (3.5) | 62 (4.0) | 12 (2.5) |
| Ghana | 15 (3.9) | 15 (3.2) | 70 (4.1) |
| Hong Kong, SAR | 69 (4.3) | 29 (4.1) | 2 (1.3) |
| Hungary | 38 (4.0) | 42 (4.3) | 20 (3.2) |
| Indonesia | 14 (3.0) | 33 (3.7) | 52 (4.1) |
| Iran, Islamic Rep. of | 21 (3.2) | 35 (3.6) | 44 (4.0) |
| Israel | 51 (4.5) | 29 (4.3) | 20 (3.5) |
| Italy | 52 (4.2) | 37 (3.7) | 12 (2.8) |
| Japan | 25 (3.3) | 38 (3.9) | 37 (3.8) |
| Jordan | 29 (4.6) | 31 (3.7) | 39 (4.5) |
| Korea, Rep. of | 30 (3.5) | 65 (3.7) | 5 (1.9) |
| Latvia | 31 (4.2) | 58 (4.7) | 11 (2.7) |
| Lebanon | 34 (4.0) | 29 (4.2) | 38 (3.5) |
| Lithuania | 34 (4.1) | 64 (4.3) | 2 (1.3) |
| Macedonia, Rep. of | 20 (3.8) | 45 (4.3) | 36 (4.3) |
| Malaysia | 28 (3.8) | 41 (4.1) | 31 (3.7) |
| Moldova, Rep. of | 53 (4.6) | 32 (4.2) | 15 (3.8) |
| Morocco | $\mathrm{s} \quad 8$ (2.2) | 23 (5.0) | 69 (5.5) |
| Netherlands | 14 (3.6) | 50 (4.9) | 36 (4.6) |
| New Zealand | 38 (5.8) | 54 (5.8) | 8 (2.8) |
| Norway | 41 (4.3) | 49 (4.4) | 10 (2.7) |
| Palestinian Nat'l Auth. | 35 (3.9) | 32 (3.9) | 33 (4.0) |
| Philippines | 55 (4.4) | 32 (4.5) | 13 (3.2) |
| Romania | 50 (4.2) | 23 (3.7) | 27 (4.1) |
| Russian Federation | 18 (2.6) | 41 (4.5) | 42 (4.0) |
| Saudi Arabia | 29 (5.5) | 23 (3.6) | 48 (5.6) |
| Scotland | s 60 (5.9) | 38 (5.8) | 2 (1.2) |
| Serbia | 32 (4.0) | 45 (4.1) | 22 (3.2) |
| Singapore | 77 (0.0) | 23 (0.0) | 0 (0.0) |
| Slovak Republic | 40 (4.5) | 41 (4.8) | 19 (3.1) |
| Slovenia | 26 (4.1) | 57 (4.8) | 17 (3.1) |
| South Africa | 38 (3.0) | 25 (3.4) | 37 (3.4) |
| Sweden | 13 (3.0) | 46 (4.4) | 42 (4.3) |
| Tunisia | 29 (3.9) | 32 (3.7) | 40 (3.7) |
| United States | 52 (3.4) | 37 (3.5) | 11 (2.2) |
| \# England | s $\quad 59$ (6.7) | 37 (6.4) | 4 (2.5) |
| International Avg. | 36 (0.6) | 38 (0.6) | 25 (0.5) |
| Benchmarking Participants |  |  |  |
| Basque Country, Spain | 50 (4.6) | 37 (4.5) | 13 (3.4) |
| Indiana State, US | 33 (6.6) | 57 (7.1) | 10 (4.1) |
| Ontario Province, Can. | 31 (4.5) | 56 (4.5) | 13 (3.4) |
| Quebec Province, Can. | 14 (3.3) | 47 (5.0) | 39 (4.8) |

Background data provided by schools.
ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science (Continued...)

| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Supporting the Implementation of the National or Regional Curriculum |  |  |  | Designing or Supporting the School's Own Improvement Goals |  |  |  |
|  |  | 3 Times or More a Year | 1-2 Times a Year | Never |  | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | r | 4 (1.9) | 22 (4.2) | 75 (4.0) | 5 | 19 (3.9) | 36 (4.8) | 46 (5.1) |
| Australia |  | 43 (4.3) | 34 (4.2) | 23 (3.9) |  | 46 (4.3) | 38 (4.4) | 16 (2.7) |
| Belgium (Flemish) |  | 28 (3.6) | 47 (4.3) | 25 (3.9) |  | 33 (3.8) | 43 (4.0) | 25 (3.9) |
| Chinese Taipei |  | 3 (1.4) | 30 (3.7) | 67 (3.8) |  | 25 (3.8) | 61 (4.1) | 14 (2.7) |
| Cyprus |  | 21 (3.4) | 68 (3.8) | 12 (2.9) |  | 20 (4.2) | 61 (4.8) | 19 (4.0) |
| England | $r$ | 61 (5.5) | 33 (5.5) | 5 (2.6) | $r$ | 50 (5.4) | 45 (5.6) | 5 (2.5) |
| Hong Kong, SAR |  | 46 (5.2) | 48 (4.8) | 5 (2.0) |  | 43 (4.7) | 50 (5.2) | 7 (2.9) |
| Hungary |  | 13 (2.6) | 24 (4.2) | 64 (4.0) |  | 69 (4.0) | 29 (3.9) | 2 (1.2) |
| Iran, Islamic Rep. of |  | 14 (3.7) | 38 (4.2) | 48 (4.7) |  | 29 (4.7) | 33 (4.5) | 38 (4.8) |
| Italy |  | 24 (3.3) | 25 (3.4) | 51 (3.7) |  | 35 (3.7) | 29 (3.5) | 36 (3.4) |
| Japan |  | 7 (2.2) | 27 (3.6) | 66 (3.7) |  | 24 (3.3) | 46 (3.4) | 30 (3.7) |
| Latvia | $r$ | 9 (2.8) | 36 (4.7) | 55 (4.9) | $r$ | 20 (3.6) | 59 (4.1) | 21 (3.4) |
| Lithuania | $r$ | 3 (1.5) | 16 (3.1) | 81 (3.1) |  | 31 (4.7) | 61 (4.4) | 7 (2.8) |
| Moldova, Rep. of | r | 27 (4.7) | 50 (5.4) | 23 (4.3) | $r$ | 41 (4.8) | 42 (4.2) | 17 (3.5) |
| Morocco | r | 6 (1.8) | 16 (3.0) | 78 (3.3) | $r$ | 9 (3.2) | 19 (3.3) | 72 (4.0) |
| Netherlands |  | 7 (2.6) | 18 (3.3) | 75 (4.0) |  | 52 (4.8) | 34 (4.6) | 14 (3.6) |
| New Zealand |  | 45 (3.2) | 35 (3.6) | 20 (3.0) |  | 47 (3.8) | 45 (4.0) | 8 (1.9) |
| Norway |  | 16 (3.6) | 44 (4.6) | 40 (4.3) |  | 20 (4.3) | 30 (4.3) | 50 (4.6) |
| Philippines |  | 53 (4.3) | 37 (4.2) | 10 (2.4) |  | 72 (3.9) | 25 (3.9) | 3 (1.2) |
| Russian Federation |  | 19 (3.2) | 56 (3.7) | 25 (3.8) |  | 13 (2.2) | 56 (3.3) | 30 (3.6) |
| Scotland |  | 38 (5.2) | 58 (5.2) | 4 (1.9) |  | 38 (4.7) | 55 (5.2) | 6 (2.2) |
| Singapore |  | 57 (4.3) | 39 (4.1) | 3 (1.5) |  | 72 (3.6) | 27 (3.6) | 1 (0.6) |
| Slovenia |  | 57 (4.3) | 38 (4.3) | 5 (1.8) |  | 38 (4.7) | 55 (4.5) | 7 (2.4) |
| Tunisia | $r$ | 29 (4.2) | 31 (4.3) | 39 (4.4) | $r$ | 37 (4.2) | 45 (4.7) | 18 (3.4) |
| United States |  | 50 (3.6) | 40 (3.5) | 9 (2.0) |  | 61 (3.3) | 31 (3.1) | 8 (1.9) |
| International Avg. |  | 27 (0.7) | 36 (0.8) | 36 (0.7) |  | 38 (0.8) | 42 (0.9) | 20 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 52 (7.1) | 42 (7.0) | 6 (3.2) |  | 48 (7.7) | 41 (6.6) | 11 (4.6) |
| Ontario Province, Can. |  | 29 (4.6) | 56 (5.0) | 15 (3.5) |  | 42 (5.0) | 44 (4.9) | 14 (3.3) |
| Quebec Province, Can. |  | 25 (4.4) | 55 (5.0) | 20 (3.9) |  | 24 (4.3) | 47 (5.0) | 29 (4.5) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science (...Continued)


| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Improving the Content Knowledge |  |  | Improving Teaching Skills |  |  |
|  | 3 Times or More a Year | 1-2 Times a Year | Never | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | r 28 (4.3) | 35 (4.9) | 37 (4.6) | 29 (4.1) | 33 (4.6) | 38 (4.8) |
| Australia | 40 (4.7) | 37 (4.6) | 23 (2.8) | 44 (4.8) | 42 (5.1) | 14 (3.0) |
| Belgium (Flemish) | 25 (4.0) | 57 (4.3) | 18 (3.4) | 22 (3.3) | 49 (4.4) | 29 (3.6) |
| Chinese Taipei | 47 (4.0) | 47 (4.1) | 6 (2.1) | 53 (4.3) | 43 (4.4) | 4 (1.7) |
| Cyprus | 16 (3.9) | 57 (5.1) | 28 (4.5) | 27 (4.2) | 62 (5.3) | 11 (3.5) |
| England | 49 (5.6) | 45 (5.7) | 5 (2.4) | 59 (5.8) | 36 (5.7) | 6 (2.5) |
| Hong Kong, SAR | 53 (5.4) | 45 (5.4) | 3 (1.5) | 56 (5.2) | 42 (5.4) | 2 (1.3) |
| Hungary | 56 (3.7) | 36 (3.7) | 8 (2.1) | 68 (3.8) | 26 (3.7) | 6 (1.8) |
| Iran, Islamic Rep. of | 22 (3.9) | 48 (4.2) | 29 (3.8) | 26 (4.4) | 50 (4.7) | 23 (3.5) |
| Italy | 26 (3.4) | 31 (4.1) | 43 (4.1) | 35 (3.6) | 33 (3.7) | 32 (3.6) |
| Japan | 44 (4.2) | 47 (4.1) | 9 (2.2) | 49 (4.2) | 46 (4.1) | 5 (1.8) |
| Latvia | 28 (4.2) | 58 (4.4) | 15 (3.2) | 35 (4.6) | 55 (4.5) | 9 (2.6) |
| Lithuania | 40 (4.4) | 56 (4.5) | 4 (1.6) | 46 (4.2) | 50 (4.1) | 5 (1.9) |
| Moldova, Rep. of | 62 (4.8) | 34 (4.9) | 4 (1.9) | 72 (5.0) | 22 (4.5) | 7 (2.6) |
| Morocco | 15 (3.8) | 27 (3.9) | 58 (4.5) | 16 (3.8) | 31 (5.1) | 53 (5.2) |
| Netherlands | 30 (5.2) | 37 (4.8) | 33 (5.0) | 38 (4.7) | 37 (4.4) | 26 (4.5) |
| New Zealand | 48 (3.6) | 40 (3.7) | 13 (2.5) | 54 (3.5) | 33 (3.5) | 12 (2.7) |
| Norway | 19 (3.5) | 53 (4.3) | 27 (4.6) | 12 (3.1) | 41 (4.4) | 46 (4.9) |
| Philippines | 74 (4.0) | 23 (3.9) | 2 (1.2) | 80 (3.5) | 20 (3.4) | 0 (0.2) |
| Russian Federation | 32 (3.9) | 47 (4.3) | 20 (3.2) | 42 (3.5) | 46 (4.0) | 12 (2.7) |
| Scotland | 30 (5.2) | 54 (5.8) | 16 (3.6) | 32 (5.2) | 49 (5.8) | 19 (3.9) |
| Singapore | 67 (3.7) | 33 (3.7) | 0 (0.0) | 78 (3.0) | 21 (3.0) | 0 (0.3) |
| Slovenia | 32 (4.3) | 56 (4.7) | 13 (2.9) | 35 (4.6) | 59 (4.4) | 6 (1.7) |
| Tunisia | 49 (4.7) | 38 (4.7) | 13 (2.7) | 56 (4.2) | 35 (4.2) | 9 (2.6) |
| United States | 49 (3.3) | 43 (3.2) | 8 (1.7) | 58 (3.9) | 36 (3.6) | 6 (1.6) |
| International Avg. | 39 (0.9) | 43 (0.9) | 17 (0.6) | 45 (0.8) | 40 (0.9) | 15 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US | 43 (6.9) | 41 (7.3) | 16 (5.6) | 51 (6.8) | 43 (5.9) | 7 (3.4) |
| Ontario Province, Can. | 30 (4.6) | 49 (4.9) | 21 (3.3) | 28 (4.3) | 56 (4.7) | 15 (3.4) |
| Quebec Province, Can. | 20 (4.3) | 61 (5.1) | 19 (3.5) | 21 (4.2) | 50 (4.4) | 30 (4.2) |

Exhibit 6.6: Professional Development Opportunities for Teachers in Mathematics and Science

| Countries | Percentage of Students by Their School's Report of Teachers' Involvement in Professional Development Opportunities in Mathematics and Science |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Using Information and Communication Technology for Educational Purposes |  |  |  |
|  |  | 3 Times or More a Year | 1-2 Times a Year | Never |
| Armenia | $r$ | 19 (3.5) | 29 (4.8) | 52 (5.0) |
| Australia |  | 48 (4.4) | 39 (4.5) | 13 (2.8) |
| Belgium (Flemish) |  | 35 (4.4) | 47 (4.6) | 18 (3.3) |
| Chinese Taipei |  | 46 (4.1) | 51 (4.1) | 4 (1.6) |
| Cyprus |  | 26 (4.6) | 52 (4.5) | 21 (3.9) |
| England | $r$ | 60 (5.6) | 36 (5.2) | 4 (2.1) |
| Hong Kong, SAR |  | 75 (3.8) | 23 (3.8) | 1 (0.9) |
| Hungary |  | 37 (4.6) | 44 (4.5) | 18 (3.1) |
| Iran, Islamic Rep. of |  | 20 (3.4) | 33 (5.1) | 47 (5.1) |
| Italy |  | 47 (3.9) | 30 (3.7) | 24 (3.5) |
| Japan |  | 23 (3.5) | 37 (4.0) | 39 (4.1) |
| Latvia |  | 22 (4.0) | 47 (4.8) | 31 (4.2) |
| Lithuania |  | 19 (3.6) | 65 (4.5) | 16 (3.0) |
| Moldova, Rep. of | $r$ | 60 (5.1) | 19 (4.0) | 21 (3.9) |
| Morocco | $r$ | 7 (2.4) | 13 (3.7) | 79 (4.0) |
| Netherlands |  | 46 (5.2) | 33 (4.6) | 20 (4.2) |
| New Zealand |  | 58 (3.3) | 35 (3.0) | 8 (2.1) |
| Norway |  | 41 (4.2) | 39 (4.6) | 20 (4.1) |
| Philippines |  | 50 (5.0) | 31 (4.5) | 19 (3.6) |
| Russian Federation |  | 5 (1.4) | 22 (2.4) | 74 (2.6) |
| Scotland |  | 54 (5.2) | 39 (5.0) | 7 (2.9) |
| Singapore |  | 82 (3.0) | 18 (2.9) | 0 (0.3) |
| Slovenia |  | 20 (3.5) | 65 (4.2) | 15 (3.5) |
| Tunisia | $r$ | 3 (1.5) | 5 (2.1) | 92 (2.6) |
| United States |  | 46 (3.6) | 42 (3.3) | 11 (2.1) |
| International Avg. |  | 38 (0.8) | 36 (0.8) | 26 (0.7) |
| Benchmarking Participants |  |  |  |  |
| Indiana State, US |  | 41 (6.0) | 46 (6.1) | 12 (4.8) |
| Ontario Province, Can. |  | 30 (4.6) | 51 (4.8) | 19 (4.2) |
| Quebec Province, Can. |  | 16 (3.6) | 48 (4.5) | 36 (4.1) |


| Countries | Percentage of Students by Their Teachers' Participation in Professional Development in Mathematics in the Past Two Years |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mathematics Content |  | Mathematics Pedagogy/ Instruction |  | Mathematics Curriculum |  | Integrating Information Technology into Mathematics |  | Improving <br> Students' Critical Thinking or Problem Solving Skills |  | Mathematics Assessment |
| Armenia | 12 (2.4) | r | 29 (3.3) | r | 28 (3.0) | r | 15 (3.1) | r | 30 (4.1) | r | 40 (4.6) |
| Australia | 68 (3.7) |  | 56 (4.0) |  | 71 (3.7) |  | 70 (4.0) |  | 47 (4.8) |  | 57 (4.4) |
| Bahrain | 24 (2.6) |  | 37 (3.4) |  | 19 (2.3) |  | 31 (3.7) |  | 41 (4.0) |  | 42 (3.7) |
| Belgium (Flemish) | 53 (3.6) |  | 40 (3.6) |  | 42 (3.8) |  | 76 (3.2) |  | 24 (3.2) |  | 20 (3.4) |
| Botswana | 39 (4.0) |  | 24 (4.6) |  | 18 (3.8) |  | 17 (3.6) |  | 50 (5.2) |  | 40 (4.7) |
| Bulgaria | 19 (3.5) | $r$ | 9 (2.7) | $r$ | 20 (3.7) | $r$ | 13 (3.7) | $r$ | 9 (2.7) | $r$ | 10 (2.7) |
| Chile | 78 (3.2) |  | 75 (3.4) |  | 50 (4.1) |  | 50 (3.8) |  | 54 (3.9) |  | 54 (3.7) |
| Chinese Taipei | 86 (3.1) |  | 89 (2.3) |  | 85 (2.8) |  | 81 (3.2) |  | 47 (4.1) |  | 69 (4.0) |
| Cyprus | 71 (2.1) |  | 65 (2.9) |  | 74 (2.6) |  | 64 (2.7) |  | 45 (3.5) |  | 50 (3.1) |
| Egypt | 28 (3.8) |  | 49 (4.1) |  | 28 (3.5) |  | 48 (4.2) |  | 80 (3.3) |  | 60 (4.3) |
| Estonia | 63 (4.1) |  | 74 (3.6) |  | 74 (3.7) |  | 70 (3.7) |  | 49 (3.9) |  | 50 (4.1) |
| Ghana | 50 (4.3) |  | 40 (4.4) |  | 41 (4.4) |  | 20 (3.8) |  | 52 (4.4) |  | 57 (4.0) |
| Hong Kong, SAR | 61 (3.9) |  | 64 (4.1) |  | 62 (4.2) |  | 79 (3.7) |  | 46 (4.0) |  | 42 (4.5) |
| Hungary | 49 (4.2) |  | 44 (3.6) |  | 48 (3.6) |  | 17 (3.0) |  | 26 (3.3) |  | 29 (3.8) |
| Indonesia | 57 (4.3) |  | 64 (4.1) |  | 59 (4.2) |  | 21 (3.1) |  | 49 (4.3) |  | 48 (4.3) |
| Iran, Islamic Rep. of | 53 (3.6) |  | 58 (3.3) |  | 40 (3.8) |  | 22 (3.6) |  | 38 (4.4) |  | 41 (4.2) |
| Israel | 63 (3.7) |  | 68 (3.4) |  | 63 (4.0) |  | 50 (3.9) |  | 52 (3.8) |  | 48 (4.0) |
| Italy | 22 (3.1) |  | 28 (3.3) |  | 15 (2.7) |  | 52 (3.8) |  | 13 (2.3) |  | 20 (3.1) |
| Japan | 63 (3.9) |  | 71 (3.7) |  | 41 (4.0) |  | 27 (4.2) |  | 30 (4.1) |  | 57 (4.3) |
| Jordan | 48 (4.2) |  | 69 (4.0) |  | 45 (4.5) |  | 35 (4.1) |  | 58 (4.3) |  | 47 (5.1) |
| Korea, Rep. of | s 32 (3.4) | 5 | 36 (3.3) | 5 | 29 (3.4) | 5 | 43 (3.5) | s | 12 (2.1) | 5 | 21 (2.7) |
| Latvia | 80 (3.5) |  | 72 (3.9) |  | 83 (3.0) |  | 48 (4.4) |  | 65 (4.1) |  | 72 (4.1) |
| Lebanon | 60 (4.6) |  | 61 (4.6) |  | 59 (4.2) |  | 39 (4.0) |  | 62 (4.4) |  | 73 (3.8) |
| Lithuania | 86 (2.7) |  | 76 (3.1) |  | 67 (3.8) |  | 63 (3.7) |  | 43 (4.1) |  | 55 (4.0) |
| Macedonia, Rep. of | 64 (4.3) |  | 67 (4.0) |  | 63 (3.7) |  | 16 (3.0) |  | 41 (3.9) |  | 42 (4.3) |
| Malaysia | 69 (3.9) |  | 64 (4.3) |  | 65 (3.9) |  | 48 (4.4) |  | 72 (3.8) |  | 29 (3.7) |
| Moldova, Rep. of | 41 (5.0) | $r$ | 45 (5.0) | $r$ | 49 (5.0) | $r$ | 50 (4.8) | $r$ | 75 (4.2) | $r$ | 75 (4.2) |
| Morocco | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | s | 16 (4.9) | s | 48 (6.5) |  | $\mathrm{x} \times$ |
| Netherlands | 38 (4.5) |  | 43 (4.6) |  | 15 (3.2) |  | 42 (4.9) |  | 29 (4.0) |  | 11 (3.0) |
| New Zealand | 82 (2.9) |  | 61 (3.9) |  | 78 (3.4) |  | 53 (5.4) |  | 52 (4.0) |  | 79 (4.0) |
| Norway | 28 (4.1) |  | 33 (4.2) |  | 16 (3.3) |  | 30 (4.2) |  | 15 (3.2) |  | 27 (3.8) |
| Palestinian Nat'l Auth. | 84 (3.1) |  | 79 (3.6) |  | 78 (3.6) |  | 33 (4.6) |  | 59 (4.7) |  | 63 (4.2) |
| Philippines | 82 (3.3) |  | 68 (4.1) |  | 77 (3.5) |  | 44 (4.5) |  | 67 (4.1) |  | 61 (4.7) |
| Romania | 71 (4.0) |  | 68 (3.8) |  | 65 (4.3) |  | 33 (3.7) |  | 54 (4.0) |  | 77 (4.0) |
| Russian Federation | 70 (4.0) |  | 64 (4.1) |  | 70 (3.8) |  | 52 (2.8) |  | 53 (4.4) |  | 55 (3.5) |
| Saudi Arabia | 43 (5.5) |  | 61 (5.7) |  | 38 (4.6) |  | 19 (4.5) |  | 49 (6.3) |  | 43 (4.7) |
| Scotland | 68 (4.5) |  | 77 (3.3) |  | 57 (4.6) |  | 83 (3.6) |  | 42 (5.1) |  | 40 (4.5) |
| Serbia | 66 (4.0) |  | 45 (4.3) |  | 60 (4.2) |  | 31 (3.4) |  | 41 (3.8) |  | 43 (4.1) |
| Singapore | 76 (2.3) |  | 78 (2.3) |  | 59 (2.4) |  | 88 (1.6) |  | 70 (2.4) |  | 58 (2.6) |
| Slovak Republic | 50 (4.4) |  | 41 (4.5) |  | 50 (3.8) |  | 34 (3.9) |  | 35 (4.5) |  | 36 (4.4) |
| Slovenia | 86 (2.8) |  | 88 (3.0) |  | 79 (3.0) |  | 46 (4.0) |  | 53 (4.0) |  | 69 (3.6) |
| South Africa | 61 (4.6) | r | 43 (4.0) | $r$ | 59 (3.7) | r | 34 (3.9) | $r$ | 58 (4.2) | $r$ | 77 (3.4) |
| Sweden | 44 (3.8) |  | 50 (3.6) |  | 35 (3.3) |  | 12 (2.7) |  | 35 (3.6) |  | 31 (3.4) |
| Tunisia | 26 (3.5) |  | 42 (3.9) |  | 22 (3.3) |  | 16 (3.0) |  | 46 (4.2) |  | 46 (4.3) |
| United States | 83 (2.5) |  | 75 (2.7) |  | 83 (2.5) |  | 74 (3.0) |  | 76 (2.4) |  | 74 (2.7) |
| \# England | 66 (5.8) | r | 83 (4.1) | $r$ | 78 (4.6) | $r$ | 63 (5.4) | r | 52 (6.1) | $r$ | 55 (5.4) |
| International Avg. | 57 (0.6) |  | 57 (0.6) |  | 52 (0.6) |  | 43 (0.6) |  | 47 (0.6) |  | 49 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 35 (5.1) |  | 44 (5.0) |  | 34 (4.6) |  | 53 (4.8) |  | 40 (4.7) |  | 35 (4.7) |
| Indiana State, US | 72 (6.2) | $r$ | 69 (6.0) | $r$ | 76 (5.2) | $r$ | 60 (6.3) | $r$ | 64 (6.6) | $r$ | 58 (5.4) |
| Ontario Province, Can. | 81 (4.0) |  | 74 (4.4) |  | 81 (3.5) |  | 48 (5.1) |  | 63 (4.5) |  | 67 (4.3) |
| Quebec Province, Can. | 36 (4.7) |  | 51 (4.6) |  | 43 (4.9) |  | 40 (4.4) |  | 42 (5.4) |  | 28 (4.1) |

Background data provided by teachers.
¥ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| Countries | Percentage of Students by Their Teachers' Participation in Professional Development in Mathematics in the Past Two Years |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mathematics Content |  | Mathematics Pedagogy/ Instruction |  | Mathematics Curriculum |  | Integrating Information Technology into Mathematics |  | Improving Students' Critical Thinking or Problem Solving Skills |  | Mathematics Assessment |
| Armenia | $r$ | 12 (2.7) | $r$ | 26 (3.7) | $r$ | 23 (3.4) | r | 9 (2.2) | $r$ | 38 (4.3) | r | 37 (3.7) |
| Australia |  | 63 (3.6) |  | 57 (3.5) |  | 58 (4.0) |  | 36 (4.3) |  | 57 (3.5) |  | 53 (4.2) |
| Belgium (Flemish) |  | 31 (3.5) |  | 21 (2.8) |  | 4 (1.3) |  | 12 (2.2) |  | 28 (3.4) |  | 18 (3.6) |
| Chinese Taipei |  | 57 (4.0) |  | 73 (3.7) |  | 61 (3.7) |  | 45 (3.5) |  | 37 (4.2) |  | 49 (4.0) |
| Cyprus |  | 73 (3.3) |  | 52 (3.5) |  | 34 (4.2) |  | 44 (3.8) |  | 49 (3.8) |  | 23 (3.9) |
| England | $r$ | 76 (3.6) | $r$ | 88 (2.7) | $r$ | 78 (4.1) | $r$ | 60 (4.3) | r | 72 (4.0) | $r$ | 51 (4.7) |
| Hong Kong, SAR |  | 55 (4.2) |  | 65 (4.3) |  | 55 (4.3) |  | 68 (4.8) |  | 49 (4.0) |  | 39 (4.4) |
| Hungary |  | 35 (4.0) |  | 37 (4.1) |  | 26 (4.0) |  | 9 (2.6) |  | 23 (3.8) |  | 20 (3.5) |
| Iran, Islamic Rep. of |  | 39 (4.8) |  | 41 (4.9) |  | 30 (4.9) |  | 12 (3.0) |  | 33 (4.1) |  | 33 (4.3) |
| Italy |  | 29 (3.4) |  | 30 (3.4) |  | 20 (3.1) |  | 37 (3.4) |  | 12 (2.1) |  | 10 (2.2) |
| Japan |  | 40 (3.9) |  | 43 (4.0) |  | 19 (3.2) |  | 16 (3.2) |  | 22 (3.8) |  | 30 (4.1) |
| Latvia |  | 49 (4.2) |  | 53 (4.2) |  | 53 (4.5) |  | 26 (3.8) |  | 68 (3.8) |  | 69 (3.7) |
| Lithuania |  | 40 (3.6) |  | 48 (4.0) |  | 38 (3.8) |  | 42 (3.5) |  | 57 (3.9) |  | 47 (3.6) |
| Moldova, Rep. of |  | 36 (4.3) |  | 42 (4.2) |  | 39 (4.3) |  | 40 (4.3) |  | 63 (4.5) |  | 66 (4.2) |
| Morocco |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |
| Netherlands |  | 19 (4.0) |  | 30 (4.3) |  | 10 (2.5) |  | 33 (4.7) |  | 27 (4.2) |  | 22 (3.2) |
| New Zealand |  | 64 (3.5) |  | 57 (3.3) |  | 58 (3.4) |  | 28 (3.1) |  | 59 (3.6) |  | 59 (3.5) |
| Norway |  | 18 (2.8) |  | 21 (3.1) |  | 8 (2.1) |  | 10 (2.0) |  | 12 (2.4) |  | 6 (1.6) |
| Philippines |  | 62 (4.6) |  | 53 (4.9) |  | 70 (4.4) |  | 51 (5.1) |  | 67 (4.6) |  | 56 (4.6) |
| Russian Federation |  | 56 (4.1) |  | 60 (4.0) |  | 67 (3.4) |  | 34 (3.7) |  | 57 (4.0) |  | 54 (3.9) |
| Scotland | $r$ | 42 (5.3) | $r$ | 47 (5.4) | s | 39 (4.6) | $r$ | 42 (5.8) | $r$ | 45 (5.2) | $r$ | 28 (4.7) |
| Singapore |  | 60 (3.7) |  | 68 (3.9) |  | 43 (4.3) |  | 56 (4.1) |  | 73 (3.6) |  | 47 (3.9) |
| Slovenia |  | 54 (4.2) |  | 41 (4.3) |  | 49 (4.1) |  | 25 (3.7) |  | 37 (4.4) |  | 53 (4.0) |
| Tunisia | $r$ | 21 (4.0) |  | 27 (4.0) | $r$ | 25 (3.7) | $r$ | 9 (2.7) |  | 51 (4.4) |  | 52 (4.5) |
| United States |  | 65 (2.9) |  | 54 (2.9) |  | 66 (2.8) |  | 41 (2.9) |  | 58 (2.9) |  | 54 (2.6) |
| International Avg. |  | 46 (0.8) |  | 47 (0.8) |  | 41 (0.8) |  | 33 (0.8) |  | 46 (0.8) |  | 41 (0.8) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 44 (5.5) |  | 40 (5.6) |  | 58 (5.3) |  | 34 (3.6) |  | 49 (5.6) |  | 36 (5.8) |
| Ontario Province, Can. |  | 62 (4.7) |  | 53 (5.1) |  | 59 (5.0) |  | 33 (4.2) |  | 54 (4.6) |  | 55 (4.7) |
| Quebec Province, Can. |  | 53 (4.5) |  | 57 (4.3) |  | 67 (4.4) |  | 26 (4.2) |  | 39 (4.2) |  | 39 (4.4) | some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.8: Types of Interactions Among Mathematics Teachers

| Countries | Percentage of Students by Their Teachers' Interactions with Other Teachers |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Discussion About How to Teach a Particular Concept |  |  | Working on Preparing Instructional Materials |  |  |
|  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |
| Armenia | 49 (4.3) | 43 (4.1) | 8 (2.3) | 34 (3.7) | 40 (3.5) | 26 (3.4) |
| Australia | 52 (4.1) | 38 (3.7) | 10 (2.5) | 51 (4.7) | 39 (4.2) | 10 (2.5) |
| Bahrain | 64 (3.7) | 31 (3.5) | 6 (1.4) | 51 (3.3) | 33 (3.4) | 16 (2.6) |
| Belgium (Flemish) | 45 (4.1) | 37 (3.9) | 17 (3.0) | 15 (2.7) | 44 (3.7) | 41 (3.9) |
| Botswana | 73 (3.9) | 25 (3.8) | 3 (1.5) | 65 (3.9) | 27 (3.5) | 8 (2.3) |
| Bulgaria | 46 (4.3) | 40 (4.2) | 14 (3.6) | 53 (4.7) | 29 (3.6) | 19 (3.6) |
| Chile | 42 (3.5) | 35 (3.3) | 24 (3.3) | 45 (3.8) | 27 (3.2) | 27 (3.7) |
| Chinese Taipei | 51 (4.0) | 42 (4.0) | 7 (1.8) | 16 (3.4) | 36 (3.7) | 48 (4.6) |
| Cyprus | 75 (2.3) | 24 (2.3) | 1 (0.4) | 63 (2.9) | 29 (2.7) | 8 (1.2) |
| Egypt | 84 (3.4) | 14 (3.1) | 2 (1.3) | 59 (3.9) | 37 (3.8) | 4 (1.8) |
| Estonia | 59 (4.5) | 34 (4.3) | 7 (2.1) | 52 (4.0) | 36 (4.0) | 12 (2.3) |
| Ghana | 37 (4.4) | 38 (4.7) | 25 (4.3) | 52 (4.8) | 26 (3.9) | 22 (3.7) |
| Hong Kong, SAR | 38 (4.5) | 51 (4.6) | 11 (3.0) | 20 (3.5) | 49 (4.1) | 31 (4.1) |
| Hungary | 48 (4.5) | 46 (4.5) | 5 (1.9) | 40 (4.1) | 41 (3.8) | 18 (3.2) |
| Indonesia | 58 (4.4) | 38 (4.3) | 4 (1.6) | 78 (3.4) | 17 (3.4) | 4 (1.7) |
| Iran, Islamic Rep. of | 39 (4.3) | 55 (4.3) | 6 (1.9) | 26 (3.9) | 56 (4.1) | 18 (3.2) |
| Israel | 51 (3.5) | 42 (3.6) | 8 (2.0) | 44 (4.0) | 46 (3.9) | 10 (1.9) |
| Italy | 33 (3.4) | 46 (3.8) | 21 (2.9) | 23 (3.1) | 44 (3.3) | 33 (3.4) |
| Japan | 34 (3.9) | 42 (4.4) | 24 (3.9) | 19 (3.3) | 37 (3.8) | 44 (4.4) |
| Jordan | 52 (4.3) | 38 (4.1) | 10 (2.5) | 33 (4.1) | 47 (5.1) | 20 (3.9) |
| Korea, Rep. of | s $\quad 18$ (2.4) | 49 (3.3) | 34 (3.4) | 35 (3.2) | 47 (3.2) | 18 (2.5) |
| Latvia | 47 (4.4) | 45 (4.3) | 8 (2.9) | 32 (4.4) | 55 (4.8) | 13 (3.1) |
| Lebanon | 40 (4.0) | 46 (4.6) | 14 (3.3) | 38 (4.6) | 32 (4.1) | 30 (4.2) |
| Lithuania | 41 (4.0) | 46 (3.8) | 13 (2.8) | 36 (3.9) | 50 (4.1) | 14 (2.9) |
| Macedonia, Rep. of | 56 (3.9) | 35 (3.9) | 8 (2.2) | 47 (4.3) | 42 (4.4) | 11 (2.7) |
| Malaysia | 58 (4.2) | 39 (4.4) | 2 (1.2) | 25 (3.5) | 59 (4.0) | 17 (3.0) |
| Moldova, Rep. of | 49 (5.1) | 38 (4.9) | 13 (3.1) | 58 (5.0) | 25 (4.0) | 17 (3.5) |
| Morocco | s 25 (5.3) | 35 (6.6) | 40 (7.2) | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ |
| Netherlands | 25 (3.9) | 55 (4.6) | 21 (3.4) | 9 (2.8) | 50 (4.7) | 42 (4.6) |
| New Zealand | 57 (5.1) | 32 (4.6) | 11 (2.9) | 38 (4.7) | 41 (4.9) | 21 (3.5) |
| Norway | 54 (4.3) | 37 (4.0) | 9 (2.1) | 36 (4.5) | 48 (4.5) | 15 (3.0) |
| Palestinian Nat'l Auth. | 70 (3.8) | 26 (4.0) | 4 (1.7) | 50 (4.6) | 42 (4.7) | 8 (2.2) |
| Philippines | 63 (4.2) | 34 (4.1) | 3 (1.5) | 64 (4.3) | 27 (4.2) | 9 (2.3) |
| Romania | 64 (4.1) | 32 (3.9) | 4 (1.6) | 63 (4.2) | 30 (4.3) | 7 (2.2) |
| Russian Federation | 59 (3.9) | 37 (3.7) | 4 (1.5) | 45 (3.8) | 45 (4.0) | 9 (2.2) |
| Saudi Arabia | 57 (5.9) | 30 (4.2) | 13 (4.8) | 42 (5.4) | 43 (4.4) | 16 (4.7) |
| Scotland | 40 (4.4) | 44 (4.7) | 17 (3.5) | 28 (4.2) | 56 (4.3) | 16 (3.4) |
| Serbia | 60 (4.0) | 32 (3.9) | 8 (2.3) | 44 (3.9) | 43 (3.6) | 12 (2.9) |
| Singapore | 42 (2.6) | 46 (2.8) | 12 (2.0) | 43 (2.4) | 36 (2.4) | 21 (2.0) |
| Slovak Republic | 54 (4.7) | 45 (4.6) | 1 (0.7) | 43 (4.1) | 45 (4.5) | 12 (2.9) |
| Slovenia | 47 (4.0) | 38 (3.8) | 15 (3.0) | 29 (4.0) | 37 (3.9) | 34 (4.1) |
| South Africa | 56 (3.6) | 36 (3.5) | 8 (2.3) | 61 (3.5) | 28 (3.4) | 11 (2.5) |
| Sweden | 60 (3.5) | 34 (3.4) | 6 (1.6) | 50 (3.6) | 33 (3.4) | 18 (3.0) |
| Tunisia | 55 (4.2) | 29 (3.6) | 16 (2.8) | 29 (4.1) | 39 (4.5) | 32 (4.0) |
| United States | 39 (2.9) | 42 (2.8) | 18 (2.2) | 43 (3.0) | 30 (3.1) | 27 (2.8) |
| ま England | 32 (5.4) | 56 (6.0) | 11 (3.3) | 40 (6.1) | 43 (6.0) | 17 (4.0) |
| International Avg. | 50 (0.6) | 39 (0.6) | 11 (0.4) | 42 (0.6) | 39 (0.6) | 19 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 56 (5.1) | 26 (4.2) | 18 (3.6) | 51 (5.0) | 32 (4.7) | 17 (3.8) |
| Indiana State, US | 34 (5.0) | 45 (6.3) | 21 (5.4) | 36 (5.3) | 37 (5.6) | 27 (5.2) |
| Ontario Province, Can. | 44 (5.3) | 38 (4.6) | 18 (3.7) | 37 (5.0) | 40 (4.8) | 23 (3.9) |
| Quebec Province, Can. | 50 (5.2) | 28 (4.1) | 23 (4.0) | 43 (4.9) | 36 (5.3) | 22 (4.1) |

Background data provided by teachers.
a Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.8: Types of Interactions Among Mathematics Teachers


| Countries | Percentage of Students by Their Teachers' Interactions with Other Teachers |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Visit to Another Teacher's Classroom to Observe Teaching |  |  | Informal Observations of Their Classroom by Another Teacher |  |  |
|  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |
| Armenia | 22 (3.0) | 67 (3.4) | 12 (2.2) | 11 (2.8) | 63 (4.1) | 26 (3.3) |
| Australia | 2 (1.0) | 13 (2.7) | 85 (2.8) | 5 (2.0) | 16 (3.0) | 80 (3.5) |
| Bahrain | 2 (1.1) | 46 (2.7) | 52 (2.9) | 6 (2.1) | 34 (3.1) | 60 (3.2) |
| Belgium (Flemish) | 0 (0.0) | 1 (0.8) | 99 (0.8) | 5 (1.9) | 2 (0.9) | 93 (2.2) |
| Botswana | 7 (2.3) | 51 (5.0) | 42 (4.9) | 9 (2.6) | 49 (4.7) | 42 (4.7) |
| Bulgaria | 3 (1.4) | 18 (3.4) | 79 (3.7) | 1 (0.8) | 16 (3.1) | 83 (3.3) |
| Chile | 6 (2.1) | 7 (2.0) | 87 (2.2) | 13 (2.5) | 15 (3.0) | 72 (3.4) |
| Chinese Taipei | 3 (1.4) | 27 (3.7) | 70 (3.8) | 1 (0.0) | 8 (2.5) | 91 (2.6) |
| Cyprus | 6 (1.8) | 17 (1.9) | 77 (2.3) | 25 (2.8) | 21 (2.8) | 54 (2.8) |
| Egypt | 37 (3.7) | 40 (4.1) | 22 (3.4) | 9 (2.4) | 32 (3.9) | 59 (4.4) |
| Estonia | 8 (1.9) | 29 (3.6) | 64 (3.8) | 7 (1.8) | 28 (3.1) | 65 (3.4) |
| Ghana | 30 (3.9) | 41 (4.4) | 30 (4.3) | 34 (4.2) | 43 (4.3) | 23 (3.7) |
| Hong Kong, SAR | 1 (1.0) | 22 (4.1) | 76 (4.2) | 1 (1.0) | 14 (3.3) | 84 (3.4) |
| Hungary | 3 (1.5) | 42 (4.1) | 55 (4.3) | 1 (1.0) | 23 (3.3) | 76 (3.3) |
| Indonesia | 35 (4.2) | 17 (3.4) | 48 (4.1) | 23 (3.4) | 18 (3.4) | 59 (4.6) |
| Iran, Islamic Rep. of | 2 (1.2) | 14 (2.9) | 84 (3.0) | 2 (1.1) | 22 (3.1) | 75 (3.4) |
| Israel | 1 (0.6) | 12 (2.8) | 87 (2.9) | 3 (1.4) | 15 (2.8) | 82 (3.0) |
| Italy | 2 (1.0) | 3 (1.6) | 95 (1.9) | 11 (2.5) | 15 (2.9) | 75 (3.1) |
| Japan | 9 (2.4) | 18 (3.0) | 74 (3.7) | 8 (2.3) | 14 (3.0) | 78 (3.7) |
| Jordan | 10 (3.0) | 52 (4.7) | 38 (3.8) | 8 (2.7) | 33 (4.2) | 59 (4.5) |
| Korea, Rep. of | 2 (1.1) | 11 (2.5) | 87 (2.7) | 2 (1.2) | 9 (2.0) | 89 (2.3) |
| Latvia | 6 (2.0) | 41 (3.7) | 54 (3.4) | 6 (2.2) | 26 (4.2) | 68 (4.5) |
| Lebanon | 8 (2.5) | 25 (3.8) | 67 (3.7) | 12 (2.5) | 39 (4.6) | 50 (4.7) |
| Lithuania | 3 (1.3) | 34 (3.9) | 63 (3.9) | 3 (1.5) | 33 (3.7) | 64 (3.9) |
| Macedonia, Rep. of | 8 (2.5) | 40 (3.9) | 52 (4.2) | 5 (2.0) | 44 (4.0) | 51 (4.1) |
| Malaysia | 8 (2.4) | 32 (4.0) | 60 (4.0) | 7 (2.1) | 43 (4.1) | 50 (4.4) |
| Moldova, Rep. of | 20 (3.6) | 56 (4.8) | 24 (4.5) | 16 (3.8) | 47 (5.0) | 38 (4.7) |
| Morocco | 0 (0.0) | 11 (4.6) | 89 (4.6) | x x | $\mathrm{x} \times$ | $\mathrm{x} \times$ |
| Netherlands | 2 (1.1) | 11 (3.2) | 87 (3.3) | 3 (1.4) | 11 (3.2) | 87 (3.4) |
| New Zealand | 2 (1.0) | 22 (2.8) | 75 (3.1) | 7 (2.2) | 41 (5.2) | 52 (4.7) |
| Norway | 10 (2.6) | 13 (2.4) | 77 (3.4) | 20 (3.3) | 17 (2.9) | 63 (4.0) |
| Palestinian Nat'l Auth. | 2 (1.4) | 51 (4.1) | 47 (4.2) | 3 (1.3) | 35 (4.0) | 62 (4.1) |
| Philippines | 6 (2.2) | 27 (4.2) | 67 (4.5) | 13 (3.0) | 54 (4.4) | 34 (4.2) |
| Romania | 10 (2.5) | 60 (4.1) | 30 (3.6) | 30 (3.9) | 45 (4.3) | 25 (3.6) |
| Russian Federation | 12 (2.7) | 69 (3.6) | 19 (2.6) | 6 (1.7) | 59 (3.4) | 35 (3.3) |
| Saudi Arabia | 2 (1.3) | 51 (4.8) | 47 (4.6) | 4 (1.9) | 17 (3.3) | 80 (3.6) |
| Scotland | 9 (3.0) | 14 (3.1) | 77 (4.1) | 9 (2.7) | 24 (4.4) | 67 (4.8) |
| Serbia | 15 (3.0) | 20 (3.4) | 66 (3.9) | 15 (3.1) | 24 (3.4) | 61 (3.7) |
| Singapore | 3 (0.8) | 14 (1.8) | 83 (2.0) | 3 (1.0) | 27 (2.6) | 70 (2.6) |
| Slovak Republic | 1 (0.8) | 23 (2.9) | 76 (2.9) | 1 (0.6) | 27 (3.6) | 72 (3.7) |
| Slovenia | 0 (0.0) | 6 (2.1) | 94 (2.1) | 2 (1.4) | 7 (2.3) | 91 (2.7) |
| South Africa | 7 (1.9) | 36 (3.5) | 57 (3.5) | 13 (2.4) | 40 (3.3) | 47 (3.4) |
| Sweden | 4 (1.2) | 7 (1.5) | 89 (1.8) | 5 (1.2) | 12 (2.7) | 83 (2.7) |
| Tunisia | 1 (1.0) | 8 (2.3) | 91 (2.5) | 1 (1.1) | 7 (1.9) | 92 (2.2) |
| United States | 4 (1.2) | 11 (2.0) | 85 (2.3) | 4 (1.2) | 17 (2.5) | 79 (2.5) |
| ま England | s $\quad 5(2.4)$ | 25 (5.0) | 71 (5.7) | s 3 (1.5) | 35 (5.7) | 63 (5.9) |
| International Avg. | 7 (0.3) | 27 (0.5) | 65 (0.5) | 8 (0.3) | 27 (0.5) | 65 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 3 (1.9) | 8 (3.0) | 89 (3.5) | 6 (2.5) | 6 (2.4) | 88 (3.5) |
| Indiana State, US | 2 (2.1) | 4 (1.9) | 94 (2.8) | 2 (2.1) | 11 (3.9) | 87 (4.4) |
| Ontario Province, Can. | 4 (1.9) | 20 (4.1) | 76 (4.5) | 5 (2.4) | 18 (3.7) | 77 (4.3) |
| Quebec Province, Can. | 2 (1.3) | 1 (0.3) | 97 (1.3) | 0 (0.0) | 4 (2.1) | 96 (2.1) |

## Background data provided by teachers.

\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.8: Types of Interactions Among Mathematics Teachers


| Countries | Percentage of Students by Their Teachers' Interactions with Other Teachers |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Discussion About How to Teach a Particular Concept |  |  | Working on Preparing Instructional Materials |  |  |  |
|  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |
| Armenia | 47 (3.6) | 48 (3.7) | 5 (1.3) | r | 30 (4.1) | 55 (4.3) | 15 (2.1) |
| Australia | 51 (4.2) | 37 (4.8) | 12 (2.7) |  | 54 (4.6) | 31 (4.9) | 15 (2.9) |
| Belgium (Flemish) | 52 (3.5) | 40 (3.5) | 9 (2.0) |  | 41 (3.8) | 37 (3.6) | 23 (2.6) |
| Chinese Taipei | 54 (4.1) | 44 (4.2) | 2 (1.2) |  | 24 (3.4) | 52 (4.5) | 25 (3.7) |
| Cyprus | 59 (3.9) | 36 (3.7) | 5 (1.7) |  | 59 (3.6) | 32 (3.2) | 9 (2.0) |
| England | 61 (5.2) | 28 (5.0) | 10 (2.7) | $r$ | 62 (4.9) | 20 (4.2) | 17 (3.5) |
| Hong Kong, SAR | 41 (4.5) | 49 (4.5) | 9 (2.3) |  | 17 (3.4) | 60 (4.8) | 24 (4.1) |
| Hungary | 55 (4.3) | 41 (4.2) | 4 (1.2) |  | 57 (4.2) | 35 (3.9) | 7 (2.3) |
| Iran, Islamic Rep. of | 62 (4.3) | 35 (4.2) | 3 (1.7) |  | 64 (4.6) | 31 (4.5) | 5 (2.0) |
| Italy | 47 (3.0) | 42 (3.0) | 11 (2.0) |  | 55 (3.6) | 32 (3.3) | 13 (2.5) |
| Japan | 52 (4.3) | 37 (4.3) | 11 (2.6) |  | 41 (4.0) | 45 (4.3) | 14 (2.5) |
| Latvia | 43 (4.1) | 45 (4.5) | 13 (2.8) |  | 36 (3.9) | 56 (4.0) | 9 (2.4) |
| Lithuania | 60 (3.5) | 33 (3.4) | 7 (1.9) |  | 68 (3.2) | 27 (3.0) | 5 (1.8) |
| Moldova, Rep. of | 57 (4.3) | 37 (4.2) | 6 (2.0) |  | 74 (3.3) | 18 (3.1) | 8 (2.2) |
| Morocco | s $\quad 31$ (4.6) | 29 (4.5) | 40 (5.1) | s | 12 (3.1) | 18 (4.2) | 70 (5.0) |
| Netherlands | 42 (4.7) | 42 (4.7) | 16 (3.2) |  | 25 (4.4) | 44 (4.7) | 32 (4.4) |
| New Zealand | 65 (3.5) | 30 (3.1) | 5 (1.5) |  | 57 (3.6) | 31 (3.4) | 12 (2.2) |
| Norway | 64 (2.9) | 28 (3.9) | 8 (2.6) |  | 50 (3.6) | 30 (3.9) | 20 (3.3) |
| Philippines | 58 (5.0) | 38 (5.1) | 3 (1.4) |  | 71 (4.6) | 26 (4.6) | 3 (1.3) |
| Russian Federation | 55 (3.3) | 43 (3.2) | 2 (1.0) |  | 46 (3.4) | 48 (3.9) | 6 (1.9) |
| Scotland | 43 (4.9) | 41 (4.7) | 16 (3.2) | $r$ | 39 (4.7) | 37 (4.5) | 24 (3.5) |
| Singapore | 42 (4.6) | 49 (4.7) | 9 (2.2) |  | 35 (4.2) | 52 (4.2) | 13 (2.8) |
| Slovenia | 64 (4.0) | 30 (3.7) | 6 (2.2) |  | 38 (4.5) | 45 (4.6) | 17 (3.4) |
| Tunisia | 55 (4.4) | 23 (3.3) | 23 (3.7) | $r$ | 29 (3.9) | 29 (3.7) | 42 (4.4) |
| United States | 62 (2.6) | 29 (2.3) | 9 (1.7) |  | 59 (2.7) | 29 (2.7) | 11 (1.7) |
| International Avg. | 53 (0.8) | 37 (0.8) | 10 (0.5) |  | 46 (0.8) | 37 (0.8) | 17 (0.6) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | 59 (5.2) | 33 (4.9) | 8 (2.9) |  | 48 (4.8) | 38 (4.6) | 15 (3.0) |
| Ontario Province, Can. | 46 (4.8) | 46 (4.7) | 9 (2.7) |  | 47 (5.2) | 33 (4.7) | 20 (3.7) |
| Quebec Province, Can. | 52 (5.0) | 34 (4.4) | 14 (3.2) |  | 46 (4.5) | 33 (4.3) | 22 (3.6) |

[^60]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

Exhibit 6.8: Types of Interactions Among Mathematics Teachers


| Countries | Percentage of Students by Their Teachers' Interactions with Other Teachers |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Visit to Another Teacher's Classroom to Observe Teaching |  |  |  | Informal Observations of Their Classroom by Another Teacher |  |  |  |
|  |  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |  | At Least Weekly | 2 or 3 Times per Month | Never or Almost Never |
| Armenia | r | 19 (3.6) | 69 (3.7) | 11 (2.2) | r | 8 (2.1) | 65 (3.8) | 27 (3.4) |
| Australia |  | 9 (2.3) | 23 (4.0) | 68 (4.3) |  | 18 (3.6) | 22 (3.5) | 60 (4.3) |
| Belgium (Flemish) |  | 1 (0.5) | 5 (1.4) | 94 (1.5) |  | 5 (1.6) | 12 (2.5) | 83 (2.9) |
| Chinese Taipei |  | 6 (1.9) | 57 (4.4) | 37 (4.0) |  | 7 (1.8) | 26 (3.8) | 67 (4.0) |
| Cyprus |  | 7 (2.1) | 33 (3.4) | 60 (3.5) |  | 30 (3.8) | 42 (3.9) | 27 (3.2) |
| England | $r$ | 2 (1.5) | 31 (4.2) | 66 (4.4) | $r$ | 3 (1.6) | 39 (4.9) | 58 (4.8) |
| Hong Kong, SAR |  | 3 (1.6) | 35 (4.8) | 62 (5.0) |  | 3 (1.6) | 15 (3.3) | 81 (3.6) |
| Hungary |  | 3 (1.4) | 52 (4.4) | 45 (4.3) |  | 2 (1.2) | 31 (3.6) | 66 (3.5) |
| Iran, Islamic Rep. of |  | 12 (3.3) | 35 (4.7) | 54 (5.0) |  | 9 (2.9) | 43 (5.0) | 48 (5.2) |
| Italy |  | 8 (1.8) | 12 (2.5) | 80 (2.9) |  | 9 (1.8) | 15 (2.4) | 76 (3.0) |
| Japan |  | 4 (1.4) | 45 (3.9) | 51 (3.7) |  | 10 (2.5) | 21 (3.4) | 69 (3.8) |
| Latvia |  | 4 (1.5) | 90 (2.3) | 6 (1.9) |  | 9 (1.9) | 75 (3.1) | 16 (2.6) |
| Lithuania |  | 1 (0.6) | 64 (3.7) | 35 (3.7) |  | 1 (0.7) | 53 (4.1) | 46 (4.1) |
| Moldova, Rep. of |  | 18 (3.3) | 67 (3.9) | 15 (2.9) |  | 11 (2.7) | 50 (3.9) | 39 (4.2) |
| Morocco | s | 5 (2.8) | 12 (3.9) | 83 (4.7) | s | 5 (3.0) | 12 (4.3) | 83 (4.8) |
| Netherlands |  | 1 (0.9) | 8 (2.8) | 92 (3.0) |  | 1 (0.9) | 11 (3.2) | 88 (3.3) |
| New Zealand |  | 4 (1.5) | 31 (3.1) | 65 (3.1) |  | 11 (2.1) | 38 (2.7) | 51 (2.9) |
| Norway |  | 13 (3.1) | 10 (2.0) | 77 (3.5) |  | 27 (3.6) | 11 (2.6) | 62 (4.4) |
| Philippines |  | 18 (3.3) | 38 (4.4) | 44 (4.1) |  | 22 (4.3) | 48 (5.0) | 30 (4.2) |
| Russian Federation |  | 12 (2.6) | 83 (2.8) | 5 (1.3) |  | 9 (2.3) | 63 (3.6) | 28 (3.1) |
| Scotland | $r$ | 1 (0.7) | 11 (2.7) | 88 (2.7) | $r$ | 11 (2.9) | 29 (5.1) | 61 (5.4) |
| Singapore |  | 0 (0.0) | 8 (1.8) | 92 (1.8) |  | 1 (0.0) | 15 (2.8) | 84 (2.7) |
| Slovenia |  | 0 (0.2) | 11 (2.9) | 88 (2.9) |  | 1 (0.6) | 9 (2.4) | 89 (2.4) |
| Tunisia |  | 8 (2.2) | 15 (2.9) | 77 (3.4) | $r$ | 5 (1.5) | 9 (2.6) | 85 (2.8) |
| United States |  | 4 (1.1) | 16 (1.7) | 80 (2.1) |  | 4 (1.1) | 17 (1.9) | 78 (2.2) |
| International Avg. |  | 7 (0.4) | 34 (0.7) | 59 (0.7) |  | 9 (0.5) | 31 (0.7) | 60 (0.7) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 3 (1.6) | 8 (2.4) | 90 (2.5) |  | 6 (1.9) | 7 (2.1) | 87 (3.0) |
| Ontario Province, Can. |  | 6 (2.4) | 12 (2.9) | 82 (3.8) |  | 8 (2.6) | 14 (3.4) | 78 (4.2) |
| Quebec Province, Can. |  | 3 (1.5) | 9 (2.9) | 88 (3.2) |  | 5 (2.1) | 13 (3.1) | 82 (3.3) |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

More than 80 percent of the students were taught mathematics by teachers having a least some professional development training in these areas.

Exhibit 6.7 presents teachers' reports about their professional development participation in six different aspects of mathematics teaching. The results were relatively consistent across the six topics - content, pedagogy, curriculum, technology, problem solving, and assessment. At the eighth grade, from 43 to 57 percent of the students, on average, internationally, were taught by teachers having participated in professional development in the area during the past two years. The highest percentages, 57 percent in both cases, were for the areas of content and pedagogy. At the fourth grade, on average, the percentages were somewhat lower, ranging from 33 to 47 percent. The highest percentages were for content ( $46 \%$ ), pedagogy ( $47 \%$ ), and problem solving ( $46 \%$ ). The lowest percentage was for integrating information technology into mathematics ( $33 \%$ ).

Because opportunities for professional development do not necessarily have to be structured by the school, teachers also were asked about how often they interacted with their colleagues. More specifically, they were asked about discussing teaching strategies for particular concepts, preparing instructional materials, and classroom observations. As shown in Exhibit 6.8, on average, the results for the TIMSS participants were consistent across grades. Teachers of most students ( $80 \%$ or more) reported weekly or monthly interaction about instructional issues. In contrast, observing other teachers or being observed themselves was relatively infrequent ( $65 \%$ never).

## How Ready Do Teachers Think They Are to Teach Mathematics?

TIMSS 2003 asked teachers how ready they felt to teach the mathematics topics included in the TIMSS 2003 mathematics framework. Across the five major content areas (number, algebra, measurement,
geometry, and data), the eighth-grade teachers were asked about 18 topics (sub-areas). Exhibit 6.9 contains teachers' reports, indicating that the teachers of almost all the eighth-grade students felt ready to teach nearly all the topics. On average, internationally, the results ranged from 84 to 98 percent, with the results above 90 percent for all but three of the data topics (sources of error, data collection methods, and simple probability). At the fourth grade, the results were very similar. Teachers were asked about 16 topics, with the results ranging from 83 to 100 percent, on average, internationally. The results dipped below 90 percent for only two geometry topics, relationships between twoand three-dimensional shapes ( $88 \%$ ) and translation, reflection, and rotation (83\%).

At the eighth grade, essentially all students in all countries were taught the number topics by teachers who felt ready to teach the topics. Teachers' reports for the algebra topics were similar, falling substantially below 90 percent of the students only in Tunisia ( 71 to $74 \%$ ). In the measurement area, percentages ranged between 55 to 89 percent for at least one topic in a number of countries, including Belgium (Flemish), Botswana, Ghana, Iran, Japan, Moldova, the Philippines, Saudi Arabia, South Africa, and Tunisia. For geometry, readiness reports were uniformly above 90 percent with only few exceptions for particular topics in Chile, Hungary, Moldova, Saudi Arabia, Serbia, and Tunisia. Across the topics, the least amount of readiness was reported for the data topics. For almost all of the countries, for one or more of the data topics, fewer than 90 percent of the students were taught by teachers who felt ready to teach the topic.

At the fourth grade, in general, almost all the students (at least $90 \%$ ) in all the participating entities (except Tunisia) were taught by teachers who felt ready to teach the topics in number, algebra, measurement, and data. Teachers in several countries felt less ready to teach one more of the geometry topics, including Belgium (Flemish), Hungary, Iran, Japan, the Netherlands, Norway, the Philippines, Singapore, Slovenia, and Tunisia.

| Countries | Percentage of Students Whose Teachers Report Feeling They Are Ready to Teach Mathematics Topics |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number |  | Algebra |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| Armenia | 99 (0.8) | 99 (0.7) | $r$ | 99 (0.7) | $r$ | 100 (0.3) |  | 100 (0.3) |  | 98 (1.1) |
| Australia | 100 (0.0) | 100 (0.0) |  | 100 (0.0) |  | 99 (0.7) |  | 99 (0.7) |  | 98 (1.3) |
| Bahrain | 99 (0.5) | 99 (0.5) |  | 94 (2.1) |  | 98 (1.3) |  | 97 (1.3) |  | 94 (2.1) |
| Belgium (Flemish) | 100 (0.4) | 99 (0.8) |  | 92 (1.8) |  | 93 (2.3) |  | 95 (1.6) |  | 93 (2.0) |
| Botswana | 97 (1.5) | 98 (1.5) | $r$ | 98 (1.2) | $r$ | 98 (1.3) | $r$ | 95 (2.0) | $r$ | 90 (2.8) |
| Bulgaria | 100 (0.0) | 100 (0.0) |  | 99 (0.7) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| Chile | 100 (0.0) | 99 (0.8) |  | 95 (1.4) |  | 94 (1.5) |  | 96 (1.5) |  | 90 (2.1) |
| Chinese Taipei | 100 (0.0) | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.6) |
| Cyprus | 98 (0.0) | 98 (0.0) | $r$ | 98 (0.6) |  | 100 (0.0) |  | 98 (0.0) |  | 97 (0.7) |
| Egypt | 99 (0.8) | 100 (0.0) |  | 96 (1.9) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| Estonia | 100 (0.4) | 100 (0.4) |  | 100 (0.0) |  | 100 (0.4) |  | 100 (0.4) |  | 100 (0.4) |
| Ghana | 98 (1.1) | 99 (0.9) |  | 97 (1.6) |  | 100 (0.0) |  | 100 (0.5) |  | 94 (2.2) |
| Hong Kong, SAR | 100 (0.0) | 100 (0.0) |  | 99 (0.8) |  | 100 (0.0) |  | 99 (0.8) |  | 98 (1.3) |
| Hungary | 100 (0.4) | 100 (0.4) |  | 99 (0.5) |  | 100 (0.4) |  | 100 (0.4) |  | 100 (0.4) |
| Indonesia | 99 (1.1) | 100 (0.0) | 5 | 98 (1.5) | 5 | 100 (0.0) | 5 | 100 (0.0) | 5 | 93 (2.9) |
| Iran, Islamic Rep. of | 99 (0.8) | 98 (1.0) |  | 90 (2.5) |  | 98 (1.2) |  | 94 (2.2) |  | 87 (2.7) |
| Israel | 99 (0.7) | 99 (0.7) |  | 99 (0.9) |  | 99 (0.8) |  | 98 (0.9) |  | 98 (0.9) |
| Italy | 100 (0.0) | 100 (0.0) |  | 92 (1.9) |  | 99 (0.7) |  | 98 (0.9) |  | 95 (1.4) |
| Japan | 95 (1.6) | 99 (0.7) |  | 93 (2.3) |  | 99 (0.7) |  | 95 (2.0) |  | 97 (1.6) |
| Jordan | 99 (0.7) | 98 (1.2) |  | 99 (0.6) |  | 99 (0.8) |  | 97 (1.4) |  | 96 (1.8) |
| Korea, Rep. of | 99 (0.5) | s 98 (1.0) | $s$ | 93 (2.0) | $s$ | 99 (0.4) | 5 | 99 (0.7) | 5 | 98 (1.0) |
| Latvia | 100 (0.0) | s 100 (0.0) | 5 | 100 (0.0) | 5 | 100 (0.0) | 5 | 97 (1.5) | 5 | 99 (1.0) |
| Lebanon | 98 (1.4) | 100 (0.0) |  | 93 (2.6) |  | 96 (1.8) |  | 95 (2.0) |  | 95 (1.6) |
| Lithuania | 100 (0.0) | 100 (0.0) |  | 98 (1.4) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| Macedonia, Rep. of | 99 (0.7) | 99 (1.0) |  | 100 (0.5) |  | 99 (0.7) |  | 99 (1.0) |  | 98 (1.3) |
| Malaysia | 100 (0.0) | 100 (0.0) |  | 100 (0.0) |  | 99 (0.7) |  | 97 (1.3) |  | 90 (2.6) |
| Moldova, Rep. of | 91 (2.8) | 91 (2.6) | $r$ | 94 (2.1) | $r$ | 91 (2.5) | $r$ | 89 (3.1) | $r$ | 92 (2.6) |
| Morocco | x x | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Netherlands | 99 (0.6) | 100 (0.0) |  | 96 (1.6) |  | 99 (0.8) |  | 99 (0.6) |  | 100 (0.0) |
| New Zealand | 100 (0.2) | 98 (2.2) |  | 100 (0.2) |  | 98 (1.2) |  | 99 (0.6) |  | 100 (0.2) |
| Norway | 100 (0.0) | 100 (0.0) |  | 97 (1.8) |  | 97 (1.7) |  | 98 (1.4) |  | 98 (1.5) |
| Palestinian Nat'l Auth. | 100 (0.0) | 100 (0.0) |  | 99 (0.8) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.9) |
| Philippines | 100 (0.0) | 100 (0.0) |  | 97 (1.5) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (1.0) |
| Romania | 100 (0.0) | 100 (0.0) |  | 97 (1.4) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| Russian Federation | - - | - - |  | - - |  | - - |  | - - |  | - - |
| Saudi Arabia | r 96 (1.8) | r 100 (0.0) | $r$ | 86 (5.9) | $r$ | 95 (2.4) | $r$ | 94 (5.3) | $r$ | 80 (6.1) |
| Scotland | 100 (0.0) | 100 (0.0) |  | 100 (0.0) |  | 95 (2.2) |  | 98 (1.1) |  | 96 (1.8) |
| Serbia | 91 (2.8) | 90 (2.9) |  | 93 (2.4) |  | 90 (2.5) |  | 90 (2.5) |  | 90 (2.5) |
| Singapore | 99 (0.4) | 100 (0.4) | $r$ | 95 (1.3) | $r$ | 99 (0.6) | $r$ | 98 (0.8) | $r$ | 97 (1.0) |
| Slovak Republic | 100 (0.0) | 100 (0.3) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.9) |  | 98 (1.2) |
| Slovenia | 100 (0.0) | 100 (0.0) |  | 99 (0.8) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| South Africa | r 99 (0.9) | r 100 (0.0) | $r$ | 99 (0.7) | $r$ | 98 (1.0) | $r$ | 95 (1.8) | $r$ | 91 (2.3) |
| Sweden | 100 (0.2) | 100 (0.2) |  | 98 (1.1) |  | 99 (0.8) |  | 98 (0.9) |  | 96 (1.2) |
| Tunisia | r 99 (1.1) | r 98 (1.3) | $r$ | 87 (2.9) | $r$ | 71 (4.5) | $r$ | 74 (3.9) | $r$ | 71 (4.1) |
| United States | 100 (0.0) | 100 (0.0) |  | 99 (0.6) |  | 100 (0.2) |  | 99 (0.4) |  | 98 (0.9) |
| \# England | - - | - - |  | - - |  | - - |  | - - |  | - - |
| International Avg. | 99 (0.1) | 99 (0.1) |  | 97 (0.3) |  | 98 (0.2) |  | 97 (0.2) |  | 95 (0.3) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 99 (0.8) | 99 (0.8) |  | 98 (1.6) |  | 99 (0.8) |  | 99 (0.6) |  | 96 (1.2) |
| Indiana State, US | r 100 (0.0) | r 100 (0.0) | $r$ | 100 (0.0) | $r$ | 100 (0.0) | $r$ | 100 (0.0) | $r$ | 100 (0.0) |
| Ontario Province, Can. | 100 (0.0) | 98 (1.3) |  | 98 (1.5) |  | 97 (1.7) |  | 99 (0.8) |  | 96 (2.0) |
| Quebec Province, Can. | 100 (0.0) | 100 (0.0) |  | 99 (0.9) |  | 90 (3.2) |  | 99 (0.9) |  | 93 (2.6) |

[^61][^62]Exhibit 6.9: Readiness to Teach Mathematics (Continued...)

| Countries | Percentage of Students Whose Teachers Report Feeling They Are Ready to Teach Mathematics Topics |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Measurement |  |  |  |  |  |  | Geometry |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Armenia | 99 (0.7) | $r$ | 100 (0.0) | $r$ | 98 (1.3) | $r$ | 99 (0.1) |  | 100 (0.3) |  | 99 (0.5) | $r$ | 99 (0.8) | r | 98 (1.0) |
| Australia | 100 (0.0) |  | 99 (1.2) |  | 97 (0.7) |  | 97 (1.5) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.8) |  | 98 (1.1) |
| Bahrain | 96 (2.0) |  | 95 (1.3) |  | 94 (2.3) |  | 93 (1.9) |  | 99 (0.5) |  | 98 (0.5) |  | $\mathrm{x} \times$ |  | 96 (1.7) |
| Belgium (Flemish) | 94 (1.6) |  | 98 (1.0) |  | 83 (2.8) |  | 91 (2.4) |  | 98 (0.8) |  | 98 (1.0) |  | 90 (2.2) |  | 98 (0.9) |
| Botswana | 99 (1.0) | $r$ | 98 (1.3) | $r$ | 89 (3.1) | $r$ | 84 (3.7) | $r$ | 97 (1.9) |  | 97 (1.7) | $r$ | 95 (2.2) | $r$ | 96 (2.1) |
| Bulgaria | 99 (0.6) |  | 99 (0.6) |  | 98 (0.9) |  | 97 (1.4) |  | 98 (1.1) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |
| Chile | 99 (0.9) |  | 98 (1.1) |  | 91 (2.6) |  | 93 (2.1) |  | 98 (1.1) |  | 100 (0.0) |  | 96 (1.6) |  | 76 (3.0) |
| Chinese Taipei | 98 (1.1) |  | 99 (0.9) |  | 99 (0.6) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 98 (0.9) |  | 96 (1.6) |
| Cyprus | 100 (0.0) |  | 98 (0.0) |  | 95 (1.4) |  | 96 (1.1) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 90 (1.7) |
| Egypt | 97 (1.5) |  | 94 (2.4) |  | 93 (2.1) |  | 94 (2.2) |  | 100 (0.0) |  | 100 (0.0) |  | $\mathrm{x} \times$ | $r$ | 99 (0.9) |
| Estonia | 100 (0.4) |  | 100 (0.4) |  | 100 (0.4) |  | 99 (0.8) |  | 99 (0.6) |  | 100 (0.4) |  | 100 (0.4) |  | 99 (0.7) |
| Ghana | 97 (1.3) |  | 89 (3.4) |  | 79 (4.3) | $r$ | 94 (2.3) |  | 96 (2.1) |  | 97 (1.6) | $r$ | 94 (2.6) |  | 94 (2.4) |
| Hong Kong, SAR | 100 (0.1) |  | 100 (0.0) |  | 99 (0.9) |  | 99 (1.1) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 96 (1.8) |
| Hungary | 99 (0.5) |  | 100 (0.4) |  | 99 (0.8) |  | 100 (0.4) |  | 100 (0.4) |  | 100 (0.4) |  | 86 (3.1) |  | 100 (0.4) |
| Indonesia | 99 (0.9) | 5 | 99 (1.0) | 5 | 96 (1.9) | 5 | 96 (1.9) | 5 | 95 (1.8) | 5 | 97 (1.9) | 5 | 100 (0.0) | 5 | 87 (3.7) |
| Iran, Islamic Rep. of | 97 (1.4) |  | 93 (2.2) |  | 87 (3.1) |  | 82 (3.4) |  | 99 (0.8) |  | 99 (0.7) |  | 98 (0.4) |  | 98 (1.3) |
| Israel | 98 (1.6) |  | 99 (0.8) |  | 95 (2.1) |  | 93 (2.3) |  | 99 (0.8) |  | 99 (0.8) |  | 98 (1.0) |  | 94 (1.7) |
| Italy | 99 (0.6) |  | 100 (0.0) |  | 96 (1.5) |  | 92 (2.1) |  | 99 (0.6) |  | 100 (0.5) |  | 98 (0.9) |  | 91 (2.0) |
| Japan | 94 (2.0) |  | 82 (3.1) |  | 81 (3.4) |  | 74 (3.7) |  | 87 (2.7) |  | 100 (0.0) |  | 97 (1.5) |  | 95 (1.7) |
| Jordan | 99 (0.6) |  | 97 (1.6) |  | 94 (2.1) |  | 97 (1.5) |  | 99 (0.7) |  | 98 (1.3) |  | 96 (1.6) |  | 90 (2.7) |
| Korea, Rep. of | 95 (1.2) | 5 | 96 (1.4) | 5 | 91 (2.5) | 5 | 96 (1.5) | 5 | 96 (1.7) |  | 98 (1.1) | $s$ | 99 (0.8) | 5 | 96 (1.2) |
| Latvia | 96 (2.0) | s | 99 (0.7) | $s$ | 95 (2.2) | 5 | 93 (2.8) | 5 | 100 (0.0) | 5 | 100 (0.0) | 5 | 91 (3.6) | 5 | 92 (2.7) |
| Lebanon | 98 (1.3) |  | 94 (2.7) | $r$ | 92 (2.3) | $r$ | 98 (1.4) |  | 98 (1.3) |  | 99 (1.2) |  | 98 (1.3) |  | 96 (1.8) |
| Lithuania | 100 (0.4) |  | 100 (0.0) |  | 99 (1.0) |  | 99 (0.9) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 98 (1.2) |
| Macedonia, Rep. of | 98 (1.1) |  | 98 (1.1) |  | 95 (1.9) |  | 96 (1.7) |  | 99 (0.7) |  | 99 (0.7) |  | 100 (0.0) |  | 98 (1.3) |
| Malaysia | 100 (0.0) |  | 95 (1.7) |  | 91 (2.4) |  | 93 (2.1) |  | 100 (0.0) |  | 99 (0.6) |  | 98 (1.2) |  | 98 (1.2) |
| Moldova, Rep. of | 91 (2.8) | $r$ | 92 (2.5) | $r$ | 89 (2.9) | $r$ | 85 (3.2) | $r$ | 87 (3.2) |  | 89 (3.0) | $r$ | 91 (2.6) | $r$ | 91 (2.7) |
| Morocco | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |  | x x |  | x x |  | x x |  | x x |
| Netherlands | 99 (0.7) |  | 99 (0.7) |  | 98 (1.1) |  | 99 (0.6) |  | 100 (0.0) |  | 100 (0.0) |  | 95 (2.0) |  | 99 (1.0) |
| New Zealand | 100 (0.2) |  | 97 (2.3) |  | 96 (2.4) |  | 99 (0.6) |  | 97 (1.3) |  | 99 (0.6) |  | 99 (0.6) |  | 97 (2.3) |
| Norway | 99 (1.4) |  | 100 (0.0) |  | 98 (1.5) |  | 97 (1.7) |  | 98 (1.6) |  | 98 (1.4) |  | 100 (0.0) |  | 99 (1.4) |
| Palestinian Nat'l Auth. | 99 (0.7) |  | 98 (1.2) |  | 96 (1.9) |  | 99 (0.7) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.9) |  | 92 (2.6) |
| Philippines | 93 (1.9) |  | 92 (2.3) |  | 79 (3.4) |  | 90 (2.8) |  | 93 (2.3) |  | 93 (2.4) |  | 96 (1.6) |  | 76 (3.7) |
| Romania | 99 (0.9) |  | 99 (1.0) |  | 97 (1.4) |  | 99 (0.8) |  | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 95 (1.9) |
| Russian Federation | - - |  | - - |  | - - |  | - - |  | - - |  | - - |  | - - |  | - - |
| Saudi Arabia | r 85 (5.8) | $r$ | 69 (6.4) | $r$ | 73 (6.0) | $r$ | 79 (6.3) | $r$ | 76 (6.6) | $r$ | 99 (1.0) | $r$ | 88 (5.6) | $r$ | 92 (2.7) |
| Scotland | 100 (0.0) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (1.0) |  | 99 (1.0) |  | 99 (1.1) |  | 94 (2.4) |  | 96 (2.1) |
| Serbia | 90 (2.9) |  | 91 (2.7) |  | 91 (2.7) |  | 92 (2.4) |  | 89 (2.7) |  | 90 (2.5) |  | 90 (2.9) |  | 91 (2.8) |
| Singapore | r 100 (0.4) | $r$ | 99 (0.6) | $r$ | 93 (1.6) | $r$ | 97 (1.2) | $r$ | 100 (0.4) | $r$ | 97 (1.0) | $r$ | 98 (0.9) | $r$ | 97 (1.1) |
| Slovak Republic | 100 (0.3) |  | 99 (1.2) |  | 99 (0.4) |  | 97 (1.3) |  | 100 (0.0) |  | 100 (0.3) |  | 98 (1.1) |  | 98 (1.0) |
| Slovenia | 99 (0.8) |  | 99 (0.8) |  | 95 (2.0) |  | 97 (1.5) |  | 100 (0.0) |  | 100 (0.0) |  | 99 (0.7) |  | 99 (0.9) |
| South Africa | r 93 (1.8) | $r$ | 88 (2.7) | $r$ | 79 (3.1) | $r$ | 88 (2.8) | $r$ | 95 (1.7) | $r$ | 98 (0.9) | $r$ | 92 (1.9) | $r$ | 81 (3.1) |
| Sweden | 100 (0.2) |  | 100 (0.2) |  | 99 (0.5) |  | 98 (0.9) |  | 98 (0.9) |  | 98 (0.9) |  | 98 (0.8) |  | 93 (1.7) |
| Tunisia | r 84 (3.5) | $r$ | 68 (4.3) | $r$ | 66 (4.4) | $r$ | 55 (5.0) | $r$ | 47 (5.1) | $r$ | 91 (2.4) | $r$ | 61 (4.8) | $r$ | 40 (4.5) |
| United States | 99 (0.6) |  | 100 (0.0) |  | 97 (0.9) |  | 97 (1.1) |  | 98 (0.8) |  | 99 (0.7) |  | 98 (1.0) |  | 97 (1.1) |
| ま England | - - |  | - - |  | - |  | - - |  | - |  | - |  | - - |  | - - |
| International Avg. | 97 (0.2) |  | 96 (0.3) |  | 92 (0.4) |  | 93 (0.3) |  | 96 (0.3) |  | 98 (0.2) |  | 96 (0.3) |  | 93 (0.3) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 99 (0.8) |  | 99 (0.8) |  | 96 (2.0) |  | 93 (2.5) |  | 99 (0.8) |  | 99 (0.8) |  | 97 (1.9) |  | 90 (3.2) |
| Indiana State, US | r 98 (0.2) | r | 100 (0.0) | $r$ | 97 (2.3) | $r$ | 95 (2.3) | $r$ | 99 (0.0) | $r$ | 100 (0.0) | $r$ | 99 (0.6) | $r$ | 99 (0.6) |
| Ontario Province, Can. | 100 (0.0) |  | 100 (0.1) |  | 93 (2.7) |  | 95 (2.0) |  | 100 (0.1) |  | 100 (0.1) |  | 91 (2.9) |  | 98 (1.2) |
| Quebec Province, Can. | 99 (0.9) |  | 99 (0.5) |  | 99 (0.9) |  | 91 (2.9) |  | 94 (2.8) |  | 98 (1.2) |  | 96 (2.1) |  | 100 (0.4) |

## Background data provided by teachers.

ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.9: Readiness to Teach Mathematics (...Continued)


Background data provided by teachers.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available.

Exhibit 6.9: Readiness to Teach Mathematics (Continued...)



[^63]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| Countries |  | Percentage of Students Whose Teachers Report Feeling They Are Ready to Teach Mathematics Topics |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Measurement |  |  | Geometry |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Armenia | 100 (0.0) | $r$ | 100 (0.4) | $r$ | 99 (0.9) | r | 100 (0.0) | $r$ | 97 (1.5) | r | 96 (1.7) |
|  | Australia | 100 (0.0) |  | 100 (0.3) |  | 100 (0.1) |  | 100 (0.1) |  | 100 (0.1) |  | 95 (1.7) |
|  | Belgium (Flemish) | 100 (0.0) |  | 99 (0.8) |  | 93 (1.9) |  | 89 (3.0) |  | 82 (2.5) |  | 81 (3.4) |
|  | Chinese Taipei | 100 (0.0) |  | 100 (0.0) |  | 99 (0.6) |  | 99 (0.6) |  | 99 (0.8) |  | 94 (2.0) |
|  | Cyprus | 100 (0.0) |  | 100 (0.0) |  | 100 (0.5) |  | 99 (0.7) |  | 99 (0.5) |  | - - |
| ま | England | - - |  | - - |  | - - |  | - - |  | - - |  | - - |
|  | Hong Kong, SAR | 100 (0.3) |  | 96 (2.1) |  | 98 (1.4) |  | 97 (1.6) |  | 98 (1.2) |  | 87 (3.3) |
|  | Hungary | 99 (1.1) |  | 99 (1.1) |  | 92 (2.4) |  | 93 (2.3) |  | 86 (3.0) |  | 90 (2.7) |
|  | Iran, Islamic Rep. of | 97 (1.5) |  | 97 (1.4) |  | 86 (3.7) |  | 97 (1.5) |  | 78 (3.8) |  | 81 (3.3) |
|  | Italy | 100 (0.0) |  | 100 (0.0) |  | 96 (1.5) |  | 98 (0.9) |  | 92 (1.9) |  | 96 (1.4) |
|  | Japan | 97 (1.4) |  | 91 (2.3) |  | 76 (3.6) |  | 86 (2.3) |  | 62 (3.6) |  | 70 (3.4) |
|  | Latvia | 99 (0.9) | $r$ | 99 (0.9) | $r$ | 96 (1.7) | $r$ | 91 (3.5) | 5 | 81 (4.3) | 5 | 68 (4.9) |
|  | Lithuania | 100 (0.0) |  | 99 (0.6) |  | 96 (1.6) |  | 100 (0.0) |  | 89 (2.3) |  | 73 (2.7) |
|  | Moldova, Rep. of | 99 (0.7) |  | 99 (0.7) |  | 90 (2.2) |  | 88 (3.0) |  | 89 (2.7) |  | 77 (3.5) |
|  | Morocco | x X |  | x x |  | x X |  | x X |  | x x |  | $\mathrm{x} \times$ |
|  | Netherlands | 97 (1.8) |  | 95 (2.2) |  | 83 (3.8) |  | 85 (3.5) |  | 79 (3.7) |  | 77 (3.8) |
|  | New Zealand | 99 (0.3) |  | 99 (0.8) |  | 99 (0.4) |  | 97 (0.9) |  | 98 (0.6) |  | 99 (0.8) |
|  | Norway | 100 (0.4) |  | 99 (0.6) |  | 96 (1.5) |  | 95 (1.4) |  | 90 (2.3) |  | 87 (2.8) |
|  | Philippines | 95 (1.9) |  | 92 (2.5) |  | 91 (2.9) |  | 96 (2.2) |  | 88 (3.3) |  | 79 (4.1) |
|  | Russian Federation | - - |  | - - |  | - - |  | - - |  | - - |  | - - |
|  | Scotland | 100 (0.0) | $r$ | 100 (0.0) | $r$ | 100 (0.0) | $r$ | 99 (0.8) | $r$ | 99 (0.7) | $r$ | 94 (2.3) |
|  | Singapore | 100 (0.2) |  | 100 (0.2) |  | 98 (0.8) |  | 95 (1.7) |  | 94 (1.9) |  | 87 (2.9) |
|  | Slovenia | 100 (0.0) |  | 99 (0.8) |  | 97 (1.7) |  | 99 (0.7) |  | 91 (2.6) |  | 84 (3.5) |
|  | Tunisia | 98 (1.1) | $r$ | 98 (1.1) | $r$ | 76 (4.2) | $r$ | 51 (4.7) | $r$ | 56 (4.5) | $r$ | 39 (4.9) |
|  | United States | 99 (0.4) |  | 100 (0.2) |  | 99 (0.5) |  | 100 (0.3) |  | 98 (0.7) |  | 97 (0.9) |
|  | International Avg. | 99 (0.2) |  | 98 (0.2) |  | 94 (0.5) |  | 93 (0.4) |  | 88 (0.5) |  | 83 (0.7) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Indiana State, US | 100 (0.0) |  | 99 (1.0) |  | 99 (0.9) |  | 99 (1.0) |  | 99 (0.9) |  | 96 (2.0) |
|  | Ontario Province, Can. | 99 (0.6) |  | 99 (0.9) |  | 100 (0.0) |  | 98 (1.6) |  | 98 (1.6) |  | 97 (2.0) |
|  | Quebec Province, Can. | 100 (0.0) |  | 100 (0.2) |  | 100 (0.1) |  | 95 (2.0) |  | 95 (1.9) |  | 97 (1.5) |

[^64]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 6.9: Readiness to Teach Mathematics

| Countries | Percentage of Students Whose Teachers Report Feeling They Are Ready to Teach Mathematics Topics |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Data |  |  |  |
|  |  |  |  |  |
| Armenia | r 98 (1.2) | r 98 (1.1) | $r$ | 97 (1.4) |
| Australia | 96 (0.7) | 100 (0.1) |  | 100 (0.1) |
| Belgium (Flemish) | 97 (1.0) | 98 (0.9) |  | 98 (0.9) |
| Chinese Taipei | 99 (0.6) | 99 (0.6) |  | 99 (1.0) |
| Cyprus | 100 (0.0) | 100 (0.4) |  | 100 (0.0) |
| England | - - | - - |  | - - |
| Hong Kong, SAR | 99 (0.8) | 100 (0.0) |  | 100 (0.0) |
| Hungary | 91 (2.7) | 89 (3.0) |  | 94 (2.1) |
| Iran, Islamic Rep. of | 93 (2.3) | 98 (1.2) |  | 95 (1.8) |
| Italy | 100 (0.0) | 100 (0.0) |  | 100 (0.0) |
| Japan | 91 (2.5) | 95 (1.8) |  | 88 (2.8) |
| Latvia | 93 (2.5) | 98 (1.0) | $r$ | 97 (1.5) |
| Lithuania | 96 (1.4) | 97 (1.1) |  | 99 (0.7) |
| Moldova, Rep. of | 97 (1.6) | 98 (1.1) |  | 97 (1.4) |
| Morocco | $\mathrm{x} \times$ | x x |  | $\mathrm{x} \times$ |
| Netherlands | 93 (2.7) | 100 (0.0) |  | 97 (1.5) |
| New Zealand | 99 (0.7) | 100 (0.0) |  | 100 (0.0) |
| Norway | 92 (2.0) | 89 (2.2) |  | 90 (2.2) |
| Philippines | 92 (2.6) | 92 (2.8) |  | 90 (2.8) |
| Russian Federation | - - | - - |  | - - |
| Scotland | 97 (1.8) | r 100 (0.0) | $r$ | 100 (0.0) |
| Singapore | 99 (0.8) | 100 (0.0) |  | 99 (0.8) |
| Slovenia | 99 (0.8) | 98 (1.4) |  | 98 (1.4) |
| Tunisia | 82 (3.6) | r 85 (3.2) | $r$ | 89 (2.8) |
| United States | 98 (0.5) | 100 (0.3) |  | 99 (0.5) |
| International Avg. | 96 (0.4) | 97 (0.3) |  | 97 (0.3) |
| Benchmarking Participants |  |  |  |  |
| Indiana State, US | 99 (1.0) | 100 (0.0) |  | 100 (0.0) |
| Ontario Province, Can. | 98 (1.6) | 100 (0.0) |  | 100 (0.0) |
| Quebec Province, Can. | 99 (0.3) | 100 (0.1) |  | 96 (1.6) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.


## Chapter 7

## Classroom Characteristics

 and InstructionAlthough the school provides the general context for learning, it is in the classroom setting and through guidance by the teacher that most instruction and learning take place. To provide information about the environment of mathematics classrooms and the instruction that takes place, Chapter 7 presents teachers' reports from the second part of the teacher questionnaire about their mathematics classrooms and instructional practices, as well as students' reports about the classroom activities they do in learning mathematics. Data are presented about class size, various limitations on instruction, instructional time, instructional emphases given different mathematics topics, and classroom activities. Information also is presented about the use of calculators and computers in mathematics lessons, the role of homework, and the reliance on different types of assessment approaches.

Teachers and the instructional approaches they use ultimately determine the mathematics students learn. Teachers structure the content and pace of lessons, introducing new material, selecting various instructional activities, and monitoring students' developing understanding of the mathematics concepts being studied. Teachers may help students use technology and tools to investigate mathematical ideas, analyze students' work for misconceptions, and promote positive
attitudes toward mathematics. They may also assign homework and conduct informal as well as formal assessments to evaluate achievement outcomes.

## How Do the Characteristics of Mathematics Classrooms Impact Instruction?

Because it can affect pedagogical strategies, class size data are shown in Exhibit 7.1. Teachers' reports about the sizes of their eighth-grade mathematics classes reveal that across countries the average class size was 30 students, but there was considerable variation - from more than 54 students in the Philippines to 20 students in Belgium (Flemish). At the fourth grade, classes typically were smaller. The average class size for the TIMSS participants was 26 students, ranging from 40 in the Philippines to 20 in Belgium (Flemish), Italy and Slovenia.

The relationship between class size and achievement is difficult to disentangle, given the variety of policies and practices that countries have in determining class size. For example, countries and schools cannot always control class size. Because of this, the ability to cap class sizes can indicate the availability of more resources in general. As another complicating factor, smaller classes can be used for advanced or practical classes such as computer laboratories on one hand, and for remedial learning or students with special needs on the other. The complexity of this issue is evidenced in the TIMSS results that show a curvilinear relationship, on average, between class size and mathematics achievement at both the eighth and fourth grades.

At the eighth grade, mathematics teachers were asked about the instructional impact of six characteristics of their students - differing academic abilities, range in backgrounds, students with special needs, uninterested students, low morale among students, and disruptive students. Responses were given on a four-point scale; "not at all," "a little," "some," and "a lot." TIMSS used the teachers' responses to construct an index and the results are presented in Exhibit 7.2.

Students were placed in the high category, if, on average, teachers reported their classrooms were impacted only a little (or less) and in the low category, if, on average, these factors impacted instruction at least somewhat. The remaining students fell in the medium category. The results show that average mathematics achievement is related to the impact of student characteristics on classroom instruction, with lower achievement related to having more instructionally challenging and diverse students in the class. On average, internationally, 20 percent of the students were in such classrooms.

Exhibit 7.1: Class Size for Mathematics Instruction

| Countries |  | Overall <br> Average Class Size | 1-24 Students |  | 25-32 Students |  | 33-40 Students |  | 41 or More Students |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | $r$ | 27 (0.9) | 39 (4.4) | 474 (5.6) | 43 (4.3) | 485 (5.0) | 7 (1.8) | 460 (9.9) | 11 (2.8) | 462 (8.4) |
| Australia |  | 26 (0.5) | 31 (4.2) | 482 (9.4) | 65 (4.7) | 518 (5.9) | 4 (2.2) | 492 (14.2) | 0 (0.4) | ~ ~ |
| Bahrain |  | 32 (0.1) | 6 (0.7) | 451 (5.8) | 52 (2.7) | 402 (2.1) | 40 (2.6) | 395 (3.5) | 3 (0.0) | 412 (3.8) |
| Belgium (Flemish) |  | 20 (0.3) | 90 (2.3) | 538 (3.3) | 10 (2.3) | 553 (10.5) | 0 (0.0) | ~ ~ | 0 (0.0) | ~ ~ |
| Botswana |  | 37 (0.4) | 1 (0.7) | ~~ | 14 (2.6) | 392 (9.1) | 60 (4.3) | 360 (3.7) | 25 (4.1) | 362 (4.1) |
| Bulgaria |  | 22 (0.5) | 64 (4.2) | 468 (4.9) | 32 (3.9) | 503 (8.0) | 3 (2.4) | 423 (5.0) | 1 (0.0) | ~ ~ |
| Chile |  | 35 (0.4) | 9 (1.5) | 385 (17.0) | 22 (2.6) | 384 (8.1) | 47 (3.6) | 390 (5.7) | 23 (3.0) | 389 (6.9) |
| Chinese Taipei |  | 37 (0.4) | 4 (1.5) | 598 (28.9) | 14 (2.8) | 567 (11.5) | 65 (4.0) | 575 (4.7) | 17 (3.2) | 636 (8.7) |
| Cyprus |  | 26 (0.1) | 21 (1.9) | 463 (3.2) | 79 (1.9) | 460 (2.0) | 0 (0.0) | ~ ~ | 0 (0.0) | ~ ~ |
| Egypt |  | 38 (0.6) | 3 (1.2) | 422 (13.8) | 9 (2.1) | 428 (11.3) | 61 (4.1) | 403 (4.3) | 27 (3.7) | 407 (7.5) |
| Estonia |  | 27 (0.5) | 32 (3.4) | 523 (5.1) | 41 (4.2) | 530 (4.3) | 27 (3.8) | 550 (5.4) | 0 (0.0) | ~ ~ |
| Ghana | $r$ | 37 (1.0) | 16 (2.7) | 232 (7.4) | 18 (3.1) | 249 (8.9) | 29 (4.0) | 292 (9.0) | 37 (4.7) | 289 (9.1) |
| Hong Kong, SAR |  | 39 (0.3) | 3 (1.1) | 504 (28.1) | 6 (1.6) | 513 (21.3) | 49 (4.1) | 575 (5.7) | 43 (4.1) | 612 (4.7) |
| Hungary |  | 22 (0.4) | 64 (3.9) | 522 (4.2) | 35 (4.0) | 540 (6.5) | 2 (0.9) | ~ ~ | 0 (0.0) | ~ ~ |
| Indonesia |  | 40 (0.5) | 3 (1.7) | 413 (8.6) | 10 (2.8) | 366 (20.0) | 38 (4.1) | 413 (8.3) | 48 (4.3) | 421 (6.7) |
| Iran, Islamic Rep. of |  | 29 (0.4) | 23 (2.9) | 397 (5.7) | 50 (4.0) | 413 (4.5) | 25 (3.3) | 420 (6.0) | 3 (1.4) | 431 (13.7) |
| Israel | $r$ | 34 (0.4) | 9 (2.2) | 512 (18.3) | 23 (3.7) | 500 (9.2) | 64 (4.5) | 490 (4.9) | 4 (1.7) | 531 (4.5) |
| Italy |  | 22 (0.3) | 78 (3.1) | 483 (3.4) | 22 (3.1) | 488 (8.3) | 0 (0.0) | ~ ~ | 0 (0.0) | ~~ |
| Japan |  | 35 (0.2) | 3 (1.2) | 561 (6.1) | 18 (2.6) | 557 (4.5) | 78 (2.6) | 571 (2.7) | 1 (1.0) | ~ ~ |
| Jordan |  | 35 (0.7) | 14 (2.8) | 430 (9.4) | 26 (3.6) | 424 (13.3) | 32 (4.4) | 417 (5.9) | 28 (3.8) | 428 (7.4) |
| Korea, Rep. of | s | 37 (0.4) | 1 (0.9) | ~ ~ | 20 (3.0) | 569 (4.6) | 57 (4.6) | 594 (2.9) | 22 (3.5) | 600 (7.0) |
| Latvia |  | 24 (0.7) | 52 (3.5) | 497 (4.4) | 42 (3.4) | 519 (5.5) | 3 (1.0) | 527 (20.3) | 3 (1.7) | 506 (12.6) |
| Lebanon |  | 29 (0.9) | 32 (3.9) | 429 (6.0) | 44 (4.8) | 429 (5.1) | 16 (3.1) | 443 (10.4) | 8 (3.1) | 464 (8.7) |
| Lithuania |  | 25 (0.3) | 39 (3.2) | 486 (4.2) | 61 (3.2) | 510 (3.0) | 0 (0.0) | ~ | 0 (0.0) | ~~ |
| Macedonia, Rep. of |  | 28 (0.4) | 24 (3.5) | 439 (9.2) | 58 (4.3) | 435 (5.9) | 17 (3.6) | 429 (13.7) | 1 (1.0) | $\sim \sim$ |
| Malaysia |  | 37 (0.4) | 1 (0.7) | ~ | 18 (3.3) | 514 (11.0) | 56 (4.4) | 503 (5.1) | 25 (3.5) | 515 (8.8) |
| Moldova, Rep. of | $r$ | 24 (0.5) | 56 (4.5) | 449 (6.0) | 38 (4.6) | 460 (7.0) | 5 (2.5) | 485 (25.2) | 1 (0.6) | ~ ~ |
| Morocco |  | x x | $\mathrm{x} \times$ | x x | x x | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x | $\mathrm{x} \times$ | x x |
| Netherlands |  | 26 (0.3) | 33 (3.9) | 514 (9.4) | 66 (4.1) | 546 (5.8) | 1 (1.0) | ~ ~ | 0 (0.0) | ~~ |
| New Zealand |  | 27 (0.4) | 22 (3.0) | 469 (8.9) | 72 (4.1) | 500 (5.7) | 6 (3.2) | 538 (17.8) | 0 (0.0) | ~ ~ |
| Norway |  | 25 (0.3) | 34 (3.8) | 467 (4.3) | 65 (3.6) | 460 (3.5) | 1 (0.7) | ~ ~ | 1 (0.7) | $\sim \sim$ |
| Palestinian Nat'l Auth. |  | 39 (0.6) | 6 (2.0) | 398 (20.0) | 17 (2.8) | 393 (7.4) | 27 (3.9) | 394 (8.9) | 50 (3.7) | 385 (4.2) |
| Philippines |  | 54 (0.7) | 1 (0.6) | ~ ~ | 1 (0.7) | ~ | 7 (2.0) | 448 (23.4) | 91 (2.1) | 372 (5.4) |
| Romania |  | 24 (0.5) | 51 (4.5) | 469 (6.7) | 46 (4.5) | 480 (7.4) | 3 (1.4) | 534 (34.7) | 1 (0.0) | ~ |
| Russian Federation |  | 24 (0.6) | 47 (4.2) | 500 (5.1) | 47 (3.6) | 515 (5.0) | 6 (3.4) | 533 (11.0) | 0 (0.0) | $\sim \sim$ |
| Saudi Arabia |  | 28 (0.9) | 36 (5.3) | 333 (7.5) | 26 (4.8) | 340 (8.1) | 29 (5.8) | 330 (5.6) | 8 (3.0) | 325 (4.1) |
| Scotland | $r$ | 27 (0.5) | 33 (3.9) | 457 (7.2) | 56 (4.4) | 520 (6.2) | 11 (3.4) | 548 (10.1) | 1 (0.7) | ~ ~ |
| Serbia |  | 26 (0.4) | 38 (3.7) | 464 (4.4) | 51 (4.0) | 483 (3.8) | 11 (2.9) | 489 (8.2) | 0 (0.0) | ~ ~ |
| Singapore |  | 38 (0.2) | 2 (0.6) | $\sim$ | 8 (1.6) | 613 (18.0) | 63 (2.7) | 606 (5.0) | 26 (2.5) | 607 (5.7) |
| Slovak Republic |  | 25 (0.4) | 42 (4.6) | 498 (4.7) | 53 (4.7) | 512 (5.4) | 5 (1.8) | 543 (19.7) | 0 (0.0) | ~ |
| Slovenia |  | 22 (0.3) | 70 (4.1) | 491 (3.0) | 30 (4.1) | 500 (4.1) | 0 (0.0) | ~ ~ | 0 (0.0) | ~ |
| South Africa | s | 45 (1.3) | 4 (1.2) | 309 (35.8) | 14 (3.0) | 290 (23.8) | 30 (3.7) | 265 (11.7) | 52 (4.1) | 249 (8.7) |
| Sweden |  | 21 (0.4) | 71 (3.6) | 491 (3.3) | 27 (3.7) | 522 (5.5) | 1 (1.0) | ~ ~ | 0 (0.5) | ~~ |
| Tunisia |  | 34 (0.3) | 1 (1.0) | ~ ~ | 26 (3.3) | 404 (3.6) | 71 (3.5) | 412 (3.2) | 2 (1.1) | $\sim \sim$ |
| United States | r | 24 (0.4) | 56 (2.9) | 504 (3.9) | 39 (2.7) | 510 (5.1) | 4 (1.2) | 531 (16.4) | 1 (0.7) | ~ ~ |
| \# England | S | 27 (0.5) | 33 (5.1) | 479 (11.6) | 57 (5.8) | 511 (8.7) | 10 (3.6) | 552 (16.5) | 0 (0.0) | ~ ~ |
| International Avg. |  | 30 (0.1) | 29 (0.5) | 461 (1.9) | 35 (0.5) | 473 (1.4) | 24 (0.5) | 470 (2.1) | 13 (0.3) | 448 (1.7) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 24 (0.4) | 49 (3.6) | 483 (4.2) | 47 (4.2) | 492 (4.3) | 4 (2.5) | 504 (2.6) | 0 (0.0) | $\sim \sim$ |
| Indiana State, US |  | 24 (1.0) | 65 (6.5) | 505 (6.3) | 31 (5.8) | 512 (8.0) | 0 (0.0) | ~ | 4 (2.5) | 517 (36.6) |
| Ontario Province, Can. |  | 26 (0.4) | 31 (4.0) | 515 (5.2) | 66 (4.1) | 523 (3.7) | 3 (2.0) | 514 (7.3) | 0 (0.0) | ~ ~ |
| Quebec Province, Can. |  | 29 (0.3) | 14 (2.8) | 530 (5.6) | 69 (3.9) | 539 (4.2) | 18 (3.0) | 573 (7.9) | 0 (0.0) | $\sim \sim$ |

## Background data provided by teachers.

\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

| Countries |  | Overall <br> Average Class Size | 1-19 Students |  | 20-26 Students |  | 27-32 Students |  | 33 or More Students |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | s | 29 (1.5) | 22 (4.1) | 467 (8.6) | 33 (4.2) | 462 (7.6) | 19 (4.3) | 456 (9.6) | 26 (4.8) | 457 (8.2) |
| Australia |  | 26 (0.6) | 16 (3.0) | 495 (9.6) | 29 (3.8) | 503 (6.7) | 53 (4.3) | 504 (5.6) | 2 (1.5) | ~ ~ |
| Belgium (Flemish) |  | 20 (0.4) | 43 (3.4) | 550 (3.6) | 50 (3.6) | 551 (2.3) | 6 (2.0) | 549 (4.9) | 1 (0.0) | ~ ~ |
| Chinese Taipei |  | 32 (0.3) | 2 (0.7) | ~ | 7 (2.0) | 546 (14.2) | 37 (4.0) | 565 (3.2) | 54 (3.7) | 567 (2.0) |
| Cyprus |  | 23 (0.3) | 18 (2.2) | 502 (4.0) | 56 (4.0) | 513 (3.9) | 25 (4.2) | 508 (4.7) | 0 (0.0) | ~ ~ |
| England | r | 28 (0.8) | 11 (2.7) | 514 (16.4) | 29 (4.7) | 528 (7.5) | 40 (4.1) | 534 (6.3) | 20 (4.4) | 539 (13.1) |
| Hong Kong, SAR |  | 34 (0.4) | 2 (0.9) | ~ ~ | 4 (1.7) | 544 (14.8) | 30 (4.0) | 566 (4.5) | 64 (4.3) | 584 (4.3) |
| Hungary |  | 24 (0.4) | 19 (3.0) | 508 (6.3) | 54 (4.1) | 523 (4.5) | 26 (4.0) | 550 (7.4) | 1 (0.9) | ~ ~ |
| Iran, Islamic Rep. of |  | 27 (0.6) | 16 (2.7) | 368 (9.8) | 28 (3.6) | 390 (6.4) | 26 (4.1) | 383 (10.4) | 30 (4.0) | 404 (6.7) |
| Italy |  | 20 (0.3) | 45 (3.4) | 508 (4.8) | 53 (3.4) | 499 (5.2) | 1 (0.7) | ~ ~ | 0 (0.0) | $\sim \sim$ |
| Japan |  | 32 (0.3) | 4 (0.9) | 572 (7.2) | 13 (2.3) | 560 (4.6) | 28 (3.0) | 566 (3.0) | 55 (2.9) | 564 (2.4) |
| Latvia |  | 23 (0.4) | 31 (3.1) | 521 (6.2) | 38 (3.8) | 529 (5.2) | 27 (2.9) | 561 (4.5) | 5 (1.9) | 561 (10.2) |
| Lithuania |  | 21 (0.4) | 30 (3.0) | 506 (6.6) | 59 (3.5) | 544 (3.3) | 11 (2.5) | 548 (7.6) | 0 (0.3) | ~ |
| Moldova, Rep. of | $r$ | 25 (0.5) | 16 (3.1) | 491 (9.6) | 49 (4.7) | 503 (8.0) | 30 (3.8) | 520 (8.9) | 5 (1.8) | 506 (25.6) |
| Morocco |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ | x x | x x | x $x$ |
| Netherlands |  | 23 (0.4) | 24 (3.4) | 544 (3.5) | 41 (4.6) | 540 (4.3) | 33 (4.2) | 542 (3.6) | 2 (1.5) | ~ ~ |
| New Zealand |  | 27 (0.3) | 10 (1.6) | 474 (8.9) | 24 (2.7) | 487 (5.4) | 56 (3.0) | 501 (3.2) | 9 (2.2) | 492 (9.6) |
| Norway |  | 21 (0.4) | 38 (3.2) | 446 (4.8) | 47 (3.5) | 451 (3.3) | 13 (3.2) | 464 (4.8) | 2 (1.3) | ~ ~ |
| Philippines |  | 40 (1.0) | 3 (1.0) | 336 (28.7) | 7 (2.4) | 350 (20.2) | 16 (3.8) | 388 (34.2) | 75 (4.2) | 353 (6.9) |
| Russian Federation |  | 21 (0.3) | 33 (3.2) | 524 (6.5) | 45 (3.6) | 539 (7.7) | 20 (2.5) | 523 (8.2) | 1 (0.9) | ~ ~ |
| Scotland | s | 26 (0.5) | 18 (3.5) | 482 (8.3) | 27 (4.5) | 489 (6.2) | 48 (4.5) | 498 (4.4) | 7 (2.5) | 505 (13.9) |
| Singapore |  | 38 (0.2) | 0 (0.1) | ~ ~ | 2 (0.8) | ~ ~ | 3 (1.0) | 506 (39.2) | 96 (1.2) | 598 (5.4) |
| Slovenia |  | 20 (0.4) | 45 (4.1) | 477 (4.7) | 49 (4.4) | 480 (4.0) | 6 (2.2) | 477 (7.8) | 0 (0.0) | ~ |
| Tunisia | $r$ | 31 (0.4) | 5 (1.5) | 319 (25.3) | 15 (2.9) | 331 (14.6) | 41 (4.2) | 341 (7.7) | 38 (4.3) | 344 (9.0) |
| United States |  | 23 (0.3) | 23 (2.5) | 519 (5.7) | 56 (3.0) | 523 (3.2) | 18 (2.3) | 509 (6.1) | 3 (1.1) | 513 (13.7) |
| International Avg. |  | 26 (0.1) | 20 (0.6) | 482 (2.5) | 34 (0.7) | 495 (1.8) | 26 (0.7) | 503 (2.6) | 21 (0.5) | 499 (3.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 22 (0.5) | 23 (5.3) | 533 (7.8) | 71 (5.8) | 535 (3.6) | 4 (2.0) | 534 (9.0) | 3 (2.2) | 522 (19.7) |
| Ontario Province, Can. |  | 25 (0.5) | 11 (2.8) | 503 (8.2) | 48 (5.5) | 520 (6.0) | 37 (5.2) | 503 (5.5) | 3 (1.5) | 497 (7.7) |
| Quebec Province, Can. |  | 26 (0.3) | 5 (1.6) | 518 (9.5) | 48 (4.6) | 503 (3.7) | 46 (4.6) | 509 (3.8) | 0 (0.0) | ~ ~ |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

## Exhibit 7.2: Index of Teachers' Reports on Teaching Mathematics Classes with Few or No

 Limitations on Instruction Due to Student Factors (MCFL)
## Index of Teachers' Reports on Teaching Mathematics Classes with Few or No Limitations on Instruction Due to Student Factors

Index based on teachers' responses to six statements about student factors limiting mathematics instruction: 1) Students with different academic abilities; 2) Students who come from a wide range of backgrounds; 3) Students with special needs; 4) Uninterested students; 5) Low morale among students;
6) Disruptive students. Average is computed across the six statements based on a 4 -point scale: 1 . Not at all/Not applicable; 2. A little; 3. Some; 4. A lot. High level indicates average is less than or equal to 2 . Medium level indicates average is greater than 2 and less than 3 . Low level indicates average is greater than or equal to 3.


[^65]
## How Much School Time Is Devoted to Mathematics Instruction?

Exhibit 7.3 presents information about the amount of mathematics instruction given to students at the eighth and fourth grades. Since different systems have school years of different lengths and different arrangements of weekly and daily instruction, the comparisons are given in terms of the average number of hours of mathematics instruction over the school year as reported by mathematics teachers. At the eighth grade, countries providing 150 or more hours per year were the Philippines, Indonesia, and Chile. Countries providing fewer than 100 hours were Bulgaria, the Netherlands, Sweden, Macedonia, and Cyprus. The percentage of instructional time at the eighth grade that was devoted to mathematics ranged from 17 percent in the Philippines to 8 percent in Cyprus.

At the fourth grade, even with fewer participating countries than at the eighth grade, a substantial number of countries provided 150 or more hours of mathematics instruction, including Italy, Belgium (Flemish), Scotland, the Netherlands, Australia, Singapore, and the Philippines. Even though Chinese Taipei was at 99 hours, the rest of the countries provided at least 110 hours of mathematics instruction per year. The percentage of instructional time at the fourth grade that was devoted to mathematics ranged from 21 percent in Italy to 12 percent in Chinese Taipei.

Exhibit 7.4 provides teachers' reports about how mathematics instructional time is allocated across the five major content areas assessed by TIMSS 2003. At the eighth grade, on average, internationally, the two areas receiving about one-fourth of the instructional time each were algebra with 27 percent and geometry with 26 percent. Number was next with 21 percent. Measurement and data each were given 10 percent and other topics 6 percent. At the fourth grade, the profile was much different. As would be anticipated, number received the largest amount of mathematics instructional time - 38 percent, on average, internationally. Patterns and relationships (beginning algebra), measurement, and geometry each were given 15 to 16 percent, data 9 percent, and other 6 percent.

## Exhibit 7.3: Mathematics Instructional Time

| Countries | Students' Average Yearly Mathematics Instructional Time in Hours |  |  | Mathematics Instructional Time as a Percent of Total Instructional Time ${ }^{1}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Philippines | $\bigcirc$ |  | 193 (3.6) |  | 17 (0.4) |
| Indonesia | $\bigcirc$ | s | 169 (4.4) |  | 13 (0.4) |
| Chile | $\bigcirc$ | r | 160 (4.1) | r | 14 (0.4) |
| Hong Kong, SAR | $\bigcirc$ | s | 145 (5.2) |  | 15 (0.5) |
| Scotland | $\bigcirc$ | s | 142 (2.2) |  | 14 (0.2) |
| Bahrain | $\bigcirc$ |  | 142 (0.8) |  | 16 (0.1) |
| Chinese Taipei | $\bigcirc$ |  | 141 (2.0) |  | 13 (0.2) |
| Australia | $\bigcirc$ | r | 136 (2.9) | $r$ | 13 (0.3) |
| New Zealand | $\bigcirc$ |  | 136 (1.7) |  | 14 (0.2) |
| United States | $\bigcirc$ | s | 135 (2.2) |  | 13 (0.2) |
| Italy | $\bigcirc$ | r | 132 (1.7) | r | 13 (0.2) |
| Russian Federation | $\bigcirc$ | r | 128 (2.1) | r | 15 (0.3) |
| Palestinian Nat'l Auth. | $\bigcirc$ | s | 127 (2.3) |  | 14 (0.3) |
| Slovak Republic | - | r | 126 (1.9) | r | 14 (0.3) |
| Estonia | $\bigcirc$ |  | 125 (1.2) |  | 12 (0.2) |
| Belgium (Flemish) | $\bigcirc$ | s | 123 (2.2) |  | 13 (0.3) |
| Latvia | $\bigcirc$ | s | 122 (1.4) |  | 13 (0.3) |
| Lithuania | $\bigcirc$ | r | 122 (0.9) | r | 11 (0.2) |
| Romania | $\bigcirc$ | r | 120 (2.1) | r | 13 (0.3) |
| Malaysia | 0 |  | 120 (1.4) |  | 12 (0.1) |
| Slovenia | $\bigcirc$ |  | 116 (1.3) |  | 11 (0.1) |
| Iran, Islamic Rep. of | $\bigcirc$ | s | 115 (3.5) |  | 12 (0.4) |
| Singapore | $\bigcirc$ |  | 114 (1.6) |  | 13 (0.2) |
| Norway | $\bigcirc$ |  | 114 (2.3) |  | 13 (0.3) |
| Hungary | $\bigcirc$ | s | 112 (2.0) |  | 11 (0.2) |
| Jordan | $\bigcirc$ |  | 110 (0.9) |  | 12 (0.2) |
| Saudi Arabia | $\bigcirc$ | s | 110 (1.0) |  | 11 (0.2) |
| Korea, Rep. of | - | s | 109 (1.2) |  | 9 (0.1) |
| Serbia | $\bigcirc$ | s | 107 (1.5) |  | 13 (0.2) |
| Japan | $\bigcirc$ |  | 107 (2.6) |  | 10 (0.2) |
| Bulgaria | $\bigcirc$ | r | 96 (1.7) | $r$ | 11 (0.2) |
| Netherlands | - | s | 94 (1.4) |  | 9 (0.1) |
| Sweden | 0 | r | 91 (1.6) | r | 10 (0.2) |
| Macedonia, Rep. of | $\bigcirc$ | r | 80 (1.2) | r | 9 (0.2) |
| Cyprus | $\bigcirc$ | s | 75 (0.4) |  | 8 (0.1) |
| Armenia |  |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Botswana |  |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Egypt |  |  | x x |  | x x |
| Ghana |  |  | X x |  | x x |
| Israel |  |  | X x |  | x x |
| Lebanon |  |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Moldova, Rep. of |  |  | x x |  | x x |
| Morocco |  |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| South Africa |  |  | X X |  | $\mathrm{x} \times$ |
| Tunisia |  |  | X X |  | $\mathrm{x} \times$ |
| \# England |  |  | x x |  | x x |
| International Avg. |  |  | 123 (0.4) |  | 12 (0.0) |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | $\longrightarrow$ |  | 123 (2.4) |  | 12 (0.3) |
| Indiana State, US | $\longrightarrow$ |  | 146 (3.2) |  | 13 (0.3) |
| Ontario Province, Can. | $\bigcirc$ | r | 166 (4.3) | r | 17 (0.5) |
| Quebec Province, Can. | $\bigcirc$ | r | 156 (3.8) | r | 17 (0.4) |
|  | 70 | 280 |  |  |  |

[^66]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data are available for at least 50 but less than $70 \%$ of the students. $A n$ " $x$ " indicates data are available for less than $50 \%$ of the students.

## Exhibit 7.3: Mathematics Instructional Time




Mathematics instructional time provided by teachers, and total instructional time provided by schools.
1 Computed as the ratio of mathematics instructional time to the total instructional time averaged across students ( 1 hour $=60$ minutes)
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 7.4: Percentage of Time in Mathematics Class Devoted to TIMSS Content Areas During the School Year

| Countries |  | Number |  | Algebra |  | Measurement |  | Geometry |  | Data |  | Other |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | s | 32 (1.7) | 5 | 21 (1.1) | s | 9 (0.5) | s | 20 (1.0) | s | 11 (0.6) | 5 | 7 (0.8) |
| Australia |  | 25 (0.8) |  | 23 (0.6) |  | 16 (0.5) |  | 18 (0.8) |  | 14 (0.6) |  | 4 (0.7) |
| Bahrain |  | 23 (0.5) |  | 26 (0.6) |  | 9 (0.4) |  | 27 (0.4) |  | 11 (0.3) |  | 5 (0.4) |
| Belgium (Flemish) |  | 30 (1.1) |  | 20 (0.8) |  | 6 (0.4) |  | 36 (0.6) |  | 5 (0.3) |  | 2 (0.5) |
| Botswana |  | 29 (1.4) |  | 20 (0.7) | $r$ | 16 (0.9) |  | 16 (0.8) |  | 12 (0.8) | $r$ | 9 (0.9) |
| Bulgaria |  | 10 (0.8) |  | 38 (1.2) |  | 6 (0.6) |  | 37 (1.1) |  | 4 (0.5) |  | 5 (1.0) |
| Chile |  | 39 (1.1) |  | 15 (0.6) |  | 10 (0.6) |  | 24 (0.7) |  | 9 (0.6) |  | 4 (0.7) |
| Chinese Taipei |  | 16 (1.0) |  | 35 (1.0) |  | 7 (0.5) |  | 38 (1.4) |  | 3 (0.4) |  | 1 (0.5) |
| Cyprus |  | 27 (0.6) |  | 27 (0.5) |  | 11 (0.4) |  | 22 (0.5) |  | 5 (0.4) | $r$ | 8 (0.7) |
| Egypt |  | 20 (0.6) |  | 21 (0.6) |  | 13 (0.4) |  | 22 (0.5) |  | 13 (0.4) |  | 10 (0.7) |
| Estonia |  | 15 (0.9) |  | 39 (1.1) |  | 9 (0.4) |  | 26 (0.7) |  | 7 (0.4) |  | 5 (0.8) |
| Ghana |  | 21 (0.8) |  | 19 (0.6) |  | 14 (0.5) |  | 20 (0.7) |  | 19 (0.7) |  | 7 (0.6) |
| Hong Kong, SAR |  | 16 (0.7) |  | 32 (0.8) |  | 12 (0.7) |  | 28 (0.8) |  | 10 (0.6) |  | 2 (0.6) |
| Hungary |  | 22 (0.7) |  | 26 (0.7) |  | 9 (0.3) |  | 28 (0.5) |  | 10 (0.4) |  | 5 (0.5) |
| Indonesia |  | 19 (0.6) |  | 23 (0.7) |  | 13 (0.4) |  | 24 (0.6) |  | 15 (0.4) |  | 6 (0.7) |
| Iran, Islamic Rep. of |  | 20 (0.7) |  | 22 (0.8) |  | 11 (0.4) |  | 27 (0.5) |  | 11 (0.5) |  | 9 (0.8) |
| Israel |  | 15 (0.9) |  | 34 (1.1) |  | 9 (0.7) |  | 28 (0.9) |  | 10 (0.5) | $r$ | 5 (0.8) |
| Italy |  | 14 (0.5) |  | 33 (0.6) |  | 10 (0.5) |  | 28 (0.7) |  | 11 (0.4) |  | 4 (0.9) |
| Japan |  | 17 (1.0) |  | 31 (1.0) |  | 4 (0.5) |  | 34 (0.6) |  | 12 (0.9) |  | 2 (0.5) |
| Jordan |  | 24 (0.9) |  | 23 (0.6) |  | 13 (0.5) |  | 21 (0.8) |  | 14 (0.5) |  | 5 (0.7) |
| Korea, Rep. of | $s$ | 18 (0.6) | s | 27 (0.6) | s | 12 (0.5) | s | 26 (0.6) | s | 15 (0.4) | s | 2 (0.3) |
| Latvia |  | 14 (0.8) |  | 39 (1.3) | s | 6 (0.6) |  | 30 (0.7) |  | 6 (0.5) |  | 5 (1.1) |
| Lebanon | s | 21 (1.1) | 5 | 21 (0.9) | 5 | 9 (0.8) | s | 35 (1.2) | s | 11 (0.8) | s | 3 (0.6) |
| Lithuania |  | 18 (0.7) |  | 34 (0.9) |  | 9 (0.3) |  | 23 (0.6) |  | 11 (0.4) |  | 4 (0.5) |
| Macedonia, Rep. of |  | 13 (0.9) |  | 26 (1.1) |  | 8 (1.1) |  | 38 (1.8) |  | 7 (0.5) |  | 8 (1.5) |
| Malaysia |  | 25 (0.9) |  | 22 (0.6) |  | 14 (0.5) |  | 20 (0.6) |  | 14 (0.5) |  | 6 (0.9) |
| Moldova, Rep. of | s | 17 (0.9) | 5 | 29 (0.8) | s | 10 (0.7) | s | 30 (0.9) | s | 9 (0.6) | s | 6 (0.9) |
| Morocco |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Netherlands |  | 16 (0.7) |  | 29 (1.2) |  | 13 (0.7) |  | 22 (0.8) |  | 14 (0.6) |  | 5 (0.8) |
| New Zealand |  | 25 (0.6) |  | 23 (0.8) |  | 17 (0.6) |  | 19 (0.4) |  | 14 (0.7) |  | 3 (0.6) |
| Norway |  | 27 (0.7) |  | 17 (0.7) |  | 12 (0.4) |  | 24 (0.6) |  | 13 (0.5) |  | 8 (0.8) |
| Palestinian Nat'l Auth. |  | 19 (0.7) |  | 21 (0.7) |  | 10 (0.5) |  | 24 (0.7) |  | 17 (0.6) |  | 11 (0.9) |
| Philippines |  | 21 (1.1) |  | 42 (1.9) |  | 12 (0.6) |  | 12 (0.7) |  | 10 (0.6) |  | 3 (0.7) |
| Romania |  | 18 (0.7) |  | 27 (0.7) |  | 9 (0.5) |  | 33 (0.9) |  | 8 (0.4) |  | 4 (0.7) |
| Russian Federation |  | 10 (0.8) |  | 49 (0.9) |  | - - |  | 35 (0.6) |  | 3 (0.4) |  | 2 (0.5) |
| Saudi Arabia |  | 29 (0.9) |  | 21 (0.6) |  | 8 (0.8) |  | 29 (1.0) |  | 8 (0.6) |  | 6 (0.8) |
| Scotland |  | - - |  | - - |  | - - |  | - - |  | - |  | - - |
| Serbia |  | 17 (1.0) |  | 25 (1.0) |  | 6 (0.6) | $r$ | 28 (1.8) |  | 6 (0.6) | $r$ | 19 (2.3) |
| Singapore |  | 13 (0.4) |  | 34 (0.7) |  | 13 (0.4) |  | 21 (0.4) |  | 11 (0.3) |  | 8 (0.5) |
| Slovak Republic |  | 16 (0.8) |  | 37 (1.1) |  | 7 (0.6) |  | 25 (1.0) |  | 7 (0.4) |  | 8 (1.1) |
| Slovenia |  | 38 (1.3) |  | 19 (0.8) |  | 11 (0.6) |  | 17 (0.9) |  | 8 (0.5) |  | 7 (1.2) |
| South Africa | $r$ | 23 (0.7) | $r$ | 23 (0.8) | $r$ | 13 (0.6) | $r$ | 23 (0.7) | $r$ | 14 (0.5) | $r$ | 4 (0.4) |
| Sweden |  | 34 (0.8) |  | 20 (0.7) |  | 12 (0.5) |  | 21 (0.4) |  | 10 (0.5) |  | 4 (0.6) |
| Tunisia |  | 34 (0.9) |  | 13 (0.6) |  | 7 (0.4) |  | 33 (0.7) |  | 7 (0.5) | $r$ | 6 (0.7) |
| United States |  | 22 (0.7) |  | 41 (1.3) |  | 10 (0.4) |  | 15 (0.6) |  | 12 (0.5) | $r$ | 2 (0.3) |
| ま England |  | - |  | - - |  | - - |  | - - |  | - - |  | -- |
| International Avg. |  | 21 (0.1) |  | 27 (0.1) |  | 10 (0.1) |  | 26 (0.1) |  | 10 (0.1) |  | 6 (0.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 34 (1.1) |  | 29 (1.0) |  | 10 (0.7) |  | 17 (0.7) |  | 8 (0.6) |  | 2 (0.5) |
| Indiana State, US |  | 27 (1.3) |  | 38 (1.6) |  | 10 (0.4) |  | 13 (1.2) |  | 10 (0.6) |  | 1 (0.3) |
| Ontario Province, Can. |  | 27 (0.7) |  | 20 (0.4) |  | 18 (0.4) |  | 18 (0.4) |  | 16 (0.4) |  | 1 (0.4) |
| Quebec Province, Can. |  | 23 (0.7) |  | 29 (0.7) |  | 12 (0.5) |  | 28 (0.8) |  | 8 (0.5) | $r$ | 2 (0.5) |

Background data provided by teachers.
\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

## Exhibit 7.4: Percentage of Time in Mathematics Class Devoted to TIMSS Content Areas During the School Year



| Countries |  | Number |  | Patterns and Relationships |  | Measurement |  | Geometry |  | Data |  | Other |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $r$ | 35 (1.3) | $r$ | 21 (0.8) | r | 13 (0.5) | r | 13 (0.5) | $r$ | 10 (0.5) | $r$ | 8 (0.8) |
| Australia |  | 40 (1.9) |  | 18 (0.9) |  | 17 (0.6) |  | 12 (0.6) |  | 11 (0.4) |  | 3 (0.5) |
| Belgium (Flemish) |  | 44 (1.1) |  | 14 (0.6) |  | 16 (0.3) |  | 14 (0.4) |  | 11 (0.5) |  | 2 (0.4) |
| Chinese Taipei |  | 39 (1.2) |  | 15 (0.6) |  | 17 (0.4) |  | 16 (0.4) |  | 11 (0.4) |  | 3 (0.4) |
| Cyprus |  | 35 (1.0) |  | 18 (0.5) |  | 14 (0.4) |  | 14 (0.4) |  | 14 (0.4) |  | 6 (0.8) |
| England |  | - - |  | - - |  | - - |  | - - |  | - - |  | - - |
| Hong Kong, SAR |  | 53 (1.7) |  | 13 (0.8) |  | 11 (0.5) |  | 12 (0.6) |  | 11 (0.5) |  | 1 (0.4) |
| Hungary |  | 42 (1.1) |  | 20 (0.6) |  | 15 (0.4) |  | 11 (0.4) |  | 7 (0.3) |  | 6 (0.9) |
| Iran, Islamic Rep. of |  | 22 (1.0) |  | 17 (0.6) |  | 16 (0.7) |  | 18 (0.8) |  | 16 (0.6) |  | 12 (1.0) |
| Italy |  | 33 (0.8) |  | 13 (0.4) |  | 19 (0.4) |  | 18 (0.4) |  | 11 (0.4) |  | 6 (0.6) |
| Japan |  | 40 (0.9) |  | 18 (0.8) |  | 13 (0.5) |  | 17 (0.5) |  | 12 (0.5) |  | 1 (0.3) |
| Latvia | s | 38 (1.6) | s | 19 (1.1) | s | 13 (0.6) | s | 12 (0.6) | s | 10 (0.6) | s | 9 (1.0) |
| Lithuania |  | 38 (1.3) |  | 16 (0.6) |  | 16 (0.5) |  | 12 (0.5) |  | 12 (0.5) |  | 6 (0.8) |
| Moldova, Rep. of | $r$ | 30 (1.3) | $r$ | 18 (0.6) | $r$ | 14 (0.5) | $r$ | 14 (0.5) | $r$ | 13 (0.6) | r | 11 (1.0) |
| Morocco |  | x x |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |
| Netherlands |  | 52 (1.6) |  | 13 (0.8) |  | 14 (0.6) |  | 7 (0.4) |  | 11 (0.6) |  | 3 (0.5) |
| New Zealand |  | 49 (1.1) |  | 13 (0.4) |  | 13 (0.4) |  | 12 (0.4) |  | 11 (0.3) |  | 3 (0.5) |
| Norway |  | 57 (1.3) |  | 10 (0.4) |  | 14 (0.6) |  | 9 (0.4) |  | 7 (0.4) |  | 3 (0.5) |
| Philippines |  | 29 (1.3) |  | 20 (0.6) |  | 16 (0.5) |  | 15 (0.6) |  | 15 (0.7) |  | 6 (0.7) |
| Russian Federation |  | -- |  | - |  | - - |  | - |  | - - |  | - |
| Scotland |  | - - |  | - |  | - - |  | - - |  | - - |  | - - |
| Singapore |  | 49 (1.3) |  | 14 (0.7) |  | 13 (0.5) |  | 11 (0.5) |  | 9 (0.3) |  | 5 (0.7) |
| Slovenia |  | 21 (1.2) |  | 18 (1.1) |  | 22 (0.9) |  | 10 (0.5) |  | 11 (0.5) |  | 18 (1.5) |
| Tunisia | $r$ | 25 (1.3) | $r$ | 19 (0.8) | $r$ | 20 (0.6) | $r$ | 18 (0.6) | $r$ | 13 (0.6) | $r$ | 5 (0.7) |
| United States |  | 38 (0.9) |  | 19 (0.4) |  | 13 (0.3) |  | 13 (0.3) |  | 15 (0.4) |  | 4 (0.5) |
| International Avg. |  | 38 (0.3) |  | 16 (0.2) |  | 15 (0.1) |  | 13 (0.1) |  | 11 (0.1) |  | 6 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 44 (2.2) |  | 18 (1.3) |  | 12 (0.7) |  | 11 (0.6) |  | 11 (0.7) |  | 3 (0.8) |
| Ontario Province, Can. |  | 34 (1.0) |  | 16 (0.4) |  | 17 (0.4) |  | 16 (0.4) |  | 15 (0.4) |  | 2 (0.5) |
| Quebec Province, Can. |  | 40 (1.4) |  | 16 (0.8) |  | 15 (0.4) |  | 16 (0.5) |  | 9 (0.5) |  | 4 (0.7) | some totals may appear inconsistent.

A dash $(-)$ indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

## What Activities Do Students Do in Their Mathematics Lessons?

Exhibits 7.5 and 7.6 present information about the frequency of students doing particular content related activities, as reported by the students themselves and by their mathematics teachers, respectively. The data presented are for doing the activities in half of their lessons or more. At the eighth grade, the activities were: 1) practicing numerical operations without a calculator, 2) working on fractions and decimals, 3) interpreting data in tables, charts, or graphs, and 4) writing equations and functions to represent relationships. According to the eighth-grade students, internationally, on average, considerable effort was devoted to working on the two activities most likely related to the number content area. Fifty-seven percent of the students reported being asked to practice numerical operations in at least half of their lessons and another 51 percent reported working on fractions and decimals at least this frequently. Fifty-five percent reported writing equations and functions in half their lessons. The smallest percentage of students spent time on data interpretation tasks in at least half their lessons ( $41 \%$ ). Teachers' reports agreed with that of their students when it came to the emphasis on number activities. For doing the activities in at least half of the lessons, teachers reported the largest percentages of students for practicing operations ( $62 \%$ ) and working on fractions and decimals ( $43 \%$ ). In contrast to students' views, teachers reported less emphasis on writing equations (30\%) and far less on data interpretation (17\%).

At the fourth grade, the activities were: 1) practicing operations, 2) working on fractions and decimals, 3) measuring things, 4) making tables charts or graphs, and 5) learning about shapes such as circles, triangles, rectangles, and cubes. Similar to the eighth-grade reports, students reported a much more balanced approach. The international averages were two-thirds of the students practicing operations in at least half the lessons and more than half (54\%) working on fractions and decimals and learning about shapes. According to the students, 39 percent, on average, were making graphs in more than half their
lessons, and one-fourth were measuring things. In contrast, teachers reported an overwhelming emphasis on having students practice numerical operations. The teachers said they asked 82 percent of the students, on average, internationally, to practice adding, subtracting, multiplying, or dividing in half of the lessons or more. They reported asking 29 percent, on average, internationally, to work on fractions and decimals this frequently. According to teachers, measuring things, making graphs, and learning about shapes were relatively infrequent activities for more than 80 percent of the fourth-grade students.

Exhibit 7.5: Students' Reports on Mathematics Content Related Emphasis in Classroom Activities



Percentage of Students Who Reported Doing the Activity About Half of the Lessons or More

|  |  |
| :--- | :--- |
| Armenia |  |
| Australia |  |
| Bahrain |  |
| Belgium (Flemish) |  |
| Botswana |  |
| Bulgaria |  |

Chile

| Cyprus |
| :--- |
| Egypt |


| Estonia | $50(1.3)$ |
| :--- | :--- |
| Ghana | $63(1.3)$ |


| Hong Kong, SAR |
| :--- |
| Hungary |

Indonesia
67 (1.2)
7 (1.2)
Iran, Islamic Rep. of
Israel
58 (1.2)
61 (1.2)
Ital
Jordan
Korea, Rep. of
Latvia
Lebanon
43 (1.5)
$6(0.6) \square$
60

| Lebanon |
| :--- |
| Lithuania |

Macedonia, Rep. of
Malaysia

| Moldova, Rep. of | $72(1.1)$ |
| :--- | :--- |

Morocco

| Netherlands |
| :--- |
| New Zealand |
| Norway |

Palestinian Nat'l Auth.
Philippines
n

Saudi Arabia
Scotland
60 (0.9)
$81(0.7) \quad 40$
$78(0.9)$
$58(1.5)$
$\begin{array}{r}73 \\ 58 \\ \hline\end{array}$
$46(1.5) \square$
56
$61(1.4) \quad \square$
51
64

| $12(1.1)$ |
| :--- |
| $46(1.3)$ |
| $21(0.9)$ |

45

| $\square$ |
| :--- |
| $(1.1)$ |

Serbia
Singapore
Stoval

| Slovak Republic | $55(1.2)$ | $47(1.1)$ | $18(1.0)$ | $65(1.1)$ |
| :--- | :--- | :--- | :--- | :--- |
| Slovenia | $57(1.3)$ | $61(1.5)$ | $40(1.6)$ | $46(1.2)$ |
| South Africa | $70(0.7)$ | $66(1.0)$ | $54(1.1)$ | $62(1.0)$ |
| Sweden | $37(1.3)$ | $37(1.3)$ | $25(1.3)$ | $30(1.3)$ |
| Tunisia | $54(0.9)$ | $66(0.8)$ | $42(0.9)$ | $45(0.9)$ |
| United States | $63(0.9)$ | $66(0.9)$ | $55(1.2)$ | $73(1.0)$ |
| England | $43(1.1)$ | $31(1.3)$ | $33(1.5)$ | $38(1.7)$ |
| International Avg. | $57(0.2)$ | $51(0.2)$ | $41(0.2)$ | $55(0.2)$ |

Benchmarking Participants

| Basque Country, Spain | $79(1.4)$ | $76(1.1)$ | $53(2.0)$ | $77(1.4)$ |
| :--- | :--- | :--- | :--- | :--- |
| Indiana State, US | $67(1.8)$ | $72(1.5)$ | $54(2.1)$ | $74(1.9)$ |
| Ontario Province, Can. | $51(1.7)$ | $50(1.4)$ | $41(1.7)$ | $53(1.3)$ |
| Quebec Province, Can. | $33(1.5)$ | $51(1.6)$ | $32(1.3)$ | $57(1.2)$ |

[^67]\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 7.5: Students' Reports on Mathematics Content Related Emphasis in Classroom Activities


| Countries | Percentage of Students Who Reported Doing the Activity About Half of the Lessons or More |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Practice Adding, ubtracting, Multiplying, and Dividing Without Using Calculator |  | Work on Fractions and Decimals |  | Measure Things in the Classroom and Around the School |  | Make Tables, Charts, or Graphs |  | Learn about Shapes such as Circles, Triangles, Rectangles, and Cubes |
| Armenia | r | 68 (1.1) | r | 76 (1.2) | s | 20 (1.0) | 5 | 34 (1.2) | s | 64 (1.4) |
| Australia |  | 75 (1.1) |  | 58 (1.7) |  | 29 (1.2) |  | 42 (1.4) |  | 52 (1.6) |
| Belgium (Flemish) |  | 74 (1.2) |  | 60 (1.3) |  | 14 (0.7) |  | 23 (1.4) |  | 51 (1.6) |
| Chinese Taipei |  | 50 (1.1) |  | 45 (1.1) |  | 29 (1.0) |  | 37 (1.1) |  | 52 (1.2) |
| Cyprus |  | 69 (0.9) |  | 69 (1.0) |  | 45 (1.2) |  | 58 (1.0) |  | 69 (1.0) |
| England |  | 63 (1.1) |  | 42 (1.6) |  | 12 (0.9) |  | 36 (1.5) |  | 33 (1.3) |
| Hong Kong, SAR |  | 53 (1.6) |  | 53 (1.1) |  | 16 (1.0) |  | 25 (1.0) |  | 46 (1.1) |
| Hungary |  | 72 (1.0) |  | 32 (1.6) |  | 12 (0.7) |  | 16 (1.0) |  | 53 (1.7) |
| Iran, Islamic Rep. of |  | 58 (2.8) |  | 64 (2.8) |  | 51 (2.3) |  | 58 (2.6) |  | 72 (2.4) |
| Italy |  | 61 (1.3) |  | 60 (1.4) |  | 21 (1.1) |  | 49 (1.6) |  | 72 (1.5) |
| Japan |  | 80 (0.9) |  | 74 (1.4) |  | 27 (0.9) |  | 50 (1.4) |  | 57 (1.3) |
| Latvia |  | 73 (1.1) |  | 46 (1.7) |  | 19 (1.0) |  | 33 (1.4) |  | 62 (1.3) |
| Lithuania |  | 76 (1.0) |  | 60 (1.4) |  | 11 (0.7) |  | 37 (1.4) |  | 57 (1.1) |
| Moldova, Rep. of |  | 65 (2.1) |  | 42 (2.1) |  | 15 (1.1) |  | 36 (2.0) |  | 49 (2.3) |
| Morocco | $r$ | 75 (2.1) | $r$ | 61 (2.8) | $r$ | 49 (2.3) | $r$ | 56 (2.6) | $r$ | 64 (2.5) |
| Netherlands |  | 74 (1.4) |  | 36 (1.8) |  | 9 (0.9) |  | 29 (1.5) |  | 15 (0.9) |
| New Zealand |  | 74 (0.8) |  | 58 (1.3) |  | 31 (1.2) |  | 48 (1.2) |  | 52 (1.1) |
| Norway |  | 56 (1.1) |  | 36 (1.6) |  | 13 (0.7) |  | 21 (1.2) |  | 41 (1.0) |
| Philippines |  | 66 (1.8) |  | 73 (1.4) |  | 45 (1.5) |  | 49 (1.5) |  | 74 (1.6) |
| Russian Federation |  | -- |  | -- |  | -- |  | -- |  | - - |
| Scotland |  | 73 (1.0) |  | 38 (1.7) |  | 25 (1.3) |  | 42 (1.5) |  | 43 (1.5) |
| Singapore |  | 77 (0.9) |  | 73 (1.0) |  | 14 (0.6) |  | 29 (0.9) |  | 47 (1.2) |
| Slovenia |  | 59 (1.3) |  | 40 (1.8) |  | 18 (1.1) |  | 26 (1.2) |  | 50 (1.9) |
| Tunisia | $r$ | 53 (2.0) | $r$ | 25 (1.8) | $r$ | 46 (2.2) | $r$ | 50 (2.6) | $r$ | 62 (2.3) |
| United States |  | 74 (0.7) |  | 64 (1.1) |  | 28 (0.8) |  | 51 (1.0) |  | 56 (1.0) |
| International Avg. |  | 67 (0.3) |  | 54 (0.3) |  | 25 (0.3) |  | 39 (0.3) |  | 54 (0.3) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 76 (1.2) |  | 66 (2.5) |  | 22 (1.4) |  | 43 (1.9) |  | 50 (1.8) |
| Ontario Province, Can. |  | 72 (1.0) |  | 58 (2.3) |  | 30 (1.3) |  | 53 (1.3) |  | 53 (1.6) |
| Quebec Province, Can. |  | 76 (0.9) |  | 57 (1.8) |  | 31 (1.4) |  | 45 (1.5) |  | 63 (1.4) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash ( - ) indicates comparable data are not available.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

Exhibit 7.6: Teachers' Reports on Mathematics Content Related Emphasis in Students' Classroom Activities


| Armenia |
| :--- |
| Australia |

Bahrain
Belgium (Flemish)
Botswana
Bulgaria
Chile
Chinese Taipei
Cyprus
Estonia
Ghana
Hong Kong, SAR
Hungary
Indonesia
Iran, Islamic Rep. of

| Israe |
| :--- |
| Italy |
| Japan |


| Japan |  |
| :--- | :--- |
| Jordan |  |
| Korea, Rep. of | s |


| Latvia | 86 |
| :--- | :--- |
| Lebanon | 5 |
| Lithuania | 66 |


| Lithuania |
| :--- |
| Macedonia, Rep. of |
| Malaysia |


| Moldova, Rep. of | $r$ |
| :--- | :--- |
| Morocco | $s$ |
| Netherlands |  |


| Netherlands |
| :--- | :--- |
| New Zealand |
| Norway |


| Palestinian Nat'l Auth. |
| :--- |
| Philippines |
| Romania |


| New Zealand | $40(4.2)$ | $24(4.3)$ | $12(3.6)$ | $15(4.4)$ |
| :--- | ---: | ---: | ---: | ---: |
| Norway | $5(2.0)$ | $5(2.1)$ | $2(1.1)$ | $4(1.5)$ |
| Palestinian Nat'I Auth. | $71(3.8)$ | $33(4.1)$ | $28(4.0)$ | $24(4.1)$ |
| Philippines | $73(4.3)$ | $52(4.9)$ | $26(3.8)$ | $46(4.3)$ |
| Romania | $85(3.2)$ | $67(4.4)$ | $13(2.8)$ | $32(3.8)$ |
| Russian Federation | $85(2.4)$ | $70(3.6)$ | $20(3.1)$ | $51(3.7)$ |
| Saudi Arabia | $85(3.5)$ | $32(4.2)$ | $25(4.6)$ | $21(4.2)$ |
| Scotland | $63(4.5)$ | $25(4.0)$ | $8(2.7)$ | $5(2.4)$ |
| Serbia | $74(3.6)$ | $59(3.9)$ | $15(3.0)$ | $45(3.6)$ |
| Singapore | $38(2.5)$ | $26(2.3)$ | $10(1.6)$ | $37(2.8)$ |
| Slovak Republic | $57(4.0)$ | $56(4.5)$ | $5(1.7)$ | $35(4.5)$ |
| Slovenia | $71(3.9)$ | $66(4.0)$ | $6(1.9)$ | $12(2.3)$ |
| South Africa | $63(3.4)$ | $26(3.6)$ | $23(3.0)$ | $25(3.5)$ |
| Sweden | $43(3.7)$ | $25(3.3)$ | $6(1.8)$ | $6(1.8)$ |
| Tunisia | $75(3.4)$ | $50(4.7)$ | $11(2.5)$ | $16(3.1)$ |
| United States | $46(2.6)$ | $45(3.1)$ | $25(2.5)$ | $47(2.9)$ |
| England | $50(5.7)$ | s | $19(4.4)$ | 5 |
| International Avg. | $62(0.5)$ | $43(0.6)$ | $9(3.2)$ | 5 |

Benchmarking Participants Basque Country, Spain Indiana State, US Ontario Province, Can.
Quebec Province, Can.
$75(4.1)$
$64(4.8)$
$37(4.5)$
$19(3.9)$

19 (3.9)

Percentage of Students Whose Teachers Reported Students Doing the Activity About Half of the Lessons or More
 or Graph

13 (2.9)
8 (2.2)
$1(0.5)$
9 (2.6) $\square$

3 (1.1)
$80(3.6)$
$85(3.3)$
$70(3.8) \quad \square$
$69(2.2)$
$44(3.7)$
4
$\square$
$0(2.1)$
0

| $63(4.3)$ | $61(4.4)$ |
| :--- | :--- |
| $73(4.2)$ | $37(4.2)$ |


| $10(2.8)$ | $6(2.2)$ | $22(3.9)$ | $30(4.5)$ |
| :--- | ---: | ---: | ---: |
| $75(3.2)$ | $80(3.4)$ | $5(2.2)$ | $32(4.2)$ |
| $48(4.2)$ | $31(3.7)$ | $30(4.3)$ | $48(4.8)$ |


| $77(3.0)$ | $50(3.8)$ | $41(3.8)$ | $33(3.9)$ |
| :--- | :--- | :--- | :--- |
| $53(3.8)$ | $44(3.8)$ | $27(3.1)$ | $34(3.9)$ |
| $53(3.5)$ | $62(3.5)$ | $20(3.0)$ | $22(2.8)$ |


| $53(4.3)$ | $11(2.6)$ | $36(3.7)$ | $62(3.7)$ |
| :--- | :--- | :--- | :--- |
| $76(3.3)$ | $41(4.3)$ | $27(3.9)$ | $40(4.3)$ |
| $56(3.8)$ | $32(3.9)$ | 5 | $41(3.3)$ |


| $56(3.8)$ | s | $32(3.9)$ | s | $18(2.4)$ |
| ---: | ---: | ---: | ---: | ---: |
| $86(2.6)$ |  | $80(3.3)$ |  | $9(2.1)$ |
| $51(4.5)$ |  | $37(4.4)$ | $29(3.6)$ | $31(3.3)$ |
| $66(3.7)$ |  | $37(4.4)$ |  |  |


| $37(4.4)$ | $29(3.6)$ | $37(4.4)$ |  |
| :--- | :--- | :--- | :--- |
| $66(3.7)$ | $62(3.8)$ | $21(3.0)$ | $16(2.8)$ |
| $67(4.0)$ | $57(4.5)$ | $21(3.5)$ | $49(4.0)$ |
| $82(3.2)$ | $46(4.2)$ | $24(4.0)$ | $31(3.6)$ |


| $79(3.8)$ | $r$ | $61(4.6)$ | $r$ | $29(4.3)$ | $r$ | 38 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

38 (4.8)
$15(3.5) \quad \mathrm{s}$
75

| $60(5.2)$ | $15(3.0)$ | $39(5.3)$ |
| :--- | :--- | :--- |
| $64(5.1)$ | $14(4.7)$ | $48(5.2)$ |
| $34(4.3)$ | $12(3.0)$ | $26(4.3)$ |
| $47(5.0)$ | $11(2.9)$ | $35(4.6)$ |

47 (5.0)
11 (2.9)
35 (4.6)

[^68]a Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 7.6: Teachers' Reports on Mathematics Content Related Emphasis in Students' Classroom Activities




[^69]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Educators, parents, employers, and most of the public support the goal of improving students' capacity for mathematics problemsolving. To examine the emphasis placed on that goal, TIMSS asked eighth-grade students and teachers about how often students were asked to do the following three activities - relate what was being learned in mathematics to their daily lives, explain their answers, and decide procedures for solving complex problems.

Exhibits 7.7 and 7.8 present students' and teachers' reports, respectively. In most of the countries, students reported a moderate emphasis on doing these types of problems in mathematics class. About two-thirds (67 percent), on average, internationally, said they were asked to explain answers in at least half their lessons, and more than half ( $53 \%$ ) reported deciding problem-solving procedures this frequently. Students reported the least attention to relating mathematics to their daily lives ( $44 \%$ ). On average, internationally, teachers reported more emphasis on explanations than did the students. They reported asking about three-fourths of the students ( $78 \%$ ) to explain answers in at least half the lessons. Perhaps as a matter for some concern, the teachers reported somewhat less emphasis on problem-solving procedures (45\%) than did the students. Teachers reported half the students were asked to relate mathematics to their daily lives in at least half the lessons.

| Countries | Percentage of Students Who Reported Doing the Activity About Half of the Lessons or More |  |  |
| :---: | :---: | :---: | :---: |
|  | Relate What is Being Learned in Mathematics to Their Daily Lives | Explain Answers | Decide Procedures for Solving Complex Problems |
| Armenia | 51 (1.1) | 72 (0.8) | 71 (0.9) |
| Australia | 37 (1.1) | 69 (1.1) | 45 (1.1) |
| Bahrain | 59 (0.9) | 73 (0.8) | 63 (0.8) |
| Belgium (Flemish) | 22 (1.0) | 71 (1.1) | 38 (1.0) |
| Botswana | 64 (0.6) | 78 (0.7) | 52 (0.8) |
| Bulgaria | 32 (1.6) | 66 (1.2) | 49 (1.6) |
| Chile | 63 (1.0) | 68 (1.0) | 55 (1.1) |
| Chinese Taipei | 28 (0.8) | 31 (0.9) | 41 (0.9) |
| Cyprus | 50 (0.8) | 81 (0.6) | 46 (0.7) |
| Egypt | 68 (0.9) | 73 (0.7) | 63 (0.8) |
| Estonia | 31 (1.2) | 65 (1.3) | 82 (0.8) |
| Ghana | 71 (1.2) | 75 (1.2) | 56 (1.0) |
| Hong Kong, SAR | 41 (0.8) | 57 (0.9) | 52 (0.7) |
| Hungary | 38 (1.4) | 72 (1.1) | 50 (1.1) |
| Indonesia | 34 (1.1) | 47 (1.0) | - - |
| Iran, Islamic Rep. of | 61 (1.2) | 75 (0.9) | 73 (0.9) |
| Israel | 50 (1.3) | 82 (0.9) | 73 (1.1) |
| Italy | 37 (1.1) | 57 (1.3) | 55 (1.1) |
| Japan | 24 (0.8) | 32 (1.5) | 45 (0.9) |
| Jordan | 63 (1.0) | 83 (0.9) | 80 (0.9) |
| Korea, Rep. of | 17 (0.6) | 29 (0.8) | 43 (0.8) |
| Latvia | 28 (1.1) | 67 (1.2) | 35 (1.2) |
| Lebanon | 56 (1.4) | 79 (1.0) | 63 (1.4) |
| Lithuania | 25 (1.0) | 60 (1.2) | 37 (1.1) |
| Macedonia, Rep. of | 53 (1.4) | 65 (1.3) | 50 (1.2) |
| Malaysia | 65 (0.9) | 62 (1.0) | 47 (1.0) |
| Moldova, Rep. of | 39 (1.6) | 72 (1.2) | 49 (1.5) |
| Morocco | 61 (1.3) | 76 (1.0) | 66 (1.1) |
| Netherlands | 22 (1.2) | 67 (1.8) | 28 (1.2) |
| New Zealand | 40 (1.2) | 68 (1.7) | 49 (1.3) |
| Norway | 35 (1.1) | 51 (1.3) | 40 (1.1) |
| Palestinian Nat'l Auth. | 63 (0.9) | 80 (0.8) | 74 (0.9) |
| Philippines | 71 (0.8) | 64 (1.0) | 59 (1.0) |
| Romania | 32 (1.3) | 71 (1.3) | 53 (1.6) |
| Russian Federation | 30 (1.4) | 84 (0.7) | 57 (1.2) |
| Saudi Arabia | 53 (1.3) | 70 (1.5) | 61 (1.7) |
| Scotland | 36 (1.1) | 75 (1.2) | 45 (1.1) |
| Serbia | 42 (1.3) | 56 (1.2) | 52 (0.9) |
| Singapore | 41 (0.9) | 60 (0.7) | 51 (0.8) |
| Slovak Republic | 51 (1.3) | 63 (1.1) | 48 (1.4) |
| Slovenia | 42 (1.3) | 57 (1.1) | 42 (1.1) |
| South Africa | 74 (1.0) | 78 (0.8) | 64 (0.8) |
| Sweden | 25 (1.1) | 57 (1.2) | 50 (1.1) |
| Tunisia | 50 (1.0) | 75 (0.9) | 53 (1.0) |
| United States | 45 (1.0) | 79 (0.8) | 53 (0.9) |
| \# England | 27 (1.2) | 69 (1.6) | 42 (1.1) |
| International Avg. | 44 (0.2) | 67 (0.2) | 53 (0.2) |
| Benchmarking Participants |  |  |  |
| Basque Country, Spain | 49 (1.6) | 73 (1.4) | 67 (1.5) |
| Indiana State, US | 45 (2.0) | 76 (1.2) | 48 (1.7) |
| Ontario Province, Can. | 44 (1.3) | 86 (1.0) | 56 (1.5) |
| Quebec Province, Can. | 38 (1.3) | 74 (1.0) | 71 (1.1) |

[^70]¥ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
A dash (-) indicates comparable data are not available.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

| Countries | Percentage of Students Whose Teachers Reported Students Doing the Activity About Half of the Lessons or More |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Relate What is Being Learned in Mathematics to Students' Daily Lives |  | Explain Answers |  | Decide Procedures for Solving Complex Problems |
| Armenia | $r \quad 45$ (4.2) | r | 82 (2.9) | $r$ | 40 (3.6) |
| Australia | 39 (4.3) |  | 64 (4.2) |  | 23 (3.7) |
| Bahrain | 56 (3.2) |  | 92 (1.3) |  | 47 (3.9) |
| Belgium (Flemish) | 32 (3.3) |  | 78 (3.0) |  | 22 (2.7) |
| Botswana | 71 (4.3) |  | 78 (4.0) |  | 46 (5.3) |
| Bulgaria | 26 (3.6) |  | 88 (3.2) |  | 28 (3.9) |
| Chile | 87 (2.2) |  | 84 (2.7) |  | 75 (3.1) |
| Chinese Taipei | 27 (3.6) |  | 58 (3.9) |  | 24 (3.2) |
| Cyprus | 50 (2.5) |  | 86 (1.3) |  | 68 (2.2) |
| Egypt | 63 (4.4) |  | 85 (3.3) |  | 41 (3.8) |
| Estonia | 62 (3.9) |  | 91 (2.5) |  | 80 (3.2) |
| Ghana | 63 (4.3) |  | 75 (4.0) |  | 36 (4.9) |
| Hong Kong, SAR | 26 (4.0) |  | 60 (4.7) |  | 40 (4.6) |
| Hungary | 63 (3.7) |  | 98 (1.2) |  | 68 (4.2) |
| Indonesia | 50 (4.4) |  | 61 (4.5) |  | 25 (3.7) |
| Iran, Islamic Rep. of | 69 (4.1) |  | 92 (2.4) |  | 64 (4.0) |
| Israel | 44 (3.6) |  | 82 (2.7) |  | 71 (3.5) |
| Italy | 31 (3.4) |  | 89 (2.1) |  | 57 (3.4) |
| Japan | 14 (3.0) |  | 44 (3.9) |  | 21 (3.5) |
| Jordan | 72 (3.9) |  | 88 (2.4) |  | 42 (4.0) |
| Korea, Rep. of | S $\quad 50$ (3.6) | s | 75 (3.1) | s | 52 (3.5) |
| Latvia | 43 (3.7) |  | 80 (3.2) |  | 54 (4.0) |
| Lebanon | 43 (4.1) |  | 89 (2.8) |  | 56 (4.5) |
| Lithuania | 52 (3.3) |  | 92 (2.0) |  | 58 (4.0) |
| Macedonia, Rep. of | 57 (4.1) |  | 76 (3.5) |  | 58 (3.8) |
| Malaysia | 64 (4.3) |  | 78 (3.5) |  | 40 (4.3) |
| Moldova, Rep. of | $r \quad 63$ (4.2) | r | 85 (3.5) | $r$ | 44 (4.7) |
| Morocco | s $\quad 45$ (6.7) | s | 81 (4.3) |  | $\mathrm{x} \times$ |
| Netherlands | 26 (4.2) |  | 62 (4.7) |  | 19 (4.0) |
| New Zealand | 57 (4.7) |  | 75 (4.3) |  | 35 (4.4) |
| Norway | 46 (4.4) |  | 60 (4.0) |  | 32 (3.9) |
| Palestinian Nat'l Auth. | 72 (3.6) |  | 92 (2.5) |  | 43 (4.3) |
| Philippines | 63 (4.4) |  | 78 (4.1) |  | 56 (4.8) |
| Romania | 57 (3.5) |  | 90 (2.4) |  | 74 (3.6) |
| Russian Federation | 24 (2.7) |  | 93 (1.6) |  | 14 (2.7) |
| Saudi Arabia | 48 (4.7) |  | 75 (5.7) |  | 21 (4.4) |
| Scotland | 41 (4.2) |  | 69 (4.5) |  | 25 (4.5) |
| Serbia | 57 (3.8) |  | 85 (3.0) |  | 58 (4.0) |
| Singapore | 32 (2.5) |  | 48 (2.7) |  | 27 (2.5) |
| Slovak Republic | 66 (4.7) |  | 84 (3.1) |  | 66 (4.5) |
| Slovenia | 58 (4.6) |  | 74 (3.6) |  | 46 (4.2) |
| South Africa | 59 (4.0) |  | 67 (3.4) |  | 36 (3.9) |
| Sweden | 40 (3.5) |  | 60 (4.0) |  | 54 (3.5) |
| Tunisia | 38 (3.8) |  | 80 (3.3) |  | 35 (4.1) |
| United States | 66 (2.8) |  | 80 (2.4) |  | 62 (2.9) |
| \# England | s $\quad 46$ (6.9) | s | 75 (5.5) | s | 45 (7.1) |
| International Avg. | 50 (0.6) |  | 78 (0.5) |  | 45 (0.6) |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | 64 (4.5) |  | 93 (2.6) |  | 48 (4.3) |
| Indiana State, US | 63 (5.3) |  | 66 (5.8) |  | 51 (6.5) |
| Ontario Province, Can. | 60 (4.5) |  | 81 (3.9) |  | 49 (4.5) |
| Quebec Province, Can. | 58 (5.1) |  | 74 (4.5) |  | 48 (5.1) |

[^71]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data

## What Instructional Strategies Are Used in Mathematics Classes?

As shown in Exhibit 7.9, the textbook is often the foundation of mathematics instruction at both the eighth and fourth grades. On average, internationally, nearly two-thirds of the eighth- and fourth-grade students $(65-66 \%)$ had teachers who reported using a textbook as the primary basis of their lessons. For another 32 percent of the eighthgrade students and 29 percent of the fourth-grade students, teachers reported using textbooks as a supplementary resource.

Exhibit 7.10 presents a profile of the activities most commonly encountered in mathematics classes around the world, as reported by mathematics teachers. At the eighth grade, the three most predominant activities, accounting for 59 percent of class time, on average, internationally, were teacher lecture ( $19 \%$ of class time), teacher-guided student practice ( $22 \%$ ), and students working on problems on their own ( $18 \%$ ). At the fourth grade, these activities accounted for approximately about the same percentage of time as at the eighth grade ( $61 \%$ ). The distribution was slightly different, though, since problem-solving activities with teacher guidance ( $22 \%$ ) and on students' own ( $23 \%$ ) accounted for nearly half the time. Teachers reported that 16 percent of the time, on average, was devoted to teacher lecture.



Background data provided by teachers.
ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

## Exhibit 7.9: Textbook Use in Teaching Mathematics



| Countries |  | Percentage of Students Taught by Teachers Reporting Textbook Use |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Do Not Use Textbook to Teach Mathematics | Use Textbook to Teach Mathematics |  |
|  |  |  | As Primary Basis for Lessons | As Supplementary Resource |
| Armenia | r | 13 (3.3) | 69 (4.7) | 19 (3.7) |
| Australia |  | 29 (3.9) | 16 (3.1) | 56 (4.1) |
| Belgium (Flemish) |  | 4 (1.4) | 85 (2.8) | 11 (2.6) |
| Chinese Taipei |  | 2 (1.1) | 92 (2.3) | 6 (2.1) |
| Cyprus |  | 0 (0.0) | 71 (3.7) | 29 (3.7) |
| England | r | 11 (2.9) | 26 (3.9) | 62 (4.5) |
| Hong Kong, SAR |  | 0 (0.0) | 81 (3.5) | 19 (3.5) |
| Hungary |  | 0 (0.0) | 77 (3.8) | 23 (3.8) |
| Iran, Islamic Rep. of |  | 5 (1.7) | 68 (4.5) | 27 (4.5) |
| Italy |  | 11 (2.0) | 11 (2.0) | 78 (2.5) |
| Japan |  | 1 (0.0) | 86 (3.0) | 14 (2.9) |
| Latvia |  | 0 (0.4) | 88 (2.6) | 11 (2.5) |
| Lithuania |  | 0 (0.0) | 100 (0.0) | 0 (0.0) |
| Moldova, Rep. of | r | 8 (2.7) | 85 (3.6) | 7 (2.5) |
| Morocco |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ |
| Netherlands |  | 2 (1.4) | 98 (1.4) | 0 (0.4) |
| New Zealand |  | 11 (2.2) | 16 (2.8) | 72 (3.0) |
| Norway |  | 1 (0.6) | 87 (3.1) | 13 (3.0) |
| Philippines |  | 6 (2.3) | 57 (5.2) | 37 (5.0) |
| Russian Federation |  | 0 (0.0) | 92 (1.9) | 8 (1.9) |
| Scotland | s | 0 (0.0) | 82 (4.2) | 18 (4.2) |
| Singapore |  | 0 (0.0) | 66 (4.0) | 34 (4.0) |
| Slovenia |  | 9 (2.5) | 44 (4.5) | 47 (4.8) |
| Tunisia | r | 3 (1.4) | 33 (4.1) | 65 (4.2) |
| United States |  | 11 (2.1) | 60 (3.1) | 29 (2.8) |
| International Avg. |  | 5 (0.4) | 66 (0.7) | 29 (0.7) |
| Benchmarking Participants |  |  |  |  |
| Indiana State, US |  | 6 (2.6) | 73 (4.8) | 21 (3.6) |
| Ontario Province, Can. |  | 6 (2.4) | 39 (4.7) | 54 (4.6) |
| Quebec Province, Can. |  | 5 (1.6) | 55 (4.5) | 40 (4.4) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 7.10: Percentage of Time in Mathematics Lessons Students Spend on Various mathematics Grade


| Countries |  | Reviewing Homework |  | Listening to Lecture-Style Presentations |  | Working Problems with Teacher's Guidance |  | Working Problems on Their Own Without Teacher's Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | r | 10 (0.5) | $r$ | 14 (0.8) | r | 26 (1.1) | r | 19 (0.9) |
| Australia |  | 8 (0.5) |  | 15 (0.8) |  | 23 (1.2) |  | 28 (1.2) |
| Bahrain |  | 13 (0.5) |  | 24 (0.9) |  | 17 (0.5) |  | 12 (0.5) |
| Belgium (Flemish) |  | 7 (0.4) |  | 14 (1.0) |  | 26 (1.0) |  | 20 (0.9) |
| Botswana | $r$ | 13 (0.9) | $r$ | 16 (1.1) | $r$ | 19 (1.1) | $r$ | 21 (1.2) |
| Bulgaria |  | 10 (0.6) |  | 18 (1.3) |  | 26 (1.0) |  | 16 (0.8) |
| Chile |  | 10 (0.4) |  | 18 (0.8) |  | 21 (0.9) |  | 18 (0.8) |
| Chinese Taipei |  | 12 (0.5) |  | 42 (1.3) |  | 13 (0.6) |  | 7 (0.5) |
| Cyprus | $r$ | 22 (0.4) | $r$ | 16 (0.5) | $r$ | 20 (0.5) | $r$ | 14 (0.4) |
| Egypt |  | 11 (0.4) |  | 18 (1.0) |  | 17 (0.8) |  | 15 (0.7) |
| Estonia |  | 10 (0.4) |  | 12 (0.6) |  | 25 (1.0) |  | 25 (0.8) |
| Ghana | r | 11 (0.4) | $r$ | 16 (0.9) | $r$ | 20 (0.8) | $r$ | 18 (0.7) |
| Hong Kong, SAR |  | 8 (0.4) |  | 36 (1.5) |  | 18 (0.7) |  | 16 (0.8) |
| Hungary |  | 12 (0.4) |  | 13 (0.7) |  | 25 (0.9) |  | 25 (1.0) |
| Indonesia | r | 12 (0.5) | $r$ | 25 (1.1) | r | 20 (0.9) | $r$ | 14 (0.9) |
| Iran, Islamic Rep. of |  | 12 (0.6) |  | 17 (0.8) |  | 18 (0.7) |  | 14 (0.7) |
| Israel | $r$ | 14 (0.6) | $r$ | 15 (0.8) | $r$ | 22 (0.7) | $r$ | 21 (0.8) |
| Italy |  | 15 (0.6) |  | 22 (0.6) |  | 19 (0.6) |  | 13 (0.6) |
| Japan |  | 7 (0.6) |  | 29 (1.3) |  | 28 (1.1) |  | 11 (1.0) |
| Jordan |  | 15 (0.7) |  | 23 (1.0) |  | 17 (0.8) |  | 13 (0.8) |
| Korea, Rep. of | $s$ | 6 (0.3) | s | 30 (1.2) | s | 19 (0.6) | $s$ | 20 (0.7) |
| Latvia | $r$ | 8 (0.6) | $r$ | 12 (0.7) | $r$ | 25 (1.1) | $r$ | 22 (0.9) |
| Lebanon | 5 | 24 (1.6) | s | 17 (0.9) | s | 23 (1.1) | $s$ | 8 (0.8) |
| Lithuania |  | 9 (0.5) |  | 7 (0.6) |  | 30 (1.2) |  | 26 (0.9) |
| Macedonia, Rep. of |  | 7 (0.3) |  | 37 (1.1) |  | 19 (0.7) |  | 15 (0.7) |
| Malaysia |  | 13 (0.7) |  | 21 (1.0) |  | 21 (0.9) |  | 16 (0.8) |
| Moldova, Rep. of | s | 9 (0.6) | 5 | 15 (1.0) | s | 23 (1.0) | 5 | 18 (0.9) |
| Morocco |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Netherlands |  | 15 (1.1) |  | 13 (0.7) |  | 21 (2.0) |  | 28 (2.5) |
| New Zealand |  | 7 (0.4) |  | 17 (0.8) |  | 24 (1.1) |  | 23 (1.3) |
| Norway |  | 8 (0.4) |  | 19 (0.6) |  | 26 (1.2) |  | 25 (1.5) |
| Palestinian Nat'l Auth. | $r$ | 13 (0.6) | $r$ | 23 (1.0) | r | 18 (0.8) | $r$ | 16 (0.9) |
| Philippines | $r$ | 9 (0.4) | r | 20 (0.9) | $r$ | 16 (0.8) | r | 15 (1.0) |
| Romania |  | 9 (0.4) |  | 24 (0.8) |  | 29 (1.0) |  | 15 (0.7) |
| Russian Federation |  | 11 (0.2) |  | 20 (0.7) |  | 20 (0.7) |  | 18 (0.7) |
| Saudi Arabia | r | 15 (1.0) | $r$ | 16 (1.6) | $r$ | 13 (1.0) | $r$ | 8 (0.7) |
| Scotland | r | 8 (0.3) | r | 22 (0.7) | $r$ | 26 (1.3) | $r$ | 22 (1.5) |
| Serbia |  | 7 (0.4) |  | 25 (1.4) |  | 23 (1.2) |  | 20 (1.2) |
| Singapore |  | 11 (0.4) |  | 27 (0.7) |  | 19 (0.6) |  | 15 (0.5) |
| Slovak Republic |  | 8 (0.3) |  | 17 (0.7) |  | 27 (0.9) |  | 17 (0.7) |
| Slovenia |  | 11 (0.4) |  | 21 (0.8) |  | 24 (0.7) |  | 22 (0.9) |
| South Africa | s | 15 (0.9) | s | 13 (0.7) | s | 19 (0.9) | 5 | 18 (0.9) |
| Sweden |  | 4 (0.4) |  | 11 (0.6) |  | 37 (1.8) |  | 28 (1.8) |
| Tunisia | r | 18 (0.9) | r | 14 (1.0) | $r$ | 17 (0.9) | $r$ | 18 (0.9) |
| United States |  | 13 (0.5) |  | 18 (0.7) |  | 21 (0.6) |  | 18 (0.6) |
| ま England | s | 8 (0.4) | 5 | 15 (1.2) | S | 32 (2.3) | 5 | 20 (1.7) |
| International Avg. |  | 11 (0.1) |  | 19 (0.1) |  | 22 (0.2) |  | 18 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 22 (1.2) |  | 16 (1.0) |  | 20 (1.1) |  | 15 (0.9) |
| Indiana State, US |  | 16 (1.0) |  | 17 (0.9) |  | 19 (1.1) |  | 18 (1.3) |
| Ontario Province, Can. |  | 16 (0.7) |  | 16 (0.8) |  | 18 (0.9) |  | 22 (1.3) |
| Quebec Province, Can. |  | 12 (0.7) |  | 25 (0.9) |  | 17 (0.9) |  | 21 (1.0) |

Background data provided by teachers.
a Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

Exhibit 7.10: Percentage of Time in Mathematics Lessons Students Spend on Various Activities in a Typical Week

| Countries |  | Listening to Teachers Re-teach and Clarify Content / Procedures |  | Taking Tests and Quizzes |  | Participating in Classroom Management Tasks Not Related to the Lesson's Content/Purpose |  | Other Student Activities |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | r | 13 (0.6) | $r$ | 11 (0.6) | r | 4 (0.3) | $r$ | 4 (0.3) |
| Australia |  | 9 (0.4) |  | 7 (0.4) |  | 7 (0.6) |  | 3 (0.4) |
| Bahrain |  | 12 (0.3) |  | 13 (0.5) |  | 6 (0.5) |  | 6 (0.3) |
| Belgium (Flemish) |  | 16 (0.8) |  | 11 (0.4) |  | 4 (0.3) |  | 2 (0.2) |
| Botswana | $r$ | 11 (0.8) | $r$ | 10 (0.7) | r | 6 (0.5) | r | 5 (0.4) |
| Bulgaria |  | 17 (0.9) |  | 8 (0.5) |  | 3 (0.4) |  | 2 (0.3) |
| Chile |  | 14 (0.7) |  | 11 (0.5) |  | 6 (0.4) |  | 3 (0.3) |
| Chinese Taipei |  | 9 (0.4) |  | 10 (0.4) |  | 4 (0.3) |  | 3 (0.3) |
| Cyprus | $r$ | 12 (0.4) | $r$ | 10 (0.5) | $r$ | 5 (0.2) | $r$ | 2 (0.2) |
| Egypt |  | 15 (0.8) |  | 11 (0.4) |  | 6 (0.3) |  | 7 (0.4) |
| Estonia |  | 11 (0.5) |  | 13 (0.6) |  | 3 (0.3) |  | 2 (0.3) |
| Ghana | $r$ | 12 (0.7) | $r$ | 12 (0.4) | $r$ | 7 (0.4) | $r$ | 6 (0.3) |
| Hong Kong, SAR |  | 9 (0.7) |  | 6 (0.3) |  | 4 (0.5) |  | 4 (0.4) |
| Hungary |  | 10 (0.4) |  | 10 (0.4) |  | 3 (0.3) |  | 3 (0.3) |
| Indonesia | $r$ | 12 (0.5) | $r$ | 12 (0.7) | $r$ | 3 (0.4) | $r$ | 3 (0.5) |
| Iran, Islamic Rep. of |  | 15 (0.7) |  | 11 (0.5) |  | 6 (0.3) |  | 6 (0.6) |
| Israel | r | 11 (0.4) | $r$ | 10 (0.5) | $r$ | 5 (0.5) | $r$ | 3 (0.3) |
| Italy |  | 13 (0.4) |  | 11 (0.5) |  | 4 (0.3) |  | 2 (0.3) |
| Japan |  | 15 (0.9) |  | 6 (0.4) |  | 2 (0.2) |  | 2 (0.4) |
| Jordan |  | 11 (0.5) |  | 9 (0.4) |  | 6 (0.4) |  | 6 (0.5) |
| Korea, Rep. of | s | 9 (0.4) | $s$ | 8 (0.4) | s | 5 (0.3) | $s$ | 3 (0.5) |
| Latvia | $r$ | 11 (0.6) | $r$ | 15 (0.7) | $r$ | 2 (0.2) | $r$ | 4 (0.4) |
| Lebanon | s | 10 (0.6) | s | 11 (0.6) | s | 4 (0.4) | s | 4 (0.4) |
| Lithuania |  | 11 (0.7) |  | 14 (0.6) |  | 1 (0.2) |  | 2 (0.2) |
| Macedonia, Rep. of |  | 6 (0.4) |  | 8 (0.4) |  | 3 (0.3) |  | 4 (0.3) |
| Malaysia |  | 9 (0.5) |  | 8 (0.4) |  | 6 (0.4) |  | 6 (0.4) |
| Moldova, Rep. of | s | 11 (0.8) | s | 14 (0.8) | s | 4 (0.7) | 5 | 5 (0.6) |
| Morocco |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |
| Netherlands |  | 7 (0.5) |  | 8 (0.5) |  | 5 (0.5) |  | 4 (0.4) |
| New Zealand |  | 9 (0.4) |  | 8 (0.4) |  | 7 (0.5) |  | 4 (0.5) |
| Norway |  | 10 (0.4) |  | 6 (0.3) |  | 4 (0.3) |  | 3 (0.4) |
| Palestinian Nat'l Auth. | $r$ | 11 (0.5) | $r$ | 9 (0.3) | $r$ | 6 (0.3) | $r$ | 6 (0.4) |
| Philippines | $r$ | 11 (0.5) | $r$ | 16 (0.7) | $r$ | 7 (0.3) | $r$ | 6 (0.4) |
| Romania |  | 10 (0.4) |  | 9 (0.5) |  | 3 (0.3) |  | 2 (0.2) |
| Russian Federation |  | 8 (0.4) |  | 18 (0.5) |  | 1 (0.2) |  | 3 (0.3) |
| Saudi Arabia | $r$ | 23 (2.2) | r | 12 (1.0) | $r$ | 6 (0.4) | $r$ | 7 (0.8) |
| Scotland | $r$ | 8 (0.5) | $r$ | 4 (0.3) | $r$ | 6 (0.5) | $r$ | 3 (0.5) |
| Serbia |  | 9 (0.5) |  | 7 (0.4) |  | 3 (0.3) |  | 5 (0.5) |
| Singapore |  | 9 (0.3) |  | 8 (0.3) |  | 6 (0.4) |  | 4 (0.4) |
| Slovak Republic |  | 13 (0.5) |  | 12 (0.4) |  | 3 (0.3) |  | 3 (0.3) |
| Slovenia |  | 10 (0.6) |  | 6 (0.3) |  | 2 (0.2) |  | 4 (0.4) |
| South Africa | s | 11 (0.6) | s | 12 (0.6) | s | 7 (0.4) | s | 5 (0.4) |
| Sweden |  | 9 (0.3) |  | 6 (0.3) |  | 3 (0.3) |  | 3 (0.4) |
| Tunisia | $r$ | 14 (0.8) | $r$ | 13 (0.7) | $r$ | 4 (0.4) | $r$ | 4 (0.5) |
| United States |  | 11 (0.3) |  | 11 (0.4) |  | 5 (0.3) |  | 4 (0.4) |
| \# England | 5 | 11 (0.6) | s | 4 (0.4) | 5 | 7 (0.6) | 5 | 4 (0.8) |
| International Avg. |  | 11 (0.1) |  | 10 (0.1) |  | 5 (0.1) |  | 4 (0.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 10 (0.7) |  | 9 (0.6) |  | 4 (0.4) |  | 3 (0.5) |
| Indiana State, US |  | 10 (0.6) |  | 10 (0.7) |  | 6 (0.6) |  | 4 (0.7) |
| Ontario Province, Can. |  | 10 (0.5) |  | 11 (0.6) |  | 5 (0.4) |  | 3 (0.4) |
| Quebec Province, Can. |  | 9 (0.4) |  | 9 (0.5) |  | 5 (0.4) |  | 3 (0.4) |

## Background data provided by teachers.

\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

## Exhibit 7.10: Percentage of Time in Mathematics Lessons Students Spend on Various Activities in a Typical Week



| Countries |  | Reviewing Homework |  | Listening to Lecture-Style Presentations |  | Working Problems with Teacher's Guidance |  | Working Problems on Their Own Without Teacher's Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | s | 10 (0.5) | 5 | 12 (0.7) | 5 | 24 (1.1) | s | 20 (0.8) |
| Australia |  | 6 (0.4) |  | 12 (0.8) |  | 27 (1.1) |  | 25 (1.0) |
| Belgium (Flemish) |  | 6 (0.4) |  | 18 (0.6) |  | 19 (0.6) |  | 32 (1.1) |
| Chinese Taipei |  | 10 (0.4) |  | 33 (1.3) |  | 16 (0.6) |  | 11 (0.7) |
| Cyprus |  | 14 (0.5) |  | 12 (0.5) |  | 22 (0.6) |  | 21 (0.7) |
| England | $r$ | 6 (0.4) | $r$ | 18 (1.2) | $r$ | 24 (1.2) | $r$ | 27 (1.1) |
| Hong Kong, SAR |  | 7 (0.4) |  | 37 (1.3) |  | 17 (0.7) |  | 15 (0.8) |
| Hungary | $r$ | 8 (0.4) | $r$ | 12 (0.8) | $r$ | 27 (0.8) | $r$ | 27 (0.8) |
| Iran, Islamic Rep. of |  | 13 (0.6) |  | 13 (0.6) |  | 17 (0.7) |  | 14 (0.7) |
| Italy |  | 11 (0.4) |  | 24 (0.6) |  | 13 (0.4) |  | 14 (0.4) |
| Japan |  | 5 (0.3) |  | 19 (0.9) |  | 32 (1.1) |  | 16 (1.0) |
| Latvia |  | 7 (0.5) |  | 10 (0.7) |  | 22 (0.8) |  | 27 (0.9) |
| Lithuania |  | 8 (0.3) |  | 6 (0.4) |  | 24 (0.8) |  | 33 (1.0) |
| Moldova, Rep. of | r | 10 (0.5) | $r$ | 12 (0.6) | $r$ | 20 (1.0) | $r$ | 18 (0.8) |
| Morocco |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |
| Netherlands | $r$ | 3 (0.3) | $r$ | 14 (0.9) | $r$ | 20 (1.2) | $r$ | 37 (1.4) |
| New Zealand |  | 4 (0.3) |  | 10 (0.5) |  | 28 (1.1) |  | 27 (0.9) |
| Norway |  | 7 (0.4) |  | 15 (0.5) |  | 23 (1.3) |  | 35 (1.6) |
| Philippines |  | 9 (0.4) |  | 18 (0.8) |  | 17 (0.7) |  | 17 (0.8) |
| Russian Federation |  | 9 (0.3) |  | 14 (0.6) |  | 21 (0.7) |  | 23 (0.6) |
| Scotland | s | 6 (0.4) | $s$ | 21 (0.9) | 5 | 20 (1.4) | s | 31 (1.8) |
| Singapore |  | 14 (0.6) |  | 21 (1.0) |  | 17 (0.8) |  | 17 (0.7) |
| Slovenia | r | 9 (0.4) | $r$ | 14 (0.8) | $r$ | 23 (1.0) | $r$ | 29 (1.2) |
| Tunisia | $r$ | 14 (1.0) | $r$ | 9 (1.0) | $r$ | 25 (1.6) | 5 | 18 (1.1) |
| United States |  | 10 (0.4) |  | 16 (0.4) |  | 23 (0.7) |  | 22 (0.7) |
| International Avg. |  | 8 (0.1) |  | 16 (0.2) |  | 22 (0.2) |  | 23 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 10 (0.8) |  | 18 (1.2) |  | 25 (1.4) |  | 21 (1.6) |
| Ontario Province, Can. |  | 13 (0.7) |  | 16 (0.8) |  | 21 (1.1) |  | 21 (1.1) |
| Quebec Province, Can. |  | 7 (0.3) |  | 20 (0.9) |  | 21 (1.0) |  | 20 (0.9) |

[^72]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

Exhibit 7.10: Percentage of Time in Mathematics Lessons Students Spend on Various Activities in a Typical Week


| Countries |  | Listening to Teachers Re-teach and Clarify Content / Procedures |  | Taking Tests and Quizzes |  | Participating in Classroom Management Tasks Not Related to the Lesson's Content/Purpose |  | Other Student Activities |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | S | 13 (0.7) | s | 12 (0.6) | S | 5 (0.4) | S | 5 (0.5) |
| Australia |  | 13 (0.6) |  | 7 (0.4) |  | 5 (0.5) | r | 5 (0.6) |
| Belgium (Flemish) |  | 11 (0.6) |  | 8 (0.3) |  | 3 (0.2) |  | 3 (0.3) |
| Chinese Taipei |  | 12 (0.4) |  | 9 (0.4) |  | 4 (0.2) |  | 4 (0.3) |
| Cyprus |  | 13 (0.5) |  | 10 (0.4) |  | 5 (0.3) |  | 6 (0.6) |
| England | $r$ | 12 (0.6) | S | 5 (0.4) | S | 4 (0.3) | s | 5 (0.7) |
| Hong Kong, SAR |  | 9 (0.5) |  | 6 (0.3) |  | 4 (0.3) |  | 6 (0.4) |
| Hungary | r | 12 (0.6) | $r$ | 8 (0.6) | $r$ | 3 (0.3) | r | 5 (0.6) |
| Iran, Islamic Rep. of |  | 15 (0.8) |  | 12 (0.6) |  | 8 (0.4) |  | 9 (0.6) |
| Italy |  | 14 (0.4) |  | 14 (0.5) |  | 6 (0.3) |  | 5 (0.4) |
| Japan |  | 15 (0.7) |  | 10 (0.4) |  | 1 (0.2) |  | 2 (0.6) |
| Latvia |  | 11 (0.5) |  | 15 (0.6) |  | 2 (0.2) | r | 6 (0.7) |
| Lithuania |  | 11 (0.6) |  | 13 (0.6) |  | 3 (0.3) |  | 2 (0.3) |
| Moldova, Rep. of | $r$ | 12 (0.6) | r | 16 (0.7) | $r$ | 6 (0.5) | r | 7 (0.5) |
| Morocco |  | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Netherlands | $r$ | 12 (0.7) | r | 7 (0.8) | r | 3 (0.3) | r | 4 (0.6) |
| New Zealand |  | 14 (0.7) |  | 7 (0.3) |  | 4 (0.2) |  | 6 (0.6) |
| Norway |  | 10 (0.4) |  | 5 (0.3) |  | 3 (0.2) |  | 3 (0.3) |
| Philippines |  | 12 (0.7) |  | 15 (0.8) |  | 8 (0.5) |  | 6 (0.3) |
| Russian Federation |  | 9 (0.4) |  | 18 (0.6) |  | 1 (0.2) |  | 5 (0.5) |
| Scotland | S | 9 (0.5) | S | 5 (0.3) | s | 4 (0.3) | S | 4 (0.5) |
| Singapore |  | 11 (0.4) |  | 8 (0.4) |  | 6 (0.3) |  | 5 (0.5) |
| Slovenia | $r$ | 10 (0.4) | r | 9 (0.6) | $r$ | 3 (0.3) | r | 4 (0.4) |
| Tunisia | $r$ | 14 (1.0) | S | 12 (0.6) | r | 5 (0.4) | S | 6 (0.7) |
| United States |  | 11 (0.3) |  | 9 (0.3) |  | 5 (0.3) |  | 5 (0.4) |
| International Avg. |  | 12 (0.1) |  | 10 (0.1) |  | 4 (0.1) |  | 5 (0.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 11 (0.6) |  | 9 (0.5) |  | 4 (0.6) |  | 4 (0.6) |
| Ontario Province, Can. |  | 12 (0.5) |  | 8 (0.6) |  | 6 (0.5) |  | 4 (0.5) |
| Quebec Province, Can. |  | 12 (0.8) |  | 7 (0.4) |  | 7 (0.5) |  | 7 (1.1) | some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

## How Are Calculators and Computers Used?

Exhibit 7.11 shows the number of countries with national policies on calculator use, the percentages of students not permitted to use calculators in mathematics class, and the percentages of students using calculators for various activities in about half of the lessons or more. At the eighth grade, 29 countries and all four benchmarking participants reported that their official curriculum contained statements about using calculators. According to their teachers, the percentages of students not permitted to use calculators varied dramatically from country to country. More than half the eighth-grade students were not permitted to use calculators in Bahrain, Cyprus, Ghana, Iran, Jordan, Romania, and Saudi Arabia. The countries permitting calculator use for essentially all eighth-grade students ( $98 \%$ or more) included Egypt, Hong Kong SAR, Lithuania, Morocco, the Netherlands, Norway, the Palestinian National Authority, Scotland, Sweden, and England. The percentages of eighth-grade students asked to use calculators in at least half of their lessons for each of four different activities reveal that, on average, internationally, teachers asked the most students to use calculators for checking answers ( $27 \%$ ), performing routine computations ( $29 \%$ ), and solving complex problems ( $31 \%$ ). Only 14 percent, on average, were asked to explore number concepts.

At the fourth grade, 14 participants reported that their national or regional mathematics curriculum contained statements about using calculators. Compared to eighth grade, teachers in the TIMSS countries reported that greater percentages of fourth-grade students were not permitted to use calculators - 57 percent, on average. The countries permitting widespread calculator usage ( $90 \%$ of the students or more) at the fourth grade included Australia, Cyprus, England, New Zealand, and Scotland. However, even in those countries, teachers reported asking relatively small percentages of students to do any calculator activities in half the lessons or more.

Countries' reports on computer use in mathematics class are presented in Exhibit 7.12. Across countries, 26 participants at the eighth grade and 12 at the fourth grade reported that their mathematics curriculum contained statements about computer use, nearly as many as reported statements about calculator use. Yet, access to computers remains a challenge in many countries. Teachers reported that, on average, internationally, computers were not available for 68 percent of the eighth-grade students and 58 percent of the fourthgrade students. Beyond that, using computers as often as in half the lessons was extremely rare at either grade, even in countries with relatively high availability.


| Iran, Islamic Rep. of | $\bigcirc$ |  | 52 (4.1) |  | 8 (2.1) |  | 5 (1.7) |  | 10 (2.4) |  | 3 (1.5) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Israel | $\bigcirc$ |  | 8 (2.2) |  | 50 (3.7) |  | 53 (4.1) |  | 47 (3.8) |  | 28 (3.2) |
| Italy | - |  | 16 (2.9) |  | 40 (4.2) |  | 45 (3.9) |  | 55 (4.0) |  | 11 (2.3) |
| Japan | - |  | 37 (4.1) |  | 0 (0.0) |  | 2 (1.2) |  | 1 (0.9) |  | 3 (1.6) |
| Jordan | - |  | 55 (4.4) |  | 4 (1.7) |  | 6 (2.1) |  | 14 (3.5) |  | 3 (1.4) |
| Korea, Rep. of | - | s | 35 (3.3) | $s$ | 2 (1.3) | s | 2 (1.2) | s | 3 (1.0) | s | 2 (0.8) |
| Latvia | $\bigcirc$ |  | 47 (4.5) |  | 10 (2.7) |  | 8 (2.4) |  | 7 (2.0) |  | 5 (1.7) |
| Lebanon | $\bigcirc$ |  | 6 (1.8) |  | 46 (4.5) |  | 39 (4.4) |  | 34 (4.1) |  | 26 (3.8) |
| Lithuania | - |  | 1 (0.7) |  | 59 (3.7) |  | 60 (3.8) |  | 68 (3.5) |  | 17 (2.9) |
| Macedonia, Rep. of | $\bigcirc$ |  | 24 (3.7) |  | 19 (3.4) |  | 19 (3.0) |  | 19 (3.3) |  | 9 (2.3) |
| Malaysia | $\bigcirc$ |  | 46 (3.9) |  | 14 (2.7) |  | 12 (2.6) |  | 23 (3.7) |  | 10 (2.4) |
| Moldova, Rep. of | $\bigcirc$ | s | 15 (3.4) | r | 24 (4.2) | r | 23 (3.9) | r | 23 (3.5) | $r$ | 22 (3.8) |
| Morocco | $\bigcirc$ | s | 1 (1.1) | 5 | 15 (4.8) | s | 10 (4.0) | s | 13 (4.1) | s | 15 (5.0) |
| Netherlands | - |  | 0 (0.0) |  | 72 (4.3) |  | 94 (2.3) |  | 75 (4.1) |  | 42 (4.8) |
| New Zealand | - |  | 4 (2.5) |  | 60 (4.8) |  | 77 (3.2) |  | 64 (5.4) |  | 42 (4.5) |
| Norway | - |  | 0 (0.0) |  | 72 (3.6) |  | 77 (3.8) |  | 68 (4.0) |  | 21 (3.4) |
| Palestinian Nat'l Auth. | - |  | 1 (0.7) |  | 24 (4.0) |  | 21 (3.9) |  | 39 (4.1) |  | 8 (2.4) |
| Philippines | $\bigcirc$ |  | 28 (4.1) |  | 10 (2.0) |  | 6 (2.1) |  | 16 (3.4) |  | 13 (2.9) |
| Romania | $\bigcirc$ |  | 52 (4.1) |  | 4 (1.6) |  | 6 (1.7) |  | 0 (0.0) |  | 0 (0.0) |
| Russian Federation | - |  | 20 (2.4) |  | 20 (2.6) |  | 13 (2.3) |  | 19 (3.2) |  | 5 (1.5) |
| Saudi Arabia | $\bigcirc$ | $r$ | 59 (4.6) |  | 10 (3.3) |  | 4 (2.0) |  | 9 (3.1) |  | 2 (1.0) |
| Scotland | - |  | 2 (1.4) |  | 11 (2.3) |  | 22 (3.8) |  | 37 (5.2) |  | 12 (3.2) |
| Serbia | - |  | 36 (4.2) |  | 19 (3.4) |  | 22 (3.4) |  | 17 (3.2) |  | 11 (2.7) |
| Singapore | - |  | 0 (0.0) |  | 63 (2.4) |  | 63 (2.1) |  | 65 (2.5) |  | 32 (2.2) |
| Slovak Republic | $\bigcirc$ |  | - | $r$ | 36 (4.6) | r | 38 (4.5) | r | 22 (4.0) | $r$ | 9 (2.8) |
| Slovenia | - |  | 40 (4.4) |  | 9 (2.5) |  | 9 (2.3) |  | 13 (2.7) |  | 3 (1.4) |
| South Africa | - | $r$ | 6 (1.8) |  | 21 (3.3) |  | 18 (2.5) |  | 32 (3.4) |  | 23 (3.1) |
| Sweden | - |  | 1 (0.4) |  | 43 (3.5) |  | 70 (3.7) |  | 55 (4.0) |  | 13 (2.1) |
| Tunisia | $\bigcirc$ | $r$ | 44 (4.6) |  | 6 (2.0) |  | 8 (2.4) |  | 5 (1.9) |  | 8 (2.4) |
| United States | - |  | 6 (1.4) |  | 55 (3.1) |  | 52 (2.6) |  | 69 (2.7) |  | 48 (3.0) |
| \# England | $\bigcirc$ | $r$ | 0 (0.0) | $r$ | 42 (6.7) | r | 35 (5.4) | $r$ | 51 (6.3) | $r$ | 16 (4.1) |
| International Avg. |  |  | 23 (0.5) |  | 27 (0.5) |  | 29 (0.5) |  | 31 (0.5) |  | 14 (0.4) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | - |  | 27 (4.3) |  | 24 (4.3) |  | 27 (4.6) |  | 48 (5.2) |  | 16 (3.3) |
| Indiana State, US | - |  | 14 (3.9) |  | 51 (5.9) |  | 40 (4.4) |  | 62 (5.7) |  | 42 (6.8) |
| Ontario Province, Can. | - |  | 1 (1.0) |  | 62 (4.5) |  | 56 (4.6) |  | 75 (4.4) |  | 44 (4.7) |
| Quebec Province, Can. | - |  | 0 (0.0) |  | 91 (2.2) |  | 86 (4.0) |  | 87 (3.7) |  | 49 (4.5) |

[^73][^74]An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.
 some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| Countries | National Curriculum Contains Policies / Statements About the Use of Computers | Percentage of Students Whose Teachers Reported That Computers Are Not Available | Percentage of Students Whose Teachers Reported on Computer Use About Half of the Lessons or More |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Discovering Principles and Concepts | Practicing Skills and Procedures | Looking up Ideas and Information | Processing and Analyzing Data |
| Armenia | $\bigcirc$ | 80 (3.4) | 0 (0.4) | 3 (1.8) | 1 (0.7) | 1 (0.9) |
| Australia | - | 46 (4.2) | 0 (0.4) | 1 (0.4) | 1 (0.6) | 0 (0.0) |
| Bahrain | $\bigcirc$ | 65 (3.5) | 1 (0.6) | 1 (0.7) | 3 (1.1) | 5 (1.3) |
| Belgium (Flemish) | - | 52 (3.8) | 1 (1.0) | $1(0.9)$ | 1 (0.9) | 1 (0.8) |
| Botswana | - | 93 (2.6) | 0 (0.0) | 0 (0.0) | 0 (0.0) | 1 (1.5) |
| Bulgaria | $\bigcirc$ | 91 (2.2) | 0 (0.0) | 0 (0.0) | 0 (0.0) | 1 (0.0) |
| Chile | $\bigcirc$ | 48 (3.8) | 1 (0.8) | $2(0.8)$ | 9 (2.1) | 7 (2.0) |
| Chinese Taipei | - | 71 (3.3) | 0 (0.0) | 0 (0.0) | 1 (1.0) | 1 (1.0) |
| Cyprus | $\bigcirc$ | 92 (1.9) | 0 (0.0) | 0 (0.0) | 0 (0.0) | 0 (0.0) |
| Egypt | - | - - | - - | - - | - - | - - |
| Estonia | - | 69 (3.8) | 0 (0.0) | 0 (0.0) | 0 (0.0) | 2 (1.0) |
| Ghana | - | 85 (3.5) | 0 (0.0) | $1(0.0)$ | 1 (0.9) | 2 (1.1) |
| Hong Kong, SAR | $\bigcirc$ | 61 (4.3) | 0 (0.4) | 0 (0.0) | 1 (0.9) | 3 (1.5) |
| Hungary | - | 73 (3.5) | 1 (0.7) | 1 (1.0) | 1 (0.7) | 1 (0.7) |
| Indonesia | $\bigcirc$ | 89 (2.5) | 1 (0.7) | 2 (1.3) | 1 (0.8) | 1 (0.8) |


| Iran, Islamic Rep. of | $\bigcirc$ |  | 98 (0.9) |  | 1 (0.0) |  | 1 (0.0) |  | 1 (0.0) |  | 1 (0.0) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Israel | - |  | 53 (3.8) |  | 5 (1.3) |  | 9 (2.1) |  | 3 (1.0) |  | 7 (1.8) |
| Italy | $\bigcirc$ |  | 68 (3.6) |  | 0 (0.3) |  | 1 (0.6) |  | 0 (0.0) |  | 1 (0.8) |
| Japan | - |  | 14 (3.2) |  | 2 (1.2) |  | 1 (0.9) |  | 1 (1.0) |  | 1 (0.7) |
| Jordan | - |  | 89 (2.8) |  | 0 (0.0) |  | 1 (1.0) |  | 0 (0.0) |  | 1 (0.0) |
| Korea, Rep. of | - | 5 | 27 (3.4) | s | 17 (2.6) | s | 7 (1.7) | s | 11 (2.3) | s | 6 (2.0) |
| Latvia | $\bigcirc$ |  | 77 (4.1) |  | 0 (0.0) |  | 0 (0.4) |  | 0 (0.0) |  | 1 (0.5) |
| Lebanon | $\bigcirc$ |  | 76 (3.8) |  | 8 (2.4) |  | 8 (2.4) |  | 6 (2.3) |  | 10 (3.2) |
| Lithuania | $\bigcirc$ |  | 30 (3.6) |  | 0 (0.0) |  | 3 (1.5) |  | 3 (1.3) |  | 3 (1.7) |
| Macedonia, Rep. of | $\bigcirc$ |  | 96 (1.4) |  | 0 (0.0) |  | 1 (0.5) |  | 0 (0.0) |  | 0 (0.0) |
| Malaysia | $\bigcirc$ |  | 95 (1.7) |  | 1 (0.7) |  | 0 (0.5) |  | 0 (0.5) |  | 0 (0.0) |
| Moldova, Rep. of | $\bigcirc$ | $r$ | 72 (3.7) | r | 13 (3.6) | r | 14 (3.2) | $r$ | 12 (2.9) | $r$ | 14 (3.1) |
| Morocco | $\bigcirc$ |  | $\mathrm{x} \times$ |  | x x |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | x x |
| Netherlands | - |  | 70 (4.6) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |
| New Zealand | - |  | 29 (4.6) |  | 1 (0.3) |  | 0 (0.3) |  | 1 (0.6) |  | 1 (0.6) |
| Norway | - |  | 45 (4.1) |  | 1 (0.5) |  | 1 (0.9) |  | 3 (1.4) |  | 3 (1.3) |
| Palestinian Nat'l Auth. | - |  | 71 (4.1) |  | 3 (1.4) |  | 3 (1.3) |  | 2 (1.2) |  | 0 (0.0) |
| Philippines | $\bigcirc$ |  | 90 (2.9) |  | 2 (1.4) |  | 2 (1.4) |  | 3 (1.6) |  | 2 (1.4) |
| Romania | $\bigcirc$ |  | 88 (2.7) |  | 0 (0.0) |  | 1 (0.5) |  | 1 (0.8) |  | 0 (0.0) |
| Russian Federation | $\bigcirc$ |  | 89 (2.6) |  | 1 (0.5) |  | 1 (0.6) |  | 1 (0.5) |  | 1 (0.7) |
| Saudi Arabia | $\bigcirc$ |  | 81 (3.6) |  | 1 (0.9) |  | 3 (1.5) |  | 5 (1.7) |  | 3 (1.3) |
| Scotland | - |  | 60 (4.8) |  | 2 (1.0) |  | 2 (1.0) |  | 0 (0.0) |  | 0 (0.0) |
| Serbia | - |  | 92 (2.4) |  | 3 (1.7) |  | 3 (1.5) |  | 3 (1.5) |  | 3 (1.5) |
| Singapore | - |  | 33 (2.7) |  | 3 (1.0) |  | 4 (1.0) |  | 3 (0.9) |  | 3 (0.8) |
| Slovak Republic | $\bigcirc$ |  | 75 (3.5) |  | 0 (0.0) |  | 1 (0.6) |  | 0 (0.0) |  | 0 (0.0) |
| Slovenia | - |  | 62 (4.1) |  | 0 (0.1) |  | 1 (1.0) |  | 0 (0.1) |  | 1 (0.2) |
| South Africa | $\bigcirc$ | $r$ | 85 (2.7) |  | 3 (1.4) |  | 3 (1.2) |  | 3 (1.2) |  | 2 (1.1) |
| Sweden | - |  | 54 (3.6) |  | 0 (0.0) |  | 2 (0.9) |  | 1 (0.7) |  | 1 (0.5) |
| Tunisia | $\bigcirc$ |  | 77 (3.5) |  | 3 (0.8) |  | 3 (0.8) |  | 4 (1.3) |  | 5 (1.3) |
| United States | $\bigcirc$ |  | 54 (3.0) |  | 2 (0.7) |  | 4 (1.0) |  | 3 (1.0) |  | 2 (0.7) |
| \# England | - | r | 34 (6.6) | r | 1 (0.8) | $r$ | 5 (2.9) | $r$ | 2 (1.4) | $r$ | 1 (1.3) |
| International Avg. |  |  | 68 (0.5) |  | 2 (0.2) |  | 2 (0.2) |  | 2 (0.2) |  | 2 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain | - |  | 65 (4.5) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |
| Indiana State, US | - |  | 49 (5.9) |  | 2 (1.5) |  | 4 (2.0) |  | 1 (1.1) |  | 2 (1.5) |
| Ontario Province, Can. | - |  | 54 (5.2) |  | 1 (0.0) |  | 2 (1.2) |  | 4 (1.5) |  | 5 (1.9) |
| Quebec Province, Can. | - |  | 89 (2.7) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |

Background data provided by National Research Coordinators and by teachers.
专 Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

| Countries | National Curriculum Contains Policies / Statements About the Use of Computers | Percentage of Students Whose Teachers Reported That Computers Are Not Available | Percentage of Students Whose Teachers Reported on Computer Use About Half of the Lessons or More |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Discovering Principles and Concepts |  | Practicing Skills and Procedures |  | Looking up Ideas and Information |
| Armenia | $\bigcirc$ | 88 (2.6) | 0 (0.0) | r | 0 (0.0) | r | 1 (0.6) |
| Australia | - | 24 (3.6) | 5 (2.3) |  | 8 (2.4) |  | 3 (1.7) |
| Belgium (Flemish) | $\bigcirc$ | 33 (3.4) | 0 (0.3) |  | 9 (2.2) |  | 1 (0.2) |
| Chinese Taipei | - | 84 (3.3) | 1 (0.0) |  | 1 (0.0) |  | 1 (0.6) |
| Cyprus | $\bigcirc$ | 19 (3.3) | 2 (1.2) |  | 7 (2.1) |  | 6 (1.8) |
| England | - | 19 (3.4) | 4 (1.9) | $r$ | 5 (2.3) | $r$ | 2 (1.4) |
| Hong Kong, SAR | $\bigcirc$ | 47 (4.4) | 1 (1.0) |  | 1 (1.1) |  | 0 (0.0) |
| Hungary | $\bigcirc$ | 86 (3.3) | 1 (0.9) |  | 3 (1.4) |  | 2 (1.1) |
| Iran, Islamic Rep. of | $\bigcirc$ | 98 (1.1) | 0 (0.0) |  | 0 (0.0) |  | 0 (0.0) |
| Italy | - | 75 (3.1) | 0 (0.0) |  | 0 (0.3) |  | 0 (0.0) |
| Japan | - | 16 (3.2) | 0 (0.0) |  | 1 (0.7) |  | 1 (0.7) |
| Latvia | $\bigcirc$ | 89 (2.9) | 0 (0.0) |  | 0 (0.0) |  | 0 (0.3) |
| Lithuania | $\bigcirc$ | 87 (2.5) | 0 (0.2) |  | 3 (1.3) |  | 0 (0.0) |
| Moldova, Rep. of | $\bigcirc$ | 94 (2.1) | 1 (0.0) | $r$ | 2 (1.2) | $r$ | 1 (0.0) |
| Morocco | $\bigcirc$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ |
| Netherlands | $\bigcirc$ | 24 (3.5) | 11 (3.0) |  | 31 (4.4) |  | 1 (0.0) |
| New Zealand | - | 30 (3.1) | 1 (0.5) |  | 4 (1.4) |  | 1 (0.6) |
| Norway | - | 41 (4.5) | 1 (0.6) |  | 3 (2.2) |  | 0 (0.0) |
| Philippines | $\bigcirc$ | 95 (2.3) | 1 (0.0) |  | 2 (1.1) |  | 2 (1.1) |
| Russian Federation | $\bigcirc$ | 96 (1.2) | 1 (0.4) |  | 1 (0.4) |  | 2 (0.7) |
| Scotland | - | 19 (3.8) | 0 (0.3) | $r$ | 2 (1.1) | r | 0 (0.3) |
| Singapore | - | 21 (3.3) | 6 (1.9) |  | 14 (3.0) |  | 4 (1.5) |
| Slovenia | $\bigcirc$ | 76 (3.7) | 0 (0.0) |  | 1 (0.8) |  | 0 (0.0) |
| Tunisia | $\bigcirc$ | 89 (2.9) | 2 (1.2) |  | 5 (1.9) |  | 10 (2.7) |
| United States | $\bigcirc$ | 40 (2.4) | 3 (0.8) |  | 7 (1.3) |  | 3 (0.9) |
| International Avg. |  | 58 (0.6) | 2 (0.2) |  | 4 (0.3) |  | 2 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | - | 43 (5.3) | 1 (1.1) |  | 9 (3.4) |  | 1 (0.8) |
| Ontario Province, Can. | - | 43 (4.6) | 1 (0.9) |  | 3 (1.8) |  | 2 (1.3) |
| Quebec Province, Can. | - | 54 (4.7) | 1 (0.6) |  | 2 (1.1) |  | 1 (1.0) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

## What Are the Roles of Homework and Assessment?

The amount of time students spend on homework assignments is an important consideration in examining their opportunity to learn mathematics. Exhibit 7.13 presents the index of teachers' emphasis on mathematics homework. Students in the high category had teachers who reported giving relatively long homework assignments (more than 30 minutes) on a relatively frequent basis (in about half the lessons or more). Those in the low category had teachers who gave short assignments (less than 30 minutes) relatively infrequently (in about half the lessons or less). The medium level includes all other possible combinations of responses.

The results show substantial variation across countries in the emphasis placed on homework. At the eighth grade, more than 70 percent of the students in Romania and Italy were in the high category. For the majority of countries, most students were in the medium category. More than half the students were in the low category in Sweden, Belgium (Flemish), Korea, Japan, and Scotland. It can be noted, however, that students in Japan and perhaps Korea may be more likely to spend extra time in tutoring and special schools than doing homework. ${ }^{1}$ At the eighth grade, there was a slight, but noticeable positive relationship between teachers assigning more homework and students having higher mathematics achievement. At the fourth grade, teachers reported giving homework much less frequently than at eighth grade. On average, internationally, only 14 percent of the fourth-grade students were in the high category. About half (49\%) were in the medium category and 37 percent were in the low category. The fourth-grade students in the high category had the lowest mathematics achievement, on average, suggesting that homework often was being used for remedial purposes.

Exhibit 7.14 presents eighth-grade teachers' reports about how they usually use homework in their mathematics instruction. Internationally, the eighth-grade mathematics teachers reported always or
almost always monitoring whether homework was completed (for 78 percent of the students, on average). For more than half the eighthgrade students, on average, teachers reported always or almost always correcting assignments and giving feedback to students, but for about one-third, on average, the students corrected their own homework in class. About one-fourth of the students, on average, had teachers that reported using homework as basis for class discussion (27\%) and to contribute toward grades or marks ( $25 \%$ ).

As shown in Exhibit 7.15, eighth-grade teachers reported substantial variation across countries in the frequency of testing in mathematics class. On average, internationally, nearly half the students $(47 \%)$ reported having a mathematics test or examination every two weeks or more and another 40 percent reported such testing about once a month. Testing every two weeks or more for most students ( $80 \%$ or more) was reported by eighth-grade teachers in Bahrain, Belgium (Flemish), Chinese Taipei, Lebanon, Lithuania, the Philippines, the Russian Federation, the Slovak Republic, and the Canadian province of Quebec. Even though the international average was low (14\%) for infrequent testing, there were countries where teachers reported testing only a few time a year or more for half or more of the eighthgrade students, including Scotland, Slovenia, Sweden, and England.

Exhibit 7.16 presents eighth-grade teachers' reports about the types of test formats they use for mathematics tests in relation to average mathematics achievement. On average, internationally, more than half the eighth-grade students ( $56 \%$ ) had teachers who used only or mostly constructed-response tests or examinations. These students had higher mathematics achievement, on average, than did students whose teachers used some constructed-response and multiple-choice items or only multiple-choice items. However, very few students ( $12 \%$, on average) had teachers who reported using only or mostly multiplechoice testing.
Index of Teachers'
Emphasis on
Mathematics Homework

Index based on teachers' responses to two questions about how often they usually assign mathematics homework and how many minutes of mathematics homework they usually assign. High level indicates the assignment of more than 30 minutes of homework about half of the lessons or more. Low level indicates no assignment or the assignment of less than 30 minutes of homework about half of the lessons or less. Medium level includes all other possible combinations of responses.


Background data provided by teachers.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde (~) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

## Exhibit 7.13: Index of Teachers' Emphasis on Mathematics Homework (EMH)



| Countries |  | High EMH |  | Medium EMH |  | Low <br> EMH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | $r$ | 46 (4.4) | 460 (6.3) | 51 (4.4) | 451 (5.7) | 3 (1.4) | 453 (28.4) |
| Singapore |  | 35 (4.2) | 593 (7.7) | 49 (3.8) | 596 (8.7) | 16 (2.8) | 598 (11.0) |
| Hong Kong, SAR |  | 33 (4.7) | 575 (5.3) | 63 (4.7) | 577 (4.1) | 4 (1.7) | 552 (8.9) |
| Italy |  | 33 (3.4) | 498 (7.0) | 33 (3.7) | 501 (7.1) | 34 (3.5) | 509 (4.6) |
| Iran, Islamic Rep. of |  | 32 (5.0) | 389 (8.7) | 33 (4.6) | 402 (7.5) | 35 (4.6) | 378 (6.0) |
| Moldova, Rep. of |  | 30 (4.2) | 516 (9.3) | 70 (4.2) | 502 (5.9) | 0 (0.0) | ~ ~ |
| Russian Federation |  | 25 (3.3) | 536 (9.9) | 73 (3.5) | 529 (4.9) | 1 (0.9) | ~ ~ |
| Cyprus |  | 15 (2.9) | 514 (6.1) | 76 (3.5) | 509 (2.8) | 8 (2.2) | 503 (8.8) |
| Tunisia |  | 14 (3.3) | 330 (15.6) | 32 (3.8) | 350 (8.7) | 53 (4.2) | 333 (7.0) |
| Chinese Taipei |  | 11 (2.7) | 555 (8.4) | 52 (4.3) | 568 (2.7) | 37 (3.9) | 561 (3.2) |
| Latvia |  | 8 (1.9) | 542 (8.6) | 86 (2.8) | 536 (3.3) | 5 (2.0) | 517 (15.5) |
| Philippines |  | 8 (2.1) | 322 (19.0) | 71 (4.3) | 360 (10.9) | 21 (3.9) | 367 (17.6) |
| United States |  | 8 (1.3) | 503 (8.8) | 68 (2.8) | 521 (2.8) | 25 (2.8) | 518 (5.6) |
| Hungary |  | 7 (2.3) | 499 (15.2) | 88 (2.8) | 529 (3.7) | 4 (1.7) | 547 (11.7) |
| Norway |  | 7 (2.0) | 448 (10.2) | 46 (4.6) | 451 (4.1) | 47 (4.6) | 452 (3.3) |
| England | $r$ | 5 (2.5) | 483 (25.2) | 13 (3.2) | 553 (10.7) | 82 (4.0) | 531 (4.4) |
| Australia |  | 4 (1.3) | 520 (12.7) | 26 (4.0) | 504 (9.4) | 70 (4.1) | 498 (4.6) |
| Japan |  | 3 (1.5) | 563 (7.9) | 40 (4.3) | 567 (2.4) | 57 (4.4) | 563 (2.5) |
| Slovenia |  | 3 (1.6) | 480 (9.7) | 87 (2.5) | 479 (2.9) | 10 (2.1) | 474 (10.0) |
| Belgium (Flemish) |  | 2 (1.0) | ~ ~ | 10 (2.4) | 544 (4.4) | 88 (2.6) | 551 (2.0) |
| Lithuania |  | 2 (1.0) | ~ ~ | 73 (2.5) | 538 (3.3) | 25 (2.4) | 519 (5.8) |
| Scotland | s | 1 (0.6) | ~ ~ | 20 (4.3) | 503 (6.1) | 80 (4.4) | 491 (4.3) |
| New Zealand |  | 1 (0.4) | ~ ~ | 11 (2.4) | 500 (10.7) | 88 (2.5) | 494 (2.7) |
| Netherlands |  | 0 (0.0) | $\sim \sim$ | 2 (1.4) | ~ ~ | 98 (1.4) | 542 (2.4) |
| Morocco |  | $\mathrm{x} \times$ | x x | x x | x x | x x | x x |
| International Avg. |  | 14 (0.6) | 491 (2.7) | 49 (0.7) | 503 (1.4) | 37 (0.6) | 498 (2.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 10 (3.7) | 523 (8.0) | 75 (5.4) | 537 (4.2) | 15 (4.3) | 521 (6.0) |
| Ontario Province, Can. |  | 6 (2.5) | 472 (10.2) | 42 (4.5) | 513 (8.0) | 53 (4.8) | 513 (3.4) |
| Quebec Province, Can. |  | 8 (2.6) | 500 (9.6) | 18 (3.6) | 503 (5.1) | 74 (4.0) | 508 (3.1) |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

|  | Percentage of Students Whose Teachers Always or Almost Always |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  | Monitor Whether or Not the Homework Was Completed |  | Correct Assignments and Then Give Feedback to Students |  | Have Students Correct Their Own Homework in Class |  | Use the Homework as a Basis for Class Discussion |  | Use the Homework to Contribute Toward Students' Grades/Marks |
| Armenia | r | 86 (2.6) | r | 68 (3.8) | r | 18 (2.9) | r | 16 (2.7) | r | 9 (2.1) |
| Australia |  | 75 (3.4) |  | 56 (3.6) |  | 25 (3.7) |  | 16 (3.2) |  | 22 (3.3) |
| Bahrain |  | 92 (2.4) |  | 91 (2.3) |  | 70 (1.8) |  | 50 (3.9) |  | 66 (2.4) |
| Belgium (Flemish) |  | 88 (2.9) |  | 83 (2.8) |  | 24 (3.3) |  | 7 (1.8) |  | 22 (3.2) |
| Botswana |  | 97 (1.8) |  | 93 (2.4) |  | 31 (4.3) |  | 30 (3.8) |  | 8 (1.6) |
| Bulgaria |  | 79 (3.9) |  | 53 (4.7) |  | 7 (2.2) |  | 22 (3.6) |  | 3 (1.2) |
| Chile |  | 79 (3.4) |  | 72 (3.4) |  | 59 (4.0) |  | 37 (3.9) |  | 20 (3.0) |
| Chinese Taipei |  | 75 (3.6) |  | 48 (4.5) |  | 46 (3.9) |  | 48 (4.5) |  | 57 (4.1) |
| Cyprus |  | 85 (1.9) |  | 84 (1.8) |  | 28 (2.1) |  | 44 (2.6) |  | 46 (2.4) |
| Egypt |  | 80 (3.1) |  | 72 (3.8) |  | 31 (3.5) |  | 37 (3.7) |  | 42 (4.3) |
| Estonia |  | 72 (3.6) |  | 20 (3.3) |  | 19 (3.2) |  | 21 (3.5) |  | 13 (2.2) |
| Ghana |  | 87 (3.3) |  | 83 (3.8) |  | 45 (4.7) |  | 43 (4.6) |  | 52 (4.5) |
| Hong Kong, SAR |  | 86 (3.2) |  | 78 (3.8) |  | 20 (3.5) |  | 23 (3.7) |  | 20 (3.5) |
| Hungary |  | 97 (1.6) |  | 38 (3.6) |  | 73 (3.5) |  | 13 (2.7) |  | 7 (2.2) |
| Indonesia |  | 92 (2.5) |  | 85 (3.0) |  | 22 (3.6) |  | 14 (3.0) |  | 37 (4.2) |
| Iran, Islamic Rep. of |  | 76 (3.5) |  | 43 (3.6) |  | 56 (3.7) |  | 41 (3.6) |  | 38 (3.9) |
| Israel |  | 71 (3.3) |  | 39 (3.7) |  | 29 (3.5) |  | 38 (3.6) |  | 47 (3.5) |
| Italy |  | 82 (2.5) |  | 41 (3.8) |  | 59 (3.7) |  | 48 (3.3) |  | 9 (2.2) |
| Japan |  | 51 (3.7) |  | 15 (2.7) |  | 41 (3.8) |  | 9 (2.3) |  | 24 (3.2) |
| Jordan |  | 83 (3.0) |  | 73 (3.6) |  | 66 (3.9) |  | 54 (3.8) |  | 35 (4.2) |
| Korea, Rep. of | s | 76 (3.0) | s | 13 (2.9) | s | 28 (3.4) | s | 3 (1.3) | $s$ | 28 (3.2) |
| Latvia |  | 80 (3.1) |  | 57 (4.1) |  | 11 (3.0) |  | 9 (2.0) |  | 26 (3.0) |
| Lebanon |  | 77 (3.7) |  | 66 (4.3) |  | 62 (4.6) |  | 44 (4.8) |  | 15 (3.0) |
| Lithuania |  | 67 (3.5) |  | 26 (3.5) |  | 8 (2.3) |  | 6 (1.6) |  | 6 (1.8) |
| Macedonia, Rep. of |  | 69 (4.0) |  | 54 (3.8) |  | 24 (3.8) |  | 27 (3.9) |  | 42 (4.5) |
| Malaysia |  | 89 (2.8) |  | 86 (3.3) |  | 14 (3.0) |  | 31 (3.9) |  | 5 (1.8) |
| Moldova, Rep. of | r | 70 (5.0) | $r$ | 34 (4.7) | $r$ | 33 (4.0) | $r$ | 21 (4.1) | $r$ | 25 (4.5) |
| Morocco | $s$ | 60 (7.0) | s | 79 (6.1) | s | 59 (5.5) | s | 41 (6.4) | $s$ | 8 (3.6) |
| Netherlands |  | 44 (4.5) |  | 39 (5.0) |  | 69 (4.4) |  | 13 (3.0) |  | 4 (1.9) |
| New Zealand |  | 68 (4.9) |  | 34 (4.2) |  | 41 (5.4) |  | 13 (3.4) |  | 12 (3.5) |
| Norway |  | 21 (3.4) |  | 4 (1.6) |  | 12 (2.6) |  | 10 (2.4) |  | 20 (3.6) |
| Palestinian Nat'l Auth. |  | 92 (2.5) |  | 66 (3.8) |  | 66 (3.5) |  | 50 (4.1) |  | 38 (4.2) |
| Philippines |  | 85 (3.6) |  | 83 (3.6) |  | 43 (4.7) |  | 41 (4.5) |  | 55 (4.9) |
| Romania |  | 86 (3.0) |  | 49 (4.1) |  | 15 (3.1) |  | 35 (3.7) |  | 9 (2.3) |
| Russian Federation |  | 86 (3.3) |  | 48 (3.1) |  | 16 (2.3) |  | 8 (1.7) |  | 6 (1.7) |
| Saudi Arabia |  | 95 (1.2) |  | 84 (5.1) |  | 65 (5.5) |  | 42 (5.4) |  | 68 (5.7) |
| Scotland |  | 88 (3.0) |  | 62 (4.6) |  | 13 (3.0) |  | 19 (3.7) |  | 11 (3.0) |
| Serbia |  | 77 (3.4) |  | 38 (3.7) |  | 21 (2.8) |  | 22 (3.4) |  | 11 (2.7) |
| Singapore |  | 89 (1.8) |  | 87 (1.8) |  | 5 (1.2) |  | 24 (2.1) |  | 18 (1.6) |
| Slovak Republic |  | 74 (4.0) |  | 46 (4.2) |  | 19 (3.1) |  | 12 (2.6) |  | 6 (2.1) |
| Slovenia |  | 79 (3.7) |  | 23 (3.2) |  | 60 (3.8) |  | 18 (3.6) |  | 3 (1.5) |
| South Africa |  | 85 (2.5) |  | 80 (2.3) | $r$ | 38 (3.6) | $r$ | 38 (3.9) |  | 30 (3.2) |
| Sweden |  | 67 (3.3) |  | 42 (3.5) |  | 12 (2.6) |  | 7 (1.9) |  | 11 (2.4) |
| Tunisia |  | 68 (4.2) |  | 58 (3.8) |  | 75 (3.5) |  | 30 (4.0) |  | 6 (2.1) |
| United States |  | 90 (1.6) |  | 45 (3.6) |  | 55 (2.8) |  | 50 (3.2) |  | 77 (2.7) |
| \# England | r | 94 (2.0) | ${ }^{r}$ | 72 (5.4) | $r$ | 8 (2.9) | r | 15 (4.4) | ${ }^{r}$ | 37 (6.4) |
| International Avg. |  | 78 (0.5) |  | 57 (0.6) |  | 36 (0.5) |  | 27 (0.5) |  | 25 (0.5) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 79 (4.0) |  | 54 (5.4) |  | 86 (3.5) |  | 29 (4.9) |  | 62 (4.8) |
| Indiana State, US |  | 97 (1.6) |  | 42 (6.5) |  | 58 (5.5) |  | 55 (6.3) |  | 80 (5.8) |
| Ontario Province, Can. |  | 82 (3.6) |  | 47 (4.9) |  | 56 (4.8) |  | 38 (4.7) |  | 38 (5.0) |
| Quebec Province, Can. |  | 64 (4.7) |  | 66 (4.1) |  | 53 (4.5) |  | 24 (3.9) |  | 19 (3.5) |

## Background data provided by teachers.

$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

| Countries |  | Percentage of Students Whose Teachers Give a Mathematics Test or Examination |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Every Two Weeks or More | About Once a Month | A Few Times a Year or Less |
| Armenia | $r$ | 38 (3.7) | 53 (3.8) | 9 (2.0) |
| Australia |  | 19 (3.6) | 64 (4.6) | 16 (3.4) |
| Bahrain |  | 85 (1.7) | 15 (1.7) | 0 (0.0) |
| Belgium (Flemish) |  | 94 (1.7) | 4 (1.5) | 2 (0.9) |
| Botswana |  | 17 (3.6) | 81 (3.8) | 1 (1.3) |
| Bulgaria |  | 31 (4.2) | 46 (4.1) | 23 (3.1) |
| Chile |  | 78 (3.3) | 20 (3.2) | 2 (0.9) |
| Chinese Taipei |  | 99 (0.9) | 1 (0.6) | 1 (0.0) |
| Cyprus |  | 9 (2.0) | 79 (2.7) | 11 (1.7) |
| Egypt |  | - | -- | - - |
| Estonia |  | 67 (4.1) | 32 (4.1) | 1 (0.8) |
| Ghana |  | 75 (3.8) | 25 (3.8) | 1 (0.0) |
| Hong Kong, SAR |  | 43 (4.8) | 39 (4.8) | 18 (3.6) |
| Hungary |  | 68 (4.1) | 30 (3.9) | 2 (1.2) |
| Indonesia |  | 45 (4.2) | 47 (4.4) | 9 (2.6) |
| Iran, Islamic Rep. of | $r$ | 34 (3.6) | 34 (3.9) | 31 (4.4) |
| Israel |  | 57 (4.0) | 34 (3.6) | 9 (2.1) |
| Italy |  | 31 (3.4) | 67 (3.4) | 2 (1.2) |
| Japan |  | 17 (3.4) | 38 (4.4) | 45 (4.3) |
| Jordan |  | 30 (3.6) | 70 (3.6) | 0 (0.0) |
| Korea, Rep. of | s | 63 (3.4) | 33 (3.1) | 5 (1.5) |
| Latvia |  | 71 (4.2) | 28 (4.2) | 1 (0.0) |
| Lebanon |  | 83 (3.4) | 17 (3.4) | 0 (0.0) |
| Lithuania |  | 80 (3.2) | 19 (3.1) | 0 (0.0) |
| Macedonia, Rep. of |  | 23 (3.8) | 49 (4.3) | 27 (3.7) |
| Malaysia |  | 5 (1.4) | 48 (3.8) | 47 (3.9) |
| Moldova, Rep. of | $r$ | 67 (4.5) | 30 (4.7) | 3 (1.6) |
| Morocco |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ | $\mathrm{x} \times$ |
| Netherlands |  | 43 (4.8) | 57 (4.8) | 0 (0.0) |
| New Zealand |  | 25 (4.4) | 59 (4.6) | 16 (4.0) |
| Norway |  | 6 (2.5) | 64 (4.4) | 30 (4.0) |
| Palestinian Nat'l Auth. |  | 61 (2.7) | 38 (2.8) | 1 (0.0) |
| Philippines |  | 93 (2.4) | 5 (1.9) | 2 (1.4) |
| Romania |  | 73 (3.9) | 25 (3.7) | 2 (1.2) |
| Russian Federation |  | 88 (2.5) | 11 (2.3) | 1 (0.9) |
| Saudi Arabia |  | 45 (5.8) | 43 (5.8) | 11 (2.8) |
| Scotland |  | 14 (3.2) | 31 (4.5) | 55 (4.6) |
| Serbia |  | 15 (2.8) | 66 (4.1) | 18 (3.2) |
| Singapore |  | 31 (1.8) | 57 (2.4) | 12 (1.5) |
| Slovak Republic |  | 81 (3.3) | 17 (3.1) | 2 (1.2) |
| Slovenia |  | 2 (1.2) | 47 (3.7) | 51 (3.8) |
| South Africa | $r$ | 41 (3.8) | 53 (4.0) | 6 (1.6) |
| Sweden |  | 1 (1.0) | 28 (3.5) | 70 (3.4) |
| Tunisia | s | 21 (4.4) | 74 (5.0) | 6 (2.5) |
| United States |  | 73 (2.6) | 24 (2.7) | 3 (1.1) |
| $\ddagger$ England | $r$ | 9 (2.6) | 38 (6.2) | 53 (6.5) |
| International Avg. |  | 47 (0.5) | 40 (0.6) | 14 (0.4) |
| Benchmarking Participants |  |  |  |  |
| Basque Country, Spain |  | 51 (4.7) | 48 (4.5) | 1 (1.4) |
| Indiana State, US |  | 77 (4.8) | 22 (4.8) | 1 (0.1) |
| Ontario Province, Can. |  | 84 (3.2) | 15 (3.0) | 1 (1.0) |
| Quebec Province, Can. |  | 61 (4.2) | 33 (4.2) | 6 (2.4) |

Background data provided by teachers.
¥ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

\section*{| Only or Mostly |  |
| :---: | :---: |
| Countries | $\begin{array}{c}\text { Constructed-Response }\end{array}$ |}


| Countries |  |
| :---: | :---: |
|  |  |
| Armenia | $r$ |


| Australia |
| :--- |
| Bahrain |

Belgium (Flemish)
Botswana
Bulgaria

| Bulgaria |
| :--- |
| Chile |
| Chinese Taipei |


| Cyprus |
| :--- | :--- |
| Egypt |
| Estonia |


| Ghana |
| :--- |
| Hong Kong, SAR |
| Hungary |


| Indonesia |
| :--- |
| Iran, Islamic Rep. of $s$ |


| Israel |
| :--- |
| Italy |


| Japan |
| :--- |
| Jordan |


| Korea, Rep. of $s$ |
| :--- |
| Latvia |


| Lebanon | 24 |
| :--- | :--- |
| Lithuania | 85 |


| Macedonia, Rep. of |  |  |
| :--- | :--- | :--- |
| Malaysia |  |  |
| Moldova, Rep. of | r | 29 |


| Morocco |  |
| :--- | :--- |
| Netherlands | 9 |
| New Zealand | 72 |


| Norway |
| :--- | :--- |
| Palestinian Nat'l Auth. |
| Philippines |


| Romania | 35 |
| :--- | :--- |
| Russian Federation | 78 |


| Saudi Arabia |
| :--- | :--- |
| Scotland |
| Serbia |


| Singapore | 8 |
| :--- | :--- |
| Slovak Republic | 98 |
| Slovenia | 88 |


| South Africa | $r$ | 4 |
| :--- | :--- | :--- |
| Sweden |  | 84 |
| Tunisia | $s$ |  |


| Tunisia | s | $8(3.0)$ | $413(11.7)$ | $20(4.3)$ | $412(5.3)$ | $72(4.6)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| United States | $55(3.3)$ | $516(4.2)$ | $31(3.1)$ | $487(5.7)$ | $14(2.0)$ | $512(4.3)$ |
| England | s | $97(2.0)$ | $509(6.6)$ | $3(2.0)$ | $392(33.1)$ | $0(0.0)$ |
| International Avg. | $56(0.5)$ | $472(0.9)$ | $32(0.5)$ | $463(1.4)$ | $12(0.4)$ | $\sim \sim$ |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | $33(4.5)$ | $487(5.3)$ | $17(3.9)$ | $482(6.2)$ | $50(5.4)$ | $490(4.1)$ |
| Indiana State, US |  | $71(6.0)$ | $513(6.1)$ | $22(6.2)$ | $497(13.5)$ | $7(3.1)$ |
| Ontario Province, Can. | r | $82(4.0)$ | $524(3.8)$ | $17(3.9)$ | $513(8.2)$ | $1(0.1)$ |
| Quebec Province, Can. | xx | xx | xx | xx | $\sim \sim$ |  |

## Background data provided by teachers.

a Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash $(-)$ indicates comparable data are not available. A tilde ( $\sim$ ) indicates insufficient data to report achievement.
"An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students."


## Chapter 8

## School Contexts for Learning

 and InstructionChapter 8 presents findings about the school contexts for learning and instruction in mathematics, including school characteristics, policies, and practices. Information is presented about the economic status of the student body, the extent of school resources in each country, the school climate, attendance problems, and school safety.

## What Are the Schools' Demographic Characteristics?

Exhibit 8.1 presents principals' reports about the economic background of the students in their schools. Internationally, about one-fifth of the eighth-grade students ( $22 \%$ ), on average, attended schools with few students (less than $10 \%$ ) from economically disadvantaged homes, 26 percent attended schools with 11 to 25 percent disadvantaged students, 21 percent attended schools with 26 to 50 percent economically disadvantaged students, and 31 percent attended schools with more than 50 percent economically disadvantaged students. There was considerable variation across countries, however. In some countries more than half the students ( 52 to $85 \%$ ) attended schools where the majority of the students came from disadvantaged homes, including Chile, Ghana, Indonesia, Lebanon, Malaysia, Morocco, the Palestinian National Authority, the Philippines, South Africa, and Tunisia.

At the fourth grade across the participating countries, 34 percent of the students, on average, attended schools with few students (less 10 percent) from economically disadvantaged homes, 25 percent attended schools with 11 to 25 percent disadvantaged students, 18 percent attended schools with 26 to 50 percent economically disadvantaged students, and 24 percent attended schools with more than 50 percent economically disadvantaged students. Among the countries participating at the fourth grade, 75 percent of the students in Morocco attended schools where the majority of the students came from disadvantaged homes, but it was the only one where more than half the students attended such schools.

At the eighth grade, on average, internationally, mathematics achievement for students in schools with few students from economically disadvantaged homes was 57 scale-score points greater than that for students attending schools with more than half their student population from disadvantaged homes (496 vs. 439). At the fourth grade, this difference also was substantial -47 points ( 515 vs. 468 ).

Exhibit 8.1: Principals' Reports on the Percentages of Students in Their Schools Coming from

| Countries |  | Schools with Few (0-10\%) Economically Disadvantaged Students |  | Schools with 11-25\% Economically Disadvantaged Students |  | Schools with 26-50\% Economically Disadvantaged Students |  | Schools with More than 50\% Economically Disadvantaged Students |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | $r$ | 3 (1.6) | 462 (21.8) | 21 (3.6) | 480 (6.2) | 29 (4.3) | 484 (6.3) | 47 (4.8) | 476 (4.5) |
| Australia |  | 32 (4.6) | 521 (8.4) | 35 (4.2) | 518 (9.9) | 23 (3.3) | 487 (10.3) | 9 (2.3) | 473 (9.8) |
| Bahrain |  | 16 (0.1) | 423 (3.4) | 20 (0.1) | 397 (3.3) | 33 (0.2) | 408 (2.5) | 31 (0.2) | 381 (3.8) |
| Belgium (Flemish) |  | 53 (3.7) | 559 (4.0) | 36 (3.9) | 526 (5.4) | 7 (2.2) | 499 (21.0) | 4 (1.7) | 404 (24.2) |
| Botswana |  | 15 (3.6) | 385 (11.0) | 22 (3.6) | 375 (6.2) | 25 (3.9) | 363 (3.2) | 38 (4.6) | 354 (3.2) |
| Bulgaria |  | 20 (3.3) | 509 (12.8) | 25 (4.2) | 480 (12.0) | 25 (3.6) | 451 (6.9) | 30 (3.9) | 469 (6.7) |
| Chile |  | 19 (2.7) | 454 (9.9) | 12 (2.2) | 403 (9.3) | 17 (3.1) | 392 (8.1) | 52 (3.7) | 353 (4.4) |
| Chinese Taipei |  | 67 (3.5) | 596 (5.3) | 25 (3.5) | 576 (8.6) | 5 (1.8) | 572 (11.8) | 3 (1.5) | 463 (12.1) |
| Cyprus |  | 38 (0.3) | 469 (2.2) | 35 (0.3) | 456 (3.2) | 15 (0.2) | 449 (3.7) | 11 (0.3) | 448 (3.4) |
| Egypt |  | 11 (2.5) | 448 (11.8) | 24 (3.7) | 410 (8.2) | 23 (3.5) | 393 (6.3) | 42 (3.8) | 392 (5.5) |
| Estonia |  | 13 (3.1) | 549 (9.3) | 45 (4.5) | 532 (4.2) | 25 (3.7) | 526 (6.2) | 18 (2.7) | 514 (6.1) |
| Ghana |  | 4 (1.6) | 295 (24.1) | 8 (2.5) | 308 (14.9) | 18 (3.5) | 286 (9.0) | 71 (4.3) | 264 (5.9) |
| Hong Kong, SAR |  | 14 (3.5) | 619 (8.3) | 27 (4.0) | 579 (11.5) | 24 (3.9) | 582 (9.7) | 35 (4.6) | 571 (8.5) |
| Hungary |  | 15 (3.0) | 557 (9.0) | 23 (3.3) | 542 (6.6) | 35 (4.3) | 527 (5.5) | 27 (3.9) | 503 (8.3) |
| Indonesia |  | 5 (1.9) | 485 (34.5) | 17 (3.5) | 423 (10.6) | 24 (3.5) | 421 (10.5) | 54 (4.1) | 395 (7.5) |
| Iran, Islamic Rep. of |  | 15 (2.6) | 458 (5.9) | 12 (2.2) | 426 (7.4) | 25 (3.5) | 408 (6.2) | 49 (4.1) | 394 (3.3) |
| Israel |  | 15 (3.1) | 531 (7.5) | 35 (3.8) | 517 (5.9) | 26 (4.1) | 483 (8.6) | 25 (3.3) | 467 (7.6) |
| Italy |  | 45 (3.4) | 496 (3.4) | 33 (3.8) | 482 (7.0) | 13 (2.4) | 465 (9.9) | 10 (2.2) | 452 (8.3) |
| Japan |  | 72 (3.6) | 575 (2.6) | 23 (3.3) | 562 (4.0) | 4 (1.7) | 553 (3.8) | 1 (0.0) | ~ ~ |
| Jordan |  | 14 (3.2) | 453 (16.8) | 22 (4.2) | 422 (7.4) | 24 (3.5) | 424 (6.4) | 40 (4.5) | 417 (6.8) |
| Korea, Rep. of |  | 34 (3.7) | 607 (3.8) | 40 (4.1) | 587 (3.2) | 16 (3.0) | 576 (3.7) | 10 (2.5) | 563 (6.1) |
| Latvia |  | 22 (4.1) | 523 (5.7) | 44 (4.6) | 510 (5.2) | 18 (3.3) | 494 (6.8) | 16 (3.5) | 492 (7.1) |
| Lebanon |  | 8 (2.6) | 415 (13.0) | 17 (3.2) | 454 (8.8) | 15 (2.7) | 449 (7.1) | 61 (4.0) | 426 (4.7) |
| Lithuania | $r$ | 20 (4.1) | 530 (6.5) | 41 (4.9) | 506 (3.9) | 31 (4.4) | 481 (4.5) | 8 (2.5) | 461 (13.6) |
| Macedonia, Rep. of |  | 11 (2.6) | 468 (16.4) | 19 (3.5) | 448 (13.6) | 35 (4.6) | 431 (6.6) | 36 (4.5) | 418 (7.0) |
| Malaysia |  | 8 (2.3) | 555 (16.2) | 12 (2.8) | 523 (11.7) | 17 (3.3) | 514 (12.3) | 64 (4.0) | 499 (4.6) |
| Moldova, Rep. of | $r$ | 7 (2.4) | 450 (18.4) | 16 (3.7) | 447 (7.4) | 35 (4.4) | 466 (7.0) | 42 (4.8) | 455 (8.7) |
| Morocco | $s$ | 0 (0.0) | ~ ~ | 5 (2.2) | 380 (13.7) | 16 (4.1) | 390 (6.0) | 79 (4.6) | 384 (3.0) |
| Netherlands |  | 60 (4.6) | 563 (6.0) | 26 (4.0) | 505 (8.1) | 10 (2.6) | 490 (11.6) | 5 (2.3) | 465 (12.6) |
| New Zealand |  | 36 (4.2) | 527 (8.9) | 30 (5.6) | 497 (8.1) | 16 (3.2) | 469 (15.0) | 18 (2.3) | 449 (11.3) |
| Norway |  | - - | - - | - - | - - | - - | - - | - - | - - |
| Palestinian Nat'l Auth. |  | 6 (2.0) | 407 (20.2) | 11 (2.6) | 389 (9.4) | 28 (3.8) | 394 (5.3) | 55 (3.7) | 387 (5.1) |
| Philippines |  | 9 (2.7) | 379 (22.3) | 16 (2.6) | 411 (15.3) | 22 (3.9) | 381 (9.3) | 53 (4.4) | 363 (7.1) |
| Romania |  | 11 (2.9) | 513 (14.1) | 18 (3.2) | 494 (10.7) | 21 (3.0) | 467 (8.1) | 50 (4.2) | 465 (6.9) |
| Russian Federation |  | 19 (2.9) | 525 (7.1) | 36 (3.0) | 510 (4.4) | 24 (2.8) | 504 (7.3) | 20 (2.9) | 493 (6.0) |
| Saudi Arabia |  | 19 (3.7) | 346 (6.7) | 28 (4.3) | 336 (9.5) | 29 (5.3) | 320 (11.7) | 24 (3.9) | 324 (10.2) |
| Scotland | s | 28 (4.7) | 525 (10.4) | 44 (5.6) | 512 (7.6) | 23 (4.7) | 477 (11.3) | 6 (2.7) | 452 (12.8) |
| Serbia |  | 10 (2.2) | 495 (11.2) | 28 (4.0) | 478 (5.8) | 23 (4.0) | 472 (6.6) | 39 (4.2) | 472 (3.6) |
| Singapore |  | 57 (0.0) | 617 (5.0) | 28 (0.0) | 596 (7.6) | 10 (0.0) | 566 (16.1) | 5 (0.0) | 578 (14.8) |
| Slovak Republic |  | 16 (2.9) | 528 (8.2) | 43 (4.8) | 510 (5.5) | 25 (3.3) | 495 (6.3) | 16 (3.6) | 494 (10.3) |
| Slovenia |  | 23 (4.0) | 499 (5.2) | 43 (4.6) | 494 (3.8) | 23 (4.1) | 488 (5.5) | 11 (2.7) | 483 (6.8) |
| South Africa |  | 3 (1.3) | 479 (44.9) | 2 (1.0) | ~ | 9 (2.4) | 334 (25.7) | 85 (2.8) | 237 (3.4) |
| Sweden | $r$ | 47 (4.0) | 515 (4.2) | 32 (4.1) | 491 (6.1) | 19 (3.8) | 487 (6.8) | 2 (1.1) | ~ |
| Tunisia |  | 10 (2.6) | 439 (8.9) | 15 (2.7) | 427 (4.4) | 17 (2.9) | 410 (4.4) | 59 (4.2) | 400 (2.4) |
| United States | $r$ | 28 (2.9) | 539 (6.8) | 23 (3.1) | 525 (6.4) | 25 (3.1) | 496 (5.1) | 24 (2.8) | 464 (4.5) |
| \# England | s | 32 (5.3) | 534 (13.4) | 33 (6.0) | 505 (10.8) | 22 (6.2) | 491 (16.4) | 13 (4.2) | 457 (12.2) |
| International Avg. |  | 22 (0.5) | 496 (2.1) | 26 (0.5) | 476 (1.3) | 21 (0.5) | 460 (1.5) | 31 (0.5) | 439 (1.3) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 65 (4.9) | 492 (3.8) | 20 (3.8) | 483 (6.1) | 9 (3.1) | 467 (8.9) | 7 (2.4) | 476 (9.9) |
| Indiana State, US |  | 9 (4.3) | 541 (17.6) | 38 (7.5) | 538 (7.2) | 36 (6.7) | 485 (7.6) | 17 (4.9) | 479 (9.5) |
| Ontario Province, Can. |  | 41 (4.7) | 532 (4.0) | 29 (4.5) | 520 (5.4) | 14 (3.5) | 518 (7.2) | 16 (3.3) | 496 (7.9) |
| Quebec Province, Can. |  | 44 (4.7) | 560 (6.4) | 30 (4.9) | 541 (4.6) | 15 (3.0) | 532 (8.6) | 11 (2.5) | 515 (7.4) |

## Background data provided by schools.

\# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates comparable data are not available. A tilde $(\sim)$ indicates insufficient data to report achievement.
An " r " indicates data are available for at least 70 but less than $85 \%$ of the students. An "s" indicates data are available for at least 50 but less than $70 \%$ of the students.

## Exhibit 8.1: Principals' Reports on the Percentages of Students in Their Schools Coming from

 Economically Disadvantaged Homes

| Countries |  | Schools with Few (0-10\%) Economically Disadvantaged Students |  | Schools with 11-25\% Economically Disadvantaged Students |  | Schools with 26-50\% Economically Disadvantaged Students |  | Schools with More than $50 \%$ Economically Disadvantaged Students |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | $r$ | 4 (1.7) | 471 (29.6) | 21 (3.5) | 457 (8.5) | 28 (4.1) | 453 (8.3) | 48 (4.6) | 455 (6.2) |
| Australia |  | 34 (4.4) | 520 (7.1) | 30 (4.0) | 498 (6.6) | 21 (3.6) | 486 (7.4) | 15 (4.0) | 456 (11.1) |
| Belgium (Flemish) |  | 59 (4.4) | 558 (1.9) | 27 (4.0) | 552 (3.5) | 7 (2.1) | 521 (5.2) | 7 (2.7) | 516 (16.0) |
| Chinese Taipei |  | 80 (3.4) | 567 (2.1) | 15 (3.0) | 559 (3.1) | 4 (1.5) | 521 (17.5) | 2 (0.9) | $\sim \sim$ |
| Cyprus |  | 58 (4.5) | 518 (3.0) | 30 (4.4) | 502 (5.0) | 6 (2.2) | 509 (8.6) | 5 (1.1) | 482 (13.6) |
| England | $r$ | 38 (4.4) | 559 (7.0) | 25 (4.5) | 528 (6.9) | 11 (3.0) | 529 (12.2) | 25 (4.2) | 484 (8.8) |
| Hong Kong, SAR |  | 23 (4.4) | 591 (5.8) | 26 (3.5) | 574 (6.1) | 25 (4.9) | 579 (6.4) | 25 (4.4) | 559 (5.6) |
| Hungary |  | 15 (3.3) | 555 (6.5) | 24 (4.2) | 533 (5.8) | 31 (4.0) | 530 (6.5) | 30 (3.6) | 505 (6.3) |
| Iran, Islamic Rep. of |  | 17 (3.5) | 429 (10.3) | 11 (3.2) | 398 (10.8) | 22 (4.3) | 394 (9.1) | 50 (4.7) | 369 (5.9) |
| Italy |  | 46 (4.1) | 510 (3.8) | 37 (3.8) | 502 (6.7) | 10 (2.4) | 478 (10.7) | 8 (1.6) | 495 (19.3) |
| Japan |  | 74 (3.9) | 566 (2.0) | 22 (3.6) | 559 (3.4) | 4 (1.5) | 559 (11.0) | 0 (0.0) | ~ ~ |
| Latvia |  | 23 (3.7) | 554 (5.4) | 42 (4.8) | 543 (4.9) | 22 (4.0) | 520 (8.8) | 14 (3.3) | 507 (7.5) |
| Lithuania |  | 26 (3.8) | 560 (6.5) | 33 (4.5) | 540 (5.8) | 31 (3.8) | 513 (5.0) | 11 (2.9) | 512 (9.7) |
| Moldova, Rep. of | $r$ | 10 (3.0) | 496 (27.5) | 17 (3.1) | 509 (10.0) | 31 (4.7) | 505 (14.4) | 43 (5.2) | 498 (6.7) |
| Morocco | $r$ | 3 (1.2) | 352 (34.9) | 4 (1.5) | 338 (11.5) | 18 (3.5) | 337 (11.5) | 75 (3.8) | 352 (6.4) |
| Netherlands |  | 64 (4.0) | 552 (2.1) | 17 (3.5) | 540 (5.1) | 8 (2.5) | 522 (8.2) | 10 (2.0) | 496 (10.2) |
| New Zealand |  | 44 (3.2) | 526 (3.9) | 22 (3.5) | 491 (5.6) | 12 (2.3) | 474 (6.7) | 22 (2.5) | 444 (7.0) |
| Norway |  | - - | - - | - - | - - | - - | - - | - - | - - |
| Philippines |  | 12 (2.7) | 368 (24.2) | 14 (3.5) | 385 (23.5) | 25 (3.9) | 335 (10.4) | 48 (4.8) | 345 (8.0) |
| Russian Federation |  | 18 (2.5) | 548 (10.5) | 33 (3.6) | 531 (8.2) | 26 (3.0) | 536 (7.8) | 23 (3.6) | 512 (8.6) |
| Scotland | $r$ | 36 (4.5) | 509 (4.4) | 31 (4.6) | 489 (4.6) | 17 (4.3) | 469 (5.3) | 15 (3.4) | 459 (6.3) |
| Singapore |  | 64 (3.7) | 608 (7.0) | 25 (3.2) | 568 (9.5) | 6 (1.7) | 564 (23.7) | 4 (1.6) | 575 (19.4) |
| Slovenia |  | 24 (4.0) | 485 (5.9) | 43 (4.6) | 478 (4.3) | 22 (4.0) | 470 (6.3) | 11 (2.7) | 483 (9.4) |
| Tunisia |  | 20 (3.1) | 387 (11.4) | 16 (2.9) | 334 (12.1) | 15 (3.0) | 337 (12.1) | 49 (3.6) | 318 (6.7) |
| United States |  | 19 (2.8) | 561 (4.1) | 23 (2.6) | 541 (4.7) | 20 (2.9) | 523 (4.8) | 38 (2.6) | 484 (3.3) |
| International Avg. |  | 34 (0.7) | 515 (2.7) | 25 (0.8) | 498 (1.7) | 18 (0.7) | 486 (2.2) | 24 (0.7) | 468 (2.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 19 (4.5) | 558 (7.1) | 27 (6.2) | 549 (5.5) | 28 (6.6) | 528 (5.7) | 26 (3.9) | 503 (6.3) |
| Ontario Province, Can. |  | 48 (5.5) | 520 (4.4) | 20 (4.1) | 522 (14.3) | 15 (3.8) | 502 (8.8) | 17 (4.1) | 482 (6.0) |
| Quebec Province, Can. |  | 41 (4.4) | 515 (4.1) | 30 (3.7) | 498 (3.3) | 13 (3.2) | 494 (5.5) | 17 (3.3) | 500 (7.0) |

[^75][^76]
## What Is the Level of School-Home Involvement?

To measure the extent to which schools expected parents to participate in school-related events, TIMSS asked about five activities: attending special events, raising funds for the school, volunteering for school projects, ensuring their child completes his/her homework, and serving on school committees. The results are presented in Exhibit 8.2. At both the eighth and fourth grades, the common activities across countries were attending special events ( $89 \%$ and $91 \%$, respectively) and ensuring that homework was completed ( $87 \%$ and $91 \%$, respectively.) Also at both grades, expecting parents to volunteer for school projects was the next activity schools expected on a relatively frequent basis (71 \% and $82 \%$, respectively), followed by serving on committees ( $62 \%$ and $68 \%$ ) and raising funds for the school ( $57 \%$ and $64 \%$ ).

| Countries | Percentages of Students Whose Schools Reported That They Expect Parents to Be Involved in the School-Related Activity |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Attend Special Events (e.g., Science Fair, Concert, Sporting Events) | Raise Funds for the School | Volunteer for School Projects, Programs, and Trips | Ensure That Their Child Completes His/Her Homework | Serve on School Committees (e.g., Select School Personnel, Review School Finances) |
| Armenia | 94 (2.5) | 57 (4.7) | 73 (4.0) | 92 (2.5) | 87 (3.1) |
| Australia | 96 (1.0) | 71 (4.1) | 64 (4.4) | 98 (1.0) | 90 (3.0) |
| Bahrain | 81 (0.2) | 29 (0.2) | 39 (0.2) | 75 (0.2) | 14 (0.1) |
| Belgium (Flemish) | 65 (4.4) | 18 (3.5) | 44 (4.2) | 89 (2.5) | 7 (2.3) |
| Botswana | 93 (2.6) | 99 (1.0) | 88 (3.0) | 97 (1.4) | 88 (3.1) |
| Bulgaria | 93 (2.2) | 71 (4.1) | 65 (4.1) | 84 (3.2) | 71 (4.0) |
| Chile | 93 (2.1) | 61 (3.6) | 86 (2.5) | 96 (1.7) | 21 (3.4) |
| Chinese Taipei | 99 (0.7) | 75 (3.1) | 97 (1.5) | 98 (1.0) | 86 (2.8) |
| Cyprus | 100 (0.0) | 97 (0.1) | 62 (0.3) | 100 (0.0) | 53 (0.3) |
| Egypt | 78 (3.4) | 37 (4.3) | 61 (4.1) | 70 (4.1) | 55 (3.9) |
| Estonia | 98 (1.1) | 27 (4.0) | 87 (2.8) | 95 (1.9) | 86 (3.4) |
| Ghana | 93 (2.5) | 93 (2.7) | 82 (4.0) | 91 (2.7) | 84 (3.8) |
| Hong Kong, SAR | 93 (2.5) | 81 (3.6) | 89 (3.1) | 94 (2.5) | 47 (4.8) |
| Hungary | 85 (3.1) | 53 (4.6) | 87 (2.4) | 91 (2.2) | 48 (4.1) |
| Indonesia | 89 (2.6) | 94 (2.3) | 72 (3.8) | 99 (0.9) | 66 (3.7) |
| Iran, Islamic Rep. of | 91 (2.2) | 83 (3.0) | 82 (3.1) | 91 (2.2) | 76 (3.6) |
| Israel | 96 (1.8) | 46 (3.9) | 81 (3.1) | 83 (3.5) | 68 (4.0) |
| Italy | 97 (1.3) | 38 (3.7) | 58 (4.1) | 97 (1.3) | 67 (3.6) |
| Japan | 95 (1.7) | 15 (2.7) | 81 (3.3) | 74 (3.7) | 30 (3.9) |
| Jordan | 89 (3.0) | 21 (3.5) | 42 (4.6) | 73 (3.9) | 25 (3.5) |
| Korea, Rep. of | 83 (3.5) | 36 (4.0) | 49 (4.1) | 83 (2.9) | 82 (2.9) |
| Latvia | 91 (2.7) | 55 (4.4) | 73 (4.0) | 82 (3.7) | 84 (3.6) |
| Lebanon | 68 (4.0) | 40 (4.2) | 42 (4.7) | 79 (3.0) | 64 (4.5) |
| Lithuania | 99 (0.7) | 70 (3.6) | 90 (2.6) | 92 (2.3) | 93 (2.2) |
| Macedonia, Rep. of | 93 (2.2) | 68 (4.0) | 77 (3.7) | 90 (2.8) | 98 (1.2) |
| Malaysia | 93 (2.0) | 83 (3.5) | 87 (2.8) | 96 (1.8) | 23 (3.5) |
| Moldova, Rep. of | 74 (4.6) | 79 (3.5) | 61 (4.5) | 64 (4.8) | 75 (4.4) |
| Morocco | s $\quad 87(3.8)$ | s 80 (4.7) | $\mathrm{s} \quad 81$ (4.3) | 70 (5.5) | 50 (6.1) |
| Netherlands | 58 (4.8) | 9 (2.3) | 29 (4.7) | 95 (1.8) | 43 (5.3) |
| New Zealand | 88 (3.8) | 53 (4.0) | 67 (4.8) | 95 (2.2) | 72 (5.5) |
| Norway | 89 (2.4) | 12 (2.3) | 77 (3.8) | 94 (2.1) | 92 (2.6) |
| Palestinian Nat'l Auth. | 95 (1.9) | 52 (4.1) | 62 (4.3) | 70 (4.1) | 12 (3.0) |
| Philippines | 91 (2.6) | 85 (2.7) | 86 (3.1) | 89 (3.1) | 53 (4.5) |
| Romania | 80 (3.8) | 80 (3.2) | 60 (4.0) | 80 (3.7) | 49 (3.8) |
| Russian Federation | 94 (1.8) | 64 (4.3) | 89 (2.1) | 84 (2.5) | 83 (2.4) |
| Saudi Arabia | 87 (2.1) | 13 (3.3) | 41 (5.1) | 58 (3.9) | 44 (5.0) |
| Scotland | s $\quad 98$ (1.4) | s 82 (4.6) | s $\quad 58$ (4.7) | 92 (3.2) | 79 (4.2) |
| Serbia | 96 (1.7) | 73 (3.5) | 89 (2.6) | 87 (3.0) | 79 (4.2) |
| Singapore | 88 (0.0) | 65 (0.0) | 81 (0.0) | 98 (0.0) | 64 (0.0) |
| Slovak Republic | 83 (3.2) | 80 (3.6) | 92 (2.2) | 95 (2.2) | 85 (3.1) |
| Slovenia | 97 (1.4) | 49 (5.0) | 69 (3.7) | 94 (1.9) | 60 (4.7) |
| South Africa | 95 (1.5) | 91 (2.2) | 91 (2.0) | 94 (2.1) | 100 (0.3) |
| Sweden | 85 (2.7) | 9 (2.5) | 65 (4.1) | 98 (1.1) | 63 (4.1) |
| Tunisia | 60 (4.4) | 19 (3.2) | 32 (3.9) | 40 (4.4) | 9 (2.4) |
| United States | 98 (0.9) | 63 (3.1) | 90 (2.1) | 98 (1.0) | 74 (3.5) |
| \# England | - - | - - | - - | - | - - |
| International Avg. | 89 (0.4) | 57 (0.5) | 71 (0.5) | 87 (0.4) | 62 (0.5) |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | 83 (3.5) | 36 (5.3) | 74 (4.5) | 88 (3.4) | 89 (3.6) |
| Indiana State, US | 98 (2.2) | 63 (7.6) | 88 (4.9) | 97 (2.3) | 86 (5.4) |
| Ontario Province, Can. | 96 (1.9) | 86 (3.2) | 94 (2.3) | 100 (0.0) | 74 (4.5) |
| Quebec Province, Can. | 92 (2.9) | 70 (4.8) | 62 (4.6) | 98 (1.0) | 66 (4.8) |

[^77]Exhibit 8.2: Schools' Expectations for Parents' Involvement


| Countries | Percentages of Students Whose Schools Reported That They Expect Parents to Be Involved in the School-Related Activity |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Attend Special Events (e.g., Science Fair, Concert, Sporting Events) | Raise Funds for the School | Volunteer for School Projects, Programs, and Trips | Ensure That Their Child Completes His/Her Homework | Serve on School Committees (e.g., Select School Personnel, Review School Finances) |
| Armenia | 95 (1.9) | 55 (4.3) | 72 (4.2) | 94 (2.2) | 88 (2.7) |
| Australia | 97 (1.6) | 95 (2.2) | 91 (2.8) | 97 (1.9) | 92 (2.6) |
| Belgium (Flemish) | 60 (4.6) | 42 (4.6) | 84 (3.4) | 98 (1.2) | 4 (1.5) |
| Chinese Taipei | 100 (0.0) | 73 (3.6) | 99 (0.6) | 100 (0.0) | 90 (2.1) |
| Cyprus | 95 (2.2) | 90 (3.0) | 52 (4.9) | 99 (0.8) | 77 (4.5) |
| England | - | - - | - | - - | - - |
| Hong Kong, SAR | 98 (1.2) | 79 (4.2) | 99 (0.9) | 99 (0.8) | 52 (4.5) |
| Hungary | 84 (3.0) | 60 (4.4) | 91 (2.2) | 94 (2.2) | 50 (3.4) |
| Iran, Islamic Rep. of | 88 (2.2) | 88 (2.7) | 83 (3.5) | 98 (1.2) | 75 (4.3) |
| Italy | 100 (0.0) | 37 (3.7) | 63 (3.6) | 97 (1.4) | 63 (3.1) |
| Japan | 97 (1.5) | 8 (2.5) | 94 (1.9) | 80 (3.5) | 20 (3.4) |
| Latvia | 94 (2.0) | 59 (4.5) | 78 (3.7) | 84 (3.3) | 86 (3.1) |
| Lithuania | 100 (0.0) | 70 (3.9) | 84 (3.4) | 94 (1.9) | 91 (2.6) |
| Moldova, Rep. of | 71 (4.1) | 71 (4.5) | 53 (4.5) | 65 (4.4) | 69 (4.1) |
| Morocco | 81 (3.0) | 68 (4.1) | 67 (3.8) | 69 (4.4) | 56 (4.5) |
| Netherlands | 77 (4.7) | 42 (4.5) | 96 (1.6) | 93 (2.6) | 85 (3.5) |
| New Zealand | 97 (1.3) | 90 (2.0) | 99 (0.7) | 97 (1.0) | 88 (2.4) |
| Norway | 97 (1.6) | 17 (3.4) | 89 (3.0) | 98 (1.2) | 91 (2.7) |
| Philippines | 93 (2.1) | 86 (2.7) | 83 (3.5) | 91 (2.9) | 65 (4.1) |
| Russian Federation | 98 (0.9) | 64 (4.0) | 92 (1.8) | 95 (1.8) | 83 (3.0) |
| Scotland | 100 (0.0) | 98 (1.2) | 94 (1.8) | 99 (1.0) | 85 (3.5) |
| Singapore | 96 (1.6) | 75 (3.5) | 96 (1.5) | 99 (0.7) | 57 (4.3) |
| Slovenia | 97 (1.3) | 50 (4.8) | 69 (3.8) | 96 (1.3) | 59 (4.8) |
| Tunisia | 73 (3.6) | 41 (4.0) | 52 (3.7) | 53 (3.8) | 28 (3.4) |
| United States | 96 (1.4) | 85 (2.3) | 97 (1.2) | 99 (0.7) | 82 (3.1) |
| International Avg. | 91 (0.5) | 64 (0.7) | 82 (0.6) | 91 (0.5) | 68 (0.7) |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US | 97 (2.3) | 89 (4.5) | 99 (1.2) | 100 (0.0) | 73 (5.5) |
| Ontario Province, Can. | 96 (2.0) | 91 (2.3) | 97 (1.9) | 100 (0.0) | 76 (4.5) |
| Quebec Province, Can. | 96 (1.8) | 92 (2.7) | 96 (1.7) | 100 (0.0) | 67 (4.6) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.

## What School Resources Are Available to Support Mathematics Learning?

Some school resources are specific to mathematics, but many are general resources that improve learning opportunities across the curriculum. All the available resources, however, can work together to support mathematics learning and instruction.

To measure the extent of school resources in each of the participating countries, TIMSS created an index of availability of school resources for mathematics instruction. As described in Exhibit 8.3, the index is based on schools' average response to five questions about shortages that affect general capacity to provide instruction and five questions about shortages that affect mathematics instruction in particular. Students were placed in the high category if principals reported that shortages, both general and for mathematics in particular, had no or little effect on instructional capacity. The medium level indicates that one type of shortage affects instruction some or a lot, and the low level that both shortages affect it some or a lot.

Since TIMSS results in 1995 and 1999 showed that students in schools that reported being generally unaffected by a lack of resources had higher average mathematics achievement than those in schools where across-the-board shortages affected instructional capacity some or a lot, TIMSS 2003 reported information on trends in school resources. Exhibit 8.3 shows changes in the percentages of eighth-grade students in the high, medium, and low categories for 1995, 1999, and 2003, and for the fourth-grade students for 1995 to 2003. At the eighth grade, the trend suggests similarity between 1995 and 2003 with a dip in available resources in 1999. Consistent with this overall pattern across countries, the results at the eighth grade show 14 countries having significantly more students in the high category in 2003 than in 1999. At the fourth grade, the results for the participating countries were even more positive. Nine of the countries showed significant increases in the high category and none showed a decrease.

Exhibit 8.3

Exhibit 8.3: Trends in Index of Availability of School Resources for Mathematics Instruction (ASRMI)

Index of Availability of School Resources for Mathematics Instruction

Index based on principals' average response to five questions about shortages that affect general capacity to provide instruction: instructional materials (e.g., textbook); budget for supplies (e.g., paper, pencils); school buildings and grounds;
heating/cooling and lighting systems; and instructional space (e.g., classrooms); and the average response to five questions about shortages that affect mathematics instruction: computers for mathematics instruction; computer software for mathematics instruction; calculators for mathematics instruction; library materials relevant to mathematics instruction; and audio-visual resources for mathematics instruction. Average is computed based on a 4point scale: $1=$ none; $2=a$ little; 3=some; 4=a lot. High level indicates that both shortages are on average lower than 2. Low level indicates that both shortages are on average greater than or equal to 3. Medium level includes all other possible combinations of responses.

| Countries |  | High ASRMI |  |  |  |  | Medium ASRMI |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 2003 Percent of Students | 1999 Percent of Students |  |  |  |  | 1999 Percent of Students |  | 1995 <br> Percent of Students |  |
| Singapore |  | 88 (0.0) | 50 (4.0) | 0 | 55 (4.6) | 0 | 10 (0.0) | 46 (4.1) | © | 43 (4.4) | - |
| Hong Kong, SAR |  | 63 (4.0) | 22 (4.1) | 0 | 23 (5.4) | 0 | 35 (4.0) | 67 (4.4) | (1) | 72 (5.6) | - |
| Belgium (Flemish) |  | 60 (4.9) | 54 (4.6) |  | 48 (5.3) |  | 38 (4.7) | 46 (4.6) |  | 52 (5.3) |  |
| Japan |  | 57 (3.8) | 36 (4.3) | 0 | 28 (3.5) | 0 | 42 (3.8) | 61 (4.2) | © | 68 (3.9) | - |
| Australia | r | 56 (3.8) | - - |  | 42 (5.0) | 0 | 43 (3.9) | -- |  | 52 (5.2) |  |
| Netherlands | $r$ | 56 (4.9) | 40 (6.2) | 0 | 46 (7.1) |  | 44 (4.9) | 60 (6.2) | © | 53 (7.0) |  |
| Slovenia | r | 55 (3.7) | -- |  | 13 (3.2) | 0 | 42 (3.7) | -- |  | 80 (4.0) | - |
| United States | r | 53 (3.8) | 37 (3.8) | 0 | 18 (3.2) | $\bigcirc$ | 46 (3.8) | 59 (3.6) | (1) | 75 (3.6) | - |
| Israel |  | 49 (4.4) | 32 (4.1) | 0 | - - |  | 48 (4.5) | 62 (4.3) | - | - |  |
| New Zealand |  | 44 (4.8) | 34 (4.3) |  | 15 (2.9) | 0 | 55 (4.9) | 62 (4.3) |  | 79 (3.6) | © |
| Italy |  | 39 (3.7) | 28 (3.4) | 0 | -- |  | 59 (3.8) | 66 (4.0) |  | -- |  |
| Sweden |  | 37 (4.2) | $\checkmark>$ |  | 39 (4.8) |  | 62 (4.2) | $\checkmark>$ |  | 56 (4.6) |  |
| Scotland |  | 37 (5.6) | -> |  | -- |  | 62 (5.7) | $\checkmark>$ |  | -- |  |
| Egypt |  | 34 (4.1) | ২৪ |  | -> |  | 48 (4.3) | $\rangle>$ |  | $\rangle>$ |  |
| Hungary |  | 32 (3.9) | 35 (4.0) |  | 19 (3.2) | 0 | 67 (3.8) | 59 (4.1) |  | 79 (3.3) | - |
| Estonia |  | 29 (4.1) | $\checkmark>$ |  | $\checkmark>$ |  | 66 (4.4) | $\checkmark>$ |  | $\checkmark>$ |  |
| Korea, Rep. of |  | 28 (4.0) | 4 (1.6) | 0 | 4 (1.6) | 0 | 69 (3.9) | 81 (3.5) | © | 82 (3.2) | - |
| Lebanon |  | 24 (3.3) | $\checkmark>$ |  | $\rangle>$ |  | 70 (3.7) | $\checkmark>$ |  | $\checkmark>$ |  |
| Chinese Taipei |  | 24 (3.4) | 6 (1.9) | 0 | $\checkmark>$ |  | 71 (3.8) | 78 (3.2) |  | $\checkmark>$ |  |
| Norway | r | 21 (3.9) | $\checkmark>$ |  | 38 (4.0) | © | 74 (4.2) | $\checkmark>$ |  | 61 (4.0) | 0 |
| Chile |  | 21 (3.0) | 22 (3.1) |  | $\checkmark>$ |  | 65 (3.7) | 68 (3.3) |  | $\checkmark>$ |  |
| Malaysia |  | 18 (3.3) | 20 (3.6) |  | ৪> |  | 70 (3.8) | 73 (3.8) |  | $\checkmark>$ |  |
| Saudi Arabia |  | 17 (5.6) | $\checkmark>$ |  | ৪> |  | 70 (6.1) | $\checkmark>$ |  | $\checkmark>$ |  |
| Jordan |  | 16 (3.4) | 5 (1.9) | 0 | ৪> |  | 74 (3.7) | 64 (4.4) |  | $\rangle>$ |  |
| Bahrain |  | 15 (0.1) | $\checkmark>$ |  | $\checkmark>$ |  | 74 (0.2) | $\checkmark\rangle$ |  | $\checkmark\rangle$ |  |
| Latvia |  | 15 (2.9) | -- |  | -- |  | 80 (3.5) | -- |  | -- |  |
| Tunisia |  | 14 (3.0) | $4(1.8)$ | 0 | -> |  | 74 (3.6) | 78 (3.9) |  | $\checkmark>$ |  |
| Philippines |  | 13 (2.6) | 12 (2.7) |  | ৪> |  | 51 (4.6) | 59 (4.1) |  | $\rangle>$ |  |
| Ghana |  | 12 (2.9) | -> |  | ৪ |  | 75 (4.2) | $\checkmark>$ |  | $\checkmark\rangle$ |  |
| Palestinian Nat'I Auth. |  | 12 (2.8) | $\checkmark>$ |  | $\checkmark>$ |  | 74 (3.7) | $\checkmark>$ |  | $\checkmark>$ |  |
| Cyprus | r | 12 (0.1) | 15 (0.2) | © | 31 (0.5) | - | 79 (0.2) | 85 (0.2) | © | 63 (0.5) | 0 |
| Slovak Republic |  | 12 (2.6) | 8 (2.4) |  | 13 (2.7) |  | 74 (4.0) | 85 (2.9) | © | 84 (2.7) | - |
| Morocco |  | 9 (3.3) | -- |  | $\checkmark>$ |  | 65 (6.5) | -- |  | $\checkmark\rangle$ |  |
| Lithuania |  | $9(2.6)$ | 8 (2.2) |  | 2 (1.1) | 0 | 81 (3.7) | 67 (3.6) | 0 | 79 (3.5) |  |
| Iran, Islamic Rep. of |  | 8 (2.3) | 6 (1.8) |  | 1 (0.9) | 0 | 71 (3.5) | 71 (4.1) |  | 67 (4.7) |  |
| Macedonia, Rep. of |  | 8 (2.4) | $2(1.2)$ | 0 | $\checkmark>$ |  | 69 (3.9) | 59 (3.7) |  | $\checkmark>$ |  |
| South Africa |  | 8 (1.6) | 8 (2.0) |  | -- |  | 53 (3.5) | 46 (4.2) |  | -- |  |
| Romania |  | 8 (2.4) | 6 (2.4) |  | 4 (1.4) |  | 82 (3.2) | 67 (3.7) | 0 | 73 (3.8) |  |
| Indonesia |  | 8 (2.0) | 23 (3.9) | © | $\checkmark>$ |  | 88 (2.6) | 66 (4.8) | 0 | $\checkmark>$ |  |
| Armenia | $r$ | 8 (2.8) | $\checkmark>$ |  | $\checkmark>$ |  | 69 (4.6) | $\checkmark>$ |  | $\checkmark>$ |  |
| Moldova, Rep. of | r | 7 (2.5) | 0 (0.4) | 0 | $\checkmark>$ |  | 71 (5.0) | 33 (4.3) | 0 | $\checkmark\rangle$ |  |
| Bulgaria |  | 5 (1.8) | 1 (1.0) |  | -- |  | 86 (2.7) | 62 (4.7) | 0 | -- |  |
| Russian Federation |  | 5 (1.4) | 1 (0.9) | 0 | 1 (0.0) | 0 | 70 (3.9) | 47 (4.0) | 0 | 46 (4.5) | 0 |
| Serbia |  | 5 (2.0) | $\checkmark>$ |  | ৪> |  | 74 (3.9) | $\checkmark>$ |  | $\checkmark>$ |  |
| Botswana |  | 4 (1.7) | -> |  | ৪> |  | 77 (3.6) | $\checkmark \stackrel{ }{ }$ |  | $\checkmark \stackrel{ }{ }$ |  |
| F England | $s$ | 35 (6.6) | 26 (4.2) |  | 25 (4.7) |  | 56 (6.2) | 72 (4.4) | © | 73 (4.9) | $\stackrel{\square}{0}$ |
| International Avg. |  | 26 (0.5) | 19 (0.6) | - | 23 (0.8) | $\bigcirc$ | 64 (0.6) | 64 (0.8) |  | 67 (1.0) |  |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Basque Country, Spain |  | 60 (5.0) | $\checkmark>$ |  | ৪> |  | 40 (5.1) | $\checkmark>$ |  | $\checkmark>$ |  |
| Indiana State, US |  | 50 (6.9) | 36 (7.8) |  | $\checkmark>$ |  | 47 (7.0) | 62 (7.7) |  | $\rangle>$ |  |
| Ontario Province, Can. |  | 28 (4.5) | 21 (3.8) |  | 17 (3.9) |  | 65 (4.9) | 71 (4.5) |  | 77 (3.9) |  |
| Quebec Province, Can. | $r$ | 56 (4.6) | 56 (5.8) |  | 41 (7.6) |  | 43 (4.8) | 44 (5.8) |  | 59 (7.6) |  |

Background data provided by schools.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia, Latvia, Morocco, and Slovenia, and 1995 data are not shown for Israel, Italy, Latvia, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.
A diamond (') indicates the country did not participate in the assessment.

Exhibit 8.3: Trends in Index of Availability of School Resources for Mathematics Instruction


[^78]() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates comparable data are not available
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " s " indicates data are available for at least 50 but less than $70 \%$ of the students.

A diamond (') indicates the country did not participate in the assessment.

## Exhibit 8.3: Trends in Index of Availability of School Resources for Mathematics Instruction

 (ASRMI)

| Countries | High ASRMI |  |  |  | Medium ASRMI |  | Low ASRMI |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 2003 <br> Percent of Students | Percent <br> Student |  | 2003 <br> Percent of Students | 1995 <br> Percent of Students | 2003 <br> Percent of Students | 1995 <br> Percent of Students |  |  |  |
| Singapore |  | 86 (2.7) | 47 (4.0) | 0 | 14 (2.6) | 53 (4.0) © | 1 (0.5) | 0 (0.0) |  | 0 | 2003 significantly |
| Scotland |  | 62 (4.3) | - - |  | 37 (4.2) | - - | 1 (0.0) | - - |  |  |  |
| Slovenia | $r$ | 58 (3.9) | 11 (2.9) | 0 | 40 (4.0) | 81 (3.9) | 2 (1.3) | 8 (2.8) |  |  |  |
| Japan |  | 57 (3.8) | 25 (3.7) | 0 | 41 (3.8) | 70 (3.7) - | 1 (1.0) | 5 (1.8) |  |  |  |
| Belgium (Flemish) |  | 53 (3.9) | $\checkmark\rangle$ |  | 44 (4.1) | $\checkmark>$ | 3 (1.4) | $\checkmark>$ |  |  | lower |
| Hong Kong, SAR |  | 51 (4.9) | 33 (5.4) | 0 | 49 (4.9) | 65 (5.5) | 0 (0.0) | 2 (1.4) |  |  |  |
| New Zealand |  | 49 (3.6) | 28 (3.9) | 0 | 49 (3.7) | 65 (4.2) (1) | 1 (0.9) | 8 (2.5) | (\%) |  |  |
| Australia |  | 46 (4.1) | 27 (4.7) | 0 | 53 (4.1) | 71 (5.0) | 1 (0.8) | 2 (1.4) |  |  |  |
| England | $r$ | 44 (4.9) | 27 (4.5) | 0 | 56 (4.9) | 66 (4.6) | 0 (0.0) | 7 (2.8) |  |  |  |
| United States | $r$ | 43 (3.3) | 32 (3.9) | 0 | 54 (3.4) | 65 (3.7) ${ }^{(7)}$ | 3 (1.2) | 3 (1.4) |  |  |  |
| Netherlands |  | 39 (5.0) | 35 (5.2) |  | 58 (4.8) | 61 (5.1) | 3 (1.5) | 4 (1.7) |  |  |  |
| Hungary |  | 38 (4.5) | 20 (3.5) | 0 | 61 (4.6) | 78 (3.6) $\left.{ }^{( }\right)$ | 1 (1.0) | 2 (1.2) |  |  |  |
| Norway | r | 32 (4.6) | 29 (4.8) |  | 62 (4.7) | 69 (4.8) | 7 (2.3) | 3 (1.6) |  |  |  |
| Italy |  | 28 (3.6) | - - |  | 70 (3.7) | - - | 2 (1.2) | - - |  |  |  |
| Latvia |  | 25 (4.0) | - - |  | 68 (4.6) | -- | 7 (2.5) | - - |  |  |  |
| Cyprus | $r$ | 19 (3.4) | 24 (3.5) |  | 68 (4.6) | 72 (3.8) | 12 (3.3) | 4 (1.8) 0 |  |  |  |
| Chinese Taipei |  | 18 (3.1) | >> |  | 78 (3.3) | ৪ $\downarrow$ | 4 (1.3) | ৪ > |  |  |  |
| Tunisia |  | 14 (2.8) | $\checkmark>$ |  | 64 (4.1) | $\checkmark>$ | 22 (3.8) | $\checkmark>$ |  |  |  |
| Iran, Islamic Rep. of |  | 13 (3.6) | 7 (2.5) |  | 63 (5.1) | 67 (4.2) | 24 (4.4) | 26 (4.1) |  |  |  |
| Philippines |  | 12 (3.1) | $\checkmark$ - |  | 62 (5.1) | $\checkmark>$ | 26 (4.6) | $\checkmark$ - |  |  |  |
| Lithuania |  | 11 (2.6) | ৪ ৪ |  | 81 (3.4) | $\checkmark$ - | 8 (2.2) | $\checkmark$ - |  |  |  |
| Russian Federation |  | 10 (1.9) | $\checkmark>$ |  | 72 (3.3) | $\checkmark>$ | 19 (3.2) | $\checkmark>$ |  |  |  |
| Armenia |  | 7 (2.7) | ৪ |  | 71 (4.5) | ৪ | 23 (4.0) | ৪ |  |  |  |
| Moldova, Rep. of |  | 3 (1.6) | $\rangle>$ |  | 76 (4.9) | $\rangle>$ | 20 (4.7) | $\rangle\langle$ |  |  |  |
| International Avg. |  | 33 (0.7) | 26 (1.1) | © | 58 (0.9) | 68 (1.2) © | 10 (0.5) | 6 (0.6) |  |  |  |
| Benchmarking Participants |  |  |  |  |  |  |  |  |  |  |  |
| Indiana State, US |  | 50 (6.1) | > $\langle$ |  | 49 (6.3) | >> | 1 (1.4) | > $\langle$ |  |  |  |
| Ontario Province, Can. |  | 35 (4.9) | 22 (4.0) | 0 | 59 (5.0) | 74 (4.4) | 6 (2.4) | 4 (2.0) |  |  |  |
| Quebec Province, Can. |  | 45 (4.6) | 54 (8.5) |  | 52 (4.3) | 46 (8.5) | 3 (1.3) | 0 (0.0) 0 | 0 |  |  |

Background data provided by schools.
Trend notes: Because of differences between 1995 and 2003 in population coverage, 1995 data are not shown for Italy and Latvia. 1995 data for New Zealand in this exhibit include students in English medium instruction only (>98\% of the estimated population).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^79]
## What Are the Perceptions of School Climate?

The school environment establishes the climate for learning. To measure the extent to which schools offer a positive school climate, TIMSS created two new indices in 2003 - one measuring the views of principals and the other the views of teachers. The results for the Index of Principals' Perception of School Climate are presented in Exhibit 8.4. On a scale from very high to very low, the index was based on principals' characterizations of the following:

- teachers' job satisfaction;
- teachers' understanding of the school's curricular goals;
- teachers' degree of success in implementing the schools' curricula;
- teachers' expectations for students' achievement;
- parental support for student's achievement;
- parental involvement in schools' activities;
- students' regard for school property;
- students' desire to do well in school.

Students in the high category attended schools where the principals averaged high or very high reports for each aspect of school climate. Students whose principals characterized school climate as medium were placed in the medium category, and whose principals characterized the school climate as low or very low were placed in the low category.

At both grades, internationally, on average, two-thirds of the students were in the medium category. At the eighth grade, 15 percent were in the high category, and 18 percent were in the low category. Morocco, Tunisia, and Botswana had from 59 to 69 percent of their students in the low category. At the fourth grade, 23 percent were in the high category and 11 percent in the low category. In both grades, based on a 5 -point scale: 1 = very high; $2=$ high; 3 = medium; $4=$ low; 5 = very low. High level indicates average is less than or equal to 2. Medium level indicates that average is greater than 2 and less or equal to 3 . Low level indicates average is greater than 3.

| Countries |  |  | High PPSC |  | Medium PPSC |  | $\begin{aligned} & \text { Low } \\ & \text { PPSC } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | United States |  | 43 (3.2) | 534 (4.9) | 49 (3.3) | 491 (5.1) | 8 (1.9) | 470 (7.0) |
|  | Scotland | s | 42 (4.3) | 527 (7.7) | 52 (4.7) | 490 (7.2) | 6 (2.6) | 459 (34.5) |
|  | Chinese Taipei |  | 37 (3.8) | 601 (7.3) | 60 (4.0) | 578 (5.4) | 3 (1.0) | 534 (33.8) |
|  | Philippines |  | 35 (4.1) | 393 (8.0) | 59 (4.1) | 371 (7.5) | 6 (2.2) | 361 (14.5) |
|  | New Zealand |  | 34 (4.7) | 525 (8.5) | 58 (4.7) | 481 (8.0) | 8 (3.2) | 479 (12.1) |
|  | Australia |  | 31 (4.3) | 520 (9.4) | 61 (4.8) | 506 (6.3) | 8 (2.7) | 444 (20.6) |
|  | Singapore |  | 30 (0.0) | 649 (5.1) | 65 (0.0) | 589 (5.5) | 5 (0.0) | 556 (17.7) |
|  | Japan |  | 29 (3.4) | 585 (5.1) | 69 (3.4) | 564 (2.2) | 3 (1.3) | 556 (5.6) |
|  | Israel |  | 28 (4.0) | 521 (6.9) | 69 (4.1) | 489 (4.4) | 2 (1.0) | ~ ~ |
|  | Egypt |  | 26 (3.3) | 418 (6.8) | 62 (4.2) | 402 (4.6) | 12 (3.0) | 402 (12.4) |
|  | Sweden |  | 21 (3.2) | 513 (5.0) | 72 (3.8) | 497 (3.8) | 7 (2.2) | 483 (14.7) |
|  | Cyprus |  | 20 (0.2) | 476 (2.9) | 76 (0.2) | 455 (1.9) | 4 (0.1) | 470 (5.5) |
|  | Indonesia |  | 19 (3.2) | 424 (13.7) | 71 (3.8) | 412 (5.8) | 11 (2.8) | 377 (19.5) |
|  | Jordan |  | 18 (3.2) | 455 (12.9) | 71 (4.2) | 420 (4.4) | 11 (2.7) | 404 (11.0) |
|  | Lebanon |  | 18 (3.5) | 457 (7.9) | 63 (4.6) | 439 (4.3) | 19 (2.9) | 398 (6.2) |
|  | Malaysia |  | 17 (3.3) | 540 (11.1) | 70 (4.1) | 504 (4.9) | 13 (3.1) | 490 (11.3) |
|  | Korea, Rep. of |  | 16 (3.3) | 609 (5.6) | 68 (3.8) | 588 (2.9) | 15 (3.0) | 576 (4.5) |
|  | Belgium (Flemish) |  | 16 (2.7) | 567 (8.2) | 74 (3.8) | 539 (4.2) | 10 (2.6) | 473 (19.1) |
|  | Chile |  | 14 (2.8) | 421 (11.8) | 67 (3.6) | 387 (4.3) | 19 (3.2) | 361 (7.2) |
|  | Palestinian Nat'l Auth. |  | 14 (3.1) | 413 (10.5) | 77 (3.5) | 389 (3.7) | 8 (2.5) | 361 (13.8) |
|  | Saudi Arabia |  | 14 (4.5) | 313 (22.7) | 68 (5.1) | 334 (4.4) | 18 (3.8) | 336 (9.1) |
|  | Macedonia, Rep. of |  | 14 (3.0) | 468 (13.2) | 74 (3.7) | 434 (4.1) | 12 (2.8) | 419 (15.9) |
|  | Ghana |  | 13 (3.4) | 310 (21.3) | 68 (4.4) | 270 (5.3) | 18 (3.3) | 261 (9.4) |
|  | Norway |  | 13 (2.6) | 473 (5.3) | 82 (3.4) | 461 (2.7) | 5 (2.2) | 459 (21.4) |
|  | Italy |  | 12 (2.7) | 505 (7.7) | 75 (3.6) | 483 (3.8) | 13 (2.3) | 464 (9.3) |
|  | Hong Kong, SAR |  | 12 (2.7) | 619 (13.6) | 70 (4.1) | 585 (3.8) | 18 (3.4) | 557 (11.5) |
|  | Bahrain |  | 11 (0.1) | 413 (2.4) | 74 (0.2) | 400 (2.1) | 15 (0.2) | 394 (5.1) |
|  | Iran, Islamic Rep. of |  | 10 (2.2) | 458 (9.2) | 69 (3.7) | 411 (3.2) | 21 (3.0) | 389 (4.5) |
|  | Slovenia |  | 9 (2.2) | 497 (5.6) | 83 (2.8) | 493 (2.7) | 8 (2.4) | 487 (11.7) |
|  | Lithuania |  | 8 (2.4) | 514 (13.6) | 88 (3.0) | 500 (2.7) | 4 (1.9) | 497 (9.1) |
|  | Romania |  | 7 (2.2) | 538 (11.8) | 69 (4.1) | 482 (5.4) | 24 (3.7) | 440 (8.1) |
|  | South Africa |  | 7 (2.1) | 347 (43.0) | 45 (4.1) | 273 (11.0) | 48 (3.9) | 244 (5.4) |
|  | Hungary |  | 7 (2.1) | 569 (11.3) | 84 (3.3) | 527 (3.9) | 10 (2.6) | 526 (13.2) |
|  | Netherlands |  | 5 (2.1) | 586 (9.7) | 81 (3.7) | 538 (4.5) | 13 (3.2) | 508 (16.4) |
|  | Bulgaria |  | 4 (1.4) | 527 (19.0) | 72 (3.4) | 482 (5.6) | 23 (3.1) | 448 (9.9) |
|  | Morocco | s | 3 (1.7) | 374 (17.1) | 37 (5.6) | 389 (5.2) | 59 (5.7) | 385 (3.4) |
|  | Slovak Republic |  | 3 (1.6) | 586 (13.8) | 78 (3.9) | 510 (3.1) | 19 (3.9) | 488 (8.9) |
|  | Serbia |  | 3 (1.4) | 519 (31.2) | 71 (4.1) | 475 (3.0) | 26 (3.8) | 476 (5.2) |
|  | Armenia | $r$ | 3 (1.5) | 506 (32.5) | 79 (4.1) | 480 (3.4) | 18 (4.0) | 460 (5.7) |
|  | Estonia |  | 1 (1.1) | ~~ | 79 (3.1) | 532 (3.8) | 20 (2.9) | 523 (4.0) |
|  | Tunisia |  | 1 (1.0) | $\sim \sim$ | 30 (3.7) | 421 (4.1) | 69 (3.7) | 405 (2.7) |
|  | Botswana |  | 1 (1.0) | ~ ~ | 31 (4.2) | 367 (5.1) | 68 (4.3) | 361 (2.9) |
|  | Moldova, Rep. of | $r$ | 1 (0.0) | ~ ~ | 50 (5.1) | 467 (5.7) | 49 (5.1) | 451 (7.9) |
|  | Russian Federation |  | 1 (0.5) | ~ ~ | 70 (2.9) | 511 (4.4) | 29 (2.9) | 499 (6.3) |
|  | Latvia |  | 0 (0.0) | ~ ~ | 84 (3.8) | 510 (3.7) | 16 (3.8) | 501 (8.4) |
| 寺 | England | s | 33 (5.8) | 526 (11.2) | 63 (6.2) | 493 (9.0) | 5 (3.1) | 456 (16.1) |
|  | International Avg. |  | 15 (0.4) | 495 (2.3) | 67 (0.6) | 466 (0.8) | 18 (0.4) | 446 (2.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
|  | Basque Country, Spain |  | 12 (3.3) | 502 (8.2) | 79 (3.8) | 488 (3.1) | 9 (2.4) | 464 (8.4) |
|  | Indiana State, US |  | 29 (6.4) | 537 (10.3) | 67 (6.7) | 502 (5.3) | 5 (2.2) | 444 (13.6) |
|  | Ontario Province, Can. |  | 42 (4.3) | 534 (3.8) | 52 (4.7) | 512 (4.2) | 5 (2.1) | 516 (10.2) |
|  | Quebec Province, Can. |  | 14 (2.2) | 582 (9.5) | 78 (3.1) | 540 (3.7) | 8 (2.2) | 526 (7.1) |

Background data provided by schools.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A tilde (~) indicates insufficient data to report achievement.

## Exhibit 8.4: Index of Principals' Perception of School Climate (PPSC)



| Countries |  | High <br> PPSC |  | Medium PPSC |  | Low <br> PPSC |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Chinese Taipei |  | 57 (3.8) | 570 (2.2) | 41 (3.8) | 558 (3.5) | 2 (0.9) | ~ |
| Scotland |  | 51 (5.0) | 498 (4.9) | 45 (4.9) | 488 (4.9) | 4 (1.8) | 451 (10.2) |
| New Zealand |  | 48 (3.3) | 520 (3.1) | 48 (3.3) | 475 (4.4) | 4 (1.5) | 445 (11.5) |
| United States |  | 48 (3.5) | 543 (3.2) | 45 (3.5) | 503 (3.7) | 7 (1.6) | 473 (8.5) |
| Australia |  | 38 (4.6) | 517 (5.6) | 55 (5.1) | 492 (4.7) | 7 (3.6) | 457 (20.3) |
| England | $r$ | 34 (4.7) | 550 (7.6) | 64 (4.9) | 521 (6.0) | 2 (1.3) | ~ ~ |
| Singapore |  | 32 (4.1) | 611 (7.5) | 63 (4.1) | 587 (7.3) | 5 (1.6) | 557 (17.3) |
| Hong Kong, SAR |  | 30 (4.6) | 586 (5.7) | 65 (4.8) | 573 (3.4) | 5 (2.1) | 556 (6.4) |
| Cyprus |  | 28 (4.0) | 513 (5.9) | 66 (4.3) | 510 (2.9) | 6 (2.3) | 504 (8.8) |
| Philippines |  | 27 (3.9) | 378 (13.7) | 66 (4.2) | 341 (7.0) | 7 (2.2) | 344 (21.5) |
| Norway |  | 26 (3.9) | 456 (5.4) | 72 (4.0) | 449 (2.6) | 2 (1.0) | ~ ~ |
| Lithuania |  | 25 (3.5) | 542 (7.1) | 72 (3.7) | 532 (3.4) | 3 (1.4) | 505 (17.3) |
| Iran, Islamic Rep. of |  | 25 (4.0) | 407 (9.1) | 67 (4.3) | 386 (5.3) | 8 (2.6) | 351 (11.2) |
| Belgium (Flemish) |  | 21 (3.3) | 558 (3.2) | 77 (3.2) | 551 (2.0) | 3 (1.4) | 508 (25.2) |
| Netherlands |  | 20 (3.8) | 544 (4.5) | 79 (4.0) | 541 (2.7) | 2 (1.2) | ~ ~ |
| Japan |  | 18 (3.1) | 576 (5.2) | 77 (3.3) | 563 (1.7) | 5 (1.8) | 547 (7.2) |
| Italy |  | 15 (2.8) | 516 (10.0) | 76 (3.4) | 502 (4.5) | 10 (2.4) | 491 (10.8) |
| Tunisia |  | 9 (2.4) | 380 (17.2) | 49 (3.9) | 350 (6.9) | 42 (3.9) | 316 (6.6) |
| Slovenia |  | 8 (2.1) | 487 (8.4) | 85 (2.7) | 478 (2.9) | 7 (2.0) | 470 (11.3) |
| Hungary |  | 8 (2.2) | 561 (8.1) | 85 (3.0) | 524 (3.5) | 7 (2.3) | 535 (23.0) |
| Latvia |  | 6 (2.2) | 547 (10.9) | 83 (3.6) | 537 (3.4) | 11 (2.9) | 520 (8.7) |
| Russian Federation |  | 4 (1.3) | 559 (22.9) | 84 (2.6) | 531 (5.4) | 12 (2.4) | 528 (10.5) |
| Morocco | $r$ | 3 (1.4) | 431 (11.1) | 41 (4.7) | 344 (7.1) | 57 (4.7) | 349 (8.3) |
| Armenia | $r$ | 2 (1.3) | ~~ | 80 (3.7) | 460 (4.3) | 18 (3.5) | 433 (8.6) |
| Moldova, Rep. of | $r$ | 0 (0.0) | ~ ~ | 55 (5.0) | 515 (6.5) | 45 (5.0) | 486 (10.5) |
| International Avg. |  | 23 (0.7) | 515 (1.9) | 66 (0.8) | 492 (0.9) | 11 (0.5) | 468 (3.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 55 (7.2) | 546 (4.4) | 42 (7.1) | 520 (5.0) | 3 (0.3) | 464 (6.8) |
| Ontario Province, Can. |  | 43 (4.5) | 530 (6.6) | 52 (4.6) | 500 (4.0) | 5 (2.4) | 490 (7.2) |
| Quebec Province, Can. |  | 25 (3.6) | 518 (2.8) | 70 (3.9) | 503 (2.9) | 5 (2.1) | 485 (8.9) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.

| Countries |  |  | High <br> TPSC |  | Medium TPSC |  | $\begin{aligned} & \text { Low } \\ & \text { TPSC } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | Israel |  | 27 (4.1) | 517 (7.7) | 60 (4.3) | 492 (4.4) | 13 (2.1) | 464 (12.5) |
|  | Philippines |  | 25 (4.0) | 395 (13.5) | 57 (4.4) | 381 (6.8) | 18 (3.2) | 344 (9.9) |
|  | United States |  | 21 (2.8) | 542 (6.6) | 56 (3.2) | 507 (3.8) | 22 (2.6) | 476 (7.3) |
|  | Chinese Taipei |  | 21 (3.3) | 617 (9.4) | 69 (3.9) | 579 (5.5) | 10 (2.6) | 563 (10.9) |
|  | Lebanon |  | 21 (4.0) | 449 (8.8) | 56 (4.8) | 432 (4.8) | 23 (3.3) | 419 (8.1) |
|  | Egypt |  | 19 (3.3) | 431 (7.8) | 58 (4.2) | 403 (4.5) | 22 (3.4) | 390 (8.2) |
|  | Indonesia |  | 18 (3.5) | 437 (13.4) | 63 (4.4) | 415 (6.1) | 19 (3.7) | 378 (14.8) |
|  | Ghana |  | 17 (3.9) | 308 (13.2) | 54 (4.6) | 272 (5.6) | 30 (4.5) | 255 (8.7) |
|  | New Zealand |  | 17 (3.1) | 512 (8.6) | 62 (4.3) | 499 (6.8) | 21 (3.7) | 472 (9.7) |
|  | Australia |  | 16 (2.6) | 530 (9.1) | 58 (4.4) | 514 (7.6) | 27 (4.0) | 462 (7.9) |
|  | Scotland |  | 15 (3.4) | 534 (15.2) | 60 (4.6) | 502 (5.6) | 25 (3.8) | 481 (8.5) |
|  | Malaysia |  | 15 (2.9) | 510 (13.5) | 67 (3.5) | 514 (5.1) | 18 (3.1) | 486 (8.1) |
|  | Cyprus |  | 15 (1.9) | 463 (5.0) | 68 (2.3) | 460 (2.1) | 17 (1.9) | 457 (4.7) |
|  | Singapore |  | 14 (1.2) | 646 (9.4) | 61 (2.1) | 610 (3.9) | 25 (2.0) | 574 (7.1) |
|  | Macedonia, Rep. of |  | 14 (3.0) | 453 (12.8) | 65 (4.0) | 438 (4.7) | 21 (3.4) | 413 (11.1) |
|  | Iran, Islamic Rep. of |  | 13 (2.6) | 441 (9.8) | 35 (3.7) | 423 (4.7) | 53 (3.9) | 397 (3.5) |
|  | Chile |  | 11 (2.4) | 434 (12.9) | 54 (3.4) | 394 (5.0) | 35 (3.7) | 365 (5.7) |
|  | South Africa |  | 10 (2.1) | 259 (22.4) | 46 (4.0) | 276 (10.2) | 44 (4.3) | 251 (5.6) |
|  | Romania |  | 10 (2.7) | 514 (26.1) | 58 (4.1) | 479 (5.3) | 32 (3.9) | 456 (7.3) |
|  | Sweden |  | 9 (2.5) | 540 (7.5) | 67 (3.6) | 499 (3.4) | 24 (3.2) | 482 (5.5) |
|  | Armenia |  | 9 (2.2) | 488 (10.7) | 60 (4.0) | 482 (4.5) | 31 (3.7) | 464 (4.3) |
|  | Norway |  | 8 (2.1) | 472 (8.4) | 82 (3.0) | 461 (2.9) | 10 (2.4) | 456 (5.3) |
|  | Palestinian Nat'l Auth. |  | 8 (2.4) | 405 (14.1) | 66 (3.8) | 390 (3.9) | 26 (3.2) | 388 (6.3) |
|  | Bahrain |  | 7 (1.8) | 405 (7.5) | 49 (3.5) | 406 (2.4) | 43 (3.4) | 396 (3.6) |
|  | Serbia |  | 7 (2.0) | 481 (12.0) | 69 (3.9) | 476 (3.4) | 24 (3.7) | 475 (6.9) |
|  | Hong Kong, SAR |  | 7 (2.5) | 625 (10.8) | 58 (3.6) | 596 (4.9) | 35 (3.5) | 557 (6.8) |
|  | Jordan |  | 7 (2.7) | 490 (22.8) | 55 (4.2) | 425 (4.3) | 38 (4.1) | 412 (6.4) |
|  | Korea, Rep. of | s | 7 (1.9) | 604 (15.5) | 61 (3.7) | 593 (3.0) | 33 (3.5) | 581 (3.9) |
|  | Saudi Arabia |  | 6 (2.4) | 355 (23.6) | 59 (5.9) | 332 (5.1) | 34 (5.8) | 335 (6.0) |
|  | Tunisia |  | 6 (1.8) | 427 (14.3) | 50 (4.2) | 414 (3.5) | 44 (4.2) | 404 (2.9) |
|  | Lithuania |  | 5 (1.7) | 525 (7.2) | 86 (2.9) | 500 (2.9) | 9 (2.3) | 497 (9.5) |
|  | Japan |  | 5 (1.8) | 636 (22.2) | 70 (3.7) | 565 (2.4) | 25 (3.6) | 564 (4.8) |
|  | Morocco | s | 4 (3.0) | 398 (6.5) | 25 (5.0) | 386 (9.2) | 71 (5.7) | 389 (3.7) |
|  | Belgium (Flemish) |  | 4 (1.3) | 578 (7.9) | 78 (2.8) | 552 (4.0) | 18 (2.5) | 466 (10.0) |
|  | Slovenia |  | 4 (1.7) | 517 (10.2) | 79 (3.7) | 493 (2.6) | 17 (3.3) | 491 (6.5) |
|  | Italy |  | 4 (1.8) | 485 (29.2) | 49 (4.2) | 494 (4.7) | 48 (3.9) | 473 (4.5) |
|  | Netherlands |  | 3 (2.7) | 521 (59.9) | 49 (4.6) | 567 (6.9) | 48 (4.7) | 508 (7.0) |
|  | Botswana |  | 3 (1.7) | 405 (40.7) | 29 (4.4) | 373 (6.1) | 68 (4.5) | 361 (3.0) |
|  | Hungary |  | 3 (1.4) | 563 (23.7) | 83 (2.9) | 532 (3.5) | 14 (2.5) | 502 (9.2) |
|  | Slovak Republic |  | 2 (1.4) | ~~ | 57 (4.2) | 512 (4.4) | 41 (4.4) | 497 (5.2) |
|  | Estonia |  | 2 (1.1) | ~ ~ | 64 (4.2) | 536 (4.0) | 34 (4.2) | 521 (5.1) |
|  | Latvia |  | 2 (1.3) | $\sim \sim$ | 70 (4.0) | 507 (3.9) | 28 (4.0) | 514 (7.2) |
|  | Bulgaria |  | 1 (0.9) | $\sim \sim$ | 58 (4.2) | 483 (6.4) | 41 (4.1) | 463 (5.9) |
|  | Russian Federation |  | 1 (0.7) | $\sim$ | 59 (4.2) | 518 (3.8) | 40 (4.1) | 495 (5.1) |
|  | Moldova, Rep. of | $r$ | 1 (0.5) | ~ ~ | 45 (4.5) | 466 (7.8) | 54 (4.6) | 451 (5.9) |
| ま | England | $r$ | 13 (3.3) | 525 (21.5) | 73 (5.0) | 511 (8.2) | 14 (4.3) | 467 (15.0) |
|  | International Avg. |  | 10 (0.4) | 486 (2.9) | 60 (0.6) | 471 (0.8) | 30 (0.5) | 450 (1.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
|  | Basque Country, Spain |  | 6 (2.7) | 493 (13.0) | 63 (4.9) | 491 (3.9) | 31 (4.9) | 479 (5.0) |
|  | Indiana State, US |  | 16 (4.3) | 526 (17.3) | 59 (4.8) | 515 (6.1) | 25 (4.2) | 485 (10.1) |
|  | Ontario Province, Can. |  | 24 (4.8) | 537 (5.5) | 61 (4.9) | 517 (3.8) | 15 (3.5) | 512 (7.2) |
|  | Quebec Province, Can. |  | 14 (2.7) | 570 (9.2) | 64 (4.4) | 541 (4.2) | 22 (4.0) | 536 (6.2) |

Background data provided by teachers.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde (~) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.

## Exhibit 8.5: Index of Mathematics Teachers' Perception of School Climate (TPSC)



| Countries |  | High TPSC |  | Medium TPSC |  | $\begin{aligned} & \text { Low } \\ & \text { TPSC } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| United States |  | 41 (2.6) | 538 (3.4) | 47 (2.6) | 512 (3.2) | 12 (1.6) | 477 (4.9) |
| Scotland | $r$ | 41 (5.1) | 507 (5.5) | 58 (5.0) | 485 (4.9) | 2 (1.1) | ~ ~ |
| New Zealand |  | 38 (2.8) | 510 (4.6) | 58 (3.1) | 490 (3.1) | 5 (1.1) | 432 (7.4) |
| Chinese Taipei |  | 35 (4.0) | 571 (3.1) | 61 (4.1) | 561 (2.4) | 4 (1.5) | 544 (11.3) |
| Philippines |  | 34 (4.5) | 380 (19.2) | 57 (4.7) | 351 (8.1) | 9 (2.8) | 331 (18.9) |
| Lithuania |  | 34 (3.4) | 544 (5.2) | 65 (3.4) | 527 (3.4) | 0 (0.0) | ~~ |
| Australia |  | 31 (3.6) | 508 (8.5) | 59 (3.7) | 504 (3.7) | 11 (2.5) | 452 (15.9) |
| England | $r$ | 29 (4.4) | 544 (6.5) | 63 (4.9) | 525 (5.5) | 8 (2.4) | 519 (17.7) |
| Cyprus |  | 27 (3.4) | 514 (4.6) | 64 (3.8) | 510 (3.2) | 9 (2.2) | 498 (7.7) |
| Iran, Islamic Rep. of |  | 25 (4.0) | 415 (8.4) | 60 (4.6) | 382 (5.9) | 15 (3.5) | 378 (8.3) |
| Singapore |  | 21 (3.9) | 629 (9.9) | 72 (3.9) | 588 (6.3) | 7 (2.0) | 570 (25.8) |
| Belgium (Flemish) |  | 18 (2.6) | 555 (3.8) | 76 (3.2) | 553 (1.6) | 6 (1.9) | 511 (15.2) |
| Norway |  | 18 (3.6) | 459 (6.9) | 76 (3.7) | 450 (2.7) | 6 (1.9) | 448 (8.8) |
| Slovenia |  | 16 (3.6) | 484 (7.1) | 80 (4.0) | 478 (3.5) | 4 (1.8) | 478 (6.3) |
| Hungary |  | 15 (2.8) | 535 (8.2) | 79 (3.2) | 529 (3.6) | 7 (2.1) | 488 (16.6) |
| Armenia | $r$ | 14 (2.9) | 466 (11.1) | 71 (3.5) | 455 (4.4) | 16 (2.8) | 436 (10.0) |
| Japan |  | 12 (2.7) | 581 (7.1) | 76 (3.4) | 563 (1.8) | 12 (2.6) | 554 (4.5) |
| Italy |  | 8 (2.2) | 506 (11.7) | 73 (3.3) | 508 (4.2) | 19 (2.7) | 480 (8.6) |
| Hong Kong, SAR |  | 8 (2.4) | 573 (11.7) | 78 (3.8) | 577 (3.1) | 14 (3.3) | 564 (7.1) |
| Netherlands |  | 8 (2.6) | 556 (5.8) | 84 (3.6) | 543 (2.6) | 8 (2.5) | 521 (10.6) |
| Tunisia | $r$ | 6 (2.2) | 390 (15.5) | 58 (3.8) | 345 (6.9) | 36 (3.7) | 321 (9.2) |
| Latvia |  | 6 (2.1) | 562 (6.7) | 84 (3.0) | 536 (3.2) | 10 (2.5) | 519 (9.9) |
| Russian Federation |  | 5 (1.8) | 573 (17.2) | 80 (3.4) | 533 (5.3) | 15 (3.1) | 510 (9.5) |
| Morocco | s | 4 (1.4) | 381 (34.2) | 34 (4.0) | 343 (14.0) | 62 (4.1) | 347 (6.1) |
| Moldova, Rep. of |  | 2 (0.7) | ~ ~ | 63 (4.1) | 505 (7.5) | 35 (4.1) | 501 (6.2) |
| International Avg. |  | 20 (0.6) | 512 (2.3) | 67 (0.8) | 494 (1.1) | 13 (0.5) | 473 (2.5) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 35 (5.3) | 549 (6.8) | 59 (4.8) | 524 (3.6) | 6 (2.4) | 523 (22.2) |
| Ontario Province, Can. |  | 37 (4.2) | 531 (7.4) | 55 (4.5) | 503 (2.7) | 9 (3.1) | 484 (13.7) |
| Quebec Province, Can. |  | 13 (2.5) | 522 (5.3) | 73 (3.6) | 505 (3.1) | 13 (3.0) | 497 (3.9) |

An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A tilde ( $\sim$ ) indicates insufficient data to report achievement.
there was a strong positive relationship between the principals' perception of school climate and average mathematics achievement.

The Index of Mathematics Teachers' Perception of School Climate is presented in Exhibit 8.5. It is based on the teachers' characterizations of the same aspects of school climate as were characterized by the principals (see list above). As can be seen from the results, fourth-grade teachers were in considerable agreement with principals, also placing two-thirds of the fourth-grade students in the medium category. According to their teachers, internationally, on average, 20 percent of the students attended schools in the high category and 13 percent attended schools in the low category. At the eighth grade, teachers had a somewhat more gloomy view of the climates in schools than did the principals. According to their teachers, on average, 10 percent of the eighth-grade students were attending schools in the high category. Sixty percent were attending schools in the medium category and 30 percent in the low category. Similar to the results for the principals, at both grades, there was a positive relationship between higher reports from teachers and higher average mathematics achievement.

## How Serious Are School Attendance Problems?

In some countries, schools are confronted with high rates of absenteeism, which can influence instructional continuity and reduce the time for learning. In general, research has shown that greater truancy is related to less serious attitudes towards school and lower academic achievement. To examine this issue, TIMSS developed an index of good school and class attendance based on schools' responses to three questions about the seriousness of students' absenteeism, arriving late at school, and skipping class. The high index level indicates schools reported that all three behaviors are not a problem. The low level indicates that two or more are a serious problem, or two are minor problems and the third a serious problem. The medium category includes all other possible combinations of responses.

The results of the index for TIMSS 2003 are presented in Exhibit 8.6, which also contains trends between 1999 and 2003 at the eighth grade. At the eighth grade, the results show very little change, on average, in attendance problems. Considering the two assessments, the high category did show a small (statistically significant) increase from 21 percent in 1999 to 23 percent in 2003. Nevertheless, the overwhelming majority of the students - 58 to 59 percent - were in the medium category in both years, and about one-fifth (19-20\%) were in the low category. Student attendance problems remain a serious problem in many countries, decreasing in five countries but increasing in four others during the same four-year period. At the fourth grade in 2003, 47 percent of students, on average, internationally, were in the high category, where principals had judged their schools to have few if any attendance problems. Another 47 percent of the students were in schools at the medium level of the index where principals reported moderate attendance problems. Only 5 percent were in schools at the low index level.


Background data provided by schools.
$\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia, Latvia, Morocco, and Slovenia. Korea tested later in 2003 than in 1999, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students.
A diamond (') indicates the country did not participate in the assessment.

## Exhibit 8.6: Index of Good School and Class Attendance (GSCA)




| Countries |  | High GSCA | Medium GSCA | Low GSCA |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 2003 <br> Percent of Students | $2003$ <br> Percent of Students | $2003$ <br> Percent of Students |
| Slovenia |  | 81 (3.8) | 18 (3.7) | 2 (1.1) |
| Chinese Taipei |  | 79 (3.5) | 21 (3.5) | 0 (0.0) |
| Italy |  | 72 (3.4) | 26 (3.3) | 2 (1.1) |
| Netherlands |  | 69 (4.1) | 31 (4.1) | 0 (0.0) |
| Singapore |  | 65 (4.3) | 33 (4.3) | 1 (0.6) |
| Hong Kong, SAR |  | 64 (5.1) | 36 (5.1) | 0 (0.0) |
| Belgium (Flemish) |  | 54 (3.9) | 45 (4.0) | 1 (0.8) |
| Scotland |  | 53 (5.4) | 43 (5.4) | 4 (1.6) |
| Japan |  | 52 (3.7) | 41 (4.0) | 7 (1.6) |
| Norway |  | 51 (4.3) | 48 (4.2) | 0 (0.0) |
| Cyprus |  | 49 (5.0) | 51 (5.0) | 0 (0.0) |
| Tunisia |  | 46 (3.6) | 45 (3.9) | 9 (2.2) |
| Hungary |  | 46 (4.0) | 51 (4.0) | 3 (1.3) |
| Lithuania |  | 46 (4.2) | 53 (4.2) | 2 (1.0) |
| Iran, Islamic Rep. of |  | 45 (4.7) | 53 (4.9) | 2 (1.3) |
| Australia |  | 41 (4.4) | 55 (4.6) | 4 (2.0) |
| Latvia |  | 41 (4.3) | 52 (4.8) | 7 (2.4) |
| Morocco | $r$ | 39 (4.8) | 41 (5.3) | 20 (3.9) |
| England | $r$ | 38 (4.9) | 58 (5.1) | 4 (1.4) |
| New Zealand |  | 35 (3.1) | 63 (3.3) | 2 (0.9) |
| Armenia | $r$ | 33 (4.1) | 55 (4.6) | 11 (3.4) |
| Russian Federation |  | 28 (3.5) | 68 (3.7) | 4 (1.4) |
| Moldova, Rep. of | $r$ | 26 (4.0) | 56 (4.6) | 19 (3.7) |
| United States |  | 21 (2.8) | 71 (2.8) | 8 (1.8) |
| Philippines |  | 11 (2.7) | 74 (3.9) | 15 (3.3) |
| International Avg. |  | 47 (0.8) | 47 (0.9) | 5 (0.4) |
| Benchmarking Participants |  |  |  |  |
| Indiana State, US |  | 29 (5.9) | 68 (5.8) | 3 (2.3) |
| Ontario Province, Can. |  | 35 (4.4) | 61 (4.4) | 3 (2.2) |
| Quebec Province, Can. |  | 43 (3.9) | 53 (4.1) | 4 (2.1) |

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.

## How Safe and Orderly Are Schools?

Since school safety is central for providing an environment conducive to learning, TIMSS asked both teachers and students to characterize their perceptions of safety in their schools. More specifically, teachers were asked how much they agreed with three statements:

- This school is located in a safe neighborhood;
- I feel safe at this school;
- This school's security policies and practices are sufficient.

TIMSS used the teachers' responses to create an index, called the Index of Mathematics Teachers' Perceptions of Safety in the Schools. If their teachers agreed or agreed a lot to all three statements, then the students were placed in the high category. If their teachers disagreed or disagreed a lot to all three statements, then students were placed in the low category. All other combinations (some agreements and some disagreements) were placed in the medium category.

Exhibit 8.7 contains the results for the Index of Mathematics Teachers' Perception of Safety in the Schools. On the positive side of things, across countries, about three-fourths of students in both grades were in the high category ( 72 percent of the eighth-grade students and 75 percent of the fourth-grade students). One-fifth were in the medium category ( 22 to 21 percent, respectively) and only 6 to 4 percent were in the low category. At both grades, there was a positive relationship between teachers' reports of school safety and mathematics achievement.

TIMSS asked the students to answer "yes" or "no" to whether each of the following five things had happened during the last month:

- Something of mine was stolen;
- I was hit or hurt by other students;
- I was made to do things that I didn't want to do by other students;
- I was made fun of or called names;
- I was left out of activities by other students.

TIMSS used students' responses to create the Index of Students' Perception of Being Safe in the Schools. Students who reported being in a safe environment, answering "no" to all five statements, were placed in the high category. Students who reported being in a much riskier school environment by answering "yes" to all five statements were placed in the low category. Students who answered "yes" to some statements and "no" to others were placed in the medium category.

Exhibit 8.8 presents the results for the Index of Students' Perception of Being Safe in the Schools. Internationally, on average, eighth-grade students reported a greater sense of security than did fourth-grade students. Nearly half of the eighth-grade students (48\%) were in the high category, 37 percent were in the medium category, and 15 percent were in the low category. It should be emphasized, however, that the feeling of safety was not universal. In several countries, more than one-third of the eighth-grade students were in the low category, including Jordan, the Philippines, Ghana, and South Africa. Eighth-grade students in the low category had lower average mathematics achievement than their counterparts in safer schools.

At the fourth grade, across the participating countries, 35 percent of the students, on average, were in the high category, 42 percent were in the medium category, and 23 percent were in the low category. The two countries with more than one-third of the fourth-grade students in the low category were Chinese Taipei and the Philippines. At the fourth grade, there was a direct relationship between students' reporting being in safer schools and having higher mathematics achievement.

Index of Teachers' Perception of Safety in the Schools

Index based on teachers' responses to three statements about their schools: this school is located in a safe neighborhood; I feel safe at this school; this school's security policies and practices are sufficient. High level indicates that the teacher agrees a lot or agrees to all three statements. Low level indicates that teacher disagrees or disagrees a lot to all three statements. Medium level includes all other combinations of responses.

| Countries |  |  | High TPSS |  | Medium TPSS |  | Low TPSS |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | Singapore |  | 91 (1.5) | 609 (3.7) | 8 (1.5) | 582 (16.6) | 1 (0.5) | ~ ~ |
|  | New Zealand |  | 90 (2.4) | 501 (5.4) | 7 (1.8) | 460 (12.2) | 3 (1.6) | 454 (25.7) |
|  | Norway |  | 88 (2.6) | 461 (2.8) | 12 (2.6) | 463 (4.7) | 0 (0.0) | ~~ |
|  | Hungary |  | 88 (2.5) | 530 (3.5) | 10 (2.0) | 519 (12.8) | 2 (1.3) | ~ ~ |
|  | Egypt |  | 87 (2.8) | 408 (3.9) | 8 (2.2) | 397 (12.5) | 5 (1.9) | 376 (13.5) |
|  | Bahrain |  | 87 (1.2) | 404 (1.8) | 11 (1.6) | 383 (11.1) | 2 (1.1) | ~ ~ |
|  | Belgium (Flemish) |  | 85 (2.7) | 539 (3.5) | 15 (2.6) | 533 (11.5) | 0 (0.0) | ~ ~ |
|  | Lithuania |  | 85 (2.5) | 501 (2.7) | 13 (2.3) | 508 (8.4) | 2 (1.0) | $\sim \sim$ |
|  | Indonesia |  | 84 (2.6) | 411 (5.6) | 13 (2.0) | 418 (12.0) | 4 (1.7) | 386 (24.9) |
|  | Malaysia |  | 84 (3.2) | 508 (4.4) | 15 (3.1) | 511 (10.4) | 1 (0.8) | ~ ~ |
|  | United States |  | 84 (2.2) | 513 (3.2) | 16 (2.2) | 488 (10.0) | 0 (0.3) | ~ ~ |
|  | Saudi Arabia |  | 83 (3.4) | 336 (4.6) | 13 (3.1) | 330 (6.8) | 4 (1.7) | 320 (11.0) |
|  | Sweden |  | 83 (3.1) | 501 (2.8) | 17 (3.0) | 493 (8.3) | 1 (0.4) | ~ ~ |
|  | Slovak Republic |  | 82 (3.3) | 510 (3.9) | 16 (3.3) | 496 (7.6) | 2 (1.2) | ~ ~ |
|  | Australia |  | 81 (3.4) | 508 (5.9) | 15 (3.1) | 489 (12.1) | 4 (1.5) | 467 (12.2) |
|  | Serbia |  | 81 (3.6) | 473 (2.6) | 12 (2.9) | 476 (9.8) | 6 (2.2) | 518 (11.9) |
|  | Netherlands |  | 81 (4.1) | 541 (5.2) | 19 (4.1) | 518 (13.5) | 0 (0.0) | ~ ~ |
|  | Israel |  | 80 (2.8) | 497 (3.5) | 19 (2.8) | 490 (10.0) | 2 (0.7) | ~ ~ |
|  | Hong Kong, SAR |  | 79 (3.5) | 588 (3.9) | 21 (3.5) | 580 (9.6) | 0 (0.0) | ~ ~ |
|  | Romania |  | 79 (3.8) | 474 (6.0) | 16 (3.4) | 481 (10.9) | 5 (1.8) | 473 (15.9) |
|  | Lebanon |  | 79 (4.1) | 440 (3.5) | 19 (4.0) | 407 (6.3) | 2 (1.0) | $\sim \sim$ |
|  | Cyprus |  | 78 (1.6) | 458 (2.0) | 19 (1.5) | 467 (3.0) | 3 (0.6) | 467 (9.7) |
|  | Tunisia |  | 78 (3.7) | 411 (2.7) | 19 (3.5) | 410 (4.0) | 3 (1.4) | 398 (12.4) |
|  | Jordan |  | 77 (3.3) | 429 (4.2) | 16 (3.3) | 416 (10.0) | 6 (2.3) | 385 (24.0) |
|  | Armenia |  | 77 (3.1) | 477 (3.2) | 21 (3.0) | 479 (7.2) | 2 (1.1) | ~~ |
|  | Philippines |  | 74 (4.2) | 387 (6.7) | 23 (4.0) | 350 (10.7) | 3 (1.5) | 362 (42.7) |
|  | Estonia |  | 72 (3.6) | 530 (3.6) | 24 (3.4) | 534 (5.4) | 4 (1.4) | 532 (19.8) |
|  | Iran, Islamic Rep. of |  | 72 (3.8) | 415 (3.0) | 25 (3.5) | 404 (4.1) | 4 (1.5) | 403 (17.6) |
|  | Slovenia |  | 70 (4.1) | 492 (2.8) | 26 (3.9) | 497 (4.1) | 4 (1.4) | 493 (13.4) |
|  | Chinese Taipei |  | 70 (3.6) | 584 (5.2) | 27 (3.2) | 588 (8.6) | 3 (1.6) | 582 (19.8) |
|  | Bulgaria |  | 69 (3.7) | 471 (5.1) | 27 (3.6) | 481 (10.5) | 4 (1.5) | 501 (26.2) |
|  | Italy |  | 68 (3.3) | 492 (3.6) | 23 (3.0) | 466 (6.5) | 9 (2.2) | 465 (8.8) |
|  | Macedonia, Rep. of |  | 68 (4.1) | 431 (5.1) | 23 (3.8) | 431 (8.4) | 9 (2.4) | 477 (12.6) |
|  | Latvia |  | 66 (4.1) | 509 (3.6) | 31 (3.9) | 507 (6.8) | 3 (1.0) | 498 (16.2) |
|  | Russian Federation |  | 61 (3.5) | 508 (4.4) | 35 (3.6) | 511 (5.3) | 4 (1.3) | 499 (11.0) |
|  | Scotland |  | 59 (4.1) | 510 (5.8) | 34 (4.1) | 488 (7.4) | 7 (2.5) | 508 (12.9) |
|  | Moldova, Rep. of | $r$ | 59 (4.9) | 463 (6.3) | 33 (4.4) | 452 (9.0) | 8 (2.5) | 451 (12.7) |
|  | Chile |  | 56 (3.9) | 401 (5.4) | 36 (3.9) | 369 (5.1) | 8 (2.2) | 376 (10.2) |
|  | Morocco | s | 55 (6.9) | 386 (4.7) | 30 (5.5) | 397 (5.0) | 16 (4.8) | 378 (6.3) |
|  | Japan |  | 54 (4.0) | 574 (3.0) | 34 (3.9) | 569 (3.5) | 12 (2.9) | 555 (5.4) |
|  | Palestinian Nat'l Auth. |  | 51 (4.7) | 391 (5.1) | 35 (4.3) | 388 (5.5) | 13 (3.1) | 396 (12.8) |
|  | Korea, Rep. of | s | 50 (3.7) | 594 (2.9) | 36 (3.6) | 585 (4.9) | 14 (2.8) | 587 (3.6) |
|  | Ghana |  | 40 (4.7) | 276 (8.3) | 46 (4.7) | 276 (6.0) | 14 (3.0) | 256 (12.3) |
|  | South Africa |  | 30 (3.5) | 306 (14.6) | 42 (4.1) | 244 (5.1) | 28 (3.4) | 242 (4.4) |
|  | Botswana |  | 22 (3.7) | 379 (8.4) | 46 (4.7) | 360 (3.6) | 32 (4.7) | 366 (4.5) |
| ま | England | r | 69 (7.0) | 506 (8.9) | 24 (5.9) | 517 (13.9) | 7 (3.5) | 474 (22.1) |
|  | International Avg. |  | 72 (0.5) | 470 (0.8) | 22 (0.5) | 461 (1.3) | 6 (0.3) | 440 (3.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
|  | Basque Country, Spain |  | 73 (4.8) | 488 (3.0) | 25 (4.8) | 488 (6.8) | 1 (1.0) | ~ ~ |
|  | Indiana State, US |  | 84 (4.1) | 515 (5.5) | 12 (3.2) | 470 (12.6) | 4 (2.7) | 481 (51.7) |
|  | Ontario Province, Can. |  | 84 (2.8) | 522 (3.2) | 13 (3.2) | 520 (11.0) | 3 (1.5) | 501 (21.2) |
|  | Quebec Province, Can. |  | 93 (2.0) | 545 (3.2) | 6 (2.1) | 527 (16.6) | 1 (1.2) | ~ ~ |

[^80]
## Exhibit 8.7: Index of Mathematics Teachers' Perception of Safety in the Schools (TPSS)



| Countries |  | High TPSS |  | Medium TPSS |  | Low <br> TPSS |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Norway |  | 91 (2.8) | 451 (2.5) | 9 (2.7) | 451 (10.4) | 1 (0.7) | ~ ~ |
| Hungary |  | 88 (3.0) | 526 (3.2) | 11 (2.8) | 541 (16.7) | 1 (1.0) | ~ |
| Singapore |  | 87 (2.8) | 599 (5.8) | 12 (2.8) | 563 (14.8) | 0 (0.2) | ~ |
| New Zealand |  | 87 (2.0) | 498 (2.5) | 13 (1.9) | 470 (11.6) | 0 (0.4) | ~ ~ |
| Netherlands |  | 85 (2.2) | 547 (2.0) | 13 (2.1) | 513 (9.5) | 2 (1.5) | ~ ~ |
| United States |  | 82 (2.2) | 526 (2.5) | 15 (2.0) | 486 (5.8) | 2 (0.8) | ~ ~ |
| Iran, Islamic Rep. of |  | 81 (4.3) | 392 (5.1) | 16 (4.1) | 378 (8.9) | 2 (1.5) | ~ ~ |
| Lithuania |  | 81 (3.1) | 535 (3.3) | 17 (2.8) | 523 (6.7) | 3 (1.1) | 519 (11.1) |
| Tunisia | r | 79 (3.8) | 342 (5.8) | 11 (2.6) | 319 (20.8) | 10 (2.8) | 331 (13.0) |
| Armenia | $r$ | 79 (3.2) | 457 (4.7) | 18 (3.5) | 443 (8.6) | 3 (1.3) | 439 (13.7) |
| Hong Kong, SAR |  | 79 (3.9) | 576 (3.7) | 17 (3.8) | 570 (4.9) | 4 (1.7) | 561 (9.0) |
| Australia |  | 79 (3.5) | 506 (4.4) | 20 (3.5) | 479 (10.5) | 1 (0.7) | ~ ~ |
| Philippines |  | 78 (3.7) | 366 (9.7) | 17 (3.3) | 336 (11.0) | 5 (2.1) | 327 (25.6) |
| Cyprus |  | 78 (3.3) | 512 (2.7) | 20 (3.3) | 501 (5.3) | 2 (0.9) | ~ ~ |
| Scotland | $r$ | 77 (3.2) | 501 (4.4) | 22 (3.1) | 471 (5.1) | 1 (0.0) | $\sim$ |
| Slovenia |  | 73 (4.1) | 475 (3.3) | 23 (4.0) | 493 (5.7) | 4 (1.7) | 476 (13.6) |
| Russian Federation |  | 72 (3.2) | 533 (5.8) | 26 (3.2) | 529 (7.8) | 1 (0.7) | ~ ~ |
| England | $r$ | 70 (4.0) | 541 (4.9) | 28 (4.0) | 507 (7.7) | 2 (1.2) | $\sim \sim$ |
| Belgium (Flemish) |  | 70 (2.9) | 552 (1.8) | 29 (2.8) | 548 (4.2) | 1 (0.4) | $\sim$ |
| Chinese Taipei |  | 69 (3.7) | 564 (2.2) | 28 (3.6) | 568 (3.0) | 3 (1.3) | 519 (12.5) |
| Italy |  | 65 (3.5) | 509 (4.3) | 24 (3.0) | 489 (8.2) | 12 (2.2) | 499 (12.0) |
| Moldova, Rep. of |  | 63 (4.3) | 501 (7.5) | 32 (4.1) | 511 (7.3) | 4 (1.6) | 488 (15.5) |
| Latvia |  | 63 (3.8) | 537 (3.7) | 34 (3.6) | 534 (6.0) | 3 (1.4) | 531 (15.7) |
| Japan |  | 55 (4.0) | 566 (2.3) | 37 (4.1) | 563 (3.0) | 8 (2.3) | 561 (4.8) |
| Morocco | 5 | 47 (4.7) | 348 (8.5) | 31 (4.6) | 361 (7.2) | 21 (4.2) | 325 (12.1) |
| International Avg. |  | 75 (0.7) | 498 (0.9) | 21 (0.7) | 486 (1.9) | 4 (0.3) | 465 (4.0) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | 88 (3.3) | 534 (3.1) | 10 (2.7) | 529 (8.7) | 2 (1.2) | ~ ~ |
| Ontario Province, Can. |  | 90 (3.1) | 513 (4.0) | 10 (3.1) | 492 (9.9) | 0 (0.3) | $\sim$ |
| Quebec Province, Can. |  | 81 (3.6) | 508 (2.5) | 17 (3.4) | 500 (7.3) | 2 (1.3) | $\sim \sim$ |

## Background data provided by teachers.

() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A tilde ( $\sim$ ) indicates insufficient data to report achievement.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. answered YES to three or more statements. Medium level includes all other possible combinations of responses.

| Countries | High SPBSS |  | Medium SPBSS |  | $\begin{gathered} \text { Low } \\ \text { SPBSS } \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Sweden | 78 (1.0) | 501 (2.6) | 20 (0.8) | 501 (3.8) | 3 (0.3) | 482 (7.9) |
| Armenia | 72 (1.0) | 487 (3.4) | 23 (0.8) | 471 (4.3) | 6 (0.6) | 455 (6.8) |
| Bulgaria | 69 (1.1) | 485 (4.8) | 25 (0.9) | 466 (4.7) | 6 (0.5) | 440 (8.9) |
| Serbia | 67 (1.2) | 484 (2.8) | 27 (1.0) | 472 (3.7) | 5 (0.5) | 450 (7.4) |
| Netherlands | 66 (1.4) | 540 (4.1) | 29 (1.1) | 533 (4.8) | 5 (0.5) | 519 (8.3) |
| Belgium (Flemish) | 64 (1.1) | 544 (2.9) | 31 (1.0) | 530 (3.2) | 5 (0.4) | 510 (6.7) |
| Estonia | 64 (1.2) | 534 (3.2) | 30 (1.0) | 529 (3.9) | 6 (0.5) | 518 (5.8) |
| Norway | 63 (1.1) | 468 (2.5) | 30 (0.8) | 457 (2.9) | 6 (0.5) | 437 (6.3) |
| Korea, Rep. of | 62 (1.1) | 591 (2.2) | 32 (0.8) | 589 (3.1) | 6 (0.5) | 578 (6.1) |
| Hungary | 61 (1.2) | 534 (3.3) | 32 (1.0) | 530 (3.9) | 7 (0.5) | 508 (6.3) |
| Japan | 61 (1.0) | 571 (2.5) | 31 (0.8) | 573 (3.1) | 8 (0.5) | 554 (5.5) |
| Lithuania | 60 (1.1) | 506 (2.8) | 34 (0.8) | 499 (3.1) | 7 (0.5) | 481 (6.0) |
| Russian Federation | 60 (0.9) | 513 (3.7) | 35 (0.9) | 505 (4.5) | 6 (0.4) | 501 (5.3) |
| Scotland | 59 (1.2) | 501 (4.1) | 33 (1.0) | 500 (4.1) | 8 (0.6) | 479 (8.3) |
| Italy | 56 (1.1) | 491 (3.3) | 35 (0.9) | 480 (3.5) | 9 (0.6) | 462 (5.6) |
| Latvia | 56 (1.4) | 517 (3.2) | 36 (1.3) | 503 (3.9) | 7 (0.6) | 488 (6.5) |
| Macedonia, Rep. of | 56 (1.2) | 453 (4.0) | 33 (0.9) | 435 (4.0) | 11 (0.8) | 395 (7.2) |
| Saudi Arabia | 55 (1.9) | 334 (5.0) | 35 (1.4) | 339 (5.0) | 11 (0.8) | 327 (6.4) |
| Israel | 53 (1.2) | 505 (3.7) | 35 (1.2) | 500 (3.9) | 11 (0.6) | 465 (5.9) |
| Slovenia | 53 (1.3) | 495 (2.7) | 38 (1.3) | 497 (3.1) | 10 (0.6) | 478 (4.0) |
| Malaysia | 51 (1.1) | 516 (4.6) | 41 (1.0) | 502 (3.8) | 8 (0.5) | 495 (6.0) |
| Slovak Republic | 50 (1.2) | 519 (3.7) | 38 (0.9) | 502 (3.6) | 12 (0.7) | 483 (5.8) |
| Iran, Islamic Rep. of | 49 (1.5) | 421 (2.4) | 39 (1.1) | 405 (3.0) | 11 (0.7) | 398 (4.9) |
| Romania | 48 (1.4) | 490 (5.4) | 38 (1.0) | 472 (4.6) | 14 (0.9) | 450 (7.3) |
| Moldova, Rep. of | 48 (1.2) | 473 (4.7) | 38 (1.0) | 456 (4.2) | 14 (0.8) | 439 (6.1) |
| Chinese Taipei | 47 (0.9) | 593 (4.9) | 36 (0.7) | 583 (5.0) | 17 (0.6) | 568 (5.9) |
| Tunisia | 47 (1.0) | 413 (2.5) | 40 (0.9) | 409 (2.6) | 13 (0.6) | 412 (3.9) |
| Hong Kong, SAR | 46 (1.3) | 589 (3.3) | 42 (1.0) | 588 (4.0) | 12 (0.7) | 573 (5.8) |
| Singapore | 44 (0.7) | 618 (3.2) | 43 (0.6) | 602 (4.0) | 13 (0.5) | 576 (5.7) |
| Australia | 43 (1.2) | 510 (4.7) | 40 (1.0) | 507 (5.3) | 18 (0.9) | 499 (5.0) |
| Egypt | 42 (1.3) | 443 (3.1) | 40 (1.0) | 400 (3.5) | 18 (0.9) | 360 (5.4) |
| Bahrain | 41 (1.0) | 413 (2.3) | 42 (0.9) | 403 (2.2) | 17 (0.8) | 376 (3.9) |
| Cyprus | 41 (0.9) | 476 (1.9) | 42 (0.8) | 461 (2.2) | 17 (0.8) | 434 (4.0) |
| Palestinian Nat'l Auth. | 41 (1.3) | 411 (3.2) | 42 (0.9) | 387 (3.6) | 17 (0.9) | 360 (4.2) |
| New Zealand | 40 (1.5) | 506 (5.7) | 41 (1.3) | 492 (5.4) | 19 (1.2) | 482 (7.6) |
| Indonesia | 39 (1.2) | 419 (4.8) | 45 (1.1) | 413 (5.3) | 16 (0.8) | 402 (6.5) |
| Lebanon | 36 (1.8) | 458 (4.1) | 37 (0.9) | 432 (3.4) | 26 (1.8) | 406 (3.6) |
| Morocco | 35 (1.2) | 393 (3.6) | 48 (1.1) | 388 (3.3) | 17 (0.8) | 384 (4.3) |
| Chile | 31 (1.0) | 400 (3.9) | 51 (0.7) | 387 (3.6) | 18 (0.8) | 366 (4.7) |
| Jordan | 17 (2.3) | 443 (12.3) | 22 (1.6) | 410 (6.2) | 61 (3.2) | 431 (3.3) |
| Philippines | 15 (0.9) | 413 (7.2) | 47 (0.9) | 382 (5.1) | 38 (1.1) | 360 (5.4) |
| Ghana | 13 (1.0) | 301 (6.8) | 49 (1.0) | 288 (5.2) | 38 (1.3) | 265 (4.5) |
| South Africa | 13 (0.9) | 341 (14.9) | 47 (0.9) | 272 (5.5) | 40 (1.2) | 231 (3.6) |
| Botswana | 12 (0.6) | 388 (4.5) | 56 (0.8) | 371 (3.3) | 32 (0.9) | 356 (2.2) |
| United States | - - | - - | - - | - - | - - | - - |
| $\ddagger$ England | 51 (1.4) | 503 (5.9) | 37 (1.0) | 503 (5.4) | 12 (1.0) | 488 (7.0) |
| International Avg. | 48 (0.2) | 478 (0.7) | 37 (0.1) | 465 (0.6) | 15 (0.1) | 447 (0.9) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 62 (2.0) | 493 (3.0) | 32 (1.6) | 484 (3.7) | 6 (0.7) | 454 (7.1) |
| Indiana State, US | - - | - | - - | - | - - | -- |
| Ontario Province, Can. | 45 (1.4) | 522 (3.6) | 40 (1.1) | 522 (3.6) | 15 (1.1) | 517 (5.7) |
| Quebec Province, Can. | 55 (1.2) | 546 (3.3) | 36 (1.0) | 542 (3.3) | 9 (0.6) | 535 (4.9) |

[^81]A dash ( - ) indicates comparable data are not available.
£ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.


Grade


| Countries |  | High SPBSS |  | Medium SPBSS |  | $\begin{gathered} \text { Low } \\ \text { SPBSS } \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Armenia | r | 58 (1.4) | 474 (4.2) | 37 (1.4) | 451 (3.5) | 5 (0.4) | 430 (8.5) |
| Norway |  | 53 (1.2) | 467 (2.3) | 34 (1.0) | 453 (3.1) | 13 (0.7) | 426 (4.0) |
| Japan |  | 45 (1.2) | 573 (1.9) | 39 (0.9) | 566 (2.2) | 17 (0.8) | 543 (3.2) |
| Lithuania |  | 44 (1.2) | 549 (3.0) | 43 (1.1) | 530 (3.9) | 13 (0.7) | 511 (5.2) |
| Netherlands |  | 44 (1.5) | 550 (2.2) | 40 (1.1) | 539 (2.9) | 17 (1.0) | 523 (3.6) |
| Latvia |  | 41 (1.3) | 549 (3.2) | 45 (1.0) | 536 (3.0) | 14 (0.8) | 504 (5.8) |
| Russian Federation |  | 40 (1.3) | 546 (5.1) | 46 (1.0) | 528 (4.9) | 14 (0.8) | 515 (6.1) |
| Hong Kong, SAR |  | 40 (1.5) | 585 (3.6) | 40 (0.9) | 572 (3.3) | 21 (1.1) | 562 (3.7) |
| Slovenia |  | 40 (1.4) | 489 (3.5) | 40 (1.1) | 481 (3.7) | 20 (1.2) | 461 (4.1) |
| Hungary |  | 37 (1.2) | 541 (3.5) | 43 (1.0) | 530 (3.8) | 20 (0.8) | 511 (4.9) |
| Moldova, Rep. of |  | 37 (2.0) | 527 (6.4) | 43 (1.4) | 502 (4.8) | 20 (1.3) | 475 (7.2) |
| Belgium (Flemish) |  | 35 (1.2) | 561 (2.4) | 41 (0.8) | 549 (2.2) | 24 (0.9) | 540 (2.4) |
| Iran, Islamic Rep. of |  | 33 (2.2) | 396 (5.3) | 44 (1.4) | 389 (4.9) | 23 (1.6) | 387 (5.6) |
| Italy |  | 33 (1.1) | 510 (5.2) | 42 (0.9) | 508 (4.1) | 25 (1.0) | 491 (4.6) |
| Scotland |  | 33 (1.4) | 506 (3.5) | 40 (1.0) | 492 (3.6) | 27 (1.2) | 472 (4.9) |
| England |  | 32 (1.2) | 550 (4.7) | 42 (0.9) | 538 (4.1) | 26 (1.2) | 502 (4.3) |
| Australia |  | 29 (1.0) | 516 (3.6) | 39 (1.0) | 504 (4.7) | 32 (1.4) | 482 (4.8) |
| Chinese Taipei |  | 28 (1.0) | 575 (2.5) | 37 (0.8) | 568 (1.6) | 35 (1.0) | 552 (2.8) |
| Cyprus |  | 27 (1.0) | 533 (3.1) | 47 (0.8) | 514 (2.8) | 25 (1.0) | 484 (3.4) |
| New Zealand |  | 26 (0.8) | 515 (3.0) | 42 (1.0) | 497 (2.6) | 32 (0.9) | 477 (3.5) |
| Singapore |  | 25 (0.9) | 616 (5.1) | 47 (0.7) | 598 (5.8) | 28 (0.9) | 572 (6.5) |
| Morocco | $r$ | 25 (2.1) | 361 (9.1) | 52 (1.7) | 352 (4.8) | 23 (1.4) | 345 (6.4) |
| Tunisia |  | 23 (1.8) | 365 (8.4) | 50 (1.2) | 347 (5.1) | 27 (1.4) | 332 (5.6) |
| Philippines |  | 7 (0.8) | 387 (20.2) | 43 (1.1) | 367 (9.0) | 50 (1.5) | 352 (6.8) |
| United States |  | - - | - - | - - | - - | - - | - - |
| International Avg. |  | 35 (0.3) | 510 (1.2) | 42 (0.2) | 496 (0.9) | 23 (0.2) | 477 (1.1) |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US |  | -- | - - | - - | - - | - - | - - |
| Ontario Province, Can. |  | 30 (1.1) | 527 (4.6) | 40 (1.0) | 513 (4.3) | 29 (1.1) | 497 (4.1) |
| Quebec Province, Can. |  | 34 (1.1) | 517 (3.1) | 42 (0.8) | 508 (2.7) | 24 (1.1) | 490 (3.6) |

[^82]A dash (-) indicates comparable data are not available.
An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.


## Appendix A

## Overview of TIMSS Procedures for Assessing Mathematics

## History

TIMSS 2003 is the latest in a long series of studies conducted by the International Association for the Evaluation of Educational Achievement (IEA). Since its inception in 1959, the IEA has conducted almost 20 studies of cross-national achievement in the curricular areas of mathematics, science, language, civics, and reading.

In particular, TIMSS 2003 continues a rich tradition of studies designed to improve teaching and learning in mathematics and science. IEA conducted the pioneering First International Science Study (FISS) in 1970-71 and the Second International Science Study (SISS) in 198384. The First and Second International Mathematics Studies (FIMS and SIMS) were conducted in 1964 and 1980-82, respectively. The Third International Mathematics and Science Study (TIMSS) in 1994-1995 was the largest and most complex IEA study ever conducted, including both mathematics and science at third and fourth grades, seventh and eighth grades, and the final year of secondary school.

In 1999, TIMSS (now renamed the Trends in International Mathematics and Science Study) again assessed eighth-grade students
in both mathematics and science to measure trends in student achievement since 1995. Also, 1999 represented four years since the first TIMSS, and the population of students originally assessed as fourthgraders had advanced to the eighth grade. Thus, TIMSS 1999 also provided information about whether the relative performance of these students had changed in the intervening years.

TIMSS 2003, the third data collection in the TIMSS cycle of studies, was administered at the eighth and fourth grades. For countries that participated in previous assessments, TIMSS 2003 provides three-cycle trends at the eighth grade $(1995,1999,2003)$ and data over two points in time at the fourth grade (1995 and 2003). In countries new to the study, the 2003 results can help policy makers and practitioners assess their comparative standing and gauge the rigor and effectiveness of their mathematics and science programs. TIMSS 2007 will again assess mathematics and science achievement at fourth and eighth grades, providing previously participating countries an opportunity to extend their trend lines and new countries an opportunity to join a valuable and exciting endeavor.

## Participants in TIMSS

Exhibit A. 1 lists all the countries that have participated in TIMSS in 1995, 1999, or 2003 at fourth or eighth grade. In all, 67 countries have participated in TIMSS at one time or another. Of the 49 countries that participated in TIMSS 2003, 48 participated at the eighth grade and 26 at the fourth grade. Yemen participated at the fourth but not the eighth grade. The exhibit shows that at the eighth grade 23 countries also participated in TIMSS 1995 and TIMSS 1999. For these participants, trend data across three points in time are available. Eleven countries participated in TIMSS 2003 and TIMSS 1999 only, while three countries participated in TIMSS 2003 and TIMSS 1995. These countries have trend data for two points in time. Of the 12 new countries participating in the study, 11 participated at eighth grade and 2 at the fourth grade. Of the 26 countries participating in

TIMSS 2003 at the fourth grade, 16 also participated in 1995, providing data at two points in time.

Inspired by the very successful TIMSS 1999 benchmarking initiative in the United States, ${ }^{1}$ in which 13 states and 14 school districts or district consortia administered the TIMSS assessment and compared their students' achievement to student achievement world wide, TIMSS 2003 provided an international benchmarking program, whereby regions or localities of countries could participate in the study to compare to international standards. TIMSS 2003 included four benchmarking participants at the eighth grade: the Basque Country of Spain, the US state of Indiana, and the Canadian provinces of Ontario and Quebec. Indiana, Ontario, and Quebec participated also at the fourth grade. Having also participated in 1999, Indiana has data at two points in time at eighth grade. Ontario and Quebec participated also in 1995 and 1999, and so have trend data across three points in time at both grade levels.


| Countries | Grade 8 |  |  | Grade 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2003 | 1999 | 1995 | 2003 | 1995 |
| 1 Argentina | - | - |  |  |  |
| Armenia | - |  |  | - |  |
| Australia | - | - | - | - | - |
| Austria |  |  | - |  | - |
| Bahrain | - |  |  |  |  |
| Belgium (Flemish) | - | - | - | - |  |
| Belgium (French) |  |  | - |  |  |
| Botswana | - |  |  |  |  |
| Bulgaria | - | - | - |  |  |
| Canada |  | - | - |  | - |
| Chile | - | - |  |  |  |
| Chinese Taipei | - | - |  | - |  |
| Colombia |  |  | - |  |  |
| Cyprus | - | - | - | - | - |
| Czech Republic |  | - | - |  | - |
| Denmark |  |  | - |  |  |
| Egypt | - |  |  |  |  |
| England | - | - | - | - | - |
| Estonia | - |  |  |  |  |
| Finland |  | - |  |  |  |
| France |  |  | - |  |  |
| Germany |  |  | - |  |  |
| Ghana | - |  |  |  |  |
| Greece |  |  | - |  | - |
| Hong Kong, SAR | - | - | - | - | - |
| Hungary | - | - | - | - | - |
| Iceland |  |  | - |  | - |
| Indonesia | - | - |  |  |  |
| Iran, Islamic Rep. of | - | - | $\bigcirc$ | - | - |
| Ireland |  |  | - |  | - |
| Israel | - | - | - |  | - |
| Italy | - | - | - | $\bigcirc$ | - |
| Japan | - | - | - | - | - |
| Jordan | - | - |  |  |  |
| Korea, Rep. of | - | - | - |  | - |
| Kuwait |  |  | - |  | - |
| Latvia | - | - | - | - | - |
| Lebanon | - |  |  |  |  |
| Lithuania | - | - | - | - |  |
| Macedonia, Rep. of | - | - |  |  |  |
| Malaysia | - | - |  |  |  |
| Moldova, Rep. of | - | - |  | - |  |
| Morocco | - | - |  | - |  |
| Netherlands | - | - | - | - | - |
| New Zealand | - | - | - | - | - |
| Norway | - |  | - | - | - |
| Palestinian Nat'l Auth. | - |  |  |  |  |
| Philippines | - | - |  | - |  |
| Portugal |  |  | - |  | - |

[^83]
## Exhibit A.1: Countries Participating in TIMSS 2003, 1999, and 1995



[^84]
## Developing the TIMSS 2003 Mathematics Assessment

The development of the TIMSS 2003 mathematics assessment was a collaborative process spanning a two-and-a-half-year period and involving mathematics educators and development specialists from all over the world. ${ }^{2}$ Central to this effort was a major updating and revision of the existing TIMSS assessment frameworks to address changes during the last decade in curricula and the way mathematics is taught. The resulting publication entitled TIMSS Assessment Frameworks and Specifications 2003 serves as the basis of TIMSS 2003 and beyond. ${ }^{3}$

As shown in Exhibit A.2, the mathematics assessment framework for TIMSS 2003 is framed by two organizing dimensions or aspects, a content domain and a cognitive domain. The five content domains, number, algebra, measurement, geometry, and data, define the specific mathematics subject matter covered by the assessment, and the four cognitive domains define the sets of behaviors expected of students as they engage with the mathematics content. The cognitive domains include knowing facts and procedures, using concepts, solving routine problems, and reasoning.

Developing the TIMSS assessments for 2003 was a cooperative venture involving all of the National Research Coordinators (NRCs) during the entire process. Although about half of the items in the 1999 eighth-grade assessment had been kept secure and were available for use in 2003 to measure trends from 1995 and 1999, the ambitious goals for curriculum coverage and innovative problem solving tasks specified in the Frameworks and Specifications necessitated a tremendous item development effort.

To maximize the effectiveness of the contributions from national centers, the TIMSS \& PIRLS International Study Center developed a detailed item-writing manual and conducted a workshop for countries that wished to provide items for the international item pool. At this workshop, an item development "Task Force" consisting of the mathematics coordinator and two experienced mathematics item writers

2 For a full discussion of the TIMSS 2003 test development effort, please see Smith Neidorf, T.A. and Garden, R.A. (2004), "Developing the TIMSS 2003 Mathematics and Science Assessment and Scoring Guides" in M.O. Martin, I.V.S. Mullis and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.

3 Mullis, I.V.S., Martin, M.O., Smith, T.A., Garden, R.A., Gregory, K.D., Gonzalez, E.J., Chrostowski, S.J, and O’Connor, K.M. (2003), TIMSS Assessment Frameworks and Specifications 2003 (2nd Edition), Chestnut Hill, MA: Boston College

For the TIMSS frameworks used in 1995 and 1999, see Robitaille, D.F., McKnight, C.C., Schmidt, W.H., Britton, E.D., Raisen, S.A., and Nicol, C. (1993), TIMSS Monograph No. 1: Curriculum Frameworks for Mathematics and Science, Vancouver, BC: Pacific Educational Press.

## Exhibit A.2: The Content and the Cognitive Domains of the Mathematics Frameworks



## Data



Knowing Facts and Procedures

## Using Concepts

## Solving Routine Problems

## Reasoning

reviewed general item-writing guidelines for multiple-choice and con-structed-response items and provided specific training in writing mathematics and science items in accordance with the TIMSS Assessment Frameworks and Specifications 2003. In the weeks that followed, more than 2,000 items and scoring guides were drafted, and reviewed by the task force. The items were further reviewed by the Science and Mathematics Item Review Committee, a group of internationally prominent mathematics and science educators nominated by participating countries to advise on subject-matter issues in the assessment. Committee members also contributed enormously to the quality of the assessment by helping to develop tasks and items to assess problem solving and scientific inquiry.

Participating countries field-tested the items with representative samples of students, and all of the potential new items were again reviewed by the Science and Mathematics Item Review Committee. The NRCs had several opportunities to review the items and scoring criteria. The resulting TIMSS 2003 mathematics tests contained 194 items at the eighth grade and 161 items at the fourth grade.

Exhibit A. 3 presents the number and percentage of items, the number of multiple-choice and constructed-response items, and the number of score points in each of the five mathematics content domains for eighth and fourth grades. Comparable information is presented for the four cognitive domains. About one-fourth of the eighthgrade items and more than two-fifths of the fourth-grade items were in constructed-response format, requiring students to generate and write their own answers. Some constructed-response questions asked for short answers while others required extended responses with students showing their work or providing explanations for their answers. The remaining questions used a multiple-choice format. In scoring the items, correct answers to most questions were worth one point. However, responses to some constructed-response questions (particularly those requiring extended responses) were evaluated for partial credit, with a fully correct answer being awarded two points (see later
section on scoring). The total number of score points available for analysis thus somewhat exceeds the number of items (215 and 169 score points for eighth- and fourth-grades, respectively). About $40 \%$ of students' testing time at eighth grade and almost half at fourth grade was allocated to constructed-response items.

To ensure reliable measurement of trends over time, the TIMSS 2003 assessment included items that had been used in the 1995 and 1999 assessments as well as items developed for the first time in 2003. Exhibit A. 4 shows the distribution of score points across content domains for both trend items and items used for the first time. Of the 215 score points available in the entire 2003 mathematics assessment, 23 came from items used also in 1995, 60 from items used also in 1999, and 132 from items used for the first time in 2003. At fourth grade, 37 score points came from 1995 items, and the remaining 132 from new 2003 items.

Every effort was made to ensure that the tests represented the curricula of the participating countries and that the items exhibited no bias toward or against particular countries. The final forms of the test were endorsed by the NRCs of the participating countries. In addition, countries had an opportunity to match the content of the test to their curriculum. They identified items measuring topics not covered in their intended curriculum. The information from this Test-Curriculum Matching Analysis, provided in Appendix C, indicates that omitting such items has little effect on the overall pattern of results.

| Content Domain | Percentage of Items | Total Number of Items | Number of Multiple-Choice Items | Number of ConstructedResponse Items ${ }^{1}$ | Number of Score Points ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number | 30 | 57 | 43 | 14 | 60 |
| Algebra | 24 | 47 | 29 | 18 | 53 |
| Measurement | 16 | 31 | 19 | 12 | 34 |
| Geometry | 16 | 31 | 22 | 9 | 34 |
| Data | 14 | 28 | 15 | 13 | 34 |
| Total | 100 | 194 | 128 | 66 | 215 |


| Cognitive Domain | Percentage <br> of Items | Total <br> Number <br> of Items | Number of <br> Multiple-Choice <br> Items | Number of <br> Constructed- <br> Response <br> Items | Number <br> of Score <br> Points |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Knowing Facts <br> and Procedures | 23 | 45 | 35 | 10 | 45 |
| Using Concepts | 19 | 37 | 31 | 6 | 39 |
| Solving Routine <br> Problems | 36 | 70 | 43 | 27 | 76 |
| Reasoning | 22 | 42 | 19 | 23 | 55 |
| Total | 100 | 194 | 128 | 66 | 215 |

[^85][^86]Exhibit A.3: Distribution of Mathematics Items by Content Domain and Cognitive Domain

| Content Domain | Percentage of Items | Total Number of Items | Number of Multiple-Choice Items | Number of ConstructedResponse Items ${ }^{1}$ | Number of Score Points ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number | 39 | 63 | 30 | 33 | 68 |
| Patterns and Relationships | 15 | 24 | 16 | 8 | 25 |
| Measurement | 20 | 33 | 23 | 10 | 33 |
| Geometry | 15 | 24 | 12 | 12 | 25 |
| Data | 11 | 17 | 11 | 6 | 18 |
| Total | 100 | 161 | 92 | 69 | 169 |


| Cognitive Domain | Percentage <br> of Items | Total <br> Number <br> of Items | Number of <br> Multiple-Choice <br> Items | Number of <br> Constructed- <br> Response <br> Items | Number <br> of Score <br> Points $^{2}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Knowing Facts and <br> Procedures | 24 | 38 | 20 | 18 | 39 |
| Using Concepts | 23 | 37 | 24 | 13 | 39 |
| Solving Routine <br> Problems | 37 | 60 | 35 | 25 | 61 |
| Reasoning | 16 | 26 | 13 | 13 | 30 |
| Total | 100 | 161 | 92 | 69 | 169 |

2 In scoring the tests, correct answers to most items were worth one point. However, responses to some constructed-response items were evaluated for partial credit with a fully correct answer awarded two points. Thus, the number of score points exceeds the number of items in the test.

Exhibit A.4: Distribution of Score Points in TIMSS 2003 from Each Assessment Year by Mathematics Content Domain


Grade 8

| Content Domain | From 1995 | From 1999 | New in 2003 | Total |
| :--- | :---: | :---: | :---: | :---: |
| Number | 6 | 20 | 34 | 60 |
| Algebra | 6 | 11 | 36 | 53 |
| Measurement | 4 | 14 | 16 | 34 |
| Geometry | 4 | 8 | 22 | 34 |
| Data | 3 | 7 | 24 | 34 |
| Total | 23 | 60 | 132 | 215 |

## Grade 4

| Content Domain | From 1995 | From 1999 | New in 2003 | Total |
| :--- | :---: | :---: | :---: | :---: |
| Number | 19 | N/A | 49 | 68 |
| Patterns and <br> Relationships | 2 | N/A | 23 | 25 |
| Measurement | 8 | N/A | 25 | 33 |
| Geometry | 4 | N/A | 21 | 25 |
| Data | 4 | N/A | 14 | 18 |
| Total | 37 | N/A | 132 | 169 |

## TIMSS 2003 Assessment Design

Not all of the students in the TIMSS assessment responded to all of the mathematics items. To ensure broad subject-matter coverage without overburdening individual students, TIMSS 2003, as in the 1995 and 1999 assessments, used a matrix-sampling technique that assigns each assessment item to one of a set of item blocks, and then assembles student test booklets by combining the item blocks according to a balanced design. Each student takes one booklet containing both mathematics and science items. Thus, the same students participated in both the mathematics and science testing.

Exhibit A. 5 summarizes the TIMSS 2003 assessment design, presenting both the matrix-sampling item blocks for mathematics and science and the item block-to-booklet assignment plan. According to the design, the 313 mathematics and science items at fourth grade and 383 items at eighth grade are divided among 28 item blocks at each grade, 14 mathematics blocks labeled M01 through M14, and 14 science blocks labeled S01 through S14. Each block contains either mathematics items only or science items only. This general block design is the same for both grades, although the planned assessment time per block is 12 minutes for fourth grade and 15 minutes for eighth grade. At the eighth grade, six blocks in each subject (blocks $01-06$ ) contain secure items from 1995 and 1999 to measure trends and eight blocks (07-14) contain new items developed for TIMSS 2003. Since fourth grade was not included in the 1999 assessment, trend items from 1995 only were available, and these were placed in the first three blocks. The remaining 11 blocks contain items new in 2003.

In the TIMSS 2003 design, the 28 blocks of items are distributed across 12 student booklets, as shown in Exhibit A.5. Each booklet consists of six blocks of items. To enable linking between booklets, each block appears in two, three, or four different booklets. The assessment time for individual students is 72 minutes at fourth grade (six 12minute blocks) and 90 minutes at eighth grade (six 15-minute blocks),

Exhibit A.5: TIMSS 2003 Assessment Design


TIMSS 2003 Item Blocks for Matrix-Sampling

| Source of Items | Mathematics Blocks | Science Blocks |  |
| :--- | :--- | :--- | :--- |
| Trend Items (TIMSS 1995 or 1999) | M01 | S01 |  |
| Trend Items (TIMSS 1995 or 1999) | M02 | S02 |  |
| Trend Items (TIMSS 1995 or 1999) | M03 | S03 |  |
| Trend Items (TIMSS 1999) | M04 | S04 |  |
| Trend Items (TIMSS 1999) | M05 | S05 |  |
| Trend Items (TIMSS 1999) | M07 | S06 |  |
| New Replacement Items (TIMSS 2003) | M08 | S07 |  |
| New Replacement Items (TIMSS 2003) | M09 | S08 |  |
| New Replacement Items (TIMSS 2003) | M10 | S09 |  |
| New Replacement Items (TIMSS 2003) | M11 | S10 |  |
| New Replacement Items (TIMSS 2003) | M12 | S11 |  |
| New Replacement Items (TIMSS 2003) | M13 | S12 |  |
| New Replacement Items (TIMSS 2003) | M14 | S13 |  |
| New Replacement Items (TIMSS 2003) |  |  | S14 |

Booklet Design for TIMSS 2003

| Student Booklet | Part I |  |  | Part II |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Booklet 1 | M01 | M02 | S06 | S07 | M05 | M07 |
| Booklet 2 | M02 | M03 | S05 | S08 | M06 | M08 |
| Booklet 3 | M03 | M04 | S04 | S09 | M13 | M11 |
| Booklet 4 | M04 | M05 | S03 | S10 | M14 | M12 |
| Booklet 5 | M05 | M06 | S02 | S11 | M09 | M13 |
| Booklet 6 | M06 | M01 | S01 | S12 | M10 | M14 |
| Booklet 7 | S01 | S02 | M06 | M07 | S05 | S07 |
| Booklet 8 | S02 | S03 | M05 | M08 | S06 | S08 |
| Booklet 9 | S03 | S04 | M04 | M09 | S13 | S11 |
| Booklet 10 | S04 | S05 | M03 | M10 | S14 | S12 |
| Booklet 11 | S05 | S06 | M02 | M11 | S09 | S13 |
| Booklet 12 | S06 | S01 | M01 | M12 | S10 | S14 |

which is comparable to that in the 1995 and 1999 assessments. The booklets are organized into two three-block sessions (Parts I and II), with a break between the parts.

The 2003 assessment was the first TIMSS assessment in which calculators were permitted, and so it was important that the design allow students to use calculators when working on the new 2003 items. However, because calculators were not permitted in TIMSS 1995 or 1999, the design also had to ensure that students did not use calculators when working on trend items from these assessments. The solution was to place the blocks containing trend items (blocks M01 - M06 and S01 - S06) in Part I of the test booklets, to be completed without calculators before the break. After the break, calculators were allowed for the new items (blocks M07-M14 and S07-S14). To provide a more balanced design, however, and have information about differences with calculator access, two mathematics trend blocks (M05 and M06) and two science trend blocks (S05 and S06) also were placed in Part II of one booklet each.

## Background Questionnaires

As in previous assessments, TIMSS in 2003 administered a broad array of questionnaires to collect data on the educational context for student achievement. For TIMSS 2003, a concerted effort was made to streamline and upgrade the questionnaires. This work began with articulating the information to be collected in the TIMSS 2003 framework and continued with extensive field testing. ${ }^{4}$

Across the two grades and two subjects, TIMSS 2003 involved 11 questionnaires. National Research Coordinators completed four questionnaires. With the assistance of their curriculum experts, they provided detailed information on the organization, emphasis, and content coverage of the mathematics and science curriculum at fourth and eighth grades. The fourth- and eighth-grade students who were tested answered questions pertaining to their attitudes towards mathematics

[^87]and science, their academic self-concept, classroom activities, home background, and out-of-school activities. The mathematics and science teachers of sampled students responded to questions about teaching emphasis on the topics in the curriculum frameworks, instructional practices, professional training and education, and their views on mathematics and science. Separate questionnaires for mathematics and science teachers were administered at the eighth grade, while to reflect the fact that most younger students are taught all subjects by the same teacher, a single questionnaire was used at the fourth grade. The principals or heads of schools at the fourth and eighth grades responded to questions about school staffing and resources, school safety, mathematics and science course offerings, and teacher support.

## Translation and Verification

The TIMSS data collection instruments were prepared in English and translated into 34 languages. Of the 49 countries and four benchmarking participants, 17 collected data in two languages and one country, Egypt, in three languages - Arabic, English, and French. In addition to translation, it sometimes was necessary to modify the international versions for cultural reasons, even in the countries that tested wholly or partly in English. This process represented an enormous effort for the national centers, with many checks along the way. The translation effort included (1) developing explicit guidelines for translation and cultural adaptation; (2) translation of the instruments by the national centers in accordance with the guidelines, using two or more independent translations; (3) consultation with subject-matter experts on cultural adaptations to ensure that the meaning and difficulty of items did not change; (4) verification of translation quality by professional translators from an independent translation company; (5) corrections by the national centers in accordance with the suggestions made; (6) verification by the International Study Center that corrections were made; and (7) a series of statistical checks after the testing to detect items that did not perform comparably across countries. ${ }^{5}$

## Population Definition and Sampling

Since it is a curriculum-based study, TIMSS 2003 had as its intended target population all students at the end of their eighth and fourth years of formal schooling in the participating countries. However, for comparability with previous TIMSS assessments, the formal definition for the eighth grade specified all students enrolled in the upper of the two adjacent grades that contained the largest proportion of 13 -yearold students at the time of testing, and for fourth grade, all students enrolled in the upper of the two adjacent grades that contained the largest proportion of 9-year-olds. These correspond to the eighth and fourth grades in practically every country. ${ }^{6}$

The selection of valid and efficient samples is crucial to the quality and success of an international comparative study such as TIMSS. The accuracy of the survey results depends on the quality of sampling information and that of the sampling activities themselves. For TIMSS, NRCs worked on all phases of sampling with the TIMSS sampling experts from Statistics Canada and the IEA Data Processing Center (DPC). NRCs received training in how to select the school and student samples and in the use of the sampling software. In consultation with the TIMSS sampling referee (Keith Rust, Westat, Inc.), the TIMSS sampling experts reviewed the national sampling plans, sampling data, sampling frames, and sample execution. The sampling documentation was used by the TIMSS \& PIRLS International Study Center, in consultation with the sampling experts and the sampling referee, to evaluate the quality of the samples.

In a few situations where it was not possible to test the entire internationally desired population (all students enrolled in the upper of the two adjacent grades that contained the largest proportion of 13-year-old or 9 -year-old students at the time of testing), countries were permitted to define a national desired population that excluded part of the internationally desired population. Exhibit A. 6 shows any differences in coverage between the international and national desired

6 The sample design for TIMSS is described in detail in Foy, P., and Joncas, M. (2004), "TIMSS 2003 Sampling Design" in M.O. Martin, I.V.S. Mullis and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.
populations for eighth and fourth grades. Almost all participants at the eighth grade achieved 100 percent coverage ( 47 out of 51 ), with Indonesia, Lithuania, Morocco, and Serbia the exceptions. Consequently, the results for these countries are annotated in exhibits in this report. At fourth grade, only Lithuania of the 29 participants had less than 100 percent coverage.

Within the desired population, countries could define a population that excluded a small percentage (less than 5\%) of certain kinds of schools or students that would be very difficult or resource-intensive to test (e.g., schools for students with special needs or schools that were very small or located in extremely rural areas). Countries excluding more than 10 percent of their population are annotated in the exhibits in this report. Exhibit A. 6 shows that only three countries exceeded the 10 percent limit at eighth grade (Israel, Macedonia, and Syria) and no fourth-grade participant did so.

Within countries, TIMSS used a two-stage sample design, in which the first stage involved selecting about 150 public and private schools in each country. Within each school, countries were to use random procedures to select one eighth-grade mathematics class (for eighth-grade participants) and one fourth-grade classroom (fourthgrade participants). All of the students in the sampled class were to participate in the TIMSS testing. This approach was designed to yield a representative sample of at least 4,000 students per country at each grade level. Typically, between 1,200 and 2,000 students responded to each achievement item in each country, depending on the booklets in which the items appeared.

Exhibits A. 7 and A. 8 present achieved sample sizes for schools and students, respectively, for participating countries. Exhibit A. 9 shows the participation rates for schools, students, and overall, both with and without the use of replacement schools. Most countries achieved the minimum acceptable participation rates -85 percent of both the schools and students, or a combined rate (the product of school and student participation) of 75 percent - although Hong Kong SAR,
the Netherlands, and Scotland did so only after including replacement schools. The United States and Morocco had overall participation rates after including replacement schools of just below 75 percent ( $73 \%$ and $71 \%$, respectively), and were annotated accordingly. Despite extraordinary efforts to secure full participation, England's participation fell below the minimum requirement of 50 percent, and so their results were annotated and placed below a line in exhibits showing achievement. Because of scheduling difficulties, Korea was unable to test its eighth-grade students in May 2003 as planned. Instead, the students were tested in September 2003, when they had moved into the ninth grade. The results for Korea are annotated accordingly in exhibits in this report. At fourth grade, all participants achieved the minimum acceptable participation rates, although Australia, England, Hong Kong SAR, the Netherlands, Scotland, and the United States did so only after including replacement schools.

Whereas countries achieved a high degree of compliance with sampling guidelines in 2003, occasionally countries' data were omitted from exhibits dealing with trends from earlier assessments because of comparability issues. Because of differences in population coverage, 1999 eighth-grade data for Australia, Morocco, and Slovenia and fourth-grade data for Italy are not shown in this report. Israel, Italy, and South Africa, experienced difficulties with sampling at the classroom level in 1995; consequently their eighth-grade data from that assessment are not shown in this report.

## Exhibit A.6: Coverage of TIMSS 2003 Target Population



| Countries | International Desired Population |  | National Desired Population |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coverage | Notes on Coverage | School-Level Exclusions | Within-Sample Exclusions | Overall Exclusions |
| Armenia | 100\% |  | 2.9\% | 0.0\% | 2.9\% |
| Australia | 100\% |  | 0.4\% | 0.9\% | 1.3\% |
| Bahrain | 100\% |  | 0.0\% | 0.0\% | 0.0\% |
| Belgium (Flemish) | 100\% |  | 3.1\% | 0.1\% | 3.2\% |
| Botswana | 100\% |  | 0.8\% | 2.2\% | 3.0\% |
| Bulgaria | 100\% |  | 0.5\% | 0.0\% | 0.5\% |
| Chile | 100\% |  | 1.6\% | 0.7\% | 2.2\% |
| Chinese Taipei | 100\% |  | 0.2\% | 4.6\% | 4.8\% |
| Cyprus | 100\% |  | 1.1\% | 1.5\% | 2.5\% |
| Egypt | 100\% |  | 3.4\% | 0.0\% | 3.4\% |
| England | 100\% |  | 2.1\% | 0.0\% | 2.1\% |
| Estonia | 100\% |  | 2.6\% | 0.8\% | 3.4\% |
| Ghana | 100\% |  | 0.9\% | 0.0\% | 0.9\% |
| Hong Kong, SAR | 100\% |  | 3.3\% | 0.1\% | 3.4\% |
| Hungary | 100\% |  | 5.5\% | 3.2\% | 8.5\% |
| Indonesia | 80\% | Non-Islamic schools | 0.1\% | 0.3\% | 0.4\% |
| Iran, Islamic Rep. of | 100\% |  | 5.5\% | 1.1\% | 6.5\% |
| Israel | 100\% |  | 15.2\% | 8.6\% | 22.5\% |
| Italy | 100\% |  | 0.0\% | 3.6\% | 3.6\% |
| Japan | 100\% |  | 0.5\% | 0.1\% | 0.6\% |
| Jordan | 100\% |  | 0.5\% | 0.8\% | 1.3\% |
| Korea, Rep. of | 100\% |  | 1.5\% | 3.4\% | 4.9\% |
| Latvia | 100\% |  | 3.6\% | 0.1\% | 3.7\% |
| Lebanon | 100\% |  | 1.4\% | 0.0\% | 1.4\% |
| Lithuania | 89\% | Students taught in Lithuanian | 1.4\% | 1.2\% | 2.6\% |
| Macedonia, Rep. of | 100\% |  | 12.5\% | 0.0\% | 12.5\% |
| Malaysia | 100\% |  | 4.0\% | 0.0\% | 4.0\% |
| Moldova, Rep. of | 100\% |  | 0.7\% | 0.5\% | 1.2\% |
| Morocco | 69\% | All students but Souss Massa Draa, Casablanca, Gharb-Chrarda | 1.5\% | 0.0\% | 1.5\% |
| Netherlands | 100\% |  | 3.0\% | 0.0\% | 3.0\% |
| New Zealand | 100\% |  | 1.7\% | 2.7\% | 4.4\% |
| Norway | 100\% |  | 0.9\% | 1.5\% | 2.3\% |
| Palestinian Nat'l Auth. | 100\% |  | 0.2\% | 0.3\% | 0.5\% |
| Philippines | 100\% |  | 1.5\% | 0.0\% | 1.5\% |
| Romania | 100\% |  | 0.4\% | 0.1\% | 0.5\% |
| Russian Federation | 100\% |  | 1.7\% | 3.9\% | 5.5\% |
| Saudi Arabia | 100\% |  | 0.3\% | 0.2\% | 0.5\% |
| Scotland | 100\% |  | 0.0\% | 0.0\% | 0.0\% |
| Serbia | 81\% | Serbia without Kosovo | 2.4\% | 0.6\% | 2.9\% |
| Singapore | 100\% |  | 0.0\% | 0.0\% | 0.0\% |
| Slovak Republic | 100\% |  | 5.0\% | 0.0\% | 5.0\% |
| Slovenia | 100\% |  | 1.3\% | 0.1\% | 1.4\% |
| South Africa | 100\% |  | 0.6\% | 0.0\% | 0.6\% |
| Sweden | 100\% |  | 0.3\% | 2.5\% | 2.8\% |
| Syrian Arab Republic | 100\% |  | 18.7\% | 0.0\% | 18.8\% |
| Tunisia | 100\% |  | 1.8\% | 0.0\% | 1.8\% |
| United States | 100\% |  | 0.0\% | 4.9\% | 4.9\% |
| Benchmarking Participants |  |  |  |  |  |
| Basque Region, Spain | 100\% |  | 2.1\% | 3.8\% | 5.8\% |
| Indiana State, US | 100\% |  | 0.0\% | 7.8\% | 7.8\% |
| Ontario Province, Can. | 100\% |  | 1.0\% | 5.0\% | 6.0\% |
| Quebec Province, Can. | 100\% |  | 1.4\% | 3.5\% | 4.8\% |


| Countries | International Desired Population |  | National Desired Population |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coverage | Notes on Coverage | School-Level Exclusions | Within-Sample Exclusions | Overall Exclusions |
| Armenia | 100\% |  | 2.9\% | 0.0\% | 2.9\% |
| Australia | 100\% |  | 1.2\% | 1.6\% | 2.7\% |
| Belgium (Flemish) | 100\% |  | 5.9\% | 0.4\% | 6.3\% |
| Chinese Taipei | 100\% |  | 0.3\% | 2.8\% | 3.1\% |
| Cyprus | 100\% |  | 1.5\% | 1.4\% | 2.9\% |
| England | 100\% |  | 1.9\% | 0.0\% | 1.9\% |
| Hong Kong, SAR | 100\% |  | 3.7\% | 0.1\% | 3.8\% |
| Hungary | 100\% |  | 4.4\% | 3.9\% | 8.1\% |
| Iran, Islamic Rep. of | 100\% |  | 3.6\% | 2.1\% | 5.7\% |
| Italy | 100\% |  | 0.1\% | 4.1\% | 4.2\% |
| Japan | 100\% |  | 0.4\% | 0.3\% | 0.8\% |
| Latvia | 100\% |  | 4.3\% | 0.1\% | 4.4\% |
| Lithuania | 92\% | Students taught in Lithuanian | 2.1\% | 2.6\% | 4.6\% |
| Moldova, Rep. of | 100\% |  | 2.0\% | 1.6\% | 3.6\% |
| Morocco | 100\% |  | 2.2\% | 0.0\% | 2.2\% |
| Netherlands | 100\% |  | 4.1\% | 1.1\% | 5.2\% |
| New Zealand | 100\% |  | 1.5\% | 2.5\% | 4.0\% |
| Norway | 100\% |  | 1.7\% | 2.7\% | 4.4\% |
| Philippines | 100\% |  | 3.8\% | 0.7\% | 4.5\% |
| Russian Federation | 100\% |  | 2.2\% | 4.7\% | 6.8\% |
| Scotland | 100\% |  | 1.5\% | 0.0\% | 1.5\% |
| Singapore | 100\% |  | 0.0\% | 0.0\% | 0.0\% |
| Slovenia | 100\% |  | 0.8\% | 0.5\% | 1.3\% |
| Tunisia | 100\% |  | 0.9\% | 0.0\% | 0.9\% |
| United States | 100\% |  | 0.0\% | 5.1\% | 5.1\% |
| Yemen | 100\% |  | 0.6\% | 8.9\% | 9.5\% |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US | 100\% |  | 0.0\% | 7.2\% | 7.2\% |
| Ontario Province, Can. | 100\% |  | 1.3\% | 3.5\% | 4.8\% |
| Quebec Province, Can. | 100\% |  | 2.7\% | 0.9\% | 3.6\% |

## Exhibit A.7: School Sample Sizes



| Countries | Number of Schools in Original Sample | Number of Eligible Schools in Original Sample | Number of Schools in Original Sample that Participated | Number of Replacement Schools that Participated | Total Number of Schools that Participated |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | 150 | 150 | 149 | 0 | 149 |
| Australia | 230 | 226 | 186 | 21 | 207 |
| Bahrain | 67 | 67 | 67 | 0 | 67 |
| Belgium (Flemish) | 150 | 150 | 122 | 26 | 148 |
| Botswana | 152 | 150 | 146 | 0 | 146 |
| Bulgaria | 170 | 169 | 163 | 1 | 164 |
| Chile | 195 | 195 | 191 | 4 | 195 |
| Chinese Taipei | 150 | 150 | 150 | 0 | 150 |
| Cyprus | 59 | 59 | 59 | 0 | 59 |
| Egypt | 217 | 217 | 215 | 2 | 217 |
| England | 160 | 160 | 62 | 25 | 87 |
| Estonia | 154 | 152 | 151 | 0 | 151 |
| Ghana | 150 | 150 | 150 | 0 | 150 |
| Hong Kong, SAR | 150 | 150 | 112 | 13 | 125 |
| Hungary | 160 | 157 | 154 | 1 | 155 |
| Indonesia | 150 | 150 | 148 | 2 | 150 |
| Iran, Islamic Rep. of | 188 | 181 | 181 | 0 | 181 |
| Israel | 150 | 147 | 143 | 3 | 146 |
| Italy | 172 | 171 | 164 | 7 | 171 |
| Japan | 150 | 150 | 146 | 0 | 146 |
| Jordan | 150 | 140 | 140 | 0 | 140 |
| Korea, Rep. of | 151 | 150 | 149 | 0 | 149 |
| Latvia | 150 | 149 | 137 | 3 | 140 |
| Lebanon | 160 | 160 | 148 | 4 | 152 |
| Lithuania | 150 | 150 | 137 | 6 | 143 |
| Macedonia, Rep. of | 150 | 150 | 142 | 7 | 149 |
| Malaysia | 150 | 150 | 150 | 0 | 150 |
| Moldova, Rep. of | 150 | 149 | 147 | 2 | 149 |
| Morocco | 227 | 165 | 131 | 0 | 131 |
| Netherlands | 150 | 150 | 118 | 12 | 130 |
| New Zealand | 175 | 174 | 149 | 20 | 169 |
| Norway | 150 | 150 | 138 | 0 | 138 |
| Palestinian Nat'l Auth. | 150 | 145 | 145 | 0 | 145 |
| Philippines | 160 | 160 | 132 | 5 | 137 |
| Romania | 150 | 149 | 148 | 0 | 148 |
| Russian Federation | 216 | 216 | 214 | 0 | 214 |
| Saudi Arabia | 160 | 160 | 154 | 1 | 155 |
| Scotland | 150 | 150 | 115 | 13 | 128 |
| Serbia | 150 | 150 | 149 | 0 | 149 |
| Singapore | 164 | 164 | 164 | 0 | 164 |
| Slovak Republic | 180 | 179 | 170 | 9 | 179 |
| Slovenia | 177 | 177 | 169 | 5 | 174 |
| South Africa | 265 | 265 | 241 | 14 | 255 |
| Sweden | 160 | 160 | 155 | 4 | 159 |
| Syrian Arab Republic | 150 | 150 | 121 | 13 | 134 |
| Tunisia | 150 | 150 | 150 | 0 | 150 |
| United States | 301 | 296 | 211 | 21 | 232 |
| Benchmarking Participants |  |  |  |  |  |
| Basque Region, Spain | 120 | 120 | 119 | 1 | 120 |
| Indiana State, US | 56 | 56 | 54 | 0 | 54 |
| Ontario Province, Can. | 200 | 196 | 171 | 15 | 186 |
| Quebec Province, Can. | 199 | 185 | 173 | 2 | 175 |


| Countries | Number of Schools in Original Sample | Number of Eligible Schools in Original Sample | Number of Schools in Original Sample that Participated | ```Number of Replacement Schools that Participated``` | Total Number of Schools that Participated |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | 150 | 150 | 148 | 0 | 148 |
| Australia | 230 | 227 | 178 | 26 | 204 |
| Belgium (Flemish) | 150 | 150 | 133 | 16 | 149 |
| Chinese Taipei | 150 | 150 | 150 | 0 | 150 |
| Cyprus | 150 | 150 | 150 | 0 | 150 |
| England | 150 | 150 | 79 | 44 | 123 |
| Hong Kong, SAR | 150 | 150 | 116 | 16 | 132 |
| Hungary | 160 | 159 | 156 | 1 | 157 |
| Iran, Islamic Rep. of | 176 | 171 | 171 | 0 | 171 |
| Italy | 172 | 171 | 165 | 6 | 171 |
| Japan | 150 | 150 | 150 | 0 | 150 |
| Latvia | 150 | 149 | 137 | 3 | 140 |
| Lithuania | 160 | 160 | 147 | 6 | 153 |
| Moldova, Rep. of | 153 | 151 | 147 | 4 | 151 |
| Morocco | 227 | 225 | 197 | 0 | 197 |
| Netherlands | 150 | 149 | 77 | 53 | 130 |
| New Zealand | 228 | 228 | 194 | 26 | 220 |
| Norway | 150 | 150 | 134 | 5 | 139 |
| Philippines | 160 | 160 | 122 | 13 | 135 |
| Russian Federation | 206 | 205 | 204 | 1 | 205 |
| Scotland | 150 | 150 | 94 | 31 | 125 |
| Singapore | 182 | 182 | 182 | 0 | 182 |
| Slovenia | 177 | 177 | 169 | 5 | 174 |
| Tunisia | 150 | 150 | 150 | 0 | 150 |
| United States | 310 | 300 | 212 | 36 | 248 |
| Yemen | 150 | 150 | 150 | 0 | 150 |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US | 56 | 56 | 56 | 0 | 56 |
| Ontario Province, Can. | 200 | 196 | 179 | 10 | 189 |
| Quebec Province, Can. | 198 | 194 | 192 | 1 | 193 |

Exhibit A.8: Student Sample Sizes


| Countries | Within-School Student Participation (Weighted Percentage) | Number of Sampled Students in Participating Schools | Number of Students Withdrawn from Class/School | Number of Students Excluded | Number of Eligible Students | Number of Students Absent | Number of Students Assessed |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | 90\% | 6388 | 56 | 0 | 6332 | 606 | 5726 |
| Australia | 93\% | 5286 | 60 | 16 | 5210 | 419 | 4791 |
| Bahrain | 98\% | 4351 | 64 | 0 | 4287 | 88 | 4199 |
| Belgium (Flemish) | 97\% | 5161 | 19 | 7 | 5135 | 165 | 4970 |
| Botswana | 98\% | 5388 | 70 | 70 | 5248 | 98 | 5150 |
| Bulgaria | 96\% | 4489 | 167 | 0 | 4322 | 205 | 4117 |
| Chile | 99\% | 6528 | 15 | 39 | 6474 | 97 | 6377 |
| Chinese Taipei | 99\% | 5525 | 54 | 37 | 5434 | 55 | 5379 |
| Cyprus | 96\% | 4314 | 79 | 66 | 4169 | 167 | 4002 |
| Egypt | 97\% | 7259 | 0 | 0 | 7259 | 164 | 7095 |
| England | 86\% | 3360 | 34 | 0 | 3326 | 496 | 2830 |
| Estonia | 96\% | 4242 | 28 | 5 | 4209 | 169 | 4040 |
| Ghana | 93\% | 5690 | 189 | 0 | 5501 | 401 | 5100 |
| Hong Kong, SAR | 97\% | 5204 | 33 | 4 | 5167 | 195 | 4972 |
| Hungary | 95\% | 3506 | 7 | 34 | 3465 | 163 | 3302 |
| Indonesia | 99\% | 5884 | 61 | 0 | 5823 | 61 | 5762 |
| Iran, Islamic Rep. of | 98\% | 5215 | 118 | 52 | 5045 | 103 | 4942 |
| Israel | 95\% | 4880 | 2 | 319 | 4559 | 241 | 4318 |
| Italy | 97\% | 4628 | 35 | 173 | 4420 | 142 | 4278 |
| Japan | 96\% | 5121 | 51 | 5 | 5065 | 209 | 4856 |
| Jordan | 96\% | 4871 | 176 | 41 | 4654 | 165 | 4489 |
| Korea, Rep. of | 99\% | 5451 | 18 | 50 | 5383 | 74 | 5309 |
| Latvia | 89\% | 4146 | 23 | 5 | 4118 | 488 | 3630 |
| Lebanon | 96\% | 4030 | 64 | 0 | 3966 | 152 | 3814 |
| Lithuania | 89\% | 6619 | 58 | 955 | 5606 | 642 | 4964 |
| Macedonia, Rep. of | 97\% | 4028 | 0 | 0 | 4028 | 135 | 3893 |
| Malaysia | 98\% | 5464 | 46 | 0 | 5418 | 104 | 5314 |
| Moldova, Rep. of | 96\% | 4262 | 58 | 0 | 4204 | 171 | 4033 |
| Morocco | 91\% | 3243 | 25 | 0 | 3218 | 275 | 2943 |
| Netherlands | 94\% | 3283 | 2 | 0 | 3281 | 216 | 3065 |
| New Zealand | 93\% | 4343 | 170 | 65 | 4108 | 307 | 3801 |
| Norway | 92\% | 4569 | 24 | 61 | 4484 | 351 | 4133 |
| Palestinian Nat'l Auth. | 99\% | 5543 | 117 | 14 | 5412 | 55 | 5357 |
| Philippines | 96\% | 7498 | 288 | 0 | 7210 | 293 | 6917 |
| Romania | 98\% | 4249 | 53 | 4 | 4192 | 88 | 4104 |
| Russian Federation | 97\% | 4926 | 50 | 62 | 4814 | 147 | 4667 |
| Saudi Arabia | 97\% | 4553 | 115 | 5 | 4433 | 138 | 4295 |
| Scotland | 89\% | 3962 | 24 | 0 | 3938 | 422 | 3516 |
| Serbia | 96\% | 4514 | 52 | 2 | 4460 | 164 | 4296 |
| Singapore | 97\% | 6236 | 5 | 0 | 6231 | 213 | 6018 |
| Slovak Republic | 95\% | 4428 | 16 | 0 | 4412 | 197 | 4215 |
| Slovenia | 93\% | 3883 | 19 | 2 | 3862 | 284 | 3578 |
| South Africa | 92\% | 9905 | 320 | 0 | 9585 | 633 | 8952 |
| Sweden | 89\% | 4941 | 58 | 93 | 4790 | 534 | 4256 |
| Syrian Arab Republic | 98\% | 5001 | 0 | 1 | 5000 | 105 | 4895 |
| Tunisia | 98\% | 5106 | 74 | 0 | 5032 | 101 | 4931 |
| United States | 94\% | 9891 | 90 | 279 | 9522 | 610 | 8912 |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Basque Region, Spain | 98\% | 2736 | 41 | 113 | 2582 | 68 | 2514 |
| Indiana State, US | 97\% | 2402 | 43 | 107 | 2252 | 64 | 2188 |
| Ontario Province, Can. | 95\% | 4693 | 59 | 208 | 4426 | 209 | 4217 |
| Quebec Province, Can. | 92\% | 4919 | 78 | 46 | 4795 | 384 | 4411 |

## Exhibit A.8: Student Sample Sizes

| Countries | Within-School Student Participation (Weighted Percentage) | Number of Sampled Students in Participating Schools | Number of Students Withdrawn from <br> Class/School | Number of Students Excluded | Number of Eligible Students | Number of Students Absent | Number of Students Assessed |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | 91\% | 6275 | 57 | 0 | 6218 | 544 | 5674 |
| Australia | 94\% | 4675 | 69 | 39 | 4567 | 246 | 4321 |
| Belgium (Flemish) | 98\% | 4866 | 17 | 20 | 4829 | 117 | 4712 |
| Chinese Taipei | 99\% | 4793 | 11 | 88 | 4694 | 33 | 4661 |
| Cyprus | 97\% | 4536 | 27 | 60 | 4449 | 121 | 4328 |
| England | 93\% | 3917 | 45 | 0 | 3872 | 287 | 3585 |
| Hong Kong, SAR | 95\% | 4901 | 23 | 4 | 4874 | 266 | 4608 |
| Hungary | 94\% | 3603 | 11 | 67 | 3525 | 206 | 3319 |
| Iran, Islamic Rep. of | 98\% | 4587 | 83 | 80 | 4424 | 72 | 4352 |
| Italy | 97\% | 4641 | 23 | 185 | 4433 | 151 | 4282 |
| Japan | 97\% | 4690 | 16 | 16 | 4658 | 123 | 4535 |
| Latvia | 94\% | 3980 | 16 | 4 | 3960 | 273 | 3687 |
| Lithuania | 92\% | 5701 | 35 | 852 | 4814 | 392 | 4422 |
| Moldova, Rep. of | 97\% | 4162 | 46 | 0 | 4116 | 135 | 3981 |
| Morocco | 93\% | 4546 | 0 | 0 | 4546 | 282 | 4264 |
| Netherlands | 96\% | 3080 | 0 | 30 | 3050 | 113 | 2937 |
| New Zealand | 95\% | 4785 | 145 | 107 | 4533 | 225 | 4308 |
| Norway | 95\% | 4706 | 22 | 107 | 4577 | 235 | 4342 |
| Philippines | 95\% | 5225 | 40 | 31 | 5154 | 582 | 4572 |
| Russian Federation | 97\% | 4229 | 54 | 66 | 4109 | 146 | 3963 |
| Scotland | 92\% | 4283 | 34 | 0 | 4249 | 313 | 3936 |
| Singapore | 98\% | 6851 | 16 | 0 | 6835 | 167 | 6668 |
| Slovenia | 92\% | 3410 | 13 | 17 | 3380 | 254 | 3126 |
| Tunisia | 99\% | 4408 | 23 | 0 | 4385 | 51 | 4334 |
| United States | 95\% | 10795 | 49 | 429 | 10317 | 488 | 9829 |
| Yemen | 93\% | 4550 | 0 | 0 | 4550 | 345 | 4205 |
| Benchmarking Participants |  |  |  |  |  |  |  |
| Indiana State, US | 98\% | 2472 | 44 | 151 | 2277 | 44 | 2233 |
| Ontario Province, Can. | 96\% | 4813 | 91 | 158 | 4564 | 202 | 4362 |
| Quebec Province, Can. | 91\% | 4864 | 51 | 73 | 4740 | 390 | 4350 |


| Countries | School Participation |  | Class <br> Participation | Student Participation | Overall Participation |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Before Replacement | After Replacement |  |  | Before Replacement | After Replacement |
| Armenia | 99\% | 99\% | 99\% | 90\% | 89\% | 89\% |
| Australia | 81\% | 90\% | 100\% | 93\% | 75\% | 83\% |
| Bahrain | 100\% | 100\% | 100\% | 98\% | 98\% | 98\% |
| Belgium (Flemish) | 82\% | 99\% | 98\% | 97\% | 77\% | 94\% |
| Botswana | 98\% | 98\% | 100\% | 98\% | 96\% | 96\% |
| Bulgaria | 97\% | 97\% | 99\% | 96\% | 92\% | 92\% |
| Chile | 98\% | 100\% | 100\% | 99\% | 97\% | 99\% |
| Chinese Taipei | 100\% | 100\% | 100\% | 99\% | 99\% | 99\% |
| Cyprus | 100\% | 100\% | 100\% | 96\% | 96\% | 96\% |
| Egypt | 99\% | 100\% | 100\% | 97\% | 97\% | 97\% |
| England | 40\% | 54\% | 99\% | 86\% | 34\% | 46\% |
| Estonia | 99\% | 99\% | 100\% | 96\% | 95\% | 95\% |
| Ghana | 100\% | 100\% | 100\% | 93\% | 93\% | 93\% |
| Hong Kong, SAR | 74\% | 83\% | 99\% | 97\% | 72\% | 80\% |
| Hungary | 98\% | 99\% | 100\% | 95\% | 94\% | 94\% |
| Indonesia | 98\% | 100\% | 100\% | 99\% | 97\% | 99\% |
| Iran, Islamic Rep. of | 100\% | 100\% | 100\% | 98\% | 98\% | 98\% |
| Israel | 98\% | 99\% | 100\% | 95\% | 93\% | 94\% |
| Italy | 96\% | 100\% | 100\% | 97\% | 93\% | 97\% |
| Japan | 97\% | 97\% | 100\% | 96\% | 93\% | 93\% |
| Jordan | 100\% | 100\% | 100\% | 96\% | 96\% | 96\% |
| Korea, Rep. of | 99\% | 99\% | 100\% | 99\% | 98\% | 98\% |
| Latvia | 92\% | 94\% | 100\% | 89\% | 81\% | 83\% |
| Lebanon | 93\% | 95\% | 100\% | 96\% | 89\% | 91\% |
| Lithuania | 92\% | 95\% | 100\% | 89\% | 81\% | 84\% |
| Macedonia, Rep. of | 94\% | 99\% | 100\% | 97\% | 91\% | 96\% |
| Malaysia | 100\% | 100\% | 100\% | 98\% | 98\% | 98\% |
| Moldova, Rep. of | 99\% | 100\% | 100\% | 96\% | 95\% | 96\% |
| Morocco | 79\% | 79\% | 100\% | 91\% | 71\% | 71\% |
| Netherlands | 79\% | 87\% | 100\% | 94\% | 74\% | 81\% |
| New Zealand | 86\% | 97\% | 100\% | 93\% | 80\% | 90\% |
| Norway | 92\% | 92\% | 100\% | 92\% | 85\% | 85\% |
| Palestinian Nat'l Auth. | 100\% | 100\% | 100\% | 99\% | 99\% | 99\% |
| Philippines | 81\% | 86\% | 100\% | 96\% | 78\% | 82\% |
| Romania | 99\% | 99\% | 100\% | 98\% | 98\% | 98\% |
| Russian Federation | 99\% | 99\% | 100\% | 97\% | 96\% | 96\% |
| Saudi Arabia | 95\% | 97\% | 100\% | 97\% | 93\% | 94\% |
| Scotland | 76\% | 85\% | 100\% | 89\% | 68\% | 76\% |
| Serbia | 99\% | 99\% | 100\% | 96\% | 96\% | 96\% |
| Singapore | 100\% | 100\% | 100\% | 97\% | 97\% | 97\% |
| Slovak Republic | 96\% | 100\% | 100\% | 95\% | 91\% | 95\% |
| Slovenia | 94\% | 99\% | 100\% | 93\% | 87\% | 91\% |
| South Africa | 89\% | 96\% | 100\% | 92\% | 82\% | 88\% |
| Sweden | 97\% | 99\% | 99\% | 89\% | 85\% | 87\% |
| Syrian Arab Republic | 81\% | 89\% | 100\% | 98\% | 79\% | 87\% |
| Tunisia | 100\% | 100\% | 100\% | 98\% | 98\% | 98\% |
| United States | 71\% | 78\% | 99\% | 94\% | 66\% | 73\% |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Region, Spain | 100\% | 100\% | 100\% | 98\% | 97\% | 98\% |
| Indiana State, US | 97\% | 97\% | 100\% | 97\% | 94\% | 94\% |
| Ontario Province, Can. | 84\% | 93\% | 100\% | 95\% | 80\% | 89\% |
| Quebec Province, Can. | 91\% | 93\% | 100\% | 92\% | 84\% | 85\% |

матнееатtics Grade

Countries


Class
Participation

## Australia

 Belgium (Flemish)Chinese Taipei
Cyprus
England
Hong Kong
Iran, Islamic Rep. of
$+$

| Japan |
| :--- |
| Latvia |

Lith

| Morocco |
| :--- |
| Netherlands |

New


| Russian Federation |
| :--- | :--- |
| Scotland |


| Singapore |
| :---: |
| Slovenia |


| Tunisia | $100 \%$ | 100 |
| :--- | ---: | ---: |
| United States | $70 \%$ | 82 |
| Yemen | $100 \%$ | 100 |

Benchmarking Participants

| Indiana State, US | $100 \%$ | $100 \%$ | $100 \%$ | $98 \%$ | $98 \%$ | $98 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Ontario Province, Can. | $89 \%$ | $94 \%$ | $100 \%$ | $96 \%$ | $85 \%$ | $90 \%$ |
| Quebec Province, Can. | $99 \%$ | $100 \%$ | $100 \%$ | $91 \%$ | $90 \%$ | $91 \%$ |

## Data Collection

Each participating country was responsible for carrying out all aspects of the data collection, using standardized procedures developed for the study. Training manuals were created for school coordinators and test administrators that explained procedures for receipt and distribution of materials as well as for the activities related to the testing sessions. These manuals covered procedures for test security, standardized scripts to regulate directions and timing, rules for answering students' questions, and steps to ensure that identification on the test booklets and questionnaires corresponded to the information on the forms used to track students. ${ }^{7}$

Each country was responsible for conducting quality control procedures and describing this effort in the NRC's report documenting procedures used in the study. In addition, the TIMSS \& PIRLS International Study Center considered it essential to monitor compliance with standardized procedures. NRCs were asked to nominate one or more persons unconnected with their national center to serve as quality control monitors for their countries. The International Study Center developed manuals for the monitors and briefed them in two-day training sessions about TIMSS, the responsibilities of the national centers in conducting the study, and their roles and responsibilities.

In all, 50 quality control monitors drawn from the 49 countries and four benchmarking participants participated in the training. ${ }^{8}$ Where necessary, quality control monitors who attended the training session were permitted to recruit other monitors to assist them in covering the territory and meeting the testing timetable. All together, the international quality control monitors and those trained by them observed 1,147 testing sessions ( 755 for grade 8 and 392 for grade 4), ${ }^{9}$ and conducted interviews with the National Research Coordinator in each of the participating countries. ${ }^{10}$

The results of the interviews indicate that, in general, NRCs had prepared well for data collection and, despite the heavy demands

7 Data collection procedures for TIMSS is described in detail in Barth, J., Gonzalez, E.J., and Neuschmidt, O. (2004), "TIMSS 2003 Survey Operations Procedures" in M.O. Martin, I.V.S. Mullis and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.

8 Iran and Israel were the only countries whose quality control monitors were not trained; Ontario and Quebec shared the same quality control monitor.

9 Operational constraints prevented quality control monitor visits in five testing sessions in Japan.
10 Steps taken to ensure high-quality data collection in TIMSS are described in detail in Gonzalez, E.J. and Diaconu, D. (2004), "Quality Assurance in the TIMSS 2003 Data Collection" in M.O. Martin, I.V.S. Mullis, and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.
of the schedule and shortages of resources, were able to conduct the data collection efficiently and professionally. Similarly, the TIMSS tests appeared to have been administered in compliance with international procedures, including the activities before the testing session, those during testing, and the school-level activities related to receiving, distributing, and returning material from the national centers.

## Scoring the Constructed-Response Items

Because 40 to 50 percent of the test time was devoted to constructedresponse items, TIMSS needed to develop procedures for reliably evaluating student responses within and across countries. Scoring used two-digit codes with rubrics specific to each item. The first digit designates the correctness level of the response. The second digit, combined with the first, represents a diagnostic code identifying specific types of approaches, strategies, or common errors and misconceptions. Although not used in this report, analyses of responses based on the second digit should provide insight into ways to help students better understand mathematics concepts and problem-solving approaches.

To ensure reliable scoring procedures based on the TIMSS rubrics, the International Study Center prepared detailed guides containing the rubrics and explanations of how to implement them, together with example student responses for the various rubric categories. These guides, along with training packets containing extensive examples of student responses for practice in applying the rubrics, were used as a basis for intensive training in scoring the constructed-response items. The training sessions were designed to help representatives of national centers who would then be responsible for training personnel in their countries to apply the two-digit codes reliably.

To gather and document empirical information about the withincountry agreement among scorers, TIMSS arranged to have systematic samples of at least 100 student responses to each item scored independently by two readers. Exhibit A. 10 shows the average and range of

## Exhibit A.10: TIMSS 2003 Within-Country Scoring Reliability for the Constructed-Response

 Mathematics Items

| Countries | Correctness Score Agreement |  |  | Diagnostic Score Agreement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  |
|  |  | Min | Max |  | Min | Max |
| Armenia | 99 | 94 | 100 | 98 | 92 | 100 |
| Australia | 100 | 97 | 100 | 99 | 95 | 100 |
| Bahrain | 99 | 98 | 100 | 98 | 91 | 100 |
| Belgium (Flemish) | 99 | 96 | 100 | 98 | 91 | 100 |
| Botswana | 99 | 91 | 100 | 94 | 81 | 100 |
| Bulgaria | 96 | 70 | 100 | 92 | 64 | 99 |
| Chile | 99 | 95 | 100 | 97 | 91 | 100 |
| Chinese Taipei | 100 | 91 | 100 | 99 | 91 | 100 |
| Cyprus | 98 | 86 | 100 | 96 | 79 | 100 |
| Egypt | 100 | 97 | 100 | 99 | 97 | 100 |
| England | 99 | 93 | 100 | 98 | 91 | 100 |
| Estonia | 100 | 98 | 100 | 99 | 96 | 100 |
| Ghana | 99 | 97 | 100 | 95 | 90 | 99 |
| Hong Kong, SAR | 100 | 98 | 100 | 99 | 98 | 100 |
| Hungary | 98 | 90 | 100 | 96 | 80 | 100 |
| Indonesia | 98 | 90 | 100 | 94 | 82 | 100 |
| Iran, Islamic Rep. of | 99 | 94 | 100 | 96 | 90 | 100 |
| Israel | 98 | 93 | 100 | 93 | 83 | 99 |
| Italy | 99 | 95 | 100 | 98 | 92 | 100 |
| Japan | 99 | 94 | 100 | 98 | 91 | 100 |
| Jordan | 99 | 98 | 100 | 98 | 92 | 100 |
| Korea, Rep. of | 99 | 87 | 100 | 98 | 87 | 100 |
| Latvia | 98 | 90 | 100 | 96 | 79 | 100 |
| Lebanon | 100 | 94 | 100 | 99 | 91 | 100 |
| Lithuania | 97 | 71 | 100 | 95 | 62 | 100 |
| Macedonia, Rep. of | 100 | 97 | 100 | 99 | 95 | 100 |
| Malaysia | 100 | 98 | 100 | 99 | 97 | 100 |
| Moldova, Rep. of | 100 | 99 | 100 | 100 | 99 | 100 |
| Morocco | 97 | 89 | 100 | 92 | 82 | 99 |
| Netherlands | 97 | 84 | 100 | 95 | 78 | 100 |
| New Zealand | 99 | 96 | 100 | 97 | 88 | 100 |
| Norway | 98 | 91 | 100 | 96 | 86 | 100 |
| Palestinian Nat'l Auth. | 99 | 94 | 100 | 97 | 88 | 100 |
| Philippines | 99 | 97 | 100 | 97 | 92 | 100 |
| Romania | 100 | 98 | 100 | 99 | 94 | 100 |
| Russian Federation | 99 | 95 | 100 | 97 | 89 | 100 |
| Saudi Arabia | 99 | 94 | 100 | 95 | 81 | 99 |
| Scotland | 99 | 95 | 100 | 98 | 92 | 100 |
| Serbia | 99 | 96 | 100 | 98 | 94 | 100 |
| Singapore | 100 | 98 | 100 | 100 | 98 | 100 |
| Slovak Republic | 100 | 98 | 100 | 99 | 96 | 100 |
| Slovenia | 97 | 86 | 100 | 94 | 75 | 100 |
| South Africa | 99 | 95 | 100 | 97 | 90 | 99 |
| Sweden | 98 | 89 | 100 | 95 | 84 | 99 |
| Tunisia | 98 | 89 | 100 | 95 | 78 | 99 |
| United States | 97 | 86 | 100 | 94 | 75 | 99 |
| International Avg. | 99 | 92 | 100 | 97 | 87 | 100 |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 98 | 87 | 100 | 96 | 83 | 100 |
| Indiana State, US | 98 | 88 | 100 | 95 | 76 | 100 |
| Ontario Province, Can. | 97 | 80 | 100 | 93 | 72 | 100 |
| Quebec Province, Can. | 97 | 81 | 100 | 94 | 79 | 100 |

## Exhibit A.10: TIMSS 2003 Within-Country Scoring Reliability for the Constructed-Response

| Countries | Correctness Score Agreement |  |  | Diagnostic Score Agreement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  |
|  |  | Min | Max |  | Min | Max |
| Armenia | 99 | 98 | 100 | 98 | 95 | 100 |
| Australia | 100 | 98 | 100 | 99 | 97 | 100 |
| Belgium (Flemish) | 100 | 96 | 100 | 98 | 87 | 100 |
| Chinese Taipei | 99 | 83 | 100 | 97 | 76 | 100 |
| Cyprus | 98 | 91 | 100 | 95 | 82 | 100 |
| England | 99 | 91 | 100 | 98 | 90 | 100 |
| Hong Kong, SAR | 100 | 98 | 100 | 99 | 87 | 100 |
| Hungary | 98 | 91 | 100 | 95 | 78 | 100 |
| Iran, Islamic Rep. of | 100 | 98 | 100 | 99 | 96 | 100 |
| Italy | 98 | 92 | 100 | 96 | 81 | 100 |
| Japan | 99 | 95 | 100 | 98 | 94 | 100 |
| Latvia | 98 | 87 | 100 | 96 | 78 | 100 |
| Lithuania | 97 | 77 | 100 | 94 | 69 | 100 |
| Moldova, Rep. of | 100 | 100 | 100 | 100 | 100 | 100 |
| Morocco | 98 | 93 | 100 | 94 | 86 | 98 |
| Netherlands | 97 | 86 | 100 | 94 | 73 | 100 |
| New Zealand | 99 | 94 | 100 | 96 | 85 | 100 |
| Norway | 99 | 95 | 100 | 97 | 92 | 100 |
| Philippines | 99 | 96 | 100 | 97 | 91 | 100 |
| Russian Federation | 100 | 97 | 100 | 99 | 96 | 100 |
| Scotland | 99 | 98 | 100 | 98 | 93 | 100 |
| Singapore | 100 | 99 | 100 | 100 | 99 | 100 |
| Slovenia | 98 | 84 | 100 | 96 | 73 | 100 |
| Tunisia | 97 | 89 | 100 | 91 | 77 | 98 |
| United States | 97 | 88 | 100 | 95 | 82 | 100 |
| International Avg. | 99 | 92 | 100 | 97 | 86 | 100 |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US | 99 | 92 | 100 | 96 | 83 | 100 |
| Ontario Province, Can. | 98 | 87 | 100 | 96 | 84 | 100 |
| Quebec Province, Can. | 98 | 92 | 100 | 96 | 86 | 100 |

## Exhibit A.11: TIMSS 2003 Trend Scoring Reliability (1999-2003) for the Constructed-Response Mathematics Items



| Countries | Correctness Score Agreement |  |  | Diagnostic Score Agreement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  | Average of Exact Percent Agreement Across Items | Range of Exact Percent Agreement |  |
|  |  | Min | Max |  | Min | Max |
| Australia | 98 | 88 | 100 | 94 | 73 | 100 |
| Belgium (Flemish) | 98 | 92 | 100 | 94 | 78 | 100 |
| Bulgaria | 99 | 82 | 100 | 94 | 71 | 100 |
| Chile | 99 | 97 | 100 | 92 | 73 | 100 |
| Chinese Taipei | 98 | 95 | 100 | 94 | 79 | 100 |
| Cyprus | 98 | 91 | 100 | 94 | 79 | 100 |
| Hong Kong, SAR | 98 | 91 | 100 | 96 | 84 | 100 |
| Hungary | 98 | 89 | 100 | 95 | 86 | 100 |
| Indonesia | 98 | 90 | 100 | 93 | 60 | 100 |
| Iran, Islamic Rep. | 98 | 83 | 100 | 89 | 24 | 99 |
| Israel | 98 | 91 | 100 | 92 | 74 | 100 |
| Italy | 99 | 91 | 100 | 97 | 86 | 100 |
| Japan | 98 | 87 | 100 | 96 | 76 | 100 |
| Jordan | 99 | 96 | 100 | 96 | 87 | 100 |
| Korea, Rep. of | 98 | 88 | 100 | 94 | 67 | 100 |
| Latvia | 90 | 34 | 100 | 78 | 32 | 100 |
| Lithuania | 98 | 93 | 100 | 94 | 74 | 100 |
| Macedonia, Rep. of | 99 | 85 | 100 | 96 | 70 | 100 |
| Malaysia | 99 | 91 | 100 | 95 | 84 | 100 |
| New Zealand | 99 | 96 | 100 | 94 | 85 | 100 |
| Philippines | 99 | 86 | 100 | 95 | 75 | 100 |
| Romania | 99 | 97 | 100 | 97 | 90 | 100 |
| Russian Federation | 98 | 94 | 100 | 92 | 62 | 100 |
| Singapore | 99 | 96 | 100 | 98 | 89 | 100 |
| Slovak Republic | 93 | 54 | 100 | 87 | 50 | 99 |
| Slovenia | 99 | 95 | 100 | 95 | 81 | 100 |
| South Africa | 99 | 92 | 100 | 93 | 47 | 100 |
| United States | 98 | 91 | 100 | 94 | 76 | 100 |
| International Avg. | 98 | 88 | 100 | 93 | 72 | 100 |
| Benchmarking Participants |  |  |  |  |  |  |
| Ontario Province, Can. | 98 | 85 | 100 | 93 | 65 | 100 |
| Quebec Province, Can. | 98 | 85 | 100 | 93 | 65 | 100 |

## Exhibit A.12: TIMSS 2003 Cross-Country Scoring Reliability for the Constructed-Response Mathematics Items


the within-country exact percent of agreement between scorers on the constructed-response items in the mathematics test for the TIMSS participants. The exhibit shows agreement for both the correctness score (the first digit) and for the two-digit diagnostic score. A high percentage of exact agreement was observed, with an overall average of 99 percent for correctness score and 97 percent for diagnostic score at both fourth and eighth grades. The TIMSS data from the reliability studies indicate that scoring procedures were robust for the mathematics items, especially for the correctness score used for the analyses in this report.

The double scoring of a sample of the student test booklets provided a measure of the consistency within each country with which constructed-response questions were scored. TIMSS 2003 also took steps to show that those constructed-response items from 1999 that were used in 2003 were scored in the same way in both assessments. In anticipation of this, countries that participated in TIMSS 1999 sent samples of scored student booklets from the 1999 eighth-grade data collection to the IEA Data Processing Center, where they were digitally scanned and stored in presentation software for later use. As a check on scoring consistency from 1999 to 2003, staff members working in each country on scoring the 2003 eighth-grade data were asked also to score these 1999 responses using the DPC software. The items from 1995 that were used in TIMSS 2003 all were in multiple-choice format, and therefore scoring reliability was not an issue. As shown in Exhibit A.11, there was a very high degree of scoring consistency, with 98 percent exact agreement, on average, internationally, between the scores awarded in 1999 and those given by the 2003 scorers. There also was very high agreement at the diagnostic score level, with 93 percent exact agreement, on average.

To monitor the consistency with which the scoring rubrics were applied across countries, TIMSS collected from the SouthernHemisphere countries that administered TIMSS in English a sample of 150 student responses to 20 constructed-response mathematics questions. This set of 3,000 student responses was then sent to each

Northern-Hemisphere country having scorers proficient in English and scored independently by one or, if possible, two of these scorers. Each of the responses was scored by 37 scorers from the countries that participated. Making all possible comparisons among scorers gave 666 comparisons for each student response to each item, and 99,900 total comparisons when aggregated across all 150 student responses to that item. Agreement across countries was defined in terms of the percentage of these comparisons that were in exact agreement. Exhibit A. 12 shows that scorer reliability across countries was very high, with the percent exact agreement ranging from 90 percent to 99 percent across the 20 items for the correctness score and from 84 to 99 percent for the diagnostic score.

## Test Reliability

Exhibit A. 13 displays the mathematics test reliability coefficient for each country. This coefficient is the median Cronbach's alpha reliability across the 12 test booklets. At both grade levels, median reliabilities generally were high, with an international median (the median of the reliability coefficients for all countries) of 0.89 for eighth grade and 0.87 for fourth grade. Despite the generally high reliabilities, there were some countries with median reliabilities below 0.80 , namely Botswana, Ghana, Morocco (both grades), Saudi Arabia, Syria, and Tunisia (both grades).

| Countries | Reliability Coefficient ${ }^{1}$ |  |
| :---: | :---: | :---: |
|  | Grade 8 | Grade 4 |
| Armenia | 0.87 | 0.87 |
| Australia | 0.90 | 0.88 |
| Bahrain | 0.82 |  |
| Belgium (Flemish) | 0.90 | 0.83 |
| Botswana | 0.71 |  |
| Bulgaria | 0.90 |  |
| Chile | 0.86 |  |
| Chinese Taipei | 0.94 | 0.85 |
| Cyprus | 0.89 | 0.89 |
| Egypt | 0.86 |  |
| England | 0.90 | 0.91 |
| Estonia | 0.90 |  |
| Ghana | 0.51 |  |
| Hong Kong, SAR | 0.91 | 0.83 |
| Hungary | 0.92 | 0.88 |
| Indonesia | 0.87 |  |
| Iran, Islamic Rep. of | 0.84 | 0.80 |
| Israel | 0.91 |  |
| Italy | 0.89 | 0.88 |
| Japan | 0.92 | 0.87 |
| Jordan | 0.87 |  |
| Korea, Rep. of | 0.93 |  |
| Latvia | 0.90 | 0.87 |
| Lebanon | 0.84 |  |
| Lithuania | 0.90 | 0.88 |
| Macedonia, Rep. of | 0.88 |  |
| Malaysia | 0.90 |  |
| Moldova, Rep. of | 0.87 | 0.90 |
| Morocco | 0.74 | 0.76 |
| Netherlands | 0.90 | 0.83 |
| New Zealand | 0.90 | 0.88 |
| Norway | 0.85 | 0.87 |
| Palestinian Nat'l Auth. | 0.83 |  |
| Philippines | 0.83 | 0.87 |
| Romania | 0.91 |  |
| Russian Federation | 0.90 | 0.88 |
| Saudi Arabia | 0.64 |  |
| Scotland | 0.90 | 0.88 |
| Serbia | 0.91 |  |
| Singapore | 0.92 | 0.91 |
| Slovak Republic | 0.91 |  |
| Slovenia | 0.88 | 0.87 |
| South Africa | 0.85 |  |
| Sweden | 0.89 |  |
| Syrian Arab Republic | 0.72 |  |
| Tunisia | 0.77 | 0.83 |
| United States | 0.90 | 0.88 |
| Yemen |  | 0.77 |
| International Median | 0.89 | 0.87 |
| Benchmarking Participants |  |  |
| Basque Country, Spain | 0.85 |  |
| Indiana State, US | 0.89 | 0.86 |
| Ontario Province, Can. | 0.89 | 0.87 |
| Quebec Province, Can. | 0.87 | 0.84 |

[^88]
## Data Processing

To ensure the availability of comparable, high-quality data for analysis, TIMSS took rigorous quality control steps to create the international database. ${ }^{11}$ TIMSS prepared manuals and software for countries to use in entering their data, so that the information would be in a standardized international format before being forwarded to the IEA Data Processing Center in Hamburg for creation of the international database. Upon arrival at the Data Processing Center, the data underwent an exhaustive cleaning process. This involved several iterative steps and procedures designed to identify, document, and correct deviations from the international instruments, file structures, and coding schemes. The process also emphasized consistency of information within national data sets and appropriate linking among the many student, teacher, and school data files.

Throughout the process, the TIMSS 2003 data were checked and double-checked by the IEA Data Processing Center, the International Study Center, and the national centers. The national centers were contacted regularly and given multiple opportunities to review the data for their countries. In conjunction with the IEA Data Processing Center, the International Study Center reviewed item statistics for each cognitive item in each country to identify poorly performing items. On the fourth-grade mathematics test, two items were deleted for all countries. In addition, 7 countries had one or more items deleted (in most cases, one or two). Usually the poor statistics (negative point-biserials for the key, large item-by-country interactions, and statistics indicating lack of fit with the model) were a result of translation, adaptation, or printing deviations. At eighth grade, no mathematics items were deleted for all countries, but 17 countries had one or more items deleted (mostly one or two). Because of a major booklet printing error, more than 40 mathematics items had to be deleted for Ghana, which may have contributed to its low Cronbach's alpha reliability.

## IRT Scaling and Data Analysis

The general approach to reporting the TIMSS achievement data was based primarily on item response theory (IRT) scaling methods. ${ }^{12}$ The mathematics results were summarized using a family of 2 -parameter and 3-parameter IRT models for dichotomously-scored items (right or wrong), and generalized partial credit models for items with 0 , 1 , or 2 available score points. The IRT scaling method produces a score by averaging the responses of each student to the items that he or she took in a way that takes into account the difficulty and discriminating power of each item. The methodology used in TIMSS includes refinements that enable reliable scores to be produced even though individual students responded to relatively small subsets of the total mathematics item pool. Achievement scales were produced for each of the five mathematics content areas (number, algebra, measurement, geometry, and data), as well as for mathematics overall.

The IRT methodology was preferred for developing comparable estimates of performance for all students, since students answered different test items depending upon which of the 12 test booklets they received. The IRT analysis provides a common scale on which performance can be compared across countries. In addition to providing a basis for estimating mean achievement, scale scores permit estimates of how students within countries vary and provide information on percentiles of performance.

As shown in Exhibit A.5, TIMSS has a complicated booklet design, with blocks of items appearing in different positions in different booklets. For example, the items in block Ml appear as the first block in Booklet 1, as the second block in Booklet 6, and as the third block in Booklet 12. This allows the booklets to be linked together efficiently, but also to monitor and counterbalance any position effect. In TIMSS 2003, the counterbalanced booklet design made it possible to detect an unexpectedly strong position effect in the data as the item statistics for each country were reviewed. More specifically, this position effect occurred
because some students in all countries did not reach all the items in the third block position, which was the end of the first half of each booklet before the break. The same effect was evident for the sixth block position, which was the last block in the booklets. The IRT scaling addressed this problem by treating items in the third and sixth block positions as if they were unique, even though they also appeared in other positions. For example, the mathematics items in block M1 from Booklet 1 (the first position) and from Booklet 6 (second position) were considered to be the same items for scaling and reporting purposes, but those in Booklet 12 (the third position) were scaled as items that were different and unique.

The TIMSS mathematics achievement scale was designed to provide a reliable measure of student achievement spanning 1995, 1999, and 2003. The metric of the scale was established originally with the 1995 assessment. When all countries participating in 1995 at the eighth grade are treated equally, the TIMSS scale average over those countries is 500 and the standard deviation is 100 . The same applies for the fourth-grade assessment. Since the countries varied in size, each country was weighted to contribute equally to the mean and standard deviation of the scale. The average and standard deviation of the scale scores are arbitrary and do not affect scale interpretation. To preserve the metric of the original 1995 scale, the 1999 eighth-grade assessment was scaled using students from the countries that participated in both 1995 and 1999. Then students from the countries that tested in 1999 but not 1995 were assigned scores on the basis of the scale.

At the eighth grade, TIMSS developed the 2003 scale in the same way as in 1999, preserving the metric first with students from countries that participated in both 1999 and 2003, ${ }^{13}$ and then assigning scores on the basis of the scale to students tested in 2003 but not the earlier assessment. At fourth grade, because there was no assessment in 1999, the 2003 and 1995 data were linked directly together using students from countries that participated in both assessments, and the students tested in 2003 but not 1995 were assigned scores on the basis of the scale.

13 Because the 1995 student data had already been linked to the 1999 student data, it was not necessary to include the 1995 data in the 19992003 calibration.

To allow more accurate estimation of summary statistics for student subpopulations, the TIMSS scaling made use of plausible-value technology, whereby five separate estimates of each student's score were generated on each scale, based on the student's responses to the items in the student's booklet and the student's background characteristics. The five score estimates are known as "plausible values," and the variability between them encapsulates the uncertainty inherent in the score estimation process.

In addition to the scales for mathematics overall, IRT scales also were created for each of the five mathematics content areas for the 2003 data. However, insufficient common items were used in 1995 and 1999 to establish reliable IRT content area scales for trend purposes. The trend exhibits presented in Chapter 3 were based on the average percentage of students responding correctly to the common items in each content area.

## Estimating Sampling Error

Because the statistics presented in this report are estimates of national performance based on samples of students, rather than the values that could be calculated if every student in every country had answered every question, it is important to have measures of the degree of uncertainty of the estimates. The jackknife procedure was used to estimate the standard error associated with each statistic presented in this report. ${ }^{14}$ The jackknife standard errors also include an error component due to variation among the five plausible values generated for each student. The use of confidence intervals, based on the standard errors, provides a way to make inferences about the population means and proportions in a manner that reflects the uncertainty associated with the sample estimates. An estimated sample statistic plus or minus two standard errors represents a 95 percent confidence interval for the corresponding population result.

## Assessing Statistical Significance

This report makes extensive use of statistical hypothesis-testing to provide a basis for evaluating the significance of differences in percentages and in average achievement scores. Each separate test follows the usual convention of holding to 0.05 the probability that reported differences could be due to sampling variability alone. There is one important difference in the way TIMSS 2003 reports significance tests compared with the practice in 1995 and 1999. In the previous assessments, significance tests in exhibits where the results of many tests are reported simultaneously were based on a Bonferroni procedure for multiple comparisons. The Bonferroni procedure was not used in TIMSS 2003. The procedure takes into account the number of comparisons being made, which is a function of the number of countries participating. Since this varies from assessment to assessment, the Bonferroni procedure makes it difficult to compare results from one assessment to the next. However, users of the reports should be aware that, following the logic of statistical hypothesis testing, on average, about five percent of statistical tests will be significant by chance alone.

## Setting International Benchmarks of Student Achievement

In order to provide meaningful descriptions of what performance on the TIMSS mathematics scale could mean in terms of the mathematics that students know and can do, TIMSS identified four points on the scale for use as international benchmarks. Selected to represent the range of performance shown by students internationally, the advanced benchmark is 625 , the high benchmark is 550 , the intermediate benchmark is 475 , and the low benchmark is 400 . Although the fourth- and eighth-grade scales are different, the same benchmark points are used at both grades.

In order to interpret the TIMSS scale scores and analyze achievement at the international benchmarks, TIMSS conducted a scale anchoring analysis to describe achievement of students at those four points on the scale. Scale anchoring is a way of describing students'
performance at different points on a scale in terms of what they know and can do. It involves a statistical component, in which items that discriminate between successive points on the scale are identified, and a judgmental component in which subject-matter experts examine the items and generalize to students' knowledge and understandings. ${ }^{15}$

## Calculator Use in the TIMSS 2003 Mathematics Assessment

Because calculators were permitted in TIMSS for the first time in the 2003 assessment at the eighth grade (not the fourth grade), TIMSS placed all the trend items in the first half of the test and only permitted eighth-grade students to use calculators for the second half. Nevertheless, capitalizing on the counterbalanced TIMSS booklet design, one block of mathematics items was included in both the testing session before the break, when calculators were not permitted, and in the session after the break, when they were allowed. This enabled a comparison of the mathematics achievement of those students having a calculator available and those that did not.

As shown in Exhibit A.14, calculator usage in the assessment was quite low. On average, internationally, 37 percent of students reported that they did not have a calculator for the test, and a further 47 percent that although they had them, they used them very little ( $39 \%$ ) or not at all ( $8 \%$ ). Most of the TIMSS mathematics items were designed so that they could be answered readily without the use of a calculator, and consequently having a calculator available may not be a great advantage. However, the Science and Mathematics Item Review Committee identified five items in the calculator block for which a calculator should be and was helpful, and Exhibit A. 14 presents for each country the average percent correct across these five calculator-sensitive items for students when they had a calculator and when they did not. On average, internationally, performance on the calculator-sensitive items was superior when students had calculators ( $66 \%$ correct with calculator vs $57 \%$ correct without a calculator). The difference was significant in almost every country where calculators were used. dards in an International Context, Chestnut Hill, MA: Boston College

Exhibit A.14: Students' Reports on the Frequency of Calculator Use During the TIMSS 2003 Test

| Countries | Percentage of Students Using a Calculator During the TIMSS Test |  |  |  |  | Average Percent Correct for the Five Calculator-Sensitive Items* |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Quite a Lot | Somewhat | Very Little | Not at All | Did Not Have a Calculator for the Test | With Calculator |  | Without Calculator |
| Armenia | 3 (0.4) | 4 (0.3) | 15 (1.0) | 2 (0.3) | 75 (1.3) | 57 (2.1) |  | 67 (1.3) |
| Australia | 2 (0.3) | 12 (1.0) | 46 (1.6) | 12 (0.7) | 28 (2.2) | 69 (1.7) | 0 | 53 (1.6) |
| Bahrain | 3 (0.3) | 8 (0.5) | 38 (0.9) | 14 (0.6) | 37 (1.1) | 45 (1.7) | 0 | 36 (1.2) |
| Belgium (Flemish) | 1 (0.2) | 16 (0.8) | 54 (1.3) | 11 (0.5) | 18 (1.6) | 82 (1.2) | 0 | 65 (1.3) |
| Botswana | 10 (0.6) | 17 (0.8) | 45 (1.0) | 22 (0.9) | 6 (0.9) | 57 (1.3) | 0 | 34 (0.9) |
| Bulgaria | 1 (0.2) | 5 (0.6) | 16 (1.3) | 4 (0.5) | 74 (1.8) | 64 (2.0) |  | 62 (1.6) |
| Chile | 1 (0.2) | 11 (0.8) | 44 (1.7) | 13 (0.6) | 31 (2.4) | 55 (1.6) | 0 | 39 (1.1) |
| Chinese Taipei | 0 (0.1) | 2 (0.3) | 12 (1.1) | 5 (0.5) | 80 (1.6) | 83 (1.3) |  | 83 (1.0) |
| Cyprus | 3 (0.4) | 10 (0.6) | 29 (0.8) | 5 (0.4) | 52 (1.0) | 60 (1.7) | 0 | 51 (1.0) |
| Egypt | 20 (0.9) | 36 (0.9) | 37 (0.9) | 4 (0.3) | 3 (0.3) | 56 (1.6) |  | 58 (1.1) |
| England | 1 (0.2) | 9 (0.8) | 48 (1.9) | 15 (1.1) | 27 (2.5) | 62 (1.9) | 0 | 44 (1.2) |
| Estonia | 1 (0.2) | 12 (0.8) | 57 (1.2) | 2 (0.3) | 27 (1.3) | 85 (1.0) | 0 | 73 (0.9) |
| Ghana | 10 (0.6) | 12 (0.8) | 15 (0.8) | 10 (0.7) | 54 (1.6) | 30 (1.7) | 0 | 26 (1.1) |
| Hong Kong, SAR | 2 (0.4) | 18 (1.0) | 51 (1.3) | 6 (0.5) | 23 (1.8) | 88 (1.0) | 0 | 81 (0.9) |
| Hungary | 1 (0.3) | 12 (0.9) | 60 (1.4) | 10 (0.6) | 17 (1.6) | 84 (1.1) | 0 | 75 (1.3) |
| Indonesia | 3 (0.3) | 10 (0.9) | 18 (1.5) | 1 (0.1) | 69 (2.3) | 57 (1.8) |  | 55 (1.5) |
| Iran, Islamic Rep. of | 2 (0.3) | 4 (0.4) | 11 (1.2) | 4 (0.5) | 79 (1.9) | 48 (1.6) |  | 48 (1.1) |
| Israel | 2 (0.3) | 15 (0.8) | 52 (1.4) | 13 (0.7) | 18 (1.4) | 74 (1.4) | 0 | 59 (1.4) |
| Italy | 1 (0.2) | 13 (0.8) | 49 (1.4) | 0 (0.1) | 36 (1.7) | 71 (1.4) | 0 | 60 (1.3) |
| Japan | 1 (0.1) | 12 (0.6) | 47 (1.3) | 22 (1.1) | 19 (2.0) | 85 (1.1) | 0 | 77 (0.9) |
| Jordan | 3 (0.3) | 7 (0.5) | 26 (1.6) | 7 (0.6) | 56 (2.0) | 50 (1.9) |  | 48 (1.5) |
| Korea, Rep. of | 0 (0.0) | 0 (0.1) | 5 (0.9) | 0 (0.0) | 95 (0.9) | 79 (1.0) |  | 81 (0.8) |
| Latvia | 1 (0.2) | 12 (0.9) | 43 (1.4) | 6 (0.6) | 38 (1.9) | 81 (1.4) | 0 | 67 (1.5) |
| Lebanon | 8 (0.8) | 18 (1.0) | 43 (1.2) | 15 (0.9) | 17 (1.1) | 70 (1.7) | 0 | 61 (1.4) |
| Lithuania | 2 (0.3) | 17 (0.8) | 49 (1.1) | 5 (0.5) | 26 (1.4) | 82 (1.2) | 0 | 67 (1.1) |
| Macedonia, Rep. of | 3 (0.4) | 13 (1.0) | 33 (1.3) | 8 (0.6) | 43 (2.1) | 61 (1.5) |  | 60 (1.4) |
| Malaysia | 2 (0.3) | 19 (0.8) | 47 (1.6) | 1 (0.2) | 31 (1.9) | 82 (0.9) | 0 | 73 (1.2) |
| Moldova, Rep. of | 1 (0.2) | 11 (0.9) | 39 (1.5) | 4 (0.5) | 45 (1.9) | 65 (1.9) |  | 65 (1.4) |
| Morocco | 1 (0.2) | 6 (0.6) | 19 (1.6) | 3 (0.5) | 71 (2.2) | 54 (2.0) | 0 | 48 (1.4) |
| Netherlands | 4 (0.4) | 25 (1.2) | 51 (1.2) | 0 (0.1) | 19 (1.3) | 80 (1.8) | 0 | 68 (1.4) |
| New Zealand | 2 (0.5) | 14 (0.7) | 49 (1.6) | 8 (0.6) | 27 (1.9) | 68 (1.9) | 0 | 50 (1.8) |
| Norway | 1 (0.1) | 7 (0.6) | 54 (1.3) | 18 (0.7) | 20 (1.5) | 59 (1.4) | 0 | 40 (1.1) |
| Palestinian Nat'l Auth. | 6 (0.4) | 13 (0.6) | 46 (1.2) | 11 (0.6) | 24 (1.5) | 48 (1.7) | 0 | 41 (1.2) |
| Philippines | 7 (0.6) | 12 (0.7) | 19 (1.1) | 8 (0.7) | 54 (1.9) | 51 (1.5) |  | 48 (1.6) |
| Romania | 2 (0.3) | 9 (0.6) | 31 (1.6) | 5 (0.5) | 53 (2.2) | 69 (2.1) | 0 | 62 (1.8) |
| Russian Federation | 1 (0.2) | 15 (0.8) | 49 (1.3) | 6 (0.6) | 29 (1.3) | 83 (1.1) | 0 | 72 (1.3) |
| Saudi Arabia | 4 (0.4) | 11 (0.7) | 48 (1.9) | 2 (0.4) | 35 (1.9) | 29 (1.7) | 0 | 21 (1.2) |
| Scotland | 1 (0.2) | 7 (0.5) | 55 (2.0) | 17 (1.0) | 19 (2.2) | 65 (1.6) | 0 | 48 (1.1) |
| Serbia | 0 (0.1) | 4 (0.4) | 29 (1.6) | 11 (0.8) | 57 (2.1) | 69 (1.6) | 0 | 61 (1.2) |
| Singapore | 5 (0.4) | 20 (0.7) | 53 (0.8) | 9 (0.4) | 12 (0.5) | 87 (1.0) | 0 | 78 (0.8) |
| Slovak Republic | 2 (0.3) | 15 (0.9) | 52 (1.4) | 15 (1.0) | 16 (1.1) | 77 (2.0) | 0 | 66 (1.3) |
| Slovenia | 2 (0.3) | 8 (0.7) | 34 (1.6) | 3 (0.3) | 53 (1.9) | 71 (1.6) |  | 68 (1.3) |
| South Africa | 9 (0.5) | 12 (0.6) | 23 (1.0) | 12 (0.6) | 45 (1.4) | 26 (1.4) | 0 | 19 (0.9) |
| Sweden | 1 (0.2) | 14 (0.7) | 58 (1.0) | 15 (0.6) | 11 (0.9) | 66 (1.3) | 0 | 45 (1.0) |
| Tunisia | 6 (0.5) | 16 (1.0) | 36 (1.5) | 7 (0.5) | 35 (2.4) | 64 (1.5) |  | 62 (1.1) |
| United States | 3 (0.2) | 22 (0.6) | 61 (0.8) | 11 (0.4) | 4 (0.4) | 75 (1.3) | 0 | 65 (1.1) |
| International Avg. | 3 (0.1) | 12 (0.1) | 39 (0.2) | 8 (0.1) | 37 (0.3) | 66 (0.2) | $\triangle$ | 57 (0.2) |
| Benchmarking Participants |  |  |  |  |  |  |  |  |
| Basque Country, Spain | 1 (0.2) | 10 (0.8) | 58 (1.7) | 14 (0.9) | 17 (1.8) | 76 (1.5) | 0 | 65 (1.4) |
| Indiana State, US | 2 (0.3) | 23 (1.1) | 59 (1.0) | 13 (0.9) | 4 (0.5) | 78 (1.9) | 0 | 70 (1.5) |
| Ontario Province, Can. | 1 (0.3) | 15 (0.9) | 62 (1.2) | 11 (0.9) | 10 (0.9) | 78 (1.4) | 0 | 59 (1.5) |
| Quebec Province, Can. | 3 (0.5) | 21 (0.9) | 59 (1.2) | 6 (0.4) | 10 (1.0) | 85 (1.2) | 0 | 71 (1.3) |

* Five calculator-sensitive items are M05_02, M06_07, M06_11, M06_12, M06_13
() $\operatorname{Stan} \square$

In scaling the mathematics achievement test, each of the five cal-culator-sensitive items was treated as two distinct items - one item when a calculator was available and the other item when a calculator was unavailable.


## Appendix B

## Multiple Comparisons of Average Achievement

 in Mathematics Content AreasInstructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Countries |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | $0 \cdot$ | - | 0 | 0 - | - 0 | 0 | 0 | 0 | 0 |  | 0 | $0 \cdot$ | 0 | Singapore |
| 0 | 0 | 00 | - | 0 | 00 | 0 | 0 | 00 | 00 | 0 |  |  | 00 | 0 | Korea, Rep. of |
| $\bigcirc$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  | 0 | 0 | 0 | Hong Kong, SAR |
| 0 | - | 0 | - | 0 | 00 | 0 | - | 0 | 00 | 0 |  |  | 0 | 0 | Chinese Taipei |
| 0 | 0 | $0 \cdot$ | 0 | 0 | 00 | 0 | 0 | 0 | 00 | 0 |  | 0 | 00 | 0 | Japan |
| $\bigcirc$ | - | 0 | - | 0 | 0 | - 0 | - | 0 | 00 | 0 |  |  | 0 |  | Belgium (Flemish) |
| 0 | 0 | 00 | 0 | 0 | 00 | 0 | 0 | 0 | 00 | 0 |  | 0 | 00 |  | Netherlands |
| 0 | 0 | 00 | - | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  | 0 | 0 | - | Hungary |
| 0 | 0 | 00 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  | 0 |  | - | Malaysia |
| $\bigcirc$ | - | $0 \cdot$ | - | 0 | $0 \cdot$ | 0 | 0 | 0 | $0 \cdot$ | 0 |  | 0 |  | - | Estonia |
| 0 | 0 | 0 - | 0 | 0 | 0 - | 0 | 0 | 0 | 00 | 0 |  | 0 |  | $\checkmark$ | Slovak Republic |
| 0 | 0 | 0 | 0 | 0 | $0 \cdot$ | - 0 | - | 0 | 00 | 0 |  | 0 |  | © | United States |
| 0 | 0 | 0 - | 0 | 0 | 00 | 0 | 0 | 0 | 00 | 0 |  | 0 |  | (1) | Latvia |
| $\bigcirc$ | - | 0 | - | 0 | 0 | 0 | - | 0 | 00 | 0 |  | 0 | ( | - | Russian Federation |
| $\bigcirc$ | 0 | $0 \cdot$ | 0 | 0 | 0 | 0 | 0 | $0 \cdot$ | 00 | 0 |  | 0 | - | - | Israel |
| 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 00 | $0 \cdot$ | 0 |  | 0 | - (1) | - | Lithuania |
| 0 | 0 | 00 | 0 | 0 | 0 | 0 | 0 | 00 | 00 | 0 |  |  | (-) (1) | - | Australia |
| 0 | - | 0 | 0 | 0 | 0 | - 0 | - | 0 | 00 | 0 |  | 0 | (1) | - | Slovenia |
| 0 | 0 | 00 | 0 | 0 | 00 | 0 | 0 | 00 | 00 | 00 |  |  | - (-) | - | Sweden |
| $\bigcirc$ | - | 0 | - | 0 | 0 | 0 | - | $0 \cdot$ | 00 | 0 |  |  | (-) | - | England |
| 0 | 0 | 00 | 0 | 0 | 0 | 00 | 0 | $0 \cdot$ | 00 | 0 |  |  | - (-) | - | Scotland |
| - | - | 0 | $\bigcirc$ | 0 | 0 | 0 | - | 0 | 00 | 0 |  |  | - - | - | New Zealand |
| 0 | 0 | 00 | - | 0 | 0 | 00 | 0 | 00 | 00 | 0 |  | - | (-) | - | Italy |
| 0 | - | 00 | 0 | 0 | $0 \cdot$ | $0 \cdot$ | - | 0 | 00 | 0 |  | (1) | (1) (1) | - | Serbia |
| 0 | 0 | 00 | 0 | 0 | 00 | 00 | 0 | 00 | 00 | 00 |  | $\checkmark$ | - (-) | - | Bulgaria |
| 0 | - | 00 | 0 | 0 | 0 | $0 \cdot$ | - | 00 | 00 | 00 |  | - | (-) ${ }^{(1)}$ | - | Romania |
| $\bigcirc$ | 0 | 0 - | - | 0 | 0 - 0 | $0 \cdot$ | 0 | $0 \cdot$ | 00 | 0 |  | $\stackrel{\rightharpoonup}{*}$ | (-) ${ }^{(1)}$ | $\stackrel{\rightharpoonup}{*}$ | Armenia |
| 0 | 0 | 00 | $\bigcirc$ | 0 | 0 | $0 \cdot$ | 0 | 00 | 00 | 0 |  | - | $\checkmark$ | - | Cyprus |
| 0 | 0 | 00 | 0 | 0 | 0 | 0 | 0 | 00 | 00 | 0 |  | © | (1) (1) | - | Moldova, Rep. of |
| 0 | - | 00 | 0 | 0 | 0 | $0 \cdot$ | - | 00 | 00 | 0 |  | - | - ${ }^{1}$ | - | Norway |
|  |  | 00 | 0 | 0 | 0 | 00 | 0 | 00 | 00 | 00 |  | - | (-) | - | Macedonia, Rep. of |
|  |  |  | $\bigcirc$ | 0 | 0 | $0 \cdot$ | - | 00 | 00 | 00 |  | - | (-) (1) | - | Lebanon |
| © |  |  |  |  | $\bigcirc$ | 0 | 0 | 0 | 00 | 0 |  | © | (-) (1) | - | Indonesia |
| - | - |  |  |  | 0 | 0 | - | $0 \cdot$ | 00 | 0 |  | - | (-) | - | Egypt |
| © | - |  |  |  | 0 | 00 | 0 | 0 | 00 | 0 |  | (1) | (-) $\square^{(1)}$ | - | Tunisia |
| - | - |  |  |  | 0 | 0 | - | 0 | 00 | 0 |  | (1) | (-) ${ }^{(1)}$ | - | Iran, Islamic Rep. of |
| © | - |  |  |  | 0 | 00 | 0 | 00 | 00 | 0 |  | - | (-) (1) | - | Jordan |
| - | - | (1) © | ( ) | - | - |  |  | 00 | 00 | 00 |  | - | (-) ${ }^{(1)}$ | - | Philippines |
| © | (-) | (-) (1) | (-) | - | - |  |  | $\bigcirc$ | 00 | 0 |  | © | (-) $\square^{(1)}$ | - | Chile |
| - | - | (-) ${ }^{(1)}$ | (1) | - | - |  |  |  | 00 | 0 |  | ( ) | (-) ${ }^{(1)}$ | - | Palestinian Nat'I Auth. |
| © | - | (-) (1) | (-) | (1) | - |  |  |  | 00 | 0 |  | ( | (-) $\square^{(1)}$ | - | Morocco |
| $\checkmark$ | - | (-) ${ }^{(1)}$ | - | (1) | (1) (1) |  |  |  | 00 | 0 |  | ( ) | (-) ${ }^{(1)}$ | - | Botswana |
| - | - | (-) (1) | (-) | - | (-) ${ }^{(1)}$ | - |  |  | 00 | 00 |  | - | - (-) | - | Bahrain |
| - | - | (-) ${ }^{(1)}$ | - | - | (1) (1) | (-) ${ }^{(1)}$ | - | (-) |  | 00 |  | - | (1) ${ }^{(1)}$ | - | Saudi Arabia |
| © | (-) | (-) (1) | (-) | (1) ${ }^{(1)}$ | (-) (1) | (-) (1) | - | (1) (1) | (1) | 0 |  | © | (-) ${ }^{( }$ | - | Ghana |
| - | - | (-) ${ }^{(1)}$ | (1) | - | (-) | (-) | - | (-) (c) | (1) (1) | - |  | (1) | (-) | © | South Africa |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Benchmarking Partici |
| $\bigcirc$ | 0 | 00 | 0 | 0 | 00 | 00 | 0 | 00 | 00 | 00 |  |  | - (-) | - | Basque Country, Spain |
| 0 | 0 | $0 \cdot$ | - | 0 | 00 | 00 | 0 | 00 | 00 | 0 |  | 0 |  | - | Indiana State, US |
| $\bigcirc$ | - | 0 | $\bigcirc$ | 0 | 0 | $0 \cdot$ | 0 | 0 | 00 | 0 |  | 0 |  | $\checkmark$ | Ontario Province, Can. |
| 0 | 0 | 0 | - | 0 | 0 | 00 | 0 | 00 | 00 | 0 |  | 0 | 00 |  | Quebec Province, Can. |

- Average achievement significantly higher than comparison country
(v) Average achievement significantly lower than comparison country

[^89]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


- Average achievement significantly higher than comparison country
(7) Average achievement significantly lower than comparison country

[^90]
## Exhibit B.3: Multiple Comparisons of Average Achievement in Measurement

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


## Benchmarking Participants



[^91]
## Exhibit B.3: Multiple Comparisons of Average Achievement in Measurement

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


[^92]
## Exhibit B.4: Multiple Comparisons of Average Achievement in Geometry

Instructions: Read across the row for a country to compare performance with the countries listed along the top of $\mathrm{t} \mathrm{O}_{\circ}^{\mathrm{O}}$ whether the average achievement of the country in the row is significantly lower than that of the comparison coun that of the comparison country, or if there is no statistically significant difference between the average achievemen


Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

| $\frac{n}{2}$ | $\begin{aligned} & \frac{c}{0} \\ & \frac{1}{0} \\ & \mathbf{0} \end{aligned}$ |  |  |  | $\begin{aligned} & \frac{\frac{\pi}{n}}{\frac{5}{\leftrightharpoons}} \\ & \risingdotseq \end{aligned}$ |  |  |  | $\begin{aligned} & \stackrel{\star}{2} \\ & \underset{\sim}{\hbar} \end{aligned}$ | $\begin{aligned} & \frac{0}{0} \\ & \frac{0}{0} \\ & \frac{0}{4} \\ & \frac{0}{0} \\ & 0 \\ & \sim \end{aligned}$ | $\frac{0}{\bar{U}}$ |  |  | $\begin{aligned} & \text { c } \\ & \frac{\pi}{0} \\ & \frac{\pi}{U} \end{aligned}$ | $\begin{aligned} & \frac{9}{4} \\ & \frac{1}{4} \\ & \stackrel{5}{5} \\ & \stackrel{0}{5} \end{aligned}$ |  |  |  |  | Countries |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | - | - | 0 | 0 | 0 | 0 | - | 0 | 0 | Korea, Rep. of |
| - | 0 | - | - | - | - | - | - | - | - | - | - | - | - | - | - | 0 | - | - | - | Hong Kong, SAR |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | Chinese Taipei |
| 0 | 0 | 0 | - | - | - | - | - | 0 | - | - | 0 | - | - | 0 | - | 0 | 0 | 0 | - | Japan |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | Singapore |
| 0 | 0 | - | 0 | 0 | 0 | - | - | 0 | 0 | - | 0 | 0 | - | - | 0 | 0 | 0 | 0 |  | Estonia |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ( ) | Belgium (Flemish) |
| - | 0 | - | 0 | 0 | - | - | - | - | - | - | - | 0 | - | - | - | 0 | 0 |  | (7) | Hungary |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | (1) | Latvia |
| 0 | 0 | 0 | 0 | - | - | 0 | 0 | 0 | 0 | - | 0 | - | 0 | 0 | 0 | 0 | 0 |  | (1) | Russian Federation |
| 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | (1) | Netherlands |
| 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | - | 0 | 0 | 0 |  | (1) | Lithuania |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ( 7 | (7) | Slovak Republic |
| - | 0 | - | 0 | - | - | - | - | - | - | - | - | 0 | - | - | - | 0 | 0 | () | (7) | Malaysia |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (1) | (1) | England |
| 0 | 0 | 0 | 0 | - | - | - | 0 | 0 | 0 | - | 0 | - | 0 | 0 | - | 0 | 0 | - | (-) | Australia |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ( $\downarrow$ | (-) | Scotland |
| 0 | 0 | - | 0 | 0 | 0 | - | 0 | 0 | 0 | - | 0 | - | 0 | - | 0 | 0 | 0 | () | (1) | New Zealand |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ( ) | (7) | Israel |
| - | - | - | 0 | 0 | - | - | - | - | - | - | - | 0 | - | 0 | - | 0 | 0 | () | (7) | Bulgaria |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | - | 0 | - | - | 0 | 0 | 0 | 0 | 0 | - | (1) | (1) | Slovenia |
| 0 | - | - | 0 | - | - | 0 | 0 | - | - | - | - | - | - | 0 | 0 | 0 | 0 | (1) | (1) | Armenia |
| 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | (1) | (1) | Romania |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | - | - | 0 |  | (7) | (1) | United States |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 |  | ( 7 | (7) | Serbia |
| - | - | - | 0 | 0 | - | 0 | 0 | - | - | - | - | 0 | - | 0 | - | 0 |  | (7) | (1) | Italy |
| 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | (-) | (1) | Sweden |
|  | 0 | - | - | - | - | 0 | 0 | - | - | - | - | - | - | 0 | - |  |  | (1) | ( ) | Moldova, Rep. of |
|  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | - | - | 0 | 0 | 0 | 0 |  |  | (7) | (1) | Norway |
|  | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 |  |  | (7) | (1) | Lebanon |
|  | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 |  | (1) | ( ) | (7) | Cyprus |
| (1) |  |  |  |  | - | 0 | - | - | - | - | - | 0 | - | 0 | - |  | (7) | () | (7) | Jordan |
| (v) |  |  |  |  | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 0 | 0 | 0 | (1) | (1) | (1) | (1) | Macedonia, Rep. of |
| (1) |  |  |  |  | - | 0 | 0 | 0 | - | - | 0 | - | 0 | 0 | 0 | (1) | (1) | (1) | (1) | Bahrain |
| (7) |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (1) | (1) | (1) | (1) | Iran, Islamic Rep. of |
| (1) | (7) | (1) | (1) | (1) |  |  | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | (1) | (1) | () | (1) | Tunisia |
| (7) | (7) | (1) | (7) | (1) |  |  | 0 |  | 0 | - | 0 | 0 | 0 | 0 | 0 | (1) | (1) | ( 7 | (7) | Palestinian Nat'l Auth. |
| (1) | (7) | (1) | (1) | (1) | (1) | (7) |  |  |  | - | 0 | 0 | 0 | 0 | - | (7) | (1) | () | (7) | Morocco |
| ( $\downarrow$ | (1) | (1) | (1) | (1) | (-) |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | (7) | (-) | (-) | (1) | Indonesia |
| (1) | (7) | (1) | (-) | (1) | (1) | (1) |  |  |  | 0 | 0 | 0 | 0 | 0 | - | (1) | (1) | (-) | (1) | Egypt |
| (1) | (-) | (1) | (1) | (7) | (1) | (v) | (-) | (1) | (1) |  |  | 0 | 0 | 0 | 0 | (1) | (1) | (-) | (1) | Saudi Arabia |
| (1) | (7) | (1) | (1) | (1) | (7) | (1) | (1) | (7) | (1) |  |  | 0 | 0 | - | 0 | (1) | (1) | () | (1) | Chile |
| (-) | (v) | (1) | ( ) | (v) | (-) | (-) | (7) | ( | ( $\downarrow$ | (-) | (-) |  |  | 0 | 0 | (-) | (-) | ( - | (-) | Philippines |
| (7) | (7) | (1) | (7) | (7) | (1) | (1) | (7) | (7) | (1) | (1) | (1) |  |  | - | - | (7) | (1) | () | (7) | Botswana |
| (7) | (7) | (1) | (7) | (1) | (1) | (7) | (7) | (1) | (7) | (7) | (1) | (7) | (-) |  | 0 | (1) | (1) | (-) | (1) | Ghana |
| (7) | (7) | (1) | (7) | (1) | (1) | (1) | (7) | (7) | (7) | (1) | (7) | (7) | (7) | (1) |  | (1) | (1) | (7) | (1) | South Africa |

- Average achievement significantly higher than comparison country
(
Average achievement significantly lower than comparison country

[^93]
## Exhibit B.5: Multiple Comparisons of Average Achievement in Data

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

| Singapore |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | - | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Japan |  |  |  |  |  | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | - | - | - | 0 | - | 0 | - | - | 0 | 0 | 0 | - | 0 | - | 0 | - | - |
| Korea, Rep. of | (\%) |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | - | 0 |
| Chinese Taipei | (1) |  |  |  |  |  | - | 0 | - | 0 | - | - | - | - | - | - | - | - | 0 | - | - | - | - | - | - | 0 | - | 0 | - | - |
| Hong Kong, SAR | (\%) |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Netherlands | () | (7) | (1) |  |  |  | - | 0 | - | - | - | - | - | - | - | - | - | - | - | - | - | 0 | - | - | - | 0 | - | 0 | - | - |
| Belgium (Flemish) | (1) | (-) | (v) | ( ) | ( | - |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Sweden | (\%) | (7) | (1) | (1) | (7) | ( ) |  |  |  |  |  |  | 0 | - | - | - | 0 | - | - | - | 0 | 0 | 0 | - | 0 | - | 0 | 0 | 0 | 0 |
| Estonia | (-) | (-) | (1) | - | (-) | (-) | (-) |  |  |  |  |  | 0 |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| England | () | (1) | - | (1) | ( - | (1) | (1) |  |  |  |  |  |  |  |  | - | 0 | - | 0 | - | - | - | - | - | - | - | - | 0 | - | - |
| Australia | (\%) | (-) | (1) | (-) | (1) | (1) | (-) |  |  |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 |
| Scotland | () | (7) | (1) | ( ) | (7) | (7) | (7) |  |  |  |  |  |  |  |  | 0 | - | - | - | 0 | - | - | - | - | - | 0 | - | - | - | - |
| United States | (1) | (-) | (v) | ( $\downarrow$ | (-) | (-) | (-) | (1) | ( ) |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 0 | 0 | 0 | 0 | - | 0 |
| New Zealand | (1) | (7) | (1) | (1) | (1) | (7) | (1) | (-) |  |  |  |  |  |  |  | 0 | 0 | - | - | 0 | 0 | 0 | 0 | - | 0 | - | - | 0 | - | - |
| Hungary | () | (-) | - | - | (-) | (-) | (-) | (\%) | - |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 |
| Latvia | (1) | (7) | - | - | (-) | (1) | (1) | (1) | (1) | (1) | - | ( | (-) | ( | (-) |  |  |  |  | 0 | - | - | - | - | - | 0 | - | - | - | - |
| Malaysia | (-) | (-) | - | - | - | (1) | (v) | (-) | (-) | (-) | (1) | - | (-) | ( $)$ | (-) |  |  |  |  | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 |
| Lithuania | (1) | (1) | (1) | (1) | ( ${ }^{\text {c }}$ | (1) | (1) | (1) | (1) | (1) | (1) | ( ${ }^{\text {c }}$ | (1) | () | () |  |  |  |  |  | - | - | - | - | - | - | - | 0 | - | 0 |
| Norway | (1) | (-) | (\%) | (1) | - | (-) | (v) | (-) | (-) | (1) | ( | - | (-) | ( $\downarrow$ | (-) |  |  |  |  |  |  |  | - | 0 | 0 | 0 | - | 0 | 0 | 0 |
| Slovak Republic | (1) | (7) | (1) | (1) | ( ) | (1) | (1) | (1) | (1) | (1) | ( ) | (1) | (1) | (1) | (1) | (v) | ( |  |  |  |  |  |  | - | - | - | - | 0 | - | 0 |
| Slovenia | (-) | (-) | (1) | (1) | (-) | (-) | (-) | (1) | (-) | (1) | (-) | (-) | (-) | (1) | (-) | (1) | - | ( ${ }^{\text {c }}$ |  |  |  |  |  | - | 0 | 0 | 0 | 0 | - | 0 |
| Israel | (-) | (7) | (1) | (1) | - | (1) | (1) | (1) | (1) | - | - | (1) | (-) | - | (-) | - | - | - |  |  |  |  |  |  | - | 0 | - | - | - | - |
| Italy | (1) | (-) | (1) | (-) | (1) | (1) | (v) | (1) | ( ) | (1) | (1) | ( | (1) | (1) | (1) | (1) | ( $)$ | (1) | (-) |  |  |  |  |  | 0 | 0 | - | 0 | - | 0 |
| Russian Federation | (-) | (-) | (1) | (-) | (1) | (1) | (7) | (1) | (-) | (1) | (1) | (-) | (1) | (-) | (1) | ( ) | (1) | (1) | (1) | - | (1) |  |  |  | - | - | - | - | - | 0 |
| Bulgaria | (1) | (-) | (v) | (\%) | (-) | (1) | (-) | (1) | (7) | (7) | (1) | (-) | (-) | (-) | (-) | (1) | (-) | (7) | (-) | (-) | (1) | - | (-) | (1) |  |  |  | 0 | 0 | 0 |
| Cyprus | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (-) | (1) | - | ( | (1) | - | (1) | - | (1) | (1) | - | (1) | - | (1) | (1) | (1) |  |  |  | 0 | 0 | 0 |
| Serbia | (-) | (-) | (1) | (1) | (7) | (1) | (-) | (1) | ( ) | ( ) | (1) | (1) | (-) | (1) | (7) | (1) | (7) | (1) | (1) | ( ) | (1) | ( - | (-) | (1) |  |  |  | 0 | 0 | 0 |
| Romania | (1) | (7) | (1) | - | (-) | (1) | (1) | (1) | (1) | (1) | - | - | (-) | - | (-) | ( ) | (1) | (1) | - | - | (1) | - | - | ( ) | ( ) | ( $)$ | - |  | - | - |
| Jordan | (\%) | (-) | (1) | (1) | (-) | (1) | (-) | (1) | (-) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (-) | (1) | (1) | ( ) | (1) | (1) | (-) | (1) | (-) | (-) | ( $\downarrow$ | ( - |  |  |
| Moldova, Rep. of | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | ( ${ }^{\text {c }}$ | (1) | () | () | (1) | (1) | (1) | (1) | - | (1) | (1) | - | () | - | (1) | (1) | (1) |  |  |
| Macedonia, Rep. of | (-) | (-) | - | (1) | ( $)$ | (-) | (-) | (\%) | (-) | (1) | (1) | ( | (-) | ( $\downarrow$ | (-) | (1) | (1) | (-) | (-) | - | (1) | - | ( $)$ | (-) | - | (-) | - | (\%) | - |  |
| Armenia | (1) | (1) | (1) | (1) | (1) | (1) | (v) | (1) | (1) | (1) | ( ) | (1) | (1) | () | (1) | ( ) | (1) | (1) | (1) | ( ) | (1) | (1) | (7) | (1) | (1) | (1) | ( ) | (1) | (1) | ( ) |
| Indonesia | (-) | (-) | (1) | (1) | (-) | (-) | (-) | (1) | ( ) | (1) | (1) | (-) | (-) | (1) | (-) | (1) | (-) | (-) | (-) | (-) | (-) | ( $\downarrow$ | (-) | (1) | (1) | (-) | ( - | - | ( $\downarrow$ |  |
| Bahrain | (-) | (7) | (1) | (1) | - | (1) | (1) | (1) | (1) | (1) | - | - | (-) | - | (-) | (1) | (1) | (-) | (-) | - | (1) | ( ) | - | (-) | - | (-) | - | - | - | ( ) |
| Chile | (v) | (-) | (1) | (-) | (1) | (1) | (v) | (v) | ( ) | (1) | (1) | ( $)$ | (v) | (v) | (1) | (1) | (1) | ( $)$ | (-) | (1) | (1) | ( $\downarrow$ | (-) | (1) | (1) | (-) | - | ( $\downarrow$ | (7) | ( ) |
| Iran, Islamic Rep. of | (-) | (-) | - | (-) | (1) | (1) | $\bigcirc$ | (1) | (-) | (1) | (1) | ( ) | (1) | (1) | (1) | (1) | (1) | (-) | (1) | (1) | ( ) | ( ) | (-) | (7) | (7) | (1) | (1) | (-) | (1) | ( ) |
| Lebanon | (7) | (-) | (1) | (1) | ( ) | (7) | (-) | (1) | (-) | (1) | (7) | (7) | (1) | (7) | (-) | (1) | (1) | (7) | (1) | (1) | (1) | ( 7 | (7) | (1) | (7) | (7) | (7) | (1) | (-) | ( ) |
| Egypt | (-) | (7) | (1) | (1) | (1) | (7) | (1) | (1) | (-) | (1) | (1) | (1) | (-) | (1) | (1) | ( ) | ( | (7) | (-) | (1) | ( ) | (1) | (-) | (1) | (1) | (7) | ( ) | (1) | (1) | ( ) |
| Philippines | (-) | (-) | (1) | (1) | (7) | (7) | (-) | (1) | ( ) | (1) | (1) | (1) | (-) | (1) | (-) | (1) | (-) | (-) | (-) | (1) | (1) | ( $\downarrow$ | (-) | (1) | (1) | (-) | ( - | (-) | ( - | ( ) |
| Palestinian Nat'l Auth. | () | (7) | - | (1) | (1) | (1) | (1) | (1) | (1) | (1) | ( | (-) | (1) | (-) | (-) | - | (1) | (1) | (-) | (-) | ( ) | ( ) | (1) | (-) | ( ) | (-) | - | (1) | (-) | - |
| Tunisia | (v) | (-) | (1) | (1) | ( | (-) | (v) | (v) | ( ) | (1) | (v) | ( ) | (-) | (v) | (1) | (1) | (-) | (-) | (-) | (1) | (1) | (v) | (-) | (-) | (1) | (1) | - | (1) | ( $)$ | - |
| Botswana | (-) | (-) | (1) | (-) | (-) | - | - | (1) | (1) | (1) | - | - | (-) | (v) | (-) | - | (1) | (1) | (-) | (1) | - | - | - | - | - | (-) | ( ) | - | - | ( ) |
| Morocco | (1) | ( $)^{\text {c }}$ | (1) | (1) | ( $)$ | (7) | ( ) | (1) | ( ) | (1) | (-) | - | (-) | (1) | (-) | (1) | (1) | (-) | (-) | (-) | (1) | (1) | ( - | (1) | - | (-) | - | (1) | ( | - |
| Saudi Arabia | (1) | (7) | (1) | (1) | ( ) | (1) | (v) | (1) | (1) | (1) | ( ${ }^{\text {c }}$ | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | ( $\downarrow$ | (1) | (1) | (1) | ( ) | (1) | ( ) | - |
| South Africa | (-) | (-) | (-) | (-) | (-) | (7) | (-) | (v) | (-) | ( ) | (-) | ( $)$ | (-) | (-) | (-) | (1) | (-) | (-) | (-) | (1) | (-) | - | - | (1) | (1) | (-) | - | - | ( ) | ( 7 |
| Ghana | (1) | (7) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (1) | (7) | (1) | (1) | (1) | () | - | (1) | (1) | (1) | (1) | (1) | (-) | (1) | (1) | (1) | (1) | (1) | (7) | (1) | ( ) |

## Benchmarking Participants

| Basque Country, Spain | (1) | - | ( | - | (1) | - | - | (1) | - | - | - | - | ( | ( |  |  |  |  |  |  |  |  |  | - | $\bigcirc$ | $\bigcirc$ | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Indiana State, US | (1) | - | - | - | - | (1) | (1) | (-) |  |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Ontario Province, Can. | - | $\bigcirc$ | - | - | - | $\checkmark$ | $\checkmark$ |  |  |  |  |  | 0 | 0 | 0 | 0 | $\bigcirc$ | - | 0 | 0 | - | 0 | - | - | $\bigcirc$ | $\bigcirc$ | 0 | 0 | 0 | $\bigcirc$ | 0 |
| Quebec Province, Can. | (1) | - | - | - | - | - |  |  | 0 |  | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Note: 5\% of these comparisons would be statistically significant by chance alone.

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


- Average achievement significantly higher than comparison country
(7) Average achievement significantly lower than comparison country

[^94]Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Benchmarking Participants

| Indiana State, US | (1) | (1) | - | $\nabla$ | (1) |  |  |  |  |  | 0 | 0 | - | - |  | - | - | - | - | - | - | - | - | - | - | 00 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ontario Province, Can. | () | (1) | (-) | - | () | ( 7 | (v) | (1) | (1) | ( 7 | () | - | - |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (7) |  | (1) |
| Quebec Province, Can. | ( ) | (1) | ( ) | - | (v) | ( - | - | ( ) | - | ( ) | ( ) | (1) |  |  |  | - | - | - | - | - | - | - | - | - | - | - |  |  |

- Average achievement significantly higher than comparison country
(7) significantly lower than comparison country

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


- Average achievement significantly higher than comparison country
- Average achievement significantly lower than comparison country

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Benchmarking Participants


- Average achievement significantly higher than comparison country
(v) Average achievement significantly lower than comparison country

Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.


Instructions: Read across the row for a country to compare performance with the countries listed along the top of the chart. The symbols indicate whether the average achievement of the country in the row is significantly lower than that of the comparison country, significantly higher than that of the comparison country, or if there is no statistically significant difference between the average achievement of the two countries.

| Countries |  |  |  |  |  |  | $\begin{array}{r} y \\ 0 \\ 0 \end{array}$ |  |  |  |  |  |  |  |  |  |  |  | $\frac{3}{3}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Japan |  |  | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | 0 | 0 |  |
| Singapore | - |  |  | - 0 | - | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | 0 | 0 | 0 |
| Chinese Taipei | - |  | - |  |  |  | 0 | 0 | - 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  |  |  | 0 |
| Hong Kong, SAR | - |  | $\bigcirc$ |  | 0 | - | 0 | - 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 |  |  |  |  |  |
| Netherlands | © |  | - | - $\cdot$ |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $0 \cdot$ | 0 | 0 |  |  | 0 |  |
| England | - |  | - | - |  |  |  |  |  | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  |  |  | 0 |
| United States | - |  | - | - $\cdot$ |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | © |  | 0 |
| Belgium (Flemish) | - |  | - | - |  |  |  |  |  | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | - |  | 0 |
| Latvia | © |  | - | - | - | $\bigcirc$ | - ${ }^{\circ}$ | - |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $0 \cdot$ | 0 | 0 |  | - | - | 0 |
| Australia | - |  | - | - $\cdot$ | - | - | - | - |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  |  | - | 0 |
| New Zealand | - |  | $\bigcirc$ | - | - | - | - ${ }^{\circ}$ | - |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | $\checkmark$ | - | 0 |
| Lithuania | - |  | - | - | - | - | - | - | - |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | - | - | 0 |
| Scotland | - |  | - | - | - | - | - ${ }^{\text {c }}$ | - | - | - |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | - | - | 0 |
| Hungary | - |  | - | - | - | - | - | - | - | - | - |  |  |  |  |  |  | 0 | 0 | $\bigcirc$ | 0 | 00 | 0 | 0 |  | - | - |  |
| Cyprus | - |  | - | - $\cdot$ | - | - | c | - | - | - | - | - |  |  |  |  | 0 | 0 | 0 | 0 | 0 | $0 \cdot$ | 0 | 0 |  | - | - |  |
| Russian Federation | - |  | - | - | - | - | - | - | - | - | - | - | - |  |  |  |  |  | 0 | 0 | 0 | 00 | 0 | 0 |  | - | - |  |
| Italy | - |  | - | - $\cdot$ | - | - | - ${ }^{\text {c }}$ | - | - | - | - | - | - | - | $\bigcirc$ |  |  | 0 | 0 | 0 | 0 | 00 | 0 | 0 |  | - | - | - |
| Slovenia | - |  | - | - - | - | - | - | - | - | - | - | - | - | - | $\bullet$ | - | - |  | $\bigcirc$ |  | 0 | 00 | 0 | 0 |  | - | - |  |
| Norway | - |  | - | - $\cdot$ | $\bigcirc$ | - | - ${ }^{\circ}$ | - | - | - | - | - | - | - | - | - | - | - |  |  | 0 | 00 | 0 | 0 |  | - | - |  |
| Moldova, Rep. of | - |  | - | - $\cdot$ | - | - | - | - | - | - | - | - | - | - | - | - | $\bigcirc$ |  |  |  | 0 | 00 | 0 | 0 |  |  | - |  |
| Armenia | - |  | - ${ }^{\circ}$ | - | $\bigcirc$ | $\bigcirc$ | -1 | - ${ }^{-1}$ | - | - | - | - | - | - | - | - | - | $\bigcirc$ | - | - |  | 00 | 0 | 0 |  | $\bigcirc$ | - | - |
| Philippines | - |  | - | - - | - | - | - | - | - | - $\cdot$ | - | - | - | - | - | - | - | - | - | - | - | $\bigcirc$ | 0 | 0 |  | - | - | - |
| Iran, Islamic Rep. of | - |  | $\bigcirc$ | - $\cdot$ | - | - | $\bigcirc$ | - $\cdot$ | - | - | - | $\bigcirc$ | - | - | - | - | $\cdot$ | $\bigcirc$ | - | - | - | - |  | 0 |  | $\bigcirc$ | - |  |
| Morocco | - |  | $\bigcirc$ | - | - | - | $\bigcirc$ | $\bigcirc$ | - | - | - | - | - | $\bigcirc$ | $\cdot$ | - | - | $\bigcirc$ | - | - | - | $\cdots$ |  | 0 |  |  | - |  |
| Tunisia | - |  | - ${ }^{\circ}$ | - ${ }^{\circ}$ | - ${ }^{\circ}$ | - | - ${ }^{\circ}$ | - ${ }^{-1}$ | - $\cdot$ | - | - | $\bigcirc$ | - | - | - | - | - | - | - | - | - | - - - | - |  |  | © | - |  |

## Benchmarking Participants

| Indiana State, US | (1) | - |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |  | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ontario Province, Can. | - | - | (1) | - | - |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |  | 0 |
| Quebec Province, Can. | - | - | - | - | - | (1) | ( | - | - | - | $\bigcirc$ | - | - |  |  |  | 0 | $\bigcirc$ | $\bigcirc$ | - | 0 | - | 0 | - | - |  |  | - |  |

- Average achievement significantly higher than comparison country



## Appendix C The Test-Curriculum Matching Analysis: Mathematics

To ensure that comparisons of student achievement across countries would be as fair and equitable as possible, TIMSS developed extensive assessment frameworks and specifications that addressed the important aspects of mathematics in countries' curricula and instructional programs, and went to great lengths to develop assessment items that faithfully represented those specifications. Similar to the procedures used for developing the original TIMSS instruments, developing the TIMSS 2003 tests involved a series of reviews by representatives of the participating countries, experts in mathematics, and testing specialists. ${ }^{1}$ The National Research Coordinators (NRCs) from each country formally approved the TIMSS 2003 tests, thus accepting them as being sufficiently fair to compare their students' mathematics achievement with that of students from other countries.

Although the tests were developed to represent an agreed-upon framework and were intended to have as much in common across countries as possible, it was inevitable that the match between the TIMSS 2003 test and the mathematics curriculum would not be the same in all countries. To restrict test items to just those topics included in the curricula of all participating countries and covered in the same sequence would severely limit test coverage and restrict the research

[^95]questions that the study is designed to address. The tests, therefore, inevitably have some items measuring topics unfamiliar to some students in some countries.

The Test-Curriculum Matching Analysis (TCMA) was conducted to investigate the appropriateness of the TIMSS 2003 mathematics test for the eighth- and fourth-grade students in the participating countries. TCMA also shows how student performance for individual countries varies when based only on the test questions that are judged to be relevant to their own curricula. ${ }^{2}$

To gather data about the extent to which the TIMSS 2003 tests were relevant to the curricula of the participating countries, each NRC reported whether each item was in that country's intended curriculum at the grade tested (eighth or fourth grade in most countries). The NRC was asked to choose a person (or persons) who was very familiar with the curriculum at these grades to make this determination. Since an item might be in the curriculum for some but not all students in a country, an item was to be determined appropriate if it was in the intended curriculum for more than 50 percent of the students. The NRCs had considerable flexibility in selecting items and may have considered items inappropriate for other reasons. All participants returned the information for analysis except Syria at eighth grade and Yemen at fourth grade.

Exhibits C. 1 and C. 2 present the TCMA results for the TIMSS 2003 tests at eighth and fourth grades. Exhibit C. 1 shows the average percent correct on the mathematics items selected as appropriate by each country. Exhibit C. 2 shows the standard errors corresponding to the percentages presented in Exhibit C.l.

In Exhibit C.1, the last row of the exhibit shows that the countries varied substantially in the number of items (score points) identified as appropriate. ${ }^{3}$ At the eighth grade, the percentage of score points ranged from 100 percent ( 213 score points) in Israel and Saudi Arabia to 71 percent ( 151 score points) in Ghana. Forty-seven of the

2 Because there may also be curriculum areas covered in some countries that are not covered by the TIMSS 2003 tests, the TCMA does not provide complete information about how well the tests cover the curricula of the countries.

3 Some items were assigned more score points than others. In particular, some items had two parts, and some extended-response items were scored on a two-point scale. The TCMA uses score points in order to give the same weight to items given them in test scoring

50 participants indicated that items representing three-quarters or more of the score points ( 160 out of a possible 213) were appropriate. At the fourth grade, the percentage of score points ranged from 99 percent ( 164 score points) in Latvia, Lithuania, the United States, Moldova, and Armenia to 51 percent ( 85 score points) in Tunisia. Twenty-three of the 28 fourth-grade participants indicated that items representing three-quarters or more of the score points ( 125 out of a possible 166) were appropriate.

Since most countries indicated that some items were not included in their intended curricula at the grade tested, the data were analyzed to determine whether the inclusion of these items had any effect on the international performance comparisons. ${ }^{4}$

The first column in Exhibit C.l shows the average percent correct on all test items for each participant. Subsequent columns show the performance of each participant on those items judged appropriate by the participant listed at the head of the column. Participants are presented in order of their performance based on average percent correct on all items, from highest to lowest. To interpret this exhibit, reading across a row provides the average percent correct for the students in that country on the items selected by each of the countries listed across the top of the exhibit. For example, at the eighth-grade, Singapore, where the average percent correct was 72 percent on its own set of items, also had 71 percent correct for the items selected by Korea, 72 percent for the items selected by Hong Kong SAR, and so forth. The column for a country listed across the top shows how each of the other participants performed on the subset of items selected as appropriate for that country's students. Using the set of items selected by the Slovak Republic as an example, on average, 71 percent of these items were answered correctly by students in Singapore, 68 percent by students in Korea, 67 percent by those in Hong Kong SAR, and so forth. The shaded diagonal element in the exhibit shows how each country performed on the subset of items that it selected based on its

4 It should be noted that the mathematics achievement presented in Exhibit C. 1 is based on average percent correct, which is different from the average scale scores that are presented in Chapter 1.

## Exhibit C.1: Average Percent Correct for Test-Curriculum Matching Analysis - Mathematics

Based on Subset of Items Specially Identified by Each Country as Addressing its Curriculum
(See Exhibit C. 2 for corresponding standard errors)
mathematics Grade

Instructions: Read across the row to compare that country's performance based on the test items included by each of the countries across the top. Read down the column under a country name to compare the performance of the country down the left on the items included by the country listed on the top. Read along the diagonal to compare performance for each different country based on its own decisions about the test items to include.
$\begin{array}{r}\text { Korea, Rep. of } \\ \hline \text { Hong Kong, SAR }\end{array}$

| $\square$ Japan |
| :--- |
| Belgium ( |$\begin{array}{r}\text { Hungary } \\ \hline \text { Estonia } \\ \hline \text { Russian Federation } \\ \hline\end{array}$



| Malaysia |
| ---: |
| United States |
| Lithuania |$\begin{array}{r}\text { Sweden } \\ \hline \text { Scotland } \\ \hline \text { England } \\ \hline \text { Israel }\end{array}$ $\begin{array}{r}\text { Israel } \\ \hline \text { New Zealand } \\ \text { Slovenia } \\ \hline\end{array}$

$\begin{array}{r}\text { Armenia } \\ \hline \text { Cyprus } \\ \hline \text { Moldova, Rep. of } \\ \hline\end{array}$| Macedonia, Rep. of |
| ---: |
| Lebanon |
| Jordan | Jordan





 Morocco Botswana

| Botswana |
| ---: |
| Saudi Arabia |
| South Africa |
| Ghana |

Benchmarking Participants

| Basque Country, Spain |
| ---: |
| Indiana State, US |
| Ontario Province, Can. |

Ontario Province, Can.
Quebec Province, Can.
Number of Items
(Score Points) Identified*


## Exhibit C.1: Average Percent Correct for Test-Curriculum Matching Analysis - Mathematics Based on Subset of Items Specially Identified by Each Country as Addressing its Curriculum (See Exhibit C. 2 for corresponding standard errors)

Instructions: Read across the row to compare that country's performance based on the test items included by each of the countries across the top. Read down the column under a country name to compare the performance of the country down the left on the items included by the country listed on the top. Read along the diagonal to compare performance for each different country based on its own decisions about the test items to include.

| $\begin{aligned} & \frac{0}{2} \\ & \frac{\pi}{0} \\ & \frac{0}{7} \\ & \frac{0}{5} \end{aligned}$ | $\frac{0}{c}$ <br> $\frac{0}{6}$ <br> $\frac{5}{4}$ | $\frac{n}{2}$ |  | $\begin{aligned} & \text { त } \\ & \sum_{0}^{0} \\ & \frac{0}{2} \end{aligned}$ |  |  |  | $\begin{aligned} & \frac{\pi}{y} \\ & \pm \\ & \frac{0}{0} \\ & \underline{c} \end{aligned}$ | $\stackrel{\stackrel{\rightharpoonup}{2}}{\underset{\sim}{2}}$ |  | $\frac{\frac{5}{0}}{\frac{0}{\pi}}$ | $\frac{\frac{\pi}{n}}{\risingdotseq}$ | $\frac{\stackrel{0}{\overline{5}}}{\frac{1}{y}}$ |  |  | $\begin{aligned} & \circ \\ & \hline 0 \\ & \text { O } \\ & \text { º } \end{aligned}$ | o 0 0 3 0 0 0 | $\begin{aligned} & \frac{0}{0} \\ & \frac{0}{0} \\ & \frac{0}{4} \\ & \frac{\overline{0}}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ভ } \\ & \frac{0}{4} \\ & \frac{1}{4} \\ & \vdots \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { © } \\ & \frac{\pi}{\pi} \\ & \text { స } \end{aligned}$ | Basque Country, Spain | $\bumpeq$ |  |  |  | Countries |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71 | 71 | 71 | 71 | 72 | 73 | 72 | 69 | 71 | 74 | 71 | 72 | 73 | 72 | 72 | 72 | 71 | 71 | 71 | 75 | 74 | 72 | 71 | 72 | 71 | 71 (0.9) | Singapore |
| 68 | 68 | 68 | 68 | 68 | 68 | 68 | 66 | 68 | 71 | 68 | 68 | 69 | 67 | 68 | 69 | 68 | 68 | 68 | 70 | 70 | 69 | 68 | 68 | 68 | 68 (0.4) | Korea, Rep. of |
| 67 | 67 | 67 | 67 | 68 | 68 | 67 | 65 | 67 | 70 | 67 | 67 | 68 | 67 | 67 | 68 | 67 | 67 | 67 | 71 | 69 | 68 | 67 | 68 | 67 | 67 (0.8) | Hong Kong, SAR |
| 65 | 66 | 66 | 66 | 66 | 67 | 66 | 64 | 66 | 69 | 66 | 66 | 66 | 65 | 66 | 67 | 65 | 66 | 66 | 69 | 67 | 66 | 66 | 66 | 66 | 66 (1.0) | Chinese Taipei |
| 63 | 63 | 63 | 63 | 64 | 63 | 63 | 61 | 63 | 66 | 63 | 63 | 64 | 63 | 64 | 64 | 63 | 64 | 64 | 64 | 65 | 64 | 63 | 64 | 64 | 64 (0.5) | Japan |
| 55 | 56 | 55 | 56 | 58 | 56 | 56 | 52 | 56 | 58 | 56 | 56 | 57 | 57 | 56 | 56 | 55 | 57 | 56 | 59 | 58 | 56 | 56 | 57 | 56 | 56 (0.7) | Belgium (Flemish) |
| 54 | 55 | 54 | 55 | 57 | 53 | 54 | 50 | 55 | 56 | 54 | 55 | 55 | 57 | 55 | 55 | 54 | 56 | 55 | 57 | 58 | 55 | 55 | 57 | 55 | 55 (1.0) | Netherlands |
| 54 | 55 | 54 | 55 | 56 | 55 | 55 | 52 | 55 | 57 | 55 | 55 | 56 | 56 | 55 | 55 | 54 | 56 | 55 | 58 | 56 | 55 | 55 | 55 | 55 | 55 (0.8) | Hungary |
| 53 | 54 | 53 | 54 | 56 | 54 | 54 | 51 | 54 | 56 | 54 | 54 | 55 | 55 | 54 | 55 | 53 | 55 | 54 | 57 | 56 | 54 | 54 | 55 | 54 | 54 (0.8) | Estonia |
| 48 | 49 | 49 | 49 | 50 | 51 | 49 | 48 | 49 | 52 | 49 | 49 | 51 | 49 | 49 | 51 | 49 | 49 | 49 | 54 | 52 | 50 | 49 | 49 | 49 | 49 (0.9) | Russian Federation |
| 48 | 48 | 49 | 48 | 50 | 50 | 49 | 46 | 48 | 51 | 49 | 49 | 51 | 50 | 49 | 50 | 48 | 49 | 49 | 53 | 52 | 49 | 49 | 49 | 49 | 49 (0.8) | Slovak Republic |
| 48 | 48 | 48 | 48 | 49 | 49 | 49 | 46 | 48 | 51 | 48 | 48 | 50 | 48 | 48 | 49 | 48 | 49 | 48 | 52 | 51 | 49 | 48 | 49 | 48 | 48 (0.8) | Latvia |
| 47 | 48 | 47 | 48 | 50 | 47 | 48 | 44 | 48 | 50 | 48 | 48 | 48 | 50 | 48 | 48 | 47 | 49 | 48 | 49 | 50 | 49 | 48 | 50 | 48 | 48 (1.1) | Australia |
| 47 | 48 | 47 | 48 | 49 | 48 | 48 | 45 | 48 | 51 | 48 | 48 | 49 | 50 | 48 | 49 | 47 | 48 | 48 | 53 | 51 | 48 | 48 | 49 | 48 | 48 (1.0) | Malaysia |
| 46 | 47 | 47 | 47 | 49 | 46 | 47 | 44 | 47 | 49 | 47 | 47 | 48 | 48 | 47 | 48 | 47 | 49 | 48 | 49 | 49 | 48 | 48 | 48 | 48 | 48 (0.8) | United States |
| 46 | 47 | 46 | 47 | 48 | 47 | 47 | 45 | 47 | 49 | 47 | 47 | 48 | 47 | 47 | 48 | 46 | 48 | 47 | 50 | 49 | 47 | 47 | 48 | 47 | 47 (0.6) | Lithuania |
| 46 | 47 | 46 | 47 | 49 | 45 | 46 | 41 | 47 | 48 | 46 | 46 | 46 | 49 | 47 | 46 | 46 | 49 | 47 | 48 | 49 | 47 | 47 | 48 | 47 | 47 (0.7) | Sweden |
| 45 | 46 | 45 | 46 | 48 | 44 | 46 | 41 | 46 | 47 | 46 | 46 | 46 | 48 | 46 | 46 | 45 | 47 | 46 | 46 | 48 | 47 | 47 | 48 | 46 | 46 (1.0) | Scotland |
| 45 | 46 | 45 | 46 | 48 | 44 | 46 | 41 | 46 | 47 | 45 | 46 | 45 | 47 | 46 | 46 | 45 | 47 | 46 | 46 | 48 | 46 | 46 | 47 | 46 | 46 (1.2) | England |
| 45 | 46 | 45 | 46 | 47 | 46 | 46 | 43 | 46 | 48 | 45 | 45 | 47 | 46 | 46 | 47 | 45 | 47 | 46 | 49 | 48 | 46 | 46 | 46 | 46 | 46 (0.8) | Israel |
| 44 | 45 | 44 | 45 | 47 | 43 | 44 | 40 | 45 | 46 | 44 | 45 | 44 | 46 | 45 | 44 | 44 | 46 | 45 | 45 | 46 | 45 | 45 | 46 | 45 | 45 (1.3) | New Zealand |
| 43 | 44 | 43 | 44 | 45 | 44 | 44 | 41 | 44 | 46 | 44 | 44 | 45 | 45 | 44 | 45 | 43 | 45 | 44 | 47 | 46 | 44 | 44 | 45 | 44 | 44 (0.6) | Slovenia |
| 42 | 43 | 43 | 43 | 44 | 43 | 43 | 40 | 43 | 45 | 43 | 43 | 44 | 44 | 43 | 43 | 42 | 44 | 43 | 46 | 45 | 43 | 43 | 44 | 43 | 43 (0.7) | Italy |
| 41 | 41 | 42 | 41 | 42 | 43 | 42 | 41 | 41 | 44 | 42 | 41 | 43 | 42 | 42 | 43 | 41 | 42 | 42 | 46 | 44 | 42 | 42 | 42 | 41 | 42 (1.1) | Romania |
| 41 | 41 | 41 | 41 | 42 | 43 | 41 | 40 | 41 | 44 | 42 | 41 | 43 | 41 | 41 | 43 | 41 | 42 | 41 | 46 | 44 | 42 | 41 | 41 | 41 | 41 (0.6) | Serbia |
| 40 | 40 | 41 | 40 | 41 | 42 | 41 | 39 | 40 | 43 | 41 | 40 | 43 | 41 | 40 | 42 | 40 | 41 | 41 | 44 | 43 | 41 | 40 | 41 | 40 | 41 (0.9) | Bulgaria |
| 39 | 39 | 40 | 39 | 39 | 42 | 40 | 40 | 39 | 42 | 40 | 39 | 41 | 37 | 40 | 41 | 39 | 39 | 39 | 44 | 40 | 40 | 39 | 39 | 39 | 39 (0.7) | Armenia |
| 36 | 37 | 38 | 37 | 38 | 38 | 38 | 36 | 37 | 40 | 38 | 37 | 39 | 38 | 37 | 38 | 37 | 38 | 37 | 41 | 40 | 38 | 37 | 38 | 37 | 37 (0.3) | Cyprus |
| 37 | 37 | 37 | 37 | 38 | 39 | 37 | 37 | 37 | 40 | 37 | 37 | 39 | 37 | 37 | 39 | 37 | 37 | 37 | 41 | 40 | 37 | 37 | 37 | 37 | 37 (0.8) | Moldova, Rep. of |
| 36 | 37 | 36 | 37 | 39 | 36 | 37 | 33 | 37 | 38 | 37 | 36 | 37 | 39 | 37 | 37 | 36 | 38 | 37 | 38 | 39 | 37 | 37 | 38 | 37 | 37 (0.5) | Norway |
| 33 | 33 | 33 | 33 | 34 | 34 | 33 | 32 | 33 | 35 | 33 | 33 | 35 | 33 | 33 | 34 | 33 | 34 | 33 | 36 | 35 | 34 | 33 | 33 | 33 | 33 (0.6) | Macedonia, Rep. of |
| 32 | 31 | 32 | 31 | 32 | 34 | 32 | 33 | 31 | 34 | 32 | 32 | 33 | 31 | 32 | 34 | 32 | 31 | 32 | 36 | 33 | 32 | 31 | 31 | 31 | 32 (0.6) | Lebanon |
| 30 | 31 | 30 | 31 | 31 | 31 | 31 | 32 | 31 | 32 | 31 | 30 | 32 | 30 | 31 | 31 | 30 | 31 | 31 | 32 | 32 | 31 | 31 | 31 | 30 | 31 (0.7) | Jordan |
| 29 | 29 | 29 | 29 | 30 | 30 | 29 | 29 | 29 | 31 | 29 | 29 | 30 | 30 | 29 | 30 | 29 | 30 | 29 | 32 | 31 | 30 | 29 | 30 | 29 | 29 (0.7) | Indonesia |
| 28 | 28 | 28 | 28 | 28 | 29 | 28 | 29 | 28 | 31 | 28 | 28 | 30 | 28 | 28 | 30 | 28 | 28 | 28 | 32 | 30 | 29 | 28 | 28 | 28 | 28 (0.5) | Egypt |
| 27 | 28 | 28 | 28 | 28 | 29 | 28 | 28 | 28 | 30 | 28 | 28 | 29 | 28 | 28 | 29 | 27 | 28 | 28 | 30 | 30 | 28 | 28 | 28 | 28 | 28 (0.4) | Iran, Islamic Rep. of |
| 27 | 27 | 27 | 27 | 28 | 27 | 27 | 28 | 27 | 29 | 27 | 27 | 28 | 28 | 27 | 28 | 27 | 28 | 27 | 28 | 29 | 27 | 27 | 28 | 27 | 27 (0.2) | Bahrain |
| 27 | 27 | 27 | 27 | 28 | 28 | 28 | 27 | 27 | 29 | 27 | 27 | 30 | 28 | 27 | 28 | 27 | 27 | 27 | 30 | 29 | 27 | 27 | 27 | 27 | 27 (0.4) | Tunisia |
| 26 | 27 | 26 | 27 | 28 | 26 | 27 | 24 | 27 | 28 | 26 | 26 | 27 | 28 | 26 | 27 | 26 | 27 | 27 | 28 | 29 | 27 | 27 | 28 | 26 | 27 (0.5) | Chile |
| 25 | 26 | 26 | 26 | 26 | 27 | 26 | 26 | 26 | 28 | 26 | 26 | 27 | 26 | 26 | 27 | 25 | 26 | 26 | 28 | 27 | 26 | 26 | 26 | 26 | 26 (0.4) | Palestinian Nat'l Auth. |
| 24 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 27 | 25 | 25 | 25 | 25 | 25 | 26 | 24 | 25 | 25 | 28 | 26 | 25 | 25 | 25 | 25 | 25 (0.8) | Philippines |
| 24 | 24 | 24 | 24 | 25 | 25 | 25 | 25 | 24 | 26 | 25 | 25 | 26 | 25 | 24 | 25 | 24 | 25 | 25 | 27 | 26 | 25 | 24 | 25 | 24 | 25 (0.4) | Morocco |
| 22 | 23 | 22 | 23 | 24 | 23 | 23 | 22 | 23 | 25 | 23 | 23 | 24 | 24 | 23 | 24 | 23 | 24 | 23 | 26 | 24 | 23 | 23 | 24 | 23 | 23 (0.3) | Botswana |
| 18 | 19 | 19 | 19 | 19 | 19 | 19 | 19 | 19 | 20 | 19 | 19 | 20 | 19 | 19 | 20 | 18 | 19 | 19 | 21 | 20 | 19 | 19 | 19 | 19 | 19 (0.3) | Saudi Arabia |
| 16 | 17 | 16 | 17 | 17 | 17 | 17 | 17 | 17 | 18 | 17 | 16 | 17 | 17 | 17 | 17 | 16 | 17 | 17 | 18 | 18 | 17 | 17 | 17 | 16 | 17 (0.7) | South Africa |
| 14 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 16 | 15 | 15 | 15 | 15 | 15 | 15 | 14 | 15 | 15 | 17 | 16 | 15 | 15 | 15 | 15 | 15 (0.4) | Ghana |
| 40 | 41 | 41 | 41 | 42 | 42 | 41 | 39 | 41 | 43 | 41 | 41 | 42 | 42 | 41 | 42 | 41 | 42 | 41 | 44 | 43 | 42 | 41 | 42 | 41 | 41 (0.1) | International Avg. |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Benchmarking Participants |
| 42 | 43 | 43 | 43 | 45 | 43 | 44 | 40 | 43 | 45 | 43 | 43 | 45 | 44 | 43 | 44 | 43 | 45 | 43 | 46 | 46 | 44 | 44 | 44 | 43 | 43 (0.7) | Basque Country, Spain |
| 46 | 47 | 47 | 47 | 49 | 46 | 47 | 44 | 47 | 49 | 47 | 47 | 48 | 48 | 47 | 48 | 47 | 49 | 47 | 50 | 49 | 48 | 48 | 48 | 48 | 47 (1.3) | Indiana State, US |
| 51 | 51 | 51 | 51 | 53 | 50 | 51 | 47 | 51 | 53 | 51 | 51 | 51 | 53 | 51 | 51 | 51 | 53 | 52 | 52 | 53 | 52 | 52 | 53 | 52 | 52 (0.7) | Ontario Province, Can. |
| 57 | 57 | 57 | 57 | 59 | 58 | 57 | 54 | 57 | 60 | 57 | 57 | 58 | 59 | 57 | 58 | 56 | 59 | 57 | 60 | 60 | 58 | 58 | 58 | 58 | 57 (0.9) | Quebec Province, Can. |
| 196 | 209 | 197 | 209 | 188 | 174 | 189 | 152 | 209 | 192 | 203 | 199 | 162 | 164 | 207 | 192 | 198 | 184 | 213 | 128 | 151 | 210 | 206 | 195 | 201 | 213 | Number of Items (Score Points) Identified* |

[^96]Exhibit C.1: Average Percent Correct for Test-Curriculum Matching Analysis - Mathematics Based on Subset of Items Specially Identified by Each Country as Addressing its Curriculum (See Exhibit C. 2 for corresponding standard errors)


* Of the 161 items in the Mathematics test, some extended-response items were scored on a twopoint scale, resulting in 169 total score points. Following item review, some items were deleted and response categories were combined for a number of items, resulting in 159 items and 166 score points.
own curriculum. Thus, Slovakian students averaged 49 percent correct on the set of items identified by the Slovak Republic for the analysis.

The international averages of each country's selected items are presented in the lower part of the exhibit. They show that the selection of items for the participating countries varied somewhat in average difficulty, ranging from 39 percent for those chosen by Jordan at the eighth grade to 45 percent for those chosen by Italy. Similarly at the fourth grade, the average percent correct ranged from 53 percent for those items chosen by England and Scotland to 59 percent for those chosen by the Russian Federation. Despite these differences in the difficulty of the selected items, the overall message of Exhibit C. 1 is that different item selections do not make a major difference in how well countries perform relative to one another. The items selected by some countries were more difficult than those selected by others. The relative performance of countries on various item selections did vary somewhat, but generally not in a statistically significant manner. ${ }^{5}$

Comparing the diagonal element for a country with the overall average percent correct shows the difference between performance on the subset of items chosen as appropriate by the country and performance on the test as a whole. In general, there were only small increases in each country's performance on its own subset of items. To illustrate, the average percent correct for Singapore across all eighthgrade mathematics items was 71 percent. The diagonal element shows that Singaporean students had a slightly greater average percent correct (72 percent) across the set of items selected as appropriate for Singapore than they did overall. Almost all participants had a difference of one or two percentage points between the two performance measures, with the largest difference - four percent - for the Netherlands (55 percent compared with 59 percent).

It is clear that the selection of items does not have a major effect on the general relationship among countries. Countries that had relatively high or low performance across all the mathematics items also had relatively high or low performance on each of the various sets of

5 Small differences in performance shown in this exhibit are not statistically significant. The standard errors for the estimated average percent correct statistics are in Exhibit C.2. It can be said with 95 percent confidence that the value for the entire population falls between the sample estimate plus or minus two standard errors.

Exhibit C.2: Standard Errors for the Test-Curriculum Matching Analysis - Mathematics

|  | Instructions: | Read across the row to compare that country's performance based on the test items included by each of the countries across the top. Read down the column under a country name to compare the performance of the country down the left on the items included by the country listed on the top. Read along the diagonal to compare performance for each different country based on its own decisions about the test items to include. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Countries |  |  |  |  |  | $\begin{aligned} & \frac{5}{0} \\ & \text { o } \\ & \text { on } \end{aligned}$ |  |  | $\begin{aligned} & \text { 륻 } \\ & \text { on } \\ & \text { ㅗㅗ } \end{aligned}$ | $\begin{aligned} & \frac{\pi}{\bar{c}} \\ & \stackrel{0}{4} \end{aligned}$ |  |  | $\sum_{\underset{\sim}{0}}^{0}$ | $\frac{\frac{. \pi}{\bar{N}}}{\frac{5}{5}}$ |  |  |  | $\stackrel{\text { © }}{\stackrel{\text { ® }}{\mathrm{O}}}$ |  | $\begin{aligned} & \text { ס } \\ & \text { No } \end{aligned}$ | $\begin{aligned} & \overline{\mathbb{0}} \\ & \stackrel{\rightharpoonup}{\underline{\omega}} \end{aligned}$ |  | $\begin{aligned} & \frac{0}{末} \\ & \frac{10}{\omega} \\ & \stackrel{0}{\omega} \end{aligned}$ | $\Phi$ |  | ~ |
| Singapore | 71 (0.9) | 0.9 | 0.9 | 1.0 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 |
| Korea, Rep. of | 68 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| Hong Kong, SAR | 67 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Chinese Taipei | 66 (1.0) | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| Japan | 64 (0.5) | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| Belgium (Flemish) | 56 (0.7) | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Netherlands | 55 (1.0) | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.1 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| Hungary | 55 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Estonia | 54 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.7 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Russian Federation | 49 (0.9) | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 |
| Slovak Republic | 49 (0.8) | 0.8 | 0.8 | 0.9 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.9 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.9 | 0.9 | 0.8 | 0.8 |
| Latvia | 48 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.7 | 0.7 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Australia | 48 (1.1) | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 |
| Malaysia | 48 (1.0) | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 |
| United States | 48 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Lithuania | 47 (0.6) | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 |
| Sweden | 47 (0.7) | 0.6 | 0.7 | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.6 | 0.6 | 0.6 | 0.7 | 0.7 | 0.6 | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.6 | 0.7 | 0.7 | 0.6 |
| Scotland | 46 (1.0) | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 0.9 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| England | 46 (1.2) | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.3 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 | 1.2 |
| Israel | 46 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| New Zealand | 45 (1.3) | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 |
| Slovenia | 44 (0.6) | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 |
| Italy | 43 (0.7) | 0.8 | 0.7 | 0.8 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0.8 | 0.8 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Romania | 42 (1.1) | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 | 1.1 |
| Serbia | 41 (0.6) | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.5 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 |
| Bulgaria | 41 (0.9) | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 |
| Armenia | 39 (0.7) | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Cyprus | 37 (0.3) | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 |
| Moldova, Rep. of | 37 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.9 | 0.9 | 0.8 | 0.8 |
| Norway | 37 (0.5) | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.6 | 0.6 | 0.5 | 0.5 | 0.6 | 0.5 | 0.5 | 0.6 | 0.6 | 0.5 | 0.5 | 0.6 | 0.6 | 0.5 | 0.5 | 0.6 | 0.5 | 0.6 | 0.5 | 0.5 |
| Macedonia, Rep. of | 33 (0.6) | 0.6 | 0.6 | 0.7 | 0.6 | 0.6 | 0.6 | 0.7 | 0.6 | 0.6 | 0.7 | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.6 | 0.6 | 0.7 | 0.6 | 0.7 | 0.7 | 0.6 |
| Lebanon | 32 (0.6) | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.7 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.7 | 0.7 | 0.6 | 0.6 |
| Jordan | 31 (0.7) | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 |
| Indonesia | 29 (0.7) | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 |
| Egypt | 28 (0.5) | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| Iran, Islamic Rep. of | 28 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| Bahrain | 27 (0.2) | 0.2 | 0.2 | 0.3 | 0.2 | 0.3 | 0.3 | 0.3 | 0.2 | 0.2 | 0.3 | 0.2 | 0.2 | 0.3 | 0.2 | 0.2 | 0.2 | 0.3 | 0.3 | 0.3 | 0.2 | 0.3 | 0.3 | 0.3 | 0.3 | 0.2 |
| Tunisia | 27 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| Chile | 27 (0.5) | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| Palestinian Nat'l Auth. | 26 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.5 | 0.4 | 0.4 | 0.4 | 0.5 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.5 | 0.5 | 0.4 | 0.4 |
| Philippines | 25 (0.8) | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.7 | 0.7 | 0.7 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 |
| Morocco | 25 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.3 | 0.4 | 0.4 | 0.4 | 0.3 | 0.3 | 0.3 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| Botswana | 23 (0.3) | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.4 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.4 | 0.3 | 0.3 | 0.3 | 0.4 | 0.4 | 0.3 | 0.3 | 0.3 | 0.3 | 0.4 | 0.3 | 0.3 |
| Saudi Arabia | 19 (0.3) | 0.4 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.3 | 0.4 | 0.3 | 0.4 | 0.3 | 0.3 | 0.4 | 0.3 | 0.3 | 0.3 | 0.4 | 0.4 | 0.3 | 0.3 | 0.4 | 0.4 | 0.4 | 0.4 | 0.3 |
| South Africa | 17 (0.7) | 0.7 | 0.7 | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Ghana | 15 (0.4) | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.3 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.3 | 0.3 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| International Avg. | 41 (0.1) | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 |

## Exhibit C.2: Standard Errors for the Test-Curriculum Matching Analysis - Mathematics

Instructions: Read across the row to compare that country's performance based on the test items included by each of the countries across the top. Read down the column under a country name to compare the performance of the country down the left on the items included by the country listed on the top. Read along the diagonal to compare performance for each different country based on its own decisions about the test items to include.


|  | 0.9 | 0.9 | 0.9 | 0.9 | 1.0 | 0.9 | 1.0 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.9 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.5 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 | 0.4 |
| 0.4 |  |  |  |  |  |  |  |  |  |  |  |  |  |

 \begin{tabular}{l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|}
\hline 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.1 \& 1.1 \& 1.0 \& 1.0 <br>
\hline

 

\hline 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.6 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 <br>
0.5 \& 0.5 \& 0.5 <br>
\hline
\end{tabular}

 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.1 | 1.0 | 1.0 | 1.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1.0 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.8 | 0.9 |

 \begin{tabular}{l|l|l|ll|l|l|l|ll|l|l|l|l}
\hline 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 <br>
\hline 1.0 \& 0.9 \& 0.9 \& 0.9 \& 0.9 <br>
\hline 0.9 \& 0.9 \& 0.9 \& 1.0 \& 0.9 \& 0.9 <br>
\hline 0.9 \& 0.9 \& 0.9 \& 0.9 \& 1.0 \& 0.9 <br>
\hline

 

\hline 0.9 \& 0.8 \& 0.8 \& 0.8 \& 0.8 <br>
\hline 0.9 \& 0.9 \& 0.9 \& 0.8 \& 0.9 <br>
\hline 0.8 \& 0.8 \& 0.9 \& 0.8 \& 0.8 \& 0.8 \& 0.9 \& 0.8 \& 0.8 \& 0.9

 $0^{0.9}$

<br>
\hline

 

\hline 0.7 \& 0.8 \& 0.8 \& 0.8 \& 0.7 \& 0.7 \& 0.8 \& 0.7 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.7 \& 0.8 \& 0.7 \& 0.8 \& 0.7 \& 0.8 \& 0.8 \& 0.8 <br>
\hline

 

\hline 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 <br>
1.1 \& 1.1 \& 1.2 \& 1.1 <br>
\hline 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.0 \& 1. \& 1.0 \& 1.0 \& 1. \& 1.0 \& 1.0 \& 1.0 \& 1.0 <br>
\hline

 

\hline 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 \& 1.1 \& 1.0 \& 1.0 <br>
\hline

 

\hline 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 <br>
\hline 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 <br>
\hline

 

\hline 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 <br>
\hline 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.7 \& 0.6 <br>
\hline

 

\hline 0.7 \& 0.6 \& 0.6 \& 0.6 \& 0.7 <br>
\hline 1.0 \& 1.0 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 <br>
\hline

 

\hline 1.0 \& 1.0 \& 1.0 \& 1.0 \& 1.0 \& 0.9 \& 0.9 \& 0.9 \& 1.0 \& 1.0 \& 1.0 \& 1.0 \& 0.9 \& 1.0 \& 1.0 \& 1.0 <br>
1.0 \& 1.0 \& 1.0 \& 1.0 \& 0.9 <br>
\hline 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& <br>
\hline

 

\hline 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.1 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 \& 1.2 <br>
\hline 08 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 <br>
\hline
\end{tabular}



 \begin{tabular}{l|l|l|lllllllllllllllllll}
\hline 0.8 \& 0.7 \& 0.8 \& 0.7 \& 0.7 \& 0.8 \& 0.7 \& 0.7 \& 0.7 \& 0.8 \& 0.7 \& 0.8 \& 0.7 \& 0.7 \& 0.8 \& 0.8 \& 0.8 \& 0.7 \& 0.7 \& 0.8 \& 0.8 <br>
\hline 1

 

\hline 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 <br>
\hline 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.1 \& 1.2 \& 1.1 <br>
\hline

 

\hline 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 <br>
\hline 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 <br>
\hline 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 \& 0.9 \& 1.0

 1.0 

0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.8 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.8 \& 0.8 <br>
\hline

 

\hline 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.4 \& 0.3 <br>
\hline

 

\hline 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.9 \& 0.8 <br>
\hline

 $\left.$

\hline 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.6 \& 0.5 \& 0.5 \& 0.5 \& 0.5 <br>
0.5 <br>
\hline 0

 $\mathbf{0 . 5} \right\rvert\,$

0.6 <br>
0.5 <br>
\hline

 

\hline 0.6 \& 0.7 \& 0.6 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.6 \& 0.7 \& 0.7 \& 0.6 \& 0.7 \& 0.7 \& 0.6 \& 0.7 \& 0.6 \& 0.7 \& 0.7 \& 0.6 \& 0.7 \& 0.7 <br>
\hline

 

\hline 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.6 \& 0.7 <br>
\hline

 

\hline 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 <br>
\hline

 

\hline 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 <br>
0.7 \& 0.8 \& 0.7 <br>
\hline

 

\hline 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 <br>
\hline 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 <br>
0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.5 \& 0.5 \& 0.5 \& 0.5 <br>
\hline

 

\hline 0.3 \& 0.2 \& 0.2 \& 0.2 \& 0.2 \& 0.3 \& 0.3 \& 0.3 \& 0.2 \& 0.3 \& 0.2 \& 0.2 \& 0.3 \& 0.3 \& 0.2 \& 0.3 <br>
0.2 \& 0.2 \& 0.2 \& 0.3 \& 0.3 <br>
\hline

 

\hline 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 <br>
0.4 \& 0.4 \& 0.4 \& 0.4 <br>
\hline

 

\hline 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 \& 0.5 <br>
0.5 \& 0.5 \& 0.5 <br>
\hline

 

\hline 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.5 \& 0.4 \& 0.4 \& 0.4 \& 0.5 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.5 \& 0.4 \& 0.4 \& 0.4 \& 0.5 <br>
\hline

 

\hline 0.7 \& 0.8 \& 0.8 \& 0.8 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.8 \& 0.8 <br>
\hline 0.7 \& 0.7 \& 0.8 \& 0.8 \& 0.7 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 \& 0.8 <br>
\hline

 

\hline 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.3 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.3 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 <br>
\hline

 

\hline 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.4 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.3 \& 0.4 \& 0.3 \& 0.4 \& 0.3 <br>
\hline

 

\hline 0.3 \& 0.3 \& 0.4 \& 0.3 \& 0.4 \& 0.4 \& 0.4 \& 0.3 \& 0.3 \& 0.4 <br>
\hline

 

\hline 0.6 \& 0.7 \& 0.6 \& 0.7 \& 0.7 \& 0.6 \& 0.6 \& 0.6 \& 0.7 \& 0.7 \& 0.6 \& 0.7 <br>
0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 \& 0.7 <br>
\hline

 

\hline 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 \& 0.4 <br>
0.4 <br>
\hline

 

\hline 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 \& 0.1 <br>
\hline
\end{tabular}

| 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |  | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | | 1.3 | 1.3 | 1.4 | 1.3 | 1.3 | 1.4 | 1.3 | 1.3 | 1.3 | 1.3 | 1.4 | 1.3 | 1.4 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0. | 0.8 | 0.8 | 0. | 0.7 | 0 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0 | | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0.7 | 0.8 | 0.8 | 0.8 | 0.7 | 0.7 | 0.7 | 0.8 | 0.7 | 0.7 | 0.7 | 0.8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.8 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 | 0.9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.9 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 196 | 209 | 197 | 209 | 188 | 174 | 189 | 152 | 209 | 192 | 203 | 199 | 162 | 164 | 207 | 192 | 198 | 184 | 213 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 128 | 151 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |



| 0.9 | 0.9 | 0.9 | 0.9 |
| :--- | :--- | :--- | :--- |
| 0.4 | 0.4 | 0.4 | 0 | | 0.4 | 0.4 | 0.4 |
| :--- | :--- | :--- |
| 0.4 |  |  |
| 0.8 | 0.8 | 0.8 | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- | :--- | | 1.0 | 1.0 | 1.0 | 1.0 |
| :--- | :--- | :--- | :--- |
| 0.5 | 0.5 | 0.5 | 0.5 | | 0.5 | 0.5 | 0.5 | 0.5 |
| :--- | :--- | :--- | :--- |
| 0.7 | 0.7 | 0.7 | 0.7 |
|  | 1.0 | .0 | 1.0 | | 1.0 | 1.0 | 1.0 |
| :--- | :--- | :--- |
| 1.0 |  |  |
| 0.8 | 0.8 | 0.8 |
| 0.8 | 0.8 |  | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- |
| 0.9 | 0.9 | 0.9 | 0.9 |
| 0.8 | 0.8 |  |  | | 0.9 | 0.9 | 0.9 |  |
| :--- | :--- | :--- | :--- |
| 0.8 | 0.8 | 0.8 | 0.8 |
| 0.8 | 0.8 | 0.8 | 0.8 | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- |
| 1.1 | 1.8 | 1. | 1.1 | | 1.1 | 1.1 | 1.1 | 1.1 |
| :--- | :--- | :--- | :--- |
| 1.0 | 1.0 | 1.0 | 1.0 | | 1.0 | 1.0 | 1.0 | 1.0 |
| :--- | :--- | :--- | :--- |
| 0.8 | 0.8 | 0.8 | 0.8 |
| 0. |  | 0.6 | 0.6 | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- | :--- |
| 0.6 | 0.6 | 0.6 | 0.6 |
| 0. | 0.7 |  |  | | 0.7 | 0.7 | 0.7 | 0.7 |
| :--- | :--- | :--- | :--- | :--- |
| 1.0 | 1.0 | 1.0 | 1.0 | | 1.0 | 1.0 | 1.0 | 1.0 |
| :---: | :---: | :---: | :---: |
| 1.2 | 1.2 | 1.2 | 1.2 | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- |
| 1.3 | 1.3 | 1.3 | 1.3 |
| 0.6 | 0.6 | 0.6 | 0.6 | | 0.6 | 0.6 | 0.6 | 0.6 |
| :--- | :--- | :--- | :--- |
| 0.8 | 0.7 | 0.7 | 0.7 |
|  | 1.1 | 1.1 | 1. | | 1.1 | 1.1 | 1.1 | 1.1 |
| :--- | :--- | :--- | :--- |
| 0.6 | 0.6 | 0.6 | 0.6 | | 0.6 | 0.6 | 0.6 | 0.6 |
| :--- | :--- | :--- | :--- |
| 0.9 | 0.9 | 0.9 | 0.9 |
| 0.7 | 0.7 | 0.7 | 0.7 | | 0.7 | 0.7 | 0.7 |
| :--- | :--- | :--- |
| 0.7 |  |  |
| 0.3 | 0.3 | 0.3 | | 0.3 | 0.3 | 0.3 | 0.3 |
| :--- | :--- | :--- | :--- |
| 0.8 | 0.8 | 0.8 | .8 | | 0.8 | 0.8 | 0.8 | 0.8 |
| :--- | :--- | :--- | :--- |
| 0.5 | 0.6 | 0.6 | 0.6 | | 0.5 | 0.6 | 0.6 | 0.6 |
| :--- | :--- | :--- | :--- |
| 0.7 | 0.7 | 0.7 | 0.7 | | 0.7 | 0.7 | 0.7 | 0.7 |
| :--- | :--- | :--- | :--- |
| 0.6 | 0.6 | 0.6 | 0.6 |
| 0. | 0.7 | 0.7 |  | | 0.6 | 0.6 | 0.6 |
| :--- | :--- | :--- |
| 0.7 | 0.7 | 0.7 |
| 0.7 |  |  |
| 0.7 | 0.7 | 0.7 | | 0.7 | 0.7 | 0.7 | 0.7 |
| :--- | :--- | :--- | :--- |
| 0.5 | 0.5 | 0.5 | 0.5 | | 0.5 | 0.5 | 0.5 | 0.5 |
| :--- | :--- | :--- | :--- |
| 0.4 | 0.4 | 0.4 | 0.4 |
| 0.2 | 0.2 | 0.2 | 0.3 | | 0.4 | 0.4 | 0.4 | 0.4 |
| :--- | :--- | :--- | :--- |
| 0.2 | 0.2 | 0.2 | 0.3 |
| 0.4 | 0.4 | 0.4 | 0.4 |
| 0.5 | .5 | 0.5 | 0.5 | | 0.4 | 0.4 | 0.4 | 0.4 |
| :---: | :---: | :---: | :---: |
| 0.5 | 0.5 | 0.5 | 0.5 |
| 0.4 | 0.4 | 0.4 | 0.4 | | 0.4 | 0.4 | 0.4 | 0.4 |
| :--- | :--- | :--- | :--- |
| 0.8 | 0.8 | 0.7 | 0.8 | | 0.4 | 0.8 | 0.7 | 0.8 |
| :--- | :--- | :--- | :--- |
| 0.4 | 0.4 | 0.4 | 0.3 | | 0.4 | 0.4 | 0.4 | 0.3 |
| :--- | :--- | :--- | :--- |
| 0.3 | 0.3 | 0.4 | 0.3 | | 0.3 | 0.3 | 0.4 | 0.3 |
| :--- | :--- | :--- | :--- |
| 0.4 | 0.3 | 0.4 | 0.4 |
| 0.7 | 0.4 |  |  | | 0.4 | 0.3 | 0.4 | 0.4 |
| :--- | :--- | :--- | :--- |
| 0.7 | 0.7 | 0.7 | 0.7 |
| 0.4 | 0.4 | 0.4 | 0.4 | | 0.4 | 0.4 | 0.4 | 0.4 |
| :--- | :--- | :--- | :--- |
| 0.1 | 0.1 | 0.1 | 0.1 |


| 0.7 | 0.7 | 0.7 | 0.7 |
| :---: | :---: | :---: | :---: |
| 1.3 | 1.3 | 1.3 | 1.3 |
| 0.7 | 0.7 | 0.7 | 0.7 |
| 0.9 | 0.9 | 0.9 | 0.9 |

$\qquad$

## 


$71(0.9)$
$68(0.4)$ 68 (0.4) 67 (0.8) 66 (1.0) $66(1.0)$

$64(0.5)$ | 64 (0.5) |
| :--- |
| $56(0.7)$ | 55 (1.0) $55(0.8)$ 54 (0.8) 49 (0.9) 49 (0.8) 48 (0.8) 48 (1.1) 48 (1.0) $48(0.8)$ 47 (0.6) 47 (0.7) 46 (1.0) 46 (1.2) 46 (0.8) 45 (1.3) 44 (0.6) 43 (0.7) 42 (1.1) 41 (0.6) $41(0.9)$ 39 (0.7) 37 (0.3) $37(0.8)$ $37(0.5)$ 33 (0.6) 33 (0.6) 32 (0.6) 31 (0.7) 29 (0.7) $28(0.5)$ 28 (0.4) 27 (0.2) 27 (0.4) 27 (0.5) $26(0.4)$ $26(0.4)$

$25(0.8)$
$25(0.4)$ 25 (0.4) 23 (0.3) Botswana 19 (0.3) Saudi Arabia 17 (0.7) South Africa 15 (0.4) Ghana International Avg. Benchmarking Participants Basque Country, Spain 47 (1.3) Indiana State, US
52 (0.7) Ontario Province, Can. 57 (0.9)

Singapore
Korea, Rep. of
Hong Kong, SAR
Chinese Taipei
Japan
Belgium (Flemish)
Netherlands
Hungary

## Estonia

Russian Federation
Slovak Republic

## Latvia

Australia
Malaysia
United States
Lithuania
Sweden
Scotland
England
Israel
New Zealand
Slovenia
Italy
Romania
Serbia
Bulgaria
Armenia
Cyprus
Moldova, Rep. of
Norway
Macedonia, Rep. of

## Lebanon

Jordan
Indonesia
Egypt
Iran, Islamic Rep. of
Bahrain
Tunisia
Chile
Palestinian Nat'l Auth.
Philippines
Morocco
$\square$
-
$\square$

## Countries

* Of the 194 items in the Mathematics test, some extended-response items were scored on a two-point scale, resulting in 215 total score points. Following item review, response categories were combined for a number of items, resulting in 213 score points.
() Standard errors for the average percent of correct responses on all items appear in parentheses. The matrix contains standard errors corresponding to the average percent correct responses based on TCMA subset of items, as displayed in Table C.1.

> Instructions:

Read across the row to compare that country's performance based on the test items included by each of the countries across the top. Read down the column under a country name to compare the performance of the country down the left on the items included by the country listed on the top. Read along the diagonal to compare performance for each different country based on its own decisions about the test items to include.

| Countries |
| :---: |
| Singapore |
| Hong Kong, SAR |
| Japan |
| Chinese Taipei |
| Belgium (Flemish) |
| Netherlands |
| Lithuania |
| Latvia |
| England |
| Russian Federation |
| Hungary |
| United States |
| Cyprus |
| Moldova, Rep. of |
| Italy |
| Australia |
| New Zealand |
| Scotland |
| Slovenia |
| Norway |
| Armenia |
| Iran, Islamic Rep. of |
| Philippines |
| Morocco |
| Tunisia |
| International Avg. |
| Benchmarking Participants |
| Indiana State, US |
| Ontario Province, Can. |
| Quebec Province, Can. |
| Number of Items (Score Points) Identified* |

* Of the 161 items in the Mathematics test, some extended-response items were scored on a twopoint scale, resulting in 169 total score points. Following item review, some items were deleted and response categories were combined for a number of items, resulting in 159 items and 166 score points.
() Standard errors for the average percent of correct responses on all items appear in parentheses. Th matrix contains standard errors corresponding to the average percent correct responses based on ICMA subset of items, as displayed in Table C. 1
items selected for the TCMA. For example, at the eighth grade, Singapore had the highest average percent correct on the test as a whole and on all of the different item selections, with Korea, Hong Kong SAR, and Chinese Taipei next in order of performance on practically all selections of items. Although there are some changes in the ordering of countries based on the items selected for the TCMA, most of these differences are within the boundaries of sampling error. As an example, consider the 197 score points selected by Cyprus. The students in Cyprus did a little better on these items than on the test as a whole, with 38 percent correct on these items, on average, compared with 37 percent correct on all items. However, most other countries also did better on these particular items, with an international average of 41 percent correct on the items selected by Cyprus. All 31 participants that performed better than Cyprus on the overall test also performed better on the items selected by Cyprus.

The TCMA results provide evidence that the TIMSS 2003 mathematics test provides a reasonable basis for comparing achievement of the participating countries and benchmarking entities. This result is not unexpected, since making the test as fair as possible was a major consideration in test development. The fact that the majority of countries indicated that most items were appropriate for their students means that the different average percent correct estimates were based on essentially the same items. Insofar as countries rejected items that would be difficult for their students, these items tended to be difficult for students in other countries as well. The analysis shows that omitting such items tends to improve the results for that country, but also tends to improve the results for all other countries, so that the overall pattern of results is largely unaffected.


# Appendix D <br> Percentiles and Standard Deviations of Mathematics Achievement 

| Countries | 5th Percentile | $\begin{aligned} & \text { 25th } \\ & \text { Percentile } \end{aligned}$ | 50th Percentile | 75th Percentile | $\begin{aligned} & \text { 95th } \\ & \text { Percentile } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | 330 (7.5) | 423 (5.1) | 483 (3.3) | 539 (3.2) | 605 (3.5) |
| Australia | 368 (10.4) | 450 (3.9) | 506 (3.7) | 561 (5.8) | 634 (6.6) |
| Bahrain | 277 (3.2) | 347 (1.5) | 402 (1.8) | 455 (2.2) | 525 (1.4) |
| Belgium (Flemish) | 398 (8.9) | 495 (3.7) | 545 (3.1) | 588 (2.8) | 643 (3.3) |
| Botswana | 251 (5.1) | 316 (3.0) | 365 (2.5) | 415 (2.7) | 487 (5.0) |
| Bulgaria | 333 (7.5) | 421 (5.5) | 478 (4.6) | 535 (4.6) | 611 (6.6) |
| Chile | 258 (4.5) | 328 (4.8) | 382 (3.4) | 441 (4.5) | 531 (4.9) |
| Chinese Taipei | 407 (6.0) | 518 (7.0) | 596 (4.6) | 657 (5.0) | 733 (6.0) |
| Cyprus | 321 (3.8) | 405 (3.4) | 463 (1.8) | 518(1.5) | 586 (1.6) |
| Egypt | 256 (3.0) | 341 (6.0) | 405(4.1) | 471 (3.7) | 560 (3.2) |
| England | 373 (5.3) | 445 (5.9) | 497 (5.9) | 552 (9.2) | 627 (5.6) |
| Estonia | 416 (4.8) | 484 (3.6) | 531 (4.0) | 577 (2.7) | 645 (4.0) |
| Ghana | 130 (5.8) | 213 (4.3) | 274(5.3) | 337 (7.3) | 430 (9.1) |
| Hong Kong, SAR | 455 (11.9) | 546 (4.0) | 593 (3.3) | 635 (3.0) | 691 (4.6) |
| Hungary | 398 (8.1) | 476 (2.9) | 531 (3.5) | $584(4.1)$ | 656 (4.2) |
| Indonesia | 266 (11.6) | 350 (7.9) | 411 (6.0) | 472 (4.0) | 558 (3.6) |
| Iran, Islamic Rep. of | 294 (4.8) | 360 (3.5) | 408 (3.0) | 461 (2.4) | 537 (6.2) |
| Israel | 353 (5.9) | 438 (4.8) | 498 (5.3) | 555 (3.5) | 630 (5.3) |
| Italy | 355 (6.0) | 432 (4.0) | 486 (2.9) | 537 (3.2) | 606 (5.0) |
| Japan | 433 (4.4) | 519 (2.0) | 572 (2.6) | 623 (2.2) | 697 (5.1) |
| Jordan | 279 (5.3) | 362 (4.1) | 427 (4.9) | 488 (5.0) | 567 (5.2) |
| Korea, Rep. of | 439 (3.1) | 537 (3.2) | 596 (2.5) | 647 (2.5) | 715(3.0) |
| Latvia | 386 (5.2) | 458 (5.2) | 510 (2.9) | 559 (3.5) | 625 (5.4) |
| Lebanon | 324 (3.4) | 387 (3.9) | 432 (3.7) | 479 (4.0) | 545 (5.8) |
| Lithuania | 370 (4.5) | 448 (2.9) | 503 (2.4) | 557 (4.0) | 628 (2.5) |
| Macedonia, Rep. of | 283 (4.8) | 376 (5.1) | 439 (2.9) | 497 (3.4) | $574(4.7)$ |
| Malaysia | 388 (3.7) | 455 (3.9) | 507 (5.5) | 562 (6.1) | 630 (5.3) |
| Moldova, Rep. of | 321 (5.8) | 405 (7.3) | 464(4.9) | 518 (4.4) | 585 (5.1) |
| Morocco | 275 (4.8) | 340 (3.0) | 387 (3.0) | 434 (3.0) | 497 (2.8) |
| Netherlands | 417 (8.4) | 488 (4.5) | 540 (5.8) | 587 (4.8) | 644 (6.8) |
| New Zealand | 364 (9.9) | 441 (5.2) | 495 (5.3) | 548 (7.1) | 623 (12.5) |
| Norway | 340 (5.2) | 414 (2.2) | 465 (3.3) | 511 (1.7) | 573 (2.4) |
| Palestinian Nat'l Auth. | 241 (5.2) | 326 (3.2) | 389 (4.1) | 455 (4.2) | 542 (5.4) |
| Philippines | 241 (3.6) | 316 (5.6) | 373 (6.4) | 437 (6.5) | 527 (8.0) |
| Romania | 321 (7.8) | 413 (4.6) | 479 (4.9) | 540 (4.9) | 619 (9.0) |
| Russian Federation | 381 (5.5) | 456 (4.2) | 509 (4.5) | 561 (4.0) | 632 (7.5) |
| Saudi Arabia | 204 (10.0) | 279 (6.6) | 331 (5.1) | 385 (4.5) | 460 (5.4) |
| Scotland | 368 (8.5) | 449 (5.0) | 501 (4.3) | 550 (3.9) | 615 (6.0) |
| Serbia | 326 (6.2) | 417 (4.8) | 479 (4.0) | 540 (3.1) | $618(4.8)$ |
| Singapore | 455 (6.6) | 556 (6.7) | 614(4.0) | 662 (3.5) | 723 (2.8) |
| Slovak Republic | 371 (6.5) | 453 (4.7) | 509 (3.9) | 564 (4.3) | 642 (4.2) |
| Slovenia | 375 (9.3) | 445 (2.4) | 492 (2.0) | 542 (1.6) | 610 (3.7) |
| South Africa | 117 (5.2) | 191 (3.5) | 248 (4.0) | 316 (7.5) | 484 (20.1) |
| Sweden | 378 (4.0) | 452 (4.3) | 501 (2.6) | 548 (2.9) | $614(6.3)$ |
| Tunisia | 316 (2.2) | 368 (2.4) | 407 (2.4) | 450 (2.6) | 515 (6.2) |
| United States | 369 (4.7) | 450 (2.9) | 505 (3.0) | 560 (3.5) | 635 (3.8) |
| Benchmarking Participants |  |  |  |  |  |
| Basque Country, Spain | 379 (6.0) | 444(4.3) | 488 (2.9) | 531 (4.2) | 591 (3.1) |
| Indiana State, US | 393 (4.2) | 461 (5.9) | 507 (4.1) | 555 (6.7) | 625 (6.3) |
| Ontario Province, Can. | 411 (7.1) | 476 (3.8) | 522 (3.9) | 567 (2.9) | $628(4.2)$ |
| Quebec Province, Can. | 449 (2.4) | 503 (3.6) | 542 (3.0) | 583 (4.3) | 640 (4.9) |

[^97]
## Exhibit D.1: Percentiles of Achievement in Mathematics



| Countries | 5th Percentile | $\begin{gathered} \text { 25th } \\ \text { Percentile } \end{gathered}$ | 50th Percentile | 75th Percentile | 95th Percentile |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Armenia | $305(4.7)$ | 400 (4.7) | 460 (3.3) | 516(4.5) | 594(5.8) |
| Australia | 359 (5.0) | 447 (5.8) | 504 (4.4) | 553 (4.0) | 625 (6.4) |
| Belgium (Flemish) | 451 (4.0) | 511 (2.5) | 552 (2.9) | 592 (2.0) | 644 (3.1) |
| Chinese Taipei | 455 (4.0) | 525 (1.9) | 567 (1.8) | 606 (2.2) | 663 (2.2) |
| Cyprus | 358 (3.3) | 454(4.4) | 516 (2.9) | 569 (2.0) | 641 (5.7) |
| England | 379 (9.5) | 474(3.6) | 536 (5.3) | 592 (3.3) | 667 (3.7) |
| Hong Kong, SAR | 466 (4.0) | 534 (2.9) | 578 (3.8) | 619 (3.4) | 674 (3.6) |
| Hungary | 393 (4.9) | 478 (5.0) | 534 (3.7) | 583 (3.4) | 647 (3.1) |
| Iran, Islamic Rep. of | 246 (6.8) | 330 (5.3) | 390 (5.0) | 450 (2.7) | 528 (4.3) |
| Italy | 362 (6.6) | 450 (4.5) | 507 (3.9) | 558 (4.6) | 632 (11.5) |
| Japan | 437 (3.6) | 518 (3.4) | 568 (1.7) | 615(1.4) | 680 (4.7) |
| Latvia | 407 (7.8) | 491 (3.8) | 540 (3.3) | 587 (2.8) | 647 (4.3) |
| Lithuania | 405 (3.6) | 487 (4.3) | 539 (3.1) | 585 (2.3) | 648 (4.3) |
| Moldova, Rep. of | 349 (11.5) | 449 (6.1) | 511 (5.4) | 566 (5.2) | 634 (7.0) |
| Morocco | 199 (9.7) | 283 (5.9) | 347 (6.8) | 412 (6.3) | 493 (2.5) |
| Netherlands | 448 (6.4) | 505 (2.3) | 542 (2.9) | 578 (1.5) | 627 (2.8) |
| New Zealand | 346 (4.7) | 438 (3.1) | 499 (2.9) | 553 (2.5) | 623 (3.2) |
| Norway | 310 (6.0) | 399 (3.1) | 456 (1.8) | 508 (3.7) | 574(4.4) |
| Philippines | 189 (11.0) | 280 (7.3) | 352 (6.8) | 431 (11.7) | 549 (21.6) |
| Russian Federation | 401 (13.7) | 479 (7.3) | 533 (6.0) | 586 (5.7) | 658 (6.6) |
| Scotland | 357 (4.7) | 441 (3.3) | 493 (3.9) | 544 (2.9) | 610 (5.4) |
| Singapore | 439 (13.4) | 546 (9.0) | 601 (5.1) | 652 (6.9) | 721 (7.0) |
| Slovenia | 343 (3.8) | 427 (2.7) | 485 (4.0) | 534 (2.9) | 598 (5.0) |
| Tunisia | 176 (7.9) | 269 (4.8) | 339 (5.0) | 409 (5.2) | 503 (5.4) |
| United States | 387 (3.3) | 467 (2.7) | 522 (4.0) | 572 (3.1) | 639 (3.4) |
| Benchmarking Participants |  |  |  |  |  |
| Indiana State, US | 421 (6.2) | 491 (4.2) | 535 (2.2) | 577 (3.0) | 638 (9.4) |
| Ontario Province, Can. | 391 (4.3) | 465 (3.7) | 513 (3.7) | 559 (5.8) | 626 (7.1) |
| Quebec Province, Can. | 393 (3.2) | 464(2.4) | 509 (1.9) | 551 (3.7) | 609 (2.8) |

[^98]| Countries | Overall |  | Girls |  | Boys |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Standard <br> Deviation | Mean | Standard <br> Deviation | Mean | Standard <br> Deviation |
| Armenia | 478 (3.0) | 84 (1.4) | 483 (3.3) | 81 (1.6) | 473 (3.4) | 86 (2.0) |
| Australia | 505 (4.6) | 82 (3.2) | 499 (5.8) | 78 (3.0) | 511 (5.8) | 84 (4.3) |
| Bahrain | 401 (1.7) | 76 (0.9) | 417 (2.4) | 70 (1.3) | 385 (2.4) | 79 (1.3) |
| Belgium (Flemish) | 537 (2.8) | 73 (2.6) | 532 (3.5) | 72 (3.2) | 542 (3.8) | 74 (3.0) |
| Botswana | 366 (2.6) | 72 (1.5) | 368 (2.6) | 71 (1.7) | 365 (2.9) | 72 (1.7) |
| Bulgaria | 476 (4.3) | 84 (2.3) | 476 (5.5) | 84 (3.0) | 477 (4.3) | 84 (2.5) |
| Chile | 387 (3.3) | 83 (1.9) | 379 (3.5) | 81 (1.9) | 394 (4.3) | 85 (2.5) |
| Chinese Taipei | 585 (4.6) | 100 (2.2) | 589 (4.9) | 94 (2.1) | 582 (5.2) | 105 (2.7) |
| Cyprus | 459 (1.7) | 81 (1.3) | 467 (1.9) | 78 (1.7) | 452 (2.3) | 84 (1.6) |
| Egypt | 406 (3.5) | 93 (1.5) | 407 (4.4) | 90 (1.9) | 406 (5.0) | 95 (2.0) |
| England | 498 (4.7) | 77 (3.1) | 499(5.3) | 76 (2.8) | 498 (5.8) | 78 (4.3) |
| Estonia | 531 (3.0) | 69 (1.6) | 532 (3.4) | 69 (2.1) | 530 (3.3) | 69 (1.8) |
| Ghana | 276 (4.7) | 91 (2.3) | 266 (5.1) | 89 (2.6) | 283 (4.9) | 92 (2.6) |
| Hong Kong, SAR | 586 (3.3) | 72 (3.2) | 587 (3.8) | 70 (3.1) | 585 (4.6) | 74 (3.9) |
| Hungary | 529 (3.2) | 80 (2.3) | 526 (3.7) | 78 (2.6) | 533 (3.5) | 81 (2.6) |
| Indonesia | 411 (4.8) | 89 (2.6) | 411 (4.9) | 88 (3.2) | 410 (5.3) | 89 (2.6) |
| Iran, Islamic Rep. of | 411 (2.4) | 74 (1.4) | 417 (4.3) | 71 (1.9) | 408(4.2) | 76 (2.6) |
| Israel | 496 (3.4) | 85 (1.8) | 492 (3.3) | 80 (1.8) | 500 (4.5) | 89 (2.6) |
| Italy | 484 (3.2) | 77 (1.8) | 481 (3.0) | 74 (2.0) | 486 (3.9) | 79 (2.2) |
| Japan | 570 (2.1) | 80 (1.3) | 569 (4.0) | 76 (3.6) | 571 (3.6) | 83 (2.2) |
| Jordan | 424 (4.1) | 89 (1.8) | $438(4.6)$ | 86 (2.3) | 411 (5.8) | 90 (2.7) |
| Korea, Rep. of | 589 (2.2) | 84 (1.3) | 586 (2.7) | 82 (1.6) | 592 (2.6) | 86 (1.4) |
| Latvia | 508 (3.2) | 73 (1.4) | 511 (3.3) | 70 (1.7) | 506 (3.7) | 76 (1.9) |
| Lebanon | 433 (3.1) | 67 (1.6) | 429 (3.6) | 66 (1.9) | 439 (3.9) | 67 (2.1) |
| Lithuania | 502 (2.5) | 78 (1.3) | 503 (2.9) | 77 (1.8) | 499 (3.0) | 82 (1.6) |
| Macedonia, Rep. of | 435 (3.5) | 88 (2.3) | 439 (4.0) | 86 (2.8) | 431 (3.9) | 90 (2.5) |
| Malaysia | 508 (4.1) | 74 (2.2) | 512 (4.7) | 73 (2.5) | 505 (4.5) | 76 (2.3) |
| Moldova, Rep. of | 460 (4.0) | 81 (1.7) | 465 (4.1) | 78 (1.8) | 455 (4.8) | 82 (2.1) |
| Morocco | 387 (2.5) | 68 (1.0) | 381 (2.8) | 68 (1.4) | 393 (3.0) | 68 (1.3) |
| Netherlands | 536 (3.8) | 69 (2.8) | 533 (4.1) | 69 (3.0) | 540 (4.5) | 70 (3.0) |
| New Zealand | 494 (5.3) | 78 (3.6) | 495(4.8) | 75 (3.5) | 493 (7.0) | 82 (4.2) |
| Norway | 461 (2.5) | 71 (1.3) | 463 (2.7) | 69 (2.0) | 460 (3.0) | 72 (1.5) |
| Palestinian Nat'l Auth. | 390 (3.1) | 92 (1.5) | 394(3.9) | 91 (1.9) | 386 (4.7) | 92 (1.9) |
| Philippines | 378 (5.2) | 87 (2.6) | 383 (5.2) | 86 (2.5) | 370 (5.8) | 89 (3.3) |
| Romania | 475 (4.8) | 90 (1.7) | 477 (5.1) | 88 (1.7) | 473 (5.0) | 92 (2.5) |
| Russian Federation | 508 (3.7) | 77 (1.4) | 510 (3.5) | 74 (1.4) | 507 (4.4) | 79 (2.1) |
| Saudi Arabia | 332 (4.6) | 78 (2.6) | 326 (7.9) | 75 (4.6) | 336(5.5) | 81 (2.7) |
| Scotland | 498 (3.7) | 75 (2.3) | 500 (4.3) | 72 (2.7) | 495 (3.8) | 77 (2.4) |
| Serbia | 477 (2.6) | 89 (1.4) | 480 (2.9) | 86 (1.9) | 473 (2.9) | 92 (1.8) |
| Singapore | 605 (3.6) | 80 (2.4) | 611 (3.3) | 75 (2.6) | 601 (4.3) | 84 (2.6) |
| Slovak Republic | 508 (3.3) | 82 (1.7) | 508(3.4) | 79 (1.9) | 508 (4.0) | 85 (2.2) |
| Slovenia | 493 (2.2) | 71 (1.5) | 495 (2.6) | 68 (1.6) | 491 (2.6) | 74 (1.9) |
| South Africa | 264 (5.5) | 107 (5.1) | 262 (6.2) | 105 (6.0) | 264 (6.4) | 110 (5.8) |
| Sweden | 499 (2.6) | 71 (1.7) | 499 (3.0) | 70 (1.9) | 499 (2.7) | 72 (2.0) |
| Tunisia | 410 (2.2) | 60 (1.3) | 399 (2.6) | 60 (1.6) | 423 (2.2) | 58 (1.4) |
| United States | 504 (3.3) | 80 (1.8) | 502 (3.4) | 78 (1.9) | 507 (3.5) | 82 (2.0) |
| Benchmarking Participants |  |  |  |  |  |  |
| Basque Country, Spain | 487 (2.7) | 64 (1.3) | 490 (2.5) | 60 (1.4) | 484 (3.7) | 68 (2.0) |
| Indiana State, US | 508 (5.2) | 70 (3.0) | 502 (5.1) | 68 (3.2) | 514 (5.8) | 72 (3.1) |
| Ontario Province, Can. | 521 (3.1) | 66 (1.1) | 520 (3.4) | 65 (1.5) | 522 (3.4) | 67 (1.4) |
| Quebec Province, Can. | 543 (3.0) | 58 (1.8) | 540 (3.7) | 57 (2.1) | 546 (3.3) | 59 (2.0) |

[^99]
## Exhibit D.2: Standard Deviations of Achievement in Mathematics



| Countries | Overall |  | Girls |  | Boys |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Standard Deviation | Mean | Standard Deviation | Mean | Standard Deviation |
| Armenia | 456 (3.5) | 87 (1.9) | 462 (3.7) | 84 (2.2) | 450 (3.8) | 89 (1.9) |
| Australia | 499 (3.9) | 81 (2.1) | 497 (4.5) | 79 (2.5) | 500 (4.3) | 83 (2.6) |
| Belgium (Flemish) | 551 (1.8) | 59 (1.1) | 549(1.8) | 57 (1.1) | 552 (2.5) | 60 (1.7) |
| Chinese Taipei | 564 (1.8) | 63 (1.1) | 564(1.7) | 59 (1.2) | 564 (2.1) | 66 (1.5) |
| Cyprus | 510 (2.4) | 85 (1.3) | 505 (2.7) | 82 (1.9) | 514 (2.9) | 88 (1.5) |
| England | 531 (3.7) | 87 (1.9) | 530 (3.9) | 85 (2.1) | 532 (4.5) | 90 (2.4) |
| Hong Kong, SAR | 575(3.2) | 63 (1.5) | 575 (3.4) | 60 (1.7) | 575 (3.4) | 66 (1.7) |
| Hungary | 529 (3.1) | 77 (2.0) | 527 (3.8) | 77 (2.6) | 530 (3.3) | 78 (2.0) |
| Iran, Islamic Rep. of | 389 (4.2) | 86 (2.1) | 394 (6.5) | 83 (2.9) | 386 (5.5) | 87 (2.6) |
| Italy | 503 (3.7) | 82 (2.2) | 498 (4.1) | 80 (2.9) | 507 (3.7) | 83 (2.0) |
| Japan | 565 (1.6) | 74 (1.0) | 563 (1.8) | 69 (1.3) | 566 (2.1) | 78 (1.4) |
| Latvia | 536 (2.8) | 73 (1.5) | 536 (2.9) | 69 (1.9) | 536 (3.5) | 75 (2.1) |
| Lithuania | 534 (2.8) | 74 (1.7) | 535 (3.5) | 73 (2.3) | 536 (3.2) | 76 (1.9) |
| Moldova, Rep. of | 504 (4.9) | 87 (3.2) | 510 (5.2) | 87 (3.9) | 499 (5.1) | 87 (3.5) |
| Morocco | 347 (5.1) | 90 (1.9) | 344 (6.1) | 91 (2.1) | 350 (5.1) | 89 (2.5) |
| Netherlands | 540 (2.1) | 55 (1.5) | 537 (2.7) | 55 (2.2) | 543 (2.2) | 54 (1.6) |
| New Zealand | 493 (2.2) | 84 (1.8) | 493 (2.7) | 82 (2.3) | 494 (2.4) | 86 (1.8) |
| Norway | 451 (2.3) | 80 (1.6) | 449 (2.7) | 78 (1.8) | 454 (2.7) | 82 (1.9) |
| Philippines | 358(7.9) | 110 (5.9) | 364 (9.2) | 111 (6.6) | 352 (7.0) | $108(5.3)$ |
| Russian Federation | 532 (4.7) | 78 (2.0) | 530 (5.4) | 78 (2.3) | 534 (4.7) | 78 (2.4) |
| Scotland | 490 (3.3) | 78 (1.8) | 485 (3.2) | 74 (1.9) | 496 (4.4) | 80 (2.8) |
| Singapore | 594 (5.6) | 84 (3.2) | 599 (5.5) | 80 (3.0) | 590 (6.2) | 88 (3.7) |
| Slovenia | 479 (2.6) | 78 (1.3) | 477 (3.0) | 75 (1.8) | 481 (3.5) | 81 (1.9) |
| Tunisia | 339 (4.7) | 100 (2.5) | 342 (5.0) | 98 (2.7) | 337 (4.9) | 101 (2.6) |
| United States | 518(2.4) | 76 (1.0) | 514(2.4) | 74 (1.2) | 522 (2.7) | 78 (1.3) |
| Benchmarking Participants |  |  |  |  |  |  |
| Indiana State, US | 533 (2.8) | 65 (2.1) | 532 (3.1) | 62 (2.1) | 534 (3.4) | 69 (2.5) |
| Ontario Province, Can. | 511 (3.8) | 71 (2.0) | 505 (3.6) | 69 (1.7) | 517 (4.7) | 72 (2.6) |
| Quebec Province, Can. | 506 (2.4) | 65 (1.2) | 502 (2.7) | 64 (1.5) | 509 (2.8) | 66 (1.4) |

[^100]

## Appendix E

## Descriptions of Mathematics Items at Each Benchmark

## Items at Low International Benchmark (400)

## Number

M05_02* Solves a word problem by adding numbers with up to three decimal places.
M06_07* Multiplies a two-place decimal by a three-place decimal.
M06_11 Solves a word problem involving a proportion with unit ratio.
M06_11* Solves a word problem involving a proportion with unit ratio.
M13_08 Selects two-place decimal closest to a given whole number.

## Measurement

M10_06 Selects the most appropriate metric unit to measure a large area.

## Data

M12_13A Selects the appropriate line on a graph and reads information from it.

## Items at Intermediate International Benchmark (475)

## Number

M03_04 Arranges four given digits in descending and ascending order and finds the difference between those two numbers.
M04_05 Solves a word problem involving subtraction of a two-place decimal number from another.
M04_06 Writes a fraction less than a given fraction.
M05_01 Identifies a circular model of a fraction that best approximates a given rectangular model of the same fraction.
M05_02 Solves a word problem by adding numbers with up to three decimal places.
M05_06 Selects the approximate quantity remaining after an amount is decreased by a given percent.
M06_03 Selects the smallest fraction from a set of familiar fractions.
M06_12* Solves a word problem about distance and time by finding the missing term in a proportion.
M10_01 Solves a word problem involving addition and multiplication of two-digit whole numbers.
M11_01 Identifies the decimal number that is equivalent to the sum of two fractions whose denominators are powers of ten.
M13_01 Uses knowledge of exponential notation to select approximations to two squared whole numbers.
M14_01 Rounds two-place decimals to whole numbers.

## Algebra

M01_02 Using properties of a balance, reasons to find an unknown weight (mass).
M01_10 Solves equation for missing number in a proportion.
M02_12 Selects the formula satisfied by the given values of the variables.
M03_01 Solves problem by interpreting information from a graph of two intersecting lines.

[^101]Items at Intermediate International Benchmark (475) - Continued

## Algebra - Continued

M08_04 Selects the rule expressed in words that generates successive terms in a given number pattern.
M08_05 Solves a linear equation in one variable.
M08_13A Identifies the straight line graph modeling a situation described in words.
M08_13B Interprets two straight line graphs and uses their intersection to solve a problem.
M12_04 Knows the meaning of a simple algebraic expression involving multiplication and addition.
M12_05 Identifies the algebraic expression that represents a situation, involving addition and multiplication.
M14_03 Extends number patterns derived from a sequence of geometric shapes.

## Measurement

M01_08 Identifies an unlabeled midway point on a number line marked in tenths.
M04_11A Finds a fraction of a given area of an irregular figure composed of squares of equal sides.
M06_01 Reads the value indicated by an unlabeled tick mark on a circular scale.
M07_05 Solves a word problem by comparing distances on a map drawn to scale with a given distance.

## Geometry

M02_03 Identifies corresponding parts of congruent trapezoids.
M05_03 Identifies the diagrammatic representation of a three-dimensional object after rotation.
M08_10 Uses properties of an isosceles triangle to identify the coordinates of a point on a grid.
M09_10 Divides an isosceles triangle in to two congruent triangles.
M09_12 Recognizes a net of a triangular prism.
M09_13 Locates a point with given coordinates in the Cartesian plane.
M11_11 Given a net of three-dimensional object, completes a two-dimensional drawing of it from a specific viewpoint.
M13_04 Uses a concept of line symmetry to complete a tiling pattern.

## Data

M01_06 Calculates and compares the averages of two sets of data.
M02_02 Reads and interprets information from a pie graph.
M02_09 Solves a comparison problem by associating elements of a bar graph with a verbal description.
M06_02 Recognizes that the probability of an outcome of a single event is inversely related to the number of elements in the population of events.
M06_08 Given a table of values for two variables, selects the graph that could represent the given data.
M11_13 Constructs and labels a pie chart representing a given situation.

## Items at High International Benchmark (550)

## Number

M01_01 Finds 4/5 of a region divided into 10 equal parts.
M01_04 Solves a word problem by finding the missing term in a proportion.
M01_11 Selects a fraction representing the comparison of part to whole, given each of two parts in a word-problem setting.
M01_13 Identifies a percent equivalent to a given fraction with a denominator that is a factor of 100 .
M01_14 Demonstrates understanding of the effect of operations involving a negative integer by identifying the largest number produced.
M02_10 Selects the statement that describes the effect of adding the same amount to both terms of a ratio.
M02_11 Estimates the product of a multiple of 1000 and a two-digit number in a word problem involving knowledge of units of time.
M03_03 Identifies the fraction of an hour representing a time interval.
M03_10 Rounds a four-place decimal to the nearest hundredth.
M03_15 Solves a one-step word problem involving division of a whole number by a unit fraction.
M04_02 Solves a multi-step word problem involving multiplication of whole numbers by fractions.
M05_09 Adds three fractions with denominators less than 10.
M06_07 Multiplies a two-place decimal by a three-place decimal.
M06_12 Solves a word problem about distance and time by finding the missing term in a proportion.
M06_13 Identifies the number that gives a specified result when divided by a given negative integer.
M06_13* Identifies the number that gives a specified result when divided by a given negative integer.
M08_01 Solves a word problem by determining a number between two given numbers that is divisible by only one of two other given numbers.
M09_03 Calculates the new price of an item given the percent increase in price.
M09_08 Solves a word problem with decimals involving a proportion.
M12_01 Solves a word problem by using the patterns in a two-column table to determine the number in the second column that would corresponds to a number midway between two entries in the first column.
M13_03 Identifies proportional share of an amount divided into three unequal parts.
M13_09 Determines the simplified ratio of shaded to unshaded parts of a shape.
M14_07 Identifies the prime factor of a given number.

## Algebra

M01_12
Finds the value of an algebraic expression involving multiplication of negative integers.
M02_05 Finds a specified term in a sequence given the first three terms pictorially.
M02_07 Subtracts algebraic fractions with the same numeric denominator.
M03_05 Identifies the linear relationship between the first and second terms in a set of ordered pairs.
M03_13 Solves a linear equation involving parentheses.
M04_10A Given a sequence of diagrams growing in two dimensions and a partially completed table, finds the next two terms in the table.

## Items at High International Benchmark (550) - Continued

## Algebra - Continued

M07_02 Recognizes the product of two algebraic terms in one variable that involve exponents.
M07_10 Identifies the linear equation represented by a set of ordered pairs given in a table.
M10_04 Solves a simultaneous linear equations.
M11_05 Identifies the algebraic expression that represents a situation involving the sum of a constant term and a product.

M11_06 Uses a formula to determine the value of one variable given the value of the other.
M12_12 Identifies the quantity that satisfies two inequalities represented by balances.
M13_05 Extends a geometric tiling pattern to identify the orientation of a tile.
M13_10 Simplifies an algebraic expression combining like terms.
M13_11 Solves a pair of simultaneous linear equations.
M14_09 Given an interval containing a number, determines the interval containing the sum of that number and a whole number.

## Measurement

M01_03 Given a length rounded to the nearest centimeter, identifies what the actual length could have been in centimeters to one decimal place.
M02_01 Compares volume by visualizing and counting cubes.
M03_12 Given the start time, and the duration of an event expressed as a fraction of an hour, determines the end time.
M04_07 Finds the area between two rectangles when one is inside the other and their sides are parallel.
M04_11B Finds the length of a side of a square, given that its area is a square number.
M05_05 Finds the perimeter of a square given that its area is a square number less than 150.
M05_12 Finds the area of a triangle, on the same base and with the same height as a square, when the length of a side of the square is known.
M07_04 Calculates the volume of a rectangular prism by using appropriate measures from its net.
M08_08 Calculates the area of an irregular figure formed by two rectangles.
M09_07A Solves a word problem to find average speed given distance and time.
M09_09 Given two touching circles of equal radius, finds the area of rectangle that encloses them.
M11_08 Given the area of a square, finds its perimeter.
M11_09 Determines the number of cubes needed to fill a hole in a given shape.
M13_12 Identifies the appropriate unit measure for an area.

## Geometry

M01_05 Identifies pairs of congruent triangles.
M01_09 Solves a problem involving adjacent and vertical angles.
M03_02 Uses properties of congruent triangles to find the measure of an angle.

## Items at High International Benchmark (550) - Continued

## Geometry - Continued

M03_09 Given two parallel lines cut by a transversal, selects a pair of supplementary angles.
M03_14 Selects the center of rotation when shown a diagram of a triangle and its image under a quarter turn.
M06_06 Uses knowledge of a straight angle to find the measure of an angle.
M06_14 Determines the measure of the missing angle in a right triangle.
M06_15 Uses properties of angles to draw and label a figure.
M07_09 Uses the properties of a triangle and regular hexagon to find the measure of an angle.
M09_11 Identifies a triangle similar to a specific triangle given the lengths of all sides.
M11_12 Identifies the transformations used to produce a sequence of figure.
M12_08 Visualizes the unfolded shape of a figure shown on a folded piece of paper and uses property of triangles to identify the shape.

## Data

M01_07 Reads data from a frequency table to solve a problem.
M03_11 In a word problem, when given the possible number of outcomes and the probability of successful outcomes, solves for the number of successful outcomes.
M04_09 Given the set of possible outcomes expressed as fractions of all outcomes, recognizes that probability is associated with the size of a fraction.
M05_07 In a word problem, when given the possible number of outcomes and the probability of successful outcomes, solves for the number of successful outcomes.
M07_07C Draws conclusions from data in a table.
M07_08 Compares and integrates several sets of data to determine which meet given conditions.
M08_13C Reads values from two straight line graphs to solve a problem.
M09_14 Uses the size of a group with a given characteristic in a sample to estimate the size of group with that characteristic in a population.
M11_14 Identifies the statement that best describes the relative likelihood of two events.
M12_13C Selects the appropriate line on a graph and determines the interval where the greatest change occurs.
M14_08 Uses percentages given in a pie chart to solve a problem.

## Items at Advanced International Benchmark (625)

## Number

M02_04 Identifies the pair of numbers satisfying given conditions involving ordering integers, decimals, and common fractions.
M02_13 Orders a set of decimals of up to three decimal places.
M02_14 Multiplies and adds fractions with different denominators in the correct order.
M03_08 Finds the percent change given the original and the new quantities.
M04_12 Solves a word problem involving multiplication and subtraction of decimals.

Number - Continued
M05_11B Given the dimensions of two rectangles, expresses the ratio of their areas.
M06_05 Given the total number and the ratio of the two parts, finds the value of one part.
M06_09 Selects appropriate data to solve a problem involving operations with fractions that have unlike denominators.
M06_10 Solves a word problem involving multiplication of a proper fraction with improper fraction.
M07_01 Identifies equivalent ratios in a problem setting.
M08_02 Identifies a procedure for subtracting fractions with unlike denominators.
M08_03 Given the total number and the ratio of the two parts, finds the value of one part.
M08_12 Given the original and reduced prices, finds the percentage reduction.
M09_01 Solves a word problem involving inverse operations and decimal place value.
M09_02 Solves a multi-step problem involving computing with whole numbers and rounding up.
M10_02 Computes with integers using order of operations.
M11_03 Solves a problem involving a fraction of a whole number of currency units.
M12_02 Converts a mixed number to a decimal rounded to two places.
M13_02 Uses the distributive property to recognize two different representations of a number.
M13_07 Solves a multi-step non-routine problem involving percents.

## Algebra

M04_04 Identifies numbers common to two different arithmetic sequences.
M04_10B Knowing the first five terms of a sequence growing in one dimension, finds the seventh term.
M04_10C Generalizing from the first several terms of a sequence growing in two dimensions, explains a way to find a specified term, e.g. the 50th.
M05_04 Solves a linear inequality involving a fraction.
M08_06 Identifies an algebraic expression to model a situation.
M09_04 Identifies algebraic expression that represents a situation involving division.
M09_05 Given a linear equation in which $y$ is expressed in terms of $x$, solves for $x$.
M09_06 Writes a pair of simultaneous equations in two unknowns to model a situation.
M10_03 Evaluates an algebraic expression by using an equivalent form and substituting given values.
M10_05 Evaluates an algebraic expression by using an equivalent form and substituting given values.
M11_04 Identifies a diagram that models addition of two like algebraic terms.
M12_03 Adds three simple algebraic rational expressions with unlike numerical denominators.
M12_09 Identifies the sum of three consecutive whole numbers given the middle number in general terms.

## Items at Advanced International Benchmark (625) - Continued

## Algebra - Continued

M14_04A Extends number patterns in a table to identify the row whose entries solve the problem.
M14_04B Extends number patterns in a table to identify the row whose entries solve the problem.
M14_04C Extends number patterns in a table to identify the row whose entries solve the problem.

## Measurement

M02_08 From a set of times expressed variously in days, hours, minutes, and seconds, determines which is least.

M03_06 Identifies the length of a rectangle given its perimeter and width.
M04_03 Applies knowledge of number of milliliters in a liter to solve a word problem.
M04_11C Finds the perimeter of a figure made up of squares with known length of sides.
M05_11A Uses computation with fractions to find the length and width of a rectangle and draws and labels that rectangle on a grid.

M09_07B Solves a multi-step problem involving time, distance, and average speed.
M10_10 Solves a non-routine problem involving the number of spheres that will fit in a rectangular box.
M11_07 Uses information about the lengths of segments on a line to determine the distance between their midpoints.

M12_06 Uses knowledge of time, clocks, and angles to solve a problem.
M12_07 Determines the area of a trapezoid inscribed in a triangle.

## Geometry

M01_15 Determines the exterior angle of a regular hexagon.
M02_15 Solves a problem involving measures of overlapping angles.
M04_08 Given only the coordinates of two points on the line, selects the coordinates of a third point on that line.

M05_08 Uses properties of congruent triangles and the sum of the angles of a triangle to find the measure of an angle.
M06_04 Identifies the image of a triangle under a rotation about a point in the plane.
M08_09 Solves a problem involving angle bisectors and angles at a point on a straight line.
M10_11 Recognizes that arcs of equal radius can generate an equilateral triangle.
M11_10 Identifies the justification that a triangle is a right triangle using Pythagorean relationship.
M12_10 Applies properties of interior and exterior angles of a triangle to find an unknown angle in overlapping triangles.
M14_06 Uses knowledge of interior angles of a triangle to determine the angle sum of a given polygon, showing calculations.

## Data

M03_07 On a given graph, interpolates to find a value between graduations on one axis matching a given value on the other axis.
M07_07A Completes a table by interpreting several time tables to identify times that meet a given set of conditions.

## Items at Advanced International Benchmark (625) - Continued

## Data - Continued

M07_07B Derives information from given timetables to complete a table for a specified journey and check that it meets given conditions.
M08_11 Uses experimental data and an understanding of probability to draw the spinner that could have produced the data.
M10_07 Interprets data from a table, draws and justifies conclusions.
M12_11 Given a spinner, identifies the frequency of a particular outcome.
M12_13B Interprets information from a graph to determine an average.

## Items Above the Advanced International Benchmark (625)

## Number

M07_06 Calculates total costs for each of two groups given different unit costs and discounts.
M11_02 Given two points on a number line representing unspecified fractions, identifies the point that represents their product.

## Algebra

M02_06 Selects an algebraic expression to answer a question about a set of linked verbal statements.
M04_01 Identifies what the variable represents in an equation for a given situation.
M07_03 Generalizes a number sequence based on a geometric pattern to find the term which produces given sum of sequence and show calculations.
M14_05 Finds the general term, express algebraically for related number patterns.

## Measurement

M05_10 Estimates the total time in minutes for an event made up of a series of events, each given in minutes and seconds.
M08_07 Uses knowledge of area of a circle and of average rate to solve a problem.

## Geometry

M13_06 Completes a geometric tiling pattern with two given lines of symmetry using letters to represent the orientation of the tiles.

## Data

M10_08 Interprets the data from a table to make calculations to solve a problem.
M10_09 Interprets the data from a table to make calculations to solve a problem.
M14_02 Solves a problem involving extrapolation of the data shown in a double bar graph.

## Items at Low International Benchmark (400)

## Number

M01_06 Recognizes the hundreds place in a four-digit number.
M01_11 Translates between a numeric and verbal representation of a four-digit number.
M03_04 Translates between standard and expanded notation of three-digit whole numbers.
M04_01 Multiplies a two-digit by a one-digit whole number.
M08_01 Identifies the difference between two fractions with the same denominator.
M11_01 Adds a four-digit and three-digit whole number.
M14_05 Solves a word problem involving addition of three-digit whole numbers.

## Patterns and Relationships

M12_04 Finds the missing number in a number sentence involving multiplication of one-digit whole numbers.

## Measurement

M02_13 Compares areas by counting squares.
M04_06 Given the base, draws a triangle on a grid whose other two sides are each the same length.

## Geometry

M02_03
Identifies two figures that have the same size and shape.
M02_10
Knows that every triangle has three sides.
M05_09
Identifies two triangles with the same size and shape in a complex figure.
M08_10 Recognizes the triangles in a set of polygons.
M10_08B Draws a line to divide one rectangle into two rectangles.

## Data

M01_01 Reads information from a simple bar graph.
M02_01 Reads information from a simple bar graph.

## Items at Intermediate International Benchmark (475)

## Number

M01_03 Recognizes a familiar fraction represented by a figure with shaded parts (region model).
M01_04 Recognizes multiplication as the appropriate operation in a one-step word problem (single-digit).
M02_04 Subtracts two decimals involving hundredths with regrouping over 0.
M02_08 Translates from a form of expanded notation to a standard notation for a five-digit number.
M02_11 Solves a one-step word problem involving multiplication of a three-digit by a one-digit number requiring regrouping.

Items at Intermediate International Benchmark (475) - Continued
Number - Continued
M02_12 Recognizes a pictorial representation of ones, tens, and hundreds and can identify the standard numeral.
M03_05 Adds decimal numbers involving tenths.
M03_06 Recognizes one-half of a set of objects.
M03_10 Recognizes inequality symbols and can choose the largest of two three-digit numbers.
M04_02 Identifies the appropriate operation to solve a word problem involving division.
M07_01 Identifies the appropriate operation to solve a word problem involving multiplication.
M09_01 Labels a point associated with a whole number on a number line.
M09_02 Uses knowledge of whole number place value to solve a word problem involving addition of a three-digit and a four-digit number.
M09_03 Identifies the fraction that represents a given part-whole situation.
M10_01 Divides a three digit by a one-digit whole number.
M10_04 Solves a word problem involving multiplication of a two-digit by a one-digit whole number.
M13_03 Solves a word problem involving finding a missing three-digit addend.
M14_01A Selects appropriate information and uses it to solve a simple proportion problem.

## Patterns and Relationships

M03_11 Identifies next terms in an alternating number pattern involving counting forward and backward by ones.
M04_04 Identifies the value that extends a pattern of time.
M04_05 Identifies a number sentence that represents a situation involving subtraction.
M11_05 Selects the expression that represents a situation involving addition.
M12_03 Generalizes from the first several terms of a numeric sequence to select another number that is also in the sequence.
M12_06B Extends a numeric sequence based on a geometric pattern.

## Measurement

M01_05 Counts weeks forward from a given date on a calendar.
M01_10 Selects a reasonable metric weight (mass) for an adult.
M05_08 Solves a measurement word problem involving subtraction of two-digit numbers.
M08_06 Recognizes that area does not change when the parts of a figure are rearranged.
M08_09 Recognizes the inverse relationship between size of a unit shown in the figure and the number of units require to cover an area.

Items at Intermediate International Benchmark (475) - Continued

## Geometry

M04_08 Draws a line parallel to a given line on a grid.
M04_09 Identifies and names common geometric shapes in a picture.
M10_08A Draws a line to divide one rectangle into two triangles.
M11_11 Identifies a pattern generated by quarter turns clockwise.
M12_10 Locates a point on an informal coordinate grid and identifies the moves to get there.
M14_06 Identifies a three-dimensional object given the pictorial representation of its faces.

## Data

M02_06 Locates data in a two-way table.
M03_01 Solves a comparison problem by associating elements of a bar graph with a verbal description.
M04_10 Completes a bar graph based on the solution of a word problem.
M05_11 Identifies the pie chart that matches the information shown in a table.
M06_10 Completes a two-by-two table to summarize information.
M07_09 Uses information to identify the number of symbols needed to complete a pictograph when the symbol represents more than one.
M08_12 Identifies the pie chart that matches a given bar graph.
M11_12 Completes a bar graph that represents a table of data.

## Items at High International Benchmark (550)

## Number

M01_07 Rounds a three-digit whole number to the nearest hundred.
M02_05 Recognizes the figure that illustrates a simple ratio.
M02_07 Solves word problem involving 1/2 and 1/4.
M03_03 Selects the number sentence that provides the best estimate of which is closest to the actual product of two two-digit numbers.
M03_07
Solves two-step word problem using doubling and adding.
M03_12 Understands tens place value and can translate between verbal and numeric representations.
M04_03 Solves a word problem by finding a fractional part of a collection of objects.
M05_01 Solves a word problem involving division of a three digit by a one-digit whole number.
M05_02 Determines the missing digit to give a specified difference in a three-digit subtraction problem.
M07_02 Solves a word problem involving division of a three-digit by a one-digit whole number.
M07_07 Solves a multi-step word problem involving addition and multiplication of whole numbers.
M08_03 Selects two-place decimal closest to a given whole number.

## Items at High International Benchmark (550) - Continued

## Number - Continued

M10_02 Solves a word problem involving simple proportional reasoning.
M10_03 Solves a word problem involving multiplication of a three-digit number by a one-digit number.
M11_09 Identifies the appropriate operation to solve a word problem involving division.
M12_02 Solves a multi-step word problem involving halving, doubling, and adding.
M13_01A Uses knowledge of place value to arrange three given digits to create a sum closest to a given two-digit number.

M13_01B Uses knowledge of place value to arrange three given digits to create a sum closest to a given two-digit number.
M13_01C Uses knowledge of place value to arrange three given digits to create a given sum in two different ways.
M13_02A Uses knowledge of place value to arrange three given digits to create the largest sum of a two-digit and onedigit number.
M13_02B Uses knowledge of place value to arrange three given digits to create the largest difference between a twodigit and a one-digit number.
M14_08 Solves a word problem involving measures and proportional reasoning.

## Patterns and Relationships

M01_12 Selects the expression that represents a situation involving multiplication.
M06_06 Identifies a number that satisfies a number sentence involving division.
M07_04A Extends entries in two tables according to numerical rules described in a situation.
M08_04 Identifies the next term in a sequence of whole numbers formed by doubling.
M08_05 Identifies a number sentence that represents a situation involving division.
M09_07 Identifies the result of a specified sequence of operations on a given number.
M10_05 Identifies the missing number in a square whose rows and columns have the same sum.
M12_06C Generalizes from the first several terms of a numeric sequence to find the tenth term.

## Measurement

M01_02 Calculates the volume of a rectangular solid given the volume of one layer and the number of layers.
M02_02 Finds the increase in temperature from a negative to a positive temperature on a thermometer.
M02_09 Selects appropriate metric unit to measure weight (mass).
M05_05 Solves a multi-step word problem involving time and temperature.
M05_06 Solves a multi-step word problem involving duration of time.
M06_07 Determines the number of non-standard units of area needed to cover a figure.
M06_08B On a map drawn to scale, positions a building within a range of distance from a specified point.

## Items at High International Benchmark (550) - Continued

## Measurement - Continued

M08_07 Identifies the value of an unlabelled mark on a circular scale.
M10_07 Selects the attribute that can be measured with a given metric unit.
M11_07 Identifies the value of an unlabelled mark on a circular scale.
M12_08
Solves a word problem involving conversion between hours and minutes.

## Geometry

M03_02 Recognizes flat and curved surfaces on solids.
M06_09 Given a figure and the line of symmetry on a grid, draws the reflection.
M07_08 Uses properties of a rectangles and triangles to solve a problem.
M08_11 Recognizes the net of a triangular prism.
M09_05A Makes and draws one large triangle from two triangle tiles (square tiles divided diagonally into one white and one black triangle).

M09_05B Makes and draws one square from four triangle tiles (square tiles divided diagonally into one white and one black triangle).

M10_08C Draws two lines to divide a rectangle into one rectangle and two triangles.
M10_09 Identifies two triangles that have the same shape but different sizes in a complex figure.
M11_10 Orders four angles by size.
M12_11 Identifies the figure in which a line of symmetry is shown.

## Data

M04_11 Uses data from a tally chart to solve a problem.
M07_04B Reads and interprets data from two tables to answer a question.
M07_04C Draws conclusions from data in two tables.
M10_10 Identifies the label for a column in a bar graph that corresponds to data in a tally chart.
M12_12 Interprets data from a bar graph to solve a problem.

## Items at Advanced International Benchmark (625)

## Number

M01_08
Identifies the decimal representation for a fraction with a denominator of 10.
M05_03 Selects the appropriate information to solve a multi-step word problem involving whole numbers.
M06_01 Solves a multi-step word problem involving divisibility.
M06_02 Solves a problem involving proportional reasons.
M09_05C Determines the fraction of a figure that is shaded.
M09_06A Uses appropriate tiles to represent one-half.

## Items at Advanced International Benchmark (625) - Continued

## Number - Continued

M11_02 Identifies all the numbers in a given interval ending in a given string of digits.
M11_03 Halves the amounts in a recipe involving whole numbers and fractions.
M12_01 Given a fraction, identifies a larger fraction with a different denominator.
M14_01B Selects appropriate information and uses it to solve a proportion problem.
M14_01C Selects appropriate information and uses it to solve a multi-step problem involving proportions.
M14_02 Selects appropriate information and uses it to solve a proportion problem.

## Patterns and Relationships

M06_04 Writes a rule for a multiplicative relationship between first and second numbers in a set of ordered pairs of numbers.
M06_05 Identifies the two-step rule used to describe the relationship between adjacent terms in a sequence of numbers.
M11_06 Identifies the two-step rule for a linear relationship between first and second numbers in a set of ordered pairs of numbers.
M12_05 Identifies the number that satisfies a number sentence involving addition of two terms on each side.

## Measurement

M01_09 Estimates the distance on a map given scale (in $\mathrm{cm}=\mathrm{km}$ ).
M03_09 Identifies the numerical expression that gives the distance around a rectangle, given its length and width.

M04_07 Completes an irregular figure on a grid so that it has a given area.
M05_07 Solves a word problem involving conversion of metric units of capacity.
M06_03 Solves a multi-step measurement problem involving multiplication and subtraction.
M06_08A On a map drawn to scale, positions a park at a given distance from a specified point.
M06_08C On a map drawn to scale, positions a building half-way between two specified points.
M07_06 Recognizes that the area does not change when a figure is cut into parts and rearranged.
M08_08 Solves a multi-step problem involving conversion between hours and minutes.
M11_08 Determines the area of a figure made up of squares and half squares on a grid.
M12_07 Estimates the length of a curved line next to the middle of ruler.
M13_04 Identifies the operation that solves a word problem involving distance, time, and speed.
M13_05 Solves a multi-step problem involving conversion between hours and minutes.

## Geometry

M12_09 Draws an angle greater than $90^{\circ}$.
M14_07 Identifies the position of a shape after a half-turn rotation.

Exhibit E.2: Descriptions of Mathematics Items at Each International Benchmark (...Continued)


## Items at Advanced International Benchmark (625) - Continued

## Data

M05_10 Organizes data and completes a tally chart to represent it.
M13_06 Reads, relates, and interprets values from two sets of data from graph to solve a problem.

## Items Above Advanced International Benchmark (625)

## Number

M08_02 Subtracts a one-place decimal from a two-place decimal presented horizontally.
M09_06B Selects the appropriate tiles from a restricted set and uses them to represent a given fraction.
M13_02C Uses knowledge of place value to arrange three given digits to create the largest product of a two-digit and one-digit number.
M14_03 Selects appropriate information and uses it to solve a multi-step problem involving two proportions.

## Patterns and Relationships

M05_04 Writes two-step rule for a linear relationship between pairs of numbers.
M07_03 Identifies the number that satisfies a number sentence involving division of two terms on each side.
M07_05 Solves a multi-step problem to find one of the two unknown values.
M09_04 Uses understanding of equality to evaluate an expression.

## Measurement

M10_06 Identifies a time in minutes in an interval given in hours and half hours.

## Geometry

M03_08
Recognizes the equivalent of a three-dimensional figure when it is rotated to a different orientation.


## Appendix F

## Syrian Arab Republic and Yemen Mathematics Achievement

Exhibit F.1: Syrian Arab Republic - Selected Mathematics Achievement Results


| Distribution of Mathematics Achievement |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mean <br> Achievement | Years of <br> Schooling | Average <br> Age | 5th <br> Percentile <br> (Scale Score) | 25th <br> Percentile <br> (Scale Score) | 50th <br> Percentile <br> (Scale Score) | 75th <br> Percentile <br> (Scale Score) | 95th <br> Percentile <br> (Scale Score) |  |
| $358(3.7)$ | 8 | 14 | $232(3.7)$ | $303(3.1)$ | $356(4.2)$ | $410(3.9)$ | $491(7.4)$ |  |


| Gender Difference in Mathematics Achievement |  |  |
| :---: | :---: | :---: |
| Mathematics <br> Achievement | Girls' Mean | Boys' Mean |
| $358(3.7)$ | $352(3.6)$ | $355(6.1)$ |

- Significantly higher
than other gender

| Average Achievement in Mathematics Content Areas by Gender |  |  |  |
| :--- | :---: | :---: | :---: |
| Content Area | Girls' Mean | Boys' Mean | Overall Mean |
| Number | $363(4.2)$ | $365(5.3)$ | $368(4.0)$ |
| Algebra | $373(2.8) \boldsymbol{0}$ | $361(4.9)$ | $371(3.1)$ |
| Measurement | $369(3.6)$ | $383(4.9) \boldsymbol{0}$ | $381(3.3)$ |
| Geometry | $397(4.2)$ | $397(6.1)$ | $400(3.3)$ |
| Data | $362(4.0)$ | $370(4.5)$ | $369(3.2)$ |

- Significantly highe than other gender

| Percentages of Students Reaching International Benchmarks in Mathematics |  |  |  |
| :---: | :---: | :---: | :---: |
| Advanced <br> International <br> Benchmark <br> $(625)$ | High <br> International <br> Benchmark <br> $(550)$ | Intermediate <br> International <br> Benchmark <br> $(475)$ | Low <br> International <br> Benchmark <br> $(400)$ |
| $0(0.0)$ | $1(0.3)$ | $7(0.9)$ | $29(1.6)$ |

[^102]Exhibit F.2: Yemen - Selected Mathematics Achievement Results


| Distribution of Mathematics Achievement |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mean <br> Achievement | Years of <br> Schooling | Average <br> Age | 5th <br> Percentile <br> (Scale Score) | 25th <br> Percentile <br> (Scale Score) | 50th <br> Percentile <br> (Scale Score) | 75th <br> Percentile <br> (Scale Score) | 95th <br> Percentile <br> (Scale Score) |
| $278(7.4)$ | 4 | 11 | $99(5.9)$ | $196(7.0)$ | $273(6.9)$ | $355(10.2)$ | $473(12.4)$ |


( Significantly higher than other gender

| Average Achievement in Mathematics Content Areas by Gender |  |  |  |
| :--- | :--- | :--- | :--- |
| Content Area | Girls' Mean | Boys' Mean | Overall Mean |
| Number | $294(8.3)$ | $303(8.2)$ | $299(6.8)$ |
| Patterns and Relationships | $283(8.1)$ | $304(8.5)$ | $296(6.0)$ |
| Measurement | $249(10.4)$ | $263(8.7)$ | $256(7.5)$ |
| Geometry | $284(8.8)$ | $269(8.5)$ | $274(6.9)$ |
| Data | $284(6.7)$ | $289(7.4)$ | $286(6.0)$ |

( ) Significantly higher

| Percentages of Students Reaching International Benchmarks in Mathematics |  |  |  |
| :---: | :---: | :---: | :---: |
| Advanced <br> International <br> Benchmark <br> $(625)$ | High <br> International <br> Benchmark <br> $(550)$ | Intermediate <br> International <br> Benchmark <br> $(475)$ | Low <br> International <br> Benchmark <br> $(400)$ |
| $0(0.1)$ | $1(0.4)$ | $5(1.1)$ | $15(1.9)$ |

[^103]

## Appendix G

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## National Research Coordinators

The TIMSS 2003 National Research Coordinators and their staff had the enormous task of implementing the TIMSS 2003 design. This involved obtaining funding for the project; participating in the development of the instruments and procedures; conducting field tests; participating in and conducting training sessions; translating the instruments and procedural manuals into the local language; selecting the sample of schools and students; working with the schools to arrange for the testing; arranging for data collection, coding, and data entry; preparing the data files for submission to the IEA Data Processing Center; contributing to the development of the international reports; and preparing national reports. The way in which the national centers operated and the resources that were available varied considerably across the TIMSS 2003 countries. In some countries, the tasks were conducted centrally, while in others, various components were subcontracted to other organizations. In some countries, resources were more than adequate, while in some cases, the national centers were operating with limited resources. All of the TIMSS 2003 National Research Coordinators and their staff members are to be commended for their professionalism and their dedication in conducting all aspects of TIMSS.

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[^0]:    Background data provided by National Research Coordinators.
    1 Age of entry to primary school based on the beginning of ISCED Level 1 in UNESCO's International Standard Classification of Education (Operational Manual for ISCED-97).

[^1]:    Background data provided by National Research Coordinators.
    1 Age of entry to primary school based on the beginning of ISCED Level 1 in UNESCO's International Standard Classification of Education (Operational Manual for ISCED-97).

[^2]:    1 Age of entry to primary school based on the beginning of ISCED Level 1 in UNESCO's International Standard Classification of Education (Operational Manual for ISCED-97).

[^3]:    Background data provided by National Research Coordinators.
    1 Age of entry to primary school based on the beginning of ISCED Level 1 in UNESCO's International Standard Classification of Education (Operational Manual for ISCED-97).

[^4]:    1 TIMSS used item response theory (IRT) methods to summarize the achievement results on a scale with a mean of 500 and a standard deviation of 100 . Given the matrix-sampling approach, scaling averages students' responses in a way that accounts for differences in the difficulty of different subsets of items. It allows students' performances to be summarized on a common metric even though individual students responded to different items in the mathematics test. For more detailed information, see the "IRT Scaling and Data Analysis" section of Appendix A.
    2 Argentina was unable to complete the necessary steps on schedule for their data to appear in this report. Because the characteristics of their samples are not completely known, achievement results for Syria at the eighth grade and Yemen at the fourth grade are presented in Appendix F.

[^5]:    3 Even though England worked very hard to meet the TIMSS sampling requirements and adjustments were made to make the results representative, it did not meet the school participation rates as specified in the guidelines and consequently its results are shown below a line.

    4 Since the TIMSS scales were developed using IRT technology, like all such scales, the eighth- and fourth-grade scales cannot be described in absolute terms.
    5 Tables of the percentile values and standard deviations for all countries are presented in Appendix D.

[^6]:    * Represents years of schooling counting from the first year of ISCED Level 1.

    Norway: 4 years of formal schooling, but First Grade is called "First grade/Preschool."
    ** Taken from United Nations Development Programme's Human Development Report, p. 237-240
    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash ( - ) indicates comparable data are not available.
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).

[^7]:    Note: 5\% of these comparisons would be statistically significant by chance alone.

[^8]:    Note: $5 \%$ of these comparisons would be statistically significant by chance alone.

[^9]:    rend notes: Because of differences in population coverage, 1999 data are not shown for Australia and lovenia, and 1995 data are not shown for Israel, Italy, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995. Data for Latvia in this exhibit include Latvian-speaking schools only.

[^10]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.
    A diamond $(\diamond)$ indicates the country did not participate in the assessment.

[^11]:    1 For example, for the advanced benchmark, an item was included if at least 65 percent of students scoring at the scale point corresponding to this benchmark answered the item correctly and less than 50 percent of students scoring at the high benchmark answered it correctly. Similarly, for the high benchmark, an item was included if at least 65 percent of students scoring at that point answered the item correctly and less than 50 percent of students at the intermediate benchmark answered it correctly.
    2 The participants in the scale anchoring process are listed in Appendix G.

[^12]:    Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
    $\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6)
    2 National Defined Population covers less than $90 \%$ of National Desired Population (see Exhibit A.6).

    - Korea tested the same cohort of students as other countries, but later in 2003, at the beginning of the next school year
    ま Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

[^13]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^14]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.
    A diamond $(\diamond)$ indicates the country did not participate in the assessment.

[^15]:    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9)
    Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia and Slovenia, and 1995 data are not shown for Israel, Italy, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in

[^16]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.
    A diamond $(\diamond)$ indicates the country did not participate in the assessment.

[^17]:    rend notes: Because of differences between 1995 and 2003 in population coverage, 1995 data are not shown for Italy. Data for Latvia in this exhibit include Latvian-speaking schools only. To be comparable with 995, 2003 data for New Zealand in this exhibit include students in English medium instruction only (98\% of the estimated population).

[^18]:    * The item was answered correctly by a majority of students reaching this benchmark.
    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

[^19]:    Country average significantly higher than international average

[^20]:    1 Mullis, I.V.S., Martin, M.O., Smith, T.A., Garden, R.A., Gregory, K.D., Gonzalez, E.J., Chrostowski, S..J, and O’Connor, K.M. (2003), TIMSS Assessment Frameworks and Specifications 2003 (2nd Edition), Chestnut Hill, MA: Boston College. Please see Appendix A for more information about the framework and test development process.

[^21]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9)
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).

[^22]:    Nearly satisfied guidelines for sample participation rates only after replacement schools were Did not satisfy guidelines for sample participation rates (see Exhibit A.9). included (see Exhibit A.9).

[^23]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

[^24]:    Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
    $\ddagger \quad$ Nearly satisfied guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    1 National Desired Population does not cover all of International Desired Population (see Exhibit A.6).

[^25]:    $\dagger$ Met guidelines for sample participation rates only after replacement schools were included (see Exhibit A.9).

[^26]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^27]:    Background data provided by students.

    * Based on countries' categorizations to UNESCO's International Standard Classification of Education (Operational Manual for ISCED-1997).
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^28]:    Background data provided by students.

[^29]:    Background data provided by students.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^30]:    Background data provided by students.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^31]:    Background data provided by students.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^32]:    Background data provided by students

    * Number of hours based on: No time $=0$; Less than 1 hour $=0.5 ; 1-2$ hours $=1.5$; More than 2 but less than 4 hours $=3 ; 4$ or more hours $=4.5$. Activities are not necessarily exclusive; students may have reported engaging in more than one activity at the same time.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

[^33]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.

[^34]:    Background data provided by students.

[^35]:    Background data provided by students.

[^36]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.
    An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students.
    A diamond (') indicates the country did not participate in the assessment.

[^37]:    Background data provided by National Research Coordinators.
    1 Belgium (Flemish): Although there is no national curriculum there are officially defined final attain-
    ment levels (comparable to educational standards); based on the final attainment levels, school
    boards develop their own curricula.

[^38]:    Background data provided by National Research Coordinators.

[^39]:    Mullis, I.V.S., Martin, M.O., Smith, T.A., Garden, R.A., Gregory, K.D., Gonzalez, E.J., Chrostowski, S.J., and O'Connor, K.M. (2003), TIMSS Assessment Frameworks and Specifications 2003 (2nd ed.), Chestnut Hill, MA: Boston College
    4 For a full description of the TIMSS 2003 test development effort, please see Neidorf, T.S. and Garden, R. (2004), "Developing the TIMSS 2003 Mathematics and Science Assessment and Scoring Guides" in M.O. Martin, I.V.S. Mullis, and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.

[^40]:    * Percentages may not add to 100 due to rounding.

[^41]:    Background data provided by National Research Coordinators.

[^42]:    Background data provided by National Research Coordinators

[^43]:    Background data provided by teachers at the time of testing.
    $\ddagger$ Did not satisfy guidelines for sample participation rates.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^44]:    Background data on intended curriculum provided by National Research Coordinators，and on imple－ mented curriculum by teachers at the time of testing．
    \＃Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
    （）Standard errors appear in parentheses．Because results are rounded to the nearest whole number， some totals may appear inconsistent．

[^45]:    Background data on intended curriculum provided by National Research Coordinators，and on imple－ mented curriculum by teachers at the time of testing．
    $\ddagger$ Did not satisfy guidelines for sample participation rates（see Exhibit A．9）．
    （）Standard errors appear in parentheses．Because results are rounded to the nearest whole number，

[^46]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.

[^47]:    All or almost all students

    - Only the more able students

    Not included in the curriculum through fourth grade

[^48]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available

[^49]:    All or almost all students $\bigcirc$ Only the more able students $\bigcirc$ Not included in the curriculum through fourth grade

[^50]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash ( - ) indicates comparable data are not available.

[^51]:    All or almost all students $\quad$ Only the more able students $\quad$ Not included in the curriculum through fourth grade

[^52]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.

[^53]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

    A dash ( - ) indicates comparable data are not available.

[^54]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available

[^55]:    Background data on intended curriculum provided by National Research Coordinators, and on implemented curriculum by teachers at the time of testing.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.

[^56]:    Background data provided by National Research Coordinators.

[^57]:    Background data provided by teachers
    *Does not include provisional or emergency certificate
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^58]:    A dash $(-)$ indicates comparable data are not available.
    An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An "x" indicates data are available for less than $50 \%$ of the students.

[^59]:    Background data provided by National Research Coordinators and by teachers
    1 Teachers who responded that they majored in more than one area are reflected in all categories that apply.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^60]:    Background data provided by teachers.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^61]:    Background data provided by teachers.
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^62]:    A dash (-) indicates comparable data are not available.
    An " $r$ " indicates data are available for at least 70 but less than $85 \%$ of the students. An " $s$ " indicates data are available for at least 50 but less than $70 \%$ of the students. An " $x$ " indicates data are available for less than $50 \%$ of the students.

[^63]:    Background data provided by teachers.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available

[^64]:    Background data provided by teachers.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available.

[^65]:    Background data provided by teachers.
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^66]:    Mathematics instructional time provided by teachers, and total instructional time provided by schools
    1 Computed as the ratio of mathematics instructional time to the total instructional time averaged across students ( 1 hour $=60$ minutes).
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).

[^67]:    Background data provided by students.

[^68]:    Background data provided by teachers.

[^69]:    Background data provided by teachers.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates comparable data are not available

[^70]:    Background data provided by students.

[^71]:    Background data provided by teachers.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^72]:    Background data provided by teachers
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^73]:    Background data provided by National Research Coordinators and by teachers.
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^74]:    A dash (-) indicates comparable data are not available.

[^75]:    Background data provided by schools.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^76]:    A dash ( - ) indicates comparable data are not available. A tilde ( $\sim$ ) indicates insufficient data to report achievement.
    An " r " indicates data are available for at least 70 but less than $85 \%$ of the students.

[^77]:    Background data provided by schools.
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9),
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^78]:    Background data provided by schools.
    $\ddagger$ Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    Trend notes: Because of differences in population coverage, 1999 data are not shown for Australia, Latvia, Morocco, and Slovenia, and 1995 data are not shown for Israel, Italy, Latvia, and South Africa. Korea tested later in 2003 than in 1999 and 1995, at the beginning of the next school year. Similarly, Lithuania tested later in 1999 than in 2003 and 1995.

[^79]:    A dash ( - ) indicates comparable data are not available.
    An " r " indicates data are available for at least 70 but less than $85 \%$ of the students.
    A diamond (') indicates the country did not participate in the assessment.

[^80]:    Background data provided by teachers.
    \# Did not satisfy guidelines for sample participation rates (see Exhibit A.9).
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^81]:    Background data provided by students.

[^82]:    Background data provided by students.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^83]:    1 Argentina adminis

[^84]:    2 Because the characteristics of their samples are not completely known, achievement data for Syrian Arab Republic and Yemen are presented in Appendix F of this report.

[^85]:    Constructed-response items include both short-answer and extended-response types.

[^86]:    2 In scoring the tests, correct answers to most items were worth one point. However, responses to some constructed-response items were evaluated for partial credit with a fully correct answer awarded two points. Thus, the number of score points exceeds the number of items in the test.

[^87]:    4 For more information, see Chrostowski, S.J. (2004), "Developing the TIMSS 2003 Background Questionnaires" in M.O. Martin, I.V.S. Mullis, and S.J. Chrostowski (eds.), TIMSS 2003 Technical Report, Chestnut Hill, MA: Boston College.

[^88]:    1 The reliability coefficient for each country is the median Cronbach's alpha reliability across the 12 test booklets.

[^89]:    Note: 5\% of these comparisons would be statistically significant by chance alone

[^90]:    Note: $5 \%$ of these comparisons would be statistically significant by chance alone.

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[^93]:    Note: 5\% of these comparisons would be statistically significant by chance alone.

[^94]:    Note: $5 \%$ of these comparisons would be statistically significant by chance alone.

[^95]:    1 See Appendix A for more information on test development.

[^96]:    * Of the 194 items in the Mathematics test, some extended-response items were scored on a two-point () Standard errors appear in parentheses scale, resulting in 215 total score points. Following item review, response categories were combined for a number of items, resulting in 213 score points.

[^97]:    () Standard errors appear in parentheses.

[^98]:    ( ) Standard errors appear in parentheses

[^99]:    () Standard errors appear in parentheses

[^100]:    () Standard errors appear in parentheses

[^101]:    Denotes with calculator available.

[^102]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^103]:    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

